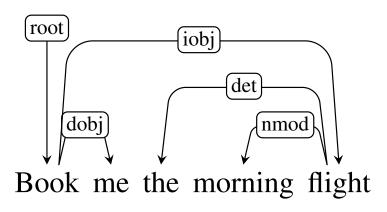
# Lecture 10-12: Language Models

USC VSoE CSCI 544: Applied Natural Language Processing
Jonathan May -- 梅約納
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#### Quiz 1

- Which of the following CFG rules are in CNF (assume capital letters signify nonterminals, lowercase letters signify terminals)?
  - S -> NP VP
  - NP -> NP PP
  - NP -> DT JJ NN
  - NP -> the boy
  - NP -> PP
  - JJ -> red
  - NP -> the NP

#### Quiz 2



- What is the next step?
  - shift
  - reduce
  - LArc
  - RArc
  - LArc-det

Step	Stack	Word List	Action	Relation Added
0	[root]	[book, me, the, morning, flight	] SHIFT	
1	[root, book]	[me, the, morning, flight]	SHIFT	al a la :
2	[root, book, me]	[the, morning, flight]	RArc-dobj	book dobj me
3	[root, book]	[the, morning, flight]	SHIFT	
4	[root, book, the]	[morning, flight]	SHIFT	
5	[root, book, the, morning]	[flight]	SHIFT	
6	[root, book, the, morning, flight]			

- RArc-det
- RArc-nmod
- LArc-nmod

#### Please turn your homework ...

- What word comes next?
  - in
  - over
  - into
  - the
  - refrigerator
- What are the probabilities of each of these?
- And why should we care?

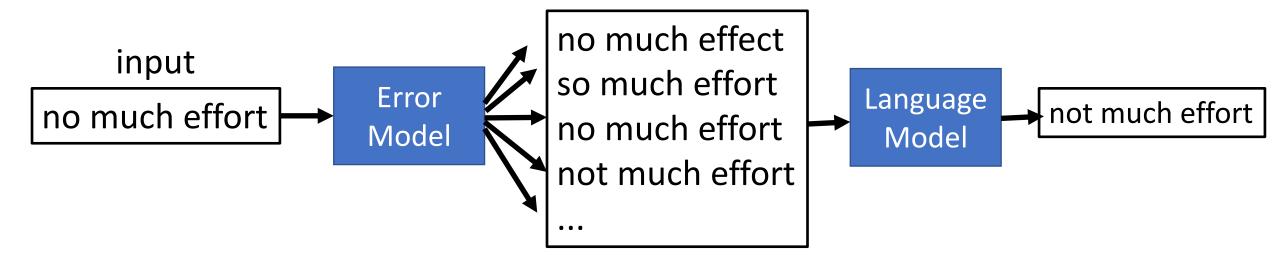
## Probability of a sentence; P(s)

- How likely is it to occur?
- Colloquially, how likely is any speaker of language X to utter s?
  - P(the cat slept peacefully) > P(slept the peacefully cat)
  - P(she studies morphosyntax) > P(she studies more faux syntax)

