# **Assignment 1**

#### 1. Problem

#### I. Jacobi iterative method

i. Code

```
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
# define m 31
# define n 21
int main()
{
  double dx = 6.0/(m-1), dy = 4.0/(n-1), psi_old[n][m], psi_new[n][m], as, aw, ap, ae, an, Error;
  int iteration = 0,i,j;
  Error=1;
  ap=2.0*((1.0/pow(dx,2.0))+(1.0/pow(dy,2.0)));
  as=(1.0/pow(dy,2.0));
  aw = (1.0/pow(dx,2.0));
  ae=(1.0/pow(dx,2.0));
  an=(1.0/pow(dy,2.0));
  //boudary conditions
  for(i=0; i<n; i++)
  {
     for(j=0; j< m; j++)
       if(i==0)
       {
          //bottom boundary
          if(j < =5){
            psi_new[i][j]=0;
```

```
if(j >= 6){
       psi_new[i][j]=100.0;
     //top boundary
     else if(i == n-1)
       psi_new[i][j]=0.0;
     //left boundary
     else if(j == 0){
       psi_new[i][j]=0.0;
     else{
       psi_new[i][j]=0.0;
//jacobi iterative method
FILE *file1;
file1= fopen("error.txt","w");
fprintf(file1,"Iter\t Error\n");
while(Error>1e-6)
{
  for( i=0; i<n; i++)
```

```
for(j=0; j< m; j++)
        psi_old[i][j]=psi_new[i][j];
    for( i=1; i<n-1; i++)
      for(j=1; j< m-1; j++)
        1]) + (an*psi\_old[i+1][j]) + (as*psi\_old[i-1][j]));
    for(i=0; i< n; i++)
      psi_new[i][m-1]=psi_new[i][m-2];
    Error=0;
    for(int i=1; i< n-1; i++)
        for(j=1; j< m-1; j++)
          Error = Error + pow((psi\_new[i][j]-psi\_old[i][j]),2);
    Error = sqrt(Error/((m-2)*(n-2)));
    iteration=iteration+1;
```

```
printf("Iteration= %d\t", iteration);
     printf("Error= %.9f\n", Error);
     fprintf(file1, "%d \t %.9f \n", iteration, Error);
  }
  FILE *file2;
  file2=fopen("Stream1a.plt","w");
  fprintf(file2, "VARIABLES = \"X\", \"Y\", \"PHI\"\n");
  fprintf(file2, "ZONE t=\"BLOCK1\", J=31,I=21,F= POINT \n\n");
  for( i=0; i<n; i++)
  {
       for(j=0; j< m; j++)
          fprintf(file2, "%lf \t %lf \n",j*dy,i*dx,psi_new[i][j]);
         printf("%f\t",psi_new[i][j]);
       }
  }
  return 0;
     II.
          Point Gauss-Seidel iterative method
                 Code
            ii.
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
```

# define m 31

```
# define n 21
```

```
int main()
  Error,tem[n][m];
  int iteration = 0,i,j;
  Error=1;
  ap=2.0*((1.0/pow(dx,2.0))+(1.0/pow(dy,2.0)));
  as=(1.0/pow(dy,2.0));
  aw = (1.0/pow(dx,2.0));
  ae=(1.0/pow(dx,2.0));
  an=(1.0/pow(dy,2.0));
  for(int i=0; i<n; i++)
    for(int j=0; j< m; j++)
    {
      if(i==0)
      {
        if(j < =4){
          psi_new[i][j]=0;
      else if(j \ge 5)
        psi_new[i][j]=100.0;
      else if(i == n-1){
        psi_new[i][j]=0.0;
```

```
else if(j == 0){
        psi_new[i][j]=0.0;
      else{
        psi_new[i][j]=0.0;
  }
 //point gauss-seidal method
 FILE *file1;
 file1= fopen("error.txt","w");
 fprintf(file1,"Iter\t Error\n");
  while(Error>1e-6)
    Error=0;
    for( i=0; i<n; i++)
    {
      for(j=0; j< m; j++)
        tem[i][j]=psi_new[i][j];
    for( i=1; i<n-1; i++)
    {
      for(j=1; j< m-1; j++)
        1])+(an*psi_new[i+1][j])+(as*psi_new[i-1][j]));
```

```
}
   for(i=0; i<n; i++)
   {
     psi_new[i][m-1]=psi_new[i][m-2];
   }
        Error = sqrt(Error/(m*n));
        printf("iteration %d\t",iteration);
        printf("error %.10lf\n",Error);
        fprintf(file1, "%d\t%.10f\n",iteration,Error);
        iteration++;
FILE *file2;
file2=fopen("Stream1b.plt","w");
fprintf(file2,"VARIABLES= \"x\",\"y\",\"PHI\"\n");
fprintf(file2, "ZONE t=\"BLOCK1\", J=31,I=21,F= POINT \n\n");
for(int i=0; i<n; i++)
     for(int j=0; j< m; j++)
       fprintf(file2, "%lf\t%lf\n",j*dy,i*dx,psi_new[i][j]);
       printf("%f\t",psi_new[i][j]);
```

