

# CS 573000 : Homework 5

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## 1 Question A.1

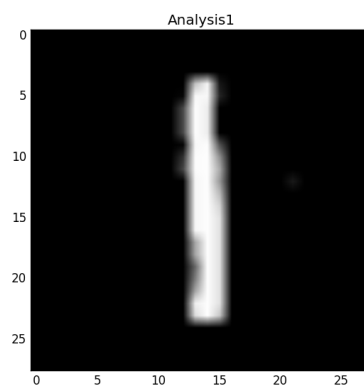


Figure 1: Visualization of digit "1"

## 2 Question A.2

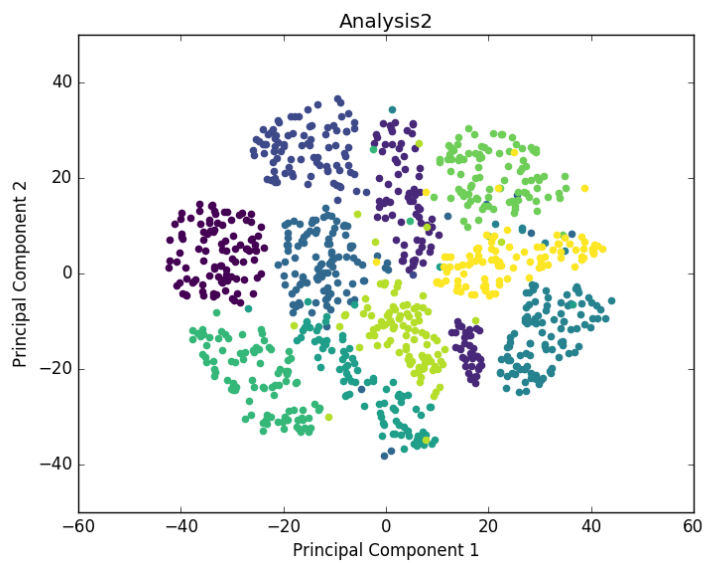


Figure 2: Visualization of random selected sample

### 3 Question B.1

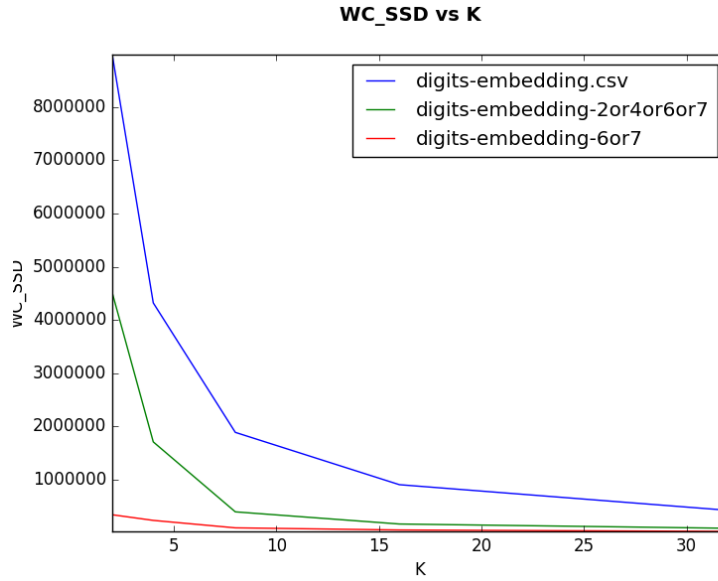


Figure 3: WC SSD vs K

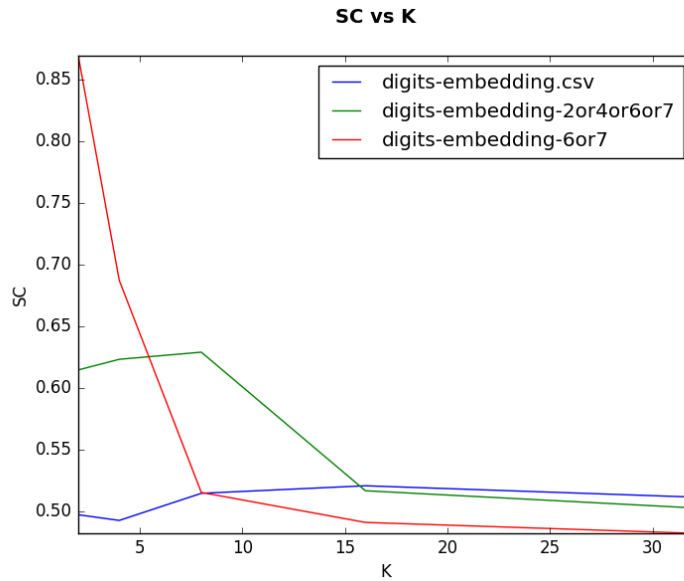


Figure 4: SC vs K

### 4 Question B.2

The Silhouette coefficient decreases for increasing K however, looking at the SC and WC SSD graphs we find that the selection of 8,4,2 are the best choices for the digits-embedding.csv, digits-embedding-2or4or6or7.csv, digits-embedding-2or4.csv files, respectively. The argument for this is that since each number would represent a cluster ideally, we should set to be atleast greater than or equal to the number of