

✓

Prove??

Price of a house

\propto # of rooms ✓

\propto Area of house ✓

\propto location ✓

transaction amt	transaction count
1000	1
2000	2
10000	3

Hardik Pandya

→ Price of house \propto Area of house, No of rooms, locality
relationship

<u>No. of matches played</u>	<u>Total score</u>
0	0
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
10	10
11	11
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90	90
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92	92
93	93
94	94
95	95
96	96
97	97
98	98
99	99
100	100

- * Measure the relationship

- ① Covariance
✓ ② Correlation.

Covariance \rightarrow

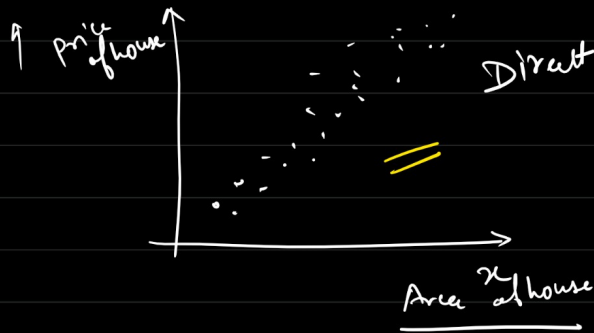
Variance:

↓

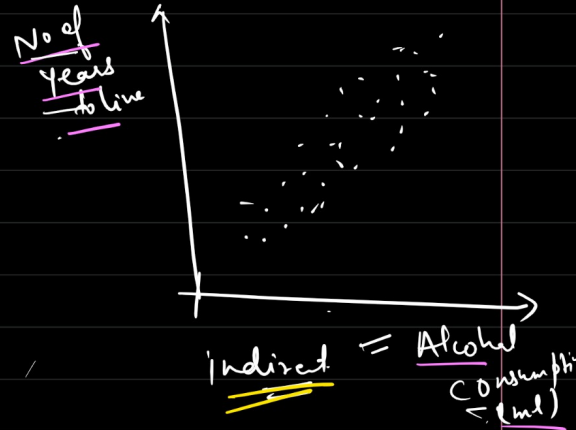
Spread of data.

Co - variance

Scen-1



Scen-2



① Covariance

② Correlation

* Covariance



Co + variance

relate of feature with itself

To determine relationship b/w two variable.

$$\sum \frac{(x_i - \bar{x})^2}{n-1}$$

$$\sum \frac{(x_i - \bar{x})(x_i - \bar{x})}{n-1}$$

$$\sum \frac{(x_i - \bar{x})(y_i - \bar{y})}{n-1}$$

Co - variance

$$Cov(x, y) = \sum \frac{(x_i - \bar{x})(y_i - \bar{y})}{n-1}$$

X	Y
2	3
3	5
6	6
1	8
$\bar{x} = 3$	$\bar{y} = 5.5$



$$(2-3)(3-5.5) + (3-3)(5-5.5) + (6-3)(6-5.5) + (1-3)(8-5.5)$$

$$\Rightarrow \frac{(-1)(-2.5) + 0 + 3 \times 0.5 + -2 \times 2.5}{3}$$

$$= -1/3 = -0.33$$

→ The two features (x & y) is negatively related.

X	Y
2	3
4	5
6	7
$\bar{x} = 4$	$\bar{y} = 5$

$$\begin{aligned} \checkmark \text{Cov}(x, y) &= \frac{\sum (x - \bar{x})(y - \bar{y})}{n - 1} \\ &= \frac{(2 - 4)(3 - 5) + (4 - 4)(5 - 5) + (6 - 4)(7 - 5)}{3 - 1} \\ &= \frac{-2(-2) + 0 + 2(2)}{2} = \frac{4 + 4}{2} = 4 \end{aligned}$$

X & Y is +vely related

→ 0 → No relationship
 ✓ magnitude

Cov(x, y) = -0.33 → negative / inversely relation
 Cov(x, y) = +4 → +ve / directly relation

Name of owner	f1 (sqft) (Area of house)	Wt of the person living	time.	Y
Ajay	1800	180	10 years	1.2 cr.

