



★ A.P ★ T.S ★ KARNATAKA ★ TAMILNADU ★ MAHARASTRA ★ DELHI ★ RANCHI

A right Choice for the Real Aspirant
ICON Central Office - Madhapur - Hyderabad

SEC: Sr.Super60_STERLING BT**Time: 09:00AM to 12:00PM****JEE-MAIN****QMT-12****Date: 05-07-2025****Max. Marks: 300****KEY SHEET****MATHEMATICS**

1	1	2	3	3	1	4	3	5	4
6	1	7	3	8	2	9	3	10	2
11	3	12	1	13	3	14	1	15	2
16	1	17	4	18	1	19	2	20	2
21	238	22	16	23	54	24	80	25	7

PHYSICS

26	1	27	1	28	4	29	3	30	3
31	1	32	1	33	2	34	4	35	1
36	3	37	1	38	1	39	1	40	2
41	3	42	3	43	1	44	1	45	1
46	1	47	130	48	34	49	120	50	10

CHEMISTRY

51	3	52	3	53	3	54	2	55	2
56	2	57	3	58	2	59	2	60	4
61	2	62	3	63	4	64	4	65	2
66	1	67	1	68	1	69	4	70	4
71	69	72	7	73	0	74	2	75	7



SOLUTIONS MATHEMATICS

1. $f'(x) = 16x - \frac{1}{x}$

$$f'(x) = 0 \Rightarrow x = \frac{1}{4}$$

$$\therefore a = \frac{1}{4}$$

$$\begin{array}{r} - \\ 0 \end{array} \quad \begin{array}{r} + \\ 1/4 \end{array} \quad \begin{array}{r} 4 \end{array}$$

Let (x_1, y_1) be any point on parabola $y^2 = 2x$ diff.

w.r.t. x

$$y' = \frac{1}{y_1} = m_T$$

$$\therefore \frac{1}{y_1} = \frac{3-y_1}{4-x_1} \Rightarrow \frac{1}{y_1} = \frac{3-y_1}{4-\frac{y_1^2}{2}} \Rightarrow 8 - y_1^2 = 6y_1 - 2y_1^2 \Rightarrow y_1^2 - 6y_1 + 8 = 0 \Rightarrow y_1 = 2, 4$$

Point is P (2, 2) or (8, 4)

Tangent at (2, 2) is

$$y - 2 = \frac{1}{2}(x - 2)$$

As (-2, 0) satisfies \Rightarrow Reject

P (8, 4)

Normal at P (8, 4) is

$$y - 4 = -4(x - 8) = -4x + 32 \Rightarrow 4x + y = 36$$

2. P) If the required image is (x, y, z) then

$$\frac{x-3}{2} = \frac{y-5}{1} = \frac{z-7}{1} = \frac{-2(6+5+7+18)}{2^2 + 1^2 + 1^2} = -12$$

Or $(x, y, z) \equiv (-21, -7, -5)$

Q) point on line is of the form $(2-3\lambda, 1-2\lambda, 3+2\lambda)$

$$\Rightarrow 2(2-3\lambda) + (1-2\lambda) - (3+2\lambda) - 3 = 0 \Rightarrow \lambda = -\frac{1}{10}$$

$$\Rightarrow \text{required point is } \left(\frac{23}{10}, \frac{6}{5}, \frac{14}{5} \right)$$

R) If (x, y, z) is the required foot of the perpendicular, then

$$\frac{x-1}{2} = \frac{y-1}{-2} = \frac{z-2}{4} = \frac{-(2-2+8+5)}{2^2 + (-2)^2 + 4^2}$$

$$\text{Or } (x, y, z) \equiv \frac{-1}{12}, \frac{25}{12}, \frac{-2}{12}$$

S) Any point on the line



$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} = \lambda$$

Is $P(2\lambda+1, 3\lambda+2, 4\lambda+3)$ which satisfies the line

$$\frac{x-4}{5} = \frac{y-1}{2} = \frac{z}{1}$$

$$\text{Or } \frac{2\lambda+1-4}{5} = \frac{3\lambda+2-1}{2} = \frac{4\lambda+3}{1}$$

$$\text{Or } \lambda = -1$$

The required point is $(-1, -1, -1)$

3. Eccentricity of ellipse $e_1 = \sqrt{1 - \frac{16}{25}} = \frac{3}{5}$

$$\text{Foci} = (\pm ae, 0) = (\pm 3, 0)$$

For hyperbola

$$\text{Eccentricity } e_2 = \frac{5}{3}$$

Semi-transverse axis $\rightarrow a = 3$

$$b^2 = a^2(e^2 - 1) = 9 \left(\frac{25}{9} - 1 \right) = 16$$

Equation of hyperbola

$$\frac{x^2}{9} - \frac{y^2}{16} = 1$$

4. Differentiate w.r.t x

$$f'(x) + \frac{f(x)}{x} = \frac{1}{2\sqrt{x+1}}$$

$$I.E. = e^{\int \frac{1}{x} dx} = e^{\ln x} = x$$

$$xf(x) = \int \frac{x}{2\sqrt{x+1}} dx$$

$$x+1 = t^2$$

$$= \int \frac{t^2 - 1}{2t} 2tdt$$

$$xf(x) = \frac{t^3}{3} - t + c$$

$$xf(x) = \frac{(x+1)^{3/2}}{3} - \sqrt{x+1} + c$$

Also putting x = 3 in given equation $f(3) + 0 = \sqrt{4}$

$$f(3) = 2 \Rightarrow C = 8 - \frac{8}{3} = \frac{16}{3}$$



$$f(x) = \frac{\frac{(x+1)^{\frac{3}{2}}}{3} - \sqrt{x+1} + \frac{16}{3}}{x}$$

$$f(8) = \frac{9-3+\frac{16}{3}}{8} = \frac{34}{24} \Rightarrow 12f(8) = 17$$

5. $3-x = \frac{x^2+3}{2} \Rightarrow x = 1, -3$

$$-x+1 = \frac{x^2+3}{2} \Rightarrow x = -1$$

$$\text{Area } A = 2\sqrt{2} \times \sqrt{2} - 2 \left(\int_0^1 \left((3-x) - \left(\frac{x^2+3}{2} \right) \right) dx \right)$$

$$A = \frac{7}{3}$$

6. $= 24 \int_0^{\frac{\pi}{48}} -\sin\left(4x - \frac{\pi}{12}\right) + \int_{\pi/48}^{\pi/4} \sin\left(4x - \frac{\pi}{12}\right) dx$

$$+ \int_0^{\frac{\pi}{6}} [0] dx + \int_{\pi/6}^{\pi/4} [2 \sin x] dx = 24 \left[\frac{\left(1 - \cos \frac{\pi}{2}\right)}{4} - \frac{\left(-\cos \frac{\pi}{12} - 1\right)}{4} \right] + \frac{\pi}{4} - \frac{\pi}{6}$$

$$= 24 \left(\frac{1}{2} + \frac{\pi}{12} \right) = 2\pi + 12 = \alpha = 12$$

7. $y = mx + \frac{2}{m} \Rightarrow m^2 x - my + 2 = 0$

Centre of circles is $(6, 0)$, $r = \sqrt{32}$

$$\left| \frac{6m^2 + 2}{r1 + m^4} \right| = \sqrt{32} \Rightarrow 4(3m^2 + 1)^2 = 32(1 + m^4) \Rightarrow m = \pm 1$$