expected clusters. For the 2-4-6-7 cast 4 clusters would be needed, and so follows for the other two csv files. In the graphs we see that the sharpest drop in scores for Silhouette score occurs at these chosen values. In the WC SSD curve, we see a similar trend of drops at these points. Hence, they are considered good values for K.

## 5 Question B.3

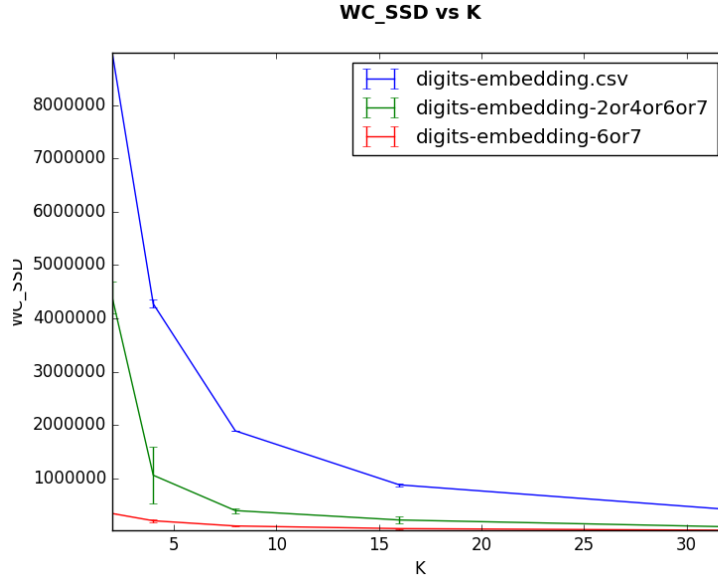


Figure 5: WC SSD vs K

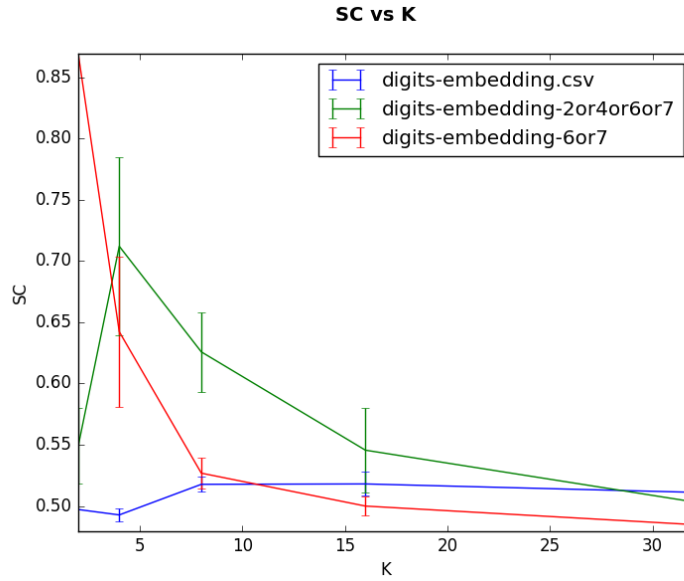


Figure 6: SC vs K

The standard error is the average standard deviation in the plots above across 10 random seed initial start initializations. The  $WC - SSD$  plot doesn't show much variance, however, the SC plot shows significant variance across K values, being more sensitive for low values of K but decreasing in effect for larger values. In addition, the digits-embedding.csv is most insensitive to start conditions.

