

Name: Prudhvi Reddy Araga

Login ID: praraga

1.  $F(n) = \Omega(g(n))$  implies g(n) = 0(f(n))

Answer: True

By definition

$$f(n) = \Omega(g(n))$$
 which implies  $0 \le c.g(n) \le f(n)$   
 $g(n) = 0(f(n))$  which implies  $0 \le g(n) \le c.f(n)$ 

Let us assume that  $f(n) = 100n^2$ ,  $g(n) = n^2$ 

$$f(n) >= c.g(n)$$
  
 $100.n^2 >= c.n^2$ 

Consider the constant c = 50

$$100n^2 >= 50n^2$$
  
2 >= 1

g(n) = 0(f(n)) which is equal to

$$\begin{array}{l} c.f(n)>=g(n)\\ c.100.n^2>=n^2\\ 50.100.n^2>=n^2\\ 5000>=1 \end{array}$$

Based on the above equations  $F(n) = \Omega(g(n))$  implies g(n) = 0 (f(n)) is true.