Perpendicular tangent meet on directrix

Equation of directrix is $x = -2 \therefore P(-2, 0)$

Ans. = 4

8. $x_1 x_2 x_3 x_4 x_5 = 1050 = 2 \times 3 \times 5^2 \times 7$

Thus 5^2 can assign in ${}^5C_1 + {}^5C_2 = 15$ ways

We can assign 2, 3 or 7 to any of 5 variables

Hence req. number of solutions = $5 \times 5 \times 5 \times 15 = 1875$

9. 210 can be factorized as $210 = 2 \times 3 \times 5 \times 7$. All the factors are primes. Clearly any number can be assigned to x_i 's in 4 ways. Hence total ways of assigning the factors to x_i 's are 4^4 . Now for a particular positive integral solution, we have 4C_2 solution when



any two x_i 's become negative, and all the four solutions can be negative in 4C_4 ways.

$$\text{Hence total number of integral solutions } 2\cos^{-1}x - \sin^{-1}(2x+1) = \frac{3\pi}{2}$$

10. $2\cos^{-1}x - \sin^{-1}(2x+1) = \frac{3\pi}{2}$

$$\cos^{-1}x = \alpha, \sin^{-1}(2x+1) = \beta$$

$$2\alpha = \frac{3\pi}{2} + \beta$$

$$\cos 2\alpha = \sin \beta$$

$$2x^2 - 1 = 2x + 1$$

$$x^2 - x - 1 = 0$$

$$x = \frac{1 - \sqrt{5}}{2}$$

$$4x^2 - 4x = 4$$

11. $|[\vec{a} \quad \vec{b} \quad \vec{c}]| = 30$

$$|abc \sin \theta \cos \phi| = 30 \Rightarrow \theta = \frac{\pi}{2}, \phi = 0 \Rightarrow \vec{a}, \vec{b}, \vec{c} \text{ are mutually perpendicular}$$

$$(2\vec{a} + \vec{b} + \vec{c}) \cdot [(\vec{a} \times \vec{c}) \times (\vec{a} - \vec{c}) + \vec{b}] = (2\vec{a} + \vec{b} + \vec{c}) \cdot [a^2 \vec{c} + c^2 \vec{a} + \vec{b}]$$

$$= 50a^2 + b^2 + 4c^2 = 200 + 9 + 100 = 309$$

$$\frac{k}{103} = \frac{309}{103} = 3$$

12. ASSASSINATION contains 4S, 3A, 2I, 2N, and one each of T and O. Four letters can be selected in following ways
 1) all four identical in 1 ways.

2) Three identical and one different letter (e.g. AAAN) in ${}^2C_1 \times {}^5C_1 = 10$ ways

3) Two identical of one kind and two identical of another kind (eg. SSNN) in ${}^4C_2 = 6$ ways

4) Two identical and other two different (e.g IIINT) in ${}^4C_1 \times {}^5C_2 = 40$ ways

Total number of ways = $1 + 10 + 6 + 40 + 15 = 72$

5) All four different letters is ${}^6C_4 = 15$ ways

13. $x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 = 12, x_i \in \{1, 2, 3, 4\}$

Number of solutions

$$= \text{coefficient of } x^{12} \text{ in } (x + x^2 + x^3 + x^4)^7$$

$$= \text{coefficient of } x^{12} \text{ in } x^7 (1 + x + x^2 + x^3)^7$$

$$= \text{coefficient of } x^5 \text{ in } \left(\frac{1 - x^4}{1 - x} \right)^7$$



$$=\text{coefficient of } x^5 \text{ in } (1-x^4)^7(1-x)^{-7}$$

$$=\text{coefficient of } x^5 \text{ in } (1-7x^4)(1+7c_1x+8c_2x^2+\dots+^{11}c_5x^5+\dots)$$

$$=^{11}c_5x^5 - 7x^7c_1 = 462 - 49 = 413$$

- 14.** Number of quadrilaterals having no side is common with the sides of the polygon.

$$={}^nC_4 - n({}^{n-5}C_2) - \frac{3}{2}n(n-5) - n. \text{ Substitute } n = 10.$$

- 15.** Each group contains 5 teams

$$\text{In the first round the number of matches} = {}^5C_2 + {}^5C_2 = 10 + 10 = 20$$

$$\text{The number of matches in quarterfinals} = {}^6C_2 = \frac{6 \times 5}{2} = 15$$

$$\text{The number of matches in semifinals} = {}^4C_2 = \frac{4 \times 3}{2} = 6$$

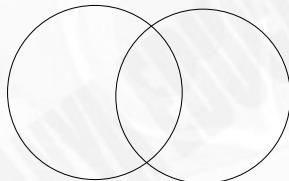
$$\text{In finals, the minimum number of matches} = 2$$

$$\text{So, required ways} = 20 + 15 + 6 + 2 = 43$$

- 16.** Given circles = 6, straight lines = 6

Case(i) \rightarrow for circles

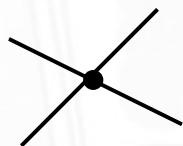
Two circles intersect at two different points



$$\text{For 6 circle we have } {}^6C_2 \times 2 = \frac{6 \times 5}{2 \times 1} \times 2 = 30$$

Case(ii) \rightarrow for straight lines

Two straight lines intersect at one point



$$\text{For 6 straight lines } {}^6C_2 \times 1 = 15$$

Case(iii) \rightarrow one circle & one straight lines

One circle & one line intersect at two different points



$$\text{So we have } {}^6C_1 \times {}^6C_1 \times 2 = 6 \times 6 \times 2 = 72$$



