



RANKRIDGE IIT JEE/NEET JUNIOR COLLEGE (LONGTERM)

STREAM: JR MPC

Time: 3:00 Hours

WEEKEND TEST-19

MATHEMATICS

PHYSICS

CHEMISTRY

SYLLABUS

- .: Hyperbolic functions and properties of vectors
- .: Mechanical Properties of Solids (complete chapter)
- .: Organic IUPAC nomenclature and isomerism

MATHEMATICS

(SINGLE CORRECT ANSWER TYPE)

This section contains 20 multiple choice questions.

Each question has 4 options (A), (B), (C) and (D) for its answer, out of which ONLY ONE option can be correct.

Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases.

1. The domain of $\cosh^{-1}(2x)$ is

- (A) $(-\infty, \infty)$
 (B) $[1, \infty)$
 (C) $[2, \infty)$
 (D) $\left[\frac{1}{2}, \infty\right)$

2. $\cosh(2x) + \sinh(2x) =$

- (A) $\frac{1 + \tanh(x)}{1 - \tanh(x)}$
 (B) $\frac{1 - \tanh(x)}{1 + \tanh(x)}$
 (C) $\frac{\tanh(x) - 1}{\tanh(x) + 1}$
 (D) $\frac{1 - \tanh(x)}{\tanh(x) - 1}$

3. If $\tanh^2(x) = \tan^2\theta$ then $\cosh(2x) =$

- (A) $\cos 2\theta$
 (B) $\sec 2\theta$
 (C) $\sin 2\theta$
 (D) $\cos \theta$

4. If $\tanh(x) = \frac{3}{5}$ then $\cosh(2x) =$

- (A) $\frac{15}{8}$
 (B) $\frac{17}{17}$
 (C) $\frac{8}{17}$
 (D) $\frac{17}{8}$

5. $\sinh^{-1}(2^{3/2}) =$

- (A) $\log(2 + \sqrt{8})$
 (B) $\log(3 + \sqrt{8})$

- (C) $\log(3 - \sqrt{8})$
 (D) $\log(\sqrt{8} + \sqrt{27})$

6. $\operatorname{sech}^{-1}\left(\frac{1}{2}\right) - \operatorname{cosech}^{-1}\left(\frac{3}{4}\right) =$

- (A) $\log(3(2 + \sqrt{3}))$
 (B) $\log\left(\frac{1 + \sqrt{3}}{3}\right)$
 (C) $\log\left(\frac{2 + \sqrt{3}}{3}\right)$
 (D) $\log\left(\frac{2 - \sqrt{3}}{3}\right)$

7. $\operatorname{sech}^2\left(\tanh^{-1}\frac{1}{2}\right) + \operatorname{cosech}^2(\coth^{-1}3) =$

- (A) $\frac{35}{9}$
 (B) $\frac{3}{2}$
 (C) $\frac{25}{4}$
 (D) $\frac{35}{4}$

8. If $y = \log_e \tan\left(\frac{\pi}{4} + \frac{x}{2}\right)$, then $\tanh\left(\frac{y}{2}\right) =$

- (A) $\cot hx$
 (B) $\tan x$
 (C) $\cot\left(\frac{x}{2}\right)$
 (D) $\tan\left(\frac{x}{2}\right)$

9. the solution of the equation
 $2\cosh 2x + 10 \sinh 2x = 5$ is

- (A) $\frac{1}{2} \log\left(\frac{3}{5}\right)$
 (B) $\frac{1}{2} \log\left(\frac{4}{3}\right)$
 (C) $\frac{1}{2} \log\left(\frac{5}{4}\right)$
 (D) $\frac{1}{2} \log\left(\frac{5}{3}\right)$

10. Let a, b and c be distinct non-negative numbers. If the vectors $ai + aj + ck, i + k$ and $ci + cj + bk$ lie in a plane, then c is
 (A) G.M. of a and b
 (B) A.M. of a and b
 (C) Equal to zero
 (D) H.M. of a and b

11. The P.V.'s of the vertices of a triangle are $2\bar{i} + 3\bar{j} + 4\bar{k}$, $4\bar{i} + 6\bar{j} + 3\bar{k}$, $3\bar{i} + 2\bar{j} + 3\bar{k}$ P.V. of its orthocenter is

