

FINAL JEE–MAIN EXAMINATION – APRIL, 2023

(Held On Thursday 13th April, 2023)

TIME : 3 : 00 PM to 6 : 00 PM

PHYSICS

SECTION-A

31. Given below are two statements : one is labelled as **Assertion A** and the other is labelled as **Reason R**
Assertion A : The binding energy per nucleon is practically independent of the atomic number for nuclei of mass number in the range 30 to 170.

Reason R : Nuclear force is short ranged.

In the light of the above statements, choose the **correct** answer from the options given below

Option :

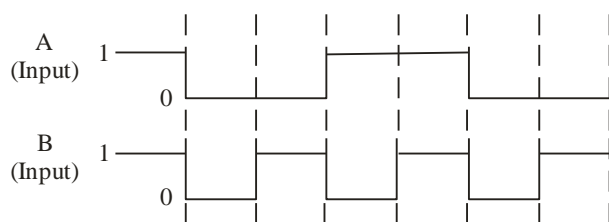
- (1) Both **A** and **R** are true but **R** is **NOT** the correct explanation of **A**
- (2) **A** is true but **R** is false
- (3) **A** is false but **R** is true
- (4) Both **A** and **R** are true and **R** is the correct explanation of **A**

Official Ans. by NTA (4)

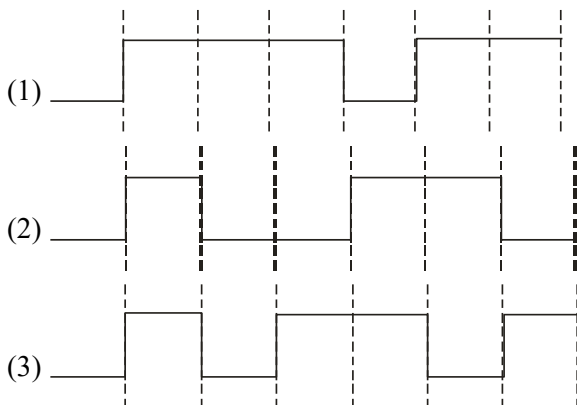
Allen Ans. (4)

- Sol.** Binding energy per nucleon is almost same for nuclei of mass number ranging 30 to 170.

32. The output from a NAND gate having inputs A and B given below will be.



Option :



Official Ans. by NTA (1)

Allen Ans. (1)

Sol. Truth table for NAND gate is

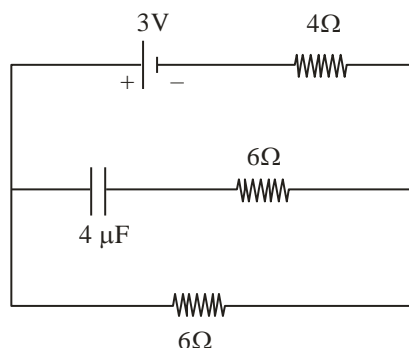
| A | B | $Y = \overline{A \cdot B}$ |
|---|---|----------------------------|
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

On the basis of given input A and B the truth table is

| A | B | Y |
|---|---|---|
| 1 | 1 | 0 |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |
| 0 | 0 | 1 |
| 0 | 1 | 1 |

So the correct answer is Option 1.

33. In the network shown below, the charge accumulated in the capacitor in steady state will be :



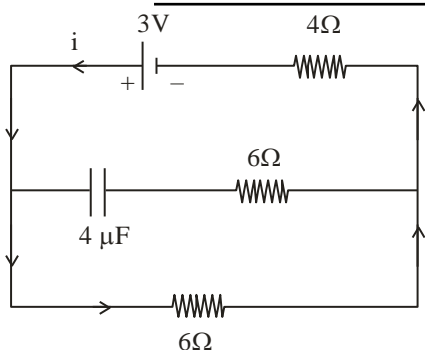
Option :

- (1) 7.2 μC
- (2) 4.8 μC
- (3) 10.3 μC
- (4) 12 μC

Official Ans. by NTA (1)

Allen Ans. (1)

Sol.



No current will flow in capacitor in steady state,
current flowing in the circuit in steady state

$$I = \frac{3}{6+4} = \frac{3}{10}$$

Potential difference on 6Ω resistance

$$V = 6 \times \frac{3}{10} = 1.8 \text{ volt}$$

Capacitor will have same potential so charge,

$$q = CV = (4 \mu\text{F}) \cdot (1.8 \text{ volt}) = 7.2 \mu\text{C}.$$

34. Given below are two statements :

Statement I: For a planet, if the ratio of mass of the planet to its radius increases, the escape velocity from the planet also increases.

