

BNF – Backus Naur Form

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BNF for date

```
<date> ::= <month> "/" <day> "/" <year>  
<month> ::= "1" [0-2] | "0" [1-9]  
<day> ::= "0" [1-9] | [1-2] [0-9] | "3" [0-1]  
<year> ::= [0-9] [0-9] [0-9] [0-9]
```

BNF for integer

$$\langle \text{integer} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{digit} \rangle \langle \text{integer} \rangle$$

BNF for floating point

```
floatnumber ::= pointfloat | exponentfloat  
pointfloat  ::= [intpart] fraction | intpart "."  
exponentfloat ::= (intpart | pointfloat) exponent  
intpart     ::= digit+  
fraction    ::= "." digit+  
exponent    ::= ("e" | "E") ["+" | "-"] digit+
```

A BNF for specifying Postal Address

`<postal-address> ::= <name-part> <street-address> <zip-part>`

`<name-part> ::= <personal-part> <last-name> <opt-suffix-part> <EOL> | <personal-part> <name-part>`

`<personal-part> ::= <initial> "." | <first-name>`

`<street-address> ::= <house-num> <street-name> <opt-apt-num> <EOL>`

`<zip-part> ::= <town-name> ", " <state-code> <ZIP-code> <EOL>`

`<opt-suffix-part> ::= "Sr." | "Jr." | <roman-numeral> | ""`

`<opt-apt-num> ::= <apt-num> | ""`

A note about Slang Compiler Infrastructure

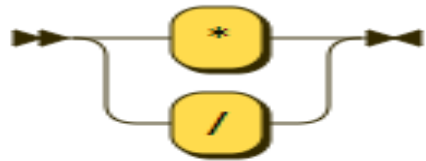
- An Open Source Compiler (to learn Compiler Engineering)
- Available @ <https://github.com/praseedpai/SlangForDotNet>
- Ports available to Java,C++,VB.net,JS,Python
- A JavaScript Port of the Compiler is available @ <http://shinexavier.github.io/SlangJS/>
- A Pascal Syntax Diagram for the BNF available @ <http://shinexavier.github.io/SlangJS/SyntaxDiagram.xhtml>

Pascal Syntax Diagram (based on BNF) for Slang

```
<expr> ::= <BExpr>
<BExpr> ::= <LExpr> LOGIC_OP <BExpr>
<LExpr> ::= <RExpr> REL_OP <LExpr>
<RExpr> ::= <Term> ADD_OP <RExpr>
<Term> ::= <Factor> MUL_OP <Term>
<Factor> ::= <Numeric> | <String> | TRUE | FALSE | <variable> | '(' <expr> ')' | {+|-|!}<Factor> | <callexpr>
<callexpr> ::= funcname '(' actuals ')'
<LOGIC_OP> ::= '&&' | '||'
<REL_OP> ::= '>' | '<' | '>=' | '<=' | '<>' | '=='
<MUL_OP> ::= '*' | '/'
<ADD_OP> ::= '+' | '-'
```


Pascal Syntax Diagram for Slang (based on BNF)

MUL_OP:

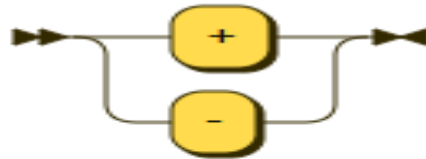


MUL_OP ::= '*'
| '/'

referenced by:

- Term

ADD_OP:

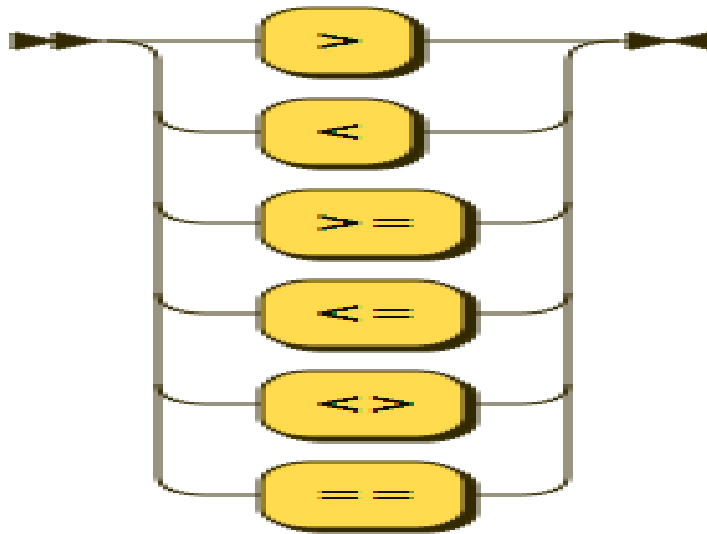


ADD_OP ::= '+'
| '-'

referenced by:

