

Lecture 4

In last lecture, we looked at some basic MATLAB syntax

Vector or array

>> $x_1 = 0$

$x_1 =$

0

>> $x_2 = 0$ *j*
→ suppress output

>> $x_1 = 1, x_2 = 10;$
↓ *→ suppress output*

Combine two variable declarations into one

using comma

>> $x_1 = 1, x_2 = 10$

$x_1 =$

1

$x_2 =$

10

>> $a = 1 : 10$

→ to create vector between 1 & 10 with spacing 1

$a =$ 1 2 3 4 5 6 7 8 9 10

>> $a = 1 : 2 : 10$

→ to create vector between 1 & 10 with spacing 2

$a =$ 1 3 5 7 9

>> $a = 0.5 : (-0.1) : 0.1$ ← You can have sequence of decreasing numbers too

$a =$

0.5000 0.4000 0.3000 0.2000 0.1000

>> $a = x1 : x2$



use variables to create vectors
(recall that we have set $x1=1, x2=10$)

$a =$

1 2 3 4 .. 10

>> $x1, x2$ ← check

$x1 =$

\cdot

$x2 =$

10

>> $a = [1 2 3]$

$a =$

1 2 3

same effect

>> $a = [1, 2, 3]$

$a =$

1 2 3

>> $\text{size}(a)$ ← compute size of vector or matrix

ans =

1

3

← row vector has just 1 row

row

columns

>> $a = [1 0 2 0 3 0 4]$

$a =$

tell MATLAB to create new row

1
2
3
4

>> size(a)

ans =

(4) (1) ← column vector has just one column

>> b = 1:4

b =

1 2 3 4

>> a = b' ← stands for transpose

row vector becomes column vector
column → , ————— row vector

a :

1
2
3
4

• Array / matrix

>> A = [1, 2, 3; 4, 5, 6; 7, 8, 9]

A =

1	2	3
4	5	6
7	8	9

→ ";" for next element in row

";" for next row

>> size(A)

ans =

(3) (3)

>> A = [1:3; 4:6; 7:9]

A =

1	2	3
4	5	6
7	8	9

Operations on vectors / matrix

+ , - are defined following usual principle

↓
elementwise operations

* , / , ^ - are defined only if these operations are valid between two variables

e.g. if a & b are row vectors

↳ a*b, a/b, a^2 are not valid operations

↳ a.*b, a./b, a.^2 are *, /, ^ operations applied to each element

Similarly

if a & b are column vectors

↳ a*b, a/b, a^2 are not valid operations

↳ a.*b, a./b, a.^2 elementwise operations defined.

General rule

(i) treat row vector or matrix with just one row

(ii) treat column $\text{---} // \text{---}$ one column

(iii) let A be a matrix of size $n \times m$

$B \text{ ---} // \text{---} l \times k$

Then
 $\text{size}(A^*B) = n \times k$

A^*B is defined only if
 $m = l$

$a \rightarrow 1 \times 3$
 $b \rightarrow 3 \times 1$
 a^*b is valid

(# columns of A should be equal to

rows of B)

With this rule, you can see multiplication of

two rows or two columns is invalid

$$\begin{array}{c} a \rightarrow 1 \times 3 \\ b \rightarrow 3 \times 1 \\ a + b \end{array}$$

$$\begin{array}{c} a \rightarrow 1 \times 3 \\ b \rightarrow 3 \times 1 \\ a + b \end{array}$$

$$\begin{array}{c} a \rightarrow 3 \times 1 \\ b \rightarrow 1 \times 3 \\ a + b \end{array}$$

$$\begin{array}{c} a \rightarrow 3 \times 1 \\ b \rightarrow 1 \times 3 \\ a + b \end{array}$$

$$a^*b$$

Example

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}, \quad B = \begin{bmatrix} 0.1 & 0.2 & 0.3 \\ 0.4 & 0.5 & 0.6 \\ 0.7 & 0.8 & 0.9 \end{bmatrix}$$