{

}

 $Error = Error + pow((psi\_new[i][j]-tem[i][j]),2);$ 

```
return 0;
```

# iii. Line Gauss-Seidel iterative method (TriDiagonal Matrix Algorithm) A. Code

```
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
# define m 31
# define n 21
int main(){
           double\ psi\_new[n][m], B, tem[n][m], ai, bi, ci, d[m-2], P[m-2], Q[m-2], dy = 4.0/(n-1),\ dx = 6.0/(m-1),\ dx = 6.0/(m-1),\
 1), error;
           int i,j,iteration=0;
               B = (dx/dy);
               ai=-2*(1+pow(B,2));
               bi=1;
               ci=1;
                   for(i=0; i<n; i++)
                 {
                               for(j=0; j< m; j++)
                                              if(i==0)
                                                              //bottom boundary
                                                              if(j < =5){
                                                                             psi_new[i][j]=0;
                                                              if(j >= 6){
```

```
psi_new[i][j]=100.0;
     }
     //top boundary
     else if(i == n-1)
       psi_new[i][j]=0.0;
     //left boundary
     else if(j == 0){
        psi_new[i][j]=0.0;
     else{
        psi_new[i][j]=0.0;
FILE *file1;
file1=fopen("error.txt","w");
error=1;
while(error > 1e-6)
 error = 0.0;
  for(j=1; j< m-1; j++)
   d[0]=-(pow(B,2))*(psi_new[0][j+1]+psi_new[0][j-1]);
   P[0]=-bi/ai;
```

```
Q[0]=d[0]/ai;
 for(i=1; i< n-1; i++){
    d[i]=-(pow(B,2))*(psi_new[i][j+1]+psi_new[i][j-1]);;
         P[i] = -(bi/(ai+ci*P[i-1]));
         Q[i]=(d[i]-ci*Q[i-1])/(ai+ci*P[i-1]);
  }
  for(i=n-2; i>0; i--){
    tem[i][j]=psi_new[i][j];
       psi_new[i][j]=P[i]*psi_new[i+1][j]+Q[i];
     error + = pow((psi_new[i][j] - tem[i][j]), 2.0);
  }
for (i=0; i< n; i++)
 psi_new[i][m-1]=psi_new[i][m-2];
error=sqrt(error/((m-2)*(n-2)));
iteration = iteration+1;
printf("iteration %d\t",iteration);
printf("error %.9f\n",error);
fprintf(file1,"%d\t%.9lf\n",iteration,error);
FILE *file2;
```

```
fprintf(file2,"VARIABLES= \"x\",\"y\",\"PHI\"\n");
fprintf(file2, "ZONE t=\"BLOCK1\", J=31,I=21,F= POINT \n\n");
for(int i=0; i<n; i++)
{
    for(int j=0; j < m; j++)
      fprintf(file2, "%lf\t%lf\n",j*dy,i*dx,psi_new[i][j]);
       printf("%f\t",psi_new[i][j]);
     }
}
return 0;
              Alternating Direction Implicit method (ADI)
A. Code
    #include<stdio.h>
    #include<stdlib.h>
    #include<math.h>
    # define m 31
    # define n 21
```

double tem[m][n], psi\_new[m][n],P[m-2],Q[m-2],d[m-2],d1[n-2],P1[n-2],Q1[n-2]