## 6 Question B.4

### 6.1 Reporting Mean NMI across 10 trials

NMI 0.686 digits-embedding.csv K = [8]

NMI 0.909 digits-embedding-2or4or6or7 K = [4]

NMI 0.981 digits-embedding-6or7 K = [2]

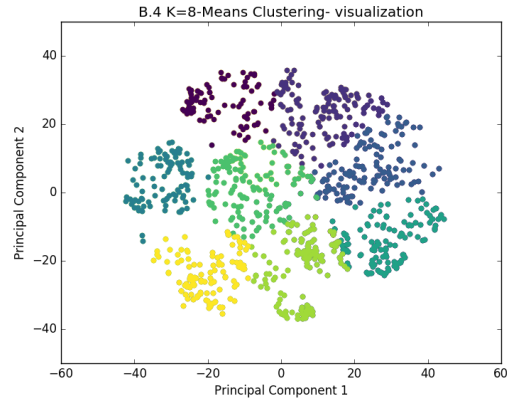


Figure 7: digits-embedding.csv

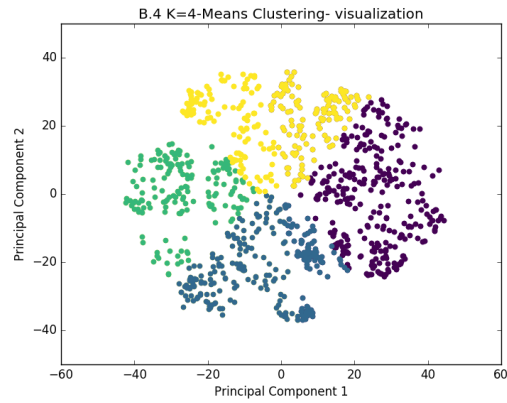


Figure 8: digits-embedding-2or4or6or7.csv

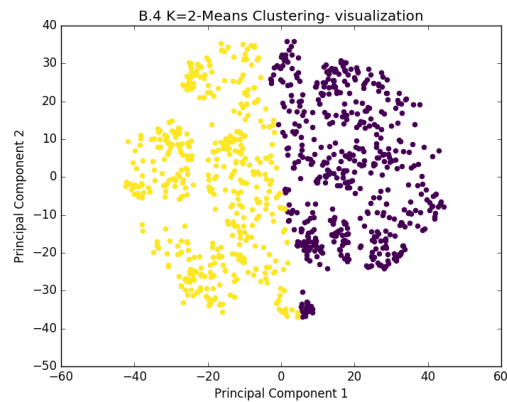


Figure 9: digits-embedding-6or7.csv

## 6.2 Analysis

The clusters are better separated on the the 2or4or6or7 , and 6or7 datasets, hence we see much higher NMI scores around 0.9 for each as compared to the NMI score of embeddings datasets which is much lower due to lower separability.

