

# Syntax And Parsing

Jonathan May  
CSCI 662  
October 14/16, 2014

# Credits/Further Reading

- Michael Collins' notes:
  - <http://www.cs.columbia.edu/~mcollins/courses/nlp2011/notes/pcfgs.pdf>
  - <http://www.cs.columbia.edu/~mcollins/courses/nlp2011/notes/lexpcfgs.pdf>
- Luke Zettlemoyer's/Dan Klein's notes:
  - <http://homes.cs.washington.edu/~lsz/lectures/parsing.pdf>
- Yoav Goldberg's notes:
  - <http://u.cs.biu.ac.il/~89-680/parsing-and-cky.pdf>
- Jason Eisner's notes:
  - <http://u.cs.biu.ac.il/~89-680/eisner-parse.pdf>
- Chris Manning's lectures:
  - <http://nlp.stanford.edu/courses/Isa354/>
- Klein and Manning on parsing:
  - <http://www.cs.berkeley.edu/~klein/papers/unlexicalized-parsing.pdf>

# Syntax

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- A system of arrangement of words and phrases of (human) language
- There's a lot of ways to communicate but we can still identify verbs, nouns, phrases acting like verbs and nouns, modifiers, etc.
- The structure helps us create sentences and inherently knowing the structure helps us interpret the unfamiliar.

# Syntax

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- “Hexy planars garumphed by the snox three zamfirs ago.”



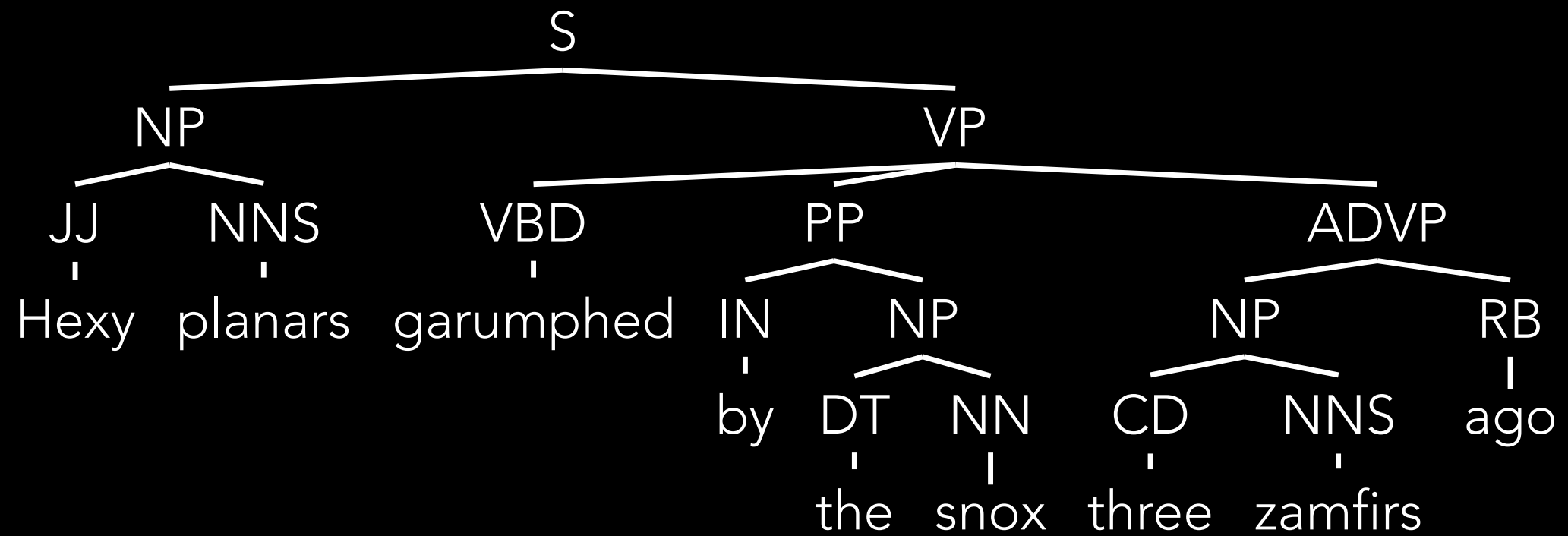
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- “Hexy planars garumphed by the snox three zamfirs ago.”
- What kind of planars are being discussed?

