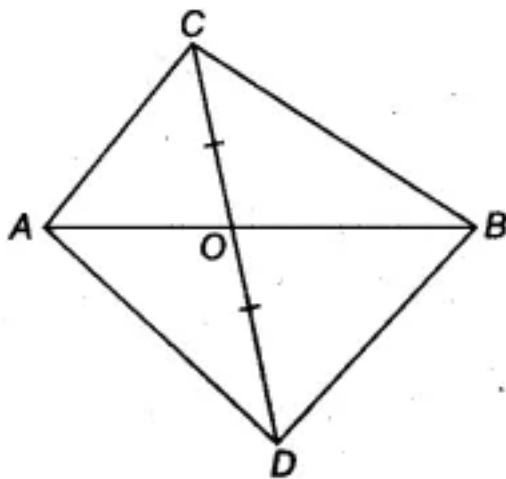


Contents

1 Problem

ABC, ABD are 2 triangles on same base AB, if line segment CD is bisected by AB at O, show that
(i) $\text{ar}(\triangle ABC) = \text{ar}(\triangle ABD)$



2 Solution

Theory:

In 2 triangles with same base and line segment CD is bisected at O **To Prove:** $\text{Ar}(\triangle ABC) = \text{Ar}(\triangle ABD)$

Theorem : Two triangles on the same base (or equal bases) and having the equal heights are equal in area.

$$\therefore \text{Ar}(\triangle ABC) = \text{Ar}(\triangle ABD) \dots (1)$$

Hence, Proved

termux commands :

```
python3 matrix.py
```

The input parameters for this construction are

Symbol	Value	Description
k1	4	length of CD
k2	6	length of AB
O	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	Point O

To Prove: $\text{Ar}(\triangle ABC) = \text{Ar}(\triangle ABD)$

$$a = A - B$$

$$b = C - B$$

$$c = B - D$$

Area of the $\triangle ABC$ is given by

$$\text{Ar}(\triangle ABC) = \frac{1}{2} \|a \times b\| \dots (2)$$

$$b = C - B$$

$$c = B - D$$

Area of the $\triangle ABD$ is given by

$$\text{Ar}(\triangle ABD) = \frac{1}{2} \|c \times d\| \dots (3)$$

$$\therefore \text{Ar}(\triangle ABC) = \text{Ar}(\triangle ABD) \dots (4)$$

The below python code realizes the above construction:

<https://github.com/anirudhkalyan/fwc>

3 Construction

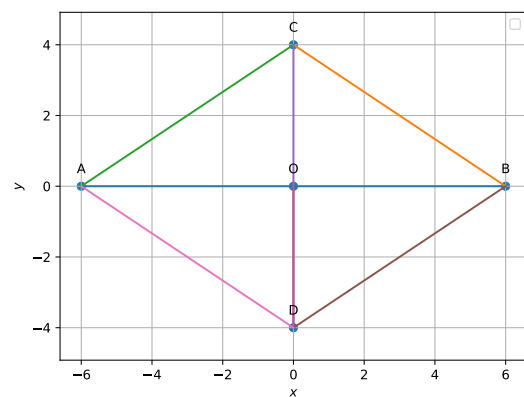


Figure of construction