



Sec: Sr.Super60\_STERLING BT

Paper -2(Adv-2022-P2-Model)

Date: 14-09-2025

Time: 02.00Pm to 05.00Pm

CTA-03

Max. Marks: 180

## KEY SHEET

### MATHEMATICS

1	<b>2</b>	2	1	3	<b>6</b>	4	<b>5</b>	5	<b>8</b>	6	<b>4</b>
7	<b>2</b>	8	<b>2</b>	9	<b>AD</b>	10	<b>CD</b>	11	<b>ABD</b>	12	<b>BCD</b>
13	<b>BD</b>	14	<b>BCD</b>	15	<b>C</b>	16	<b>A</b>	17	<b>D</b>	18	<b>B</b>

### PHYSICS

19	<b>2</b>	20	<b>3</b>	21	<b>4</b>	22	<b>2</b>	23	<b>1</b>	24	<b>8</b>
25	<b>9</b>	26	<b>4</b>	27	<b>BC</b>	28	<b>ABC</b>	29	<b>CD</b>	30	<b>AC</b>
31	<b>AC</b>	32	<b>BD</b>	33	<b>A</b>	34	<b>A</b>	35	<b>B</b>	36	<b>D</b>

### CHEMISTRY

37	<b>2</b>	38	<b>6</b>	39	<b>5</b>	40	<b>6</b>	41	<b>7</b>	42	<b>3</b>
43	<b>2</b>	44	<b>4</b>	45	<b>ABCD</b>	46	<b>ABCD</b>	47	<b>ABCD</b>	48	<b>AC</b>
49	<b>ACD</b>	50	<b>ABCD</b>	51	<b>A</b>	52	<b>D</b>	53	<b>B</b>	54	<b>B</b>

## SOLUTIONS MATHS

1. Let  $f(x) = k^x$   $f(a_{31}) = k^{a+30d}$   $f(a_{25}) = k^{a+24d}$

$$\sum_{i=6}^{30} f(a_i) = \frac{3}{2^{25}-1} \times 2^5 \times \frac{(2^{25}-1)}{2-1} = 96$$

2.  $f(x) = 100\{x\} \Rightarrow f(\sqrt{2}) = 100\{\sqrt{2}\} = 100 \times 0.414 = 41.4$   
 $[f\sqrt{2}] = 41$

3.  $L = \frac{-\lim_{x \rightarrow 0} \frac{d}{dx} \prod_{r=2}^n (\cos rx)^{-1}}{2x}$

Let  $y = \prod_{r=2}^n (\cos 2x) \Rightarrow$

$$\log y = \sum_{r=2}^n \frac{1}{2} \ln(\cos rx)$$

$$\frac{1}{y} \frac{dy}{dx} = -\sum_{r=2}^n \tan x$$

$$\Rightarrow \frac{dy}{dx} = -y \sum_{r=2}^n \tan rx$$

$$= \frac{1}{2}[2 + 3 + \dots + n] = \left[ \frac{n(n+1)}{2} - 1 \right] \frac{1}{2} = \frac{n^2 + n - 2}{4} = 10$$

$$\Rightarrow n = 6$$

4. We have  $(gof)(x) = x$

$$\Rightarrow g'(f(x)) \cdot f'(x) = 1$$

$$\text{when } f(x) = -\frac{7}{6}, x = 1$$

$$g'\left(-\frac{7}{6}\right) f'(1) = 1$$

$$g'\left(-\frac{7}{6}\right) = \frac{1}{f'(1)} = \frac{1}{5}$$

$$\frac{1}{g'\left(-\frac{7}{6}\right)} = 5$$

5. Let  $f(x)$  is non-differentiable at  $x = 0, 1$

$$\text{Also } f\left(\frac{1}{2} + x\right) = f\left(\frac{1}{2} - x\right)$$

Hence graph of  $f(x)$  is symmetrical about the line  $x = 1/2$   
 Where derivable is zero



