

Name: Prudhvi Reddy Araga Login ID - praraga

## Answer -1:

```
PruneAndSearch (A, low, high)
   if (low < high)
        mid = (low + high) / 2;
        m_1 = (low + mid) / 2;
        m_2 = (mid+1+high) / 2;
        if(comparator(A[m_1], A[m_2])
            PruneAndSearch(A, low, m_1-1);
            PruneAndSearch(A, m<sub>1</sub>+1, high);
            PruneAndSearch(A, mid+1, m2-1);
            PruneAndSearch(A, m<sub>2</sub>+1, high);
         }
        else if (m_1 \le n \text{ and comparator}(A[m_1], A[m_1+1]) or (o \le m_1 \text{ and comparator}(A[m_1],
A[m_1-1]))
                return A[m_1];
        }
       else
        {
                return A[m<sub>1</sub>];
       }
T(n) = T(n/2) + T(n/2) + k
```

As we are dividing the problem into half and solving each half time complexity reduces to two times of T(n/2) and a constant time to do the comparison.

$$T(n) = 2.T(n/2) + k$$

As per the master's theorem  $\rightarrow$  a = 2, b = 2, f(n) = k. n<sup>0</sup>

$$c = 0$$

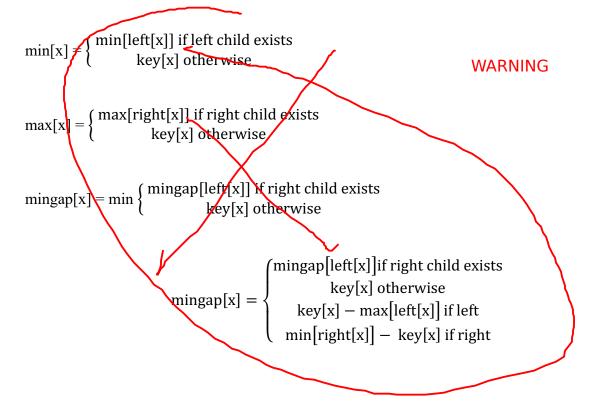
$$f(n) = O(n^{\log_2 2 - \epsilon}), \epsilon = 1$$
  
=  $O(n^{1-1})$   
=  $O(n^0)$  (True)

So, 
$$T(n) = \theta(n)$$

## Answer - 2:

To Compute mingap, Redblack tree can be used by adding additional fields min,max and mingap to each node.

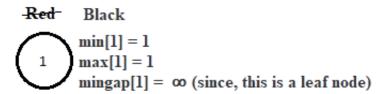
Values are computed using below. Mingap of leaf node is  $\infty$ 



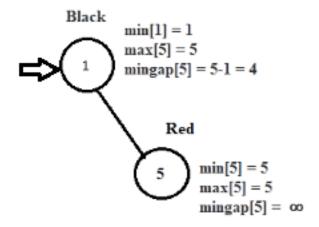
After each operation and Red Black Tree update min, max and mingap values from newly inserted/deleted to the root as long as there is change in the values.

