

# C++

## Unit I:- Introduction

1. Structured vs OO development
2. Elements of OO programming
3. Abstraction - Importance
4. Polymorphism -
5. Encapsulation -
6. static & Dynamic Binding

## Unit - II: Classes and Objects:

1. Classes and Objects
2. Accessing members of class
3. member func & inline func
4. Accessing mem. func within class
5. Data hiding and member accessibility
6. Empty classes
7. Constructors & Overloading
8. "new", "delete", "this"
9. friend class and friend functions

## Unit -III: Overloading:

1. function overloading
2. Operator overloading
  - 'operator' keyword
  - unary operator overloading
3. Generic Programming with templates
  - function templates
  - class templates.

## Unit -IV Inheritance:

1. Base-class - derived class relationship
2. Forms of Inheritance
3. "Constructors" & "destructors" in derived class
4. Constructor Invocation
5. Data Conversion (from one obj to other)
6. Virtual base classes, virtual functions

## Unit -V Exceptional handling & files:

1. exception model
2. E. handling constructs
3. list of exceptions, catching & handling
4. Opening & closing file
5. file modes
6. file pts & manipulation
7. seq. access & RAM access
8. error handling during file manipulations

## structured

1. focus on algo
2. ~~No control over data flow & visibility~~
3. program is divided into object functions
4. ~~static pop-down Design~~
5. No dynamic binding
- 6.
7. difficult to design, maintain & upgrade the system
- 8.

1. emphasis on data
2. control over data flow & visibility (data hidden)
3. pgm is divided into objects & functions
4. Bottom up Design
5. Dynamic binding
6. Message passing
7. easy to design, maintain & enhance the system

- static, re-usable, stable, less prone to errors
- inheritance is forward i.e. from parent to child
- polymorphism and generic methods are available
- classes are user-defined datatype or blueprints

## Elements of Object Oriented Programming:

1. Class : logical entity, user defined data type and collection of objects, of same attributes & behavior.

2. Object : physical entity, and has a state & behav.

3. Data Encapsulation

3. Data Abstraction:-

Creating new data types using encapsulated items, that are well suited to an application to be programmed, is known as "Data Abstraction" and data types are, "Abstract Data types".

Hiding internal details and showing only required functionality is known as "Abstraction".

4. Data Encapsulation :-

Binding code and data together into a single unit is known as "Encapsulation".

In this data cannot be accessed directly & allowed to access only through functions.

Thus, it enables important concept of

Data hiding possible

## 5. Inheritance:-

- \* It is the process by which one object can acquire the properties of another.
- \* allows declaration & implementation of one class to be based on an existing class
  - Reusability
  - along with dynamic binding, polymorphism enhances the sw.

## 6. Polymorphism:-

- Some operations may behave differently, in different situations. (many forms)

Ex:- if you call "move()" function with Human object it performs differently when it is called with other animal object.

## 7. Dynamic Binding:-

C++ provides facility to specify that the compiler should match function calls with the correct definition at the run time.

this is called Dynamic Binding (or) Run-time binding

binding (or) Late Binding; it is to

Ex:-

if we have class Animal &

virtual move();

y

}

int main();

class Human : public Animal {

move();

};

class Dog : public Animal {

move();

y

};

## classes :-

Consider following example:

```

1. class Test {
    char a;
    int b;
    char c;
};

int main() {
    Test t;
    cout << sizeof(t);
}

```

output:

12

size of object

class Test

char a;

char b;

int c;

}

int main()

Test t;

cout << sizeof(t);

output:

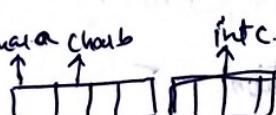
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- \* Here the placing of variables in class also defines the size of the ~~new~~ object.

- \* In Case 1 :



- In Case 2 :



- \* Size of ~~empty~~ empty class objects will be 1

## Operator Overloading:

- static polymorphism

Designed to apply in

following principle

1. Extending capability of operators on user defined data

2. Data Conversion

## Overloadable Operators:

Operator Category	Operators
Arithmetic	+, -, *, /, %
Bit-wise	&,  , ~, ^
Logical	&&,   , !
Relational	<, <=, !=, >, >=
Assignment	=
Initialisation	=
Arithmetic assignment	+=, -=, *=, /=, %=
Shift	<<, >>, >>=, <<=
Unary	++, --
Subscripting	[]
Function call	()
Dereferencing	→
Unary sign prefix	+, -
Allocate and free	new, delete

## Syntax for operator overloading:

Return type      operator      OperatorSymbol ([arg<sub>1</sub>, arg<sub>2</sub>])

↳

3

~~Complex~~  
~~ClassName~~

operator + (complex c<sub>2</sub>)

↳ // one object 'c1' implicit & other explicit c<sub>2</sub>

3

for istream & ostream

only using friend function & find function  
with both classes

cannot

be invoked using objects. so  
it expects two arguments

$c_3 = c_1 + c_2;$

function call

~~Complex~~

operator >> (istream & in, complex &c)

↳

3

expresion of benefit of using friend function (d)

for prefix & post fix:

void operator ++(int x) → post fix

1 {  
2     friend class op2; }  
3 }

void operator ++() → prefix

9  
3

## Overloading New and delete Operators

### Data Conversion:

#### 1. Conversion b/w Basic Data Types

weight → (float) age // typecast operator

#### 2. Conversion b/w Objects and Basic Types:

##### a. Conversion from Basic to User defined

Define a constructor and assign actual values  
by converting to object values.

##### Constructor (Basic type)

d) Steps for converting

1) Basic type to Object attributes

3

##### b) Conversion from UserDefined to Basic Type

##### operator BasicType()

e) Steps for converting

1) Object attributes to Basic type

- It doesn't specify any return value, but it returns the datatype into which we have to convert.

Ex:-

operator float ()

float lengthcms;

lengthcms = length \* 100;

return (lengthcms);

}

void main ()

{

length = M1;

}

Ex :- object from Basic:

metre ((~~float~~ float lcms))

length = lcms \* 100;

void main () {

M1 = lengthcms;

(or)

M1 (lengthcms);

}

3. Conversion b/w objects of two different classes.

class A object a;

class B object b;

object a = object b;

Conversion Routine in Source Object : Operator function

class classA

{

};

class classB

{

private:

public:

operator · classA()

{ (and half part) return }

};

Conversion Routine in Destination Object:

Constructor functions

class classA ( constructor )

private:

public:

class B ( classB & obj )

{ converting 'B' to 'A';

};

```
class classB
```

```
{
```

```
};
```

## Subscript Operator Overloading:-

All operators cannot be overloaded:

Category	operator
member access	.
Scope Resolution	:
conditional	?:
Pointer to member	*
size of Datatype	sizeof();
<u>Exception Handling</u>	

→ Synchronous Exception

exception which occur during the pgm execution due to some fault in the i/p data or technique that is not suitable to handle the current class of data.

→ Asynchronous :-

Caused by events or faults unrelated (external) to pgm & beyond the ctrl of the pgm. ex: Keyboard, disk failure

## Inheritance:

The technique of building new classes from the existing classes is called "Inheritance".

class A ↗

↗

class B: public A ↗  
↳ if private 'A' cannot access members of 'A'

↗

if protected 'A's' private members become private in 'B'.

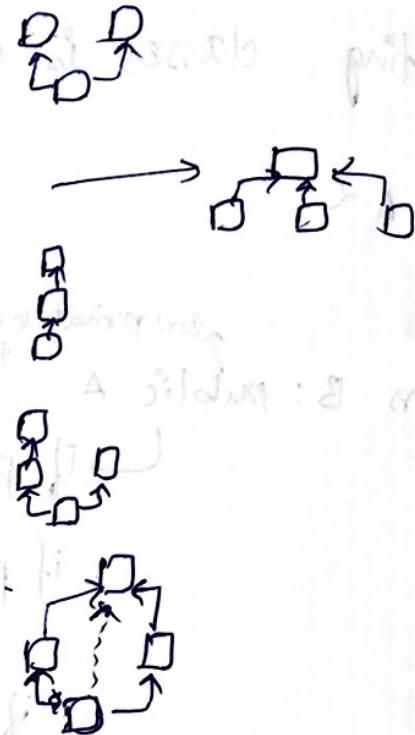
if public 'A's' functions or members can be accessed by 'B'

## Member Functions Accessibility:

Function type	Access directly to		
	Private	Protected	Public
class member	✓	✓	-
derived class member	✗	-	-
friend	✗	✓	✓
friend class member	✓	✓	✓

## Forms of Inheritance:

1. Single Inheritance
2. Multiple Inheritance
3. Hierarchical Inheritance
4. Multilevel Inheritance
5. Hybrid Inheritance
6. Multipath Inheritance



## Inheritance & member accessibility:

### Public Inheritance:

class D : public B

### Private Inheritance:

class D : private B

\* we cannot have constructor with arguments without defining the default constructor in C++

It shows error in above case

## Constructors in Derived classes:

1. No constructors in Derived & Base class.
2. Constructor only in B.C
3. C only in D.C
4. Const. in both B.C & D.C
5. ~~multiple~~ Consts in b.c & a single inherited D.C  
for every object of derived class,  
base class default constructor will be  
invoked
6. Const in B & D classes without default  
const in both!  
→ error
7. Explicit invocation in the absence of  
default const:  

```
class D : public B
{
    D(int a) : B(a) {}
}
```

8. Constructor in a multiple inherited class with default invocation:

class D : public B2, public B1

}      order of constructor call

first B2  
↓  
B1  
↓  
D

9. Const in multiple inherited class with explicit invocation:

class D : public B1, public B2  
  public:

D() : B2, B1()

10. Constructor in base & derived classes in multiple inheritance:

class D : public B1, virtual B2

};

B2  
  |  
  B1  
  ↓  
D

(virtual first)

## Const in multi-level Inheritance:

~~class A~~

A

↓  
B : A

↓  
C : B

↓  
D : C

## Destructors in Derived Classes:

Class A

↳ class B : public A

↳ class C : public B

A  
↓  
B

↓  
C

destructors

constructors

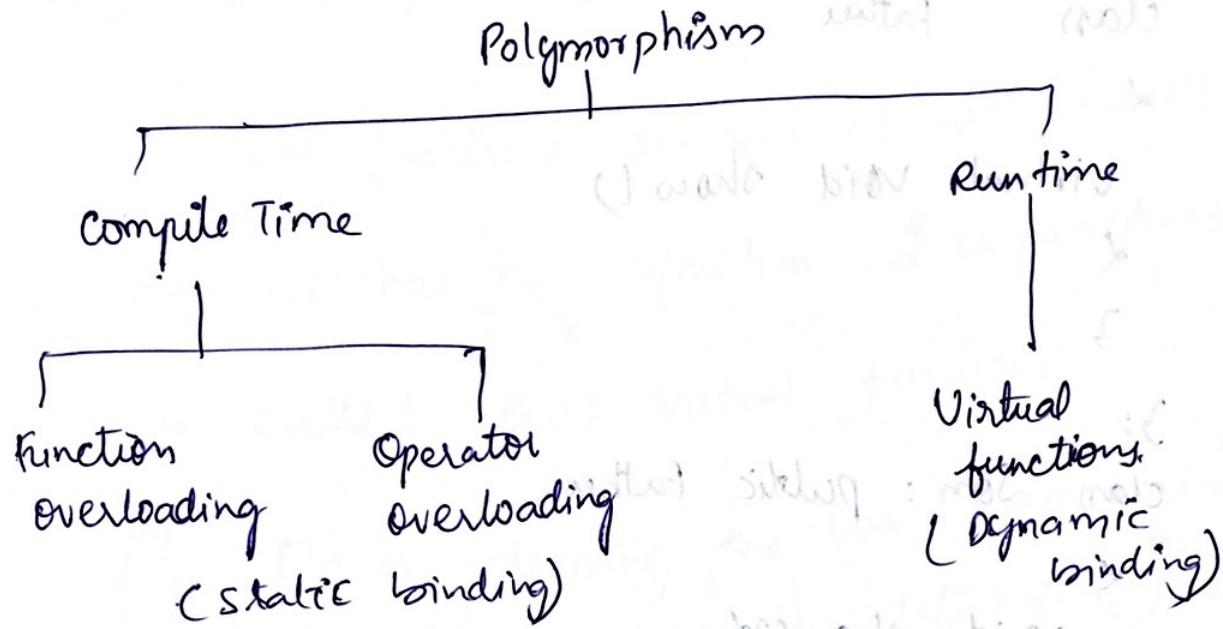
## Resolution of Ambiguity in multiple Inherited classes

:: (Scope Resolution Operator)

Obj. A :: func();

## Virtual functions :-

- \* Polymorphism means in biology, the ability of an organism to assume a variety of forms.
- \* In C++, it indicates the form of a member function that can be changed at runtime. Such functions are called "Virtual Functions" and corresponding class is called "Polymorphic class".
- \* The objects of the polymorphic class are addressed by pointers, change at runtime and respond differently for the same message.
- \* Such mechanism requires postponement of binding of function call to the member function until 'Run time'. So, 'late binding'



### Need for virtual functions:

→ When objects of different classes in a class hierarchy react to the same message in their own unique ways, they are said to exhibit polymorphic behavior.

- Resolving a function call at a compile time is known as "compile-time" (or) "early" binding.
- static " binding"
- Resolving a function call at run time is known as "run-time" (or) "late binding" (or) Dynamic Binding

1) class Father {

2

virtual void show()

3

4

};

class Son : public Father

5

void show()

6

int main()

Father \*fp;

fp = &f;

fp = &f;

f->show();

7 son s;

fp = &s;

fp->show();

8

## Pure Virtual functions

- \* Virtual functions are defined with a null body; it has no definition. Such functions are called pure virtual functions.
- \* Classes deriving the base class having pure virtual functions should define it again if it is virtual.
- \* Classes having pure v. func cannot be used to define any objects of its own. and those are called Abstract classes.

## Abstract classes:

→ Abstract classes (classes with atleast one virtual function) can be used as a framework upon which new classes can be built to provide new functionality.

Ex: Debugging process

## Virtual Destructors:

~~Virtual Constructor~~ → no. wait of base class  
Virtual Destructor → same as virtual function

## Dynamic Binding:

## Rules for Virtual func:

1. Virt-func def is compulsory in base class but not necessary for derived classes
2. cannot be static members
3. can be a friend func to another class
4. accessed using obj pointers
5. base → derived
6. prototype identical in both base & derived
7. cannot have virt const
8. benefit → public

## Templates (Generic Programming)

generic function for swapping

```
#include <iostream.h>
template <class T>
void swap (T&x, T&y) {
    T t;
    t = x;
    x = y;
    y = t;
```

Finding Maximum

```
template <class T>
```

```
T getMax (T x, T y)
```

```
{ if (x > y)
    return x;
else
    return b;
```

class Templates:-

Single inheritance - most popular

Multiple inheritance - complex

Abstract inheritance - needed

template < class T<sub>1</sub>, class T<sub>2</sub>, ... >

class CN

{  
    T<sub>1</sub> data;

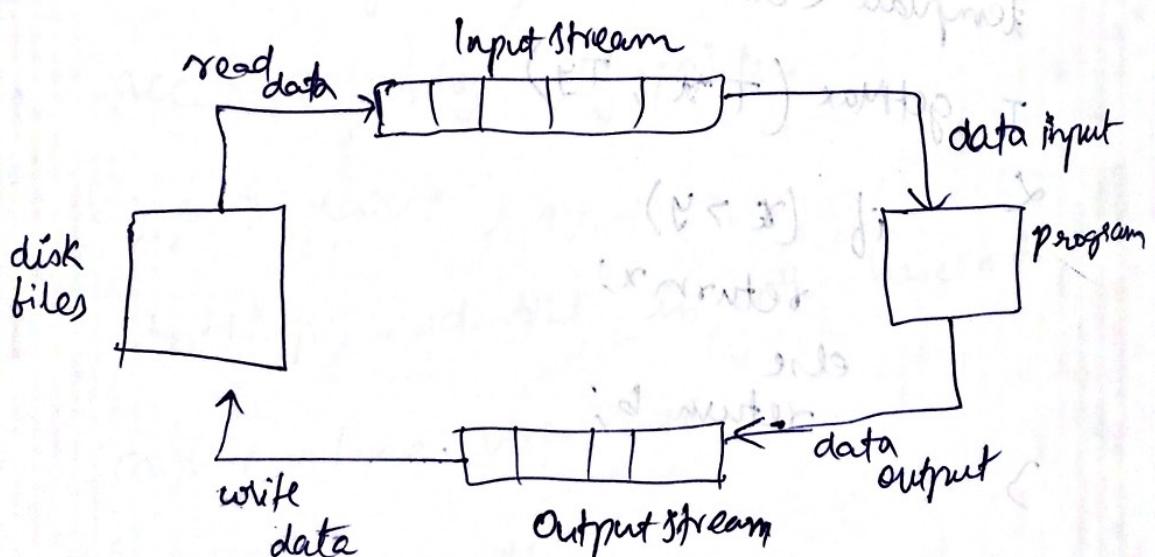
    void func1(T<sub>1</sub> a, T<sub>2</sub> b);

    T<sub>2</sub> func2(T<sub>2</sub> x, T<sub>2</sub> y);

} ;

## Stream Computation with files

file manipulation services such as create, open,  
write, read, rewind, close and delete



② ofstream - for handling o/p files

ifstream - for handling i/p files

fstream - for handling both i/p & o/p

void main()

of stream found ("student.out");

cin >> name;

fout << name;

}

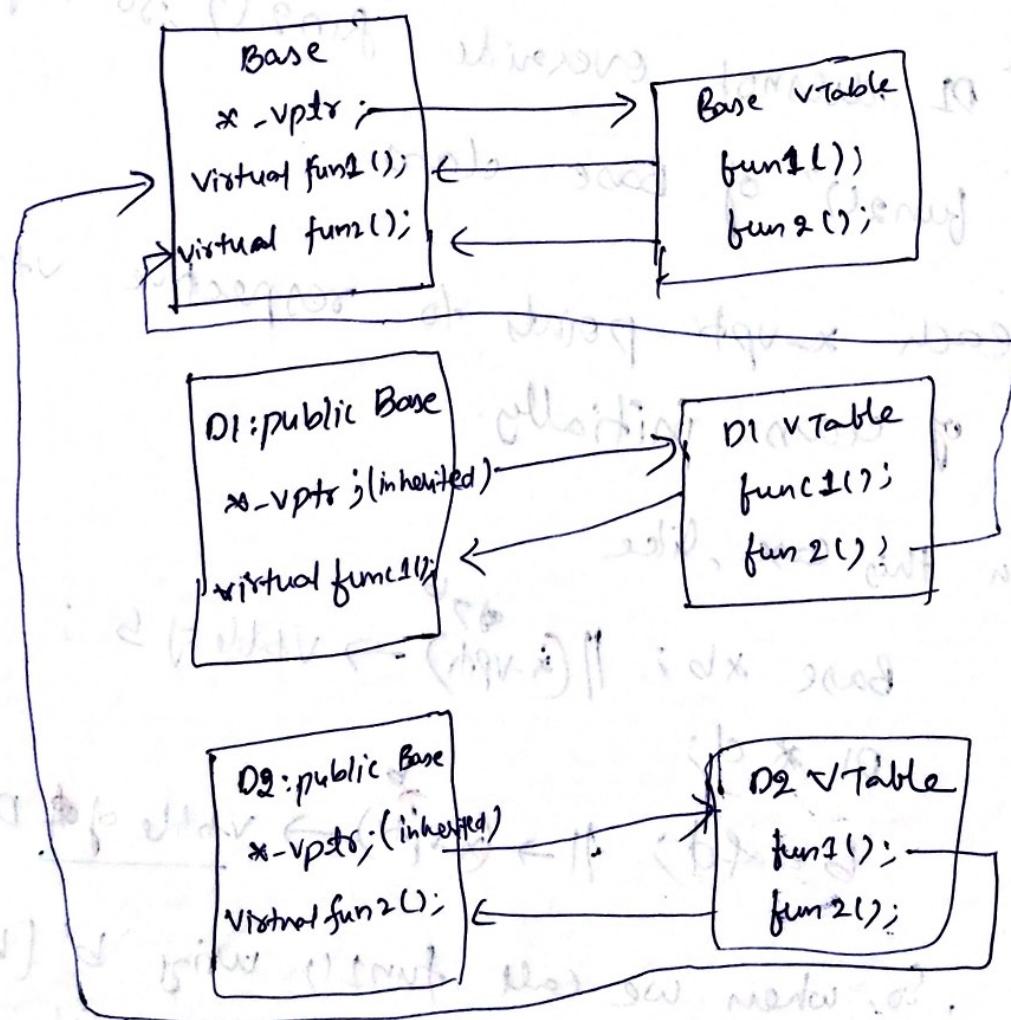
void main()

ifstream fin(" ");

fin >> name;

cout << name;

## Virtual Tables (VTables):



- \* "Virtual table" +  $\star\text{-vptr}$  are set-up at compile time by compiler for each class.
  - \* 'vtbl' consists of total no. of v-functions in the environment placed like static array, each element of ~~a~~ vtbl func.
  - \* On each virtual function in vtbl of each class maps to the most derived function of the class.
  - \* D1 does not override "fun2()", so it points to "fun2()" of Base class.
  - \* Each  $\star\text{-vptr}$  points to respective vtable of class initially.
  - \* In this case, like

Base  $x^b$ ;  $\prod (x - \sqrt{p_i x}) \rightarrow$  Ntable of  $S$ ;

D1 \* d;

$b = \&d$ ;  $\&1 \rightarrow (\text{char}^*) \rightarrow \underline{\text{vtable of } D}$

, so, when we call `fun2()` using '`b`' (`b>fun1`)  
it calls '`D::fun1()`'

# Operating Systems

An O.S. is a program that acts as an intermediary/interface between a user of a computer and the computer hardware.

## OS Functions

1. concurrency
2. virtual memory
3. multiprocessor support
4. file system
5. Security & Protection

features

- Abstraction: hide details of W/S
- Configuration
- Arbitration: manages access to shared resources

## Services provided by OS

1. Pgm creation
2. Pgm execution
3. access to file
4. System access

## Goals:

Primary - convenience  
secondary - efficiency

## types:

- Batch OS
- multiprogramming
- multi processing → many cores
- multitasking
- Real time → dead line

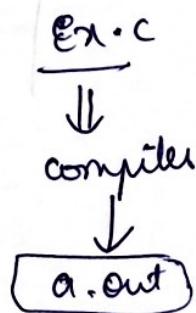
## Process Management

### Attributes of a Process:

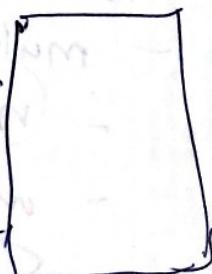
- PCB
- 1. Process id
  - 2. Program counter
  - 3. Process state (Ready, Running, waiting)
  - 4. Priority
  - 5. General purpose Registers (Register values which are preserved during pre-emption are stored in GPRs of PCB)
  - 6. List of open files
  - 7. List of open devices
  - 8. Protections



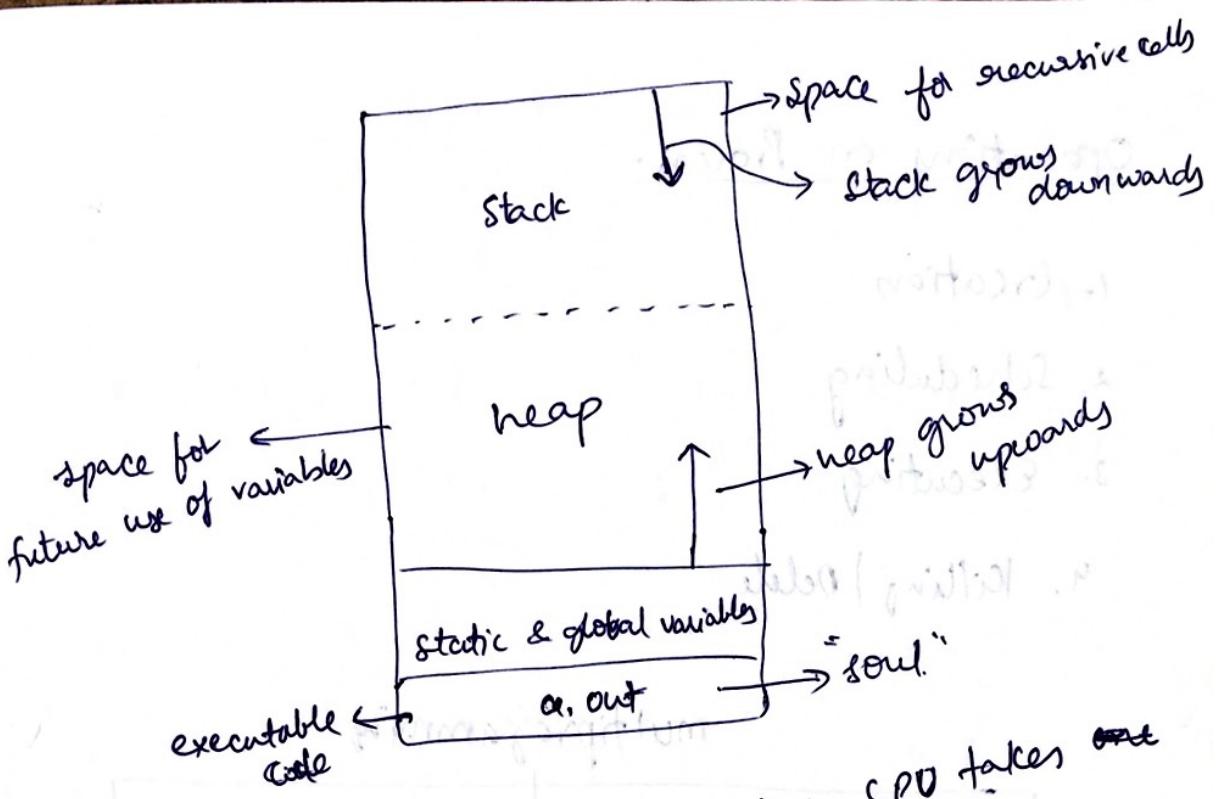
Process when we should start execution it creates a following structure



- All the attributes of a process are maintained in a PCB (Program control block)



PCB



- When a process is executed, the CPU takes one line by line and starts execution within its boundaries.
- The CPU should access only the process boundaries otherwise it generates "segmentation fault".