17. $x + y + z + w = 15, x \geq 0, y > 5, z \geq 2, w \geq 1$

$$x + y - 6 + z - 2 + w - 1 = 6, y \geq 6$$

$$N = {}^{6+4-1}C_{4-1}$$

18. Given $y+z = 5$ (i)

$$\text{and } \frac{1}{y} + \frac{1}{z} = \frac{5}{6}, y > z \quad \dots \text{ (ii)}$$

Solving (i) and (ii), we get $y=3, z=2 \Rightarrow n = 2^x \cdot 3^3 \cdot 5^2 = (2.2.2....)(3.3.3)(5.5)$

\therefore Number of odd divisors

$$= (3+1)(2+1) = 4 \times 3 = 12$$

19. $(b) |A| = m - n$

$$\text{And } 4m + n = 22 \Rightarrow n = 22 - 4m$$

$$\text{Also, } 17m + 4n = 93$$

$$\Rightarrow m = 5$$

$$\therefore n = 22 - 4 \times 5 = 2$$

$$|A| = m - n = 5 - 2 = 3$$

$$\text{Det det}(n \text{adj}(\text{adj}(mA))) = 3^a 5^b 6^c$$

$$= n^m [\det(mA)]^{(m-1)^2} = n^m (m^m \det(A))^{(m-1)^2} = n^m \cdot m^{m(m-1)^2} (|A|)^{(m-1)^2}$$

$$\therefore n = 2, m = 5 \text{ and } |A| = 3$$

$$\therefore 2^5 \cdot 5^{5(5-1)^2} (3)^{(5-1)^2} = 2^5 \cdot 5^{5 \times 4^2} (3)^{4^2} = 2^5 \cdot 5^{80} \cdot 3^{16} = 2^5 \times 3^5 \times 3^{11} \times 5^{80} = 3^{11} \times 5^{80} \times 6^5 = 3^a 5^b 6^c$$

20. $\frac{1}{x} + \frac{1}{y} = \frac{1}{n} \Rightarrow (x-n)(y-n) = n^2$

No. of divisors of n^2 is equal to number of pairs but if n is prime then no of divisors of n^2 is 3

21. Conceptual

22. $(1 + \sin^4 x)(2 + \cot^2 y)(4 + \sin 4z) \leq 12 \sin^2 x$

$$\Rightarrow (\sin^2 x + \operatorname{cosec}^2 x)(2 + \cot^2 y)(4 + \sin 4z) \leq 12$$

Now, $\sin^2 x + \operatorname{cosec}^2 x \geq 2, 2 + \cot^2 y \geq 2, 4 + \sin 4z \geq 3$

$$\Rightarrow \sin^2 x = 1, \cot^2 y = 0, \sin 4z = -1 \Rightarrow x = \frac{\pi}{2}, \frac{3\pi}{2}, y = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$z = \frac{3\pi}{8}, \frac{11\pi}{8}, \frac{15\pi}{8}, \frac{7\pi}{8}$$

Number of triplets = $2 \times 2 \times 4 = 16$

23. $(1 + 2x - 3x^2) \left(\frac{3}{2}x^2 - \frac{1}{3x} \right)^9$

$$\text{General term} = \left(\frac{3}{2}x^2 - \frac{1}{3x} \right)^9 = {}^9C_r \cdot \frac{3^{9-2r}}{2^{9-r}} (-1)^r \cdot x^{18-3r}$$



Put $r = 6$ to get coef. Of $x^0 = {}^9C_6 \cdot \frac{1}{6^3} \cdot x^0 = \frac{7}{18} x^0$

Put $r = 7$ to get coeff. Of $x^{-3} = {}^9C_7 \cdot \frac{3^{-5}}{2^2} \cdot (-1)^7 \cdot x^{-3} = -{}^9C_7 \cdot \frac{1}{3^5 \cdot 2^2} \cdot x^{-3} = \frac{-1}{27} x^{-3}$

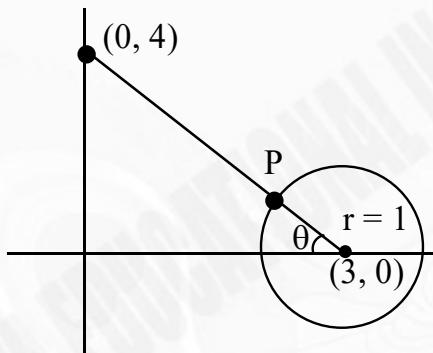
$$\frac{7}{18} + \frac{3}{27} = \frac{7}{18} + \frac{1}{9} = \frac{7+2}{18} = \frac{9}{18} = \frac{1}{2}$$

$$108 \cdot \frac{1}{2} = 54$$

24. Here $|z - 3| < 1 \Rightarrow (x - 3)^2 + y^2 < 1$

And $z = (4 + 3i) + \bar{z}(4 - 3i) \leq 24 \Rightarrow 4x - 3y \leq 12$

$$\tan \theta = \frac{4}{3}$$



Coordinate of $P = (3 - \cos \theta, \sin \theta) = \left(3 - \frac{3}{5}, \frac{4}{5} \right)$

$$\alpha + i\beta = \frac{12}{5} + \frac{4}{5}i$$

$$25(\alpha + \beta) = 80$$

25. $\int \frac{1}{\sqrt[5]{(x-1)^4(x+3)^6}} dx = A \left(\frac{\alpha x - 1}{\beta x + 3} \right)^B + C$

$$I = \int \frac{1}{(x-1)^{4/5}(x+3)^{6/5}} dx = \quad I = \int \frac{1}{\left(\frac{x-1}{x+3} \right)^{4/5} (x+3)^2} dx$$

$$\left(\frac{x-1}{x+3} \right) = t \Rightarrow \frac{4}{(x+3)^2} dx = dt \quad t^{-4/5+1}$$

$$I = \frac{1}{4} \int \frac{1}{t^{4/5}} dt = \frac{1}{4} \frac{t^{1/5}}{1/5} + C = I = \frac{5}{4} \left(\frac{x-1}{x+3} \right)^{1/5} + C$$

$$A = \frac{5}{4} \alpha = \beta = 1 \quad B = \frac{1}{5}$$

$$\alpha + \beta + 20AB = 2 + 20 \times \frac{5}{4} \times \frac{1}{5} = 7$$



PHYSICS

26.