$$\text{Local min.} = f\left(\frac{1}{2}\right) = \frac{4}{3}$$

$$\text{global max.} = f(0) = f(1) = \frac{3}{2}$$

$$\therefore k = \frac{4}{3} + \frac{3}{2} = \frac{17}{6}$$

$$6k - 9 = 8$$

$$\begin{aligned} 6. \quad & \int_0^1 f(x) dx + \int_1^2 f(x) dx + \int_0^{30} f^{-1}(y) dy \\ &= \int_0^1 (4x^3 + 2x - 6) dx + \int_1^2 f(x) dx + \int_1^2 t f'(t) dt \\ &= [x^4 + x^2 - 6x]_0^1 + \int_1^2 f(x) dx + (t f(t))_1^2 - \int_1^2 f(t) dt \\ &= -4 + (2 f(2) - f(1)) \\ &= -4 + 2 \times 30 - 0 \\ &= 56 \end{aligned}$$

$$7. \quad A = 2 \int_0^1 [y \sqrt{1-y^2} - (y^2 - 1)] dy = 2$$

$$\begin{aligned} 8. \quad & \int \frac{dy_1}{y_1} + \frac{dy_2}{y_2} + \frac{dy_3}{y_3} = \int \left( \sin^2 x + \cos^2 x + \frac{2}{x^3} - 1 \right) dx \\ & \log_e |y_1 y_2 y_3| = \frac{-2}{x^2} + C \\ &= \lim_{x \rightarrow 0^+} \frac{y_1 y_2 y_3}{e^{3x} \sin x} = \lim_{x \rightarrow 0^+} \frac{2x \pm e^{-1/x^2}}{e^{3x} \sin x} = 2 \end{aligned}$$

$$9. \quad \frac{dy}{dx} = \frac{(x+1)^2 + y - 3}{x+1} = x + 1 + \frac{y-3}{x+3}$$

Putting  $x+1=X$  and  $y-3=Y$

$$\frac{dY}{dX} = X + \frac{Y}{X}$$

$$\Rightarrow \frac{dy}{dx} - \frac{y}{x} = x$$

Solution is  $\frac{y}{x} = x + c$

$$\Rightarrow y - 3 = (x+1)^2 + (2+1)$$

It passes through  $(2, 0) \Rightarrow c = -4$

Equation of curve is  $y = x^2 - 2x$



$$\text{Area bounded} = \int_0^2 (2x - x^2) dx = \frac{4}{3} \text{sq.u}$$

10.  $u = \int_0^\infty \frac{1}{x^4 + 7x^2 + 1} dx$  put  $X = \frac{1}{t}$ ,  $dx = \frac{-1}{t^2} dt$

$$u = \int_{\infty}^0 \frac{1}{\frac{1}{t^4} + \frac{7}{t^2} + 1} \left( \frac{-dt}{t^2} \right) = \int_0^\infty \frac{t^2 dt}{t^4 + 7t^2 + 1} = v$$

$$\Rightarrow u = v$$

$$\Rightarrow 2u = \int_0^\infty \frac{\left(1 + \frac{1}{x^2}\right) dx}{\left(x - \frac{1}{x}\right)^2 + 9} = \int_0^\infty \frac{dt}{t^2 + 9} = \frac{\pi}{6} \text{ where } t = x - \frac{1}{x}$$

11.  $\frac{dy}{dx} + (2 \tan x)y = \sin x$  (LDE)

$$\Rightarrow y(x) = \cos x - 2 \cos^2 x$$

$$(A) y'\left(\frac{\pi}{6}\right) = \frac{2\sqrt{3}-1}{2} \quad (B) y(\pi) = -3$$

$$(C) y(x) = -1 \Rightarrow 2 \cos^2 x - \cos x - 1 = 0$$

$$\text{but } x \in (0, 2\pi) \Rightarrow x = \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$(D) \int_0^{\frac{\pi}{2}} y(x) dx = 1 - \frac{\pi}{2}$$

