

**KEY SHEET****MATHEMATICS**

1)	2	2	2	3)	1	4)	1	5)	3
6)	4	7)	1	8)	1	9)	2	10)	2
11)	3	12)	3	13)	4	14)	2	15)	1
16)	2	17)	3	18)	2	19)	3	20)	4
21)	29	22)	5	23)	1	24)	4	25)	11

**PHYSICS**

26	4	27	4	28	3	29	3	30	2
31	3	32	2	33	3	34	1	35	1
36	4	37	4	38	4	39	3	40	2
41	3	42	4	43	4	44	3	45	4
49	150	47	0	48	3	49	2	50	45

**CHEMISTRY**

51	4	52	1	53	2	54	3	55	4
56	3	57	4	58	4	59	1	60	1
61	2	62	4	63	4	64	4	65	1
66	4	67	2	68	3	69	4	70	4
71	0	72	1	73	1	74	3	75	256



# SOLUTION MATHEMATICS

1. LET  $S = 20_{C_0} + 20_{C_1} - 1 + 20_{C_{10}} \dots (1)$

And  $S = 20_{C_{20}} + 20_{C_{19}} - 1 + 20_{C_{10}} \dots (2)$

Adding (1) and (2) we get

$$2S = (20_{C_0} + 20_{C_1} + \dots + 20_{C_{20}}) + 20_{C_{40}} \quad S = 2^{19} + 19_{C_9}$$

2.  $(\sqrt{2} + 1)^6 = I + f, I = \text{integer}, 0 < f < 1 = 6_{C_0} (\sqrt{2})^6 + 6_{C_1} (\sqrt{2})^5 t \dots + 6_{C_6}$

$$(\sqrt{2} - 1)^6 = G = 6_{C_0} (\sqrt{2})^6 - 6_{C_1} (\sqrt{2})^5 \dots + 6_{C_6}, 0 < G < 1$$

$$I + f + G = 2[6_{C_0} + 6_{C_2} \cdot 2^2 + 6_{C_4} \cdot 2 + 6_{C_6}] = 198 \quad \therefore 197 < I + f < 197 \Rightarrow n = 198$$

3. We have  $\left( \frac{x+1}{x^{2/3} - x^{1/3} + 1} - \frac{x-1}{x - x^{1/2}} \right)^{10} = (x^{1/3} - x^{-1/2})^{10} = r = \frac{np}{p+v} = \frac{10 \times \frac{1}{3}}{\frac{1}{3} + \frac{1}{2}} = 4$

$$\therefore T_5 = 10_{C_4} = 210$$

4.  $S = (1+x)^{1000} + 2x(1+x)^{999} + 3x^2(1+x)^{998} + \dots + 1001x^{1000}$

$$\frac{x \cdot S}{1+x} = x(1+x)^{999} + 2x^2(1+x)^{998} + \dots + 1001 \frac{x^{1001}}{1+x}$$

On subs tracking these two we get

$$S - \frac{x \cdot S}{1+x} = [(1+x)^{1000} + x(1+x)^{999} + x^2(1+x)^{998} + \dots + x^{1000}] - 1001 \frac{x^{1001}}{1+x}$$

$$S = (1+x)^{1002} - 1002 \cdot x^{1001} \cdot x^{1002}$$

Coefficient of  $x^{50}$  in  $S = \text{coefficient of } x^{50} \text{ in } (1+x)^{1002} = 1002_{C_{50}}$

5.  $7^{103} = 7(49)^{51} = 7(50-1)^{51} = 7[50^{51} - 51_{C_1} \cdot 50^{50} \dots - 1] = 7[50^{51} - 51_{C_1} \cdot 50^{50} \dots] - (7+18) - 18$   
 $= k + 18 [\because K \text{ is divisible by 25}]$

6. Conceptual

7. a)  $\sum_{r=0}^{10} (r+2^r) 10_{C_r} = \sum_{r=0}^{10} r \cdot 10_{C_r} + \sum_{r=0}^{10} 2^r \cdot 10_{C_r} = 10 \cdot 2^9 + [10_{C_0} + 2 \cdot 10_{C_1} + 10_{C_2} + \dots + 2^{10} \cdot 10_{C_{10}}]$

$$= 10 \cdot 2^9 + 3^{10} = a + b = 19$$

b)  $T_{r+1} = m_{C_r} \cdot x^{m-r} \cdot \frac{1}{(ax)^r} = m_{C_r} \cdot \frac{x^{m-2r}}{a^r} = 5/2 \Rightarrow m-2r=0 \Rightarrow m=2r \text{ but } r=3 \Rightarrow m=6$

$$\therefore T_4 \frac{6_{C_3}}{a^3} = 5/2 \Rightarrow a=2 = ma=12$$

c)  $r = \frac{55}{6} = 9.1 \quad \therefore T_{9+1} = 10_{C_0} \cdot 5^9 = \lambda$