$$\lambda^1 = \frac{C - V_w}{f_o} \Rightarrow \lambda^1 < \frac{C}{f_0}$$

$$n^1 = f_o \left(\frac{C}{C - V_o - V_w} \right) \Rightarrow n^1 > f_o$$

$$\lambda^1 = \frac{C + V_w}{f_o} \Rightarrow \lambda^1 > \frac{C}{f_0}$$

$$n^1 = f_o \left(\frac{C}{C + V_w} \right) \Rightarrow n^1 < f_o$$

$$\lambda^1 = \left(\frac{C + V_o + V_w}{f_o} \right) \Rightarrow \lambda^1 > \frac{C}{f_0}$$

$$n^1 = f_o$$

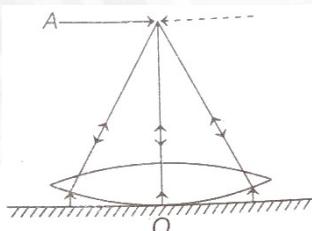
$$\lambda^1 = \frac{C - (V_o + V_w)}{f_o} \Rightarrow \lambda^1 < \frac{C}{f_o}$$

$$n^1 = f_o$$

27. Conceptual

28. Conceptual

29. Light from plane mirror is reflected back on its path, so that image of A coincides with A itself.



This would happen when rays refracted by the convex lens falls normally on the plane mirror, i.e. the refracted rays from a beam parallel to principal axis of the lens. Hence, the object would then be considered at the focus of convex lens.

\therefore Focal length of curvature of convex lens is $f_1 = 18\text{cm}$

With liquid between lens and mirror, image is again coincides with object, so the second measurement is focal length of combination of liquid lens and convex lens.

$$\therefore \frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{f_{eq}} \Rightarrow \frac{1}{18} + \frac{1}{f_2} = \frac{1}{27} \Rightarrow f_2 = -54\text{cm}$$

For convex lens by lens maker's formula, we have

$$\frac{1}{f} = (\mu - 1) \left(\frac{2}{R} \right) \Rightarrow \frac{1}{18} = 0.5 \times \frac{2}{R}$$

And for plano=convex liquid lens, we have

$$\frac{1}{f} = (\mu - 1) \left(\frac{-1}{R} \right) \Rightarrow -\frac{1}{54} = (\mu_l - 1) \left(\frac{-1}{18} \right) \Rightarrow \mu_l = 1 + \frac{1}{3} = \frac{4}{3}$$

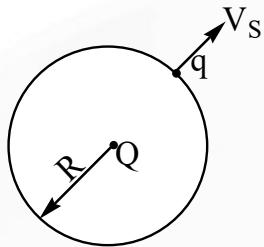


30. Let q be positive

If it escapes then, from energy conservation principle

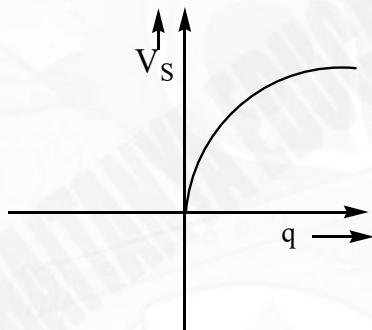
$$\frac{1}{2}mv_s^2 + \frac{KQq}{R} = 0$$

$$v_s = \sqrt{\frac{-2KQq}{Rm}}$$



{Note that Q is negative, therefore the quantity within the root is positive} $v_s \propto \sqrt{|q|}$

When q is negative, escape velocity will be zero due to electrostatic repulsion from negative Q $v_s \propto \sqrt{|q|}$



$$31. \vec{v}_{cm} = \frac{m_1\vec{v}_1 + m_2\vec{v}_2}{m_1 + m_2}$$

$$\vec{v}_{cm} = \frac{nmv\hat{i} + nmv\cos\theta\hat{i} + nmv\sin\theta\hat{j}}{m + nm}$$

$$v_{cm} = \frac{\sqrt{(nmv + nmv\cos\theta)^2 + (nmv\sin\theta)^2}}{m(1+n)}$$

$$v_{cm} = \frac{nmv\sqrt{(1+\cos\theta)^2 + (\sin\theta)^2}}{m(1+n)}$$

$$= \frac{nv\sqrt{1+\cos^2\theta} + 2\cos\theta + \sin^2\theta}{(1+n)} = \left(\frac{nv}{n+1}\right)\sqrt{2^2\cos^2\frac{\theta}{2}}$$

$$v_{cm} = \frac{2nv\cos\frac{\theta}{2}}{n+1} = \frac{nv\sqrt{3}}{(n+1)} = \frac{3n}{n+1}$$



32. The graph of current is given by

$$i = i_0(1 - e^{-t/\tau}) \Rightarrow \frac{di}{dt} = \frac{i_0}{\tau} e^{-t/\tau}$$

Energy stored in the form of magnetic field energy is

$$U_B = \frac{1}{2} L i^2$$

Rate of increase of magnetic field energy is

$$\begin{aligned} R &= \frac{dU_B}{dt} = Li \frac{di}{dt} \\ &= \frac{Li_0^2}{\tau} (1 - e^{-t/\tau}) e^{-t/\tau} \end{aligned}$$

This will be maximum when $\frac{dR}{dt} = 0 \Rightarrow e^{-t/\tau} = 1/2$

Substituting

$$R_{\max} = \frac{Li_0^2}{\tau} = \frac{Li_0^2}{\tau} \left(1 - \frac{1}{2}\right) \left(\frac{1}{2}\right) = \frac{Li_0^2}{4\tau} = \left[\frac{L(E/R)}{4(L/R)}\right] = \frac{E^2}{4R}$$

33. The focal length of combination is given by

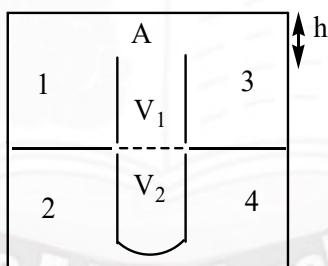
$$\frac{1}{F} = \frac{1}{40} - \frac{1}{25} \left(\frac{1}{F} = \frac{1}{F_1} + \frac{1}{F_2} \right)$$

or $f = -\frac{200}{3} \text{ cm} = -\frac{2}{3} \text{ m}$

\therefore Power of the combination in diopters,

$$p = -\frac{3}{2} \quad \left[p = -\frac{1}{F(m)} \right] = -1.5$$

- 34.