(A) $2\bar{i} - 3\bar{j} + 4\bar{k}$ (B) $2\bar{i} + 3\bar{j} - 4\bar{k}$

(C) $2\bar{i} + 3\bar{j} + 4\bar{k}$ (D) $-2\bar{i} + 3\bar{j} + 4\bar{k}$

12. The vectors $\overline{AB} = 3\bar{i} + 4\bar{k}$ and $\overline{AC} = 5\bar{i} - 2\bar{j} + 4\bar{k}$ are the sides of a triangle ABC. The length of the median through A is

(A) $\sqrt{72}$

(C) $\sqrt{288}$

(D) $\sqrt{18}$

13. Unit vectors along the diagonals of the parallelogram whose adjacent sides are $\bar{i} + \bar{j} + \bar{k}$ and $\bar{i} - \bar{j} + \bar{k}$ are

(A) $\frac{\bar{i} + \bar{k}}{\sqrt{2}}, \frac{\bar{i} - \bar{j}}{\sqrt{2}}$

(B) $\frac{\bar{i} - \bar{k}}{\sqrt{2}}, \bar{j}$

(C) $\frac{\bar{i} - \bar{k}}{\sqrt{2}}, \bar{k}$

(D) $\frac{\bar{i} + \bar{k}}{\sqrt{2}}, \bar{j}$

14. If $A(3\bar{i} + 2\bar{j} - \bar{k})$, $B(2\bar{i} - 2\bar{j} + 5\bar{k})$,

$C(\bar{i} + 3\bar{j} - \bar{k})$ then vector equation of the

line passing through the centroid of ΔABC and parallel to \overline{BC} is

(A) $\bar{r} = 2\bar{i} + \bar{j} + \bar{k} + t(-\bar{i} + 5\bar{j} - 6\bar{k})$

(B) $\bar{r} = 2\bar{i} - \bar{j} + \bar{k} + t(\bar{i} + 5\bar{j} - 6\bar{k})$

(C) $\bar{r} = 2\bar{i} + \bar{j} - \bar{k} + t(-\bar{i} + 5\bar{j} + 6\bar{k})$

(D) $\bar{r} = 2\bar{i} + \bar{j} - \bar{k} + t(\bar{i} - 5\bar{j} + 6\bar{k})$

15. The point of intersection of the lines

$\bar{r} = \bar{a} + t(\bar{b} + \bar{c})$, $\bar{r} = \bar{b} + s(\bar{c} + \bar{a})$ is

(A) \bar{c} (B) \bar{a}

(C) \bar{b} (D) $\bar{a} + \bar{b} + \bar{c}$

16. If $A(1, -1, -3)$, $B(2, 1, -2)$, $C(-5, 2, -6)$

are the vertices of a ΔABC , then the length of internal bisector of angle A is

(A) $\frac{3}{4}\sqrt{10}$ (B) $\frac{1}{2}\sqrt{10}$

(C) $\frac{1}{4}\sqrt{10}$ (D) $\sqrt{10}$

17. If the vector $\bar{a} = 2\bar{i} + 3\bar{j} + 6\bar{k}$ and \bar{b} are collinear and $|\bar{b}| = 21$ then $\bar{b} =$

(A) $\pm(2\bar{i} + 3\bar{j} + 6\bar{k})$

(B) $\pm 3(2\bar{i} + 3\bar{j} + 6\bar{k})$

(C) $\bar{i} + \bar{j} + \bar{k}$

(D) $\pm 21(2\bar{i} + 3\bar{j} + 6\bar{k})$

18. Let $f(t) = [t]\bar{i} + \{t - [t]\}\bar{j} + [t + 1]\bar{k}$

where $[.]$ denotes the greatest integer function. If the vectors $f\left(\frac{5}{4}\right)$ and

$\bar{i} + \bar{j} + \mu\bar{k}$ are parallel then $(\lambda, \mu) =$

(A) $\left(\frac{1}{4}, 2\right)$ (B) $\left(2, \frac{1}{4}\right)$

(C) $(1, 2)$ (D) $(4, 1)$

19. The sum of the distinct real values of μ , for which the vectors $\hat{\mu}\bar{i} + \bar{j} + \bar{k}$, $\hat{\mu}\bar{i} \pm \bar{k}$, $\bar{i} + \mu\bar{k}$ are co-planar is

(A) -1 (B) 0

(C) 1 (D) 2

20. The vector of magnitude $3\sqrt{6}$ along the bisector of the angle between the vectors $4\bar{i} - 7\bar{j} + 4\bar{k}$ and $\bar{i} + 2\bar{j} - 2\bar{k}$ is

(A) $7\bar{i} - \bar{j} - 2\bar{k}$ (B) $\pm(7\bar{i} - \bar{j} - 2\bar{k})$

(C) $-7\bar{i} - \bar{j} - 2\bar{k}$ (D) $\pm(-7\bar{i} - \bar{j} - 2\bar{k})$

NUMERICAL VALUE TYPE

Section-II contains 5 Numerical Value Type questions.