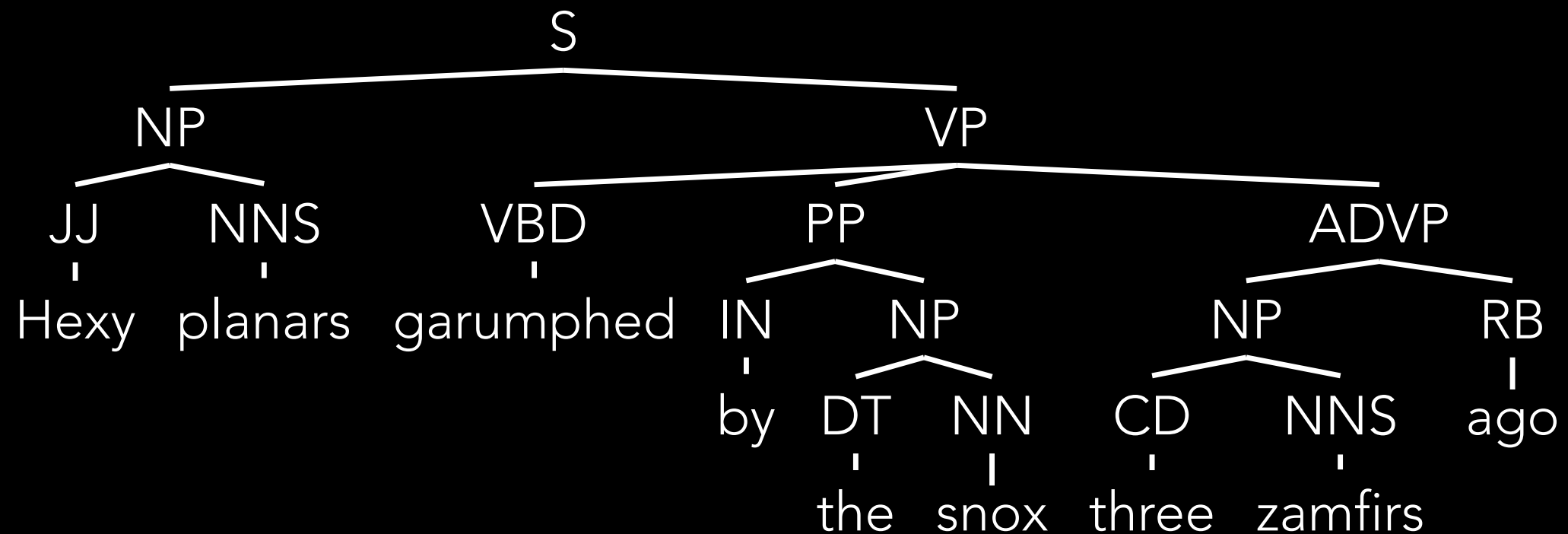
# Syntax

- “Hexy planars garumphed by the snox three zamfirs ago.”
- What kind of planars are being discussed?
- Why do you know that?