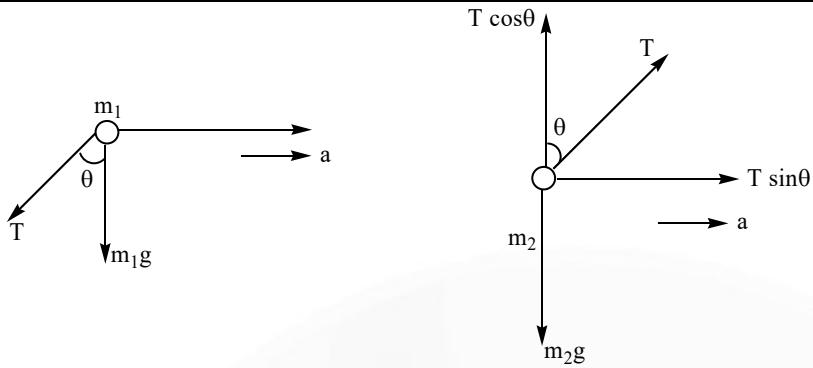


$\rho_1 v_1 g$ is not the force applied by liquid 1 on body, it is $\rho_1 g h \times A$, although net force (buoyant) comes out to be $\rho_1 v_1 g + \rho_2 v_2 g$

35. $1 \rightarrow d; ii \rightarrow c; iii \rightarrow b; iv \rightarrow a$

$$F = (m_1 + m_2)a$$

$$T \sin \theta = m_2 a$$



$$T \cos \theta = m_2 g \Rightarrow T = m_2 g \sec \theta$$

From (ii) and (iii) $a = g \tan \theta$

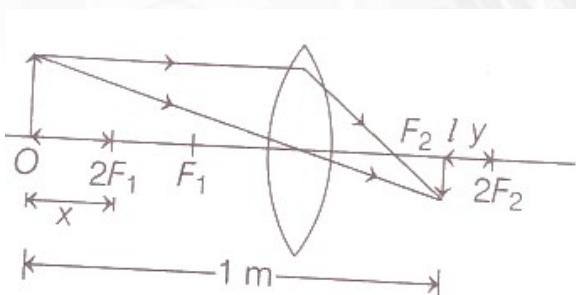
Put in (i), $F = (m_1 + m_2)g \tan \theta$

$$\text{Net force acting on } m_2 = m_2 a = \frac{m_2 F}{m_1 + m_2}$$

Force acting on m_1 by wire:

$$m_1 g + T \cos \theta = m_1 g + m_2 g$$

36. Image can be formed on the screen if it is real. Real image of reduced size can be formed by a concave mirror or a convex lens.



A diminished real image is formed by a convex lens when the object is placed beyond $2f$ and the image of such object is formed between f and $2f$ on other side

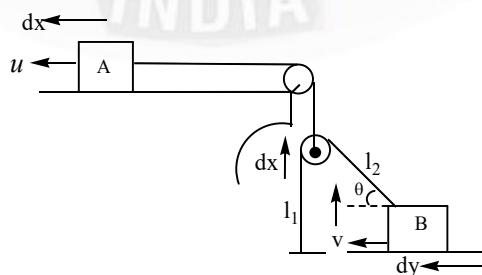
$$\text{Thus, } d > (2f + 2f) \quad (x > y)$$

$$\text{or } 4f < 0.1m$$

$$\text{or } f < 0.25m$$

37. Let in a small time dt , displacement of A is dx and displacement of B is dy . Increase in length $l_1 = dx$

$$\text{Increase in the length } l_2 = dx \sin \theta - dy \cos \theta$$



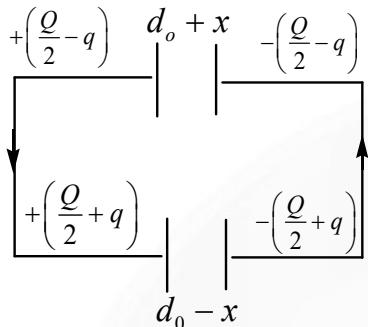
But net increase in the length should be zero, so



$$dx + dx \sin \theta - dy \cos \theta = 0$$

$$\Rightarrow dy = \frac{(1 + \sin \theta)dx}{\cos \theta} \Rightarrow \frac{dy}{dx} = \left(\frac{1 + \sin \theta}{\cos \theta} \right) \frac{dx}{dt} \Rightarrow v = \left(\frac{1 + \sin \theta}{\cos \theta} \right) u$$

38. Let each plate moves a distance 'x' from its initial position



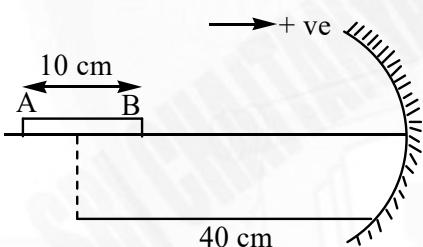
Let q charge flows in the loop using KVL

$$\frac{\left(\frac{Q}{2} - q\right)(d_0 + x)}{\epsilon_0 A} - \frac{\left(\frac{Q}{2} + q\right)(d_0 - x)}{\epsilon_0 A} = 0$$

$$q = \frac{Qx}{2d_0}; I = \frac{dq}{dt} = \frac{Q}{2d_0} \left(\frac{dx}{dt} \right);$$

$$I = \frac{Qu_0}{2d_0}$$

- 39.



$$u_A = -45 \text{ cm}, f = -20 \text{ cm}$$

$$\frac{1}{v_A} + \frac{1}{u_A} = \frac{1}{f} \Rightarrow \frac{1}{v_A} - \frac{1}{45} = \frac{-1}{20}$$

$$\frac{1}{v_A} = \frac{1}{45} - \frac{1}{20} \Rightarrow v_A = -36 \text{ cm and } u_B = -35 \text{ cm}$$

$$\frac{1}{v_B} + \frac{1}{u_B} = \frac{1}{f} \Rightarrow \frac{1}{v_B} - \frac{1}{35} = \frac{-1}{20}$$

$$\frac{1}{v_B} = \frac{1}{35} - \frac{1}{20} \Rightarrow v_B = -\frac{700}{15} = -\frac{140}{3} \text{ cm}$$

$v_A - v_B$ = length of image

$$= \left(-36 + \frac{140}{3} \right) \text{ cm} = \frac{-108 + 140}{3} \text{ cm} = \frac{32}{3} \text{ cm} \therefore x = 32$$



40. Let focal length of convex lens is $+f$, then focal length of concave lens would be $-\frac{3}{2}f$

$$\text{From the given condition, } \frac{1}{30} = \frac{1}{f} - \frac{2}{3f} = \frac{1}{3f}$$

Therefore, focal length of convex lens = +10 cm and that of concave lens = -15 cm.

$$41. \mu = \frac{\lambda_{\text{air}}}{\lambda_{\text{medium}}} = \frac{3}{2}$$

$$\text{Further } |m| = \frac{1}{3} = \left| \frac{v}{u} \right| \Rightarrow u = -24 \text{ m and } v = +8 \text{ m}$$