12.  $f(x)f''(x) - f(x)f'(x) = (f'(x))^2$

$$\therefore \frac{f''(x) - f'(x)}{f'(x)} = \frac{f'(x)}{f(x)}$$

One integration we set

$$\ln(f'(x)) - x = \ln(f(x)) + c$$

$$\therefore \ln(f(x)) = e^x + d$$

$$f(0) = 1 \Rightarrow d = -1$$

$$f(x) = e^{e^x - 1}$$

$$\text{Hence, } \lim_{x \rightarrow -\infty} f(x) = e^{-1}$$

$$\lim_{x \rightarrow -0} \frac{f(x)-1}{x} = 1$$



13.  $f(x) = x^2 - 2ax + a(a+1)$

$$f(x) = (x-a)^2 + a = a + \sqrt{x-a} = f^{-1}(x)$$

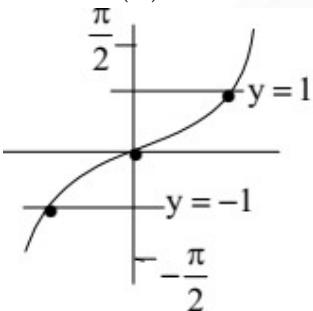
$$(x-a)^2 = \sqrt{x-a}$$

$$x = a \text{ or } a+1$$

$$\text{if } a = 5049, \text{ then } a+1 = 5050$$

$$\text{if } a+1 = 5049, \text{ then } a = 5048$$

14. (A)  $\operatorname{sgn}(x) = \sin^{-1} x$  has three solutions



(B)  $|x^2 - 4|x| + 3| = 1$

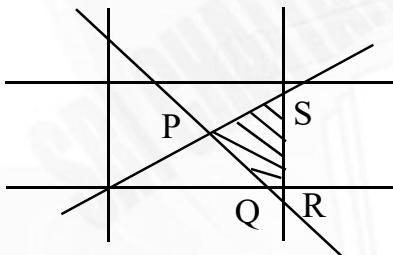
has six solutions

(C)  $\log_{10}(-x) = 4 \Rightarrow x = -10^4 = \alpha \Rightarrow \operatorname{sgn}(\alpha) = -1$

(D)  $\sin^{-1} x + \cos^{-1} x + \tan^{-1} x \neq 0$  and  $\sin^{-1} x, \cos^{-1} x, \tan^{-1} x$  can't be equal for same 'x'

15. Conceptual

16.  $x + y - 2 = 0, x = 3y, x = \frac{9}{4}, y = 1$



$$P\left(\frac{3}{2}, \frac{1}{2}\right), Q(2, 0), R\left(\frac{9}{4}, 0\right), S\left(\frac{9}{4}, \frac{3}{4}\right)$$

$$\text{area} = \frac{11}{32}$$

17.  $x_1 = 10, y_1 = 5 \quad PQ = \min = \sqrt{(10-5)^2 + 5^2} = 5\sqrt{2} - 2 \Rightarrow PQ^2 = (5\sqrt{2} - 2)^2$

18.  $\frac{1}{2}$

## PHYSICS

19.  $W = q\Delta V$
20. Opposite faces having equal and opposite charges
21.  $W_g = m(V_A - V_B)$

$$V_A = -\frac{GM_1}{R} - \frac{GM_2}{2R}$$

$$\text{and } V_B = -\frac{2GM_2}{2R} - \frac{GM_1}{2R}$$

$$22. \frac{n_1}{\gamma_1 - 1} + \frac{n_2}{\gamma_2 - 1} = \frac{n_1 + n_2}{\gamma_{\text{mean}} - 1}$$

$$23. \frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2}$$

24. Velocity of object relative to mirror

$$[\vec{v}_{\text{om}}]_{\perp} = 16\hat{i} - (-18\hat{i}) = +34\hat{i} \text{ m/s}$$