### States of a Process

1. New (secondary m)
2. Ready (main m)
3. Run (m m)
4. Block (or) wait (m m) (PC & every time about process will be deleted)
5. Termination (or) completion
6. Suspend Ready ( $m \rightarrow s$ )
6. Suspend wait (or) suspend block (from waiting to second m)

## Operations on Process:

1. Creation
  2. Scheduling
  3. Executing
  4. Killing | Delete

## multiprogramming

with pre-emption

(multi-tasking)

## Time sharing

→ Long Term scheduler ( $\text{new} \rightarrow \text{Gedy}$ )

→ short term Scheduler (Ready → Run)  
Dispatcher

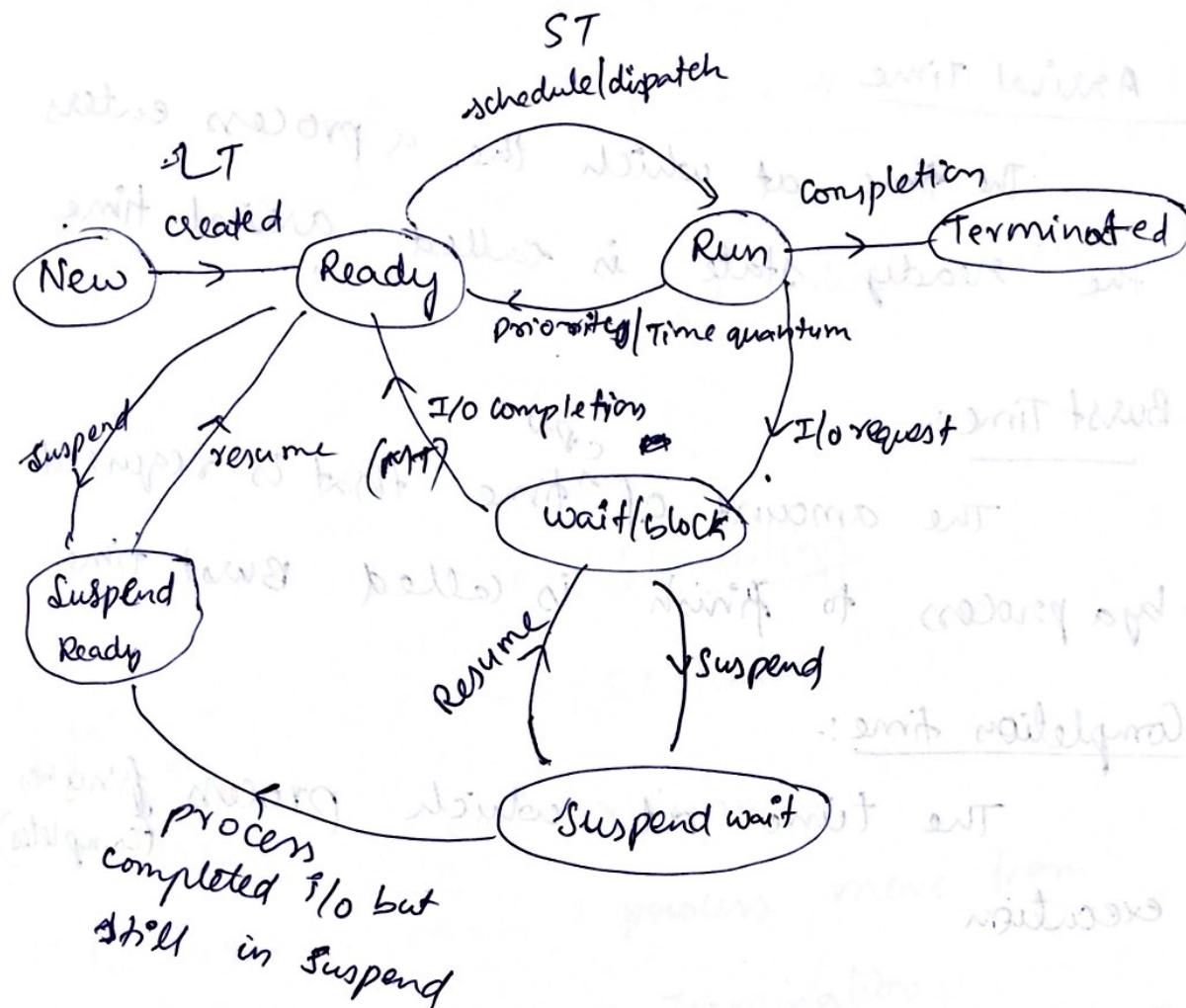
→ medium term Scheduler (wait  $\rightarrow$  ready)

Degree of Multi-programming:

→ The maximum no of processes that can be in Ready state is called P.O.M.P)

→ long term Schedule

# Process State Transition Diagram



→ CPU Bound → I/O Bound process new  
more CPU required more I/O required

- Q consider a system with 'N' CPU processors and 'm' processes then

	min	max
ready	0	M
running	0	N
block	0	M

## Important Parameters of Processes :-

### 1. Arrival Time

The time at which the process enters the ready state is called arrival time.

### 2. Burst Time

The amount of time required by a process to finish is called burst time.

### 3. Completion Time:

The time at which process finishes execution.

### 4. Turn Around Time:

The difference between completion time & arrival time is - turnaround time.

$$\text{TAT} = \text{B.T} + \text{W.T}$$
$$(\text{Completion time}) - (\text{Arrival time}) = \text{B.T} + \text{W.T}$$

TAT :

$$\Rightarrow \text{TAT} = \text{B.T} + \text{W.T}$$

## 5. Waiting Time :-

$$W.T = TAT - B.T$$

$$W.T = (C.T - A.T - B.T)$$

## 6. Response Time :-

The time at which a process first hits CPU

## CPU Scheduling

who  $\rightarrow$  short term scheduler

where  $\rightarrow$  ready  $\rightarrow$  running

when  $\rightarrow$  when a process move from

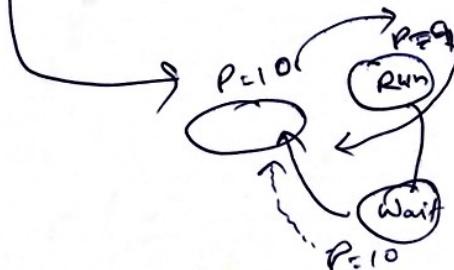
1. Run  $\rightarrow$  Termination

2. Run  $\rightarrow$  wait

3. Run  $\rightarrow$  Ready

2. New  $\rightarrow$  Ready i.e. when a process is just created (high priority)

3. wait  $\rightarrow$  Ready  
(when CPU idle, it takes from ready)



## FCFS (first come first serve)

Criteria : Arrival time  $T_A = T_0$   
mode  $\rightarrow$  non-pre-emptive

## Implementation of C++

- 1. Company :- In & Out's
    - clients
    - financial matters (share holdings)
- class StudentInfo, name, age, department:

class StudentInfo {

char name[20];

int age;

char dept[10]; int deptId;

public:

StudentInfo() {

name = " ";

age = 0.0;

dept = " ";

}

studentInfo ( ~~name~~, age, dept ) {

this.name = name;

this.age = age;

this.dept = dept;

}

void Input () {

cout << "

cin >> name;

cin >> age;

cin >> dept;

}

```

void display()
{
    cout << "Name : " << name;
    cout << "Age : " << age;
    cout << "Dept : " << dept;
}

};

class EmployeeInfo {
private protected:
    char name[20];
    char degn[10];
    char dept[10];
    char doj[10];
    int empId;
    int sal;

public:
    void Input()
    {
        cin >> name;
        cin >> degn;
        cin >> dept;
        cin >> doj;
        cin >> empId;
        cin >> sal;
    }

    void display()
    {
        cout << name << "\n" << degn << "\n" << dept
            << "\n" << doj << "\n" << empId << "\n" << sal;
    }
}

```

class TeachingStaff : public EmployeeInfo

d

private:

int no-of-classes;  
char free-hours [20];

class diagram  
(Architect)

SRS (UML)

SDS

High level  
design

Architecture

LLD.D

};

class NonTeachingStaff : public

EmployeeInfo

d private:

int

};  
public Department {

private:

char dept [20];

→ int dept-id;

int no-of-t-staff;

int no-of-stud;

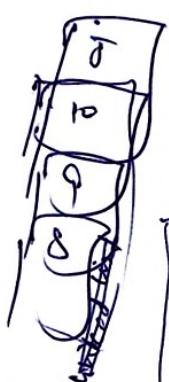
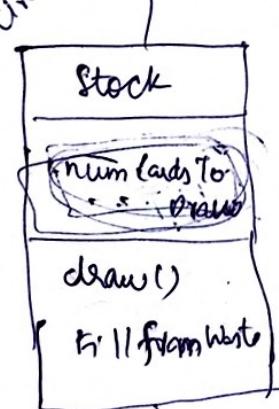
int no-of-non-t-staff;

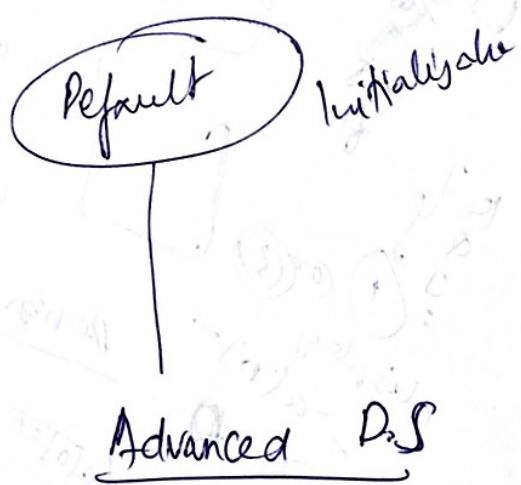
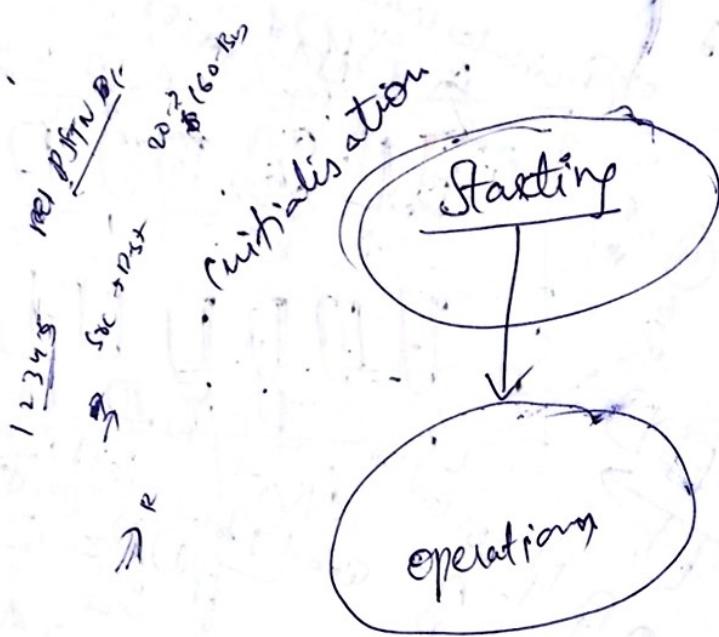
int

23 dec  
dec  
dec  
dec

};

Circular linked list





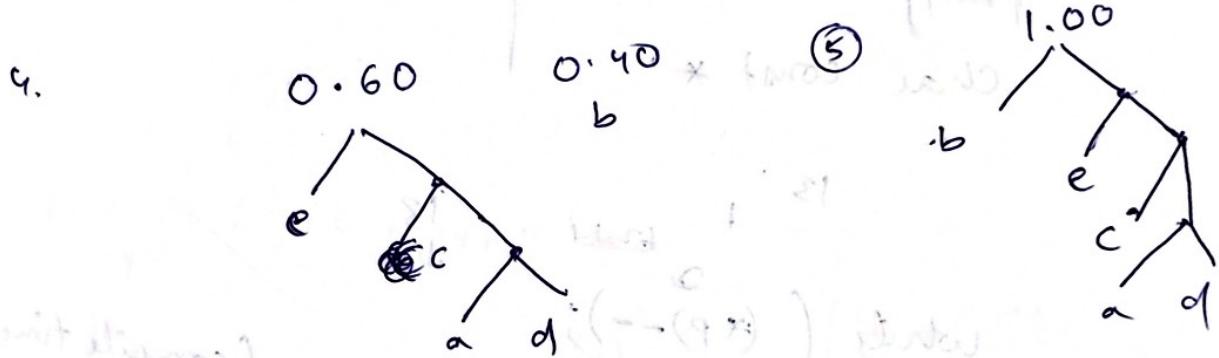
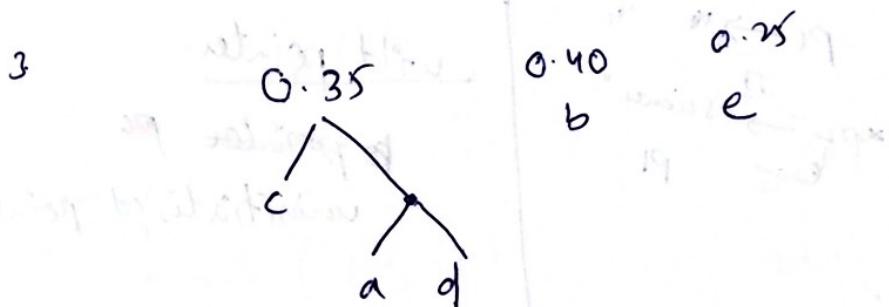
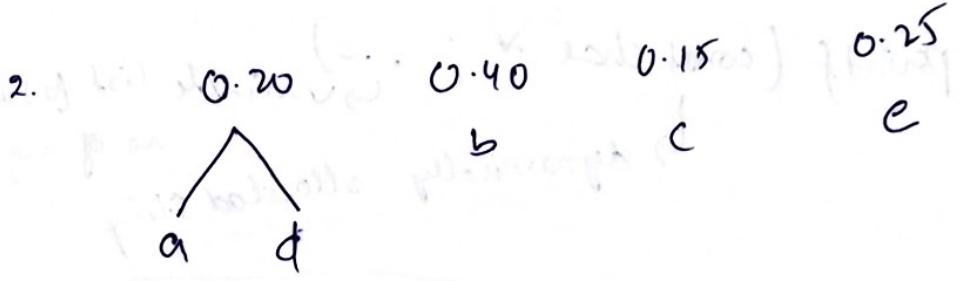
## 1. extended Binsley Tree

- 2. Quill tree
  - 3. left

## Huffman Coding

0.12      0.40      0.15      0.08      0.25  
a            b            c            d            e

- Take minimum value elements & merge them

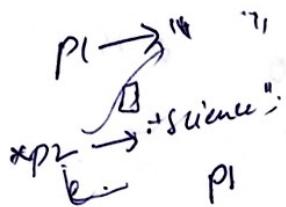


## Query Operations

1. Dynamic transitive closure graph (directed graph, G) Reachable(x, y)

16/7/15

printf (const char \* ...);  
variable list  
↳ dynamically allocated string  
no of args



wild pointer:

↳ pointer `p1`  
uninitialised pointer

printf

char const \*

while ((~~\*p~~)--);  
conditional statement error (compile time)

→ heap storage - static & ~~global~~ variables.

→ void main() { } ;

char \* str = "good";

char \* str2;

strcpy (str2, str);

printf ("%s", str2);

}

error: (for str2 no memory allocated)

hello ,

~~str[0, 1, 2]~~  
~~if (l == 0)~~

~~if~~  
permute ( str, 0, 2 )

b, bac,  
abc, acb, bac,  
bca, cda, cab

for ( i = l ; i < r ; i++ )

for ( i = 0 ; i < n ; i++ )

for ( j = i + 1 ; j < size ; j )

if ( arr[j] == arr[i] )

for ( k = j ; k < n ; k++ )

arr[k] = arr[k + 1];

y size --;

} else

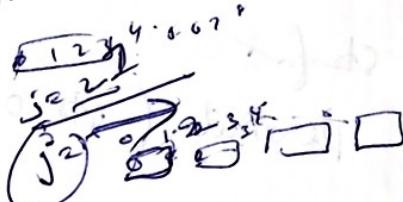
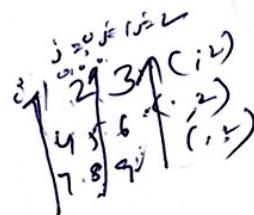
removes  
consecutive  
duplicates

Deshane

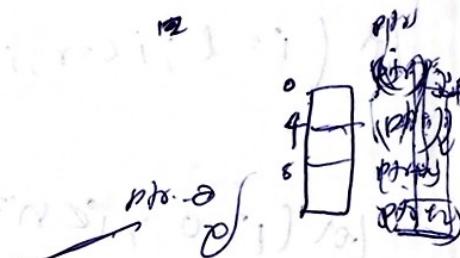
20 Aptitude      ~~20~~ 20 technical questions

MFC

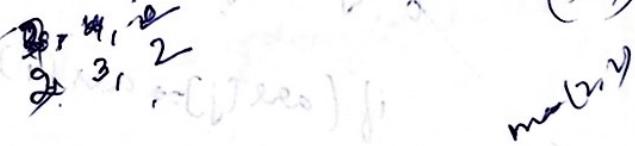
$a[0], a[1], a[2]$



$\max(1, 2)$

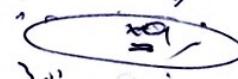


$\rightarrow (2, 2, 2)$



$\max^{\text{row}}$

Struct



16/7/15

Pointers

`int a;` → variable

`int *b;` → ptr

`int **c;` → ptr to a ptr

value in pointer is constant  
const char \*a; //  
 ↓  
 the address can be changed  
 and point to a diff address      char r = 't';  
 char \*a = &r;  
\*a = 't2'; → error

char \* const a;  
 ↓ Here address cannot be changed  
 but value pointing to can be changed  
 char r = 't';  
 char \*a = &r;  
 char r2 = 'x';  
 a = &r2 → error  
\*a = 'x2'; → ✓  
 → ~~key~~: infinite loop, for whatever may be  
 the input:

```

char ch = 'A';
while(ch)
  ch = getch();
}
  
```

$a = 20$

$\&a =$

$\rightarrow \text{int } T;$

main() {

struct T {

char c; }

printf("%d", sizeof(T));

}

	C	C++
sizeof(i)	2	1
sizeof(i=7)	2	2
sizeof(a)	2	1

Output

c	C++
2	(If considers 'T' as an independent data type)
1	(It does not consider 'i' as an independent data type & takes value of int T)

1

Insert into table ( col<sub>1</sub>, col<sub>2</sub>, ... col<sub>n</sub> ) select  
~~from table~~ ~~order by~~ ~~group by~~

( , , , , ) from ~~table~~ table where

col = " ";



Create Object ( <sup>SAPI. SpVoice</sup> )

or speak & Name, VIT

.Vbs

17/7/15

struct employee

{ int empid;

char name(20)

float salary;

union employee

int empid;

char name(20);

float salary;

3/4/15;

3/4/15;

e1 = 13 ( $\Rightarrow$  first member will be assigned with value)

Memory Allocation

malloc();

alloc();

realloc();

free();

## Storage classes in 'c'

Register

Static

Auto

extern

2 Choose collection

i) short const register  $i = 10;$

ii) static volatile const int  $i = 10;$

iii) unsigned auto long register  $i = 10;$

iv) signed extern float  $i = 10.0;$

3  $\text{sizeof}(3.14)$  -  $\text{sizeof}(3.14f), \text{sizeof}(3.14e);$

$\frac{1}{4}$  -  $10$

6' main()

int i = -1, j = -1, k = 0, l = 2, m;

$m = i++ + j++ + k++ + l++;$

~~printf~~ cout << i << j << k << m;

3  $i = 0 ; k = 1$   
 $j = 0 ; l = 3 \quad \therefore m = 1$

7

$$\begin{array}{r} 0600\ 0000\ 0000\ 0001 - 1 \\ 1111\ 1111\ 1111\ 1110 \\ \hline & & & 1 + 1 \end{array}$$

-1

$$\begin{array}{r} 1111\ 1111\ 1111\ 1111 \\ 1111\ 1111\ 1111\ 0000 \end{array}$$

-1cc4

FIFO wait

8)

if(a)

10

else  
break; → "break" cannot be placed in  
if else

⑨

a = 2

a = na + 2

ascii value  
a = 97

⑩

'n' → ascii value  
10

⑪

P = 1

q = 8

i = 2

13

15



i = 1

+ P = 2

x q = 8

1111  
1110  
1000

1111  
1110  
1000

13  
Date \_\_\_\_\_  
returns length of string  
printf("%s");

dersana.jayashankar@faceacademy.in.

## Time Complexity

### ④ Asymptotic Notations

only care consider the no of loops running on

## Database

DDL - autosave

DML - Commit to save

TCL - Rollback

- Commit  
- Savepoint

DCL - grant, Revocate

## DQL

Select first\_name

Select upper(first\_name)

22/7/15

# Database Systems

Data - Fact recorded  
e.g. Text, images, numbers, video, speech

Database - Collection of related data

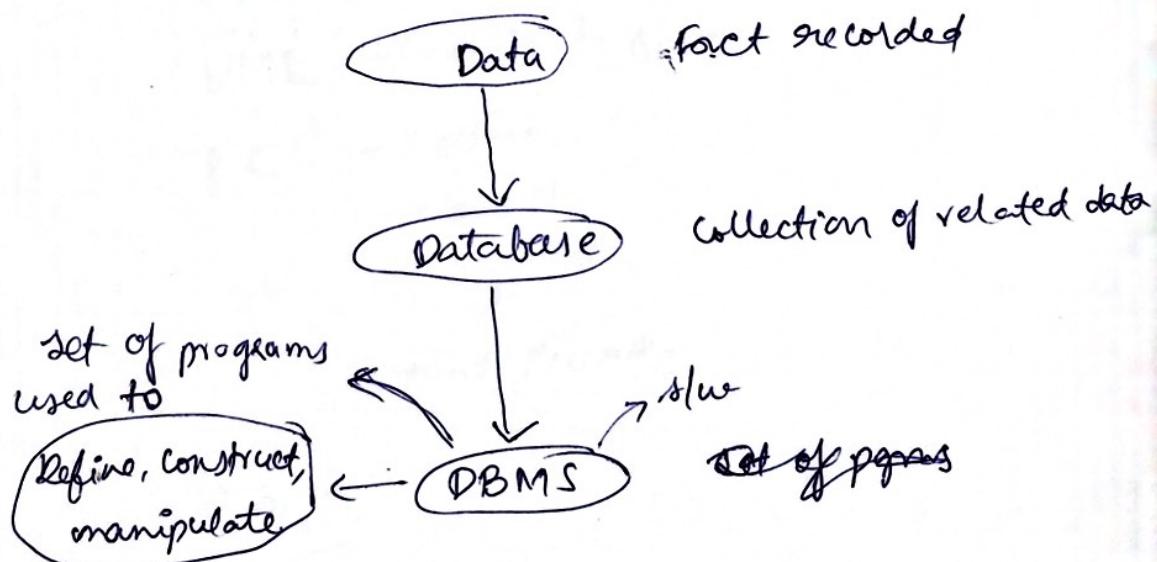
(Text & number) → Traditional database

(video & audios) → Multimedia DB

(geographical Img., videos) → Geographical Info System

(stocks, alert when out of stock) → Realtime DB

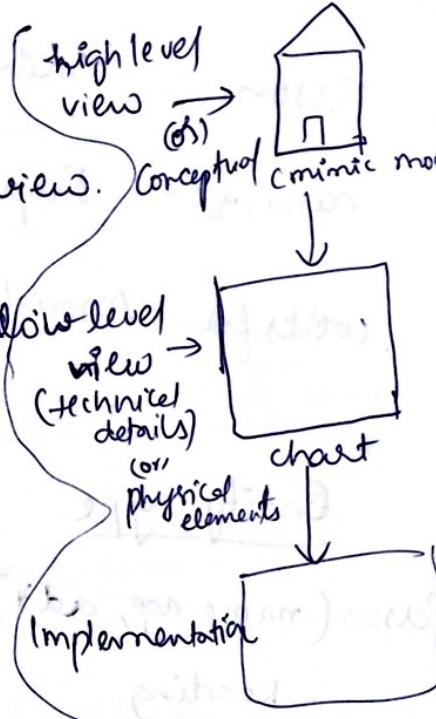
(historical DB) → Data warehouse



(Database + DBMS) → Database Systems  
ex: Book, Pen

\* Naïve Users cannot understand low level view (or) technical view. Conceptual (minic model)

so high level design is made.



## DB Design

### 1) High Level (or) Conceptual

E-R modelling

### 2) Representational

relations (tables)

### 3) Low level (or) Physical Data elements:

Implementation

Accessing

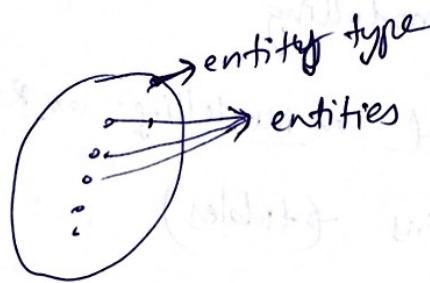
## E-R Model

- entity (Noun) → Any object in db
- Attributes → (verbs describing entities) ↳ properties of entities.
- Relationship (Verb) → Describe the relationship b/w entities

Person - Thing - Entity - Noun  
 name, age - Properties Attributes - verb  
 works for Association Relationship - verb

### Entity Type

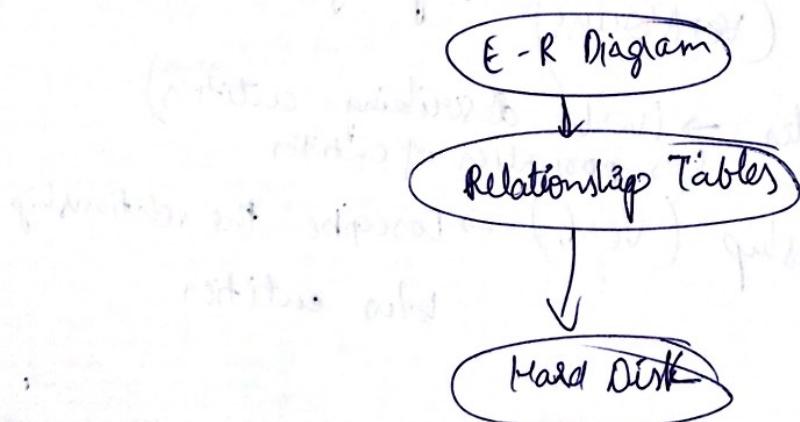
Person (name, age, add) — Entity  
 - Heading — (Rajiv, 26, Hyd.)  
 - Intention — instance of entity type  
 - — extension



→ At any instance the no of elements (v) all elements in an entity type is called "State of Entity"

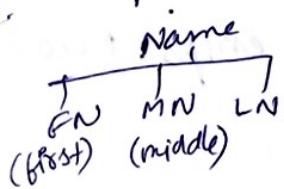
Why for

Relationship Type — Relations



## Attributes

Composite vs Simple Attributes



↓  
First Name

2. single valued

↓  
age (only one)

vs Multi Valued attributes

Ph. no , Add

↓  
more than  
one ph. no's

3. stored vs Derived attributes

↓  
~~dob~~

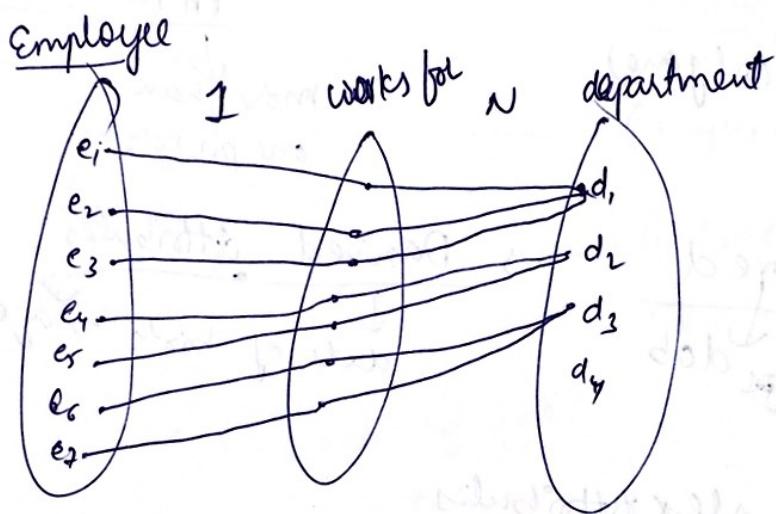
↓  
date of birth  $\Rightarrow$  age

4. Complex Attributes

composite + Multi-valued

## Relationships

~~Reg:~~ Every emp works for exactly a department and a dept can have many emps: New d<sub>4</sub> need not have any emp.



