

**FINAL JEE–MAIN EXAMINATION – APRIL, 2023**

**(Held On Saturday 08<sup>th</sup> April, 2023)**

**TIME : 9 : 00 AM to 12 : 00 NOON**

**PHYSICS**

**TEST PAPER WITH SOLUTION**

**SECTION-A**

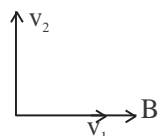
31. A charge particle moving in magnetic field B, has the components of velocity along B as well as perpendicular to B. The path of the charge particle will be

- (1) helical path with the axis perpendicular to the direction of magnetic field B
- (2) straight along the direction of magnetic field B
- (3) helical path with the axis along magnetic field B
- (4) circular path

**Official Ans. by NTA (3)**

**Allen Ans. (3)**

**Sol.**



Due to component  $v_1$ ,

magnetic force  $F = qv_1B\sin\theta=0$

So  $v_1$  remains unchanged

but due to component  $v_2$  magnetic force act towards centre i.e. moving it circular. So path is helical with the axis parallel to magnetic field B.

32. Two projectiles A and B are thrown with initial velocities of 40 m/s and 60 m/s at angles  $30^\circ$  and  $60^\circ$  with the horizontal respectively. The ratio of their ranges respectively is ( $g=10\text{ m/s}^2$ )

- (1)  $\sqrt{3} : 2$
- (2)  $2 : \sqrt{3}$
- (3)  $1 : 1$
- (4)  $4 : 9$

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

**Sol.**  $R_1 = \frac{u_1^2 \sin 2\theta_1}{g}; R_2 = \frac{u_2^2 \sin 2\theta_2}{g}$

$$\frac{R_1}{R_2} = \frac{u_1^2 \sin 2\theta_1}{u_2^2 \sin 2\theta_2} = \frac{40^2 \sin(2 \times 30^\circ)}{60^2 \sin(2 \times 60^\circ)} = \frac{4}{9}$$

33. Certain galvanometers have a fixed core made of non magnetic metallic material. The function of this metallic material is

- (1) to oscillate the coil in magnetic field for longer period of time
- (2) to bring the coil to rest quickly
- (3) to produce large deflecting torque on the coil
- (4) to make the magnetic field radial

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

**Sol.** Due to motion of the coil eddy current develops thus bringing the coil to rest.

34. A TV transmitting antenna is 98 m high and the receiving antenna is at the ground level. If the radius of the earth is 6400 km, the surface area covered by the transmitting antenna is approximately:

- (1) 1240 km<sup>2</sup>
- (2) 3942 km<sup>2</sup>
- (3) 4868 km<sup>2</sup>
- (4) 1549 km<sup>2</sup>

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

**Sol.**  $h_T = 98\text{m}, h_R = 0, R = 6400\text{ km}$

$$d = \sqrt{2h_T \cdot R} + \sqrt{2h_R \cdot R}$$

$$= \sqrt{2 \times 98 \times 6400 \times 10^3} + 0 = \frac{112}{\sqrt{10}} \text{ km}$$

So area =  $\pi d^2$

$$= 3.14 \times \frac{112^2}{10} = 3942 \text{ km}^2$$

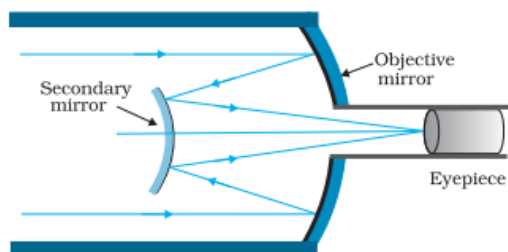
35. In a reflecting telescope, a secondary mirror is used to:

- (1) reduce the problem of mechanical support
- (2) remove spherical aberration
- (3) make chromatic aberration zero
- (4) move the eyepiece outside the telescopic tube

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

Sol.



It has advantage of a large focal length in a short telescope

36. Given below are two statements:

**Statement I:** If heat is added to a system, its temperature must increase.

**Statement II:** If positive work is done by a system in a thermodynamic process, its volume must increase.

In the light of the above statements, choose the correct answer from the options given below

- (1) Statement I is true but Statement II is false
- (2) Both Statement I and Statement II are true
- (3) Both Statement I and Statement II are false
- (4) Statement I is false but Statement II is true

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

**Sol. Statement I:**  $\Delta Q > 0$

According to 1<sup>st</sup> law of thermodynamics

$$\Delta Q = \Delta U + W$$

If  $\Delta Q > 0$ ,  $\Delta U < 0$  and  $W > 0$  is also possible.