Statement II: Escape velocity is independent of the radius of the planet.

In the light of above statements, choose the **most appropriate** answer from the options given below

Option :

- (1) Both Statement I and Statement II are incorrect
- (2) Statement I is correct but statement II is incorrect
- (3) Statement I is incorrect but statement II is correct
- (4) Both Statement I and Statement II are correct

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. $V_e = \sqrt{\frac{2GM}{R}} \Rightarrow V_e \propto \sqrt{\frac{M}{R}}$

As $\frac{M}{R}$ increases $\Rightarrow V_e$ increases

Statement (1) is correct

Also $V_e \propto \frac{1}{\sqrt{R}}$

As V_e depends upon R

\Rightarrow Statement (2) is incorrect

Option (2) is correct

35. A particle executes SHM of amplitude A . The distance from the mean position when its kinetic energy becomes equal to its potential energy is :

Option :

- (1) $\sqrt{2}A$
- (2) $2A$
- (3) $\frac{1}{\sqrt{2}}A$
- (4) $\frac{1}{2}A$

Official Ans. by NTA (3)

Allen Ans. (3)

Sol. $KE = PE$

$$\frac{1}{2} M \omega^2 (A^2 - x^2) = \frac{1}{2} M \omega^2 x^2$$

$$A^2 - x^2 = x^2 \Rightarrow A^2 = 2x^2$$

$$\Rightarrow x = \pm \frac{A}{\sqrt{2}}$$

36. A passenger sitting in a train A moving at 90 km/h observes another train B moving in the opposite direction for 8 s. If the velocity of the train B is 54 km/h, then length of train B is :

Option :

- (1) 80 m
- (2) 200 m
- (3) 120 m
- (4) 320 m

Official Ans. by NTA (4)

Allen Ans. (4)

Sol. Velocity of train A

$$V_A = 90 \frac{\text{km}}{\text{hr}} = 90 \times \frac{5}{18} = 25 \text{ m/s}$$

Velocity of train B

$$V_B = 54 \frac{\text{km}}{\text{hr}} = 54 \times \frac{5}{18} = 15 \text{ m/s}$$

$$\text{Velocity of train B w.r.t. train A} = \vec{V}_B - \vec{V}_A$$

$$= 15 - (-25) \text{ m/s}$$

$$= 40 \text{ m/s}$$

$$\text{Time of crossing} = \frac{\text{length of train}}{\text{relative velocity}}$$

$$(8) = \frac{\ell}{40}$$

$$\ell = 8 \times 40 = 320 \text{ meter.}$$

37. The initial pressure and volume of an ideal gas are P_0 and V_0 . The final pressure of the gas when the gas is suddenly compressed to volume $\frac{V_0}{4}$ will be :
(Given γ = ratio of specific heats at constant pressure and at constant volume)

Option :

- (1) $P_0(4)^{\frac{1}{\gamma}}$ (2) $P_0(4)^{\gamma}$
(3) P_0 (4) $4P_0$

Official Ans. by NTA (2)

Allen Ans. (2)

- Sol. As gas is suddenly compressed, the process is adiabatic.

Equation of gas for adiabatic process is $PV^{\gamma} = \text{constant}$.

$$\Rightarrow P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

$$\Rightarrow P_0 V_0^{\gamma} = P_2 \left(\frac{V_0}{4} \right)^{\gamma}$$

$$\Rightarrow P_2 = P_0(4)^{\gamma}$$

Option (2) is correct

38. Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**
Assertion A : A spherical body of radius (5 ± 0.1) mm having a particular density is falling through a liquid of constant density. The percentage error in the calculation of its terminal velocity is 4%.

Reason R : The terminal velocity of the spherical body falling through the liquid is inversely proportional to its radius.

