

## Appendix: HQF-DE Implementation Details

### A System Architecture

Figure 1 shows the overall HQF-DE system architecture with the four document variants flowing through both retrieval paths.

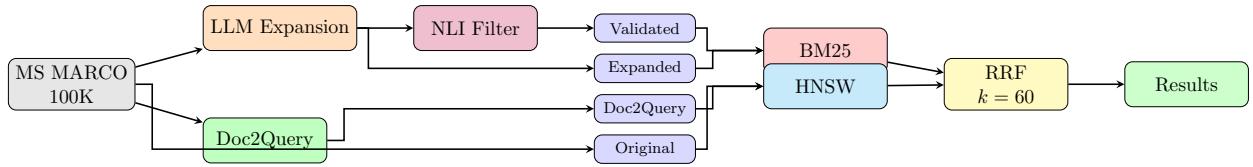


Figure 1: HQF-DE system architecture: document expansion variants flow through dual retrieval paths.

### B Pipeline Stages

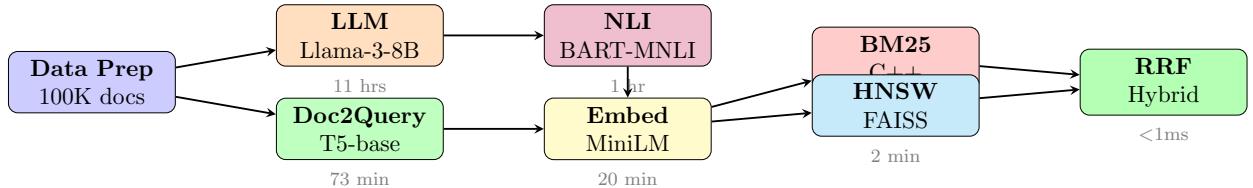


Figure 2: Pipeline stages with processing times. GPU stages run on Colab A100; CPU stages run locally.

### C Infrastructure Adaptation

Due to GPU memory constraints on local hardware, we adopted a hybrid execution approach.

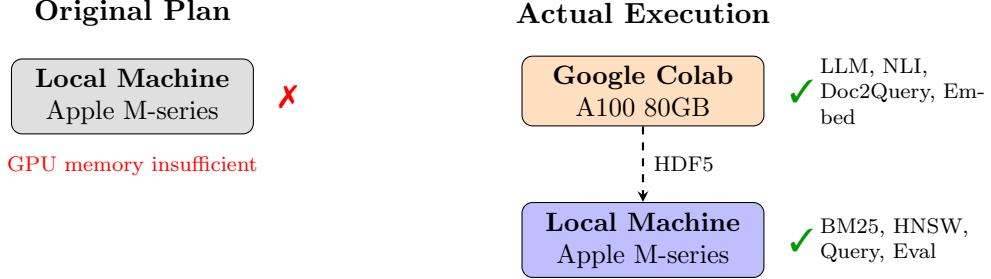


Figure 3: Infrastructure adaptation: GPU tasks on Colab, CPU tasks locally.

Table 1: Time and Space Complexity of Key Components

Component	Time	Space
BM25 Indexing	$O(N \cdot L)$	$O(V + P)$
BM25 Query	$O(\sum_t  L_t )$	$O(k)$
HNSW Construction	$O(N \log N \cdot M)$	$O(N \cdot M \cdot \log N)$
HNSW Query	$O(\log N + k \cdot ef)$	$O(ef)$
RRF Fusion	$O(k_1 + k_2)$	$O(k_1 + k_2)$

$N = \text{docs}$ ,  $L = \text{doc length}$ ,  $V = \text{vocab}$ ,  $P = \text{postings}$ ,  $|L_t| = \text{posting list}$ ,  $M = \text{connections}$ ,  $ef = \text{beam width}$

## D Complexity Summary

## E Complete Results

### E.1 HNSW Dense Retrieval

### E.2 BM25 Sparse Retrieval

### E.3 Hybrid Retrieval (RRF)

## F Key Findings Visualization

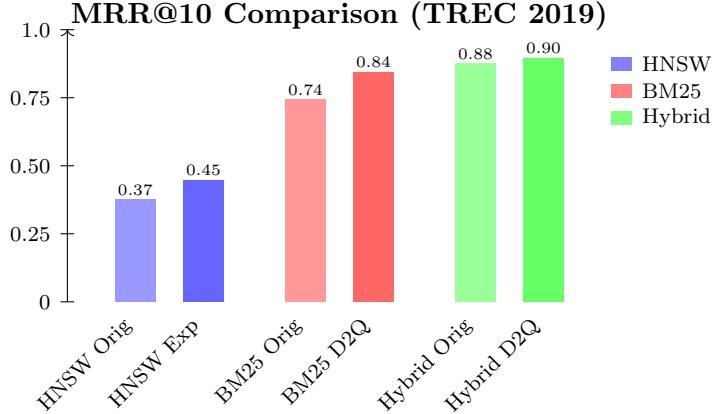


Figure 4: MRR@10 comparison. Hybrid + Doc2Query achieves best performance (0.90).

Table 2: HNSW Results (MRR@10 / nDCG@10 / Recall@100)

Variant	TREC 2019	TREC 2020	Dev Set
Original	0.374 / 0.154 / 0.485	0.275 / 0.105 / 0.551	0.011 / 0.002 / 0.876
Expanded	<b>0.447 / 0.154 / 0.471</b>	0.273 / 0.094 / 0.550	0.012 / 0.003 / 0.866
Validated	0.381 / 0.149 / 0.472	0.267 / 0.092 / 0.551	0.013 / 0.004 / 0.869
Doc2Query	0.305 / 0.134 / 0.472	<b>0.307 / 0.085 / 0.540</b>	0.013 / 0.003 / 0.865

Table 3: BM25 Results (MRR@10 / nDCG@10 / Recall@100)

Variant	TREC 2019	TREC 2020	Dev Set
Original	0.744 / 0.419 / 0.568	0.688 / 0.428 / 0.590	0.689 / 0.712 / 0.933
Expanded	0.752 / 0.428 / 0.579	0.713 / 0.412 / 0.602	0.658 / 0.685 / 0.908
Validated	0.736 / 0.415 / 0.578	0.703 / 0.411 / 0.601	0.662 / 0.689 / 0.911
Doc2Query	<b>0.844 / 0.492 / 0.596</b>	<b>0.741 / 0.465 / 0.628</b>	<b>0.746 / 0.767 / 0.944</b>

## G Expansion Method Comparison

LLM Expansion	Doc2Query
Best for: Dense retrieval Gain: +19% MRR (HNSW) Time: 11 hours	Best for: BM25 & Hybrid Gain: +13% MRR (BM25) Time: 73 minutes

### Recommendation

Use Doc2Query for production  
(faster, better for BM25/Hybrid).  
Use LLM expansion for dense-only retrieval.

Figure 5: Expansion method comparison with practical recommendations.

Table 4: Hybrid Results (MRR@10 / nDCG@10 / Recall@100)

Variant	TREC 2019	TREC 2020	Dev Set
Original	0.877 / 0.475 / 0.594	0.757 / 0.431 / 0.641	0.701 / 0.730 / 0.945
Expanded	0.810 / 0.459 / 0.588	0.723 / 0.412 / 0.636	0.676 / 0.707 / 0.923
Validated	0.810 / 0.451 / 0.587	0.719 / 0.410 / 0.635	0.680 / 0.709 / 0.926
Doc2Query	<b>0.896 / 0.512 / 0.613</b>	<b>0.779 / 0.468 / 0.653</b>	<b>0.762 / 0.783 / 0.951</b>