2],dx=6.0/(m-1),dy=4.0/(n-1),as,aw,ap,ae,an,aj,bj,cj,ai,bi,ci,error;

file2=fopen("tdmam1.plt","w");

}

int main()

int i,j, iteration = 0; as=(1.0/pow(dy,2.0)); aw=(1.0/pow(dx,2.0));

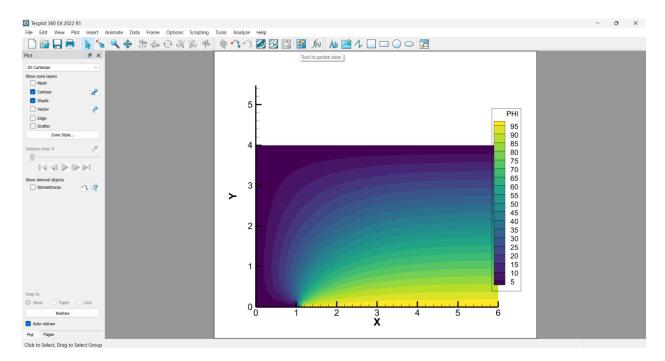
```
ap=2.0*((1.0/pow(dx,2.0))+(1.0/pow(dy,2.0)));
ae=(1.0/pow(dx,2.0));
an=(1.0/pow(dy,2.0));
ai=ap;
bi=-ae;
ci=-aw;
aj=ap;
bj=-an;
cj=-as;
for(i=0; i<m; i++)
  for(j=0; j< n; j++)
     if(j==0)
       //bottom boundary
       if(i < =5){
          psi_new[i][j]=0;
       if(i > = 6){
       psi_new[i][j]=100.0;
     //top boundary
     else if(j == n-1)
       psi_new[i][j]=0.0;
     //left boundary
     else if(i == 0){
       psi_new[i][j]=0.0;
     else{
       psi_new[i][j]=0.0;
  }
}
```

FILE \*file1;

```
file1=fopen("error.txt","w");
  error=1;
  while(error > 1e-6)
      for(i=0; i<m; i++)
     for(j\!\!=\!\!0;j\!\!<\!\!n;j\!\!+\!\!+\!\!)
      tem[i][j]= psi_new[i][j];
}
 for(j=1; j< n-1; j++)
  d[0]=an*(psi_new[0][j+1]+psi_new[0][j-1]);
  P[0]=-bi/ai;
  Q[0]=d[0]/ai;
  for(i=1; i<m-1; i++)
    d[i]=an*(psi\_new[i][j+1]+psi\_new[i][j-1]);
    P[i] = -(bi/(ai+ci*P[i-1]));
    Q[i]=(d[i]-ci*Q[i-1])/(ai+ci*P[i-1]);
  for(i=m-2; i>0; i--)
     psi_new[i][j]=P[i]*psi_new[i+1][j]+Q[i];
  for(i=1; i<m-1; i++)
    d1[0]=ae*(psi_new[i+1][0]+psi_new[i-1][0]);
    P1[0] = -(bj/aj);
    Q1[0]=(d1[0])/aj;
  for(j=1; j< n-1; j++)
```

```
d1[j]=ae*(psi\_new[i+1][j]+psi\_new[i-1][j]);
    P1[j] = -(bj/(aj+cj*P1[j-1]));
     Q1[j]=(d1[j]-cj*Q1[j-1])/(aj+cj*P1[j-1]);
  for(j=n-2; j>0; j--){
  psi_new[i][j]=P1[j]*psi_new[i][j+1]+Q1[j];
  for (j=0; j<n; j++)
  psi_new[m-1][j]=psi_new[m-2][j];
  error=0.0;
    for(i=0; i<m; i++)
       for(j=0; j< n; j++)
       error+=pow((psi_new[i][j]-tem[i][j]),2);
   iteration=iteration+1;
   error=sqrt(error/((m-2)*(n-2)));
   printf("iteration %d\t",iteration);
   printf("error %.9f\n",error);
   fprintf(file1,"%d\t%lf\n",iteration,error);
FILE *file2;
file2=fopen("adi_1.plt","w");
fprintf(file2,"VARIABLES= \"x\",\"y\",\"PHI\"\n");
fprintf(file2, "ZONE t= \"BLOCK1\", J=31, I=21, F=POINT \ \ \ \ \ \ \ \ );
for(i = 0; i < m; i++) {
    for(j = 0; j < n; j++)
  fprintf(file2, "%lf\t%lf\n", dx*i, dy*j, psi_new[i][j]);
   printf("%f\t",psi_new[i][j]);
return 0;
```