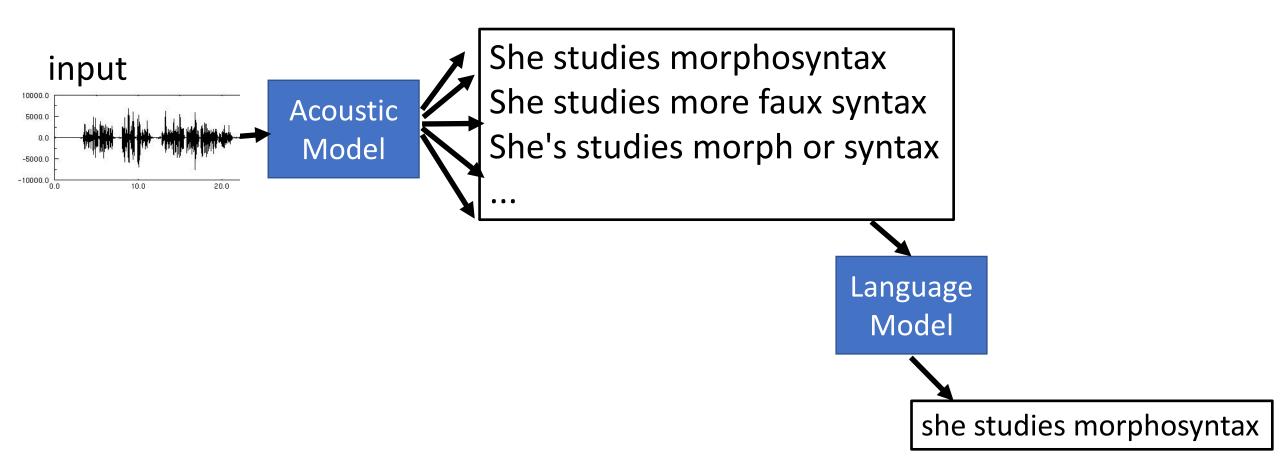
#### Language Models in NLP

- It's very difficult to know the true P(s) for an arbitrary sequence of words
- But we can define a language model that will give us good approximations
- Language models (LMs) are very useful whenever we are generating output
  - Machine Translation
  - Spelling Correction
  - Summarization
  - Speech Recognition
- There are some very good, easy-to-use toolkits for building and using LMs
  - SRILM: around since the 90s. not advised with >300m tokens
  - KenLM: preferred choice; great scalability in memory and time with even billions of tokens
  - NLTK has some LM training/using support (ok for prototyping)

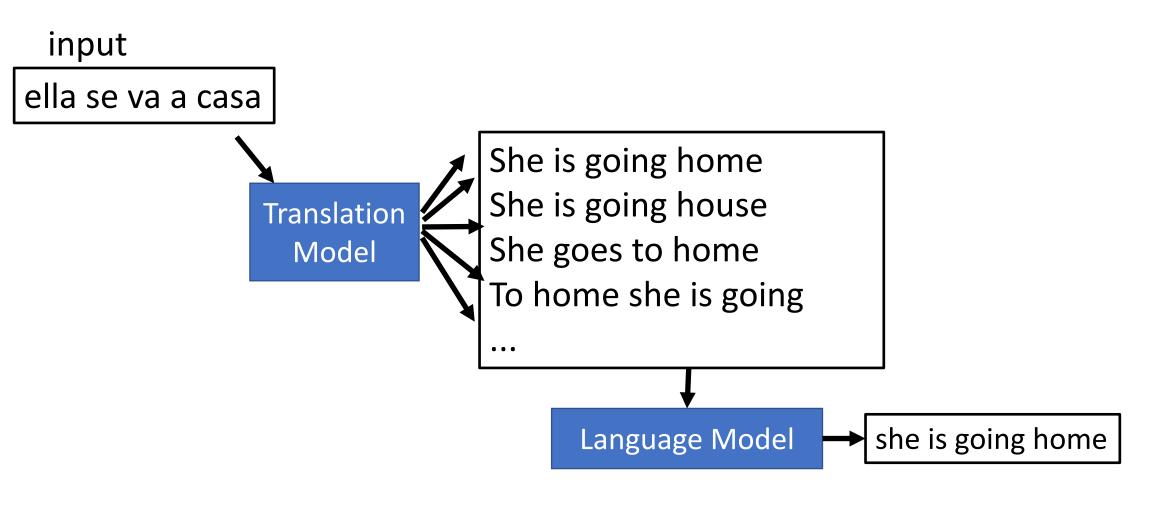
### Use of Language Models: Spelling Correction