# Syntax

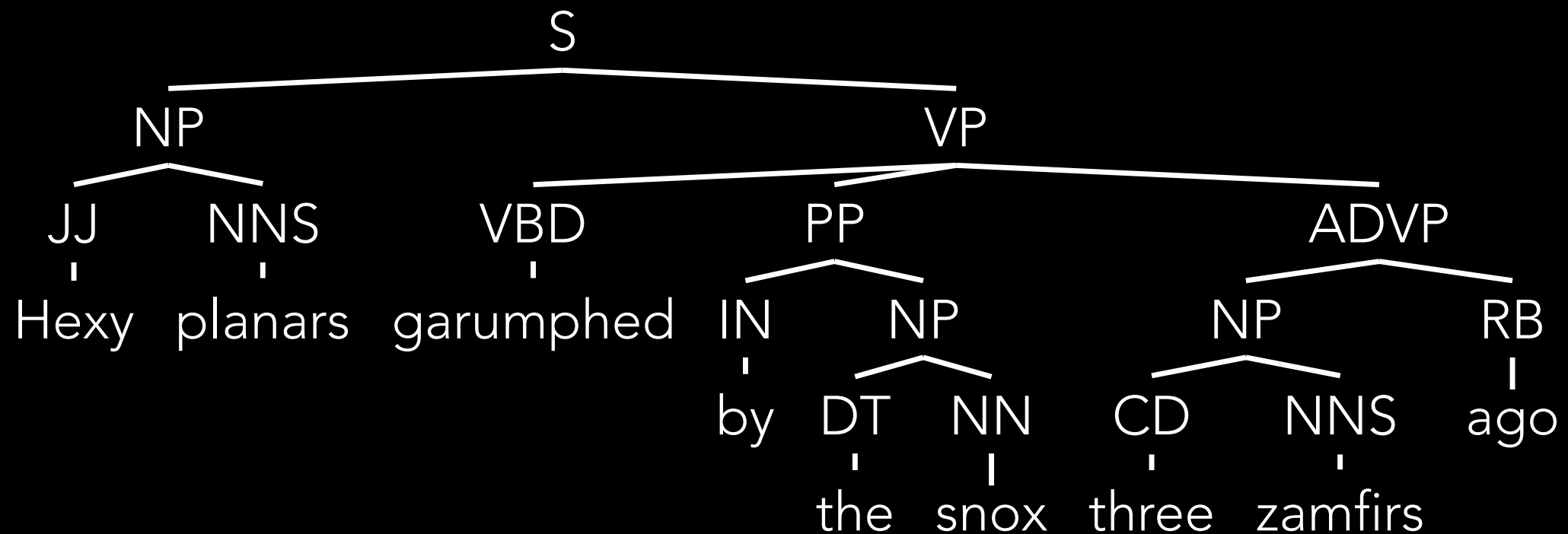


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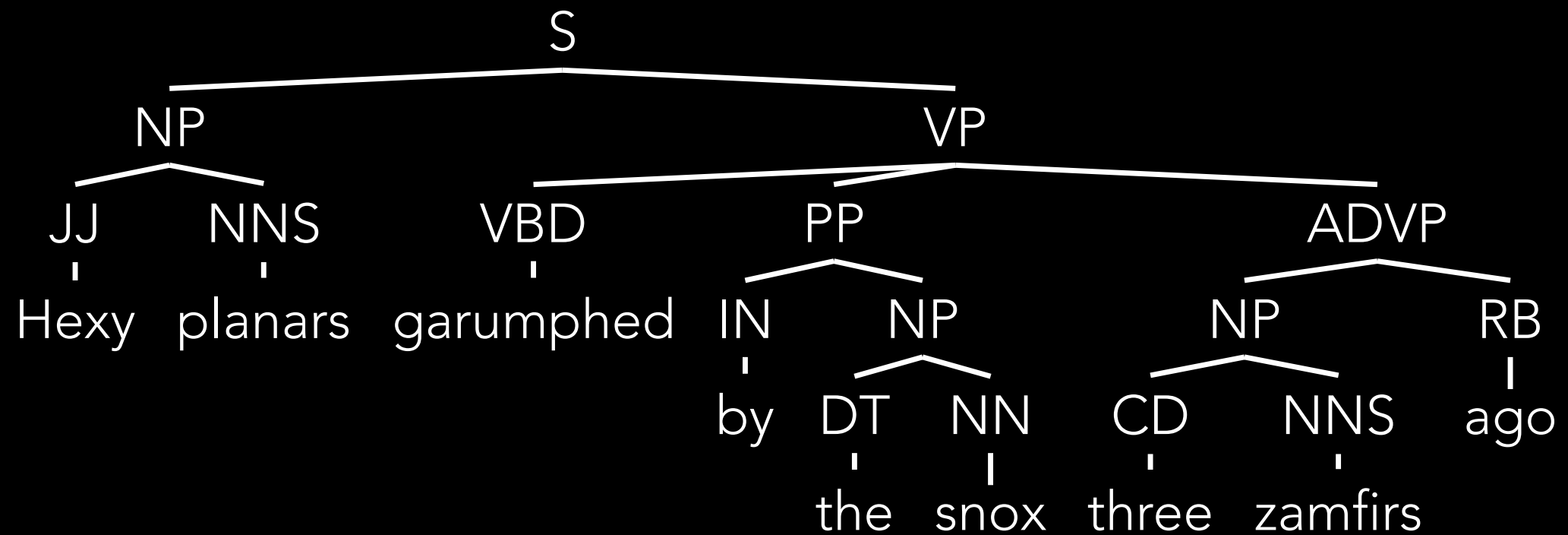
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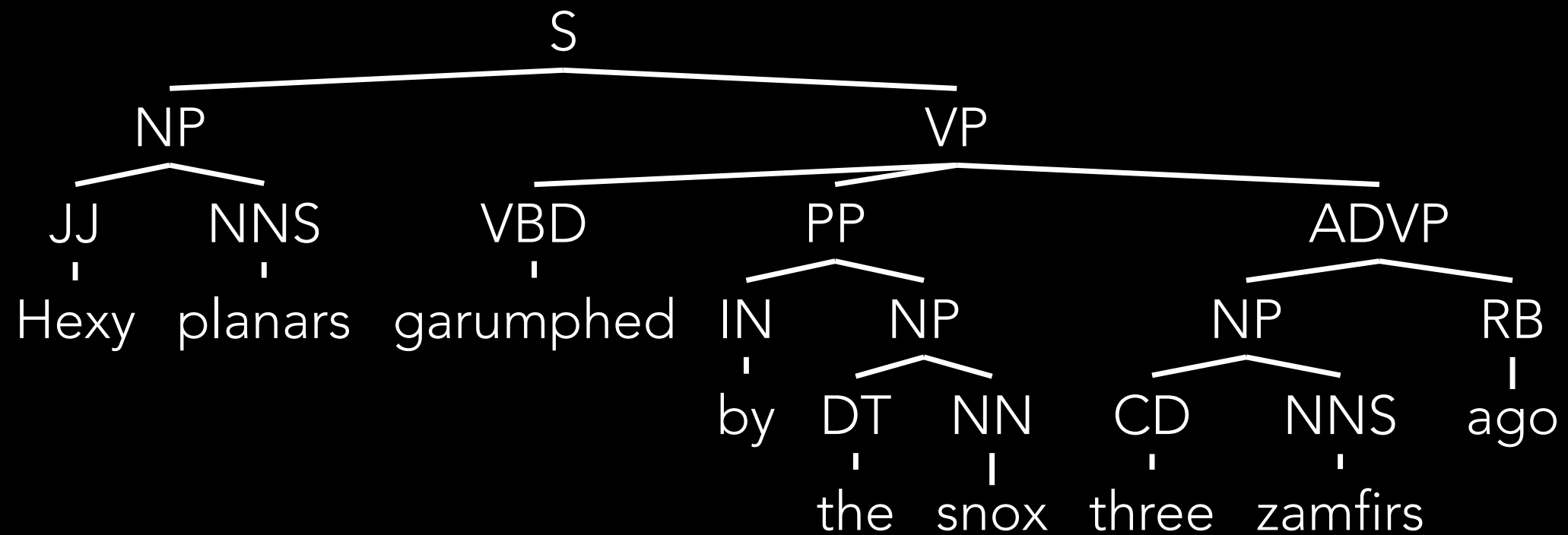


