# MATRICES USING PYTHON(CIRCLE)

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Assignment

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FWC22066

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### 1 Problem

The centre of the circle passing through (0,0)and (1,0) and touching the circle  $x^2+y^2=9\,$ 

### 2 Construction

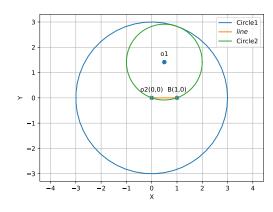


Figure of construction

## 3 Solution

The standard circle equation

$$\mathbf{x}^{\top}\mathbf{V}\mathbf{x} + 2\mathbf{u}^{\top}\mathbf{x} + f = 0 \tag{1}$$

Given Circle equation :  $x^2 + y^2 = 9$ 

The given circle can be expressed as conics with parameters

$$\mathbf{x}^{\top} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \mathbf{x} + 2 \begin{pmatrix} 0 & 0 \end{pmatrix} \mathbf{x} + f_2 = 0$$
 (2)

$$\mathbf{V_1} = \mathbf{I}, \mathbf{u_2} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, f_2 = -9 \tag{3}$$

$$r_2 = \sqrt{\mathbf{u_2}^\top \mathbf{u_2} - f_2} \tag{4}$$

 $r_2 = 3 \tag{5}$ 

The given circle can be expressed as conics with parameters For finding center  $\mathbf{u}_{1}$ 

$$\mathbf{x}^{\top} \mathbf{V} \mathbf{x} + 2\mathbf{u_1}^{\top} \mathbf{x} + f_1 = 0 \tag{6}$$

$$\mathbf{A}^{\top}\mathbf{A} + 2\mathbf{u_1}^{\top}\mathbf{A} + f_1 = 0 \tag{7}$$

$$\mathbf{B}^{\top}\mathbf{B} + 2\mathbf{u_1}^{\top}\mathbf{B} + f_1 = 0 \tag{8}$$

$$\mathbf{V} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \tag{9}$$

when substitute  $\mathbf{A},\mathbf{B}$  in eq 6and 7

 $f_1 = 0$ , by eq 7

$$1 + 2\mathbf{u_1}^{\top} \begin{pmatrix} 1\\0 \end{pmatrix} + f_1 = 0 \tag{10}$$

$$1 + 2\mathbf{u_1}^{\mathsf{T}} \mathbf{e_1} = 0 \tag{11}$$

$$\mathbf{u_1}^{\mathsf{T}} \mathbf{e_1} = -1/2 \tag{12}$$

$$\mathbf{u_1} = \begin{pmatrix} x \\ y \end{pmatrix} \tag{13}$$

substitute in eq-11

$$\begin{pmatrix} x & y \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -1/2 \tag{14}$$

$$x = -1/2 \tag{15}$$

substitute  $\times$  in eq-13

$$\mathbf{u_1} = \begin{pmatrix} -1/2 \\ y \end{pmatrix} \tag{16}$$

$$\|\mathbf{u_1} - \mathbf{u_2}\| = (r_1 - r_2)^2$$
 (17)

$$r_1 = \frac{r_2}{2} \tag{18}$$

$$\|\mathbf{u_1}\|^2 = r_1^2 \tag{19}$$

$$\|\mathbf{u_1}\|^2 = (r_2/2)^2 \tag{20}$$

by using eq-15

$$\|\mathbf{u_1}\|^2 = 1/4 + y^2 = \frac{r_2^2}{4}$$
 (21)

$$y = \pm \sqrt{\frac{r_2^2}{4} - \frac{1}{4}} \tag{22}$$

yielding,

$$y = \pm \sqrt{2} \tag{23}$$

substituting y in eq-15  $\,$ 

$$\mathbf{u_1} = \begin{pmatrix} -1/2 \\ -\sqrt{2} \end{pmatrix} \tag{24}$$

$$\mathbf{o_1} = -\mathbf{u_1} \tag{25}$$

$$r_1 = \sqrt{\mathbf{u_1}^\top \mathbf{u_1} - f_1} \tag{26}$$

$$r_1 = 3/2$$
 (27)

The input parameters for this construction are

Symbol	Value	Description
A	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	Centre1,point p1
В	$\begin{pmatrix} 1 \\ 0 \end{pmatrix}$	point2
02	$\begin{pmatrix} -1/2 \\ -\sqrt{2} \end{pmatrix}$	center2
R	(1.5)	Radius2

Below python code realizes the above construction

https://github.com/Radhikarkv/fwcproject.git