## Use of Language Models: Speech Recognition



#### Use of Language Models: Machine Translation



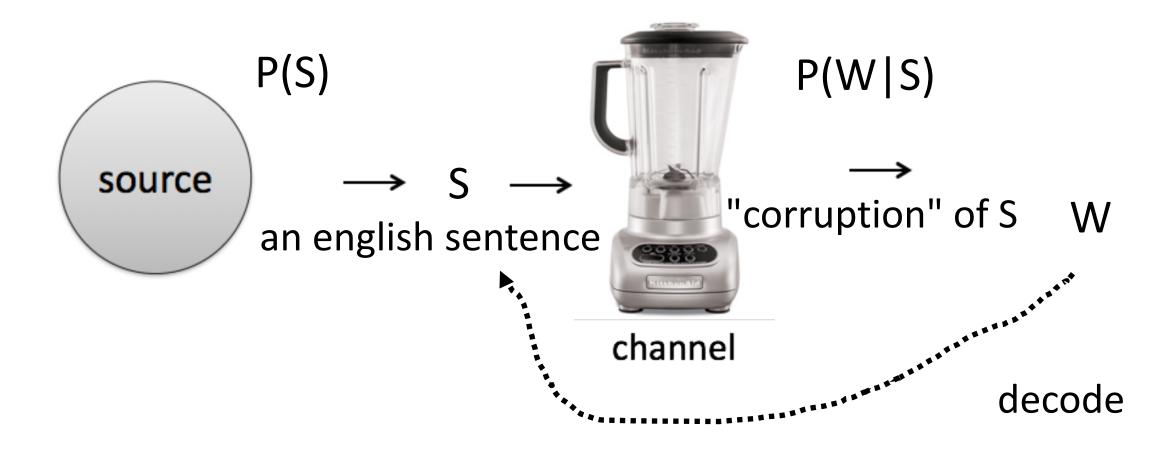
#### LMs for Prediction

- LMs can be used to <u>predict</u> what a human will do next, rather than <u>correct</u> a possibly faulty model
- Example: predictive text correction/completion on your phone
  - Keyboard is tiny, so it's easy to touch a spot slightly off from the letter you intend
  - Correct these errors as you go and also provide possible completions

in e f f i cient

 In this case, LM may be defined over sequences of characters instead of (or in addition to) sequences of words

## Noisy Channel Model



#### But How To Estimate These Probabilities?

- We want to to know the probability of word sequence  $\mathbf{w} = \mathbf{w}_1, \mathbf{w}_2, ..., \mathbf{w}_n$  occurring in English
- Assume we have some <u>training data</u>: large corpus of general English text
- We use this data to <u>estimate</u> the probability of **w** (even if we never see it in the corpus)

#### Bit of Notation: Random Variables

- Random Variable = variable that represents all the possible events in some partition of  $\Omega$
- So if X is a coin flip I can say P(X=heads) to mean probability the flip comes up heads or just P(X) to mean the probability table for the events (heads, tails)
- We can treat Random Variables like events
  - Flip coin A. Independently, flip coin B
  - P(A=heads | B=tails) = P(A=heads); A=heads and B=tails are independent events
  - for all x in {heads, tails}, for all y in {heads, tails}, P(A=x | B=y) = P(A=x); A and B are independent random variables
- We've been using Random Variables all along, actually, but have been a bit sloppy
- (I probably should have discussed these back in Lecture 4)

#### Probability of a word sequence

- $P(\mathbf{w}) = P(w_1, w_2, w_3, w_4, ..., w_n)$
- e.g.  $P(\mathbf{w} = \text{the cat slept quietly}) = P(w_1 = \text{the, } w_2 = \text{cat, } w_3^= \text{slept,}$  $w_4 = \text{quietly})$
- We'll often abuse notation when talking about specific events and context is clear, e.g. P(the cat slept quietly)

#### Maximum Likelihood Estimation?

- Recall Maximum Likelihood Estimations (MLE) for our HMM POS tagger
  - AKA "Count and divide"
- So get a corpus of N sentences
  - P<sub>MLE</sub>(w = the cat slept quietly) = C(the cat slept quietly)/N
- But consider these sentences:
  - the long-winded peripatetic beast munched contentedly on mushrooms
  - parsimonius caught the of about for syntax
- Neither is in a corpus (I just made them up), so  $P_{MIF}=0$  for both
  - But one is meaningful and grammatical and the other isn't!