Hence  $\Delta T < 0$ , so T decreases.

Statement I is false

**Statement II:**  $W > 0$

$$\therefore \int P dv > 0$$

Therefore volume of system must increase during positive work done by the system.

Statement II is true

37. The weight of a body on the earth is 400 N. Then weight of the body when taken to a depth half of the radius of the earth will be:

- (1) Zero
- (2) 300 N
- (3) 100 N
- (4) 200 N

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

**Sol.**  $W = mg = 400 \text{ N}$

$$\text{At depth } d, \text{ gravity } g' = g \left( 1 - \frac{d}{R} \right)$$

$$\text{For } d = \frac{R}{2} \quad g' = g \left( 1 - \frac{R}{2R} \right) = \frac{g}{2}$$

$$W' = mg' = \frac{mg}{2} = 200 \text{ N}$$

38. An aluminium rod with Young's modulus  $Y = 7.0 \times 10^{10} \text{ N/m}^2$  undergoes elastic strain of 0.04%. The energy per unit volume stored in the rod in SI unit is:

- (1) 5600
- (2) 8400
- (3) 2800
- (4) 11200

**Official Ans. by NTA (1)**

**Allen Ans. (1)**

**Sol.**  $Y = 7 \times 10^{10} \text{ N/m}^2$

$$\text{Strain} = \frac{0.04}{100}$$

$$\text{Energy} = \frac{1}{2} \left( \frac{YA}{l} \right) \Delta x^2$$

$$\text{Energy} = \frac{1}{2} YA \left( \frac{\Delta x}{l} \right)^2 \times l$$

$$\frac{E}{V} = \frac{1}{2} \times Y \times \text{strain}^2$$

$$= \frac{1}{2} \times 7 \times 10^{10} \times \frac{0.04 \times 0.04}{10^4} = 56 \times 10^2$$

39. At any instant the velocity of a particle of mass 500 g is  $(2t\hat{i} + 3t^2\hat{j})\text{ms}^{-1}$ . If the force acting on the particle at  $t=1\text{s}$  is  $(\hat{i} + x\hat{j})\text{N}$ . Then the value of  $x$  will be:

(1) 3 (2) 4 (3) 6 (4) 2

Official Ans. by NTA (1)

Allen Ans. (1)

Sol.  $\vec{v} = 2t\hat{i} + 3t^2\hat{j}$

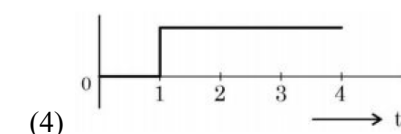
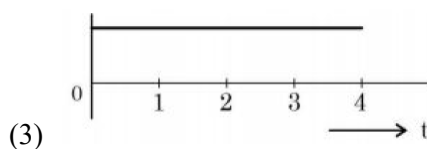
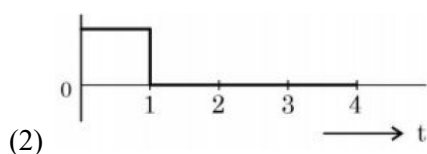
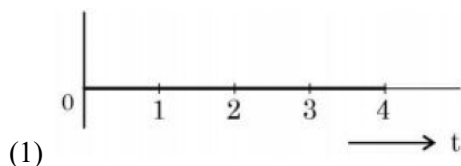
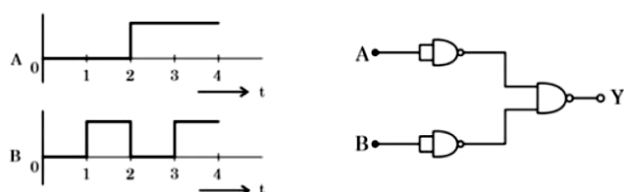
$$\vec{a} = 2\hat{i} + 6t\hat{j}$$

at  $t=1$ ,  $\vec{a} = 2\hat{i} + 6\hat{j}$

$$\vec{F} = m\vec{a} = 0.5(2\hat{i} + 6\hat{j}) = \hat{i} + 3\hat{j}$$

$$\vec{F} = \hat{i} + x\hat{j} \quad \text{Hence } x = 3$$

40. For the logic circuit shown, the output waveform at Y is:



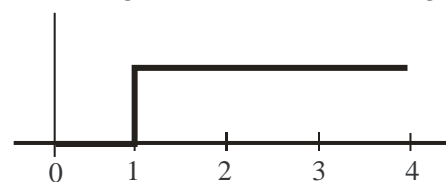
Official Ans. by NTA (4)

Allen Ans. (4)

Sol.