- The characteristics of the words and their relative location to each other allow us to generate this interpretation even though we don't really understand the sentence
- Goal of *parsing* is to write a computer program to generate this automatically.

# Uses of Syntax

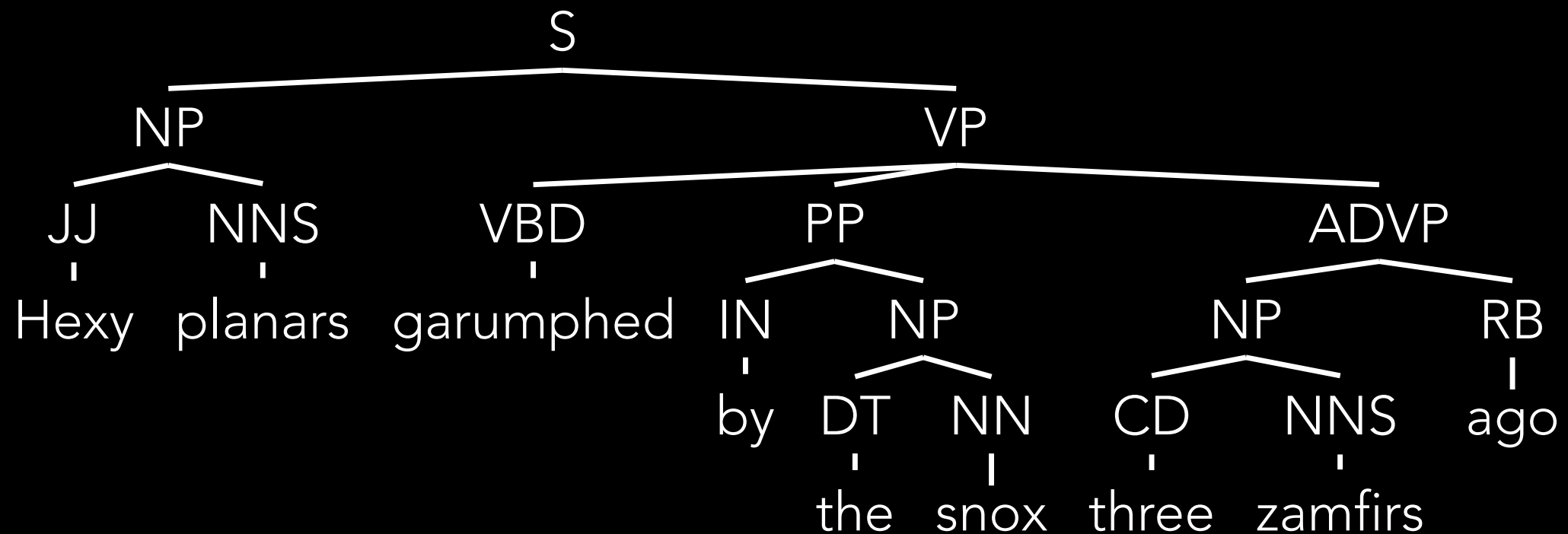


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- Question answering (When did hexy planars garumph?)