#### Sparse Data and MLE

- If something doesn't occur, MLE thinks it can't occur
- No matter how much data you get, you won't have enough observations to model all events well with MLE
- We need to make some assumptions so that we can provide a reasonable probability for grammatical sentences, even if we haven't seen them

### Independence (Markov) Assumption

- Recall,  $P(w_1, w_2, ..., w_n) = P(w_n | w_1, w_2, ..., w_{n-1})P(w_{n-1} | w_1, w_2, ..., w_{n-2})...$ 
  - $\prod_{i=1}^{n} P(w_i|w_1,...,w_{i-1})$
- Still too sparse (nothing changed)
  - if we want P(I spent three years before the mast)
  - we still need P(mast | I spent three years before the)
- Remember definition of independence; A and B are independent if P(A) = P(A|B)

### Independence (Markov) Assumption

- Make an <u>n-gram</u> independence assumption: probability of a word only depends on a fixed number of previous words (<u>history</u>)
  - trigram model:  $P(w_i|w_1,...,w_{i-1}) \approx P(w_i|w_{i-2},w_{i-1})$
  - bigram model:  $P(w_i|w_1,...,w_{i-1}) \approx P(w_i|w_{i-1})$
  - unigram model:  $P(w_i|w_1, ..., w_{i-1}) \approx P(w_i)$
- I.e. a trigram model says
  - P(mast | I spent three years before the) ≈ P(mast | before the)
- It also assumes all these are equal:
  - P(mast | I spent three years before the)
  - P(mast | I went home before the)
  - P(mast | I saw the sail before the) because all are estimated as P(mast | before the)
- Not always a good assumption! But it does reduce the sparse data problem

#### Estimating Trigram Conditional Probabilities

- P<sub>MLE</sub>(mast | before the) = Count(before the mast)/Count(before the)
- In general, for any trigram, we have

• 
$$P_{MLE}(w_i|w_{i-2},w_{i-1}) = \frac{\text{Count}(w_{i-2},w_{i-1},w_i)}{\text{Count}(w_{i-2},w_{i-1})}$$

### Example from *Moby Dick* corpus

- C(before, the) = 25; C(before, the, mast) = 4
- C(before, the, mast) / C(before, the) = 0.16
- mast is the most common word to come after "before the" (wind is second most common)
- $P_{MLE}(mast) = 56/110927 = .0005$  and  $P_{MLE}(mast|the) = .003$
- Seeing "before the" vastly increases the probability of seeing "mast" next

#### Trigram model summary

- To estimate P(w), use chain rule and make an independence assumption
  - $P(w_1, ..., w_n) = \prod_{i=1}^n P(w_i|w_1, ..., w_{i-1})$
  - $\approx P(w_1)P(w_2|w_1)\prod_{i=3}^n P(w_i|w_{i-2},w_{i-1})$
- Then estimate each trigram prob from data (here, using MLE)
  - $P_{MLE}(w_i|w_{i-2},w_{i-1}) = \frac{\text{Count}(w_{i-2},w_{i-1},w_i)}{\text{Count}(w_{i-2},w_{i-1})}$

#### Midterm Info

Some of you will NOT BE IN SAL 101 YOU WILL BE IN MHP (Mudd) 101





#### Who is Where?

- If your last\* name is from Aggarwal to Patel, you are in SAL 101
- If it is from Pathapi to Zhu, you are in MHP 101
- \* "Last" is a very western term. I have an alphabetization based on what USC has your surname listed as.
- To avoid confusion, please check the course website, which has a very prominent link to a roster with firstname, last name, partially masked email address, and assignment
- If you are still unsure of where to go, contact us on piazza ASAP

#### Midterm Logistics

- Length: 1 hour, 40 minutes (you will need time to set up and hand in exam)
- Date: Friday, October 6, 8:00 AM (Please arrive promptly!)
- Please Bring:
  - Pencils/pens/erasers as needed
  - one 8.5x11 inch (or A4) sheet of paper with notes on both sides (optional)
  - NO OTHER NOTES
  - NO ELECTRONIC RESOURCES
  - NO BOOKS
- We will provide extra paper for scratch work
- Sit only at seats with exams on them. Fill up all available space.