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

According to truth table, resultant graph is



41. For a nucleus  ${}^A_Z\text{X}$  having mass number  $A$  and atomic number  $Z$

- A. The surface energy per nucleon  $(b_s) = a_1 A^{2/3}$   
 B. The Coulomb contribution to the binding energy  $b_c = -a_2 \frac{Z(Z-1)}{A^{4/3}}$   
 C. The volume energy  $b_v = a_3 A$   
 D. Decrease in the binding energy is proportional to surface area.  
 E. While estimating the surface energy, it is assumed that each nucleon interacts with 12 nucleons, ( $a_1$ ,  $a_2$  and  $a_3$  are constants)

Choose the **most appropriate** answer from the options given below:

- (1) C, D only (2) B, C, E only  
 (3) A, B, C, D only (4) B, C only

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. Surface energy per nucleon  $\propto \frac{r^2}{A} \propto \frac{A^{2/3}}{A} \propto \frac{1}{A^{1/3}}$

$$\left( \text{Mass number } A \propto r^3 \Rightarrow r \propto A^{1/3} \right).$$

A is incorrect

Contribution to binding energy by columbic forces is

$$= \frac{-a_2 Z(Z-1)}{A^{1/3}}$$

B is incorrect

Volume energy  $\propto A$

C is correct

For (D), if we consider only surface energy contribution then option is correct.

For (E) only 3 interactions contribute to surface energy.

42. Given below are two statements:

**Statement I :**

If E be the total energy of a satellite moving around the earth, then its potential energy will be  $\frac{E}{2}$ .

**Statement II:**

The kinetic energy of a satellite revolving in an orbit is equal to the half the magnitude of total energy E.

In the light of the above statements, choose the most appropriate answer from the options given below

- (1) Both Statement I and Statement II are correct
- (2) Both Statement I and Statement II are incorrect
- (3) Statement I is incorrect but Statement II is correct
- (4) Statement I is correct but Statement II is incorrect

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

**Sol.** Energy of satellite in orbit  $E = \frac{-GMm}{2R}$ .

PE of satellite in orbit  $U = \frac{-GMm}{R}$

$\Rightarrow U = 2E$

KE of satellite in orbit  $K = E - U$

$$K = \frac{GMm}{2R} = (-E)$$

43. Dimension of  $\frac{1}{\mu_0 \epsilon_0}$  should be equal to

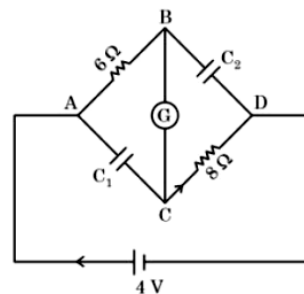
- (1)  $T^2/L^2$
- (2)  $L/T$
- (3)  $L^2/T^2$
- (4)  $T/L$

**Official Ans. by NTA (3)**

**Allen Ans. (3)**

**Sol.**  $\frac{1}{\mu_0 \epsilon_0} = c^2 \Rightarrow \left[ \frac{1}{\mu_0 \epsilon_0} \right] = [c^2] = [L^2 T^{-2}]$

44. In this figure the resistance of the coil of galvanometer G is  $2 \Omega$ . The emf of the cell is 4 V. The ratio of potential difference across  $C_1$  and  $C_2$  is:



- (1) 1
- (2)  $\frac{4}{5}$
- (3)  $\frac{3}{4}$
- (4)  $\frac{5}{4}$

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

**Sol.** At steady state, current in the circuit is

$$i = \frac{4V}{6 + 2 + 8} = \frac{1}{4} A$$

Voltage across  $C_1$  is

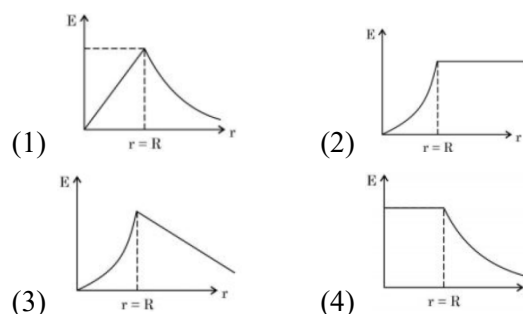
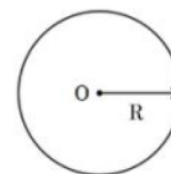
$$V_1 = V_{AC} = i(6\Omega + 2\Omega) = \frac{1}{4} \times 8 = 2V$$