## v. The output



The conclusion

## Method in term speed

Adi method> Tdma>Point gauss seidel> jacobi

#### 2. Problem 2

## i. Jacobi iterative method

#### Code

```
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
# define m 41
int main()
  {
            double dx = 1.0/(m-1), dy = 1.0/(m-1), psi_old[m][m], degree between the simple sign of the si
               int iteration = 0,i,j;
            Error=1;
            ap=2.0*((1.0/pow(dx,2.0))+(1.0/pow(dy,2.0)));
            as=(1.0/pow(dy,2.0));
            aw = (1.0/pow(dx, 2.0));
            ae=(1.0/pow(dx,2.0));
            an=(1.0/pow(dy,2.0));
            //boudary conditions
            for (i = 0; i < m; i++)
              {
                        for (j = 0; j < m; j++)
                           {
                                  psi_new[0][j]=1.0;
                                  psi_new[m-1][j]=1.0;
                                  psi_new[i][0]=1.0;
                               if (j==m-1)
                                {
```

```
psi_new[i][j]=0.0;
     else
      psi_new[i][j]=0.0;
 FILE *file1;
 file1= fopen("error.txt","w");
 fprintf(file1,"Iter\t Error\n");
 while (Error>1e-6)
    for ( i = 0; i < m; i++)
      for (j = 0; j < m; j++)
        psi_old[i][j]=psi_new[i][j];
    for ( i = 1; i < m-1; i++)
      for (j = 0; j < m-1; j++)
        1])+(an*psi_old[i+1][j])+(as*psi_old[i-1][j]));
```

```
}
  Error=0.0;
  for (i = 0; i < m; i++)
  {
    for (j = 0; j < m; j++)
       Error = Error + pow((psi_new[i][j]-psi_old[i][j]),2);
     }
  Error = sqrt(Error/((m-2)*(m-2)));
  iteration=iteration+1;
  printf("Iteration= %d\t", iteration);
  printf("Error= %.9f\n", Error);
  fprintf(file1, "%d \t %.9f \n", iteration, Error);
FILE *file2;
file2=fopen("Stream1Ta.plt","w");
fprintf(file2,"VARIABLES=\"X\",\"Y\",\"T\"\n");
fprintf(file2, "ZONE t=\"BLOCK1\", J=41,I=41,F= POINT \n\n");
```

```
for( i=0; i<m; i++)
{
    for(j=0; j<m; j++)
    {
        fprintf(file2, "%lf \t %lf \t %lf \n",j*dy,i*dx,psi_new[i][j]);
        printf("%f\t",psi_new[i][j]);
    }
}
return 0;
}</pre>
```