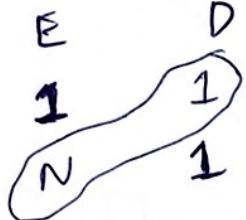
Degree: No. of entities participating in a relationship  
 ex: In above ex: degree: 2 (emp, dept)

Cardinality Ratio:  
 max. no. of relations, an entity can participate  
 Ex:- employee : 1  
 dept : N

Participation (or) Existence:

min no. of relationships an entity can participate

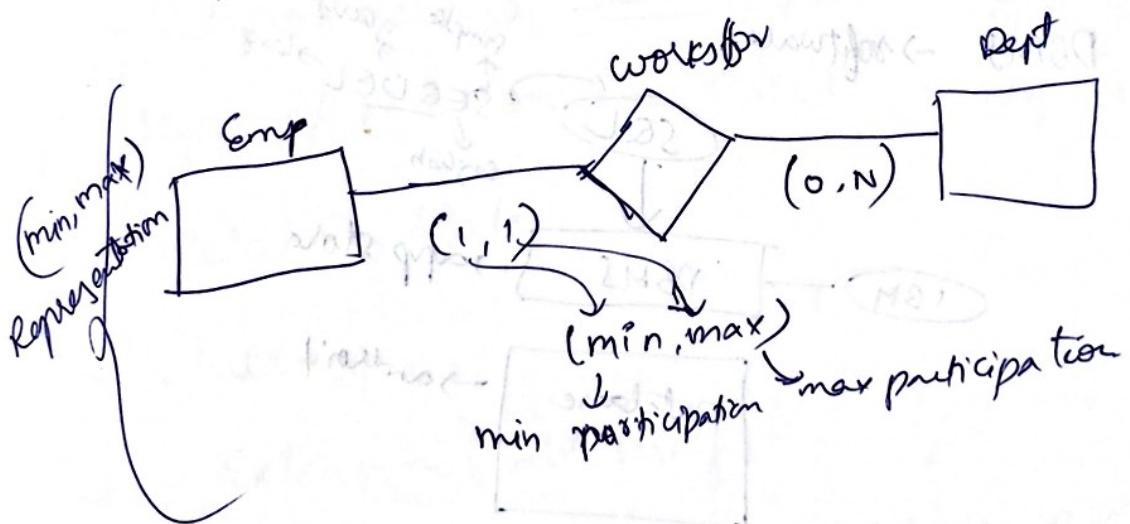
Ex:- emp: 1  
 dept: 0



$N:1$

→ Partial participation  
→ total participation

if all entities are participating in relation  
then, it is total participation

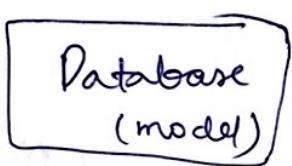
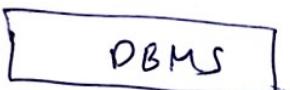


## Relational Model

Conc. L

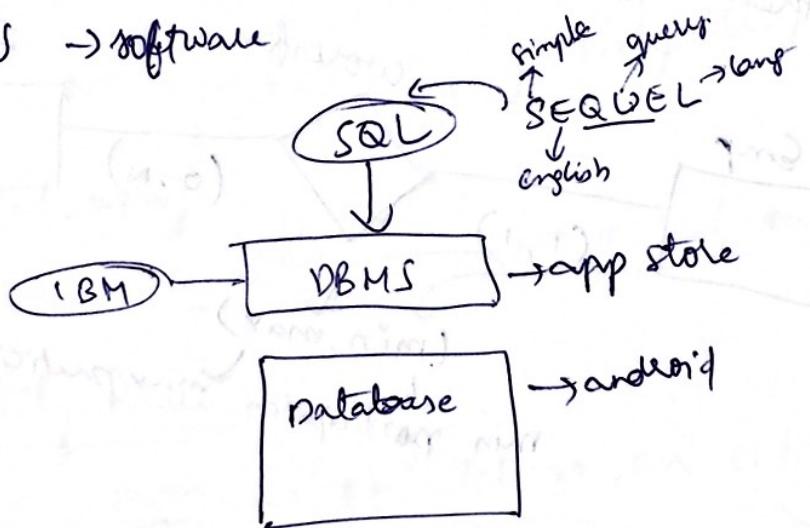
Rep. L

low level



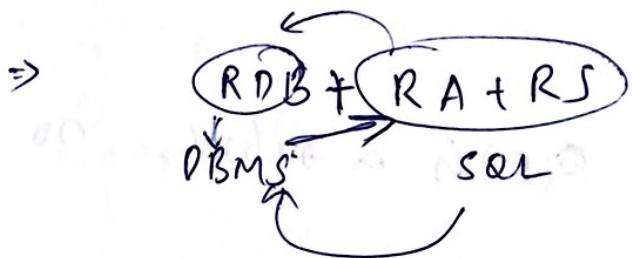
## Relational model - Database model

DBMS → software



↳ hierarchical, Network databases  
↳ legacies

Relational calculus + Relational DB + Relational algebra



## Terminology

Relation

- Table

tuple

- row

attribute

- column

domain

- {set of values}

Relation Schema

→ heading of table  $\Rightarrow R(A_1, A_2, A_3, A_4)$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 $D_1, D_2, D_3, D_4$   
 set of values

degree of Relation

Relation State

intension

extension (Table itself)

Current Relation State  $\Rightarrow$  no. of tuples present in table at that pt of time

$R(A_1, A_2, A_3, A_4)$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 $D_1, D_2, D_3, D_4$

table  
table name

$\delta(R) \subseteq D_1 \times D_2 \times D_3 \times D_4$

— (ordered pair combining one value from all of the domains)

In mathematics, any subset of a cross product  
is relation.

$\tau(R) \subseteq (\subseteq)$  is a subset, so  $\tau(R)$   
 $\downarrow$  table 'R' (table) is

called relation.

→ maximum no. of tuples,

$$\tau(R) \subseteq |D_1| \times |D_2| \times |D_3| \times |D_4|$$

but all possibilities  $\stackrel{10^5}{=} e_{\max}$  may not be meaningful  
like, a student might not have all  
possible ph.no's

### Tuple, Tuple Values & Null

Relation = Set



- \* A set cannot have two same values,
- ⇒ A relation cannot have all the values  
in tuple same.  
↳ too different

## Exceptions

RN, MN, LN

↓  
not applicable

⇒ NULL

not present  
shows ~~street~~ ⇒ NULL

## Relational Constraints :-

→ 1 values range

1. Domain constraints

2. Key constraints → uniqueness

3. Entity integrity constraints

4. Referential integrity constraints.

### 1) Domain

Atomic

↳ smallest individual unit

- flat file system

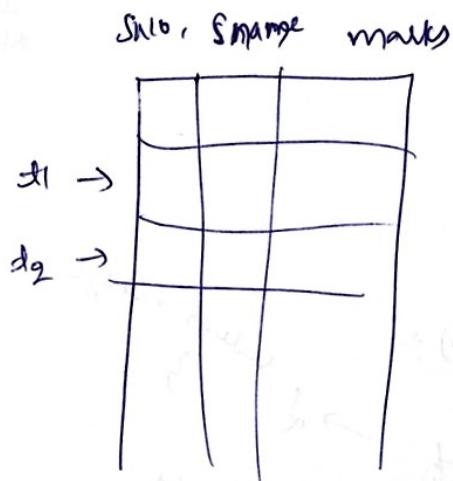
only atomic

- composite  
multivalued

⇒ multivalued → new relation

composite → break

## Q) Key Constraints



No two tuples in a relation will have all the values in tuples same.

$$t_1 \neq t_2$$

Super key :-

the set of attributes in which no two tuples will have all the attributes same

super key

Sno, Sname, Marks

Super key  $\subseteq$  Attributes

R.D.B

Key = minimal Superkey

Ex. for key having two attributes

Name	Age	Door no	Street no

(Name, dno, sno)  
Super key

default key  $\Rightarrow$  (set of all attributes)  
 $\Downarrow$   
 (super key)

Any superset of a key is a Super Key

(Sno, Sname)  $\rightarrow$  Super Key

$\rightarrow$  ~~A~~  $\rightarrow$  key  
 $R(A_1, A_2, A_3, A_4)$

for  $A_1$ ; no of superkeys

$A_1, A_2, A_3, A_4$   
 $2 \times 2 \times 2$

$2^3 = 8$  S.K's

→ More than one key in a table

Ex - ①

owner	sim no	IMEI-no

② Car

Owner name	color	Reg.no	engine.no

Candidate keys { Keys of table }

Primary key of one of candidate keys

$A_1, A_2, A_3, A_4$   
 $\times$   
 $A_2, A_3, A_4$   
 $\times$   
 $A_3, A_4$

$\rightarrow$  Super Key (uniquely identifies)

- S.K

- S.K (If I remove  $A_3$   
 If we don't &  
 cannot uniquely identify, it is K)

Either candidate key 1 or candidate key 2 can  
be primary key

Entity Integrity

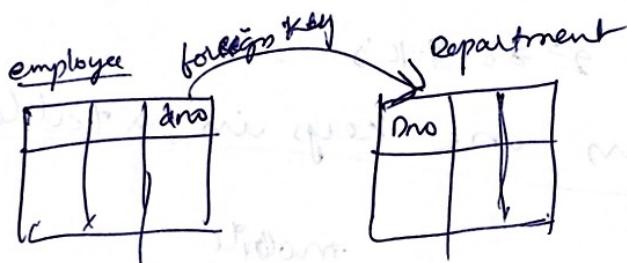
Referential Integrity

} constraint

→ According to entity integrity  
P. Key cannot be null

Referential I.C

↳ foreign key cannot be null



~~fact~~  
f K can be null  
↳ can be duplicate

↳ more than one is allowed

Semantic

↳ rules

Ex:- emp sal < 1,00,000

## Actions upon constraint violations

- i) insert
- ii) Delete
- iii) Update

	insert	delete	
Domain . c	✓	*	
Key . c	✓	✗	
Entity . c	✓		
Referential . c		✓ (f, k, r, k)	
action	rejection		

PK null

### Three Actions

dept	d-name
1	abc
2	def
3	ghi

3-actions

d-no
1
2
3

① Rejection

(cascade delete  
(delete all tuples in  
table referring to particular  
id))

Ex:- emp-dependents of  
emp-id

dept-id	emp-id
1	1
1	2

dept-id	emp-id
1	1
1	2

Set NULL

Set NULL  
for the  
particular  
value.

dept-id &  
employees

Modify ? delete + insert

## Normalisation

1)

~~Consider~~,

emp	eid	e-n	did

dept		
did	d-name	s-id

all tables in a universal table

eid	e-n	did	d-name	supervisor-id

Problems in universal table;

1) Redundancy

2) Anomalies

- Insertion

In universal table, at one place,

did	a	d-name
		CSE

another place

did.	a	d-name
		ECE

while inserting we may go wrong,

and creates erroneous data, this cause  
insertion anomalies

## Deletion Anomalies:

Ex:- If you want to delete all emp of dept-no '1'. you should delete emp-details in V-table & replace null values  $\oplus 1$    
delete all tuples, where you cannot have dept info of department itself.

## 2) Update (Modify):-

$\rightarrow$  if you want to change dept-name entire V-table you have to change

Procedure of Dividing Tables into ~~some~~  
according to rules is called

## 2) Normalisation

$\rightarrow$  we use Functional Dependencies and

Candidate keys for Normalisation.

## Functional Dependencies

table T

If key is given in a table, then we can extract the remaining attributes in the respective tuple

A	B	C
1		
2	a	b
3		
2	a	b

Ex:-

~~as given~~

$\rightarrow A$  determines  $(B, C)$   
 $A \rightarrow (B, C)$   $(B, C)$  functionally  
 $(2) \rightarrow (a, b)$   $(a, b)$  dependent on A

Def:-

$t_1(A) = t_2(A)$

then  $t_1(B, C) = t_2(B, C)$

\* If there are lots of repetitions in table, & few attributes which are functionally dependent, then replace the attributes with a new table

Ex:-

A	B	C
a	1	d
a	1	e
a	1	f
a	1	g
a	1	h
b	2	f
b	2	d

A	C
a	d
a	e
a	f
a	g
a	h
b	c
b	d

A	B
1	
2	

By this, we eliminate the redundancy in attributes (table).

$$A \rightarrow B$$

(A determines B)

(B functionally dependent on A)

(BCNF)

+  $\rightarrow$  ~~(A, B)~~

A, B = collection of attributes

\*  $X \rightarrow Y$  (functional dependency)  
3 types

Non-Trivial

$$X \cap Y = \emptyset$$

$$A \rightarrow B$$

$$A \rightarrow BC$$

$$AB \rightarrow CD$$

Semi-trivial  
Trivial

$$X \cap Y \neq \emptyset$$

$$AB \rightarrow BC$$

Trivial

$$A \rightarrow A$$

$$AB \rightarrow A$$

$$X \supseteq Y$$

Rule out the functional dependencies based on the tables:

(may be)  
~~e-id~~  $\rightarrow$  e-name

~~e-name~~  $\rightarrow$  e-id

Eid	Name
1	a
2	b
3	b

	A	B	C
$x A \rightarrow B$	1	1	4
$x B \rightarrow C$	1	2	4
$x B \rightarrow A$	2	1	3
$x C \rightarrow B$	2	2	3
$\cancel{x} C \rightarrow A$	2	4	3
$\checkmark A \rightarrow C$ (may be)			

### Formal Definition:

	A	B
$t_1$		
$t_2$		

if  $t_1, t_2$  agree then they must agree here  
here

if  $t_1 \neq t_2$  they may agree or  
disagree here

### Various Usages of FD's

1) Identifying additional FD's  
(extra) two rules

2) Identifying Keys

3) Identifying equivalences of FD's

4) Finding minimal FD set

$$\begin{array}{l} A \rightarrow BC \\ \text{or} \\ A \rightarrow B \\ A \rightarrow C \end{array}$$

operations of ~~DB~~'s DB using FD's

two methods

- (i) Inference Rules      ~~error prone~~  
ii) Closure set of attributes - easy

Inference Rules:

- a) Reflexive :  $A \rightarrow B$  if  $B \subseteq A$   
b) Transitive :  $A \rightarrow B$  and  $B \rightarrow C$  then  $A \rightarrow C$   
c) Decomposition :  $A \rightarrow BC$  then  $A \rightarrow B$  &  $A \rightarrow C$   
d) Augmentation : if  $A \rightarrow B$  then  $A \cup C \rightarrow BC$   
e) Union : if  $A \rightarrow B$  &  $A \rightarrow C$  then  $A \rightarrow BC$   
f) Composition rule : if  $A \rightarrow B$  &  $C \rightarrow D$  then  $AC \rightarrow BD$

Closure set of Attributes

func. Dependencies:

- $$\begin{aligned} A &\rightarrow B \\ B &\rightarrow D \\ C &\rightarrow DE \\ CD &\rightarrow AB \end{aligned}$$

Closure Set:

It contains all the attributes which can be derived from the given attribute.

Ex:-

$$FD's: A \rightarrow B$$

$$B \rightarrow D$$

$$C \rightarrow DE$$

$$CD \rightarrow AB$$

$$A^+ = \{B, D, A\} ; \quad B^+ = \{B, D\}$$

$$C^+ = \{E, D, E, A, B\} ; \quad D^+ = \{D\}$$

$$E^+ = \{E\} ; \quad (CD)^+ = \{A, B, C, D, E\}$$

### Determining Candidate Keys

If  $R(AB)$  then, no of candidate keys possible

$$= \{A, B, AB\}$$

$$R(ABC)$$

then,  $\{A, B, C, AB, BC, AC, ABC\}$

$\Rightarrow (2^n - 1)$  candidate keys

Ex:-  $R(A B C D)$

$$A \rightarrow B$$

$$B \rightarrow C$$

$$C \rightarrow D$$

$$D \rightarrow A$$

$\Rightarrow 2^4 - 1 = 15$  cand. keys may be possible

if 'A' is candidate key  
then key containing 'A'  
is 'super key'

and key of length '4' -  $(A B C D)$

length '3' -  $(A B C) (B C D) (C D A) (A B D)$

length '2' -  $(A B) (B C) (C D) (D A) (A C) (B D)$

length '1' -  $(A) (B) (C) (D)$ . } candidate key

Super Keys

$$A^+ = \{A, B, C, D\}$$

$$B^+ = \{B, C, D\}$$

$$C^+ = \{A, B, D\}$$

$$D^+ = \{A, B, C\}$$

Equivalence of FD's

$$F: dA \rightarrow c, AC \rightarrow D, E \rightarrow AD, E \rightarrow H \}$$

$$G: dA \rightarrow CD, E \rightarrow AH \}$$

$\rightarrow F$  covering  $G$

check i)  $F \supseteq G$   
and ii)  $G \supseteq F$

$$\Rightarrow F \supseteq G$$

$$A^+ = \{C, D, A\}$$

$$\Rightarrow F \supseteq G$$

$$E^+ = \{A, D, H\}$$

ii)  $G \geq F$

$$A^* \sim A \underline{CD}$$

$$E^* = \{A, H, S\}$$

$\Rightarrow \underline{G \geq F \text{ true}}$

$\Rightarrow$  both are equivalent

### Lossless Decomposition

$\rightarrow$  ~~or~~ Normalisation mostly implies dividing a large table into small ones

$\rightarrow$  If we again combine these small tables, we should not get any additional data.

$\rightarrow$  we have to take care while splitting the table.

A	B	C
a <sub>1</sub>	b <sub>1</sub>	c <sub>1</sub>
a <sub>2</sub>	b <sub>1</sub>	c <sub>1</sub>
a <sub>1</sub>	b <sub>2</sub>	c <sub>2</sub>

↓

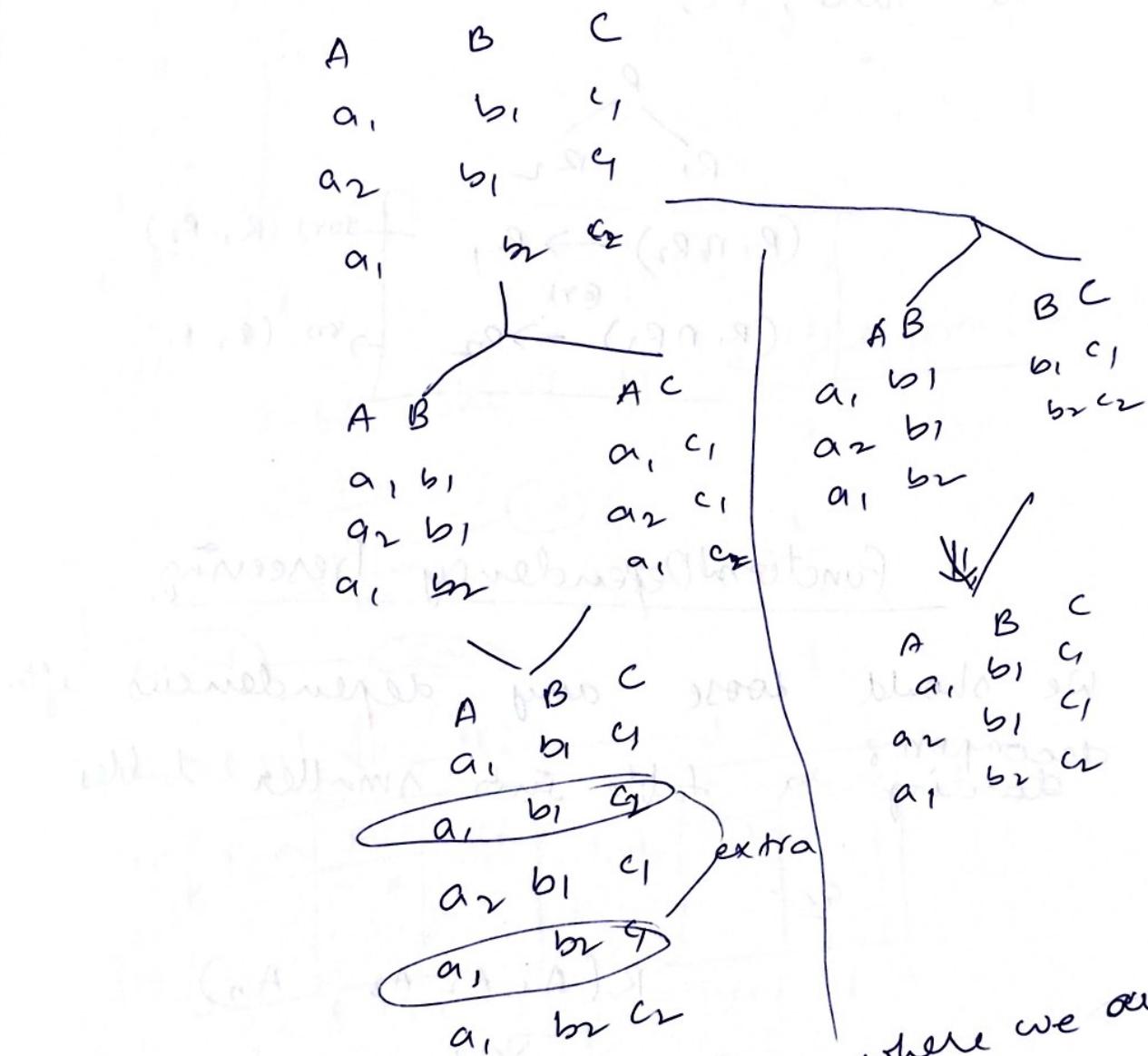
A	B	C
a <sub>1</sub>	b <sub>1</sub>	c <sub>1</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>2</sub>

↓

a <sub>1</sub> , b <sub>1</sub> , c <sub>1</sub>
a <sub>1</sub> , b <sub>2</sub> , c <sub>2</sub>
a <sub>2</sub> , b <sub>1</sub> , c <sub>1</sub>

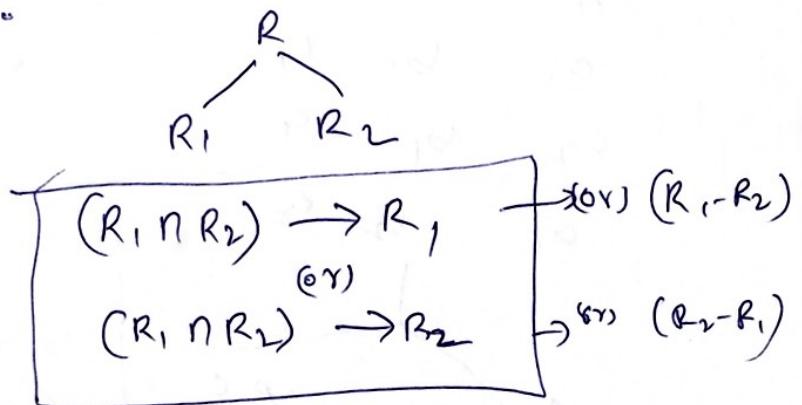
(a<sub>2</sub>, b<sub>2</sub>, c<sub>2</sub>)  $\rightarrow$  extra

→ when we are dividing, we should take care that some attributes of tables should be common.



→ This type of decomposition, where we are gaining additional data which is not real is "Lossy Decomposition"

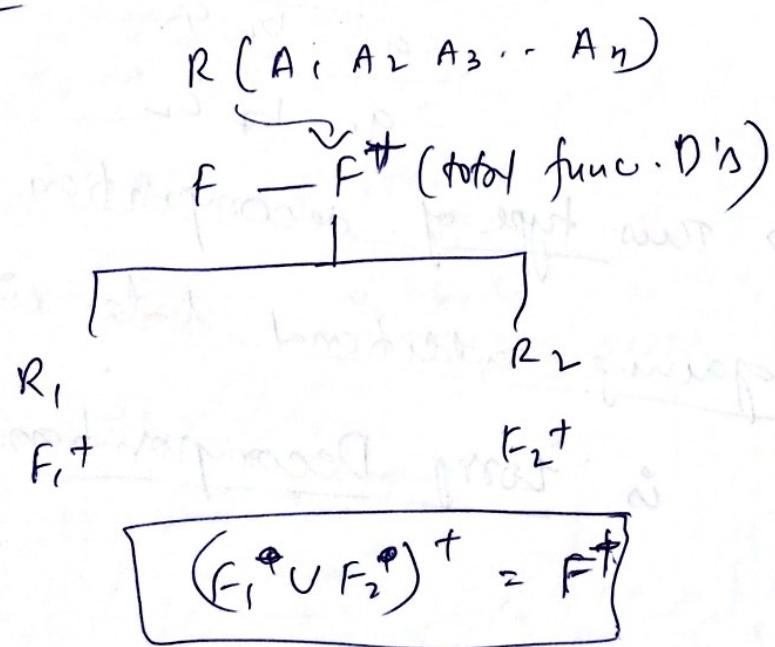
→ The Decomposition will not be lossy if the common attribute is a key in any one of the table, i.e.,



### Functional Dependency Preserving

We should loose any dependencies after decomposing ~~dividing~~ a table into smaller tables

e.g.



