AI MIDSEM – 1 EXAMINATION

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SECTION – C

INTRODUCTION

Prime numbers are a fundamental concept in number theory, defined as natural numbers greater than 1 that have no positive divisors other than 1 and themselves. Prime numbers are essential in various areas, including cryptography, algorithms, and computational mathematics.

In this project, we aim to create two functionalities using Python:

1. **Prime Number Generator**: A tool that generates all prime numbers within a specified range.
2. **Prime Number Checker**: A function that checks if a given number is prime or not.

These functionalities will be implemented using efficient algorithms to ensure optimal performance and accuracy.

METHODOLOGY

The methodology for creating the **Prime Number Generator** and **Prime Number Checker** involves using well-established algorithms and Python functions to ensure the correctness and efficiency of the solution.

**1. Prime Number Checker (iS\_prime function)**

To determine if a number n is prime:

* A prime number is only divisible by 1 and itself. So, if any number from 2 to n\sqrt{n}n​ divides n evenly, it’s not prime.
* We can optimize the checking by limiting the range to n\sqrt{n}n​ and skipping even numbers (after checking 2).

Steps:

1. If n is less than 2, it's not prime.
2. If n=2n = 2n=2, it’s prime (2 is the only even prime).
3. For numbers greater than 2, check divisibility from 3 up to n\sqrt{n}n​, skipping even numbers.
4. If no divisor is found, n is prime.

**2. Prime Number Generator (generate\_primes function)**

To generate prime numbers in a given range:

* We use the **Sieve of Eratosthenes** algorithm, which efficiently marks non-prime numbers and returns the primes up to a given number n.
* Alternatively, a simpler method can use the **is\_prime function** to check all numbers in the range.

Steps:

1. Start from 2 and check each number up to n using the **is\_prime function**.
2. For each prime number found, add it to a list of primes, then return the list of primes.

CODE

import math

# Method 1: Prime Checker

def is\_prime(n):

"""

Function to check if a number 'n' is prime.

A prime number is greater than 1 and divisible only by 1 and itself.

"""

# Step 1: If n is less than or equal to 1, it's not a prime number.

if n <= 1:

return False

# Step 2: 2 is the only even prime number, so return True if n is 2.

if n == 2:

return True

# Step 3: Eliminate even numbers greater than 2 (they are not prime).

if n % 2 == 0:

return False

# Step 4: Check divisibility from 3 to the square root of n.

# Only check odd numbers (skip even numbers).

for i in range(3, int(math.sqrt(n)) + 1, 2):

if n % i == 0:

return False # If n is divisible by any of these, it's not prime.

# Step 5: If no divisors were found, n is a prime number.

return True

# Method 2: Prime Number Generator

def generate\_primes(limit):

"""

Function to generate all prime numbers up to a given limit.

This function iterates through each number up to 'limit' and checks if it's prime.

"""

primes = [] # List to store prime numbers

# Step 1: Loop through all numbers from 2 to the specified 'limit'

for num in range(2, limit + 1):

# Step 2: Check if the number is prime using the is\_prime function

if is\_prime(num):

primes.append(num) # Add the prime number to the primes list

# Step 3: Return the list of prime numbers

return primes

# Example usage

if \_\_name\_\_ == "\_\_main\_\_":

# Example 1: Checking if a specific number is prime

number = 29

print(f"Is {number} prime? {is\_prime(number)}") # Expected output: True

# Example 2: Generating prime numbers up to a specified limit

limit = 50

print(f"Prime numbers up to {limit}: {generate\_primes(limit)}")

# Expected output: [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47]

OUTPUT

**References and Credits:**

1. **Prime Number Theory**:
   * A foundational concept in number theory that has been studied for centuries. More information can be found in standard mathematics textbooks such as:
     + *"Elementary Number Theory"* by David M. Burton.
     + *"An Introduction to the Theory of Numbers"* by G.H. Hardy and E.M. Wright.
2. **Sieve of Eratosthenes**:
   * The Sieve of Eratosthenes is an ancient algorithm used to find all primes up to any given limit. For an introduction, refer to:
     + *"The Art of Computer Programming, Volume 1: Fundamental Algorithms"* by Donald E. Knuth.
     + *"Introduction to Algorithms"* by Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest, and Clifford Stein (often referred to as CLRS).
3. **Python Math Library**:
   * The Python math library was used to compute the square root and optimize prime checking. Official documentation can be found here:
     + Python Math Library Documentation: <https://docs.python.org/3/library/math.html>
4. **Python Documentation**:
   * Python’s official documentation provides a thorough guide on language features and standard libraries used for implementing algorithms.
     + Python 3 Documentation: <https://docs.python.org/3/>
5. **Online Resources and Tutorials**:
   * Many online resources, including Stack Overflow and Python documentation, were useful in shaping the logic and structure of the functions:
     + Stack Overflow: <https://stackoverflow.com/>
     + Real Python: <https://realpython.com/>
6. **Mathematical Algorithms**:
   * The algorithm for checking if a number is prime and for generating primes has been inspired by common algorithms used in computational mathematics and number theory.
     + *The Prime Number Theorem* and optimizations in prime checking can be further studied in online platforms like:
       - Khan Academy: <https://www.khanacademy.org/math>
       - GeeksforGeeks: <https://www.geeksforgeeks.org/>