$$\frac{\lambda}{10_{C_9} \cdot 5^7} = 5^2 = 25$$

d)  $n_{p_r} = 5040 \cdot n_{C_r} \Rightarrow r! = 5040 = 7 = r = 7$

8.  $T_{r+1} = 9_{C_r} (3^{1/3})^{9-r} (5^{1/2})^r = 9_{C_r} \cdot 3^{3-2/3} \cdot 5^{r/2}$



$$\frac{r}{3} \rightarrow r = 0, 3, 6, 9$$

$$\frac{r}{2} \rightarrow r = 0, 4, 6, 8$$

Common 'r' = 0,6

Rotational terms  $T_1$  and  $T_7$

Sun  $T_1 + T_7 = 31527$

$$9. \quad (1+x-2x^2)^7 = \sum_{r=0}^7 7_{c_r} (1+x)^{7-r} \cdot (-2x^2)^r$$

Thus required coefficient =  $7_{c_0} \cdot 7_{c_4} + 7_{c_4} (-2) \cdot 6_{c_2} + 6_{c_2} + 7_{c_2} (-2)^2 \cdot 5_{c_0} = 1.35 - 7.2.15 + 21.4.1 = -91$

10. Coefficient of  $x^2$  = coefficient of  $x^3$

$$\therefore 9_{c_2} 3^{9-2} \cdot k^2 = 9_{c_3} 3^{9-3} \cdot k^3 \quad 36 = 28k \rightarrow k = 9/7$$

$$11. \quad A = 30_{c_0} \cdot 30_{c_{10}} - 30_{c_1} \cdot 30_{c_{11}} + \dots + 30_{c_{20}} \cdot 30_{c_{30}} = \text{coefficient of } x^{20} \text{ in } (1+x)^{30} (1-x)^{30}$$

$$= (1-x^2)^{30} = (-1)^{10} \cdot 30_{c_{10}} = 30_{c_{10}}$$

$$12. \quad (x^2 + 2x + 2)^n = \{2 + x(2+x)\}^n$$

$$2^n + n \cdot 2^{n-1} \cdot x(2+x) + n_{c_2} \cdot 2^{n-2} \cdot x^2(2+x)^2 + n_{c_3} \cdot 2^{n-3} \cdot x^3(2+x)^3$$

$$\text{Coefficient of } x^3 = n_{c_2} \cdot 2^{n-2} \cdot 4 + n_{c_3} \cdot 2^{n-3} \cdot 2^3 = 2^n \cdot n + 1_{c_3}$$

$$13. \quad \text{Given } m_{c_0} + m_{c_1} + m_{c_2} = 46$$

$$\rightarrow 1+m + \frac{m(m-1)}{2} = 46$$

$$\rightarrow m^2 + m - 90 = 0 \Rightarrow m = 9$$

$$\therefore T_{r+1} = 9_{c_r} (x^2)^{9-1} \cdot \left(\frac{1}{x}\right)^r = 9_{c_r} \cdot x^{18-3r}$$

For constant terms  $18-3r=0 \Rightarrow r=6$

$$\therefore T_r = 9_{c_6} = 84$$

$$14. \quad \text{Let } y = x-3 \Rightarrow y+1 = x-2$$

$$b_n = \text{coefficient of } y^n \text{ in } (1+y)^{n-1} + \dots + (1+y)^{2n}$$

$$= \text{coefficient of } y^n \text{ in } \sum_{r=n}^{2n} (y+1)^r = \text{coefficient of } y^n \text{ in } \frac{[(y+1)^{n+1}-1](y+1)^n}{y}$$

$$= \text{coefficient of } y^{n+1} \text{ in } (y+1)^{2n+1} - (y+1)^n \text{ in } 2n+1_{c_{n+1}}$$

$$15. \quad \text{We have } \left[ \sqrt{25^{x-1} + 7} + (5^{x-1} + 1)^{-1/8} \right]^{10}$$

$$T_9 = 180 \Rightarrow 10_{c_8} (25^{x-1} + 7) (5^{x-1} + 1)^{-1} = 180 \Rightarrow \frac{25^{x-1} + 7}{5^{x-1} + 1} = 4 \Rightarrow \frac{y^2 + 7}{y + 1} = 4 \text{ where } y = 5^{x-1}$$

$$\Rightarrow y^2 - 4y + 3 = 0 \Rightarrow y = 3 \text{ or } 1 \Rightarrow 5^{x-1} = 3 \text{ or } 1 \Rightarrow 5^x = 15 \text{ or } 5 \Rightarrow x = \log_5^{15} \text{ or } x = 1$$

$$16. \quad T_n < T_{n+1} > T_{n+2} \Rightarrow 2n_{c_{n-1}} \cdot x^{n-1} < 2n_{c_n} \cdot x^n > 2n_{c_{n+1}} \cdot x^{n+1} \Rightarrow \frac{2n_{c_n} \cdot x^n}{2n_{c_{n-1}} \cdot x^{n-1}} > 1 \text{ & } \frac{2n_{c_{n+1}} \cdot x^{n+1}}{2n_{c_n} \cdot x^n} < 1$$

$$\Rightarrow \left(\frac{n+1}{n}\right)x > 1 \text{ and } \left(\frac{n}{n+1}\right)x < 1 \Rightarrow x > \frac{n}{n+1} \text{ and } x < \frac{n+1}{n} \Rightarrow \frac{n}{n+1} < r < \frac{n+1}{n}$$