In the light of the above statements, choose the **correct** answer from the options given below

Option :

- (1) Both **A** and **R** are true but **R** is **NOT** the correct explanation of **A**
(2) Both **A** and **R** are true and **R** is the correct explanation of **A**
(3) **A** is false but **R** is true
(4) **A** is true but **R** is false

Official Ans. by NTA (4)

Allen Ans. (4)

- Sol. Terminal velocity of a spherical body in liquid

$$\Rightarrow V_t \propto r^2$$

$$\Rightarrow \frac{\Delta V_t}{V_t} = 2 \cdot \frac{\Delta r}{r}$$

$$\Rightarrow \frac{\Delta V_t}{V_t} \times 100\% = 2 \frac{(0.1)}{5} \times 100 = 4\%$$

$$\text{Also } V_t \propto r^2$$

Reason R is false

Option (4) is correct

39. In an electromagnetic wave, at an instant and at a particular position, the electric field is along the negative z-axis and magnetic field is along the positive x-axis. Then the direction of propagation of electromagnetic wave is :

Option :

- (1) at 45° angle from positive y-axis
(2) negative y-axis
(3) positive z-axis
(4) positive y-axis

Official Ans. by NTA (2)

Allen Ans. (2)

- Sol. Direction of propagation of EM wave will be in the direction of $\vec{E} \times \vec{B}$.

40. The distance travelled by an object in time t is given by $s = (2.5)t^2$. The instantaneous speed of the object at $t = 5$ s will be :

Option :

- (1) 12.5 ms^{-1} (2) 62.5 ms^{-1}
(3) 5 ms^{-1} (4) 25 ms^{-1}

Official Ans. by NTA (4)

Allen Ans. (4)

- Sol. Distance $(s) = (2.5)t^2$

$$\text{Speed } (v) = \frac{ds}{dt} = \frac{d}{dt} \{(2.5)t^2\}$$

$$v = 5t$$

$$\text{At } t = 5, v = 5 \times 5 = 25 \text{ m/s.}$$

Option (4) is correct

41. An electron is moving along the positive x-axis. If the uniform magnetic field is applied parallel to the negative z-axis. then

- A. The electron will experience magnetic force along positive y-axis
B. The electron will experience magnetic force along negative y-axis
C. The electron will not experience any force in magnetic field
D. The electron will continue to move along the positive x-axis
E. The electron will move along circular path in magnetic field

Choose the correct answer from the options given below :

Option :

- (1) B and E only (2) A and E only
(3) C and D only (4) B and D only

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. $\vec{F} = -e(\vec{v} \times \vec{B})$

Force will be along -ve y-axis.

As magnetic force is \perp to velocity, path of electron must be a circle.

42. Two planets A and B of radii R and 1.5 R have densities ρ and $\rho/2$ respectively. The ratio of acceleration due to gravity at the surface of B to A is :

Option :

- (1) 2 : 3 (2) 2 : 1
(3) 3 : 4 (4) 4 : 3

Official Ans. by NTA (3)

Allen Ans. (3)

Sol. $g = \frac{GM}{R^2} = \frac{4}{3} \pi G \rho R$

$$\therefore \frac{g_2}{g_1} = \frac{\rho_2}{\rho_1} \times \frac{R_2}{R_1} = \frac{1}{2} \times 1.5 = \frac{3}{4}$$

43. Given below are two statements:

Statement I : An AC circuit undergoes electrical resonance if it contains either a capacitor or an inductor.

Statement II : An AC circuit containing a pure capacitor or a pure inductor consumes high power due to its non-zero power factor.

In the light of above statements, choose the **correct** answer from the options given below :

Option :

- (1) Both Statement I and Statement II are false
(2) Statement I is true but Statement II is false
(3) Both Statement I and Statement II are true
(4) Statement I is false but Statement II is true

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. For resonance, $\phi = 0$, hence both inductor & capacitor must be present. Also power factor is zero for pure inductor or pure capacitor hence both the component consume zero average power.

44. A vehicle of mass 200 kg is moving along a levelled curved road of radius 70 m with angular velocity of 0.2 rad/s. The centripetal force acting on the vehicle is :

Option :

- (1) 560 N (2) 2800 N
(3) 14 N (4) 2240 N

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. $F_c = m\omega^2 r = 200 \times (0.2)^2 \times 70 = 560 \text{ N}$

45. To radiate EM signal of wavelength λ with high efficiency, the antennas should have a minimum size equal to :

Option :

- (1) $\frac{\lambda}{2}$ (2) $\frac{\lambda}{4}$
(3) 2λ (4) λ

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. Minimum length of antenna should be $\frac{\lambda}{4}$.