Velocity of its image

$$[\vec{v}_{\text{im}}]_{\perp} = -34\hat{i} \text{ m/s}$$

Now velocity of image w.r.t ground observer

$$[\vec{v}_{\text{ig}}]_{\perp} = [\vec{v}_{\text{im}}]_{\perp} + [\vec{v}_m]_{\perp}$$

$$25. \frac{1}{v} + \frac{1}{-20} = \frac{1}{-30}$$

$$v_{ix} = \frac{v^2}{u^2} v_0$$

$$\text{Lateral magnification, } m = \frac{h_i}{h_0} = -\frac{v}{u}$$

$$\text{or } h_i = -h_0 \frac{v}{u}$$

$$\text{now } v_{iy} = -h_0 \left[ u \frac{dv}{dt} - v \frac{du}{dt} \right]$$

$$26. \tau = PE \sin \theta$$

$$I\alpha = PE \sin \theta$$

$$\alpha = \frac{PE}{I}$$

$$\alpha = \omega^2 \theta$$

$$27. \text{Conceptual}$$

$$28. R = \frac{u^2 \sin 2\theta}{g + \frac{\text{Eq.}}{m}}$$



$$T_1 = \frac{u \sin \theta}{g - \frac{\text{Eq.}}{m}}$$

$$T_2 = \frac{u \sin \theta}{g + \frac{\text{Eq.}}{m}}$$

$$T = T_1 + T_2$$

29. Conceptual

$$30. \frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\frac{I}{O} = \frac{v}{u}$$

$$31. dq = \rho dv$$

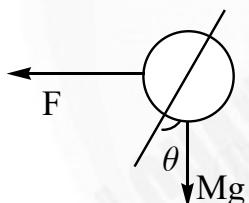
$$dq = \rho (4\pi r^2 dr)$$

$$E \oint ds = \frac{q}{\epsilon_0}$$

32. Work done is area under curve

$$dQ = dU + dW$$

33.



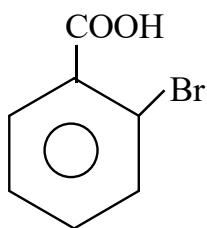
34. Opposite faces should have equal and opposite charges, earthed surface potential zero

$$35. \frac{\theta_A - \theta_F}{R} = \frac{\theta_A - \theta_B}{R_1}$$

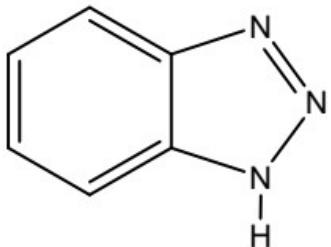
$$36. E = \sigma t_s^4 \cdot (4\pi R_s^2)$$

CHEMISTRY

37.



38.



39. Meta directing groups :

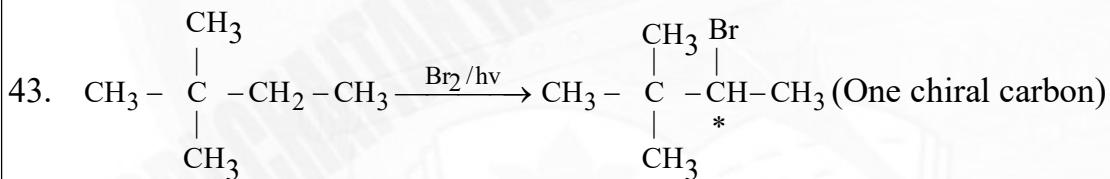


Total 5 groups are meta directing groups

40. 6

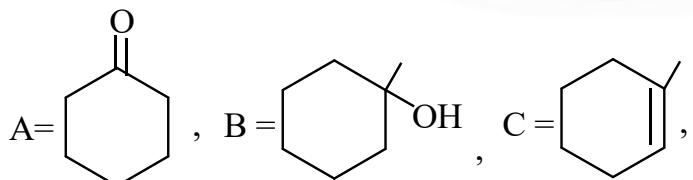
41. III, VI, VIII  $\rightarrow$  Phenolic ether will not give cleavage with HI

