

# Matrix Assignment

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## 1 Problem Statement

In a triangle ABC, E is the mid-point of median AD.

Show that  $\ar(\triangle BED) = \frac{1}{4} \ar(\triangle ABC)$

## 2 Diagram

Plot of Triangle is shown in figure 1, where point B is origin and points A, B, C and D are the vertices of Triangle.

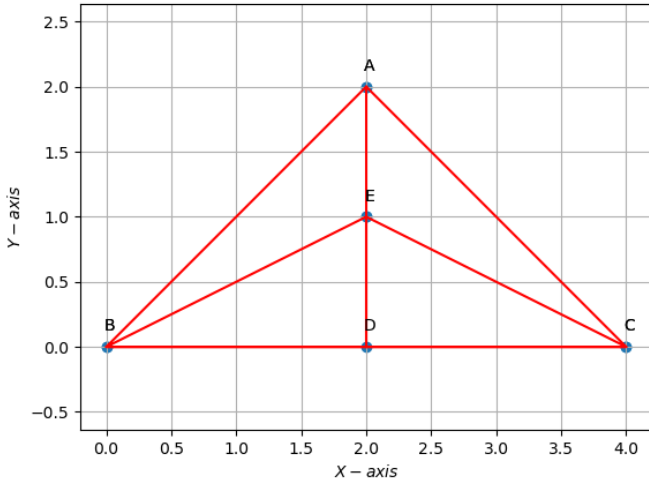


Figure 1: Triangle

## 3 PROOF

In  $\triangle ABC$ , with AD as median E is the mid-point of AD

$$\|\mathbf{E} - \mathbf{A}\| = \|\mathbf{E} - \mathbf{D}\|$$

$$\|\mathbf{D} - \mathbf{B}\| = \frac{1}{2} \|\mathbf{C} - \mathbf{B}\| \quad (1)$$

From  $\triangle ABC$

$$\ar(\triangle ABC) = \frac{1}{2} \times \|\mathbf{B} - \mathbf{A}\| \times \|\mathbf{C} - \mathbf{B}\| \quad (2)$$

From  $\triangle BED$

$$\ar(\triangle BED) = \frac{1}{2} \times \|\mathbf{E} - \mathbf{B}\| \times \|\mathbf{D} - \mathbf{B}\|$$

From Eq(1) we can write as

$$\ar(\triangle BED) = \frac{1}{2} \times \|\mathbf{E} - \mathbf{B}\| \times \frac{1}{2} \|\mathbf{C} - \mathbf{B}\| \quad (3)$$

We know that from Parallelogram law of Vector Addition

$$\mathbf{E} - \mathbf{B} = \frac{1}{2}((\mathbf{B} - \mathbf{A}) + \mathbf{C} - \mathbf{B}) \quad (4)$$

Substituting Eq(4) in Eq(3) & re-writing the Eq(3)

$$\ar(\triangle BED) = \frac{1}{2} \times ((\frac{1}{2} \|(\mathbf{B} - \mathbf{A}) + (\mathbf{C} - \mathbf{B})\|) \times \frac{1}{2} \|\mathbf{C} - \mathbf{B}\|)$$

$$\ar(\triangle BED) = \frac{1}{2} \times \frac{1}{4} (\|\mathbf{B} - \mathbf{A}\| \times \|\mathbf{C} - \mathbf{B}\|)$$

$$\ar(\triangle BED) = \frac{1}{4} (\frac{1}{2} \times \|\mathbf{B} - \mathbf{A}\| \times \|\mathbf{C} - \mathbf{B}\|)$$

From Eq(2)

$$\ar(\triangle BED) = \frac{1}{4} (\ar(\triangle ABC))$$

$$\boxed{\ar(\triangle BED) = \frac{1}{4} \ar(\triangle ABC)}$$

Hence Proved

## 4 Software

Download the codes given in the link below and execute them.

<https://raw.githubusercontent.com/19PA1AO410/FWC-Module-1/main/Matrix>