17.  $(xy + yz + zx)^6 = \sum_{r+s+t=6} \frac{6!}{r!s!t!} (xy)^r \cdot (yz)^s \cdot (zx)^t = \sum_{r+s+t=6} \frac{6!}{r!s!t!} x^{r+t}, y^{r+s}, z^{s+t}$   
 $\Rightarrow r+t=3, r+s=4 \text{ and } s+t=5$

Also  $r+s+t=6 \Rightarrow r=1, s=3, t=2$

18.  $\sum_{r=0}^n \frac{(-1)^r}{n_{c_r}} = \sum_{r=0}^{\left(\frac{n+1}{2}\right)} \left[ \frac{(-1)^r}{n_{c_r}} + \frac{(-1)^{n-2}}{n_{c_{n-r}}} \right]$   
 $\sum_{r=0}^{\left(\frac{n+1}{2}\right)} (-1)^r \left[ \frac{1}{n_{c_r}} + \frac{(-1)^n}{n_{c_{n-r}}} \right]$   
 $\sum_{r=0}^{\left(\frac{n+1}{2}\right)} (-1)^r \left[ \frac{1}{n_{c_r}} - \frac{1}{n_{c_r}} \right] = 0$

19.  $T_2 = 135 \rightarrow n_{c_1} x^{n-1}, y^1 = 135; T_3 = 30 \Rightarrow n_{c_2} \Rightarrow x^{n-2}, y^2 = 30$

And  $T_4 = \frac{10}{3} \Rightarrow n_{c_3} x^{n-2}, y^3 = \frac{10}{3}$

$$\frac{T_2 \times T_4}{T_3} = \frac{135 \times 10/3}{(30)^2} \Rightarrow \frac{n_{c_1} \times n_{c_3}}{(n_{c_2})} = \frac{135 \times 10}{900 \times 3} \Rightarrow n = 5$$

20.  $\sum_{r=1}^n \left( \sum_{r_1=0}^{r-1} n_{c_r} \cdot r_{C_{r_1}} \cdot 2^{r_1} \right) = \sum_{r=1}^n n_{c_r} \left( \sum_{r_1=0}^{r-1} r_{c_{r_1}} 2^{r_1} \right) = \sum_{r=1}^n n_{c_r} \left( (1+2)^r - 2r \right) = \sum_{r=1}^n n_{c_r} (3^r - 2^r)$   
 $= \sum_{r=1}^n n_{c_r} \cdot 3^r - \sum_{r=1}^n n_{c_r} \cdot 2^r = [(1+3)^n - 1] - [(1+2)^n - 1] = 4^n - 3^n$

21. The expression  $(2+x)^2 (3+x)^3 (4+x)^4$   
 $= (x+2)(x+2)(x+3)(x+3)(x+3)(x+4)(x+4)(x+4)$   
 $= x^9 + (2+2+3+3+3+4+4+4+4+4) x^8 r = \text{Coefficient of } x^8 = 29$

22.  $= \sum_{k=0}^4 \left( \frac{5^{4-k}}{(4-k)!} \right) \left( \frac{x^k}{k!} \right) = \sum_{k=0}^4 \left( \frac{5^{4-k}}{(4-k)!} \right) \left( \frac{x^k}{k!} \right) \cdot \frac{4!}{4!} = \sum_{k=0}^4 \frac{4_{c_k} \cdot 5^{4-k} x^k}{4!} = \frac{(5+x)^4}{4!}$   
 $n_{c_5} \frac{(5+x)^4}{4!} = \frac{8}{3} \Rightarrow x = 2\sqrt{2} - 5$

23.  $\left( \sum_{r=0}^{10} 10_{c_r} \right) \left( \sum_{k=0}^{10} (-1)^k \frac{10_{c_k}}{2^k} \right) = 2^{10} \left( 10_{c_0} - \frac{10_{c_1}}{2} + \frac{10_{c_2}}{2^2} - \dots + \frac{10_{c_{10}}}{2^{10}} \right) = 2^{10} \cdot \left( 1 - \frac{1}{2} \right)^{10} = 1$

24. Coefficient of  $x^3$  in  $(1+x+2x^2+3x^3)^4 = a$

Coefficient of  $x^3$  in  $[f(x)]^4 = a$

$b = \text{coefficient of } x^3 \text{ in } (1+x+2x^2+3x^3+4x^4)^4$

$b = \text{coefficient of } x^3 \text{ in } (f(x)+4x^4)^4 \text{ where } f(x) = 4x + 2x^2 + 3x^3$

$= \text{coefficient of } x^3 \text{ in } (f(x))^4 = a \Rightarrow a - b = 0$

25.  $\frac{1}{11!} \left[ \frac{11!}{1!10!} + \frac{11!}{2!9!} + \frac{11!}{3!10!} + \dots + \frac{11!}{1!10!} \right] = \frac{1}{11!} [11_{c_1} + 11_{c_2} + \dots + 11_{c_{10}}] = \frac{1}{11!} (2^{11} - 2)$