Marking scheme: +4 for correct answer, 0 if not attempted and -1 in all other cases

21. If the points with position vectors

$60\bar{i} + 3\bar{j}, 40\bar{i} - 8\bar{j}, a\bar{i} - 52\bar{j}$ are collinear then $|a| = \sqrt{10}$

22. Let the vectors $\overline{AB} = 2\bar{i} + 2\bar{j} + \bar{k}$ and $\overline{AC} = 2\bar{i} + 4\bar{j} + 4\bar{k}$ be two sides of a triangle ABC. If G is the centroid of ΔABC , then $\frac{27}{7}|\overline{AG}|^2 + 5 = ?$

23. Let $\vec{a} = \vec{i} + \vec{j} + \vec{k}$ and $\vec{c} = a\vec{i} + b\vec{j} + c\vec{k}$

The vector $\vec{i} - 2\vec{j} + \vec{k}$, $3\vec{i} + 2\vec{j} - \vec{k}$ and \vec{c} are coplanar then $\frac{a}{3b}$ equals

If the vector $\vec{a} + \vec{i} + \vec{j} + \vec{k}$, $\vec{j} + \vec{b} + \vec{k}$,

$\vec{i} + \vec{j} + c\vec{k}$ ($a \neq b \neq c \neq 1$) are coplanar,

$$\text{then } \frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} =$$

If the position vectors of the points

A, B, C, D given by

$$\vec{i} + 2\vec{j} + 3\vec{k}, 2\vec{i} - \vec{j} + 2\vec{k}, \frac{1}{4}(\vec{i} + 15\vec{j} + 15\vec{k})$$

and $\frac{1}{3}(\vec{i} + 2\vec{j} + (5 + 3a)\vec{k})$ respectively

are such that $|\vec{AC}| = |\vec{BD}|$, then

$$16(3a - 1)^2 = 187$$

PHYSICS

(SINGLE CORRECT ANSWER TYPE)

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26. An air filled balloon is at a depth of 1 km below the water level in an ocean.

Determine the normal stress on the

balloon (atmospheric pressure = 10^5 Pa).

(A) $98 \times 10^5 \text{ N/m}^2$ (B) $99 \times 10^5 \text{ N/m}^2$

(C) $98 \times 10^3 \text{ N/m}^2$ (D) $99 \times 10^3 \text{ N/m}^2$

A steel wire of 2 mm in diameter is

stretched by applying a force of 72N.

Stress in the wire is

(A) $2.29 \times 10^5 \text{ N/m}^2$ (B) $1.7 \times 10^5 \text{ N/m}^2$

(C) $3.6 \times 10^5 \text{ N/m}^2$ (D) $0.8 \times 10^5 \text{ N/m}^2$

The length of two wires are in the ratio 3:

4. Ratio of the diameters is 1:2; young's modulus of the wires are in the ratio 3:2; If they are subjected to same tensile force, the ratio of the elongation produced is

(A) 1:1 (B) 1:2

(C) 2:3 (D) 2:1

29. An aluminium rod has a breaking strain 0.2%. The minimum cross-sectional area of the rod in m^2 in order to support a load of 10^4 N is if Young's modulus is

$$7 \times 10^9 \text{ Nm}^{-2}$$

31. (A) $LT \times 10^4$ (B) $LT \times 10^5$
 (C) 7.1×10^4 (D) $Lx \times 10^4$

32. The length of a metal wire is 10cm when the tension in it is 20N and 12cm when the tension is 40N. Then natural length of the wire is in cm

- (A) 5 (B) 4
 (C) 8 (D) 9

33. A steel wire of uniform cross section 1mm² is heated to 70°C and stretched by tying it two ends rigidly. Calculate the change in tension on the wire when temperature falls from 70°C to 35°C

$$a_s = 1.1 \times 10^{-5} / ^\circ\text{C} Y_s = 2 \times 10^{11} \text{ N/mm}^2$$

