



4. If  $\alpha + i\beta$  and  $\gamma + i\delta$  are the roots of  $x^2 - (3-2i)x - (2i-2) = 0$ ,  $i = \sqrt{-1}$ , then  $\alpha\gamma + \beta\delta$  is equal to :

**Ans. (2)**

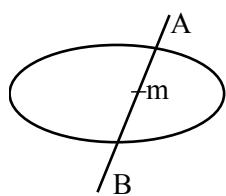
$$\text{Sol. } x^2 - (3 - 2i)x - (2i - 2) = 0$$

$$\begin{aligned}
 x &= \frac{(3-2i) \pm \sqrt{(3-2i)^2 - 4(1)(-(2i-2))}}{2(1)} \\
 &= \frac{(3-2i) \pm \sqrt{9-4-12i+8i-8}}{2} \\
 &= \frac{3-2i \pm \sqrt{-3-4i}}{2} \\
 &= \frac{3-2i \pm \sqrt{(1)^2 + (2i)^2 - 2(1)(2i)}}{2} \\
 &= \frac{3-2i \pm (1-2i)}{2} \\
 \Rightarrow & \frac{3-2i+1-2i}{2} \text{ or } \frac{3-2i-1+2i}{2}
 \end{aligned}$$

5. If the midpoint of a chord of the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  is  $(\sqrt{2}, 4/3)$ , and the length of the chord is  $\frac{2\sqrt{\alpha}}{3}$ , then  $\alpha$  is :

**Ans. (2)**

Sol



If  $m \left( \sqrt{2}, \frac{4}{3} \right)$  than equation of AB is

$$T = S_1$$

$$\frac{x\sqrt{2}}{9} + \frac{y}{4} \left( \frac{4}{3} \right) = \frac{(\sqrt{2})^2}{9} + \frac{\left( \frac{4}{3} \right)^2}{4}$$

$$\frac{\sqrt{2}x}{9} + \frac{y}{3} = \frac{2}{9} + \frac{4}{9}$$

$$\sqrt{2}x + 3y = 6 \Rightarrow y = \frac{6 - \sqrt{2}x}{3} \text{ put in ellipse}$$

$$\text{So, } \frac{x^2}{9} + \frac{(6 - \sqrt{2}x)^2}{9 \times 4} = 1$$

$$4x^2 + 36 + 2x^2 - 12\sqrt{2}x = 36$$

$$6x^2 - 12\sqrt{2}x = 0$$

$$x = 0 \text{ & } x = 2\sqrt{2}$$

$$\text{So } y = 2 \quad y = \frac{2}{3}$$

$$\text{Length of chord} = \sqrt{\left(2\sqrt{2} - 0\right)^2 + \left(\frac{2}{3} - 2\right)^2}$$

$$= \sqrt{8 + \frac{16}{9}}$$

$$= \sqrt{\frac{88}{9}} = \frac{2}{3}\sqrt{22} \text{ so } [\alpha = 22]$$

6. Let S be the set of all the words that can be formed by arranging all the letters of the word GARDEN. From the set S, one word is selected at random. The probability that the selected word will NOT have vowels in alphabetical order is :

$$(1) \frac{1}{4} \qquad (2) \frac{2}{3}$$

$$(3) \frac{1}{3} \qquad (4) \frac{1}{2}$$

**Ans. (4)**



**Level up your prep for JEE Adv. 2025 with  
ALLEN Online's LIVE Rank Booster Course!**

**Enrol Now**







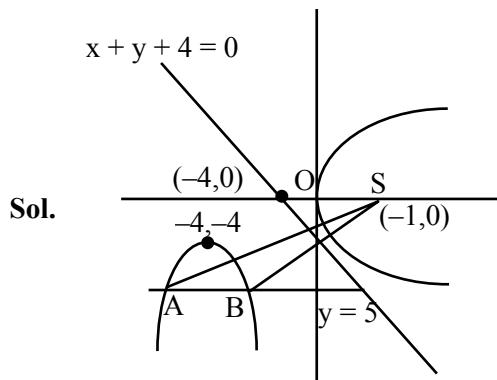






24. Let A and B be the two points of intersection of the line  $y + 5 = 0$  and the mirror image of the parabola  $y^2 = 4x$  with respect to the line  $x + y + 4 = 0$ . If d denotes the distance between A and B, and a denotes the area of  $\Delta SAB$ , where S is the focus of the parabola  $y^2 = 4x$ , then the value of  $(a + d)$  is \_\_\_\_\_.

