



# The Bitcoin Cryptocurrency: Part 5

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# References

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<https://www.ee.iitb.ac.in/~sarva/bitcoin.html>
- A. Narayanan, J. Bonneau, E. Felten, A. Miller, S. Goldfeder, “*Bitcoin and Cryptocurrency Technologies: A Comprehensive Introduction*”, Princeton University Press, 2016

# Determination of Transaction Fee

- Recall: max. size of a block is 4 MB
- Miners seek to maximize the total transaction fees earned from a block
- Miners prefer to include in candidate blocks transactions with:
  - ☐ high transaction fees and
  - ☐ small sizes
- In particular, let the “transaction fee per byte” or “fee rate” of a transaction be defined to be:
  - ☐  $\text{transaction fee} / \text{size of transaction}$
- Miners prefer transactions with high fee rates
- So nodes that want to add their regular transaction to the blockchain need to pay a fee rate that is competitive with other transactions being broadcast on the network
- How can a node that wants to add its regular transaction to the blockchain find out what fee rate is competitive?

# Determination of Transaction Fee (contd.)

- When a transaction  $t$  with fee rate  $r$  is first heard by a node, the height  $h_1$  of the latest block in blockchain is recorded
- If  $t$  gets included in a block of height  $h_2$ :
  - $h_2 - h_1$  gives an estimate of the expected delay incurred by a transaction which pays fee rate  $r$
- Using such estimates from several transactions, a competitive fee rate can be estimated as a function of:
  - the amount of delay in blocks that the node creating the transaction is willing to tolerate

# Unspent Transaction Output (UTXO)

- Recall: when an output of a previous transaction is unlocked by an input of a later transaction:
  - all the bitcoins in the output are spent by the input
- Hence, a transaction output can be in one of only two states: “spent” and “unspent”
- UTXOs refer to outputs in transactions recorded on the blockchain which have not been unlocked by inputs of later transactions
- The total amount of bitcoins owned by an address is:
  - sum of the amounts in all the UTXOs it can unlock
- When a blockchain fork occurs, the sets of UTXOs seen by different nodes in the Bitcoin network differ
  - once the fork is resolved, the UTXO set seen by all the nodes in the Bitcoin network will be identical

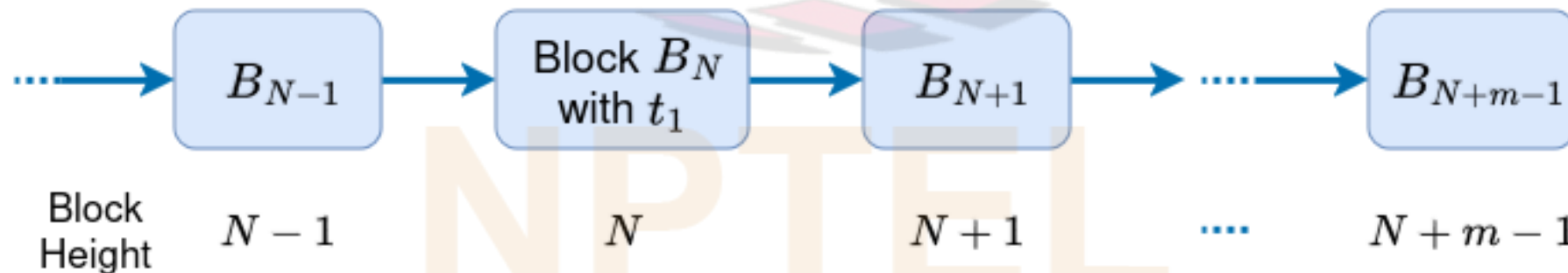


# Confirmations

- Suppose Alice wants to use bitcoins to pay for some goods that Bob is selling
- Alice creates a new regular transaction, say  $t_1$ , such that:
  - ❑ one or more of its inputs unlock UTXOs that Alice owns
  - ❑ one of its outputs contains the amount of bitcoins Alice wants to pay Bob and a challenge script such that:
    - to create a valid response to it, a private key owned by Bob is required
- Alice broadcasts the transaction  $t_1$  on the Bitcoin network
- Miners include it in the candidate blocks they are mining
- When should Bob hand over the goods to Alice?
  - ❑ Bob keeps scanning the new blocks being added to the blockchain for  $t_1$
  - ❑ once Bob sees a new block with  $t_1$  included in it, he will wait for the branch containing this block to grow further before handing over the goods to Alice