46. Given below are two statements:

Statement I : Out of microwaves, infrared rays and ultraviolet rays, ultraviolet rays are the most effective for the emission of electrons from a metallic surface.

Statement II : Above the threshold frequency, the maximum kinetic energy of photoelectrons is inversely proportional to the frequency of the incident light.

In the light of above statements, choose the **correct** answer from the options given below

Option :

- (1) Statement I is true but Statement II is false
- (2) Both Statement I and Statement II are true
- (3) Statement I is false but Statement II is true
- (4) Both Statement I and Statement II are false

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. UV rays have maximum frequency hence are most effective for emission of electrons from a metallic surface.

$$KE_{\max.} = hf - hf_0$$

47. A 10 μC charge is divided into two parts and placed at 1 cm distance so that the repulsive force between them is maximum. The charges of the two parts are :

Option :

- (1) 9 μC , 1 μC (2) 5 μC , 5 μC
- (3) 7 μC , 3 μC (4) 8 μC , 2 μC

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. Divide $q = 10 \mu\text{C}$ into two parts x & $q - x$.

$$F = \frac{Kx(q-x)}{r^2}$$

For F to be maximum

$$\frac{dF}{dx} = \frac{K}{r^2} (q - 2x) = 0$$

$$x = \frac{q}{2}$$

48. In the equation $\left[X + \frac{a}{Y^2}\right] [Y - b] = RT$, X is pressure, Y is volume, R is universal gas constant and T is temperature. The physical quantity equivalent to the ratio $\frac{a}{b}$ is :

Option :

- (1) Energy
- (2) Impulse
- (3) Pressure gradient
- (4) Coefficient of viscosity

Official Ans. by NTA (1)

Allen Ans. (1)

Sol. X and $\frac{a}{Y^2}$ have same dimensions

Y and b have same dimensions

$$\therefore [a] = [\text{ML}^5\text{T}^{-2}]$$

$$[b] = [\text{L}^3]$$

$$\frac{[a]}{[b]} = [\text{ML}^2\text{T}^{-2}] \text{ has dimensions of energy}$$

49. In a Young's double slits experiment, the ratio of amplitude of light coming from slits is 2:1. The ratio of the maximum to minimum intensity in the interference pattern is :

Option :

- (1) 9 : 4 (2) 9 : 1
- (3) 2 : 1 (4) 25 : 9

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. Given that $\frac{A_1}{A_2} = \frac{2}{1}$

$$\frac{I_{\max}}{I_{\min}} = \left(\frac{A_1 + A_2}{A_1 - A_2}\right)^2 = \frac{9}{1} = 9 : 1$$

50. The mean free path of molecules of a certain gas at STP is 1500d, where d is the diameter of the gas molecules. While maintaining the standard pressure, the mean free path of the molecules at 373K is approximately :

Option :

- (1) 1098d (2) 2049d
- (3) 750d (4) 1500d

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. Mean free path

$$\lambda = \frac{RT}{\sqrt{2}\pi d^2 N_A P}$$

$$\lambda \propto T$$

$$\frac{1500d}{\lambda} = \frac{273}{373}$$

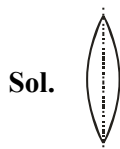
$$\lambda = 2049d$$

SECTION-B

51. A bi convex lens of focal length 10 cm is cut in two identical parts along a plane perpendicular to the principal axis. The power of each lens after cut is _____ D.

Official Ans. by NTA (5)

Allen Ans. (5)



Let power of each part is P_1 , then

$$P_1 + P_1 = P = \frac{1}{f}$$

$$2P_1 = \frac{1}{0.1} = 10$$

$$P_1 = 5D$$

52. An atom absorbs a photon of wavelength 500 nm and emits another photon of wavelength 600 nm. The net energy absorbed by the atom in this process is $n \times 10^{-4}$ eV. The value of n is _____.

[Assume the atom to be stationary during the absorption and emission process]

(Take $h = 6.6 \times 10^{-34}$ Js and $c = 3 \times 10^8$ m/s).