#### ii. Point Gauss-Seidel iterative method

```
Code
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
# define m 41
int main()
  double dx = 1.0/(m-1), dy = 1.0/(m-1), tem[m][m], psi_new[m][m], as, aw, ap, ae, an, Error;
  int iteration = 0,i,j;
  Error=1;
  ap=2.0*((1.0/pow(dx,2.0))+(1.0/pow(dy,2.0)));
  as=(1.0/pow(dy,2.0));
  aw = (1.0/pow(dx,2.0));
  ae=(1.0/pow(dx,2.0));
  an=(1.0/pow(dy,2.0));
  //boudary conditions
  for (i = 0; i < m; i++)
```

```
for (j = 0; j < m; j++)
      psi_new[0][j]=1.0;
      psi_new[m-1][j]=1.0;
      psi_new[i][0]=1.0;
      if (j==m-1)
        psi_new[i][j]=0.0;
      else
       psi_new[i][j]=0.0;
     }
  FILE *file1;
  file1= fopen("error.txt","w");
  fprintf(file1,"Iter\t Error\n");
  while (Error>1e-6)
     Error=0.0;
    for (i = 0; i < m; i++)
       for (j = 0; j < m; j++)
          tem[i][j]=psi_new[i][j];
    for (i = 1; i < m-1; i++)
       for (j = 0; j < m-1; j++)
          psi_new[i][j]=(1/ap)*((ae*psi_new[i][j+1])+(aw*psi_new[i][j-1])
1])+(an*psi_new[i+1][j])+(as*psi_new[i-1][j]));
          Error = Error + pow((psi_new[i][j]-tem[i][j]),2);
```

```
}
          Error=sqrt(Error/((m-2)*(m-2)));
          iteration=iteration+1;
           printf("Iteration= %d\t", iteration);
          printf("Error= %.9f\n", Error);
          fprintf(file1, "%d \t %.9f \n", iteration, Error);
        }
        FILE *file2;
        file2=fopen("Stream1Tb.plt","w");
        fprintf(file2, "VARIABLES = \"X\", \"Y\", \"T\"\");
        fprintf(file2, "ZONE t=\"BLOCK1\", J=41,I=41,F= POINT \n\n");
        for( i=0; i<m; i++)
             for(j=0; j< m; j++)
                fprintf(file2, "\%lf \ \%lf \ \%lf \ \ ",j*dy,i*dx,psi\_new[i][j]);
                printf("%f\t",psi_new[i][j]);
        }
        return 0;
      }
iii.
      Line Gauss-Seidel iterative method (TriDiagonal Matrix Algorithm)
      Code
      #include<stdio.h>
      #include<stdlib.h>
      #include<math.h>
      # define m 41
      int main()
```

```
double dx = 1.0/(m-1), dy = 1.0/(m-1)
1),tem[m][m],psi_new[m][m],Error,B,ai,bi,ci,d[m],P[m],Q[m];
  int iteration = 0,i,j;
  Error=1.0;
  B=(dx/dy);
  ai=-2*(1+pow(B,2));
  bi=1.0;
  ci=1.0;
  //boudary conditions
  for (i = 0; i < m; i++)
    for (j = 0; j < m; j++)
      psi_new[0][j]=1.0;
      psi_new[m-1][j]=1.0;
      psi_new[i][0]=1.0;
      if (j==m-1)
       psi_new[i][j]=0.0;
      else
       psi_new[i][j]=0.0;
     }
  FILE *file1;
  file1= fopen("error.txt","w");
  fprintf(file1,"Iteration\t Error\n");
  while (Error>1e-6)
   Error=0.0;
    for (j = 1; j < m; j++)
      d[0]=-pow(B,2)*(psi_new[0][j+1]+psi_new[0][j-1]);
```

```
P[0]=-bi/ai;
   Q[0]=d[0]/ai;
  for (i = 1; i < m; i++)
    d[i]=-pow(B,2)*(psi\_new[i][j+1]+psi\_new[i][j-1]);
    P[i]=-(bi/(ai+ci*P[i-1]));
    Q[i]=(d[i]-ci*Q[i-1])/(ai+ci*P[i-1]);
  }
  for (i = m-2; i > 0; i--)
    tem[i][j]=psi_new[i][j];
     psi_new[i][j]=P[i]*psi_new[i+1][j]+Q[i];
     Error = Error + pow((psi\_new[i][j]-tem[i][j]), 2.0);
  }
  Error=sqrt(Error/((m-2)*(m-2)));
  iteration=iteration+1;
  printf("Iteration= %d\t", iteration);
  printf("Error= %.9f\n", Error);
  fprintf(file1, "%d \t %.9f \n", iteration, Error);
FILE *file2;
file2=fopen("Stream1Tcccv.plt","w");
fprintf(file2,"VARIABLES=\"X\",\"Y\",\"T\"\n");
fprintf(file2, "ZONE t=\"BLOCK1\", J=41,I=41,F= POINT \n\n");
for( i=0; i<m; i++)
     for(j=0; j< m; j++)
       fprintf(file2, "%lf \t %lf \n",j*dy,i*dx,psi_new[i][j]);
       printf("%f\t",psi_new[i][j]);
```

```
}
  return 0;
}
Alternating Direction Implicit method (ADI)
Code
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
# define m 41
int main()
  double dx = 1.0/(m-1), dy = 1.0/(m-1)
1),tem[m][m],psi_new[m][m],Error,B,ai,bi,ci,d[m],P[m],Q[m],d1[m],P1[m],Q1[m];
  int iteration = 0,i,j;
  Error=1.0;
  B=(dx/dy);
  ai=-2*(1+pow(B,2));
  bi=1.0;
  ci=1.0;
  //boudary conditions
  for (i = 0; i < m; i++)
    for (j = 0; j < m; j++)
      psi_new[0][j]=1.0;
      psi_new[m-1][j]=1.0;
      psi_new[i][0]=1.0;
      if (j==m-1)
       psi_new[i][j]=0.0;
      else
       psi_new[i][j]=0.0;
```