## First Normal Form:

Aim :- BCNF (0% Redundancy)

1NF

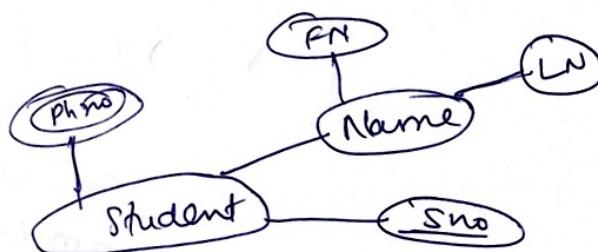
2NF

3NF

BCNF

1NF :-

The table should be in flat form (hierarchy)



↓

S-no	FN	LN

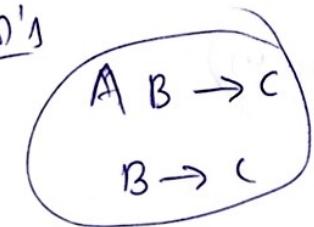
S-no	Ph-no

→ By default

(No multivalued, No composite)  
Attributes

## Second Normal Form:-

FD's



$$\Rightarrow A^+ = \{A\}$$

$$B^+ = \{B, C\}$$

$$C^+ = \{C\}$$

$$(AB)^+ = \{A, B, C\} \Rightarrow (AB) \text{ unique}$$

$$(BC)^+ = \{B, C\}$$

$$(CA)^+ = \{C, A\}$$

A	B	C
1	a	$C_1$
2	a	$C_1$
1	b	$C_2$
2	b	$C_2$
3	c	$C_3$
2	c	$C_3$
3	c	$C_3$
4	c	$C_3$
5	c	$C_3$

Can be avoided

→ 2 NF is based on full functional dependency

No partial dependency is allowed

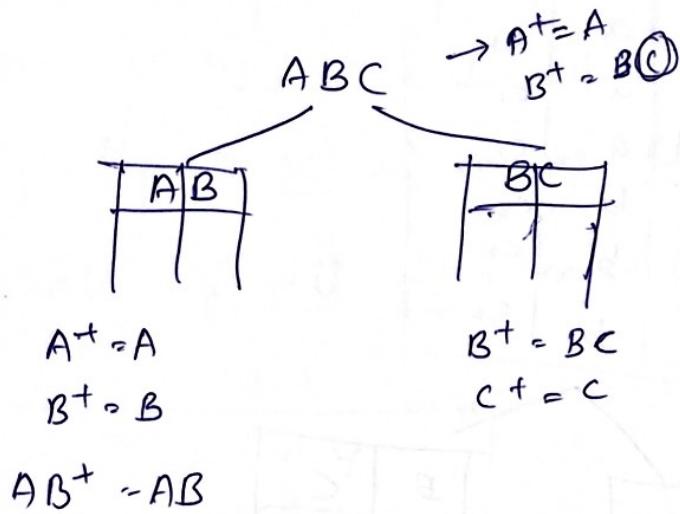
~~prime attribute part of cand-key~~

→ if ~~(AB)~~ Cand. key contains more than one attribute, then part of it or no single attribute in Cand. key should not determine anything

Ex:-  $(A, B) \rightarrow C$   $\rightarrow$  Cand. key

$B \rightarrow C$   $\rightarrow$  not allowed

→ So, Remove part of attribute which is determining and place it separately



3NF :-

No transitive Dependencies

Transitive dependency:-

Non-prime attributes transitively depending on the key

Prime Attribute:-

Part of candidate-key

$$A \rightarrow B, B \rightarrow C \Rightarrow A \rightarrow C$$

$$R(A|BC) \rightarrow A^+ = ABC$$

$$B^+ = BC$$

$$C^+ = C$$

$$A \rightarrow B$$

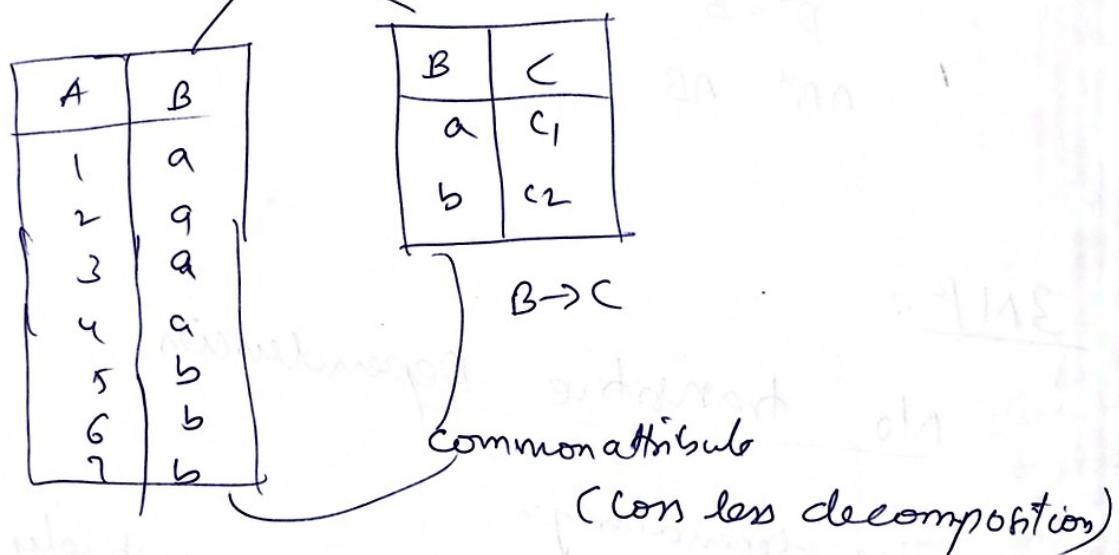
$$B \rightarrow C$$

↓  
Transitive dependency

LHS = Superkey

RHS = Key

A	B	C
1	a	c <sub>1</sub>
2	a	c <sub>1</sub>
3	a	c <sub>1</sub>
4	a	c <sub>1</sub>
5	b	c <sub>2</sub>
6	b	c <sub>2</sub>
7	b	c <sub>2</sub>



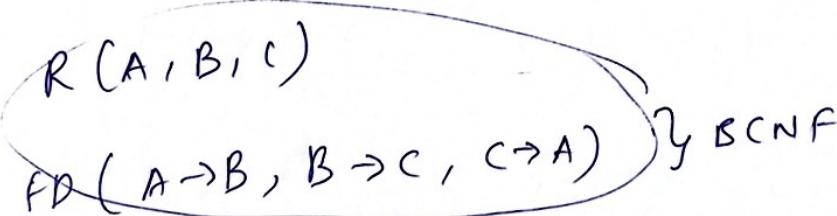
3NF may preserve f. dependencies

## BCNF (Boyce Codd)

A Relational Schema ' $R$ ' is in BCNF, if whenever a non-trivial FD  $X \rightarrow A$ , holds in ' $R$ ', then ' $X$ ' is super key of  $R$ , i.e., determinants of all FD's must be super keys.

$x \ y$
$a \ c$
$a \ c$
$a \ c$
$b \ d$
$b \ d$
$b \ d$

wherever you see,  $X \rightarrow Y$ , form a new table where-  $X$  is key,  $Y$  is attribute



$$A^+ = ABC$$

$$B^+ = ABC$$

$$C^+ = ABC$$

Q.R.

$R(ABC)$

$f: d \{A, B \rightarrow C, C \rightarrow B\}$

~~$A^+ = d \{A, B, C\}$~~   $A^+ = d \{A\}$

~~$B^+ = B$~~

$C^+ = B, C$

$AB^+ = A, B, C$

$BC^+ = B, C$

$AC^+ = A, B, C$

$(A, B, C) \rightarrow$  prime attributes

2/10/15

finding Candidate Keys in relation,

$R(A B C D E F)$  with functional dependencies

$$f.D = \{AB \rightarrow C, C \rightarrow D, D \rightarrow EB, E \rightarrow F, F \rightarrow A\}$$

Sol: with '1' key Attribute

$$A^+ = \{A\}$$

$$B^+ = \{B\}$$

$$\checkmark C^+ = \{C, D, E, B, F, A\}$$

$$\checkmark D^+ = \{D, E, B, F, A, C\}$$

$$E^+ = \{E, F, A\}$$

$$F^+ = \{F, A\}$$

with '2' attributes

$$\checkmark (BE)^+ =$$

$$(AE)^+ =$$

$$\checkmark (AB)^+ =$$

$$\checkmark (ABE)^+ =$$

with '2' attributes

$$\checkmark (AB)^+ = \{A, B, C, D, E, F\}$$

$$(AE)^+ = \{A, E, F\}$$

$$(AF)^+ = \{A, E\}$$

$$\checkmark (BE)^+ = \{B, E, F, A, C, D\}$$

$$\checkmark (BF)^+ = \{B, F, A, C, D, E\}$$

$$(EF)^+ = \{E, F, A\}$$

with '4' attributes

$$(ABEF)^+$$

↓ \*

⇒ '8' candidate keys

Q Candidate keys of sub relations

$$R(ABCD) : \{AB \rightarrow CD, D \rightarrow A\}$$

what are the candidate keys of sub relation  $R(BCD)$

$$\underline{R(BCD)}$$

$$B^+ = \{B\}$$

$$C^+ = \{C\}$$

$$D^+ = \{D, A\}$$

$$BC^+ = \{B, C\}$$

$$CD^+ = \{C, D, A\}$$

$$\checkmark BD^+ = \{B, D, A, C\}$$

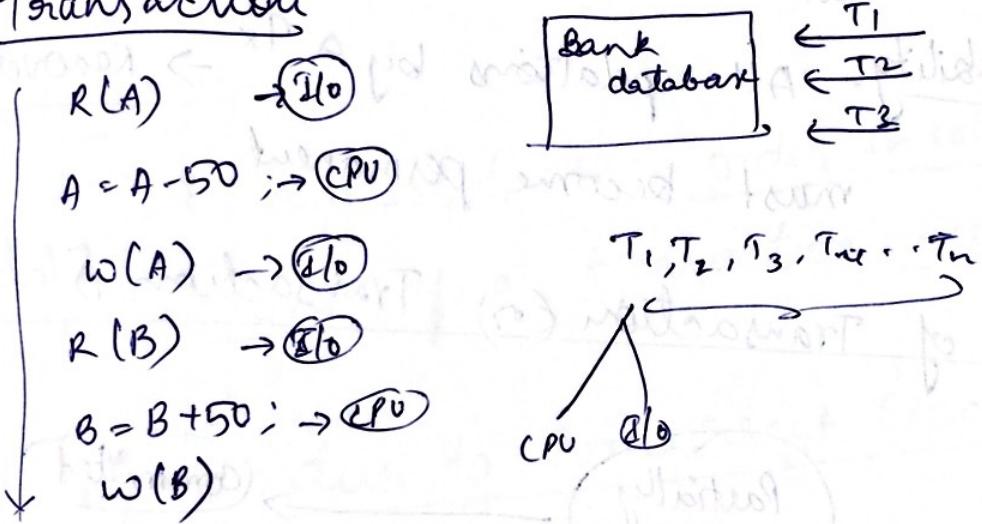
is candidate key

# Transactions Management & Concurrency Control

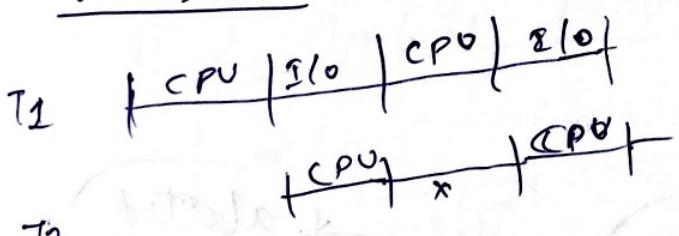
## Transactions:-

A transaction is a collection of operations that forms a single logical unit of work.

## Transaction



## Transactions



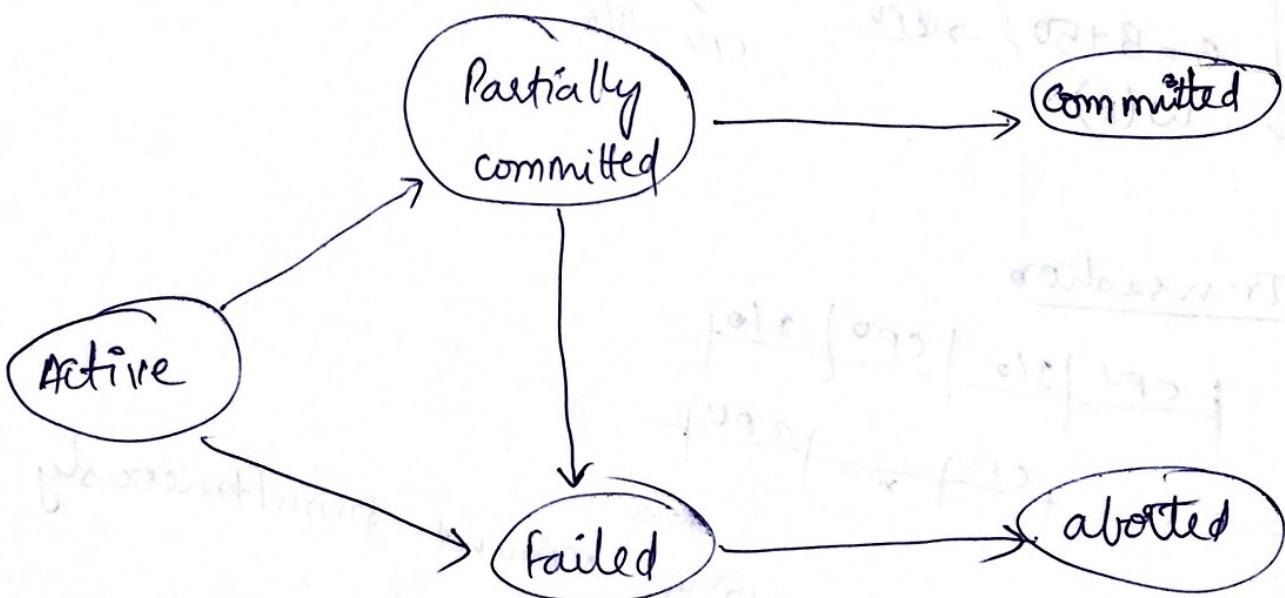
→ Problem of accessing account simultaneously

Similar to Synchronisation techniques in O.S  
we have Transaction Management  
Techniques in DBMS

## Transaction Properties

1. Atomicity: All or none → Transaction Manager
2. Consistency: Correctness → User/Application Program
3. Isolation: Each Tx should be executed without knowing what is happening with other transaction → Concurrency Control Management
4. Durability: All updates by a Tx must become permanent → Recovery

## States of Transaction (or) Transaction States



## Concurrent Execution :-

Interleaving execution of the operations of a transaction.

why?

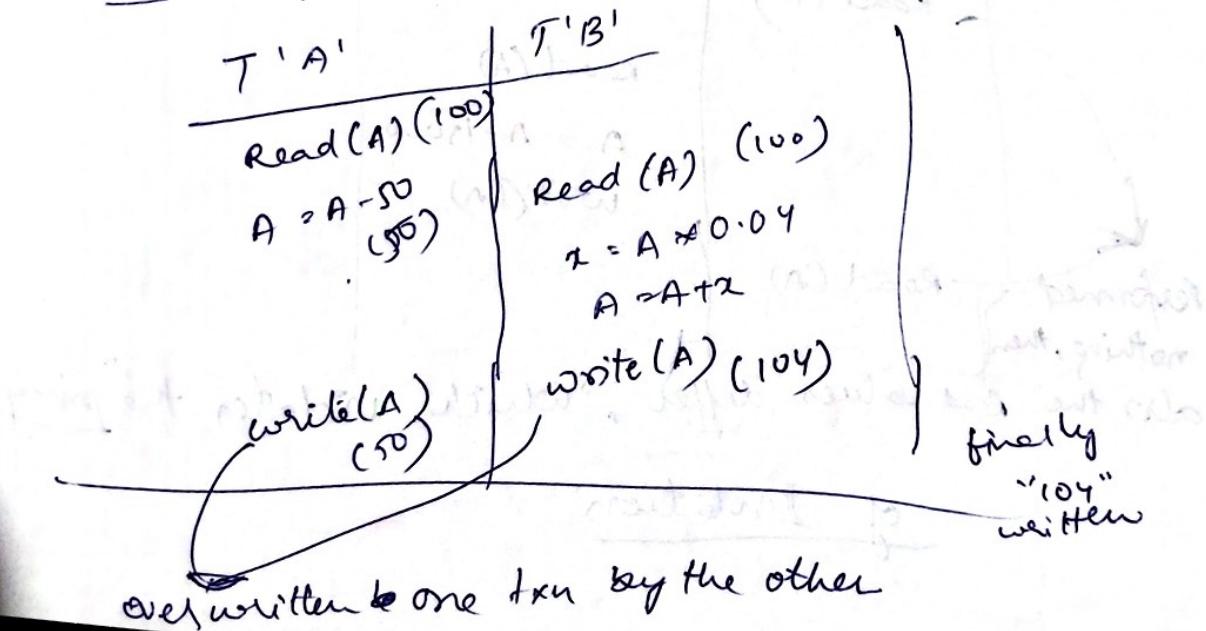
1. for avoiding longer waiting time
2. simultaneous & effective use of I/O & CPU
3. the processor & disk utilization increases

Schedule :-

It represents the order in which instructions of a transaction executed.

Problems due to concurrent execution of the transactions

1. Lost Update Problem (W-W. conflict)



## 2. Dirty Read Operation (W-R conflict)

T <sub>1</sub>	T <sub>2</sub>
Read(A) $A = A - 50$ write(A)	Read(A) $x = A + 0.04$ $A = A + x$ write(A)
$\xrightarrow{\text{Fail}} \leftarrow$ Read(B) $B = B + 50$ write(B)	

→ Reading an un-committed data is called dirty read operation.

## 3. Unrepeatable Reads (or) Non-Repeatable Reads (R-W)

T <sub>1</sub>	T <sub>2</sub>
Read(A)	read(A)
Read(A)	$A = A - 15000$ write(T <sub>1</sub> )

Performed nothing, then also the Read values differ, which violates the principle of Isolation.

## phantom Tuple (Phantom Phenomenon):

→ Tuple is added by transactions

	T1	T2
		salary will go in blocks prioritized
	<u>eno</u> <u>ename</u> <u>salary</u>	
1	A	5000
3	C	4000
	select * from emp	
	where salary > 3000	
		insert into EmpValues(4,0,3500)
		salary will go in blocks prioritized
	<u>eno</u> <u>ename</u> <u>salary</u>	
1	A	5000
3	C	4000
4	D	3500
	select * from emp	
	where salary > 3000	

→ Reading Tuples by one transaction at different times gives different results

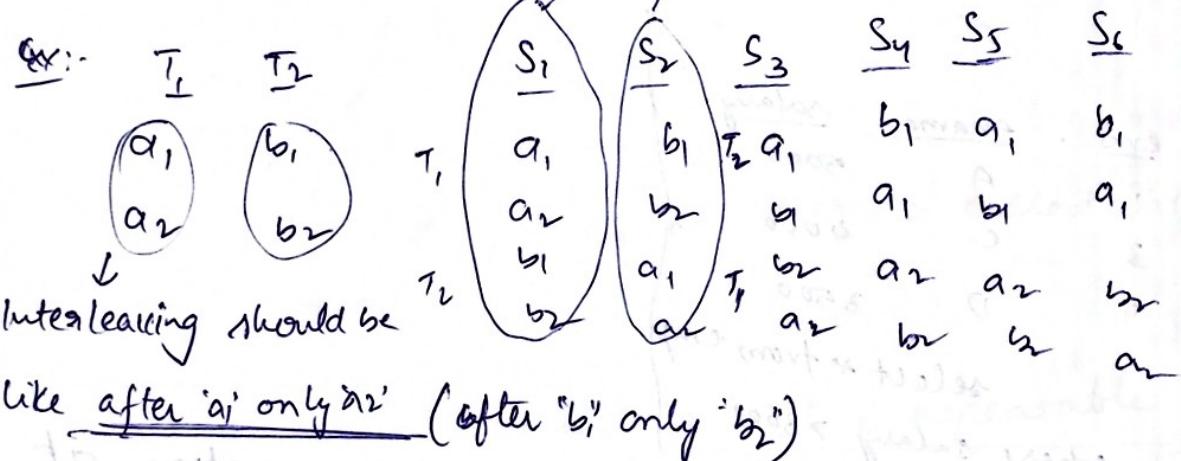
## 4) Incorrect Summary Problem:-

	T1	T2
		sum = 0
	Read(x)	Read(x);
	x = x + 500;	sum = sum + x;
	write(x);	
		Read(y);
		sum = sum + y;
		read(y);
		sum = sum + y;
	Read(y); y = y + 500; (y);	

We will get wrong summary if some transaction is interfering and changing the values in between, when we are summing up the values

### Characterising Schedules :-

#### 1) Serial Schedule :-



If there are 'm' transactions like and 'n' operations in each transaction, then

$T_1, T_2, T_3, \dots, T_m$

$n_1, n_2, n_3, \dots, n_m$

the no. of ~~possible~~ <sup>possible</sup> schedules are

$$\frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{n_1! \times n_2! \times n_3! \times \dots \times n_m!}$$

Serial Schedules are like  $T_1$  on  $T_2 \Rightarrow \frac{T_2}{T_1} \Rightarrow 2!$   
 $\Rightarrow m!$

\* Serial schedules  $\Rightarrow$  Consistent  $\Rightarrow$  but hurt performance  
, we have to allow those schedules, which  
are logically equivalent to serial schedules.

### Types of Schedules :-

① Serial Schedule:  
Serial schedules, that does not interleave the  
actions of any operations of diff transaction.

$T_1 \rightarrow T_2 \text{ or } T_2 \rightarrow T_1$

$T_1$	$T_2$
$R(A)$	
$A = A + 100$	
$W(A)$	

consistent  
constant state  
of operation

$T_1$	$T_2$
$R(A)$	
$A = A + 100$	
$W(A)$	

inconsistent state  
of operation

② Complete Schedule :-

A Schedule is said to be complete  
schedule, if the last operation of each  
transaction is either abort or commit

T1	T2
R(A)	
$A = A - 60$	
w(A)	
commit	

R(A)

$$A = A - 60$$

w(A)

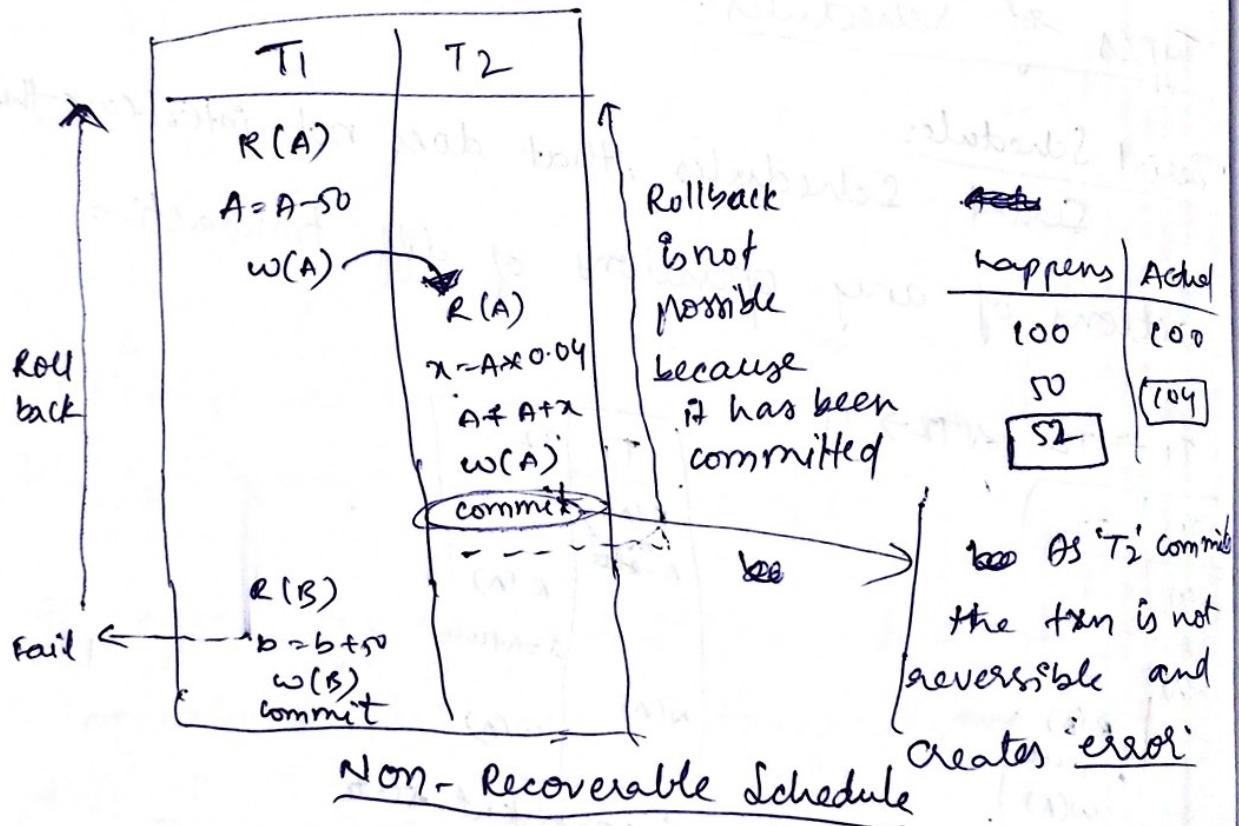
commit

$$A = A + 60$$

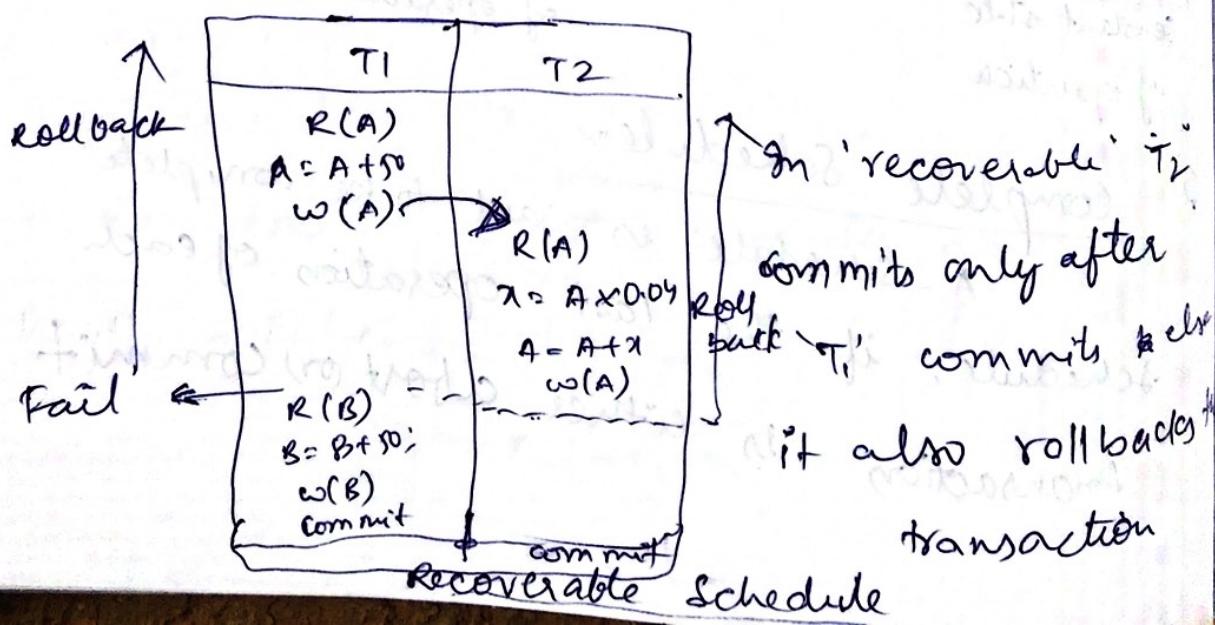
w(A)

abort

### 3) Recoverable Schedule:



As 'T<sub>2</sub>' commits  
the transaction is not  
reversible and  
creates 'error'

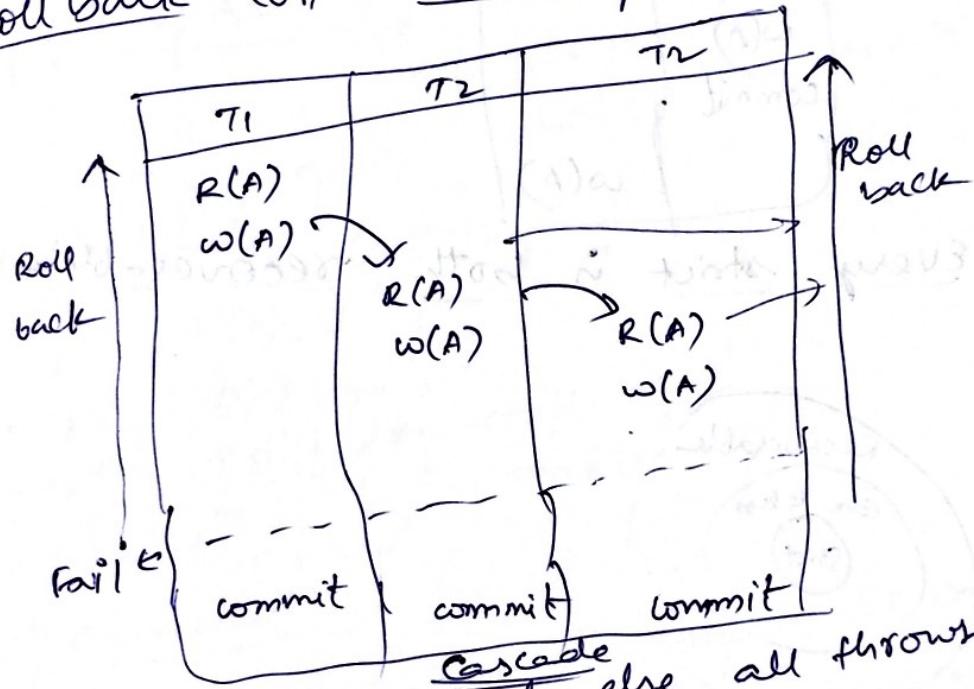


Recoverable Schedule

Ex: offering poisoned food, taking only after the person who offers consumes.

