LINE

$1 \quad 11^{th} \text{ Maths} - \text{EXERCISE-10.4}$

1. What are the points on the y-axis whose distance from the line $\frac{x}{3} + \frac{y}{4} = 1$ is 4 units.

2 SOLUTION

Given line equation is

$$\frac{x}{3} + \frac{y}{4} = 1\tag{1}$$

$$(4\mathbf{x} + 3\mathbf{y} - 12) = 0 \tag{2}$$

$$\mathbf{n} = \begin{pmatrix} 4\\3 \end{pmatrix} \tag{3}$$

$$\mathbf{d} = 4 \tag{4}$$

The distance of the line from y-axis

$$\mathbf{d} = \frac{\mathbf{n}^{\top} \mathbf{P} - \mathbf{c}}{\|\mathbf{n}\|} \tag{5}$$

$$4 = \pm \frac{\begin{pmatrix} 4 & 3 \end{pmatrix} \begin{pmatrix} 0 \\ y \end{pmatrix} - 12}{5} \tag{6}$$

$$4 = \pm \frac{\binom{0}{3y} - 12}{5} \tag{7}$$

$$20 = \pm 3y - 12 \tag{8}$$

$$3y = 20 \pm 12$$
 (9)

$$y = \left(\frac{32}{3}\right)\left(\frac{-8}{3}\right) \tag{10}$$

Thus, the required points are $(0, \frac{32}{3})$ and $(0, \frac{-8}{3})$

3 FIGURE

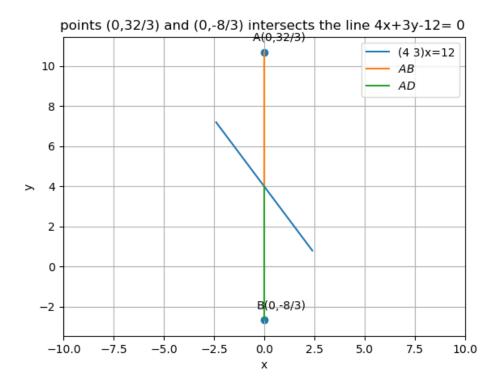


Figure 1: line