- RExpr

REL_OP:



REL_OP ::= '<'
| '<='
| '>'
| '>='
| '≠'
| '=='

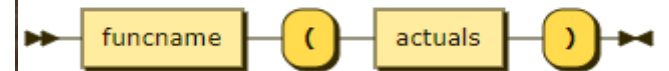
referenced by:

- LExpr

referenced by:

- Factor
- Term

callexpr:

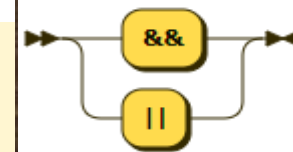


callexpr ::= funcname '(' actuals ')'

referenced by:

- Factor

LOGIC_OP:



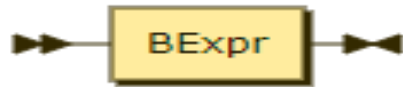
LOGIC_OP ::= '&&'
| '||'

referenced by:

- BExpr

Pascal Syntax Diagram for Slang (based on BNF)

expr:

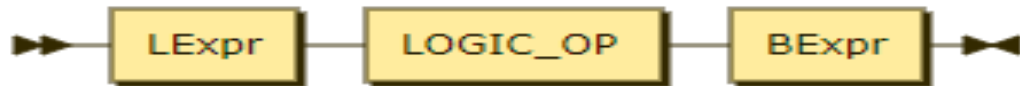


expr ::= BExpr

referenced by:

- Factor
- ifstmt
- printstmt
- returnstmt
- whilestmt

BExpr:

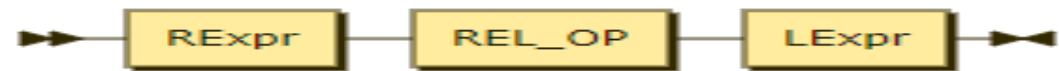


BExpr ::= LExpr LOGIC_OP BExpr

referenced by:

- BExpr
- expr

LExpr:

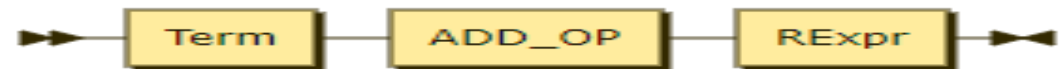


LExpr ::= RExpr REL_OP LExpr

referenced by:

- BExpr
- LExpr

RExpr:



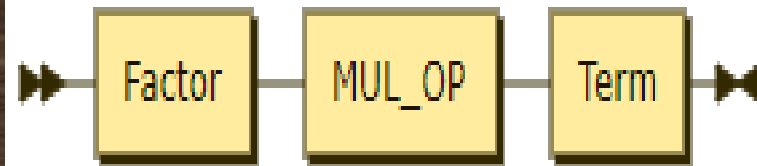
RExpr ::= Term ADD_OP RExpr

referenced by:

- LExpr
- RExpr

Pascal Syntax Diagram for Slang (based on BNF)

Term:

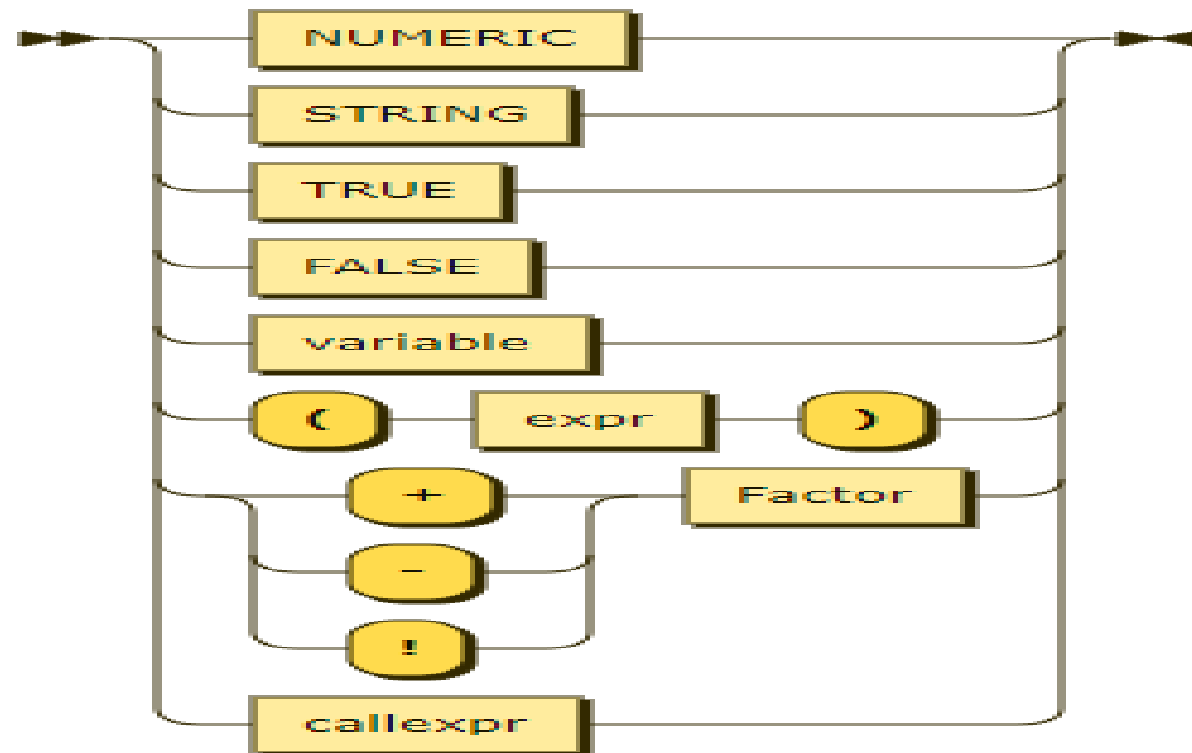


`Term ::= Factor MUL_OP Term`

referenced by:

- RExpr
- Term

Factor:



```
Factor ::= NUMERIC
          STRING
          TRUE
          FALSE
          variable
          '(' expr ')'
          ( '+' | '-' | '!' ) Factor
          callexpr
```

Backus Naur Form for a Four function Calculator

$\langle \text{Expr} \rangle ::= \langle \text{Term} \rangle \mid \text{Term} \{ + \mid - \} \langle \text{Expr} \rangle$

$\langle \text{Term} \rangle ::= \langle \text{Factor} \rangle \mid \langle \text{Factor} \rangle \{ * \mid / \} \langle \text{Term} \rangle$

$\langle \text{Factor} \rangle ::= \langle \text{number} \rangle \mid (\langle \text{expr} \rangle) \mid \{ + \mid - \} \langle \text{factor} \rangle$

Tokens and Lexical Analysis

```
TOK_PLUS - '+' TOK_MUL - '*' TOK_SUB - '-' TOK_DIV - '/'  
TOK_OPAREN - '(' TOK_CPAREN - ')' TOK_DOUBLE - [0-9] +
```

```
// Enumeration for Tokens
```

```
public enum TOKEN {  
    ILLEGAL_TOKEN = -1, // Not a Token  
    TOK_PLUS = 1, // '+'  
    TOK_MUL, // '*'  
    TOK_DIV, // '/'  
    TOK_SUB, // '-'  
    TOK_OPAREN, // '('  
    TOK_CPAREN, // ')'   
    TOK_DOUBLE, // '['  
    TOK_NULL // End of string  
}
```

```
while ( there is input ) {  
    switch(currentchar) {  
        case Operands:  
            advance input pointer  
            return TOK_XXXX;  
        case Number:  
            Extract the number( Advance the input )  
            return TOK_DOUBLE;  
        default:  
            error  
    }  
}
```