### Cascadeless Schedule:

If one transaction fails causes multiple transactions to roll back, called cascading roll back coz cascading aborts



→ If one eats all eats else all throws one after the other

### Cascade less:

→ If you don't take it unless the other eats it

T1	T2	T3
R(A) w(A) commit	R(A) w(A) commit	R(A) w(A) commit

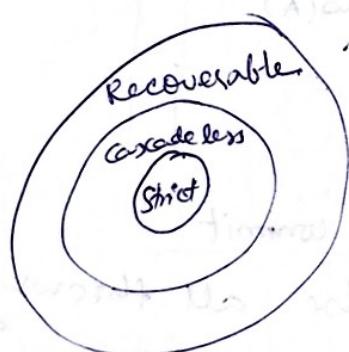
Cascade less Schedule

### Strict Schedule:-

→ It will not either read (or) write until the other commits unlike cascaded which only does not read until other commit.

T <sub>1</sub>	T <sub>2</sub>
R(A)	
w(A)	
commit	w(A)

→ Every strict is both recoverable & cascaded.



### Result Equivalent Schedule:-

#### Equivalent Schedule:-

The two schedules 'S<sub>1</sub>' & 'S<sub>2</sub>' are said to be equivalent schedules if they produce the same final database state.

#### Result Equivalent Schedule:-

The two schedules are said to be result equivalent if they produce the same final database state for the same initial values of data.

<u>S1</u>	<u>S2</u>
R(A)	R(A)
A = A + 10	A = A + 11
w(A)	w(A)

conflict equivalent & conflict serializable

### conflict Operations

diff txns on same data item  
with atleast one write

<u>T<sub>i</sub></u>	<u>T<sub>j</sub></u>
R(A)	w(A)
w(A)	R(A)
w(A)	w(A)

Conflicting operations

<u>T<sub>i</sub></u>	<u>T<sub>j</sub></u>
R(A)	R(A)
R(A)	R(A)

non-conflicting operations

operating on diff data

### conflict equivalent:

Two schedules  
equivalent if all  
both the schedules  
order

are said to be conflict  
conflicting operations in  
must be executed in same

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
R(A)	
w(A)	
R(B)	R(A)
w(B)	w(A)

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
R(A)	
w(A)	
	R(A)
	w(A)
	R(B)
	w(B)

Q Test which of the following schedules are conflict serializable

$S_1 : R_1(A) \quad R_2(B) \quad w_1(A) \quad w_2(B)$

$S_2 : R_2(B) \quad R_1(A) \quad w_2(B) \quad w_1(A)$

$S_1$	
$T_1$	$T_2$
$R(A)$	
$w(A)$	$R(B)$

$S_2$	
$T_1$	$T_2$
	$R(B)$
$R(A)$	
$w(A)$	$w(B)$

$S_1 \xrightarrow{\text{Conflict}} S_2$

$\Rightarrow$

$S_1 : R_1(A) \quad w_1(A) \quad R_2(B) \quad w_2(B) \quad R_1(B)$

$S_2 : R_1(A) \quad w_1(A) \quad R_1(B) \quad R_2(B) \quad w_2(B)$

$S_1$	
$T_1$	$T_2$
$R(A)$	
$w(A)$	
	$R(B)$
	$w(B)$
	$R(B)$

$S_2$	
$T_1$	$T_2$
$R(A)$	
$w(A)$	
	$R(B)$
	$R(B)$
	$w(B)$

here write is occurring first

here read occurring first

$\Rightarrow$  so  $S_1 \neq S_2$  are not conflict equivalent

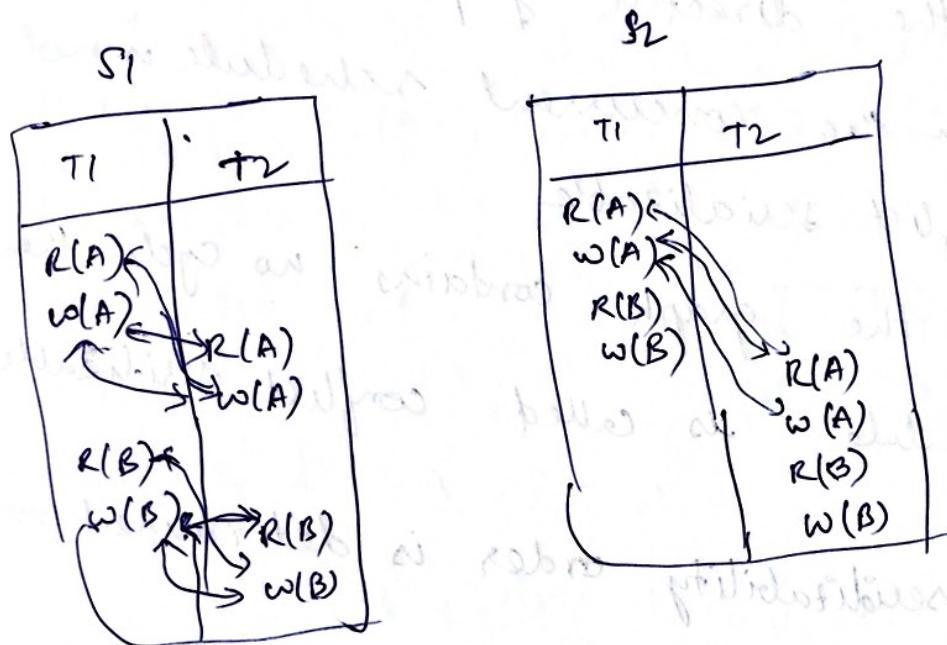
$S_1$	
$T_1$	$T_2$
$R(A)$	
$w(B)$	$w(B)$

$S_2$	
$T_1$	$T_2$
$R(A)$	
	$R(A)$
	$w(B)$

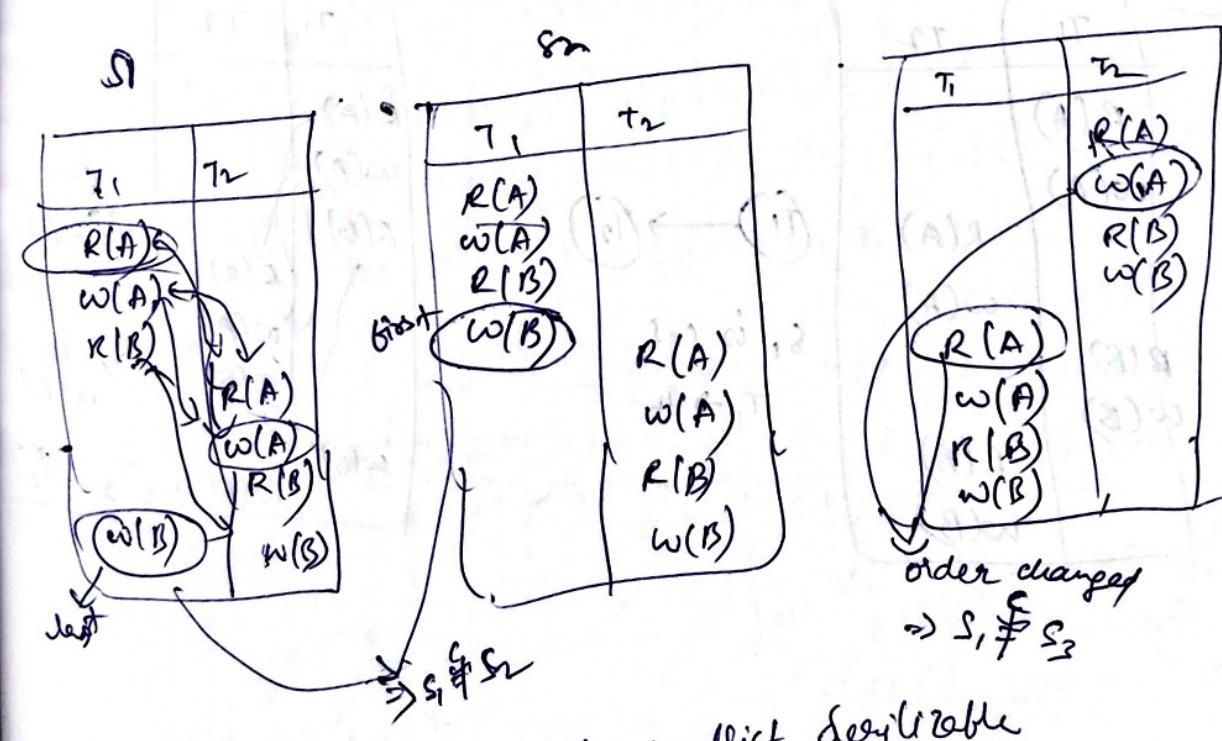
## conflict Serializable :-

A Schedule is said to be conflict serializable if it is conflict equivalent to a serial schedule.

Given schedule, f) check whether it is conflict serializable or not.



$\Rightarrow S_1$  is conflict serializable

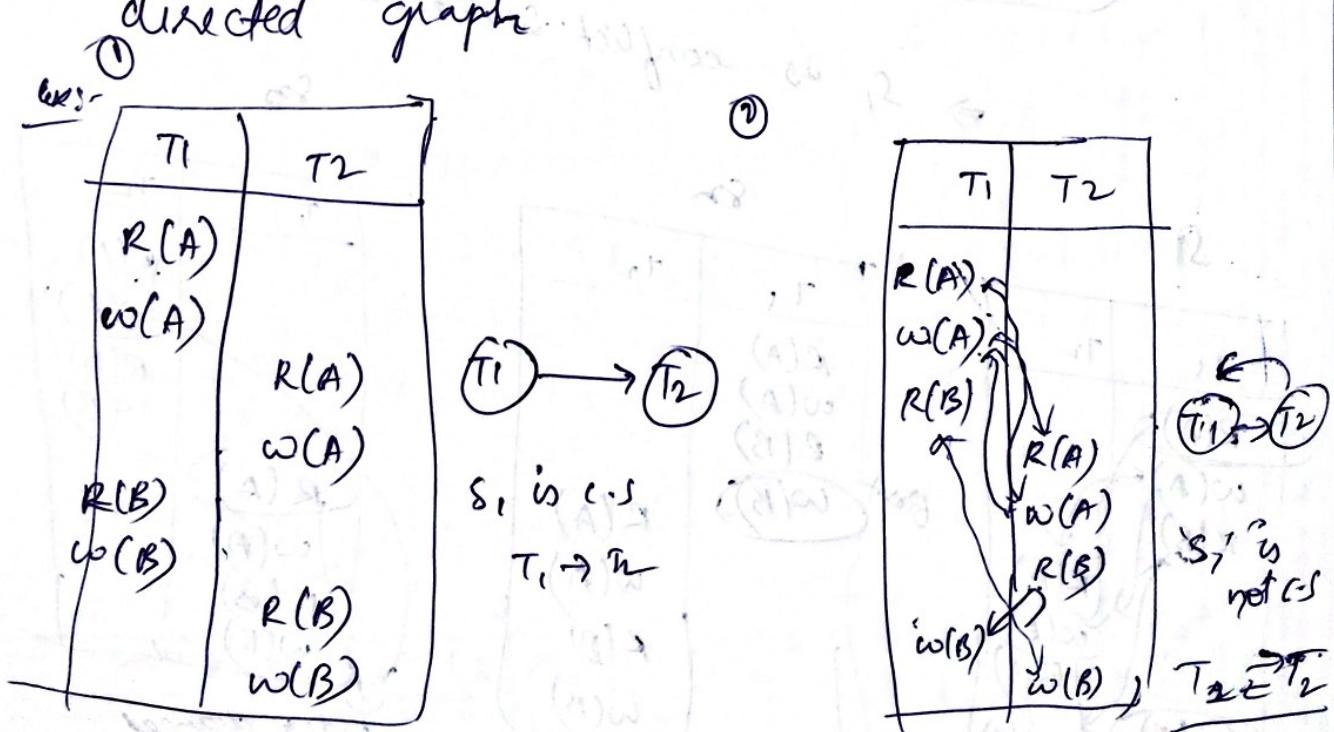


$S_1$  is not conflict serializable

# Test for Conflict Serializability using precedence graph.

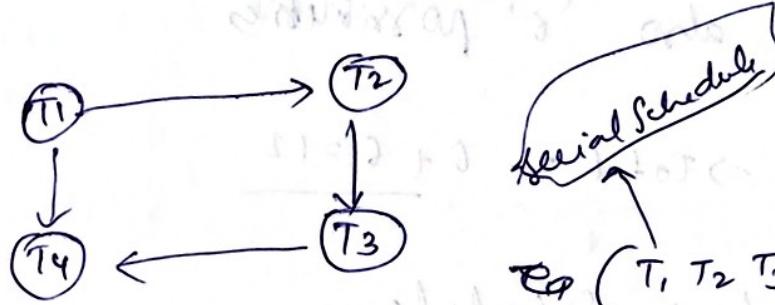
1. Construct a directed graph where each vertex corresponds to a transaction and each directed edge represents a conflicting operation.
2. If the directed graph contains cycles, then the concurrent schedule is not conflict serializable.
3. If the graph contains no cycle then the schedule is called conflict serializable.

The serializability order is determined based on directed graphs.



find the serializability order of the concurrent schedule given below

$R_1(x) \quad W_3(x) \quad N_1(y) \quad R_2(y) \quad W_2(z) \quad R_4(y)$

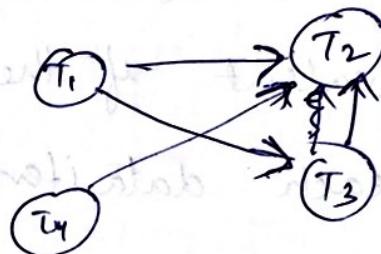


$T_1$	$T_2$	$T_3$	$T_4$
			$R(y)$
			$w(x)$
			$R(y)$
			$w(z)$
			$R(x)$
			$R(y)$

$\text{seq}(T_1, T_2, T_3, T_4)$

$R_1(A), R_2(A), R_3(A), w_1(B), w_2(A), R_3(B), w_2(B)$

- a) not CS
- b)  $T_3 T_4 T_1 T_2$
- c)  $T_1 T_4 T_3 T_2$
- d)  $T_2 T_3 T_1 T_4$



Two transactions  $T_1$  &  $T_2$  are given as follows.

$T_1 : R_1(A) \quad w_1(A) \quad R_1(B) \quad w_1(B)$

$T_2 : R_2(A) \quad w_2(A) \quad R_2(B) \quad w_2(B)$

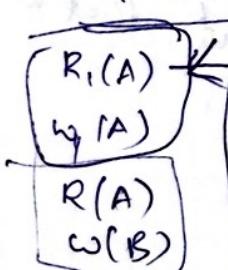
find the total no of conflict serializable schedules that can be formed by  $T_1$  &  $T_2$ ?

Ans:

$T_1 \rightarrow T_2$

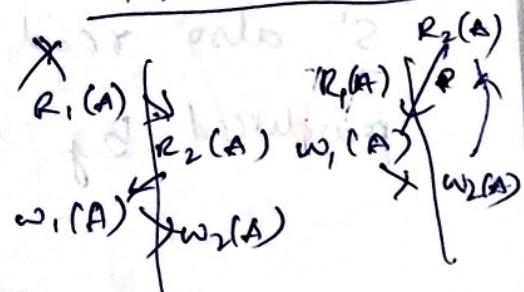
(or)  $T_2 \rightarrow T_1$

because of these reasons  
there should occur first



These should be only last

\* trial & error



$$\Rightarrow \frac{4!}{2!2!} = 6$$

$T_2 \rightarrow T_1$  also '6' possibilities

$$\Rightarrow \text{Total} = 6 + 6 = 12$$

### View Equivalent Schedule:

Two schedules  $S$  &  $S'$  are said to be view equivalent if the following 3 condn's are met

for each data item (say A)

- i) for each data item 'A', if transaction  $T_i$  reads the initial value of 'A' in schedule  $S$ , then transaction  $T_i$  must in schedule  $S'$  also read the initial value of (A)
- ii) If transaction  $T_i$  executes read -  $R(A)$  in schedule  $S$ , and that was produced by transaction 's', then transaction  $T_i$  must in schedule  $S'$  also read the value of 'A' that was produced by  $T_j$ .

- for each data item the transaction (if any) that performs final write of 'A' operation in 'S' must also perform the final write of 'A' operation in "S".

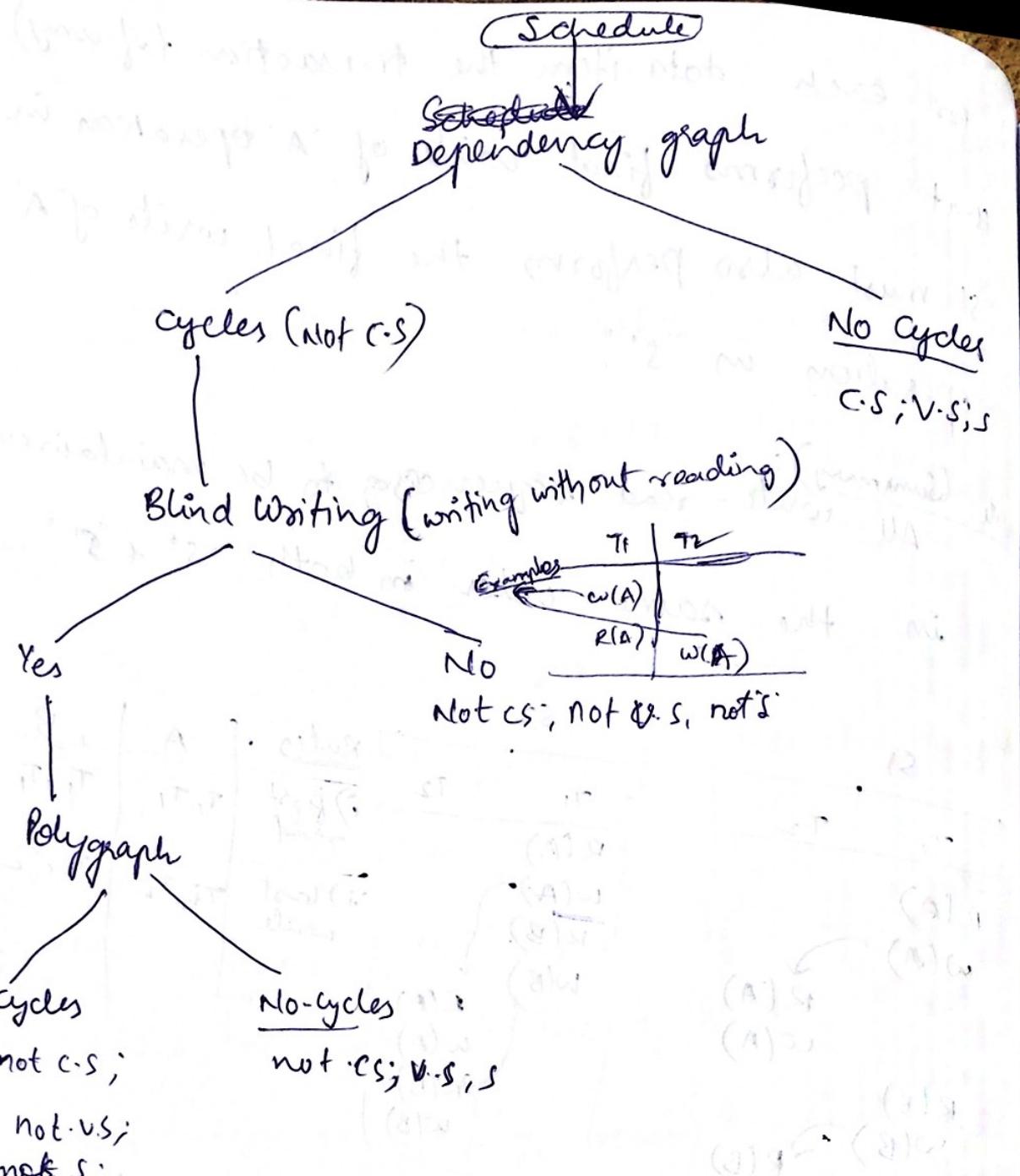
Note - Summary: All write-read sequencing to be maintained in the same order in both "S" & "S".