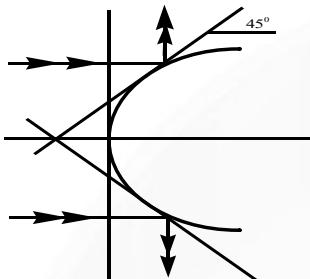
## PHYSICS

26. At the point incidence slope should be  $\pm 1$

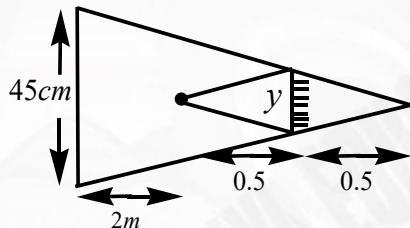
$$Y^2 = 2x$$

$$y = \sqrt{2x}$$

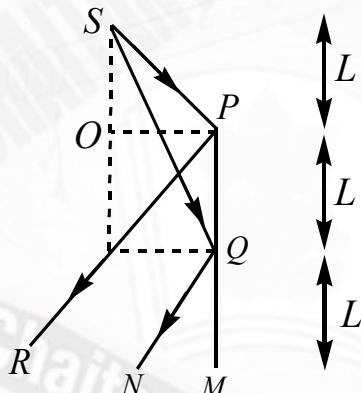
$$\frac{dy}{dx} = \sqrt{2} \cdot \frac{1}{2\sqrt{x}} = \frac{1}{\sqrt{2x}} = 1 \Rightarrow \sqrt{2x} = 1 \Rightarrow 2x = 1 \Rightarrow x = \frac{1}{2} \Rightarrow y = \pm 1$$



27.  $\frac{0.5}{3} = \frac{y}{0.45}$        $\frac{0.5}{3} = \frac{x}{1.2}$   
 $y = 7.5\text{cm}$      $\Rightarrow x = 20\text{cm}$



28. Ray diagram is as shown in the figure below



$$\text{Here, } \frac{SO}{OP} = \frac{PM}{RM} \Rightarrow RM = 2L$$

$$\text{Also } \frac{ST}{TQ} = \frac{QM}{SN} \Rightarrow SN = \frac{L}{2}$$

$$\therefore RS = RM - SN = \frac{3L}{2}$$

29.  $f = 10\text{cm}$        $m = \frac{f}{f-u}$

$$m = \frac{1}{2} \quad \frac{1}{2} = \frac{10}{10-u}$$

$$10-u = 20 \Rightarrow u = -10$$

30. Here  $\vec{a} = |\vec{a}| \sin \theta \hat{i} - |\vec{a}| \cos \theta \hat{j}$

As  $\vec{a}$  is an unit vector, So  $|\vec{a}| = 1$

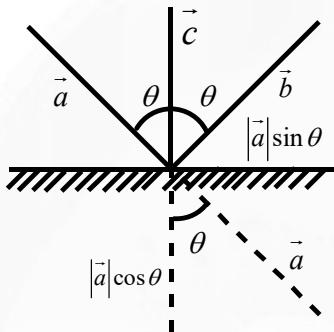
$$\therefore \vec{a} = |\vec{a}| \sin \theta \hat{i} - |\vec{a}| \cos \theta \hat{j} = \sin \theta \hat{i} - \cos \theta \hat{j}$$

Similarly  $\vec{b} = \sin \theta \hat{j}$

And  $\vec{c} = \hat{j}$

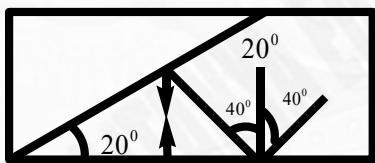
From option (B)

$$\vec{a} - 2(\vec{a} \cdot \vec{c})\vec{c} = \sin \theta \hat{i} + \cos \theta \hat{j} = \vec{b}$$



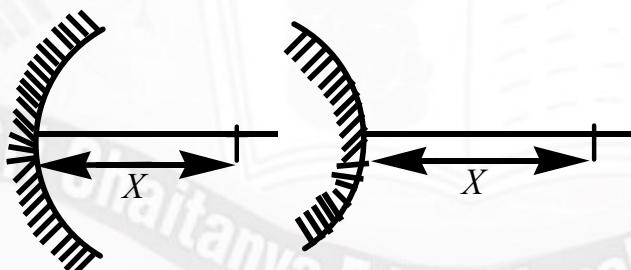
31.  $\delta_1 = \pi - 2 \times 40^\circ = 100^\circ - \text{clockwise}$

$\delta_2 = \pi - 2 \times 40^\circ = 140^\circ - \text{anticlockwise}$



$$\delta_3 = \pi - 2 \times 00^\circ = 140^\circ - \text{clockwise} \Rightarrow \text{Deviation (Net)} = 140^\circ - \text{clockwise}$$

32.