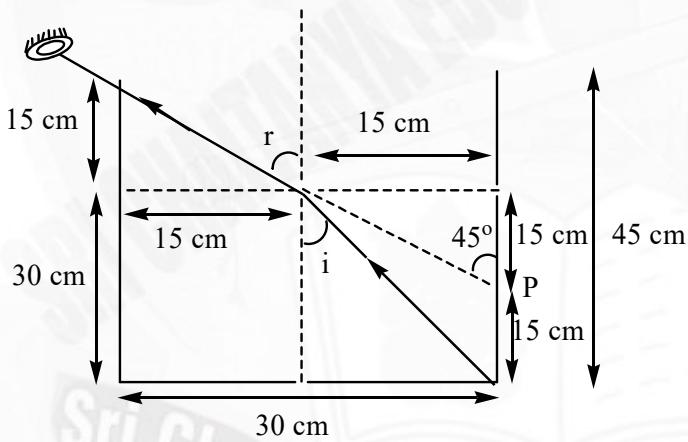
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f} = (\mu - 1) \left(\frac{1}{R} - \frac{1}{\infty} \right)$$

$$\therefore R = 3 \text{ m}$$

$$42. \text{ From figure, } \sin i = \frac{15}{\sqrt{15^2 + 30^2}}$$

$$\sin r = \frac{15}{15} = 1 \Rightarrow r = 45^\circ$$

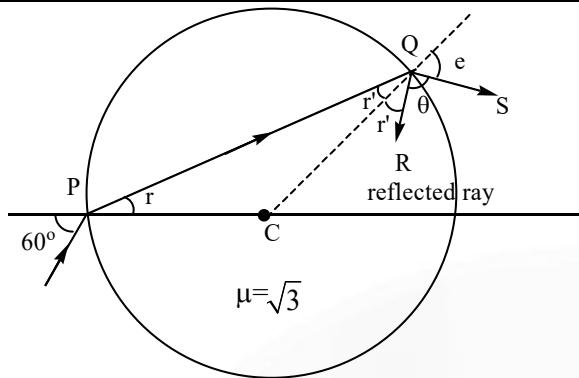
$$\text{From Snell's law, } \mu \times \sin i = 1 \times \sin r \Rightarrow \mu \times \frac{15}{\sqrt{15^2 + 30^2}} = 1 \times \sin 45^\circ = \frac{1}{\sqrt{2}}$$



$$\mu = \frac{\frac{1}{\sqrt{2}}}{\frac{15}{\sqrt{1125}}} = 158 \times 10^{-2} = \frac{N}{100}$$

Hence value of N = 158

43. In the figure, QR is the reflected ray and QS is refracted ray. CQ is normal.
Apply Snell's law at P



$$1 \sin 60^\circ = \sqrt{3} \sin r \Rightarrow \sin r = \frac{1}{2} \Rightarrow r = 30^\circ$$

From geometry,

$$CP = CQ = \text{radius}$$

$$r' = 30^\circ$$

Again apply snell's law at Q

$$\sqrt{3} \sin r' = 1 \sin e \Rightarrow \frac{\sqrt{3}}{2} = \sin e \Rightarrow e = 60^\circ$$

From geometry

$$r' + \theta + e = 180^\circ \quad (\text{As angle lines on a straight line}) \Rightarrow 30^\circ + \theta + 60^\circ = 180^\circ \Rightarrow \theta = 90^\circ$$

- 44.** Using lens formula

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{1}{V_1} - \frac{1}{-30} = \frac{1}{+10} \Rightarrow V_1 = 15\text{cm}$$

$$\text{So, } u_2 = (15 - 5)\text{cm} = 10\text{cm}$$

$$\frac{1}{V_2} - \frac{1}{+10} = \frac{1}{-10} \Rightarrow \frac{1}{V_2} = 0 \Rightarrow V_2 = \infty$$

$$\text{So, } u_3 = \infty$$

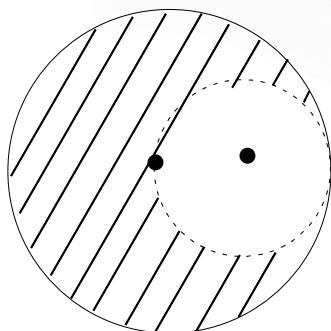
$$\text{Then, } V_3 = 30\text{cm}$$

$$OV_3 = 75\text{cm}$$

- 45.** Conceptual.

- 46.** Due to complete solid sphere, potential at point P

$$V_{\text{sphere}} = \frac{-GM}{2R^3} \left[3R^2 - \left(\frac{R^2}{2} \right) \right] = \frac{-GM}{2R^3} \left(\frac{11R^2}{4} \right) = -11 \frac{GM}{8R}$$



Due to cavity part potential at point P

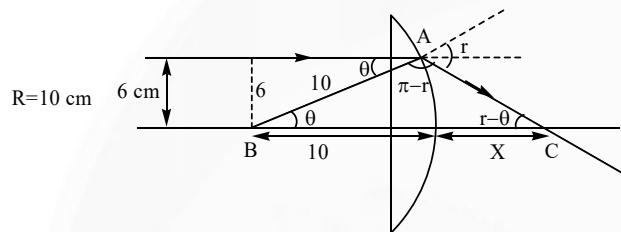


$$V_{cavity} = -\frac{3}{2} \frac{\frac{GM}{8}}{\frac{R}{2}} = -\frac{3GM}{8R}$$

So potential at the centre of cavity

$$= V_{sphere} - V_{cavity} = -\frac{11GM}{8R} - \left(\frac{-3GM}{8R} \right) = \frac{-GM}{R}$$

47.



$$\text{Applying Snell's law } \frac{\sin \theta}{\sin r} = \frac{3}{4} \Rightarrow r = 53^\circ$$

$$\text{By sine law in } \Delta ABC \frac{\sin(r - \theta)}{10} = \frac{\sin(\pi - r)}{(10 + x)}$$

$$\frac{10 + x}{10} = \frac{4}{5(\sin r \cos \theta - \cos r \sin \theta)} = \frac{4}{5\left(\frac{4}{5} \times \frac{4}{5} - \frac{3}{5} \times \frac{3}{5}\right)}$$

$$10 + x = \frac{200}{7}$$

$$(\text{note : } f = 30\text{cm for paraxial rays})(f_m < f_p) \Rightarrow x = \frac{200 - 70}{7} = \frac{130}{7} = 18.5\text{cm}$$

