VECTORS

$1 \quad 10^{th} \text{ Maths}$ - EXERCISE-7.2

1. Find the coordinates of the points of trisection of the line segment joining (4,-1) and (-2,-3)

2 SOLUTION

Given points are

$$\mathbf{Q} = \begin{pmatrix} 4 \\ -1 \end{pmatrix}, \mathbf{P} = \begin{pmatrix} -2 \\ -3 \end{pmatrix} \tag{1}$$

The equation of the formula is

$$\mathbf{R} = \frac{\mathbf{Q} + n\mathbf{P}}{1 + n} \tag{2}$$

Ratio 2:1 has taken

$$n = \frac{1}{2} \tag{3}$$

$$\mathbf{R} = \frac{1}{1 + \frac{1}{2}} \left(\begin{pmatrix} 4 \\ -1 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} -2 \\ -3 \end{pmatrix} \right) \tag{4}$$

$$\frac{1}{\frac{3}{2}} \left(\begin{pmatrix} 4 \\ -1 \end{pmatrix} + \begin{pmatrix} -1 \\ \frac{-3}{2} \end{pmatrix} \right) \tag{5}$$

$$\frac{1}{\frac{3}{2}}\left(\left(4+-1\right)\begin{pmatrix}-1\\\frac{-3}{2}\end{pmatrix}\right)\tag{6}$$

$$\frac{1}{2} \left(\begin{pmatrix} 3 & \frac{-2}{2} \end{pmatrix} \right) \tag{7}$$

$$\frac{3}{\frac{3}{2}} \left(\frac{\frac{-5}{2}}{\frac{3}{2}} \right) \tag{8}$$

$$\mathbf{R} = \begin{pmatrix} 2 & -5 \\ 2 & \frac{-5}{3} \end{pmatrix} \tag{9}$$

Ratio 1:2 has taken

$$n = \frac{2}{1} \tag{10}$$

$$\mathbf{S} = \frac{1}{1 + \frac{2}{1}} \left(\begin{pmatrix} 4 \\ -1 \end{pmatrix} + \frac{2}{1} \begin{pmatrix} -2 \\ -3 \end{pmatrix} \right) \tag{11}$$

$$\frac{1}{3}\left(\binom{4}{-1} + \left(-4 - 6\right)\right) \tag{12}$$

$$\frac{1}{3}((4+ -4)(-1+ -6))$$

$$\frac{1}{3}((0 -7))$$
(13)

$$\frac{1}{3}\left(\begin{pmatrix} 0 & -7 \end{pmatrix}\right) \tag{14}$$

$$\mathbf{S} = \begin{pmatrix} 0\\ \frac{-7}{3} \end{pmatrix} \tag{15}$$

3 Figure

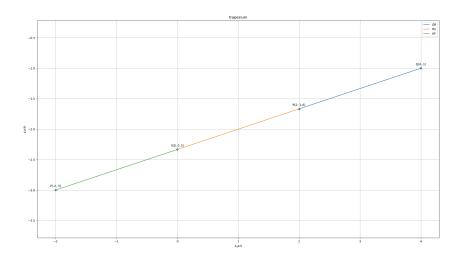


Figure 1: trisecton

 $https://\,github.com/\,prasaddeva 287/FWC/\,tree/main/VECTORS/7.2/\,codes$