$$m = \frac{f}{f-u} = \frac{\frac{R}{2}}{\frac{-R}{2} + \frac{3R}{2}} = -\frac{1}{2}$$

$$m = \frac{f}{f-u} = \frac{\frac{R}{2}}{\frac{R}{2} + x} = \frac{1}{4} \Rightarrow 4R = R + 2x \Rightarrow x = \frac{3R}{2}$$

33.  $\frac{1}{-0.5} + \frac{1}{0.2} = \frac{2}{r} \Rightarrow \frac{1}{r} = \frac{3}{2}; r = 0.667m$



34. Using Newton's formula

$$(f + d_1)(f - d_2) = f^2$$

$$f^2 + fd_1 - fd_2 - d_1d_2 = f^2$$

$$f = \frac{d_1d_2}{d_1 - d_2}$$

$$\therefore R = \frac{2d_1d_2}{d_1 - d_2}$$

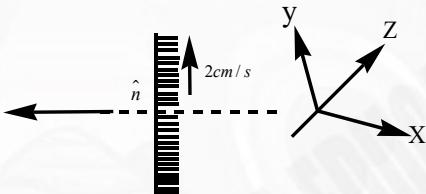
$$35. \frac{2\hat{i} - 3\hat{j} + 4\hat{k}}{\sqrt{29}} - 2\left(\left(\frac{3\hat{i} - 6\hat{j} + 2\hat{k}}{7}\right)\left(\frac{2\hat{i} - 3\hat{j} + 4\hat{k}}{\sqrt{29}}\right)\right)\frac{3\hat{i} - 6\hat{j} + 2\hat{k}}{7} = \frac{2\hat{i} - 3\hat{j} + 4\hat{k}}{\sqrt{29}} - 2\left[\frac{6+18+8}{7 \times \sqrt{29} \times 7}\right](3\hat{i} - 6\hat{j} + 2\hat{k})$$

$$= \frac{98\hat{i} - 147\hat{j} + 196\hat{k} - (192\hat{i} - 384\hat{j} + 128\hat{k})}{\sqrt{29} \times 49} = \frac{-98\hat{i} + 237\hat{j} + 68\hat{k}}{49\sqrt{29}}$$

36.  $v_0$  is decreasing  $\Rightarrow a_0$  is  $-Ve$   $\Rightarrow a_1$  is in opposite direction  $\Rightarrow a_1$  is  $+Ve$

37. The velocity of image

$$v' = \vec{v} = 2(\vec{v} \cdot \hat{n})\hat{n} = (\hat{i} + \hat{j}) - 2[(\hat{i} + \hat{j}) - \hat{i}](-\hat{i}) = (-\hat{i} + \hat{j}) \text{ cm/s}$$



Velocity of image with respect to mirror,

$$v'' = \vec{v} - \vec{v}_m = (-\hat{i} + \hat{j}) - 2\hat{j} = (-\hat{i} - \hat{j}) \text{ cm/s}$$

Velocity of image with respect to object

$$v' - v_0 = (-\hat{i} + \hat{j}) - (\hat{i} + \hat{j}) = -2\hat{i} \text{ cm/s}$$

Unit vector in the direction of reflected ray =  $\frac{(-\hat{i} + \hat{j})}{\sqrt{2}}$

38. Here  $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$  .....(1)

$$\Rightarrow \frac{1}{v} + \frac{1}{-190} = \frac{1}{10} \Rightarrow V = \frac{19}{2}$$

Differentiating equation (1) w.r.t we get

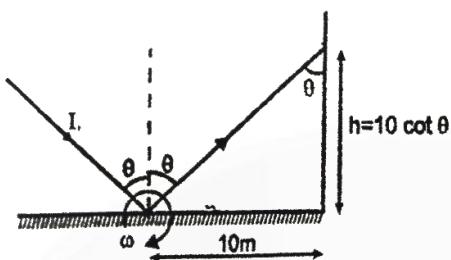
$$-\frac{1}{v^2} \left( \frac{dv}{dt} \right) - \frac{1}{u^2} \left( \frac{du}{dt} \right) = 0 \Rightarrow \left( \frac{dv}{dt} \right) = \frac{v^2}{u^2} \left( \frac{du}{dt} \right) \Rightarrow \left( \frac{dv}{dt} \right) = - \left( \frac{\frac{19}{2}}{190} \right)^2 \times 40 = \frac{1}{400} \times 40 = 0.1 \text{ m/s}$$

39. The maximum velocity of the insect is  $A\sqrt{\frac{K}{M}}$

Its component perpendicular to the mirror is  $A\sqrt{\frac{K}{M}} \sin 60^\circ$

Thus, maximum relative speed =  $\frac{\sqrt{3}}{2} A\sqrt{\frac{K}{M}}$ .