#### What's On The Exam?

- Fair game
  - Anything on the slides
  - Anything in the required reading
  - Anything in the homeworks
- But
  - We're not trying to trick you
  - We're not trying to make this impossible
  - If you understand the lectures well, you should be ok

#### What's On The Exam

- Major Topics
  - Levels of Linguistic Knowledge (L1)
  - Corpora, Regex, Basic text processing (L2)
  - Morphology, Finite State Automata and Transducers (L3)
  - Probability Theory (L4)
  - Naive Bayes, Features, Perceptron, Logistic Regression (L5)
  - POS Tagging and HMM tagger, Viterbi Decoding (L6)
  - Constituency Syntax Trees, Context-Free Grammars, CKY, CNF, Smoothing, Interpolating, Beam Decoding (L7-8)
  - Dependency Syntax Trees, Arc-Standard and Arc-Eager Dependency Parsing (L9-10)
  - Ngram Language Models, Smoothing, Backoff, Interpolation, alternate language models (L10-11) (Probably no neural; depends on how far we get)
- It won't all be on there because there isn't enough time
  - But there is plenty of room on the final

## Practical details (I)

- Trigram model assumes two-word history
- But consider these sentences:

$\mathbf{w_1}$	W <sub>2</sub>	W <sub>3</sub>	$\mathbf{w}_4$
he	saw	the	yellow
feeds	the	cats	daily

- What's wrong?
  - a sentence shouldn't end with 'yellow'
  - a sentence shouldn't begin with 'feeds'
- Does the model capture these problems?

## Beginning / end of sequence

• To capture behavior at beginning/end of sequences, we can augment

• 1		•				
T	na	ın	n	1 1	т•	
u	he		IJ	u	L.	
			1	•		

<b>W</b> <sub>-1</sub>	$\mathbf{w_0}$	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	W <sub>4</sub>	<b>w</b> <sub>5</sub>
<b>&lt;</b> \$>	<s></s>	he	saw	the	yellow	
<s></s>	<s></s>	feeds	the	cats	daily	

- That is, assume  $w_{-1}=w_0=<s>$  and  $w_{n+1}=</s>$  so:
  - $P(\mathbf{w}) = \prod_{i=1}^{n+1} P(w_i | w_{i-2}, w_{i-1})$
- Now P(</s>|the, yellow) is low, indicating this is not a good sentence
- P(feeds | <s>, <s>) should also be low

### Beginning/end of sequence

- Alternatively, we could model all sentences as one (very long) sequence, including punctuation
  - two cats live in sam 's barn . sam feeds the cats daily . yesterday , he saw the yellow cat catch a mouse . [...]
- Now, trigram probabilities like P(. | cats daily) and P(, | . yesterday)
   tell us about behavior at sentence edges
- Here, all tokens are lowercased. What are the pros/cons of <u>not</u> doing that?

## Practical details (II)

- Word probabilities are typically very small.
- Multiplying lots of small probabilities quickly gets so tiny we can't represent the numbers accurately, even with double precision floating point.
- So in practice, we typically use <u>log probabilities</u> (usually base-e)
  - Since probabilities range from 0 to 1, log probs range from -∞ to 0
  - Instead of <u>multiplying</u> probabilities, we <u>add</u> log probs
  - Often, negative log probs are used instead; these are often called "costs";
     lower cost = higher prob
- Recall: we saw this with bigram HMM for POS tagging

### Interim Summary: N-gram probabilities

- "Probability of a sentence": how likely is it to occur in natural language?
- We can never know the true probability, but we may be able to estimate it from corpus data.
- N-gram models are one way to do this:
  - To alleviate sparse data, assume word probs depend only on short history
  - Tradeoff: longer histories may capture more, but are also sparser
  - So far, we estimated N-gram probabilities using MLE

#### Interim Summary: Language Models

- <u>Language Models</u> tell us  $P(\mathbf{w}) = P(w_1, ..., w_n)$ : How likely is this sequence of words to occur?
  - Roughly: Is this sequence of words a "good" one in my language?
- LMs are used as a component in applications such as speech recognition, machine translation, and predictive text completion
- To reduce sparse data, N-gram LMs assume words depend only on a fixed-length history, even though we know this isn't true
- Next:
  - How to evaluate a language model
  - Weaknesses of MLE and how to address them (more sparsity)

