

~~P[M=a]~~ $P[M=a] = 1/4$

$$P[M=b] = 3/4$$

$$P[k=k_1] = 1/2$$

$$P[k=k_2] = P[k=k_3] = 1/4$$

$$P[C=1] = P[M=a] * P[k=k_1] = \frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$$

$$\begin{aligned} P[C=2] &= P[M=a] * P[k=k_2] + P[M=b] * P[k=k_1] \\ &= \frac{1}{4} \times \frac{1}{4} + \frac{3}{4} \times \frac{1}{2} \end{aligned}$$

$$= \frac{1}{16} + \frac{3}{8} = \frac{7}{16}$$

$$\begin{aligned} P[C=3] &= P[M=a] * P[k=k_3] + P[M=b] * P[k=k_2] \\ &= \frac{1}{4} \times \frac{1}{4} + \frac{3}{4} \times \frac{1}{4} \end{aligned}$$

$$= \frac{4}{16} = \frac{1}{4}$$

$$\begin{aligned} P[C=4] &= P[M=b] * P[k=k_3] \\ &= \frac{3}{4} \times \frac{1}{4} = \frac{3}{16} \end{aligned}$$

$$P[M=a | C=1] = \frac{P[M=a] \times P[K=k_1]}{P[C=1]} = 1$$

$$P[M=a | C=4] = 0$$

$$P[M=a | C=2] = \frac{P[M=a] \times P[K=k_2]}{P[C=2]} = \frac{\frac{1}{16}}{\frac{7}{16}} = \frac{1}{7}$$

$$P[M=a | C=3] = \frac{P[M=a] \times P[K=k_3]}{P[C=3]} = \frac{\frac{1}{16}}{\frac{4}{16}} = \frac{1}{4}$$

$$P[M=b | C=1] = 0$$

$$P[M=b | C=4] = 1$$

$$P[M=b | C=2] = \frac{P[M=b] \times P[K=k_1]}{P[C=2]} = \frac{\frac{3}{8}}{\frac{7}{16}} = \frac{6}{7}$$

$$P[M=b | C=3] = \frac{P[M=b] \times P[K=k_2]}{P[C=3]} = \frac{3}{4}$$