40. When mirror is rotated with angular speed  $\omega$ , the reflected ray rotates with angular speed  $2\omega (= 36 \text{ rads}^{-1})$



$$\text{Speed of the spot} = \left| \frac{dh}{dt} \right| = \left| \frac{d}{dt} (10 \cot \theta) \right| = \left| -10 \cos \theta \epsilon c^2 \theta \frac{d\theta}{dt} \right| = \left| -\frac{10}{(0.6)^2} \times 36 \right| = 1000 \text{ ms}^{-1}$$

41. When object is at 8 cm

$$\text{Image } V_1 = \frac{f \times u}{u - f} = \frac{5 \times 8}{8 - 5} = -\frac{40}{3} \text{ cm}$$

When object is at 12 cm

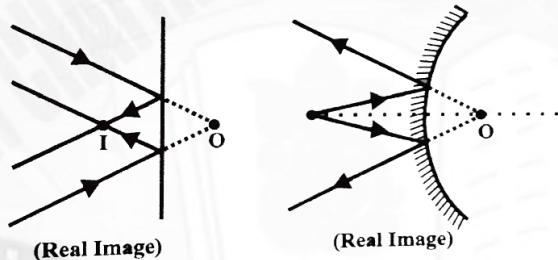
$$\text{Image } V_2 = \frac{f \times u}{u - f} = \frac{5 \times 12}{12 - 5} = -\frac{60}{7} \text{ cm}$$

$$\text{Separation} = |V_1 - V_2| = \frac{40}{3} - \frac{60}{7} = \frac{100}{21} \text{ cm}$$

So A, C and D are correct statements

42. If the mirror is shifted parallel to itself such that the velocity of the mirror is parallel to its surface, the image shall not shift. Hence statement I is false.

43. We can produce a real image by a plane or convex mirror



Focal length of a convex mirror is taken positive.

44. Laws of reflection can be applied to any type of surface.

45. Multiple reflection from two mirrors

Option a

Image	Mirror	Angle
$I_1$	$M_1$	$30^\circ$
$I_2$	$M_2$	$90^\circ$
$I_3$	$M_1$	$150^\circ$
$I_1^1$	$M_2$	$30^\circ$
$I_2^1$	$M_1$	$90^\circ$
$I_3^1$	$M_2$	$150^\circ$



Here  $I_3$  and  $I_3^1$  coincide hence  $N = 5$

Option b

Image	Mirror	Angle
$I_1$	$M_1$	$36^\circ$
$I_2$	$M_2$	$108^\circ$
$I_1^1$	$M_2$	$36^\circ$
$I_2^1$	$M_1$	$108^\circ$

$$N = 4$$

Option c

Image	Mirror	Angle
$I_1$	$M_1$	$42^\circ$
$I_2$	$M_2$	$114^\circ$
$I_1^1$	$M_2$	$30^\circ$
$I_2^1$	$M_1$	$102^\circ$
$I_3$	$M_2$	$176^\circ$

$$N = 5$$

Option d

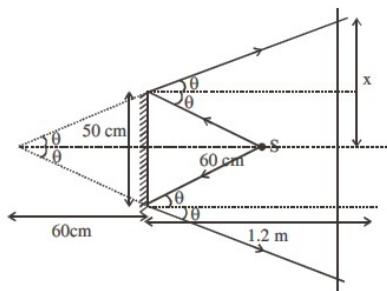
Image	Mirror	Angle
$I_1$	$M_1$	$50^\circ$
$I_2$	$M_2$	$120^\circ$
$I_1^1$	$M_2$	$20^\circ$
$I_2^1$	$M_1$	$90^\circ$
$I_3$	$M_2$	$160^\circ$

$$N = 5$$

46.  $\tan \theta = \frac{25}{60} = \frac{x}{180}$

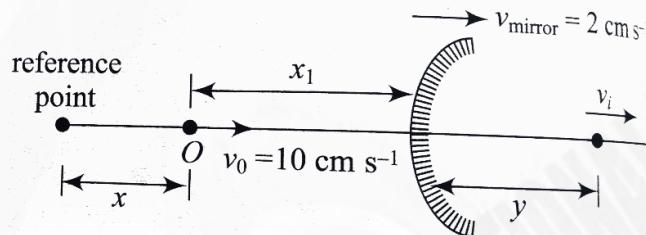
$$x = 75\text{cm}$$

So distance between extreme points  $= 2x = 2 \times 75 = 150\text{cm}$



$$47. \frac{1}{y} + \frac{1}{-x_1} = \frac{1}{10}$$

$$\frac{1}{y} - \frac{1}{10} = \frac{1}{10} \Rightarrow y = 5 \text{ cm}$$



$$\frac{dx}{dt} = 10 \text{ cm/s}, \frac{d(x+x_1)}{dt} = 2 \text{ cm/s}$$

$$\frac{dx_1}{dt} = -8 \text{ cm/s}$$

$$\frac{dy}{dt} = v_i = 2$$

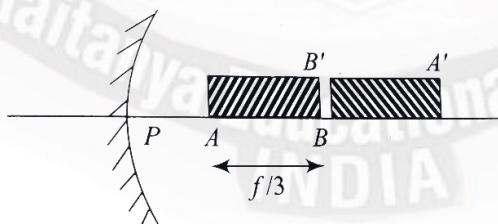
$$\text{From(i): } \frac{dy}{dt} = \left( \frac{y}{x_2} \right)^2 \frac{dx_1}{dt} \Rightarrow v_i - 2 = \left( \frac{5}{10} \right)^2 (-8) \Rightarrow v_i = 0$$