Voltage across  $C_2$  is

$$V_2 = V_{BD} = i(2\Omega + 8\Omega) = \frac{1}{4} \times 10 = 2.5V$$

$$\Rightarrow \frac{V_1}{V_2} = \frac{2}{2.5} = \frac{4}{5}$$

45. Graphical variation of electric field due to a uniformly charged insulating solid sphere of radius R, with distance r from the centre O is represented by:



**Official Ans. by NTA (1)**

**Allen Ans. (1)**

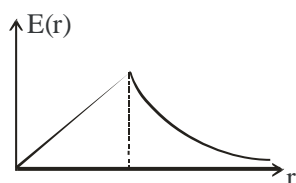
**Sol.** Electric field of solid sphere (uniformly charged)

$$E(r) \begin{cases} \frac{Q}{4\pi\epsilon_0 r^2} & r \geq R \\ \frac{Qr}{4\pi\epsilon_0 R^3} & r \leq R \end{cases}$$

Graphically

$$E(r) \propto r \text{ for } r \leq R$$

$$\propto \frac{1}{r^2} \text{ for } r \geq R$$



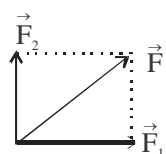
46. Two forces having magnitude  $A$  and  $\frac{A}{2}$  are perpendicular to each other. The magnitude of their resultant is

- (1)  $\frac{\sqrt{5}A}{4}$  (2)  $\frac{5A}{2}$   
(3)  $\frac{\sqrt{5}A^2}{2}$  (4)  $\frac{\sqrt{5}A}{2}$

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

**Sol.**



$$\vec{F} = (\vec{F}_1 + \vec{F}_2)$$

$$|\vec{F}| = \sqrt{F_1^2 + F_2^2 + 2F_1F_2 \cos 90^\circ}$$

$$= \sqrt{A^2 + \frac{A^2}{4}} = \frac{A\sqrt{5}}{2}$$

47. The engine of a train moving with speed  $10\text{ms}^{-1}$  towards a platform sounds a whistle at frequency  $400\text{Hz}$ . The frequency heard by a passenger inside the train is (neglect air speed. Speed of sound in air  $330\text{ms}^{-1}$ )

- (1)  $200\text{Hz}$  (2)  $400\text{Hz}$   
(3)  $412\text{Hz}$  (4)  $388\text{Hz}$

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

- Sol.** The relative velocity of a passenger with source of sound (engine) is 0. So there will be no doppler's effect. So frequency heard is  $400\text{Hz}$ .

48. An air bubble of volume  $1\text{cm}^3$  rises from the bottom of a lake  $40\text{m}$  deep to the surface at a temperature of  $12^\circ\text{C}$ . The atmospheric pressure is  $1 \times 10^5\text{Pa}$ , the density of water is  $1000\text{kg/m}^3$  and  $g = 10\text{m/s}^2$ . There is no difference of the temperature of water at the depth of  $40\text{m}$  and on the surface. The volume of air bubble when it reaches the surface will be

- (1)  $5\text{cm}^3$  (2)  $2\text{cm}^3$   
(3)  $4\text{cm}^3$  (4)  $3\text{cm}^3$

**Official Ans. by NTA (1)**

**Allen Ans. (1)**

- Sol.**  $P = P_0 + \rho gh = 10^5\text{Pa} + 10^3 \times 10 \times 40 = 5 \times 10^5\text{Pa}$

At  $T$  is constant

$$PV = P_0V_0$$

$$\Rightarrow 5 \times 10^5\text{Pa} \times 1\text{cm}^3 = 10^5\text{Pa} \times V_0 \Rightarrow V_0 = 5\text{cm}^3$$

49. A cylindrical wire of mass  $(0.4 \pm 0.01)\text{g}$  has length  $(8 \pm 0.04)\text{cm}$  and radius  $(6 \pm 0.03)\text{mm}$ . The maximum error in its density will be