#### Quiz 3

- Which of These Statements are True?
  - Naive Bayes is a probabilistic model
  - Perceptron is a generative model
  - Logistic regression has a closed-form solution
  - Logistic regression is a discriminative model

#### Two Types of Evaluation in NLP

- Extrinsic: measure performance on a downstream application
  - For LM, plug it into a machine translation/ASR/etc system
  - The most reliable and useful evaluation: We don't use LMs absent other technology
  - But can be time-consuming
  - And of course we still need an evaluation measure for the downstream system
- Intrinsic: design a measure that is inherent to the current task
  - much quicker/easier during development cycle
  - not always easy to figure out what the right measure is. Ideally, it's one that correlates with extrinsic measures
  - Extra-hard for LMs

## Intrinsically Evaluating a Language Model

- For parsing, tagging, sentiment, etc. it was fairly clear how to evaluate: Hold a set of labeled data out and see how often your model gets it right
- For LM, it's not quite so clear
  - Given a corpus of sentences and non-sentences, see how often the LM thinks you have a sentence?
  - Not a very realistic evaluation of how an LM is used
  - Often we are deciding between not-that-grammatical outputs
- Ideally we want a regression evaluation
  - Given a sentence, how close is the model probability to the true probability
  - But we don't know the true probability of a sentence!

## Idea: Model should give high probability to an unseen corpus

- Assume that you have a proper probability model, i.e. for all sentences S in the language L,  $\sum_{S \in L} P(S) = 1$
- Then take a held-out test corpus T consisting of sentences in the language you care about
- $\prod_{t \in T} P(t)$  should be as high as possible; model should think each sentence is a good one
- Let's be explicit about evaluating each word in each sentence
  - $\prod_{t \in T} \prod_{w \in t} P(w)$
- Collapse all these words into one big 'sentence' N:
  - $\prod_{w \in N} P(w)$

# Resolving Some Problems

- $\prod_{w \in N} P(w)$  is going to result in underflow. Ok, let's use logs again!
- Also we tend to like positive sums.
  - $-\sum_{w \in N} \log(P(w))$
- This can be tough to compare against corpora of different length (or sentences of different length), so normalize by the number of words:
  - $\frac{-\sum_{w\in N}\log(P(w))}{|N|}$  is called the <u>cross-entropy</u> of the data according to the model
- When comparing models, differences between these numbers tend to be pretty small, so we exponentiate
  - $2^{\frac{-\sum_{w\in N} \log(P(w))}{|N|}}$  is called the <u>perplexity</u> of the data

### Example

- Three word sentence with probabilities ¼, ½, ¼
  - ½ \* ½ \* ¼ = .03125
  - cross-entropy:  $-(\log(1/4) + \log(1/2) + \log(1/4))/3 = 5/3$ ;  $2^{5/3} \approx 3.17$
- Six word sentence with probabilities ¼, ½, ¼, ¼, ½, ¼
  - $\frac{1}{4}$  \*  $\frac{1}{2}$  \*  $\frac{1}{4}$  \*  $\frac{1}{4}$  \*  $\frac{1}{2}$  \*  $\frac{1}{4}$  = .00097
  - cross-entropy:  $-(\log(1/4) + \log(1/2) + \log(1/4) + \log(1/4) + \log(1/4) + \log(1/4))/6 = 10/6$ ;  $2^{10/6} \approx 3.17$
- If you overfit your training corpus so that P(train) = 1, then Perplexity on train is 0
- But Perplexity on test (which doesn't overlap with train) will be infinite

#### Intrinsic Evaluation Big Picture

- Lower Perplexity is better
- Roughly = number of bits needed to communicate information about a word
  - The terms 'cross-entropy' and 'perplexity' come out of information theory; it's in the reading if you're interested but we won't dwell on it
- In principle you could compare on different test sets
- In practice, domains shift. To know which of two LMs is better, train on common training sets, test on common test sets

#### Sparse data, again

- Suppose we build a trigram model from Moby Dick and evaluate the sentence "I spent three years before the mast"
- "I spent three" never occurs in training, so P<sub>MLE</sub>(three | I spent) = 0
- so cross-entropy is infinite
- This is basically right; our model says "I spent three" should never occur so when it does our model is infinitely surprised!
- Even with a unigram model we run into words we never saw, so we need better ways to estimate probabilities from sparse data