48. For  $v_1 = 50/7 \text{ m}, u_1 = -25 \text{ m}$

$$v_2 = 25/3 \text{ m}, u_2 = -50 \text{ m}$$

$$\text{Speed of object} = \frac{25}{30} \times \frac{18}{3} = 3 \text{ kmph}$$

49. Since the image formed is real and elongated, the situation is as shown in the figure. Since the image of B is formed at B' itself, therefore



B is situated at the center of curvature that is at a distance 2f from the pole.

$$\therefore PA = 2f - \frac{f}{3} = \frac{5f}{3}$$

Let us find the image of A for point A

$$u = -\frac{5f}{3}, v = ? \text{ Applying } \frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$



$$\Rightarrow \frac{1}{\frac{-5f}{3}} + \frac{1}{v} = \frac{1}{-f} \Rightarrow \frac{1}{f} + \frac{3}{5f} = \frac{1}{v} = \frac{-5+3}{5f} = \frac{-2}{5f} \Rightarrow v = -2.5f$$

$$\therefore \text{Image length} = 2.5f - 2f = 0.5f = \frac{f}{2}$$

$$\therefore \text{Magnification} = \frac{\frac{f}{2}}{\frac{f}{3}} = 1.5$$

50. For n mirror 1

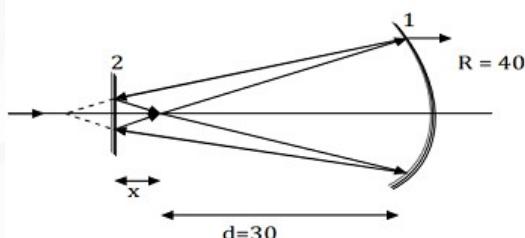
$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \quad | u = -30 \\ v = f = -20$$

$$\frac{1}{v} - \frac{1}{30} = -\frac{1}{20}$$

$$\frac{1}{v} = \frac{1}{30} - \frac{1}{20}$$

$$v = -60 \text{ cm}$$

$$\text{So } x = 15 \text{ cm}$$

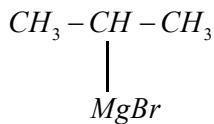


So distance between two mirrors = 45 cm



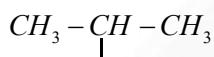
## CHEMISTRY

51. In final product D-atom is attached to 2<sup>nd</sup> carbon during duterolysis, hence compound C is

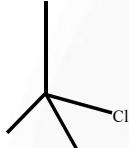


And

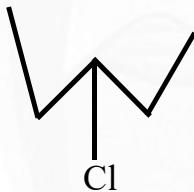
Alkyl group R is



52.

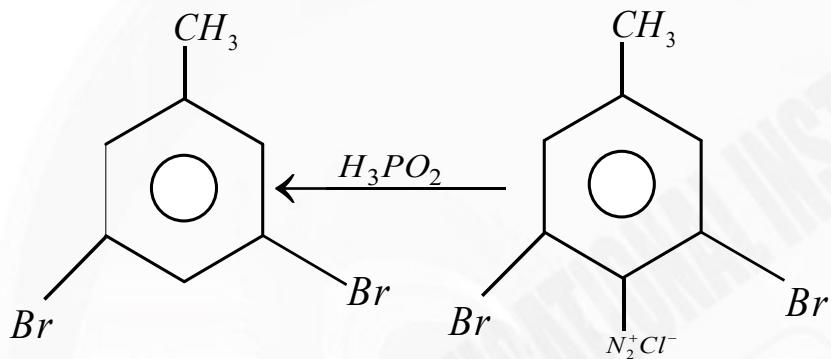
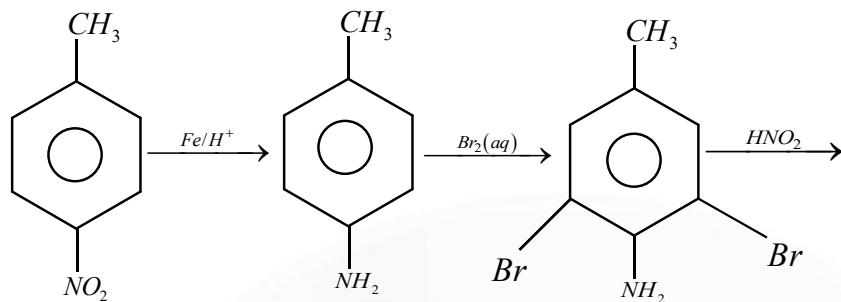


forms 3° carbanion in  $SN_1$  reaction which is more stable compared to 2° carbanion ion formed by