- (1)  $1\%$  (2)  $3.5\%$   
(3)  $4\%$  (4)  $5\%$

**Official Ans. by NTA (3)**

**Allen Ans. (3)**

**Sol.**  $\rho = \frac{m}{\pi r^2 l} \Rightarrow \left| \frac{d\rho}{\rho} \right|_{\max} = \left| \frac{dm}{m} \right| + 2 \left| \frac{dr}{r} \right| + \left| \frac{dl}{l} \right|$

$$= \frac{0.01}{0.4} + \frac{2(0.03)}{6} + \frac{0.04}{8}$$

$$\Rightarrow \% \text{ error in density} = \left( \frac{d\rho}{\rho} \right) \times 100\%$$

$$= (2.5 + 1 + 0.5)\% = 4\%$$

- 50.** Proton (P) and electron (e) will have same de-Broglie wavelength when the ratio of their momentum is (assume,  $m_p = 1849m_e$ )

(1) 1 : 43                                      (2) 43 : 1

(3) 1 : 1849                                      (4) 1 : 1

**Official Ans. by NTA (4)**

**Allen Ans. (4)**

**Sol.** De Broglie wavelength is  $\lambda = \frac{h}{mv}$

$$\lambda_p = \lambda_e \Rightarrow m_p v_p = m_e v_e \Rightarrow p_p = p_e$$

### SECTION-B

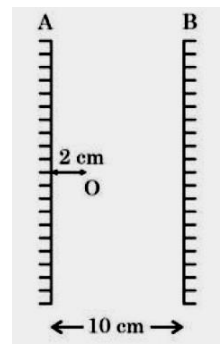
- 51.** An electric dipole of dipole moment is  $6.0 \times 10^{-6} \text{ Cm}$  placed in a uniform electric field of  $1.5 \times 10^3 \text{ NC}^{-1}$  in such a way that dipole moment is along electric field. The work done in rotating dipole by  $180^\circ$  in this field will be \_\_\_\_\_ mJ

**Official Ans. by NTA (18)**

**Allen Ans. (18)**

**Sol.** The work done in rotating the electric dipole  $= \Delta U$   
 $= U_f - U_i$   
 $= (-pE \cos(180^\circ)) - (-pE \cos(0^\circ))$   
 $= pE + pE = 2pE$   
 $= 2 \times 6 \times 10^{-6} \times 1.5 \times 10^3 = 18 \text{ mJ}$

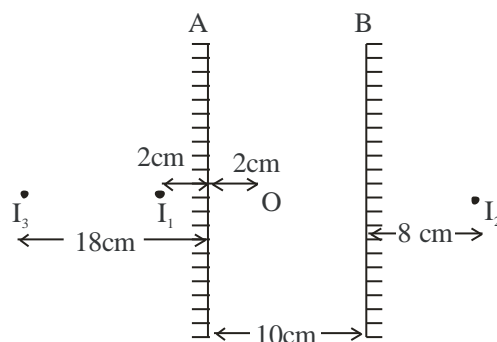
- 52.** Two vertical parallel mirrors A and B are separated by 10 cm. A point object O is placed at a distance of 2 cm from mirror A. The distance of the second nearest image behind mirror A from the mirror A is \_\_\_\_\_ cm



**Official Ans. by NTA (18)**

**Allen Ans. (18)**

**Sol.**



The desired image is 18 cm from A.

- 53.** The momentum of a body is increased by 50%. The percentage increase in the kinetic energy of the body is \_\_\_\_\_ %

**Official Ans. by NTA (125)**

**Allen Ans. (125)**

**Sol.** Kinetic energy of body  $= \frac{p^2}{2m}$

Initial kinetic energy  $= \frac{p_i^2}{2m}$

Final kinetic energy  $= \frac{p_f^2}{2m} = \frac{(1.5 p_i)^2}{2m}$

$$= \frac{2.25 p_i^2}{2m}$$

$$\% \text{ increase in KE} = \frac{2.25 \frac{p_i^2}{2m} - \frac{p_i^2}{2m}}{\frac{p_i^2}{2m}} \times 100 = 125\%$$

54. The moment of inertia of semicircular ring about an axis, passing through the center and perpendicular to the plane of ring, is  $\frac{1}{x}MR^2$ , where R is the radius and M is the mass of semicircular ring. The value of x will be

**Official Ans. by NTA (1)**

**Allen Ans. (1)**

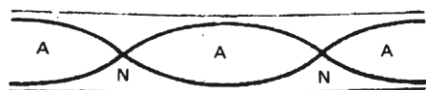
- Sol.** The moment of inertia of semicircular ring about axis passing through centre of ring and perpendicular to plane of ring is  $= MR^2$   
so  $x = 1$

55. An organ pipe 40cm long is open at both ends. The speed of sound in air is  $360\text{ms}^{-1}$ . The frequency of the second harmonic is \_\_\_\_ Hz.