(A) 70N (B) 72N
 (C) 75N (D) 77N

34. A steel wire of length 5 m and cross sectional area $2 \times 10^{-4} \text{ m}^2$ stretches by the same amount as a copper wire of length 4 m and cross sectional area of $3 \times 10^{-4} \text{ m}^2$ under a given load. The ratio of young's modulus of steel to that of copper is

- (A) 8:15 (B) 15:8
 (C) 5:3 (D) 3:5

35. A brass wire of length 300 cm when subjected to a force F produces an elongation "a". Another wire of twice the diameter and of same length and material, when subjected to the force F produces an elongation b. Then the value of a/b is

- (A) 1:1 (B) 4:1
 (C) 2:1 (D) 1:2

34. A tungsten wire, 0.5 mm in diameter, is just stretched between two fixed points at a temperature of 40°C. Determine the tension in the wire when the temperature falls to 20°C. (coefficient of linear

$$\text{expansion of tungsten} = 4.5 \times 10^{-5}/^\circ\text{C};$$

$$\text{Young's modulus of tungsten} = 3.45 \times 10^{11} \text{ Nm}^{-2}$$

(A) 0.609TN (B) 3.09TN
 (C) 5.09TN (D) 7.09TN

35. Two rods of different materials are clamped at their ends rigidly. When they are heated for the same rise in temperature, same thermal stresses are produced in them. If their Young's moduli are in the ratio x:y then ratio of coefficients of their linear expansion is

- (A) x:y (B) y:x
 (C) $x^2 : y^2$ (D) $y^2 : x^2$

36.

A metal cube of side length 8.0 cm has its upper surface displaced with respect to the bottom by 0.10 mm when a tangential force of 4×10^4 N is applied at the top with bottom surface fixed. The rigidity modulus of the material of the cube is

- (A) 4×10^4 N/m² (B) 5×10^4 N/m²
 (C) 8×10^4 N/m² (D) 1×10^4 N/m²

37.

A spherical ball of volume 1000 cm³ is subjected to a pressure of 10 atmosphere.

The change in volume is 10^{-3} cm³. If the ball is made of iron find its bulk modulus.

(Atmospheric pressure = 1×10^5 Nm⁻²)

- (A) 1×10^4 N/m² (B) 2×10^4 N/m²
 (C) 3×10^4 N/m² (D) 4×10^4 N/m²

38.

A uniform bar of length L' and cross sectional area 'A' is subjected to a tensile load 'F'. 'Y' be the Young's modulus and

'σ' be the Poisson's ratio then volumetric strain is

- (A) $\frac{F}{AY}(1-\sigma)$ (B) $\frac{F}{AY}(2-\sigma)$
 (C) $\frac{F}{AY}(1-2\sigma)$ (D) $\frac{F}{AY}\cdot\sigma$

39. Two wires of same radius and length are subjected to the same load. One wire is of steel and the other is of copper. If the

Young's modulus of steel is twice that of copper, the ratio of elastic energy stored per unit volume in steel to that of copper wire is

- (A) 1:2 (B) 2:1
 (C) 1:4 (D) 4:1

40.

Two wires of equal cross section, but one made up of steel and the other copper are joined end to end. When the combination is kept under tension, the elongations in the two wires are found

to be equal. If $Y_{\text{steel}} = 2.0 \times 10^{11}$ N.m⁻² and $Y_{\text{copper}} = 1.1 \times 10^{11}$ N.m⁻², the ratio of the lengths of the two wires is

- (A) 20:11 (B) 11:20
 (C) 5:4 (D) 4:5

41.

A cubical ball is taken to a depth of 200m in a sea. The decrease in volume observed to be 0.1% the bulk modulus of the ball is

- (g = 10m/s^2)
 (A) 2×10^9 pa (B) 2×10^6 pa
 (C) 2×10^9 pa (D) 1.2×10^9 pa

42. A fractional change in volume of oil is 1 percent. When a pressure of 2×10^5 N/m² is applied. Calculate the bulk modulus and its compressibility.

- (A) 3×10^4 N/m²; 0.33×10^{-9} m²/N
 (B) 5×10^5 N/m²; 2×10^{-10} m²/N
 (C) 2×10^8 N/m²; 5×10^{-10} m²/N
 (D) 2×10^9 N/m²; 5×10^{-9} m²/N

43.