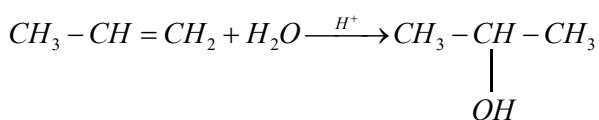
53. 1<sup>st</sup> step is diazotization of aniline X is  $C_6H_5N_2^+Cl^-$   
2<sup>nd</sup> step is sand Meyers reaction Y is  $C_6H_5Cl$
54. Addition of HCl across double bond of side chain follows Markonikoff's addition giving  $C_6H_5 - CH_2 - CH(Cl) - CH_3$
55. Presence of –M group increases the reactivity for aromatic nucleophilic substitution, –M group at O,P increases reactivity to greater extent compared to same group at Meta position ( $a < C < b$ )
56. As OH is attached on same side as leaving group i.e Cl<sup>-</sup>. This indicates  $SN_1$  mechanism and intermediate formed will be a carbocation.
57. In aryl halides, halogen is directly bonded to benzene ring. Hence a & d, are aryl halides. b and c are benzylic halides
58. Cl is O,P-directing group, hence nitration of chlorobenzene will give mixture of O-nitro chlorobenzene and p-chloronitrobenzene,  $NO_2$  is –M group & hence metadirecting
59.  $NO_2$  Group at ortho or para position to halogen in benzene makes carbon attached to halogen electron deficient, this facilitates attack of nucleophile on this carbon atom
60. A–2, B–1, C–4, D–3 Factual

61.



62. Freon – 12 -  $\text{CCl}_2\text{F}_2$ , Chloral -  $\text{CCl}_3\text{CHO}$ , Chloropierin -  $\text{CCl}_3\text{NO}_2$ , gammamaxene -  $\text{C}_6\text{H}_6\text{Cl}_6$
63.  $-\text{OH}$  group can react with  $\text{C}_2\text{H}_5\text{MgBr}$  releasing  $\text{C}_2\text{H}_6$  gas  
 $-\text{CH} = \text{CH}_2$  group attached to ring can decolorize  $\text{Br}_2$  water
64. Ethanolic KOH causes dehydrahologenation to give cyclohexene
65. In friedel craft's alkylation  $\text{R}^+$  is attacking electrophile  
a)  $\text{C}_6^+\text{H}_5$  is unstable  
b)  $\text{Cl}^+$  can attack benzene ring for electrophilic substitution  
c)  $\text{CH}_2 = \text{CH} - \text{CH}_2^+$  is stable  
d)  $\text{CH}_2 = \text{CH}^+$  is unstable
66.  $\text{NaBH}_4$  can only reduce  
 $\begin{array}{c} -\text{C}-\text{group} \\ \parallel \\ \text{O} \end{array}$  and does not affect ester group

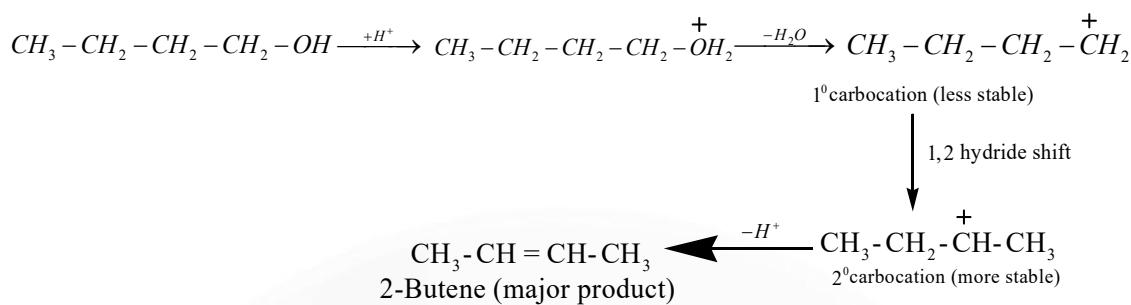
67. i) Reduction of propanal gives 1-propanol  
ii)



- iii) Reaction of propanone with grignard's reagent followed by hydrolysis gives 3° alcohol

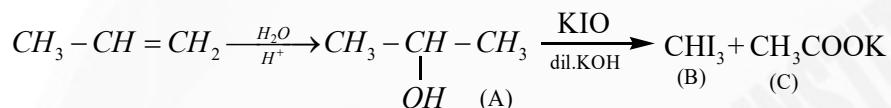


68.



69. Given product is  $3^{\circ}$  alcohol which can be formed by reaction of ketone with  $C_6H_5MgBr$  followed by hydrolysis

70.



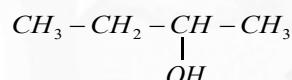
71.  $3^{\circ}$  alkyl halide (2) - 1,6

allylic halides (2) - 3,5

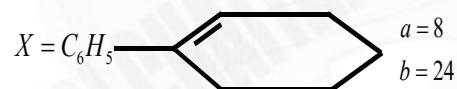
$X = 2$ ,  $y = 2$

72. Cl attached to  $SP^3$  c-atom only can give  $AgCl$

73. Only 2-butanol is chiral in nature



74. a,c,d only.  $KMnO_4 / H^+$  will give carboxylic acid



75.

$$(24 - 8)^2 = 256$$