<u>S1</u>	<u>S2</u>	<u>Rules</u>	
<u>T1</u>	<u>T2</u>	<u>A</u>	<u>B</u>
$R(A)$ $w(A)$	$R(A)$ $w(A)$	i) first read ii) last write	$T_1, T_1$ $T_2, T_2$
$R(B)$ $w(B)$	$R(B)$ $w(B)$		

~~when a view equivalent schedule~~  
when a Schedule 'S' is view equivalent when a Schedule 'S' is view equivalent to its serial schedule

<u>S1</u>	<u>S2</u>	<u>Rule</u>	<u>A</u>	<u>B</u>
<u>T1</u>	<u>T2</u>		<u>T1, T1</u>	<u>X</u>
$R(A)$ $w(A)$	$R(A)$ $w(A)$	i)	$T_1, T_1$	$X$
$w(A)$	$w(A)$	ii)	$T_1, T_2$	$X$

$\Rightarrow S_1 \neq S_2$



Serializable Schedule: - A Schedule is serialisable if it is either conflict serialisable (1) view serialisable (2) both.

$$\rightarrow \text{concurrent schedules} = 6 = \frac{24}{2!2!} = \frac{24}{4} = 6$$

$$\text{Non-serial schedules} = 6 - 2 = 4$$

Note: The no. of concurrent schedules that can be formed over no. of transactions having  $n_1, n_2, n_3, \dots, n_m$  operations respectively are

$$= \left[ \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{n_1! \times n_2! \times n_3! \dots \times n_m!} \right]$$

The no. of non-serial schedules are,

$$\left[ \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{n_1! \times n_2! \times n_3! \dots \times n_m!} \right] - m!$$

Q Examples of

i) Un-repeatable Read Pblm

ii) Lost Update Pblm

Examples of polygraphs for View Serializability

$$S = r_1(A) w_2(A) r_3(A) w_1(A) w_3(A)$$

i) Checking for C.S

$\Rightarrow$  cycle  $\Rightarrow$  not C.S

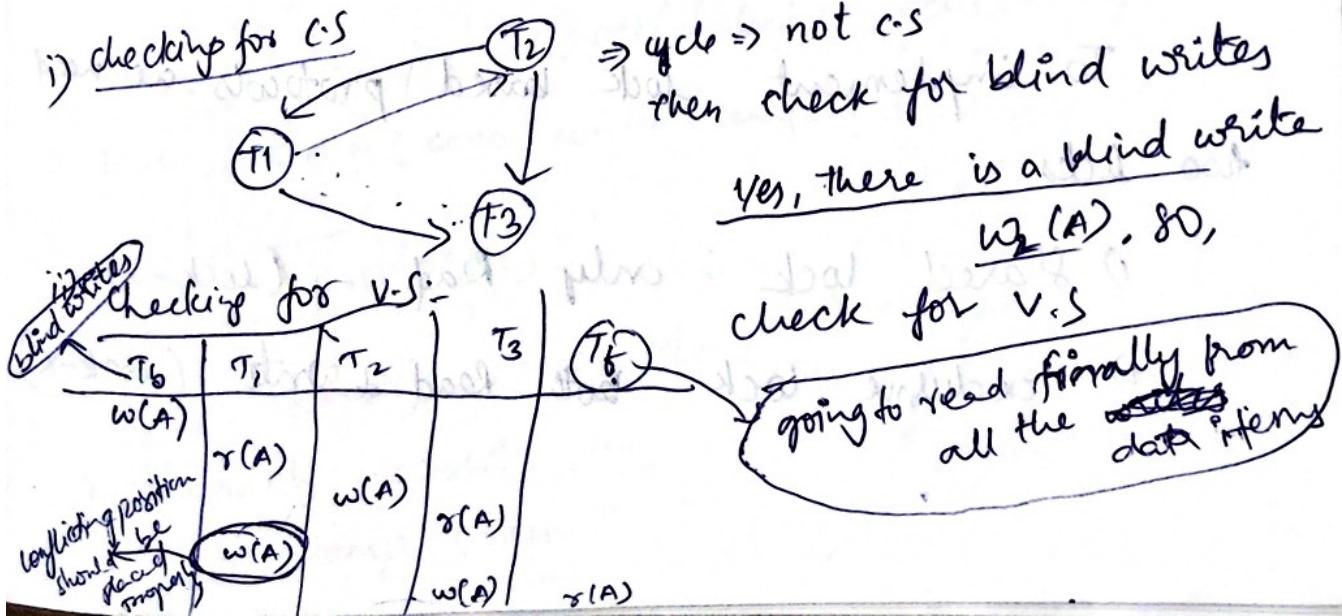
then check for blind writes

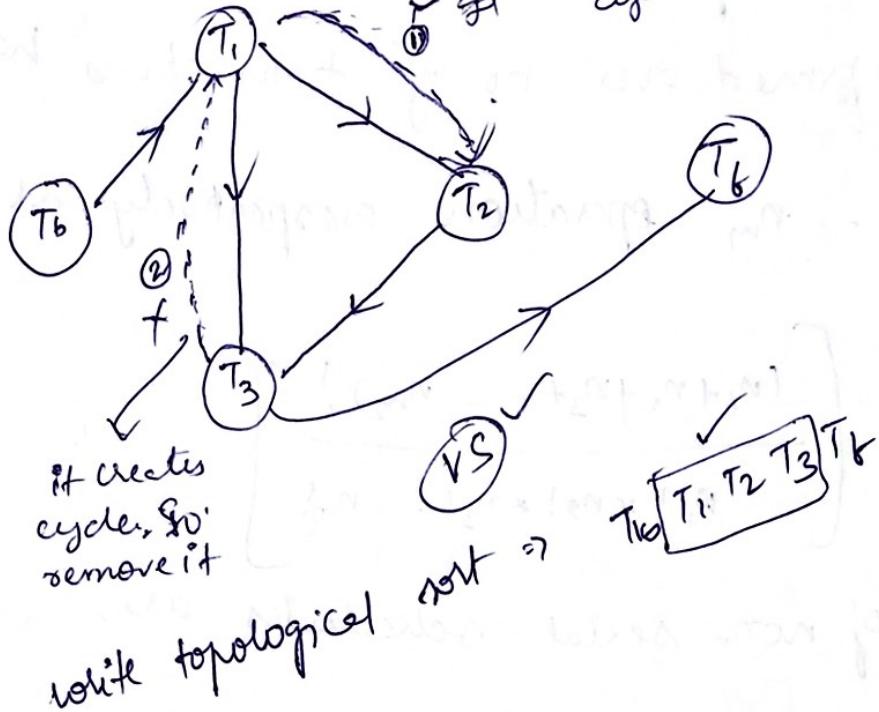
Yes, there is a blind write

$w_2(A)$ , so,

check for V.S

going to read finally from all the ~~data~~ items





## Concurrency Control:

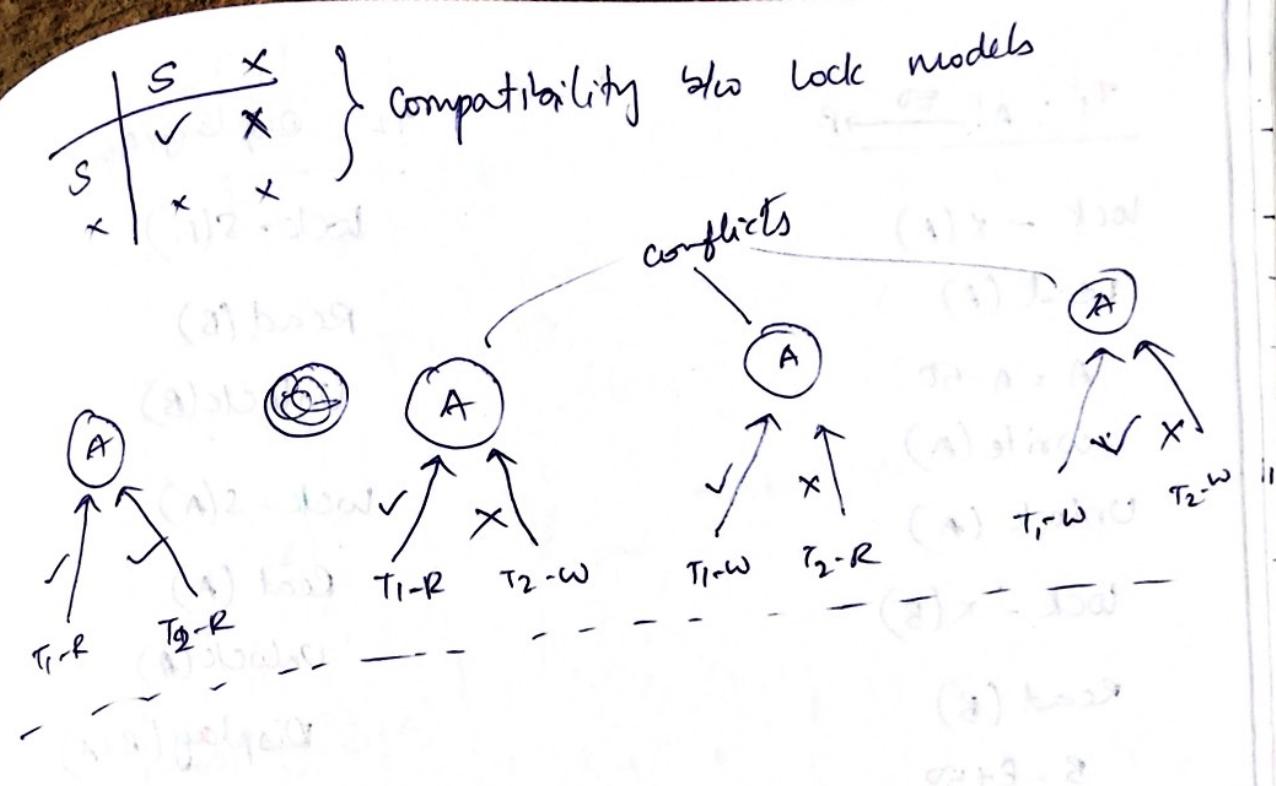
### 1) Lock based Protocols:-

which requires that all data items must be accessed in a mutually exclusive manner. i.e, when one transaction is accessing the data item, no other transaction simultaneously update the data item.

To implement lock based protocols we need two locks.

1) Shared lock : only Read (lock-s)

2) Exclusive lock : both Read & write (lock-x)



- ~~concurrency~~ concurrency control manager in DBMS takes care of concurrency with some rules kept in mind.
- Serial schedules are logical schedules
- Serial schedules are generating & executing schedule
- ~~Before & After~~ Before generating the serializability itself, we have to check the serializability with CCM (conc. control manager).
- Rules to be followed before generating schedules.

### Three protocols

1. lock based protocol
2. graph based "
3. remap based "

T<sub>1</sub> : A  $\xrightarrow{50}$  B

lock - x(A)

Read (A)

A = A - 50

write (A)

Unlock (A)

lock - x(B)

Read (B)

B = B + 50

write (B)

unlock (B)

T<sub>2</sub> : Display (B+A)

lock - s(B)

Read (B)

Unlock (B)

lock - s(A)

Read (A)

Unlock (A)

Display (B+A)

### Problems in Interleaving

①

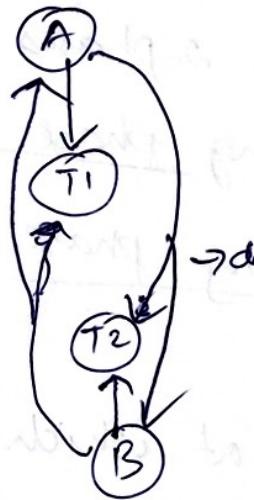
T <sub>1</sub>	T <sub>2</sub>
lock - x(A)	
Read (A)	
A = A - 50	
write (A)	
unlock (A)	
	lock - s(B)
	Read (B)
	unlock (B)
	lock - s(A)
	Read (A)
	unlock (A)
	display (B+A)
lock - x(B)	
Read (B)	
B = B + 50	
write (B)	
unlock (B)	

### Inconsistent Result

B	A	B	= 300
before T <sub>i</sub>	100	200	
After T <sub>i</sub>	50	250	= 300
		but off = 250	$\Rightarrow$ error

## ② Deadlock

	T1	T2
lock - x(A)		
R(A)		
A = A + S <sup>0</sup>		
w(A)		
lock - s(B)		
R(B)		
lock - s(A)		
R(A)		
display (B+A)		
commit		
unlock (B)		
unlock (A)		
lock - x(B)		
R(B)		
B = B + S <sup>0</sup>		
w(B)		
commit		
unlock (B)		
unlock (A)		

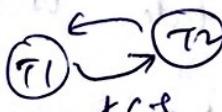


deadlock

③ Simple locking Cannot always provide Serialisation

	T1	T2
L(A)		
V(A)		
L(B)		
V(B)		

	T1	T2
L(A)		
V(A)		
L(B)		
V(B)		



T2 → T1

not CS

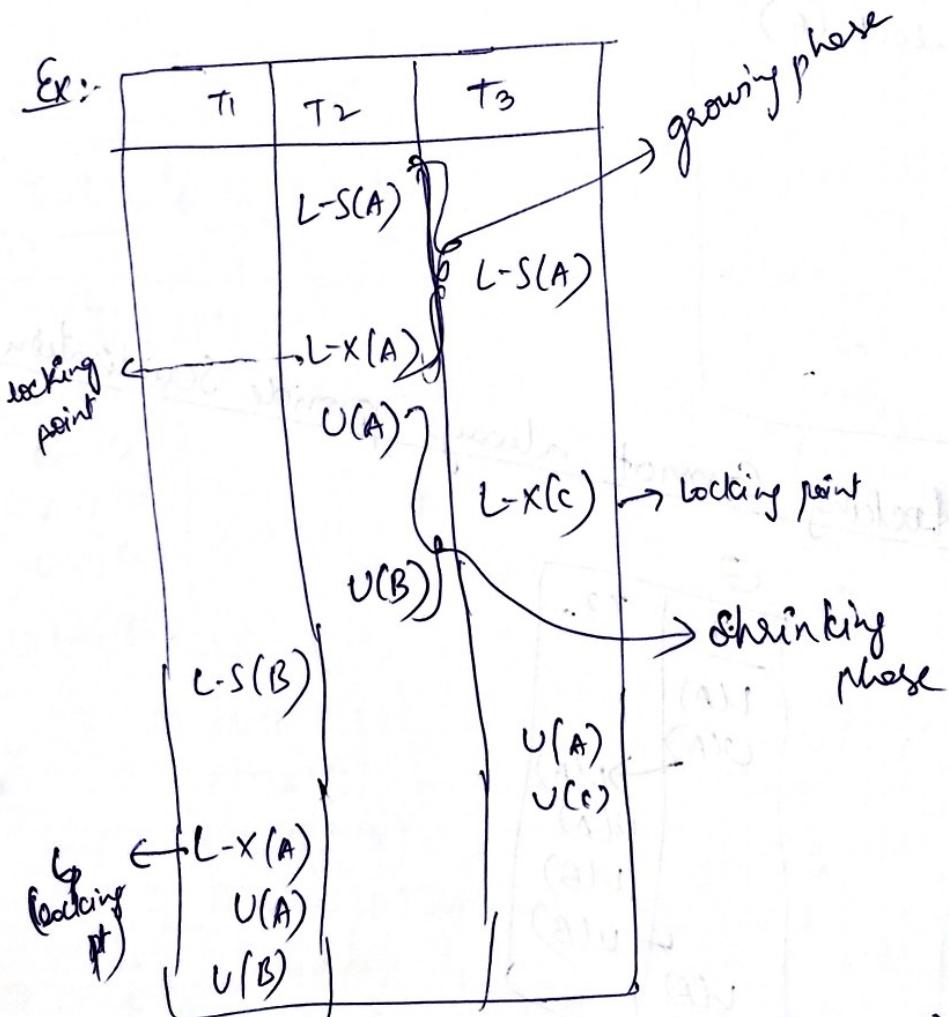
2 - Phase Locking Protocol:  
which requires both locks & tombstones

being done in 2-phases

- 1) Growing phase - "obtains locks"
- 2) Shrinking phase - "release locks"

Lock Point:

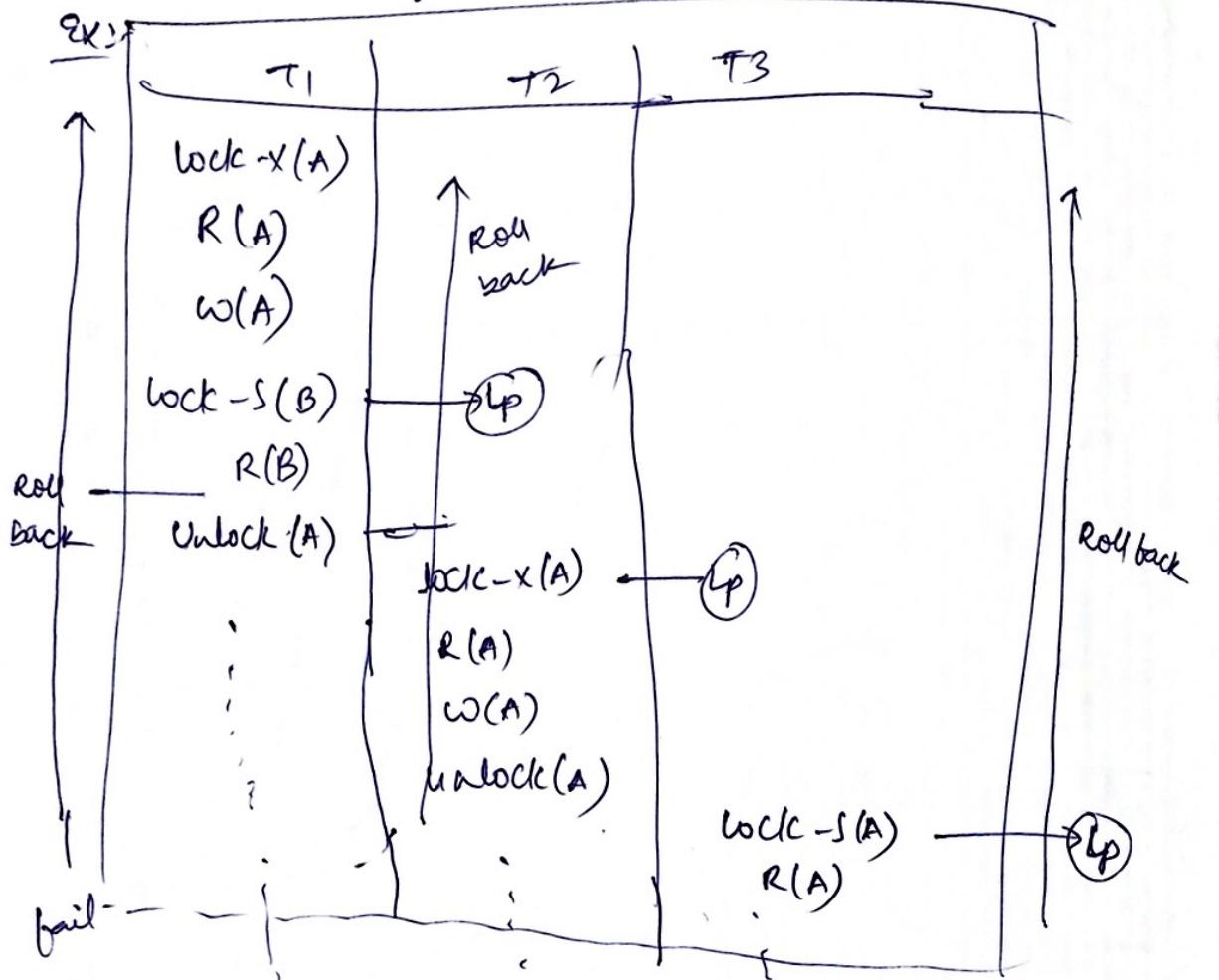
The point at which the transaction has obtained its final lock is called a "lock point"



→ Serial Schedule is  $(T_2 \ T_3 \ T_1)$

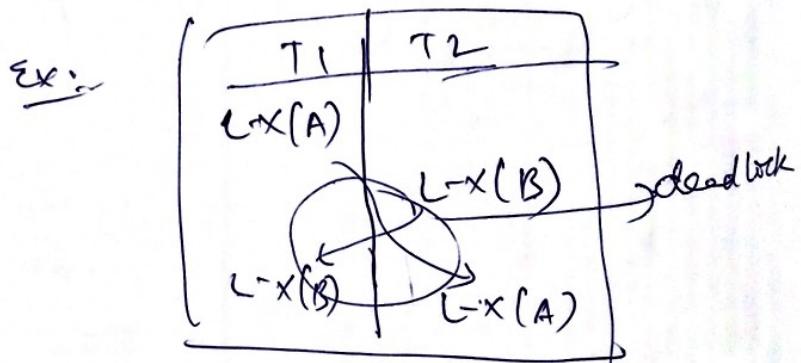
→ Two phase locking protocol ensures conflict serializability & serializability order is determined based on their lock

→ 2-phase locking protocol fails during rollbacks



→ Cascading rollbacks may occur in 2-phase locking protocol

\* Deadlocks may also occur during 2-phase locking protocol



→ Cascading Rollbacks can be avoided by a modification of 2-phase locking protocol

strict 2-phase locking protocol (strict 2PL):-

which requires that in addition to locking being 2-phase all exclusive mode locks taken by a transaction must be held until the transaction commits

Rigorous - 2-phase locking protocol (Rigorous 2PL):-

which requires that in addition to locking being 2-phase all locks must be held until the transaction commits

Avoids cascading rollbacks but deadlocks can occur

Conservative 2PL:-

which requires the transaction to update all the locks before it starts & release all the locks after it commits

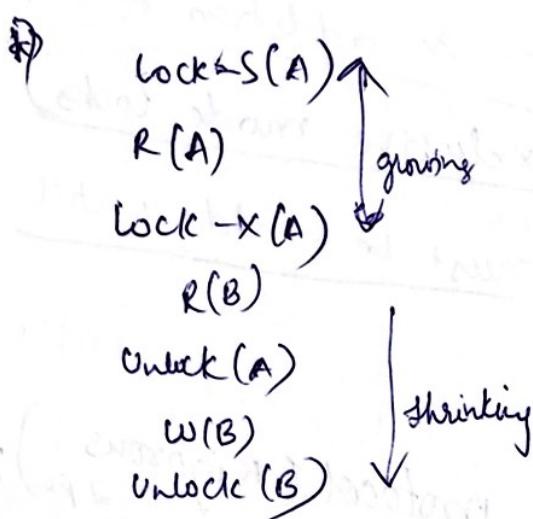
Avoids cascading rollbacks & deadlocks

Disadvantages

- holds lock for long time
- suppose to know all requirements

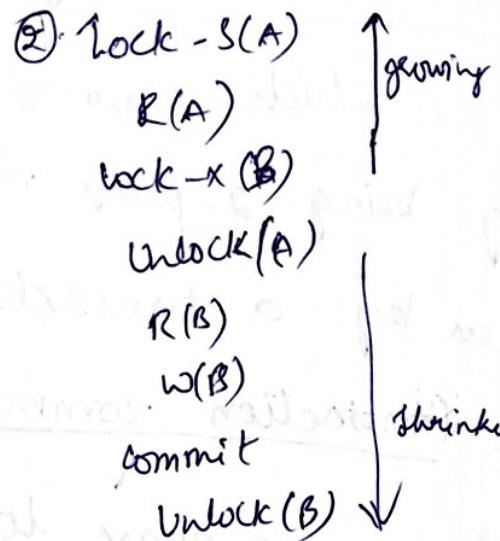


## Examples of 2PL



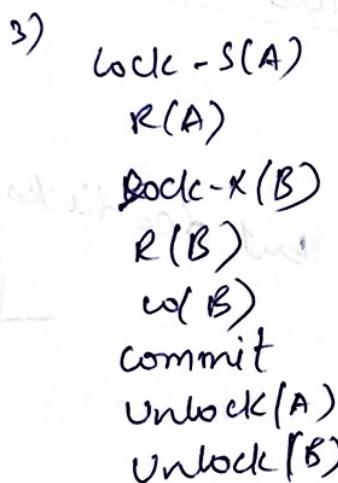
not 2PL but not

strict, vigorous, conservative

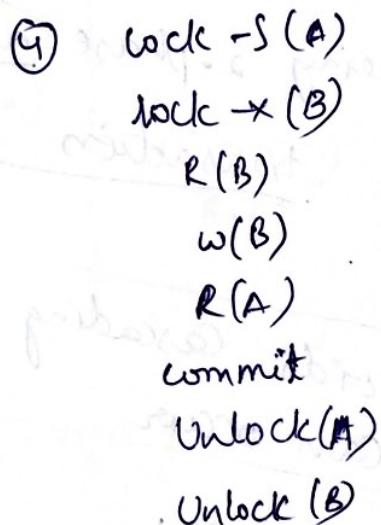


2PL, strict, but not

Reflex.



strict, rigorous 2PL



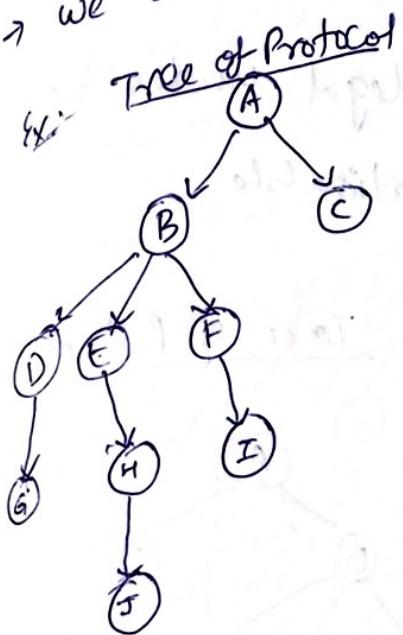
strict, rigorous, conservative 2PL

- \* In growing phase you can upgrade a shared lock to Exclusive lock (or) In shrinking phase you can degrade a lock from Exclusive to Shared lock

## Graph based Protocol

→ To overcome the disadvantages of locking protocols we have developed graph based protocol.

→ we use trees in GBP



1) locks must be done in order of the tree  
ex. for A, B, H  
 $A \rightarrow B \rightarrow H$

2) In tree no cycles will be formed

### Rules:

- In tree protocol the only lock instruction allowed is "lock-x" (exclusive) and each transaction, T<sub>i</sub> can lock a data item at most once and must observe the following rules
- i) the first lock by T<sub>i</sub> may be on any data item
  - ii) Subsequently a data item can be locked by T<sub>i</sub> only if the parent of the data item is currently locked by T<sub>i</sub>.
  - iii) Data items can be unlocked at any time

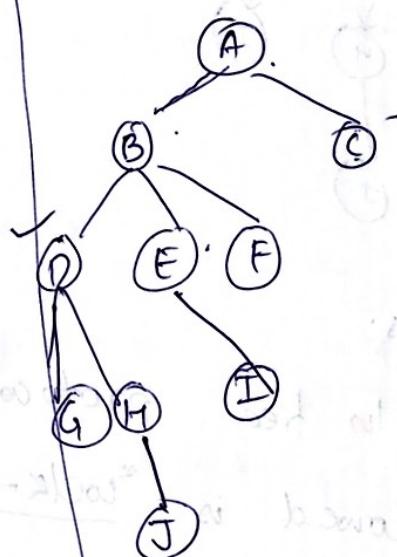
A data item that has been locked and unlocked by  $T_i$  cannot subsequently be locked by  $T_i$ .

NOTE:-

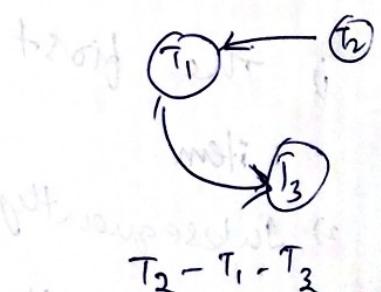
All schedules that are legal under tree protocol are conflict serialisable.

$T_1$	$T_2$	$T_3$
lock-x(B)		
	lock-x(B)	
	lock-x(H)	
	unlock(D)	
lock-x(E)		
lock-x(D)		
unlock(B)		
unlock(E)		
	unlock(H)	
lock-x(W)		
unlock(D)		
		lock-x(B)
		lock-x(E)
		unlock(E)
		unlock(B)
		unlock(G)

Tree of Protocol



Conflict Serialisable



## Advantages:

1. Unlocking will be done much earlier, as we are not going to wait until commit is done

2. There are no deadlocks: - because, deadlock occurs if we wait for ~~a~~ resource which is held by other, but here we have required resource as we have parent



if we want 'H' we have 'D' (parent) & no one can have 'H' as we block the way at 'D' by having it

3. Ensures conflict serializability

## Disadvantages:

1. Requires prior knowledge about the order of the data items

2. Unnecessary locking overheads i.e. In some cases lock the data items that if does not access

## Time Stamp Ordering Protocol

Timestamp based protocol:

which requires that ordering among the transactions is determined in advance based on their timestamps (i.e., the time when ever it enters into the system for execution).

Each transaction is given unique fixed time.