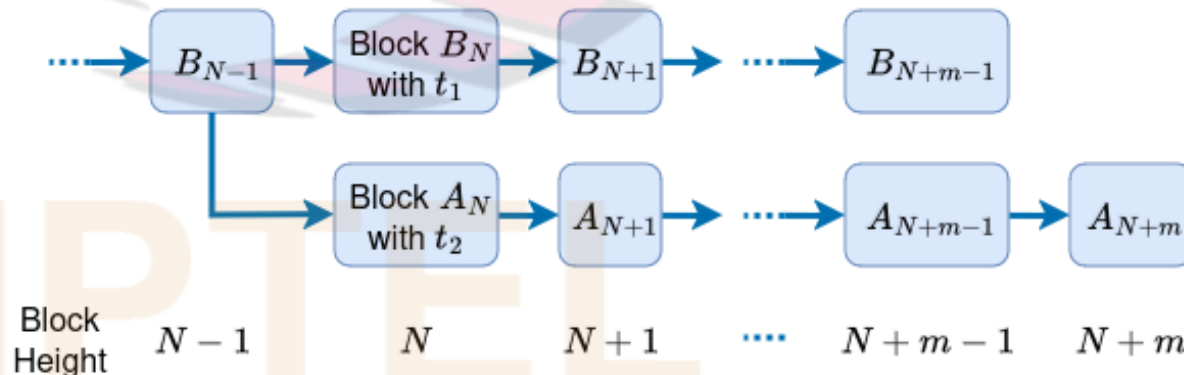
# Confirmations (contd.)

- In particular:
  - ❑ if the transaction  $t_1$  is included in a block  $B_N$  at height  $N$ , then  $t_1$  is said to have received one confirmation
  - ❑ when a valid block  $B_{N+1}$  at height  $N + 1$  is added to the blockchain with  $B_N$  as its previous block, the transaction  $t_1$  is said to have received two confirmations
  - ❑ more generally, when  $m - 1$  valid blocks have been appended to the block  $B_N$ , the transaction  $t_1$  is said to have received  $m$  confirmations
- Bob waits until  $t_1$  has received  $m$  confirmations before handing over the goods to Alice
  - ❑  $m$  is chosen depending on the value of the goods
- Why does Bob wait for  $m$  confirmations, instead of handing over the goods to Alice after one confirmation has been received?
  - ❑ to safeguard against a “*double spending attack*” by Alice in which the transaction  $t_1$  can be cancelled



# Double Spending Attack

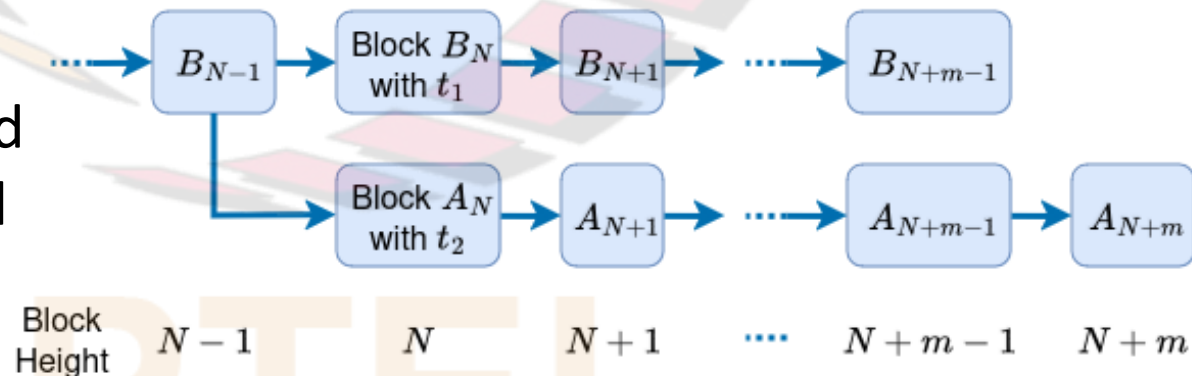
- Suppose:
  - ❑ Bob asks Alice for  $x$  bitcoins as payment for the goods
  - ❑ Alice can unlock a UTXO  $O_A$  which has at least  $x$  bitcoins
- A double spending attack proceeds as follows:
  - 1) Alice creates two transactions  $t_1$  and  $t_2$ :
    - ❑ in  $t_1$ , an input unlocks  $O_A$  and an output pays Bob  $x$  bitcoins
    - ❑ in  $t_2$ , an input unlocks  $O_A$ , but  $x$  bitcoins are paid back to Alice in an output
    - ❑ Note that the transactions  $t_1$  and  $t_2$  conflict with each other because they both spend the same UTXO  $O_A$ ; only one of them can be included in blockchain
  - 2) Alice broadcasts  $t_1$  on the Bitcoin network for inclusion in the blockchain
    - ❑ she keeps  $t_2$  a secret
  - 3) Suppose a miner includes  $t_1$  in a valid block  $B_N$  at height  $N$ 
    - ❑ Bob waits until  $t_1$  has received  $m$  confirmations before handing over the goods to Alice
  - 4) Immediately after broadcasting  $t_1$ , Alice begins work on constructing a branch containing  $t_2$ 
    - ❑ she does not announce the valid blocks found on this branch to the Bitcoin network before Bob transfers the goods to her