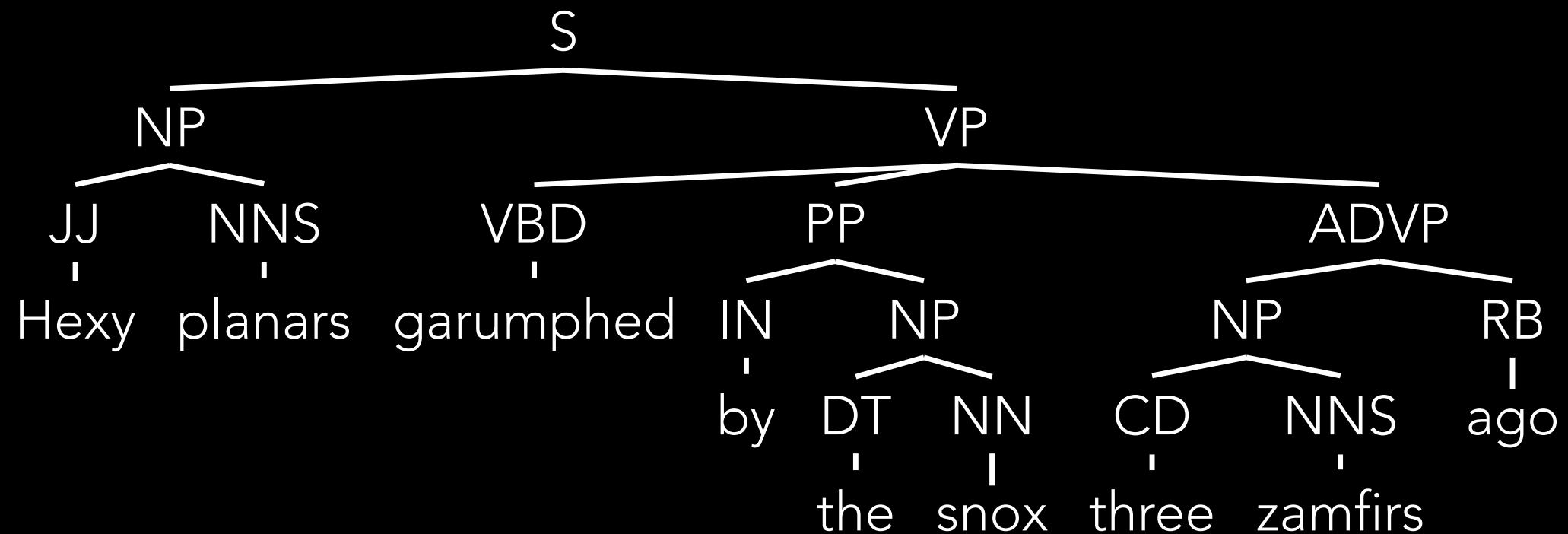
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- Sentence compression (Hexy planars garumphed.)



# Uses of Syntax



- **Question answering** (When did hexy planars garumph?)
- Sentence compression (Hexy planars garumphed.)
- Machine translation (Planares hexos ...)