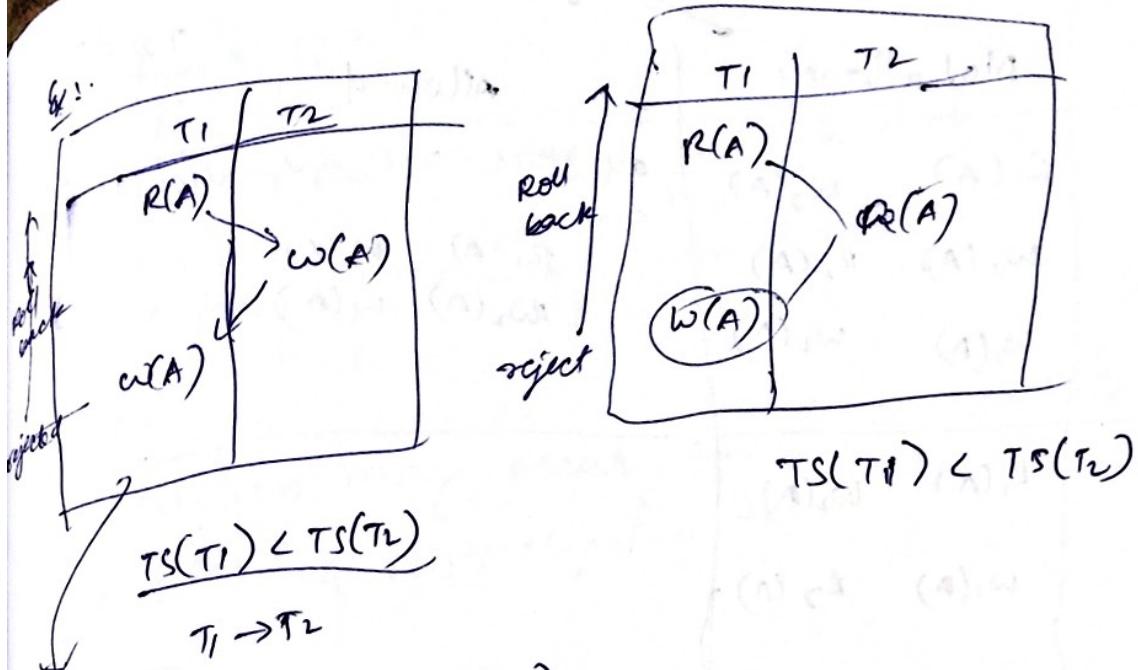
-stamp denoted by  $TS(T_i)$ :

If any transactions  $T_j$  that enters after  $T_i$ , the relation between their timestamps be  $TS(T_i) < TS(T_j)$  which means that the producing schedule must be equivalent to a serial

Schedule  $T_i \rightarrow T_j$

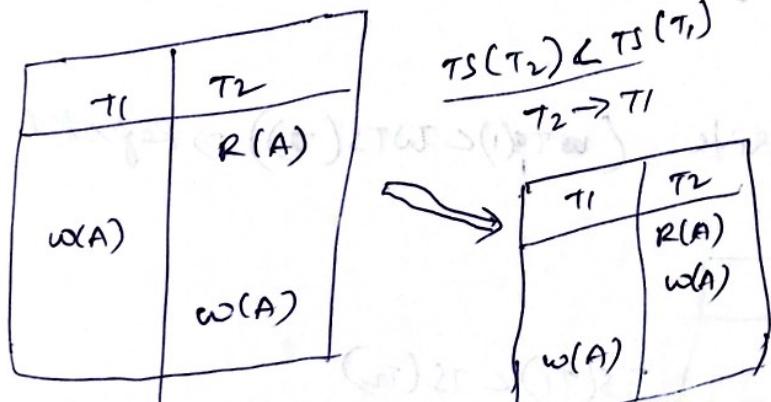
Time Stamp Ordering Protocol:-

In timestamp ordering protocol ensures that ~~they~~ any conflicting read & write operation are executed in timestamp order, if not such an operation is rejected and the transaction will be rolled back. The rolled back transaction will be restarted with a new timestamp.

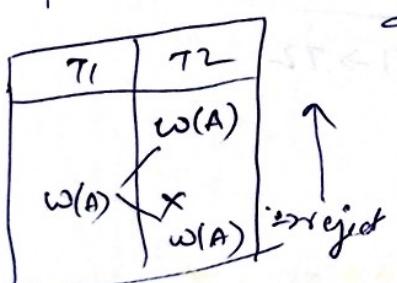


~~only if~~  $(RTS)$   
 $(WTS)$   
 Read Time Stamp } are used to implement  
 write Time Stamp } conflict resolution  
 $\{$

Thomas Write Rule :-  
 which requires to ignore all obsolete  
 write operations



\* It is saying  
 that late writes  
can be ignored



	Not allowed	Allowed	$T_2 \subset T_1$
$T \leq P$	$R_1(A)$ $w_1(A)$ $w_1(A)$	$w_2(A)$ $R_2(A)$ $w_2(A)$	all other cases are allowed ex:- $R_2(A)$ $w_1(A)$ $w_2(A)$ $R_1(A)$
$T \leq R$	$R_1(A)$ $w_1(A)$	$w_2(A)$ $R_2(A)$	

### Implementation

for each data item, (ex: A) it will maintain the values RTS, WTS & check when a new transaction comes with the values,

	A
RTS	2
WTS	2

$$T_1 = 1$$

$$T_2 = 2$$

if  $T_2$  tries to write  $(\text{RTS}(1) \subset \text{WTS}(2)) \Rightarrow \text{Rejected}$

	$T_1$	$T_2$
	$R(B)$	$R(B)$ $B = B + S_0$ $w(B)$
	$R(A)$ $\text{display}(A+B)$	$R(A)$ $A = A + S_0$ $w(A)$ $\text{display}(A+B)$

$$\text{TS}(T_1) \subset \text{TS}(T_2)$$

$$\Rightarrow T_1 \rightarrow T_2$$

### Advantages of TSP:

1. This protocol ensures serialisability
2. ensures freedom from deadlock

### Disadv:

starvation may occur due to continuously getting aborted & restarting the txn.

Organisation of Records in a file:-

ordered file organisation :-

All the records of file are ordered based on some search key value

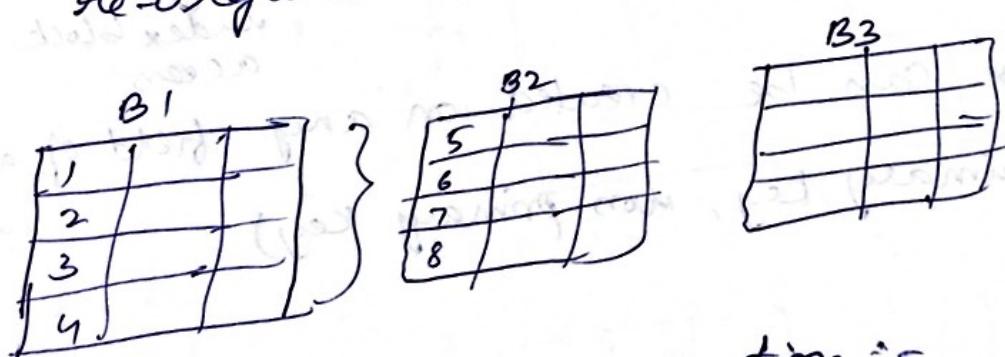
Searching: Binary Search

B data blocks

To access a record, the average no of block access =  $\lceil \log_2 B \rceil$  blocks

Adv: Searching is efficient

Disadv:- insertion is expensive due to re-organisation of the entire file.



Un-Ordered file Organisation :-

All the records of file are inserted at wherever the place is available usually at the end of the file

Searching: 1. linear search

B-data block

to access a record, the average no of block access =  $\frac{B}{2}$  blocks

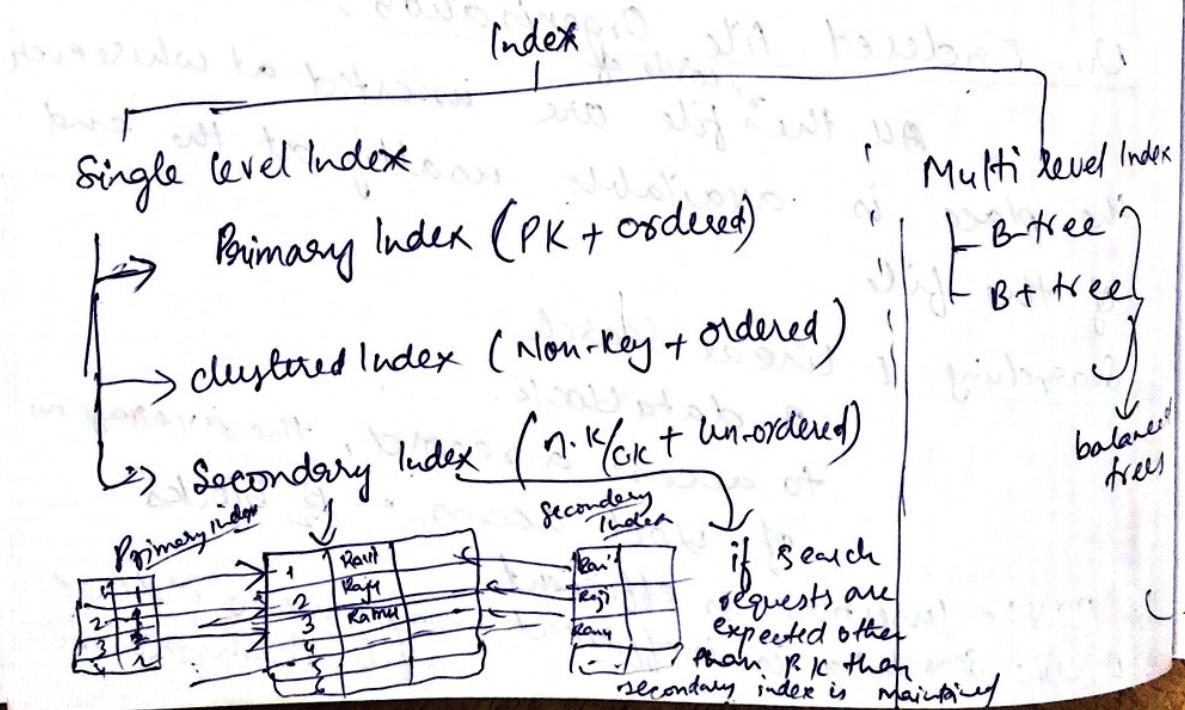
Adv: Insertion is efficient

Disadv:- Searching is inefficient compared to ordered file organisation.

## Indexing

### Index:

1. Indexes are used to improve search efficiency
  2. Index is a record consists of two fields
- |     |                |
|-----|----------------|
| Key | Block position |
|-----|----------------|
- ↳ pointer to a block where key is available
3. Index is an ordered file
  4. Searching: Binary Search
  5. To access a record using the index,  
the avg no of block accesses =  $\log_2 B_i + 1$
  6. Index can be created on any field of a relation  
(primary key, non primary key)

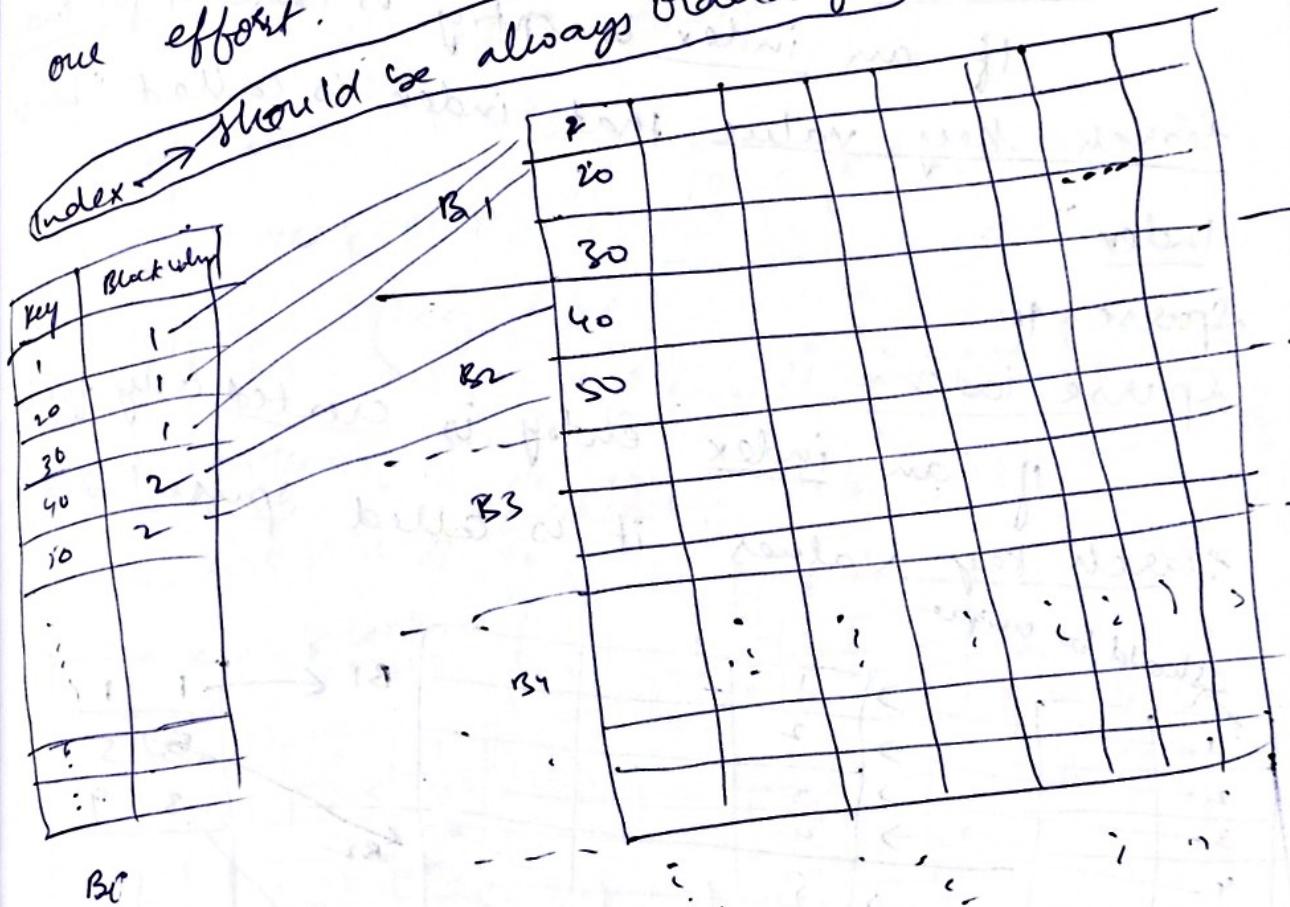


Self explanation

consider you have a large file with many blocks & attributes & searching all the blocks takes huge cost.

so, index is maintained which reduces our effort.

Index  $\rightarrow$  should be always ordered file

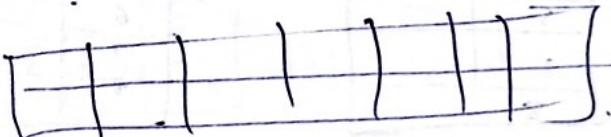


B<sup>0</sup>

$$\Rightarrow (\log_2 B^0)$$

occupies less no of blocks due to only 2 attributes in file

B<sup>50</sup>



( $\log_2 + 1$ ) searches are required

$\log_2$  searches are minimum

$\Rightarrow$  Requires  $(\log_2 B^0 + 1)$   $\Rightarrow$  no of searches

index block access

data block access

## Classification of Indexes:

1. Dense Index

2. Sparse Index

Data should be ordered  
for sparse index

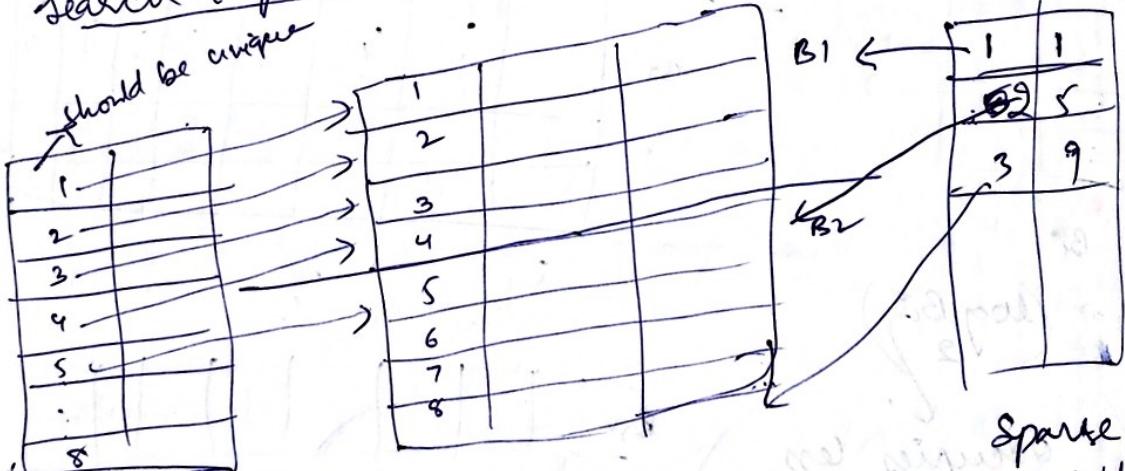
Dense Index:-

If an index  $\Rightarrow$  entry is created for every search key value that index is called "Dense Index"

Sparse :-

Sparse Index:-

If an index entry is created only for some search key values it is called sparse index



dense  
(for every record)  
(we will have index)

Sparse  
(for only in blocks  
we have index)

Primary Index (P.K + Ordered):-

A primary index is an ordered file whose records are of fixed length with two fields, the ~~first~~ first field is same as P.K of data file and the second field is "

pointer to data block where the key is available

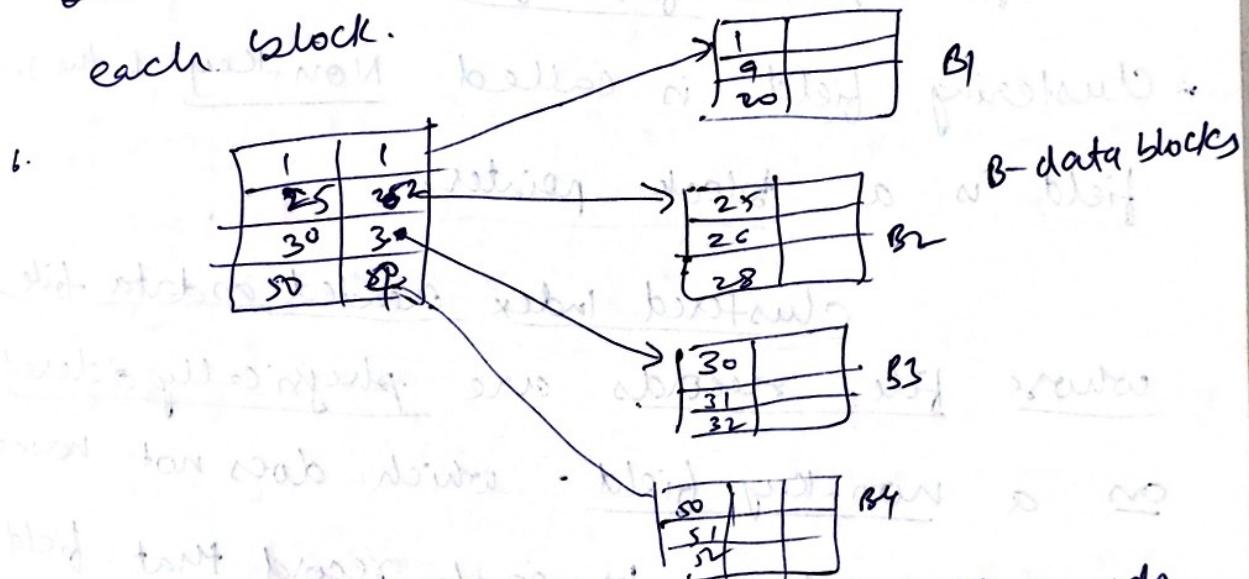
- entry is created for first record of each entry called "block Anchor" (Sparse Index)
- 2. Index block
  - 3. The no of index entries is equal to the no of data blocks

no of block access required

average no of block access

will be  $(\log_2 b + 1)$  → index blocks

4. The type of index is called sparse index because it is indexing only first record of each block.



Ex: Records = 30000; block size = 1024 bytes; unspanned.  
size = 100 bytes; suppose primary index created  
of Key Field of size 9 bytes & block pointer of

6 bytes  $\Rightarrow$  key + block ptr = 6 + 9 = 15 bytes = each record

Find the avg no of block accesses to search for a record using with & without indexing?

sol:- Records  $\approx 30000 \Rightarrow$  blocks  $= \frac{30000}{10} = 3000$

blocks without indexing  $\Rightarrow \lceil \log_2 3000 \rceil \boxed{12}$

Index records / block  $\left\lceil \frac{1024}{15} \right\rceil = 68$

Index records  $\approx 3000$   
 $\Rightarrow$  no of blocks  $\approx$  index blocks  $\approx \frac{3000}{68} \approx 45$

$\Rightarrow$  Avg no of block access  $= \lceil \log_2 45 \rceil + 1$   
(with indexing)  $= \boxed{7}$

clustered Index :- (Non Key + Ordered):-

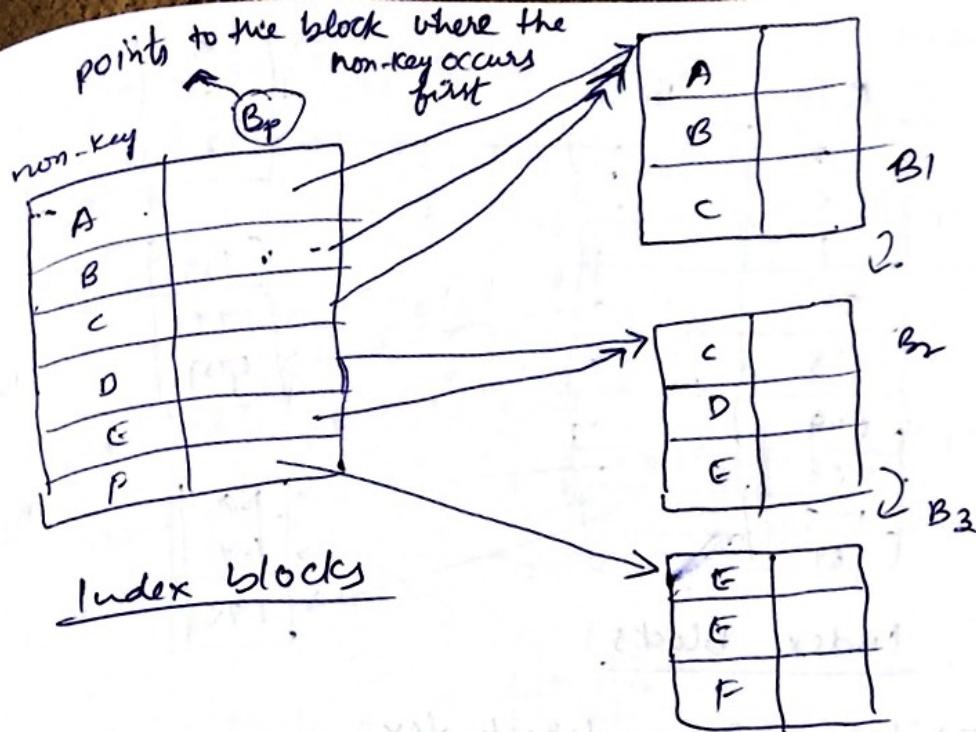
clustered Index is an ordered file with two fields, the first field is same as the clustering field is called Non-key & the second field is a block pointer.

clustered index created on data file  
whose file records are physically ordered on a non-key field which does not have a distinct value for each record that field

Called 'clustering field'

\* Index entry is created for each distinct value of a clustering field

\* the block pointer points to the first block in which the key is available.