## 7 Question C1

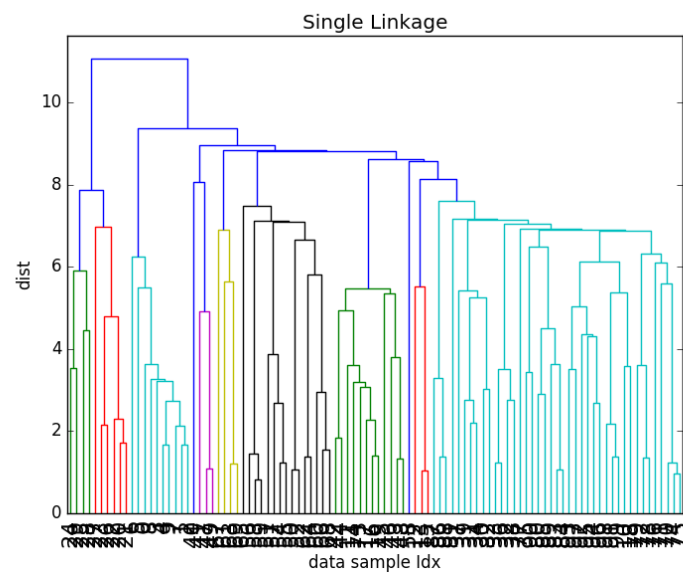


Figure 10: Single Linkage

## 8 Question C2

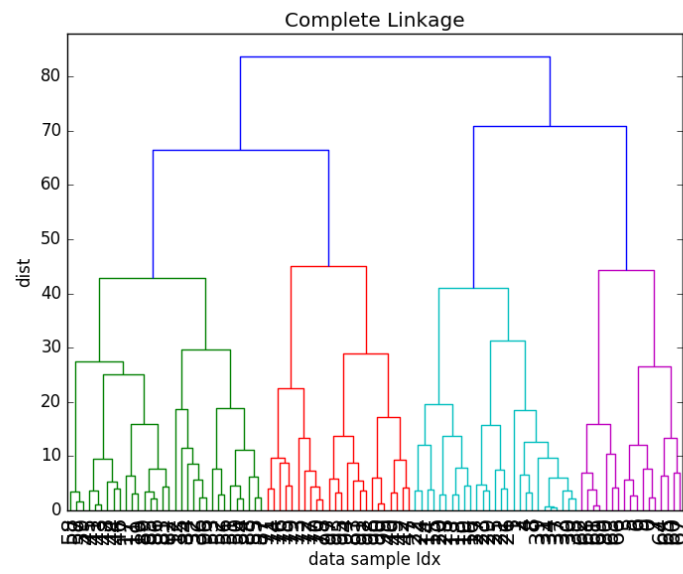


Figure 11: Complete Linkage

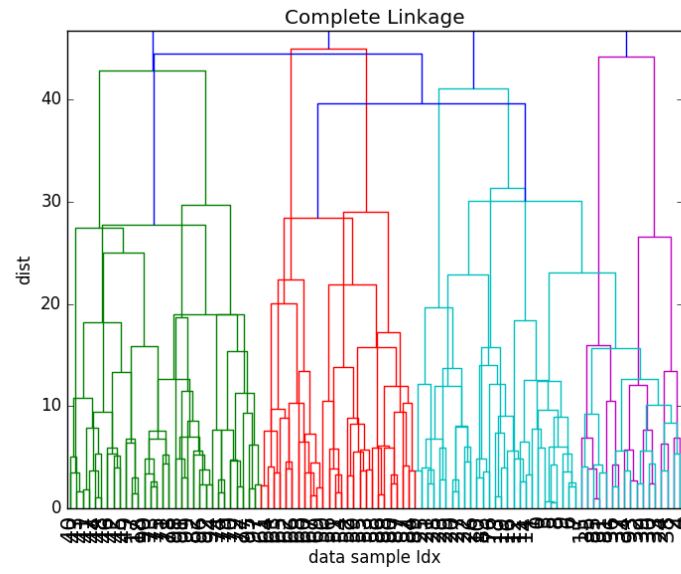


Figure 12: Average Linkage

## 9 Question C3

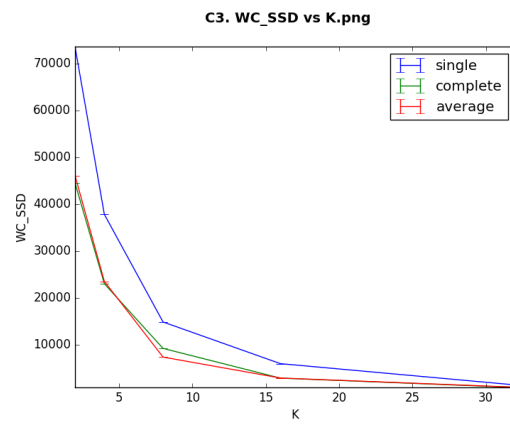


Figure 13: WC-SSD vs K for Agglomerative Clustering

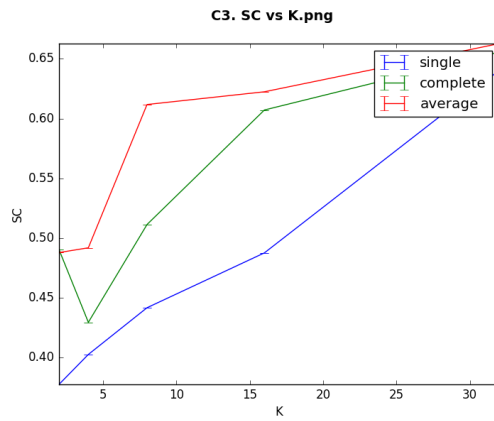


Figure 14: SC vs K for Agglomerative Clustering

## 10 Question C4

Since the SC scores are high for K values 32, 16, 16 for single, complete and average linkages respectively. The K values differ from those chosen in part B since we observe that the NMI scores for these choices are much higher than the previous choices.

## 11 Question C5

### 11.1 Reporting Mean NMI across 10 trials

Here we show the K = 32, single linkage, K = 16 complete linkage, K = 16 average linkage mean NMI over 10 runs. [ 0.74995836 0.76696711 0.77013204]

As mentioned earlier for the embeddings dataset, we get highest for K = 16 which beats the previous obtained NMI score of 0.686.

## 12 Bonus