A 8m long string of rubber, having density 5×10^3 kg/m³ and young's modulus

of a room. The increase in its length due to its own weight will be ($g = 10\text{m/s}^2$)

- (A) 96×10^{-5} m (B) 960×10^{-4} m
 (C) 9.6×10^{-2} m (D) 96×10^{-1} m

44.

When a wire of length 10 m is subjected to a force of 100N along its length, the lateral strain produced is 0.01×10^{-3} . Poisson's ratio was found to be 0.4. If area of cross section of wire is 0.025m^2 its Young's modulus is

- (A) 1.6×10^8 N/m² (B) 19×10^6 N/m²
 (C) 2×10^8 N/m² (D) 5×10^6 N/m²

A copper wire and an aluminium wire has lengths in the ratio 3:2 diameter in the ratio 2:3 and force applied in the ratio 4:5 find the ratio of the increase in length of the two wires $Y_{\text{Cu}} = 7 \times 10^{10}$ N/m²,

$$Y_{\text{Al}} = 11 \times 10^{10}$$
 N/m²

(A) 110:89 (B) 180:110
 (C) 189:110 (D) 80:11

NUMERICAL VALUE TYPE

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46. A wire of length 1m fixed at one end has a sphere attached to it at the other end. The sphere is projected horizontally with a velocity of $\sqrt{9g}$. When it describes a vertical circle, the ratio of elongations of the wire when the sphere is at the top and

- bottom of the circle is $5^{\frac{x}{x}}$ where x =
 Two separate wires A and B are stretched by 2mm and 4mm respectively, when they are subjected to a force of 2N. Assume

57

The label of a bromobutanoic acid bottle has been washed away. Someone is trying to relabel it with correct IUPAC name.

Which of the following cannot be a name?

- (1) 2-bromobutanoic acid
- (2) 3-bromobutanoic acid
- ~~(3) 4-bromobutanoic acid~~
- ~~(4) 1-bromo-3-butanoic acid~~

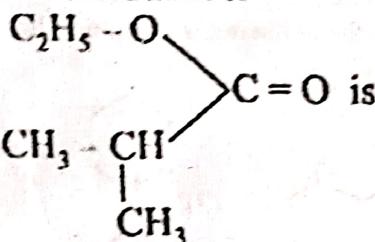
58

Which is the wrong IUPAC name of chlorocyclohexane-dione?

- ~~(1) 3-chloro-1,4-cyclohexanedione~~
- (2) 2-chloro-1,3-cyclohexanedione
- ~~(3) 4-chloro-1,3-cyclohexanedione~~
- (4) 5-chloro-1,3-cyclohexanedione

59

The IUPAC name of

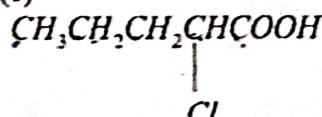


- (1) ethoxy methanone
- ~~(2) ethyl-2-methyl propanoate~~
- (3) ethoxypopropane
- (4) 2-methyl ethoxy propanone

60

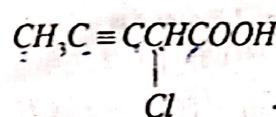
Which of the following compound is wrongly named?

(1)



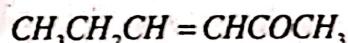
~~2-Chloro pentan oic acid~~

(2)



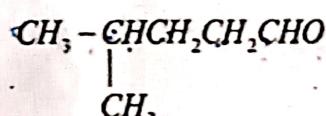
~~2-Methyl hex-3-enoic acid~~

(3)



~~Hex-3-en-2-one~~

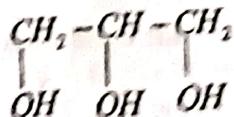
(4)



~~4-Methyl pentanal~~

61

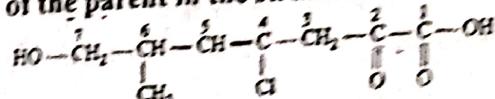
The IUPAC name of the compound



- (1) 1,2,3-dihydroxy propane
- (2) 3-hydroxy pentane-1,5-diol
- (3) 1,2,3-hydroxy propane
- ~~(4) Propane-1,2,3-triol~~

62

The suffix of the principal group, the prefixes for the other groups and the name of the parent in the structure