# Penn Treebank (Marcus et al., '93)

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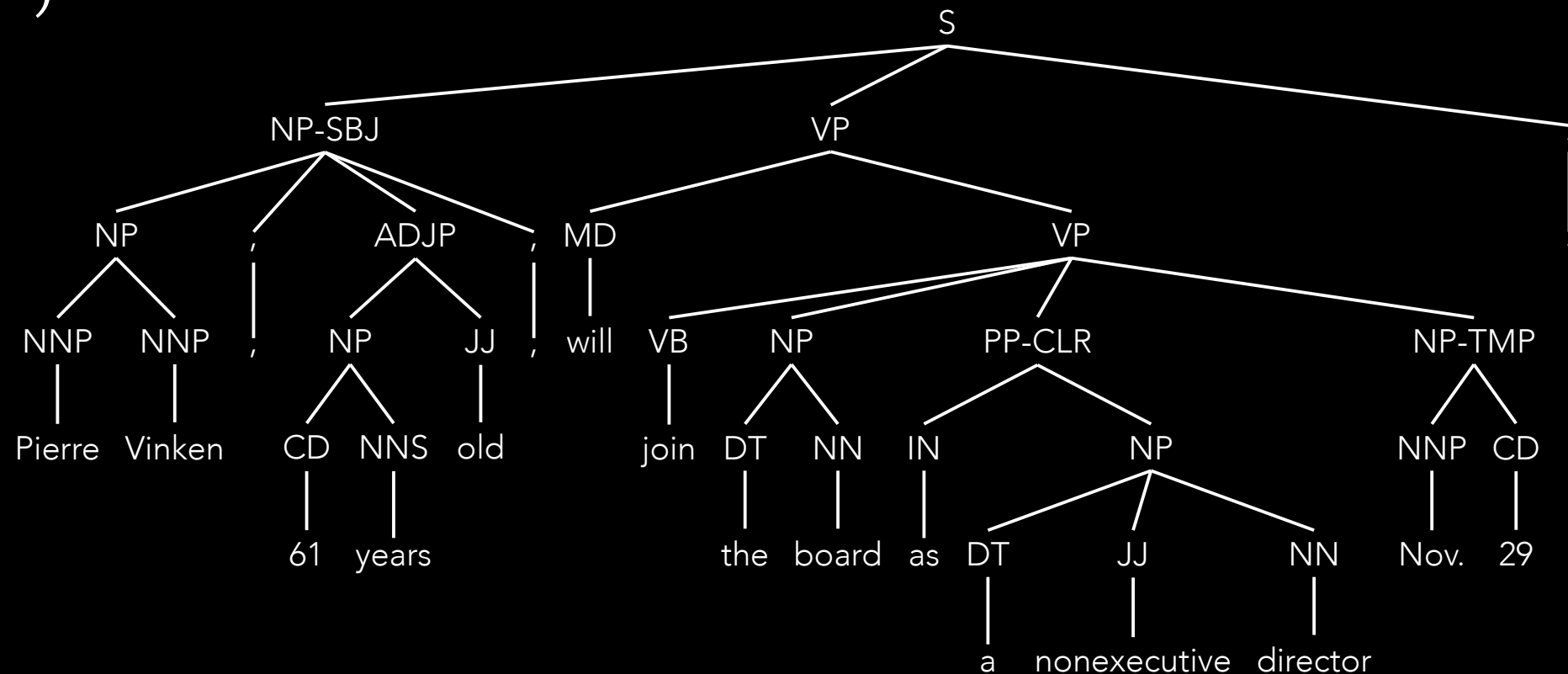
- Goal: investigate the syntactic phenomena that naturally occur
- 1 million words of English Wall Street Journal text in 40,000 sentences, annotated with syntactic structure
- \$1/word
- Since then, treebanks have been created for many other languages

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36 POS (part of speech) tags:

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MD = modal IN = preposition

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punctuation, pronouns, adverbs, the word “to”, foreign words, etc.

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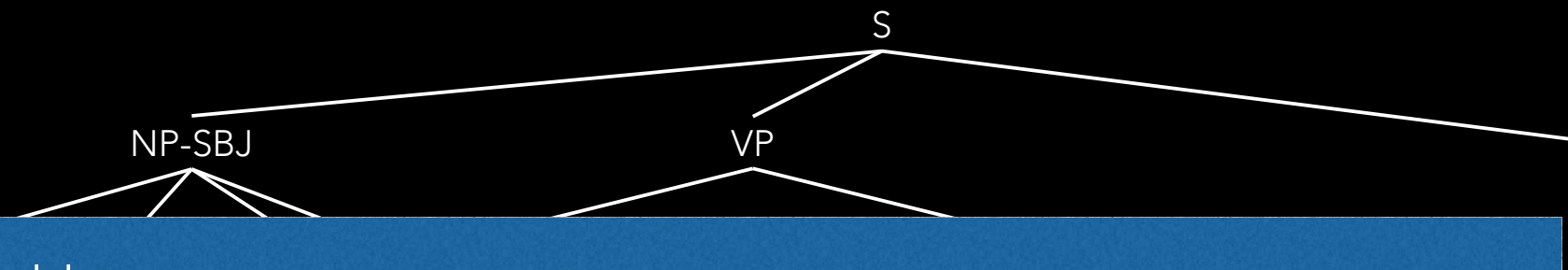
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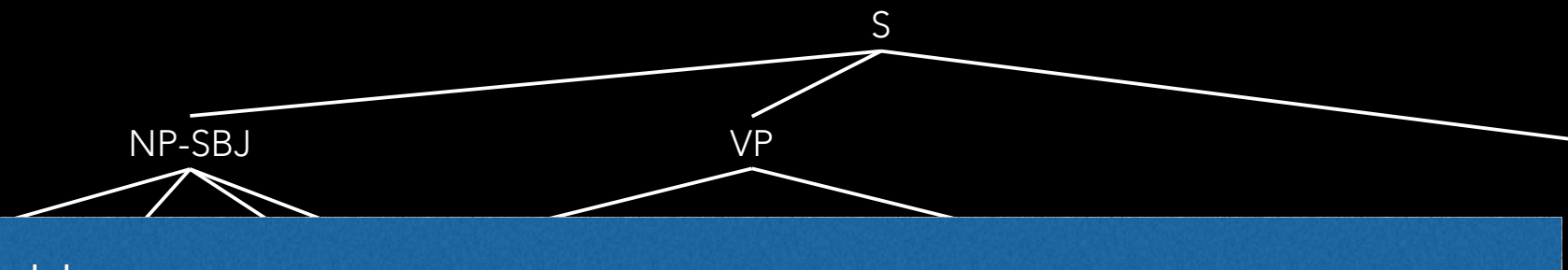