48. Given focal length of $L_1 = 24\text{m}$

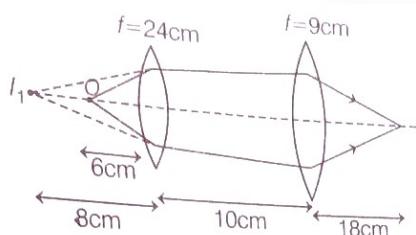
Focal length of $L_2 = 9\text{cm}$ distance b/w two lenses = 10 cm

According to question, for L_1

$$\frac{1}{v} + \frac{1}{6} = \frac{1}{24} \Rightarrow v = -8\text{cm}$$

$$\text{For } L_2 \frac{1}{v} + \frac{1}{18} = \frac{1}{9} \Rightarrow \frac{1}{v} = \frac{1}{18}$$

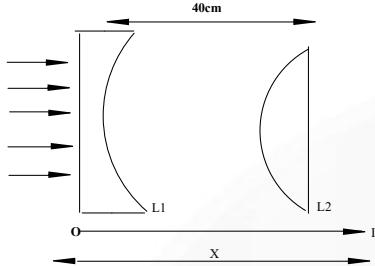
$$\Rightarrow v = 18\text{ cm}$$





49. Using lens maker's formula,

$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$



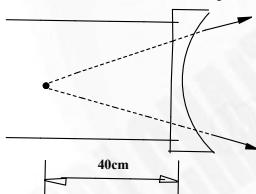
For lens, $L_1 \Rightarrow R_1 = \infty, R_2 = 30\text{cm}$ and $\mu = 175$

$$\text{So, } \frac{1}{f_2} = 0.75 \left(\frac{1}{30} \right) = 40\text{cm}$$

Now, in given situation for lens L_1

$$\mu = \infty, f_1 = -40\text{cm}, v = ?$$

$$\text{Using, } \frac{1}{v} - \frac{1}{u} = \frac{1}{f} \quad \text{We have } \frac{1}{v} = \frac{1}{-40} \Rightarrow v = -40\text{cm}$$



$$\text{Now lens } L_2, \quad \mu = -80\text{cm}, v = ?, f = 40\text{cm} \quad \text{So } \frac{1}{v} - \frac{1}{-80} = \frac{1}{40}$$

$$\text{or } \frac{1}{v} = \frac{1}{40} - \frac{1}{80} = \frac{1}{80}$$

$$\text{or } v = 80\text{ cm}$$

So, distance of image from plano concave (L_1) is $80 + 40 = 120\text{ cm}$.

$$50. \quad \frac{1}{10} = \left(\frac{3}{2} - 1 \right) \left(\frac{1}{R} - \frac{1}{\infty} \right) \Rightarrow \frac{1}{2R} = \frac{1}{10} \Rightarrow R = 5\text{cm}$$

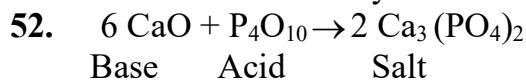
Rays should retrace the path \Rightarrow incident rays on mirror should be normal

$$\Rightarrow \frac{3/2}{\infty} - \frac{1}{-d} = \left(\frac{1/2}{5} \right) [\text{u} = -d, \text{ as lens is their}] \Rightarrow \frac{1}{d} = \frac{1}{10} \Rightarrow d = 10\text{cm}$$



CHEMISTRY

51. Friedel craft's benzoylation



$$\text{Mole ratio of reactant} = \frac{\text{CaO}}{\text{P}_4\text{O}_{10}} = \frac{6}{1}$$

Mol. wt of P_4O_{10} = 284

$$\text{Mole of CaO required} = 6 \times \text{Mole of P}_4\text{O}_{10} = 6 \times \frac{852}{284}$$

$$\text{Weight of CaO required} = \frac{6 \times 852}{284} \times 56 = 1008 \text{ g}$$

53. Basic hydrolysis of gem dihalide

54. Both are Correct but **STATEMENT -II** not the correct explanation for **STATEMENT-I**.



$$E_1 = E_{\text{Cu}^{+2}/\text{Cu}}^o - \frac{0.0591}{2} \log \left(\frac{1}{\text{Cu}^{2+}} \right)_1 \text{ as } E_{\text{SHE}}^o = 0 \text{ and } {}^a\text{H}_2(g) \text{ and } {}^a\text{H}_3\text{O}^+ \text{ in SHE are 1}$$

$$E_2 = E_{\text{Cu}^{+2}/\text{Cu}}^o - \frac{0.0591}{2} \log \left(\frac{1}{\text{Cu}^{2+}} \right)_2 \text{ as } E_{\text{SHE}}^o = 0 \text{ and } {}^a\text{H}_2(g) \text{ and } {}^a\text{H}_3\text{O}^+ \text{ in SHE are 1}$$

$$E_2 = E_{\text{Cu}^{+2}/\text{Cu}}^o - \frac{0.0591}{2} \log \frac{10}{(\text{Cu}^{+2})_1}$$

$$= E_{\text{Cu}^{+2}/\text{Cu}}^o - \frac{0.0591}{2} \log \frac{1}{(\text{Cu}^{2+})_1} - \frac{0.0591}{2} \log 10 = E_1 - 0.030 \text{ V}$$

56. $\pi_1 v_1 + \pi_2 v_2 = \pi_R (v_1 + v_2)$

$$\pi_R = \frac{\pi_1 v_1 + \pi_2 v_2}{(v_1 + v_2)} = \frac{1.2 \times 100 + 2.4 \times 300}{500} = 1.86 \text{ atm}$$

57. $\Delta S = \frac{\Delta H}{T}$

$$T = \frac{1.435 \times 10^3}{5.26} = 273 \text{ K or } 0^\circ \text{C}$$

58. Smaller cation and high charge has more polarizing power.

59. +M effect of $\text{NH}_2 > M$ of $-\text{OH}$ group disperse the charge of carbocation, hence increase the stability $-\text{CH}_3$ group shows +I effect, so it will disperse the charge less than $-\text{NH}_2, -\text{OH}$ group. Whereas $-\text{NO}_2$ group shows $-M / -I$ effect due to which the positive charge on the carbocation increases, hence stability decreases

60. Friedel-Crafts alkylation

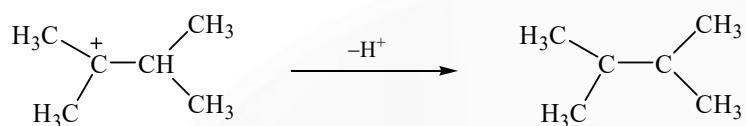
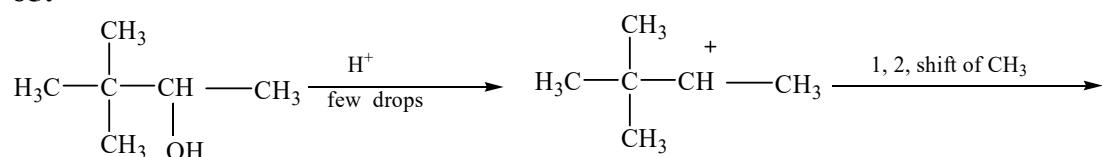
61. Hydrogenation followed by ozonolysis