Official Ans. by NTA (4125)

Allen Ans. (4125)

Sol. $E = E_1 - E_2 = \frac{hc}{\lambda_1} - \frac{hc}{\lambda_2} = hc \left(\frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right)$

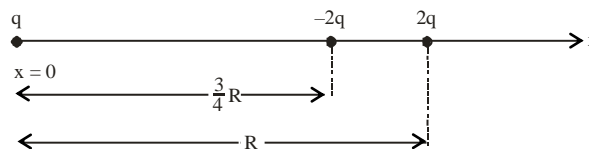
$$= 6.6 \times 10^{-34} \times 3 \times 10^8 \left(\frac{1}{500 \times 10^{-9}} - \frac{1}{600 \times 10^{-9}} \right)$$

$$= 6.6 \times 10^{-20} \text{ J}$$

$$= \frac{6.6 \times 10^{-20}}{1.6 \times 10^{-19}} \text{ eV} = 4.125 \times 10^{-1} \text{ eV}$$

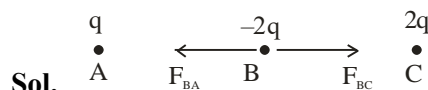
$$= 4125 \times 10^{-4} \text{ eV}$$

53. Three point charges q , $-2q$ and $2q$ are placed on x -axis at a distance $x = 0$, $x = \frac{3}{4}R$ and $x = R$ respectively from origin as shown. If $q = 2 \times 10^{-6}$ C and $R = 2$ cm, the magnitude of net force experienced by the charge $-2q$ is _____ N.



Official Ans. by NTA (5440)

Allen Ans. (5440)



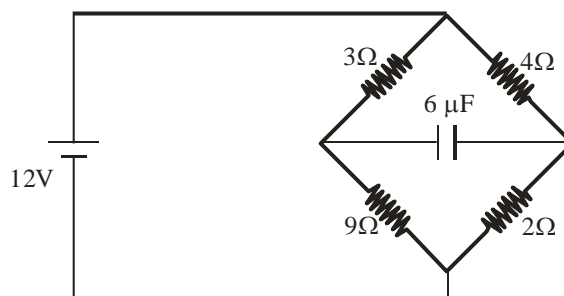
$$F_{BA} = \frac{Kq(2q)}{\left(\frac{3}{4}R\right)^2} = \frac{32Kq^2}{9R^2}$$

$$F_{BC} = \frac{K(2q)(2q)}{\left(\frac{R}{4}\right)^2} = \frac{64Kq^2}{R^2}$$

$$F_B = F_{BC} - F_{BA} = \frac{544Kq^2}{9R^2}$$

$$= \frac{544 \times 9 \times 10^9 \times (2 \times 10^{-6})^2}{9 \times (2 \times 10^{-2})^2} = 5440 \text{ N}$$

54. In the circuit shown, the energy stored in the capacitor is $n \mu\text{J}$. The value of n is _____.

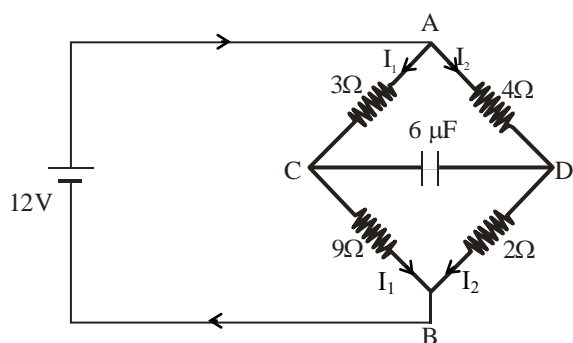


Official Ans. by NTA (75)

Allen Ans. (75)

Sol. $I_1 = \frac{12}{3+9} = 1\text{A}$

$I_2 = \frac{12}{4+2} = 2\text{A}$



$V_A - V_C = 3I_1 = 3\text{V} \quad \dots(1)$

$V_A - V_D = 2 \times 4 = 8\text{V} \quad \dots(2)$

Subtracting eq. (1) from eq. (2)

$V_C - V_D = 5\text{V} \Rightarrow V = 5\text{V}$

$U = \frac{1}{2} CV^2 = \frac{1}{2} \times 6 \times 5^2 = 75 \mu\text{J}$

- 55.** An insulated copper wire of 100 turns is wrapped around a wooden cylindrical core of the cross-sectional area 24 cm^2 . The two ends of the wire are connected to a resistor. The total resistance in the circuit is 12Ω . If an externally applied uniform magnetic field in the core along its axis changes from 1.5 T in one direction to 1.5 T in the opposite direction, the charge flowing through a point in the circuit during the change of magnetic field will be _____ mC .