$$Q = \{1,5,9,15,18,22\}$$

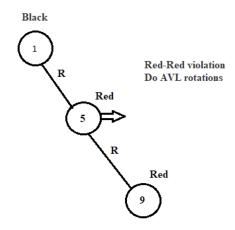
Insert 1 in Red black tree

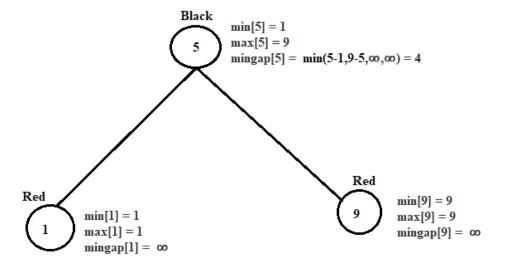


Insert 5 in Reb black tree

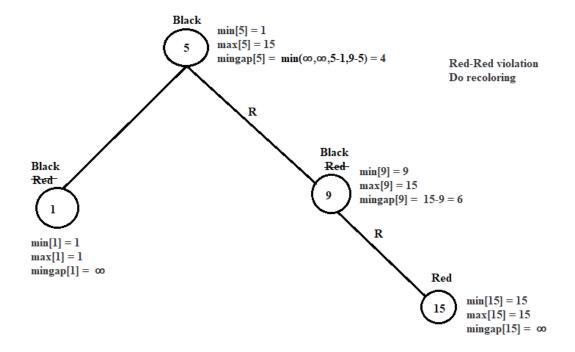


Insert 9 in Red black tree

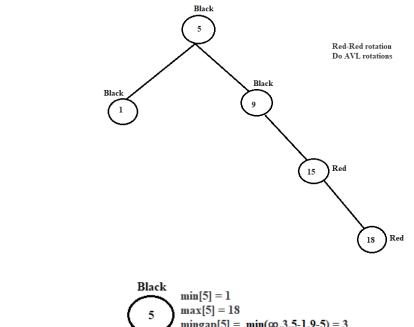


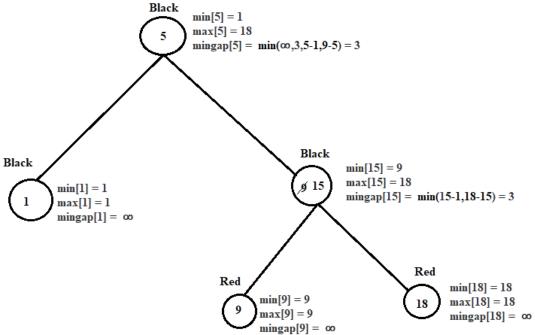


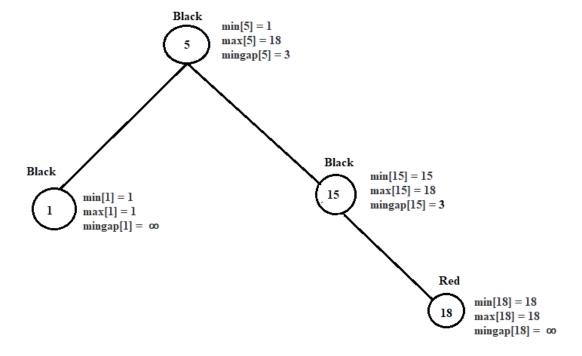
Insert 15 in Red black tree



Insert 18 in Red black tree

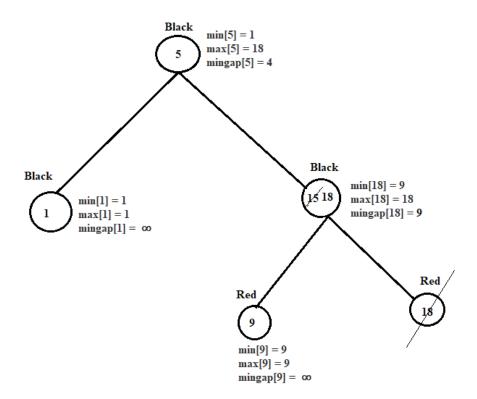


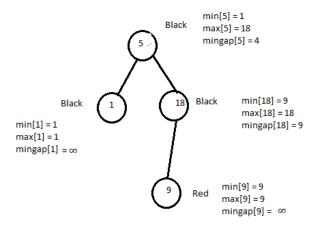


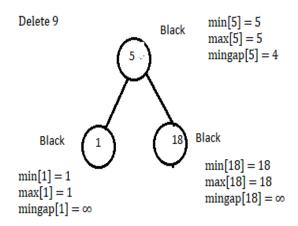


Red node is deleted. So, no recoloring/balancing is needed.

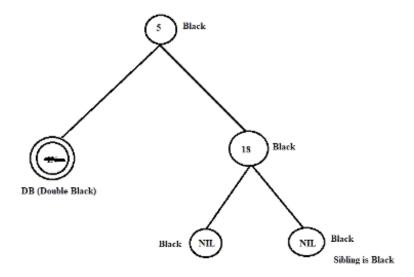
Delete 15



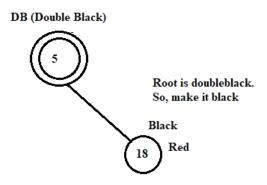


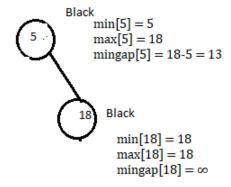


There are no children left for 9. So, simly delete it and update min, max and mingap values.

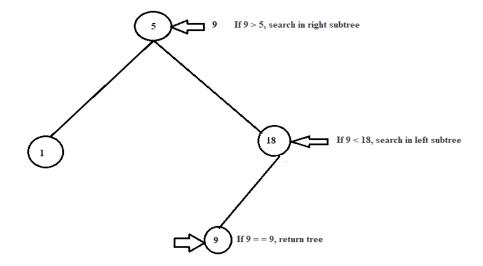


Sibling is black and both the children are black. So, make the parent as black and sibling as red. As parent is already black, it becomes double black.

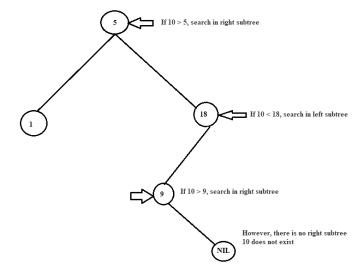




## Search 9



## Search 10



Time to insert, delete and search depends on the height of the tree and constant number of rotations of insert and delete and time to compute min, max value which also depends on height of tree.

As red black tree is balanced, tree is O(h) @ O(logn).

Mingap value is stored at root.

So, time complexity is O(1).