**Ans. (14)**



**Sol.**

$$\text{Area} = \frac{1}{2} \times 4 \times 5 = 10 = a$$

$$d = 4$$

$$\text{So } a + d = 14$$

25. If  $y = y(x)$  is the solution of the differential equation,

$$\sqrt{4-x^2} \frac{dy}{dx} = \left( \left( \sin^{-1} \left( \frac{x}{2} \right) \right)^2 - y \right) \sin^{-1} \left( \frac{x}{2} \right),$$

$$-2 \leq x \leq 2, y(2) = \left( \frac{\pi^2 - 8}{4} \right), \text{ then } y(0) \text{ is equal to } \underline{\hspace{2cm}}.$$

**Ans. (4)**

$$\begin{aligned} \text{Sol. } \frac{dy}{dx} + \frac{\left( \sin^{-1} \frac{x}{2} \right)}{\sqrt{4-x^2}} y &= \frac{\left( \sin^{-3} \frac{x}{2} \right)^3}{\sqrt{4-x^2}} \\ y e^{\int \frac{\left( \sin^{-1} \frac{x}{2} \right)^2}{\sqrt{4-x^2}} dx} &= \int \frac{\left( \sin^{-3} \frac{x}{2} \right)^3}{4-x^2} e^{\int \frac{\left( \sin^{-1} \frac{x}{2} \right)^2}{\sqrt{4-x^2}} dx} dx \\ y &= \left( \sin^{-1} \frac{x}{2} \right)^2 - 2 + c.e^{-\int \frac{\left( \sin^{-1} \frac{x}{2} \right)^2}{\sqrt{4-x^2}} dx} \\ y(2) &= \frac{\pi^2}{4} - 2 \Rightarrow c = 0 \\ y(0) &= -2 \end{aligned}$$



Level up your prep for JEE Adv. 2025 with  
ALLEN Online's LIVE Rank Booster Course!

Enrol Now



# Level up your prep for JEE Adv. 2025 with our **Online Rank Booster Course!**



LIVE classes for JEE Main & Advanced



Soft copies of ALLEN's study material

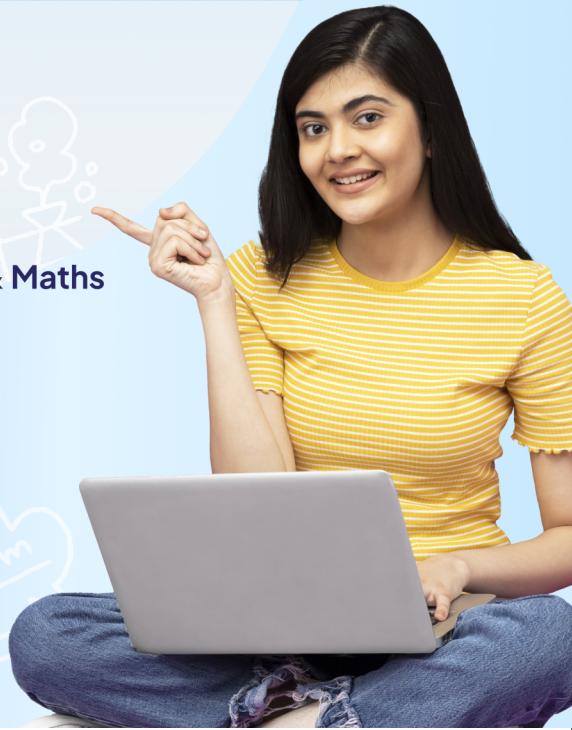


Covers important questions across **Physics, Chemistry & Maths**



ALLEN App Advantage: **24/7 doubt support,  
Custom Practice & more**

**Enrol Now**



Win up to  
**90% scholarship\***  
with the ALLEN Online Scholarship Test

at just **₹49/-**



1-hour online test  
Can be taken from anywhere

**Register Now**