**Official Ans. by NTA (900)**

**Allen Ans. (900)**

**Sol.**



For second harmonic of open organ pipe

$$L = \lambda$$

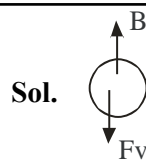
So frequency of vibration is  $f = \frac{V}{\lambda}$

$$f = \frac{V}{\lambda} = \frac{V}{L} = \frac{360}{\frac{40}{100}} = 900\text{Hz}$$

56. An air bubble of diameter 6 mm rises steadily through a solution of density  $1750\text{kg/m}^3$  at the rate of  $0.35\text{ cm/s}$ . The co-efficient of viscosity of the solution (neglect density of air) is \_\_\_\_ Pas (given,  $g = 10\text{ms}^{-2}$ )

**Official Ans. by NTA (10)**

**Allen Ans. (10)**



**Sol.**

Since the bubble is moving at constant speed the force acting on it is zero.

$$B = F_v$$

$$\frac{4}{3}\pi R^3 \rho g = 6\pi \eta R v$$

$$\eta = \frac{2R^2 \rho g}{9v} = \frac{2 \times (3 \times 10^{-3})^2 \times 1750 \times 10}{9 \times 0.35 \times 10^{-2}} = 10\text{Pas}$$

57. An oscillating LC circuit consists of a 75 mH inductor and a  $1.2\mu\text{F}$  capacitor. If the maximum charge to the capacitor is  $2.7\mu\text{C}$ . The maximum current in the circuit will be \_\_\_\_ mA.

**Official Ans. by NTA (9)**

**Allen Ans. (9)**

- Sol.** Maximum energy stored in capacitor is same as maximum energy stored in inductor.

$$\frac{1}{2}Li_{\text{max}}^2 = \frac{1}{2}\frac{Q_{\text{max}}^2}{C}$$

$$i_{\text{max}} = \sqrt{\frac{1}{LC}}Q_{\text{max}}$$

$$= \frac{2.7 \times 10^{-6}}{\sqrt{75 \times 10^{-3} \times 1.2 \times 10^{-6}}} = 9\text{mA}$$

58. The magnetic intensity at the centre of a long current carrying solenoid is found to be  $1.6 \times 10^3\text{ Am}^{-1}$ . If the number of turns is 8 per cm, then the current flowing through the solenoid is \_\_\_\_ A.

**Official Ans. by NTA (2)**

**Allen Ans. (2)**

**Sol.**  $H = \frac{B}{\mu_0} = \frac{\mu_0 n i}{\mu_0} = ni$

$$i = \frac{H}{n} = \frac{1.6 \times 10^3}{\left(\frac{8}{10^{-2}}\right)} = 2\text{A}$$

59. A current of 2 A flows through a wire of cross-sectional area  $25.0 \text{ mm}^2$ . The number of free electrons in a cubic meter are  $2.0 \times 10^{28}$ . The drift velocity of the electrons is  $\text{_____} \times 10^{-6} \text{ ms}^{-1}$  (given, charge on electron =  $1.6 \times 10^{-19} \text{ C}$ )

**Official Ans. by NTA (25)**

**Allen Ans. (25)**

**Sol.** Drift velocity  $v_d = \frac{I}{neA}$

$$= \frac{2}{2 \times 10^{28} \times 1.6 \times 10^{-19} \times 25 \times 10^{-6}}$$

$$= 25 \times 10^{-6} \text{ ms}^{-1}$$

60. A nucleus with mass number 242 and binding energy per nucleon as 7.6 MeV breaks into fragment each with mass number 121. If each fragment nucleus has binding energy per nucleon as 8.1 MeV, the total gain in binding energy is  $\text{_____ MeV}$

**Official Ans. by NTA (121)**

**Allen Ans. (121)**

- Sol.** Initial binding energy =  $242 \times 7.6 \text{ MeV}$   
Final binding energy

$$= 121 \times 8.1 \text{ MeV} + 121 \times 8.1 \text{ MeV}$$

$$= 242 \times 8.1 \text{ MeV}$$

Total gain in binding energy

$$= 242 (8.1 - 7.6) = 121 \text{ MeV}$$