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## Assignment-1

# EE:1205 Signals and System Indian Institute of Technology, Hyderabad

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### I. Question 12.7-15

A  $100\mu\text{F}$  capacitor in series with a  $40\Omega$  resistance is connected to a 110V, 60Hz supply.

- (a) What is the maximum current in the circuit?
- (b) What is the time lag between the current maximum and the voltage maximum?

For an RC circuit, we have the relation for impedance as:

$$Z = R^2 + \frac{1}{\omega^2 C^2} \tag{7}$$

Maximum current is given as:

$$I_0 = \frac{V_0}{Z} \tag{8}$$

From (7), (8)

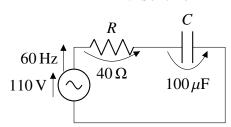
$$I_0 = \frac{V_0}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}} \tag{9}$$

$$I_0 = \frac{V_0}{\sqrt{40^2 + \frac{1}{(120\pi)^2 \times (10^{-4})^2}}}$$
 (10)

$$I_0 = \frac{100\sqrt{2}}{\sqrt{1600 + \frac{10^8}{(120\pi)^2}}} \tag{11}$$

$$I_0 = 3.24 \tag{12}$$

II. SOLUTION



Capacitance of the capacitor:

$$C = 100\mu F = 100 \times 10^{-6} \tag{1}$$

Resistance of the resistor:

$$R = 40\Omega \tag{2}$$

Supply voltage:

$$V = 110V$$

(a) Frequency of oscillations:

$$v = 60Hz \tag{4}$$

Angular frequency:

$$\omega = 2\Pi v = 2\pi \times 60 \tag{5}$$

Peak voltage:

$$V_0 = V\sqrt{2} = 110\sqrt{2}V$$
 (6)  $\phi = tan^{-1}(0.6635) = 33.56 \deg = \frac{33.56\pi}{180} rad$  (15)

(3)

(b) In a capacitor circuit, the voltage lags behind the current by a phase angle of 
$$\phi$$
. This angle is given by the relation:

 $tan\phi = \frac{1}{120\pi \times 10^{-4} \times 40}$ 

$$tan\phi = \frac{1}{\omega CR} \tag{13}$$

(14)

$$\therefore Time \ lag = \frac{\phi}{\omega}$$
 (16)

$$Time \ lag = \frac{33.56\pi}{180 \times 120\pi} \tag{17}$$

Time lag = 
$$1.55 \times 10^{-3} s = 1.55 ms$$
 (18)

Hence, the time lag between maximum current and maximum voltage is 1.55ms.