62. Hydro boration followed by oxydation

63. Aldol condensation

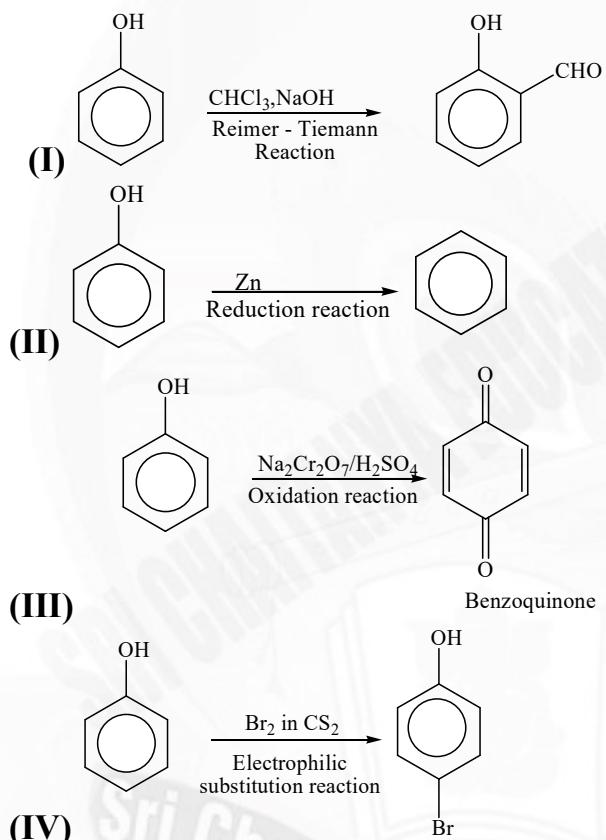
64. Conceptual

65.

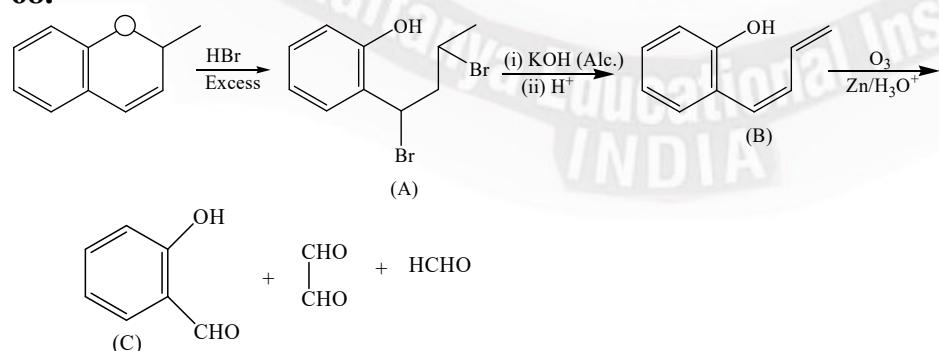


66. Nucleophilic addition

67.



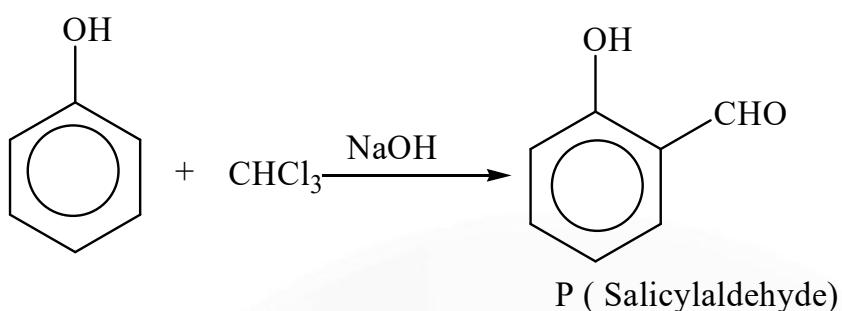
68.



69. Addition of Grignard's reagent followed by SN

70. Nucleophilic addition

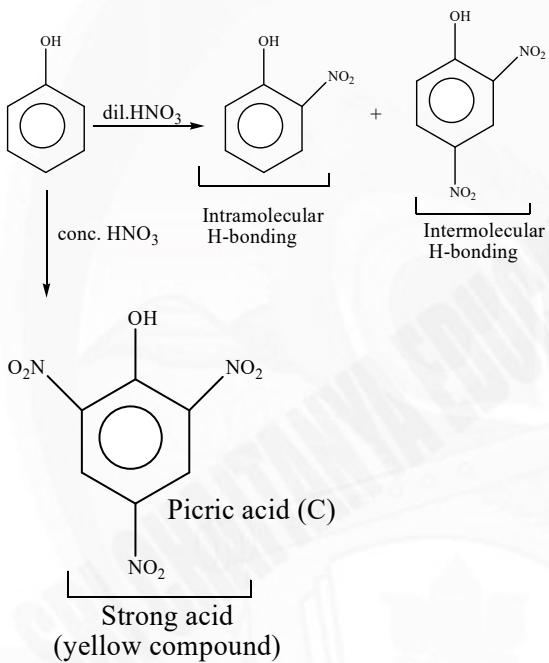
71.



Molecular formula of product 'P' = C₇H₆O₂

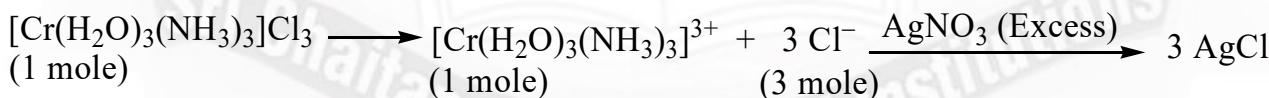
$$\text{So, mass \% of C in 'P'} = \frac{12 \times 7}{84 + 6 + 32} \times 100 = 68.85\% \approx 69\%$$

72.



Number of Oxygen atoms present in compound 'C' are 7

73.



None of the chloride ion is directly bonded to metal ion. Hence, number of chloride ions satisfying the secondary valency of the metal ion is zero.

74. Steereo isomerism

75. Polymerisation of Acetylene followed by Friedel Craft's Acylation