Converting $\langle \text{Expr} \rangle$ Production to the Code

```
//  $\langle \text{Expr} \rangle ::= \langle \text{Term} \rangle \{ + \mid - \} \langle \text{Expr} \rangle$ 
Void Expr() {
    Term();
    if ( Token == TOK_PLUS || Token == TOK_SUB ){
        // Emit instructions
        // and perform semantic operations
        Expr(); // recurse
    }
}
```

Converting $\langle \text{Term} \rangle$ Production to the Code

```
//  $\langle \text{Term} \rangle ::= \langle \text{Factor} \rangle \{ * | / \} \langle \text{Term} \rangle$   
Void Term() {  
    Factor();  
    if ( Token == TOK_MUL || Token == TOK_DIV ){  
        // Emit instructions  
        // and perform semantic operations  
        Term(); // recurse  
    }  
}
```

Converting <Factor> Production to the Code

```
// <Factor> ::= <TOK_DOUBLE> | ( <expr> ) | { + |- } <Factor>
//
Void Factor() {
    switch(Token)
        case TOK_DOUBLE:
            // push token to IL operand stack return
        case TOK_OPAREN:
            Expr(); //recurse
            // check for closing parenthesis and return
        case UNARYOP:
            Factor(); //recurse
        default:
            //Error
    }
}
```


A “Naïve” Stack Class

```
class Stack {  
    double[] stk;  
    int top_stack = 0;  
    public Stack() { stk = new double[256]; top_stack = 0; }  
    public void Clear(){ top_stack = 0; }  
    public void push(double dbl ){  
        if ( top_stack == 255 ){ throw new Exception();}  
        stk[top_stack++] = dbl;  
    }  
    public double pop(){  
        if ( top_stack == 0 ){ throw new Exception(); }  
        return stk[--top_stack];  
    }  
}
```

Recursive Descent Parsing

```
class RDParse : Lexer {
    TOKEN Current_Token; Stack ValueStack = new Stack() ;
    public RDParse(String str):base(str){}
    public double CallExpr(){
        ValueStack.Clear(); Current_Token= GetToken(); Expr();
        double nd = ValueStack.pop(); return nd;
    }
    public void Expr(){
        TOKEN l_token; Term();
        if (Current_Token == TOKEN.TOK_PLUS || Current_Token == TOKEN.TOK_SUB){
            l_token = Current_Token; Current_Token = GetToken();
            Expr();
            double x = ValueStack.pop(); double y = ValueStack.pop();
            ValueStack.push( (l_token == TOKEN.TOK_PLUS ) ? (x + y) : (y-x) );
        }
    }
    public void Term(){
        TOKEN l_token; Factor();
        if (Current_Token == TOKEN.TOK_MUL || Current_Token==TOKEN.TOK_DIV) {
            l_token = Current_Token; Current_Token = GetToken(); Term();
            double x = ValueStack.pop();double y = ValueStack.pop();
```

Recursive Descent Parsing (Contd...)

```
        if ( x == 0 ) { throw new Exception();}
        ValueStack.push( (l_token == TOKEN.TOK_MUL ) ? (x * y) : (y/x) );
    }
}

public void Factor(){
    TOKEN l_token;
    if ( Current_Token == TOKEN.TOK_DOUBLE ){
        ValueStack.push(GetNumber());Current_Token = GetToken();
    } else if ( Current_Token == TOKEN.TOK_OPAREN ) {
        Current_Token = GetToken(); Expr(); // Recurse
    } if ( Current_Token != TOKEN.TOK_CPAREN ){ throw new Exception();}
        Current_Token = GetToken();
    } else if (Current_Token == TOKEN.TOK_PLUS || Current_Token == TOKEN.TOK_SUB ){
        l_token = Current_Token; Current_Token = GetToken();
        Factor(); double x = ValueStack.pop();
        if ( l_token == TOKEN.TOK_SUB ) { x = -x; }
        ValueStack.push(x);
    } else { throw new Exception();}
}
}
```

Run and Evaluate

<https://github.com/praseedpai/ElementaryMathForProgrammingSeries/blob/master/AlgebraNArith/ExprEval/RDParserStack.cs>

```
D:\csharp>RDParserStack "2+3"  
The Evaluated Value is 5
```

```
D:\csharp>RDParserStack "2+3*4"  
The Evaluated Value is 14
```

```
D:\csharp>RDParserStack "2+3*-4"  
The Evaluated Value is -10
```

Q&A

- If any!