$$\text{Cov} = \frac{\sum (x - \bar{x})(y - \bar{y})}{n - 1}$$

sqft (ft) wt
↑ ↓
x y

$$\underline{\underline{\text{Cov} = \text{sqft} \cdot \text{kg}}}$$

disadvantage of covariance

→ dimensional quantity

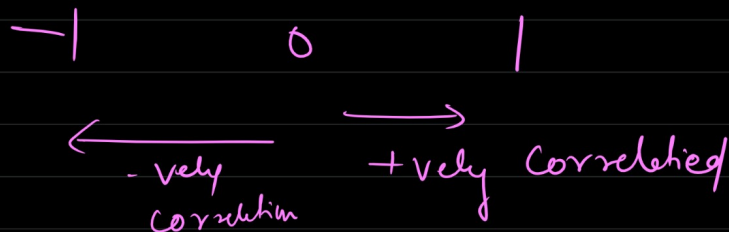
→ ranges between -∞ to ∞

$$\text{Cov}(x, y) \xrightarrow{\text{sqft} \rightarrow \text{kg}} \text{sqft} \cdot \text{kg}$$

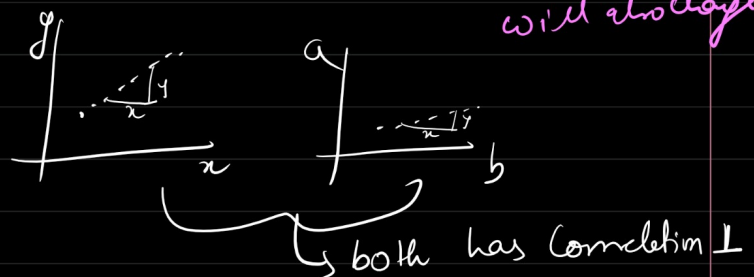
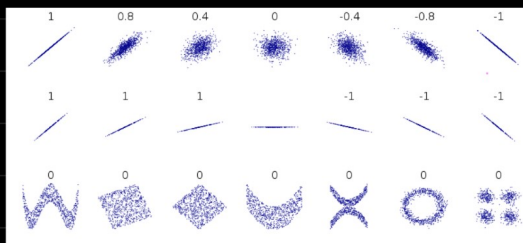
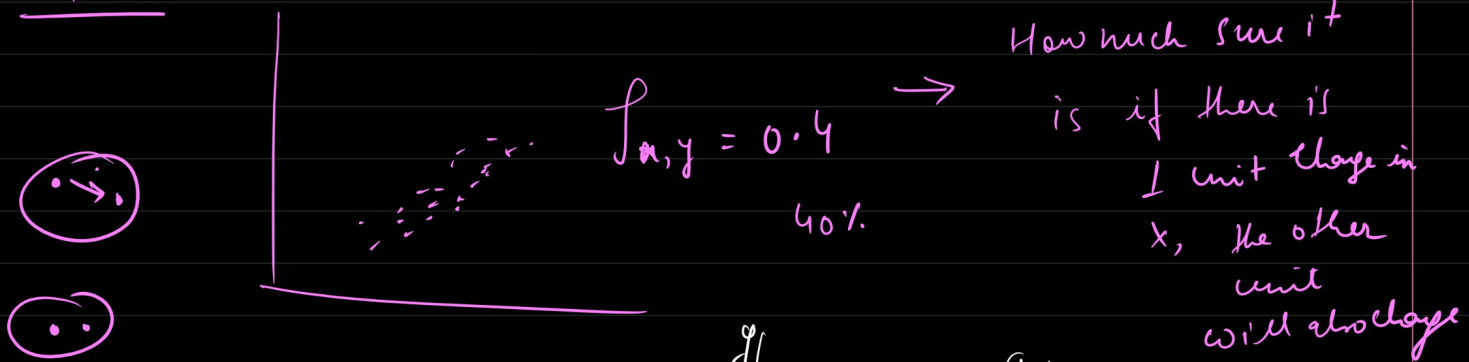
Correlation

$$\frac{\text{Cov}(x, y)}{\sigma_x \times \sigma_y} \frac{\frac{\text{kg}}{\text{kg}}}{\frac{\text{kg}}{\text{kg}}} \rightarrow \text{dimensionless quantity}$$

→ ranges from -1 and 1



Interpretation



* Correlation measures — linear relationship

* Spearman rank — Non linear relationship

$$\gamma_s = \frac{\text{Cov}(R(x), R(y))}{\sigma_{R(x)} \times \sigma_{R(y)}}$$

x	y	R(x)	R(y)
5	6	3	1
7	4	2	2
8	3	1	3
1	1	5	5
2	2	4	4

* Use case of correlation \rightarrow To select the relevant feature.