# Add-1 (Laplace) and Add-α (Lidstone) Smoothing Again

- Pretend we saw everything 1 ( $\alpha$ ) more times than we did before
- $P_{+1}(w_i|w_{i-2}, w_{i-1}) = (C(w_{i-2}, w_{i-1}, w_i)+1)/(C(w_{i-2}, w_{i-1})+|V|)$  where |V| is the size of the vocabulary
- $P_{+\alpha}(w_i|w_{i-2},w_{i-1}) = (C(w_{i-2},w_{i-1},w_i)+\alpha)/(C(w_{i-2},w_{i-1})+\alpha|V|)$

# Dealing with unknown vocabulary

- Can we also add a new 'OOV' token as was done in HMM emission table?
- It gets kind of complicated...
- $P_{+\alpha}(w_i|w_{i-2},w_{i-1}) = (C(w_{i-2},w_{i-1},w_i)+\alpha)/(C(w_{i-2},w_{i-1})+\alpha|V|+1)$
- $P_{+\alpha}$  (wi=OOV|  $W_{i-2}$ ,  $W_{i-1}$ ) =  $\alpha/(\alpha |V|+1)$
- But then we also have to deal with, e.g.,  $P_{+\alpha}$  ( $w_i | w_{i-2}$ ,  $w_{i-1}$ =OOV)
- Better solution: replace low-count words in corpus with "OOV"
- Intuition: 1-count is basically the same as 0-count

#### Remaining Problem

- In a training corpus, suppose we see Scottish beer but neither of
  - Scottish beer drinkers
  - Scottish beer eaters
- If we build a smoothed trigram model (with any kind of smoothing), which example has higher probability?
  - Both the same! Unknown events are treated equally by smoothing!

### Remaining Problem

- Previous smoothing methods assign equal probability to unseen events
- Better: use information from lower-order N-grams (shorter histories)
  - beer drinkers
  - beer eaters
- Two ways: <u>backoff</u> and <u>interpolation</u>

#### Backoff

- Idea: Trust the highest order language model that contains your N-gram
- $P_{BO}(z|xy) =$   $(1-\alpha_{xy})P(z|xy)$  if count(xy) > 0 $\alpha_{xy}P_{BO}(z|y)$  else
- where  $\alpha_{\mbox{\tiny {\rm XV}}}$  is an interpolation parameter

# Simple Interpolation

Idea: Trust different amounts of context differently

• 
$$P_{SI}(z|xy) =$$

$$\lambda_3 P(z|xy) +$$

$$\lambda_2 P(z|y) +$$

$$\lambda_1 P(z) +$$

$$\lambda_0$$

- where  $\lambda_0 + \lambda_1 + \lambda_2 + \lambda_3 = 0$ , all >=0
- We did something similar in lexicalized constituency parsing

### Better Interpolation

Idea: As in backoff, particular contexts matter

• 
$$P_{SI}(z|xy) =$$

$$\lambda_{xy} P(z|xy) +$$

$$\lambda_{y/xy} P(z|y) +$$

$$\lambda_{1/xy} P(z) +$$

$$\lambda_{0/xy}$$

- where, for each xy,  $\lambda_{0/xy} + \lambda_{1/xy} + \lambda_{y/xy} + \lambda_{xy} = 0$ , all >=0
- Best not to actually have a different set for each unique context; can group by context <u>count</u>

### State-of-the-art Smoothing

- There is lots and lots of work done on smoothing and lots of variants
- See Chen and Goodman (optional reading); it's actually quite comprehensive, though mathy
- Best today is <u>Modified Kneser-Ney</u>
  - replace MLE with estimates based on count of unique histories
  - 4 interpolation lambdas based on ngram counts
- For very large data, Google's <u>Stupid Backoff</u>
  - Really fast to calculate
  - Doesn't give proper perplexities!
  - Works well in practice
- These are available in SRILM (K-N) and KenLM (both)