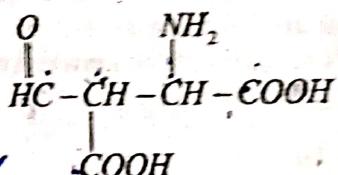


Are given by the set

- (1) -oic acid, ~~chloro~~, hydroxy, oxo, methyl, 4-heptene
- ~~(2) -oic acid, chloro, hydroxy, methyl, oxo, 4-heptene~~
- ~~(3) -one, carboxy, chloro, methyl, hydroxy, 4-heptene~~
- ~~(4) -one, carboxy, chloro, methyl, hydroxy, 4-heptene~~

63

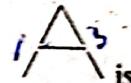
Correct IUPAC name of the following compound is



- ~~- (1) 2-Amino-3-Formyl butane-1,4-dioic acid
 - (2) 2-formyl-3-amino butane-1,4-dioic acid
 - (3) 3-Amino-2-formyl butane-1,4-dioic acid
 - (4) 2-Amino-3-carboxy oxo butanoic acid~~

64

The IUPAC name of



is

- (1) Dimethyl cyclopropane
- (2) 1,3-Dimethylcyclopropane
- ~~(3) 1,2-Dimethylcyclopropane~~
- (4) None of these

65

According to Huckel's rule compound is said to be aromatic contains

- (1) $4n$ bonds
- (2) $4n$ atoms
- (3) $(4n+2)$ atoms
- ~~(4) $(4n+2)\pi$ electrons~~

66

Which of the following is not a cyclic compound?

- (1) Anthracene
- ~~(2) Pyrrole~~
- (3) Phenol
- ~~(4) Isobutylene~~

67

Which of the following contains acetic acid?

- ~~- (1) Vinegar
 - (2) Molasses
 - (3) Coal tar
 - (4) Butter~~

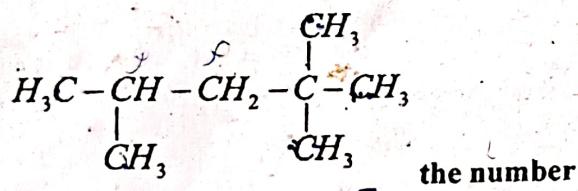
68. I.U.P.A.C name of ester is
 (1) Alkoxy alkane (2) Alkyl alkanoate
 (3) Alkanoyl halide
 (4) Alcanoic anhydride
69. Which is an alicyclic compound
 (1) Benzene (2) cyclohexane
 (3) pyridine (4) pyrrole
70. Organic compounds can be formed by
 (1) Plants only (2) Animals only
 (3) Plants and Animals
 (4) Plants, animals and can be synthesized in laboratory

(NUMERICAL VALUE TYPE)

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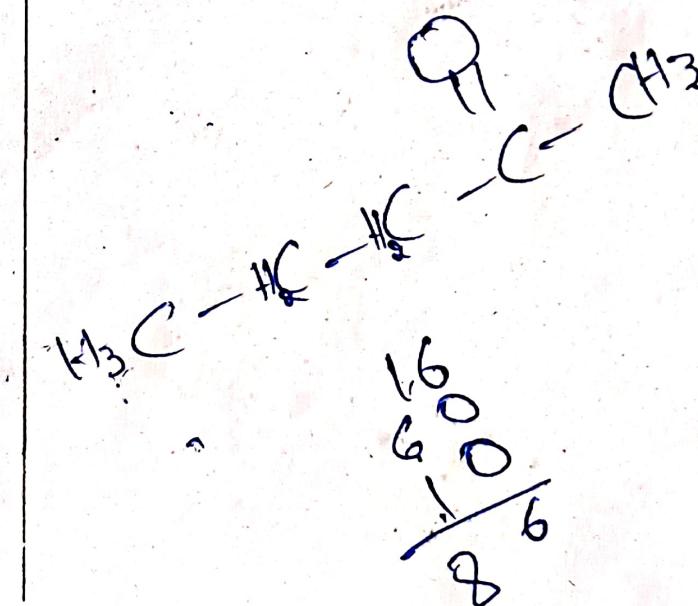
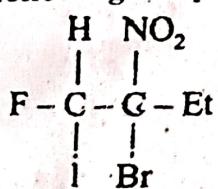
71. The number of π electrons present in phenanthrcene 14
72. The number quarternary of carbon atom present in neopentane are 1.
73. In the structure,



of primary carbons are: 5

74. Molecular weight of 2-pentanone is 86.

75. The position of the NO_2 group in the following compound is:



BEST OF LUCK