iv.

```
}
FILE *file1;
file1= fopen("error.txt","w");
fprintf(file1,"Iteration\t Error\n");
  while (Error>1e-6)
{
  for (i = 0; i < m; i++)
    for (j = 0; j < m; j++)
    tem[i][j]=psi_new[i][j];
  }
  for (j = 0.5; j < m-1; j++)
   d[0]=-pow(B,2)*(psi_new[0][j+1]+psi_new[0][j-1]);
   P[0]=-bi/ai;
   Q[0]=d[0]/ai;
  for (i = 0.5; i < m-1; i++)
    d[i]=-pow(B,2)*(psi_new[i][j+1]+psi_new[i][j-1]);
    P[i] = -(bi/(ai+ci*P[i-1]));
    Q[i]=(d[i]-ci*Q[i-1])/(ai+ci*P[i-1]);
   for (i = m-2; i > 0; i--)
    psi_new[i][j]=P[i]*psi_new[i+1][j]+Q[i];
  }
  for (i = 1; i < m-1; i++)
```

```
d1[0]=-pow(B,2)*(psi_new[i+1][0]+psi_new[i-1][0]);
   P1[0]=-bi/ai;
   Q1[0]=d1[0]/ai;
   for (j = 1; j < m-1; j++)
    d1[j]=-pow(B,2)*(psi_new[i][j+1]+psi_new[i][j-1]);
    P1[j] = -(bi/(ai+ci*P1[j-1]));
    Q1[i]=(d1[i]-ci*Q1[i-1])/(ai+ci*P1[i-1]);
   for (j = m-2; j > 0; j--)
    psi_new[i][j]=P1[j]*psi_new[i+1][j]+Q1[j];
  Error=0.0;
  for (i = 0; i < m; i++)
    for (j = 0; j < m; j++)
     {
      Error = Error + pow((psi\_new[i][j]-tem[i][j]), 2.0);
  Error=sqrt(Error/((m-2)*(m-2)));
  iteration=iteration+1;
  printf("Iteration= %d\t", iteration);
  printf("Error= %.9f\n", Error);
  fprintf(file1, "%d \t %.9f \n", iteration, Error);
FILE *file2;
file2=fopen("Stream1Tddd.plt","w");
fprintf(file2, "VARIABLES = \"X\", \"Y\", \"T\"\n");
fprintf(file2, "ZONE t=\"BLOCK1\", J=41,I=41,F= POINT \n\n");
```

```
for( i=0; i<m; i++)
{
    for(j=0; j<m; j++)
    {
       fprintf(file2, "%lf \t %lf \t %lf \n",j*dy,i*dx,psi_new[i][j]);
       printf("%f\t",psi_new[i][j]);
    }
}
return 0;
}</pre>
```

## v. The output