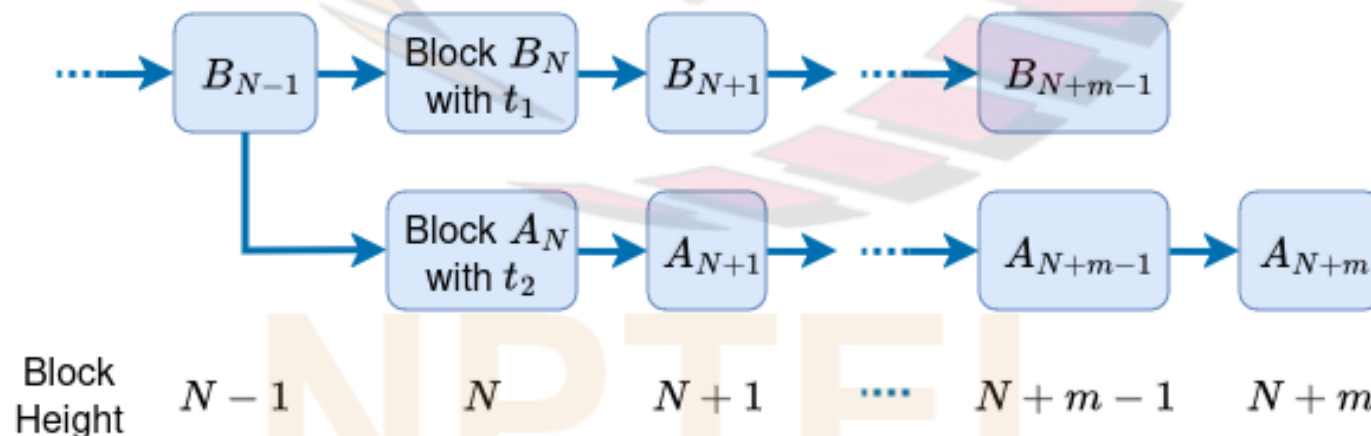
# Double Spending Attack (contd.)

- 5) After receiving the goods, if Alice succeeds in creating a branch containing  $t_2$  which is longer than the branch containing  $t_1$ , then:
  - ❑ she broadcasts all the blocks in the  $t_2$  branch in the Bitcoin network
- 6) All the nodes in the Bitcoin network will eventually switch to the  $t_2$  branch and the  $t_1$  branch will be abandoned
- Note: usually, transactions present in blocks in abandoned branches are added back to the transaction pool (mempool) if they have not already appeared in the surviving branch
  - ❑ Miners use this transaction pool for constructing new candidate blocks
  - ❑ However, miners which have switched to the  $t_2$  branch will not add  $t_1$  to their mempools since:
    - it conflicts with  $t_2$



# Double Spending Attack (contd.)

- In summary:
  - ❑ Bob has already transferred the goods to Alice
  - ❑ but the  $x$  bitcoins he thought he received from Alice in  $t_1$  are back in Alice's possession
  - ❑ since Alice can now spend these bitcoins again, this attack is called a “double spending attack”



# Number of Confirmations $m$

- Recall: in above example:
  - Bob waits until  $t_1$  has received  $m$  confirmations before handing over the goods to Alice
- How many confirmations  $m$  should Bob wait for?
- Assuming that Alice controls less than 50% of the network hash rate:
  - the success probability of a double spending attack decreases as  $m$  increases
- But  $m$  cannot be very large as each confirmation takes approximately 10 minutes to appear
  - so a customer, irrespective of whether he/ she is honest or malicious, will experience a delay of about  $10m$  minutes before the seller transfers the goods to him/ her
- Several merchants in the Bitcoin network wait for six confirmations ( $m = 6$ ), which corresponds to a delay of about an hour before goods are transferred from merchant to customer
  - smaller or larger values of  $m$  may be used by merchants depending on the value of the goods being sold