Official Ans. by NTA (60)

Allen Ans. (60)

Sol. $\Delta Q = -\frac{\Delta\phi}{R} = -\left(\frac{\phi_2 - \phi_1}{R}\right)$

$\phi_1 = NBA$

$\phi_2 = -NBA$

$\therefore \Delta Q = \frac{2NBA}{R} = \frac{2 \times 100 \times 1.5 \times 24 \times 10^{-4}}{12}$

$= 6 \times 10^{-2} \text{ C} = 60 \text{ mC}$

- 56.** In an experiment with sonometer when a mass of 180 g is attached to the string, it vibrates with fundamental frequency of 30 Hz . When a mass m is attached, the string vibrates with fundamental frequency of 50 Hz . The value of m is _____ g .

Official Ans. by NTA (500)

Allen Ans. (500)

Sol. $f = \frac{1}{2\ell} \sqrt{\frac{T}{\mu}} \quad (T : \text{Tension})$

$\frac{f_2}{f_1} = \sqrt{\frac{T_2}{T_1}}$

$\left(\frac{50}{30}\right)^2 = \frac{mg}{180g} \Rightarrow m = \frac{25}{9} \times 180 = 500 \text{ gram}$

- 57.** A light rope is wound around a hollow cylinder of mass 5 kg and radius 70 cm . The rope is pulled with a force of 52.5 N . The angular acceleration of the cylinder will be _____ rad s^{-2} .

Official Ans. by NTA (15)

Allen Ans. (15)

Sol. $\tau = I\alpha$

$\Rightarrow FR = mR^2\alpha$

$\alpha = \frac{F}{mR} = \frac{52.5}{5 \times 0.7} = 15 \text{ rad s}^{-2}$

- 58.** A car accelerates from rest to $u \text{ m/s}$. The energy spent in this process is $E \text{ J}$. The energy required to accelerate the car from $u \text{ m/s}$ to $2u \text{ m/s}$ is $nE \text{ J}$. The value of n is _____.

Official Ans. by NTA (3)

Allen Ans. (3)

Sol. $E_1 = \frac{1}{2} mu^2 - 0 = \frac{1}{2} mu^2 = E$

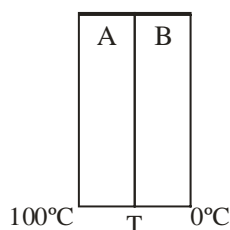
$E_2 = \frac{1}{2} m(2u)^2 - \frac{1}{2} mu^2 = \frac{3}{2} mu^2 = 3E$

59. Two plates A and B have thermal conductivities $84 \text{ Wm}^{-1}\text{K}^{-1}$ and $126 \text{ Wm}^{-1}\text{K}^{-1}$ respectively. They have same surface area and same thickness. They are placed in contact along their surfaces. If the temperatures of the outer surfaces of A and B are kept at 100°C and 0°C respectively, then the temperature of the surface of contact in steady state is _____ $^\circ\text{C}$.

Official Ans. by NTA (40)

Allen Ans. (40)

Sol.



Let the temperature of contact surface is T , then

$$H_A = H_B$$

$$\frac{K_A A (T_A - T)}{L} = \frac{K_B A (T - T_B)}{L}$$

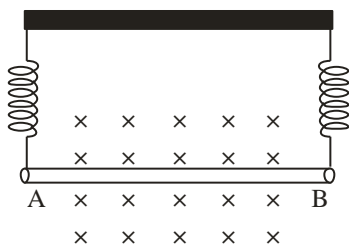
$$84(100 - T) = 126(T - 0)$$

$$2(100 - T) = 3T$$

$$200 - 2T = 3T$$

$$T = 40^\circ\text{C}$$

60. A straight wire AB of mass 40 g and length 50 cm is suspended by a pair of flexible leads in uniform magnetic field of magnitude 0.40 T as shown in the figure. The magnitude of the current required in the wire to remove the tension in the supporting leads is _____ A. (Take $g = 10 \text{ ms}^{-2}$).



Official Ans. by NTA (2)

Allen Ans. (2)

Sol. For equilibrium

$$Mg = I\ell B$$

$$I = \frac{mg}{\ell B} = \frac{40 \times 10^{-3} \times 10}{50 \times 10^{-2} \times 0.4} = 2 \text{ A}$$