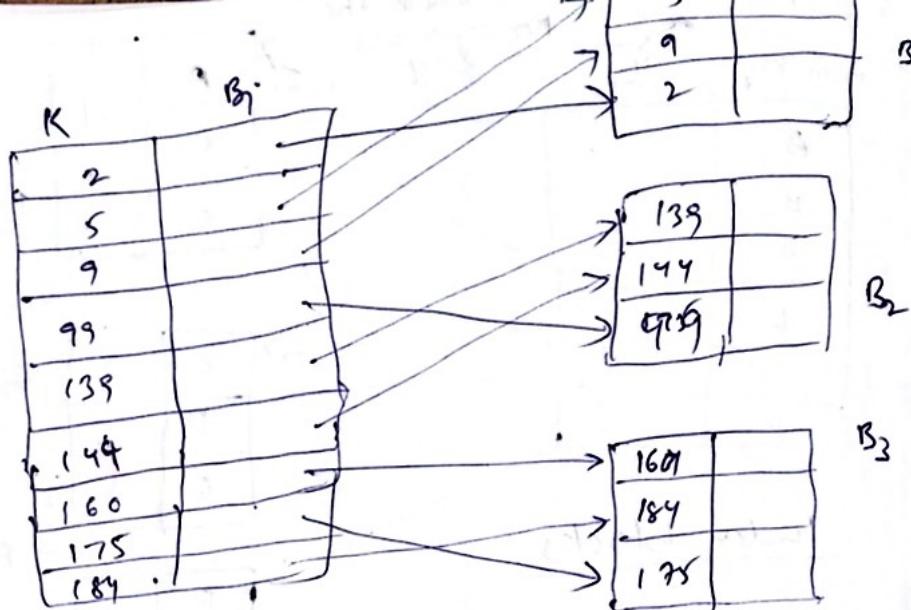
- i) Type of Index is Dense / Sparse
- ii) The average no. of block access using index  

$$= \left( \log_2 B_i + 1 \right)$$

### Secondary Index $(n, k)$ + Unordered :-

- i. Secondary index provides a secondary means of accessing a file for which some primary access already exist.
- ii. Secondary index may be on a non-key
- iii. a candidate key is relative to each record
- iv. Index entry is created for each record in a data file.
- v. No of index entries - No. of records
- vi. Type of secondary index = dense

Ex:-



Index blocks

Q:- consider secondary index  
no. of records = 30,000 ; block size = 1024 bytes ; Records  
unspanned ; Record size = 100 bytes ; Index P.K = 5 bytes  
blk.ptr = 9 bytes ; find the avg. no of blk.  
access with & without indexing

Ans:-

without indexing

without indexing  $\Rightarrow$  linear search  $\Rightarrow$  no of op's  
all the blks should be accessed  
 $\Rightarrow \frac{30000}{10} = 3000$  blocks

$$\text{Avg case} = \frac{\text{best case} + \text{worst case}}{2} = \frac{3001}{2}$$

with indexing

$\Rightarrow$  Index is ordered  
no of records/block  $\Rightarrow \frac{1024}{15} = 68$  records/block

$$\text{dense index} \Rightarrow \text{no. of blks} = \frac{30000}{68} = 442 \text{ blks}$$

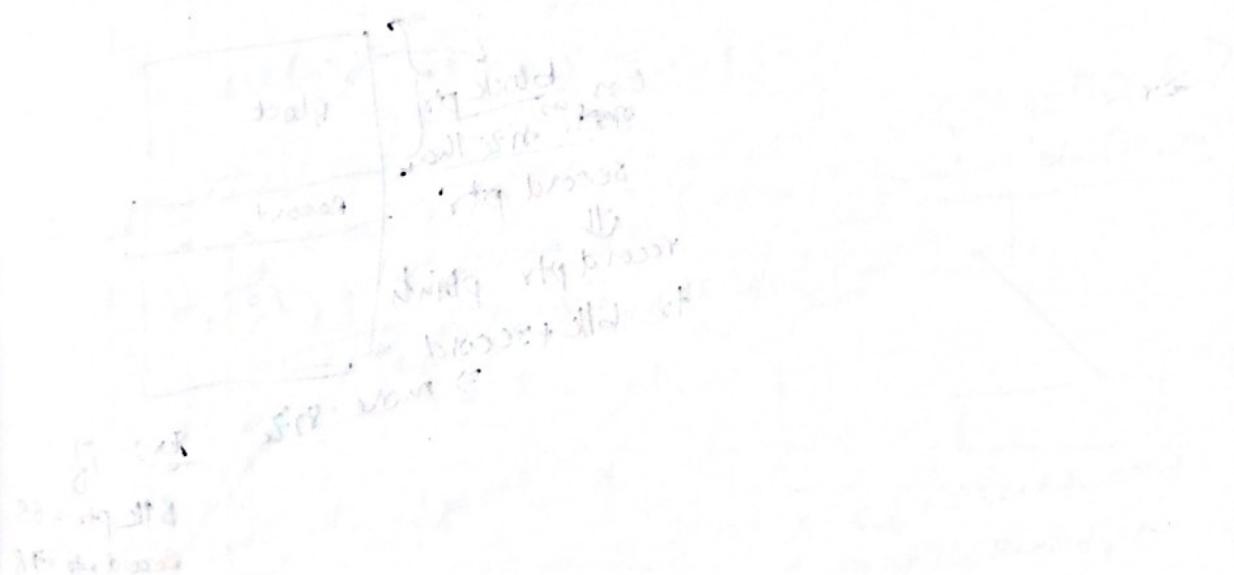
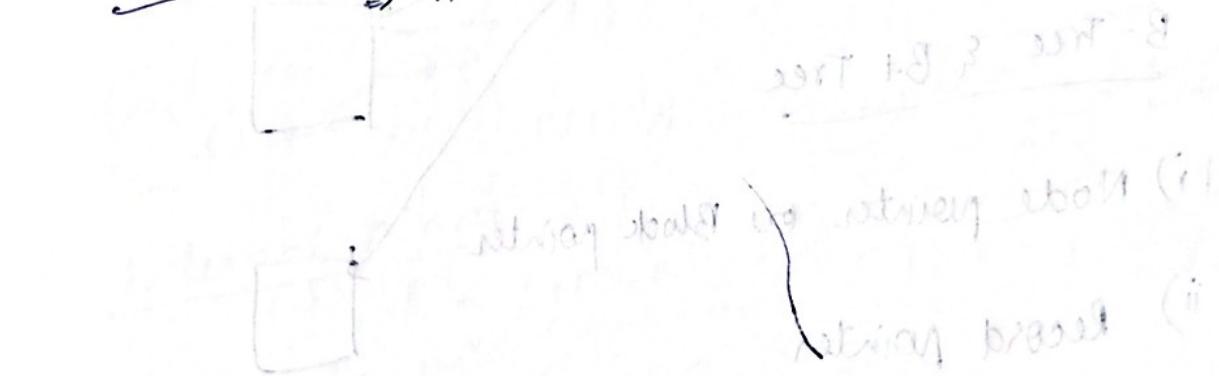
$$\Rightarrow \text{Avg no of blk accesses} = \left( \log_2 \frac{442}{1} + 1 \right)$$

$\Rightarrow$  with indexing  $\frac{10}{15}$  block access

data records =  $16,384 = 2^{14}$ ; Record size = 32 bytes  $\times 2^3$   
 unspanned. If ~~sec~~ block size = 1024 bytes;  
 key field size = 6 B; Blk pte size = 10 B.  
 If secondary index is built on the key field of  
 the file and multi-level index scheme is used  
 the no. of 1st level and 2nd level blocks in  
 multilevel index respectively are?

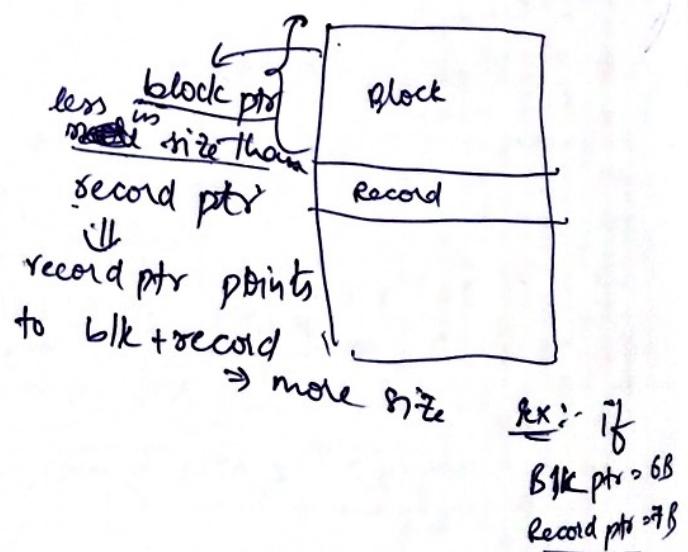
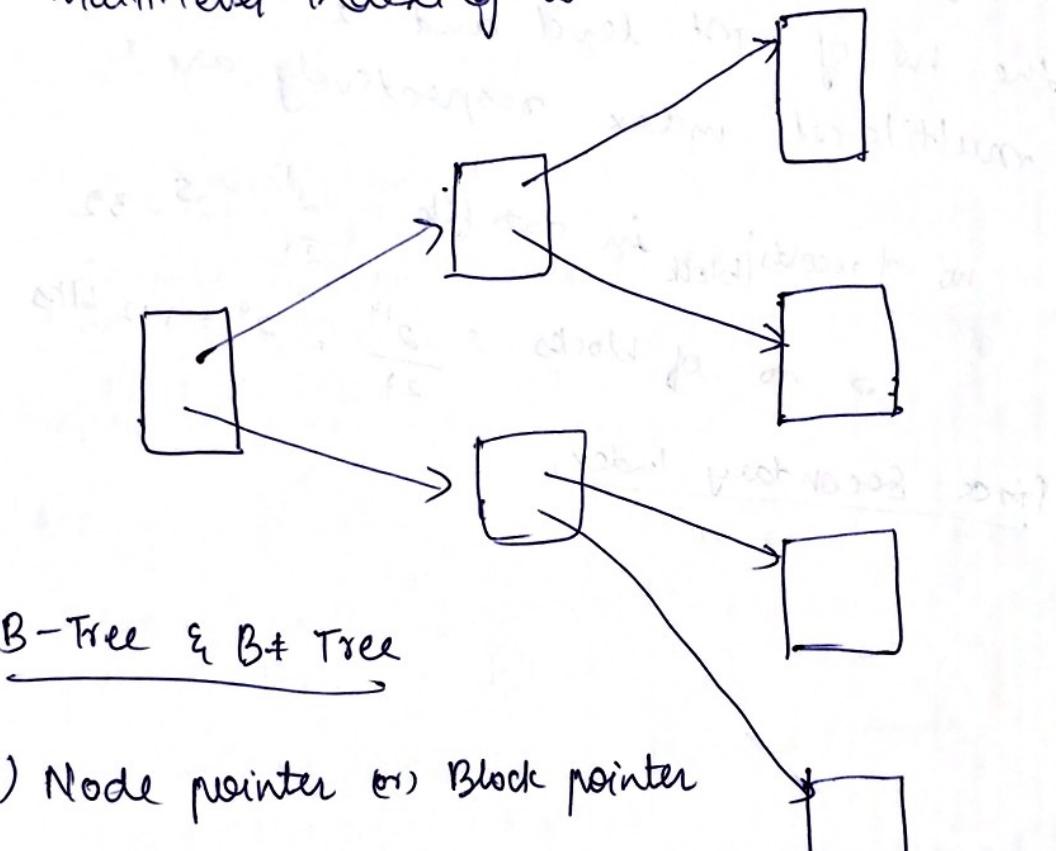
$$\begin{aligned}
 &\text{no. of records/block in data file} = \frac{2^{10}}{2^5} = 32 \\
 &\Rightarrow \text{no. of blocks} = \frac{2^{14}}{2^5} = 2^9 = 512 \text{ b/ks}
 \end{aligned}$$

Since secondary index,  
 $\Rightarrow n$ .



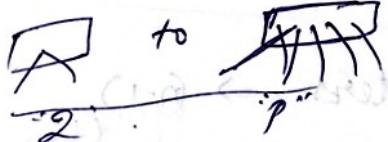
## Introduction to B-trees and B+ Trees

- Generalisation of multi-level indexing
- Dynamic (they can grow & shrink) whereas multi-level indexing is static



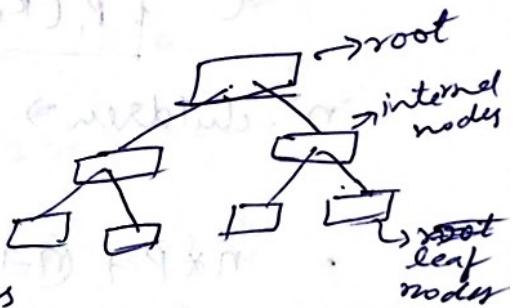
## Properties of B-Trees:-

- 1) Root :- should have children b/w "2" and "p" children

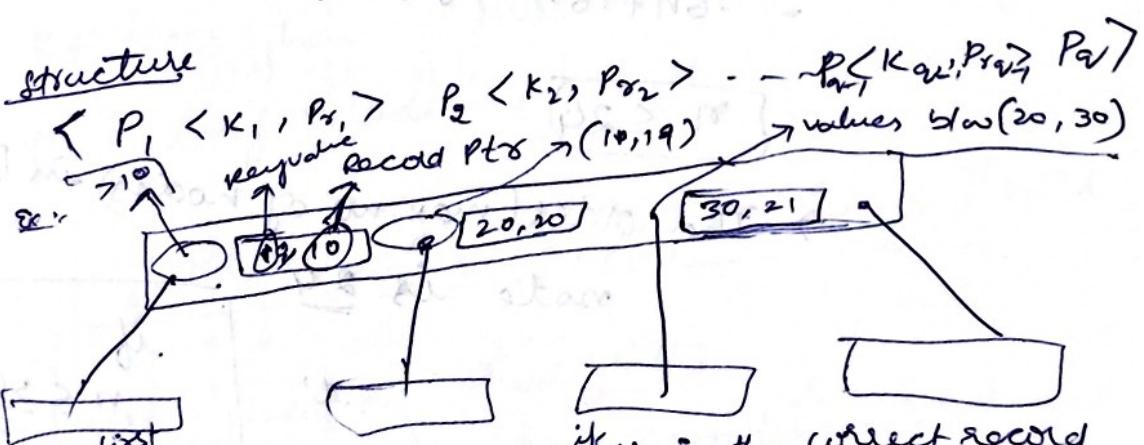


- 2) Internal Nodes :-

I.N. can store upto " $p-1$ " keys  
and have ab/w  $\lceil \frac{p}{2} \rceil$  \* and "p" children



## Ex. structure

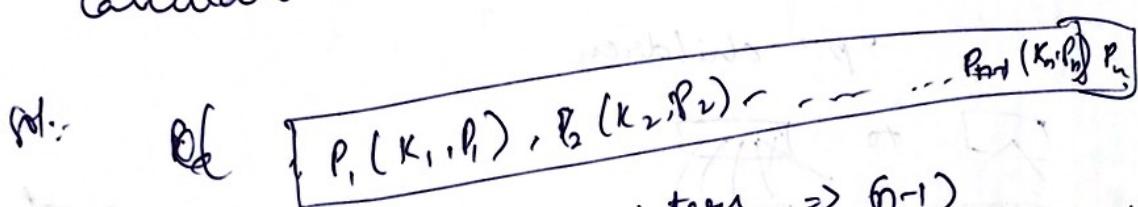


1) At first it checks  $(K_1, P_r)$  and if it is the correct record then it traverses to the record pointed by Record ptr else checks it

### Leaf Node:-

- can store between  $\lceil \frac{(P-1)}{2} \rceil$  and "P-1" keys
- all leaves are at same depth

Q In a B tree, suppose search key is 9 bytes, record length, disk block size is 512 Bytes, record pointer is 7B, block pointer is 6B then calculate the order of B-tree node.



$n$ -children  $\Rightarrow n$ -Blk pointers  $\Rightarrow (n-1)$  (Key, Record P)

$$\begin{aligned} & n \times P + (n-1) (K + RP) \leq \text{block size} \\ & n \times 6 + (n-1) (9+7) \leq 512 \\ & 6n + 16n - 16 \leq 512 \Rightarrow 22n \leq 528 \end{aligned}$$

$$n \leq 24$$

$\Rightarrow$  The order (max no of nodes) in B-tree  
node is 24

if  $n \leq \frac{530}{23}$   
 $\Rightarrow 23.04$   
 $\Rightarrow \lfloor 23 \rfloor \Rightarrow 23$

Suppose that the order of a B-tree is 23.

then how many index records will be stored in a 4-level (including root as 1-level) across the B-tree.

	node	records & index entries	disk pointers
to root	1 node	$22 \text{ IE}$	$23 \text{ DP}$
L1	23 nodes	$23 \times 22 \text{ IE}$	$23 \times 23 \text{ DP}$
L2	$23 \times 23$ nodes	$23 \times 23 \times 22 \text{ IE}$	$23 \times 23 \times 23$
L3	$23 \times 23 \times 23$ nodes	$23 \times 23 \times 23 \times 22 \text{ IE}$	"0" null in leaf

The max no. of index entries in 4-level B tree where order = 23  $\geq 2^3$

$$(22 + 23 \times 22 + 23 \times 23 \times 22 + 23^3 \times 22)$$

$$= 22(1 + 23 + 23^2 + 23^3)$$

$$= 22(23^4 - 1) = 6156480$$

B+ trees have index pointers only in the leaf nodes.

## Overflow & Underflow In B Trees

- Insert - Overflow (node full)
- Delete - Underflow (node doesn't have what required to delete)

order - B-tree - "P"

Root:-

min

2 tree  
key

pointers  
entry



max

"P" tree pointers  
(P-1) key entries

Internal Nodes:-

min

[P/2] tree pointers

[P/2] - 1 key entries

max

P - tree pointers  
(P-1) - key entries

Leaf Nodes:-

min - [P/2] - 1 key entries

max - 2 (P-1)

Ex:-

Order of B-tree is 5: calculate min & max

in each type of node of tree.

Root:-

min 2 TP

1 KE

max: 5 TP

4 KE

Internal:

min - 3 TP

2 KE

max: 5 TP

4 KE

leaf:-

min 2 KE

delete

underflow

merge two nodes  
into one

if (7)  
then overflow

split the  
node

Insert the following keys in B-tree of order-4  
 Keys: 2, 5, 10, 1, 6, 9, 4, 3, 12, 18, 20, 25

Root:  
min

2 TP  
 1 KE

max: 4TP  
 3KE

Internal nodes  
min

2 TP  
 1 KE

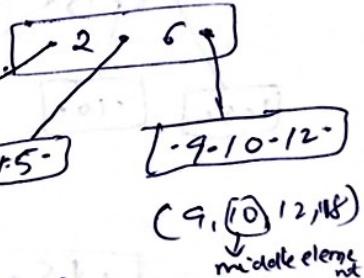
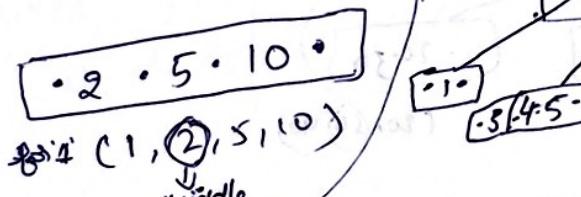
max: 4TP  
 3KE

Leaf Nodes  
min: 1KE

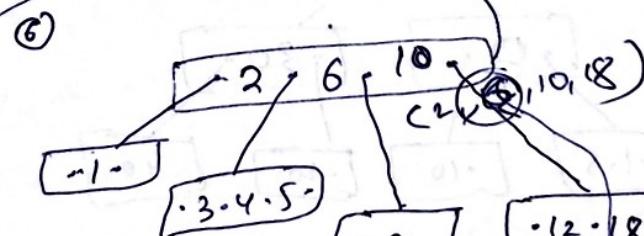
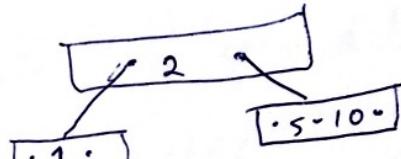
max: 3KE

condns: - If overflow occurs break the node  
 into two & take the middle key to the top  
 if underflow occurs combine the two nodes & make  
 it to one & too

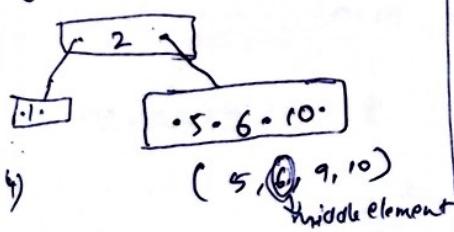
Steps:- ①



②

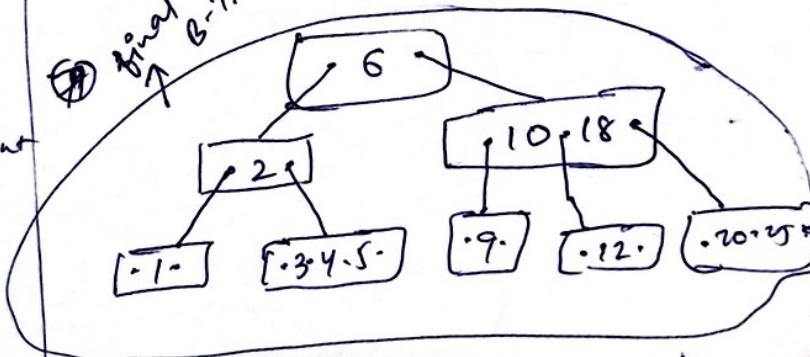


③



④

final B-tree



Q Construct a B-tree of order '3', for the keys

20, 15, 10, 5, 8, 30, 1, 40.

Root: min:  $\frac{2}{3}$  TP  
1 KE

max: 3 TP  
2 KE

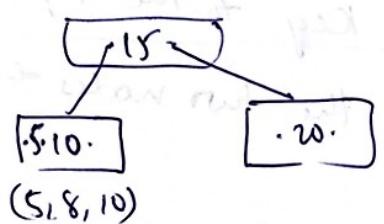
Internal node: min: 2 TP  
 $\left[\frac{P}{2}\right] - 1$  KE

max: 3 TP  
2 KE  
2 KE

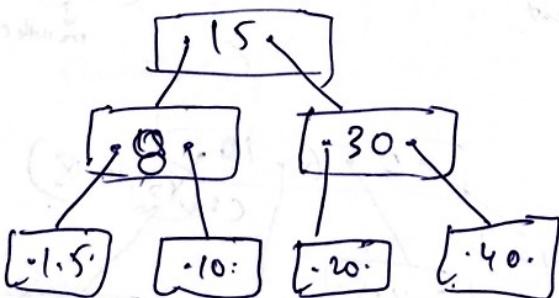
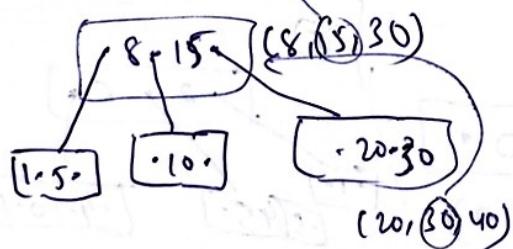
Leaf Node: min: 1 KE

①

15.20.  
(10, 15, 20)

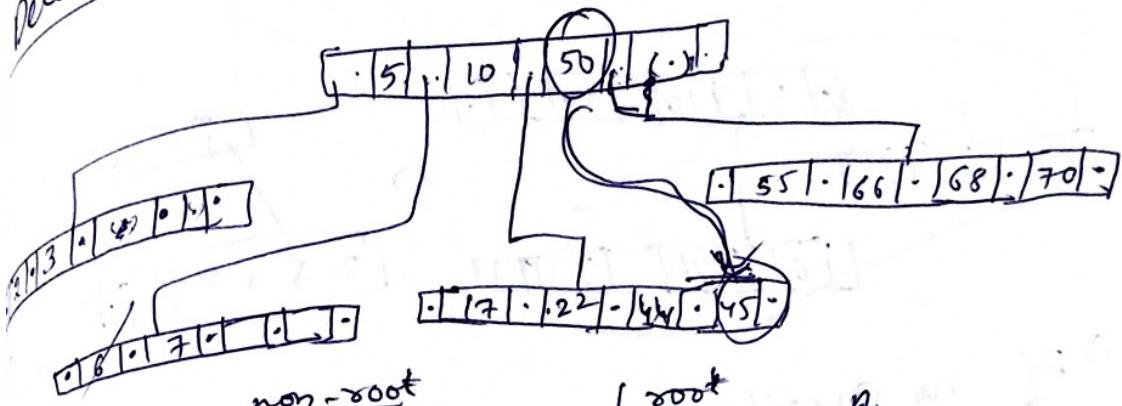


②



Final B-tree

# Deletion from a B-tree



$$P=5; \quad \begin{cases} \text{max keys} = 4 \\ \text{min keys} = 2 \end{cases} \quad \begin{cases} \text{root} \\ \text{max } k - q \\ \text{min } k - 1 \end{cases}$$

In B-trees deletion should occur at the leaf

- if not we will make it to occur at the  
leaf level & delete it and check for the  
underflow

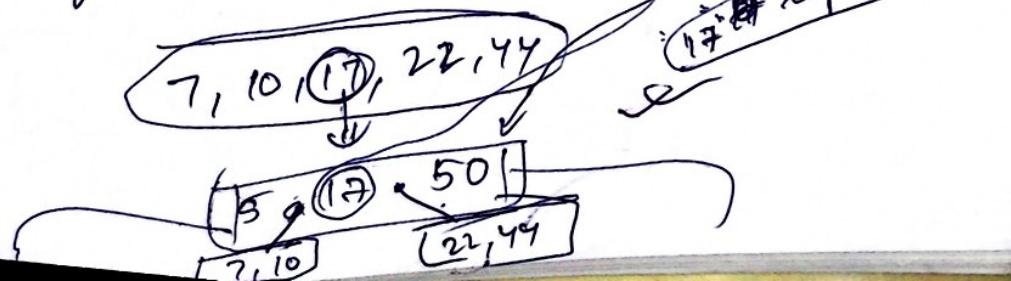
underflow

like for '50', if we want to delete, we take either in-order predecessor (or) in-order successor replace it and delete it & check for underflow.

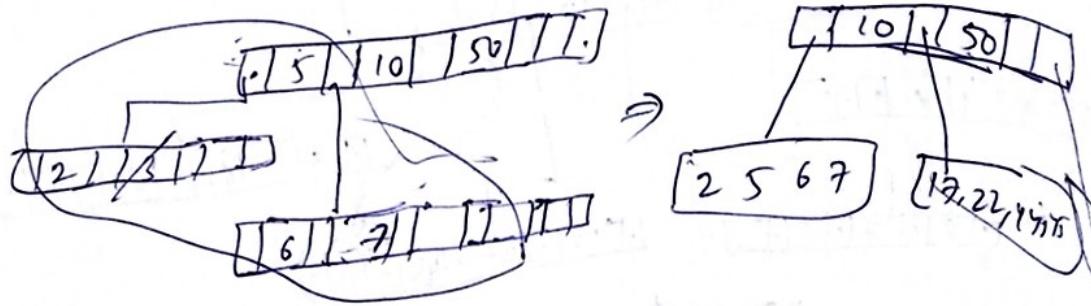
ii- if you delete "6", we get underflow with  
we merge the node which has underflow with

most populous sibling (only on both sides)  $\leftarrow$   
nodes  $T_{\{5(0), 50\}}$

re-arrange & into two nodes

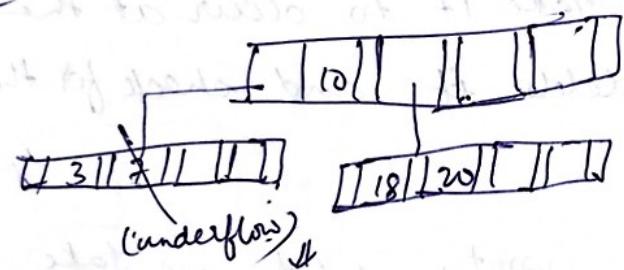


2) when you are deleting

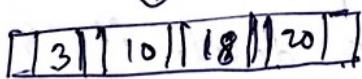


→ If no overflow occurs, then remove key in parent & merge into a single node

Ex 3



$(3, 10, 18, 20) \Rightarrow$  underflow in root  $\Rightarrow$  no need of another level



B+ Trees

## File Organisation



Db is a collection of files  
 files " " " of Records  
 Records " " " of attributes

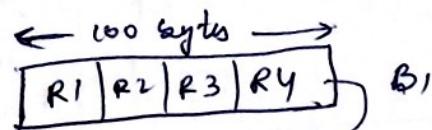
### Blocking factor:

average no of records , that can be kept  
 in a block (per block)

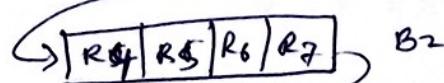
Strategies to store file into blocks :  
(of records)

#### 1) Spanned Strategy :

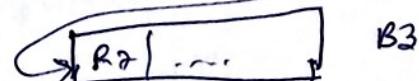
It allows partial part of record can be stored in a block



adv: no wastage of mem



disadv: Block access increases



Suitable: Variable length record

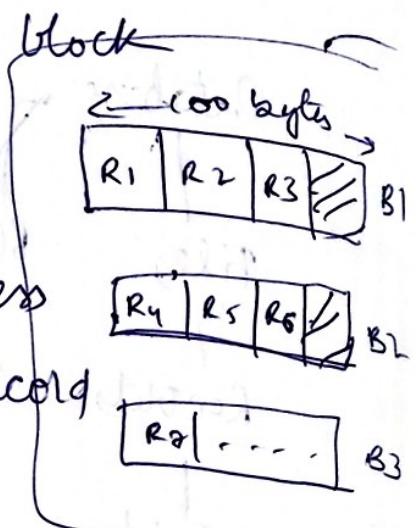
## Unspanned Strategy

entire record in a single block

disadv: waste of memory

adv: reduces block access

suitable: for fixed length record



## Organisation of records in a file :

### Ordered file Organisation

Continuation after fix & concurrency