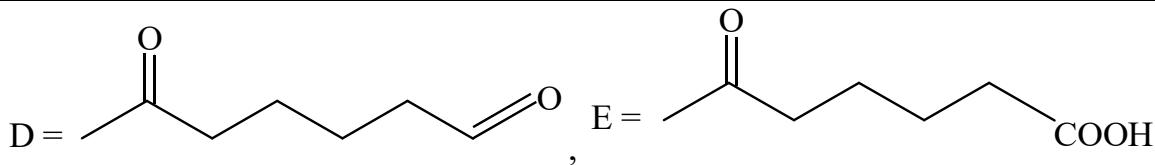
42. II, III and IV are correct



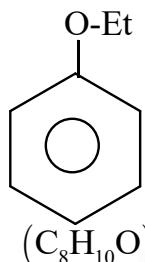
44. Given reaction is Gabriel-Phthalimide synthesis, which is involved  $\text{SN}_2$  reaction and which is applicable for the preparation of primary amines. Secondary and tertiary amines cannot be prepared by using Gabriel-Phthalimide synthesis. From the given list 2 and 8 cannot be prepared, because these amines are  $2^0$  amines. From the remaining molecules 3<sup>rd</sup> and 5<sup>th</sup> cannot be prepared, because for the preparation of these amines, substrates must be vinyl and aryl halides, which are not suitable substrates for  $\text{SN}_2$  reactions. Remaining three amines along with amide (7<sup>th</sup> molecule) can be prepared by using Gabriel. Phthalimide reaction.

45.

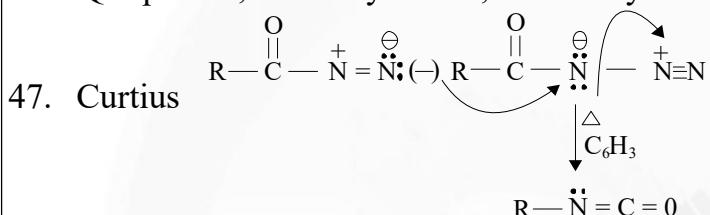




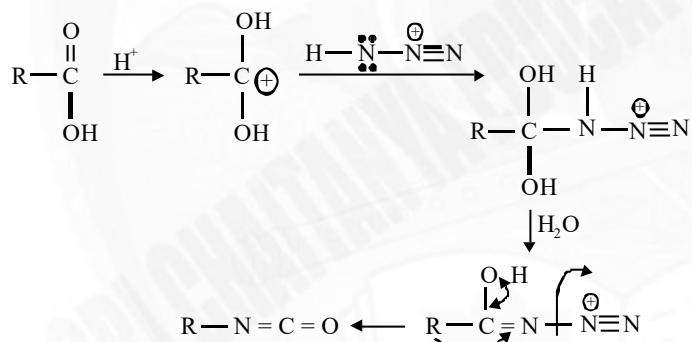
46.



Q = phenol, R = Ethyliodide, S = Salicylic acid, T = Asprine, W = ethyne



### No evidence for formation of Nitrene

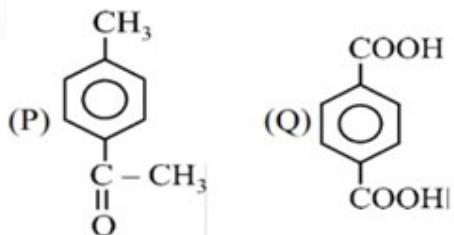


Migration is intra molecular no interne formation.

48. A = Ph - CH<sub>2</sub> - CH<sub>2</sub> - CH<sub>2</sub> - OH

49. A, C, D will give stable hydrates

50.

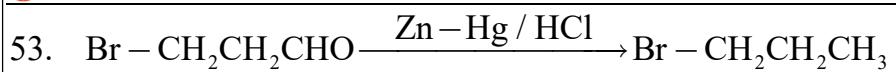


## 51. Conceptual

$$52. \quad P = C_6H_5COONH_4$$

$$Q = C_6H_5CONH_2$$

$$R = C_6H_5CH_2NH_2$$



54.