Then

$$A^*B = \begin{bmatrix} [1, 2, 3] \times \begin{bmatrix} 0.1 \\ 0.4 \\ 0.7 \end{bmatrix} & [1, 2, 3] \times \begin{bmatrix} 0.2 \\ 0.5 \\ 0.8 \end{bmatrix} & [1, 2, 3] \times \begin{bmatrix} 0.3 \\ 0.6 \\ 0.9 \end{bmatrix} \\ [4, 5, 6] \times \begin{bmatrix} 0.1 \\ 0.4 \\ 0.7 \end{bmatrix} & [4, 5, 6] \times \begin{bmatrix} 0.2 \\ 0.5 \\ 0.8 \end{bmatrix} & [4, 5, 6] \times \begin{bmatrix} 0.3 \\ 0.6 \\ 0.9 \end{bmatrix} \\ [7, 8, 9] \times \begin{bmatrix} 0.1 \\ 0.4 \\ 0.7 \end{bmatrix} & [7, 8, 9] \times \begin{bmatrix} 0.2 \\ 0.5 \\ 0.8 \end{bmatrix} & [7, 8, 9] \times \begin{bmatrix} 0.3 \\ 0.6 \\ 0.9 \end{bmatrix} \end{bmatrix}$$

$$= \begin{bmatrix} 3.0 & 3.6 & 4.2 \\ 6.6 & 8.1 & - \\ - & - & - \end{bmatrix}$$

3×3

↳ From our general rule

- multiplication of row and column vectors
- multiplication of column & row vectors

are valid.

e.g. $a = [1, 2, 3]$, $b = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

Then (i) $a * b = 14$ ← scalar

(ii) $b * a = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$ ← matrix

size(a), size(b)

Annotations on the left side of the box:

- 1×3 ← a
- 3×1 ← b
- 1×1 ← $a * b$
- 3×1 ← b
- 1×3 ← a
- 3×3 ← $b * a$

In today's lecture

- plotting
- script file
- function file

Plotting:

```
>> t = 0:0.1:10; ← "vector"  
>> yt = sin(t);
```

$t = [0, 0.1, 0.2, \dots, 10]$

$\sin(t) = [\sin(0), \sin(0.1), \sin(0.2), \dots, \sin(10)]$

$\cos(), \tan(), \tanh()$

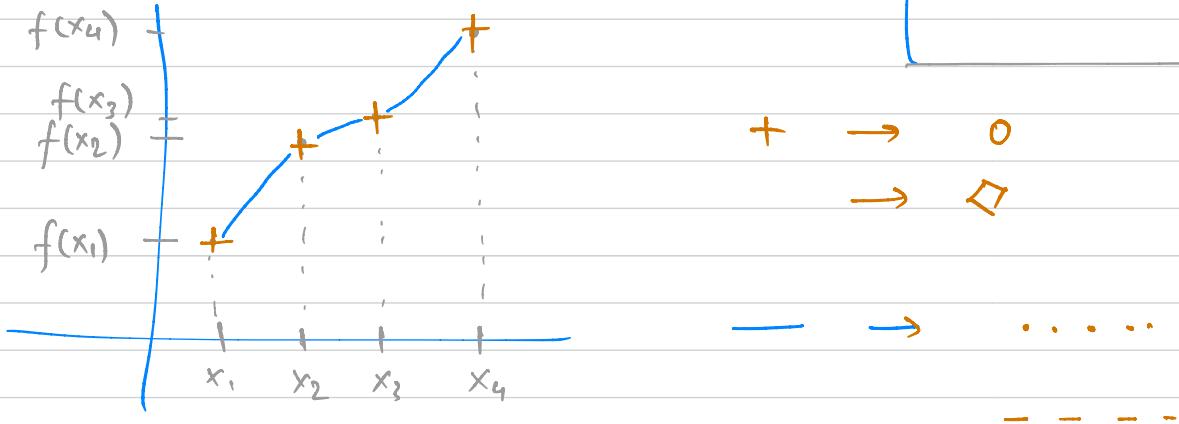
```
>> plot(t, yt)
```

\uparrow function values at
x points

Documentation

>> help plot

help	sin
help	size



Script file:

>> t = 0:0.1:10; \leftarrow row vector

>> yt = sin(t); \leftarrow row vector

>> zt = yt.^2; \leftarrow row vector

>> plot(t, yt, 'r+:') \leftarrow dotted line

>> hold on \leftarrow I want to add more plots to the same figure

>> plot(t, zt, 'g*-') \leftarrow solid line

→ Create a demoPlot.m file

demoPlot.m

t = 0:0.1:10;

20

y_t = sin(t);

z_t = y_t.^ 2;

plot (t, y_t, 'r+')

hold on

plot (t, z_t, 'g*-')

>> demoPlot ↵

↳ it will put variables in your workspace
↳ script file