26 constituent tags:

S = declarative sentence	NP = noun phrase
VP = verb phrase	ADJP = adjective phrase
PP = prepositional phrase	SBAR = sentential clause
SQ = question	SINV = inverted sentence
	FRAG = fragment
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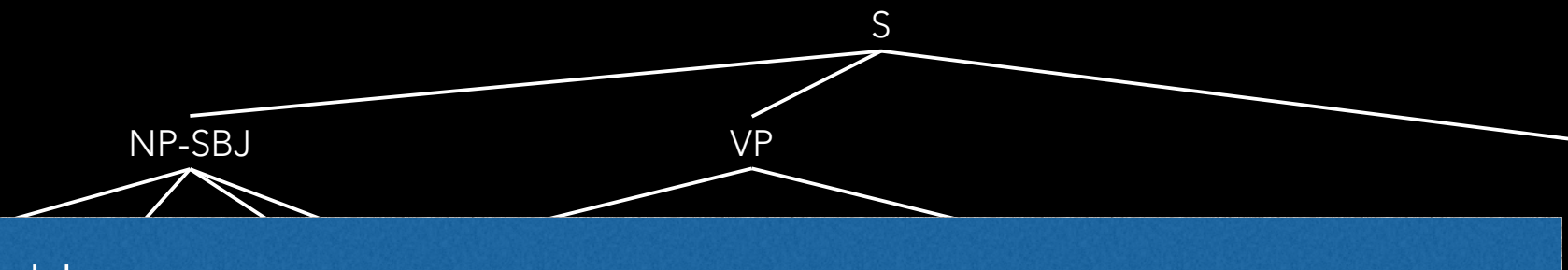
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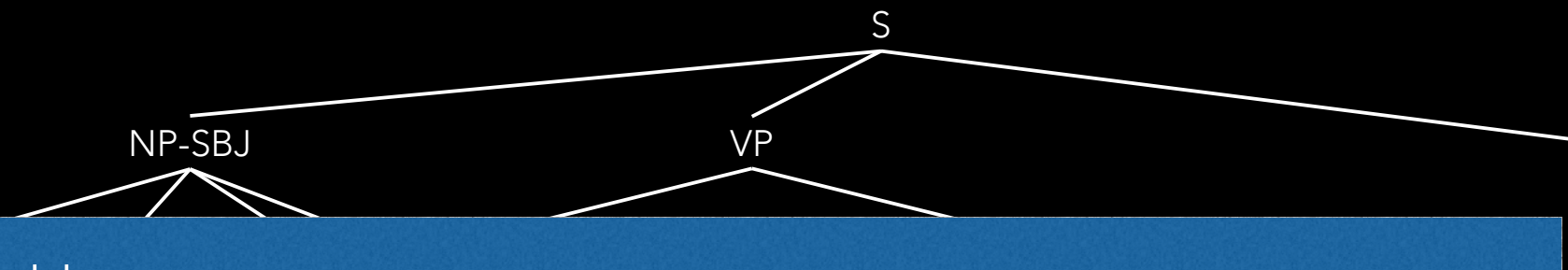
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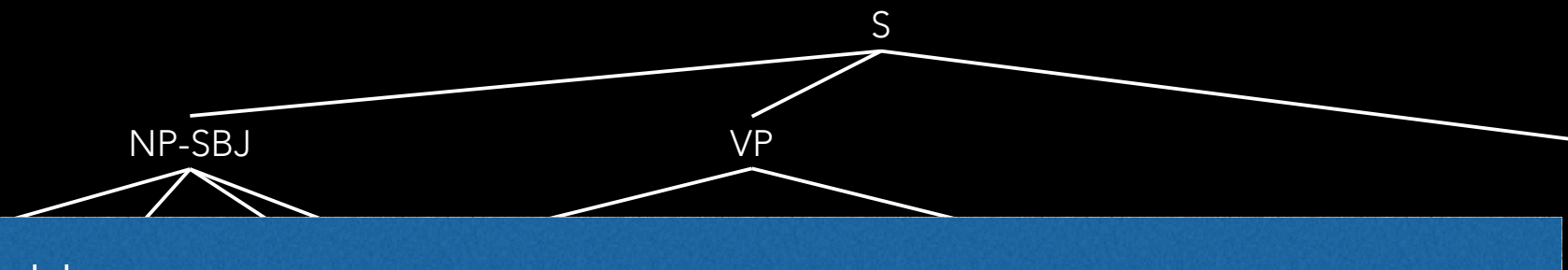
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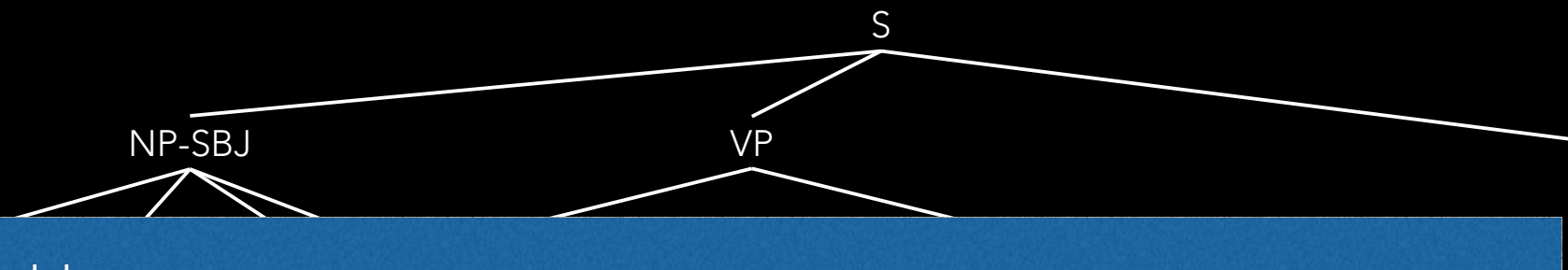
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20 function tags:

- SBJ = subject of sentence
- CLR = closely related (in this case, to the verb)
- TMP = temporal
- ...

These are usually not considered in parsing. I've never paid any attention to them.

a nonexecutive director



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- The Treebank provides a documentation of how (a very specific subset of) people actually structure English.
- Constructed with this goal: given a new sentence, can we automatically put the tree on top? (i.e. syntactic parsing)

# How to Use The Treebank

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- Evaluation:
  - I'll give you some of the sentences from the treebank (without trees).
  - You give me the trees your computer parser produced.
  - I'll tell you how close you were to the human trees.

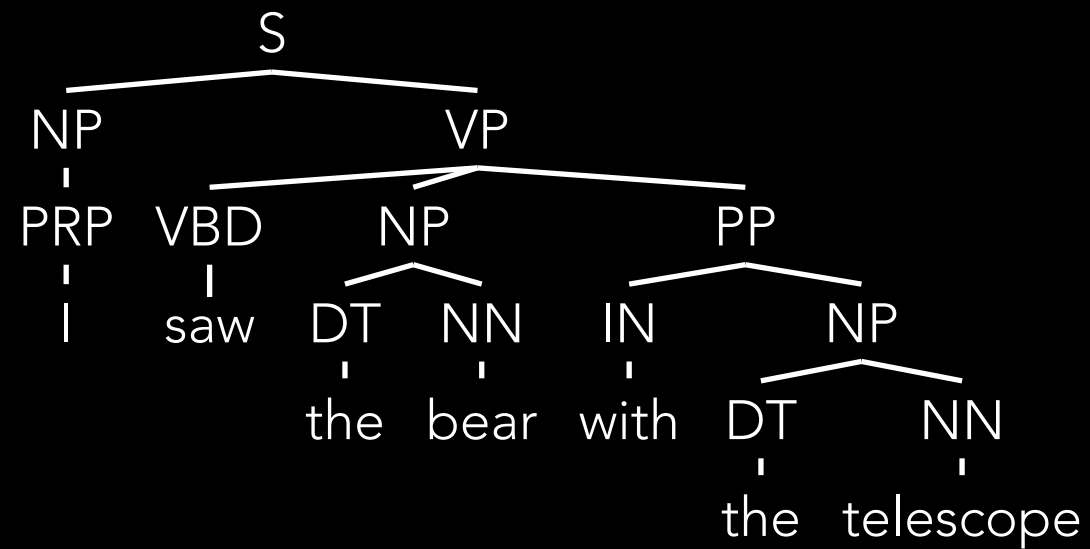
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- Training:
  - Use the treebank trees as input to some data-driven parsing algorithm (just don't use the same trees to evaluate)
  - Standard split: sections 2-21 for training, section 23 for test

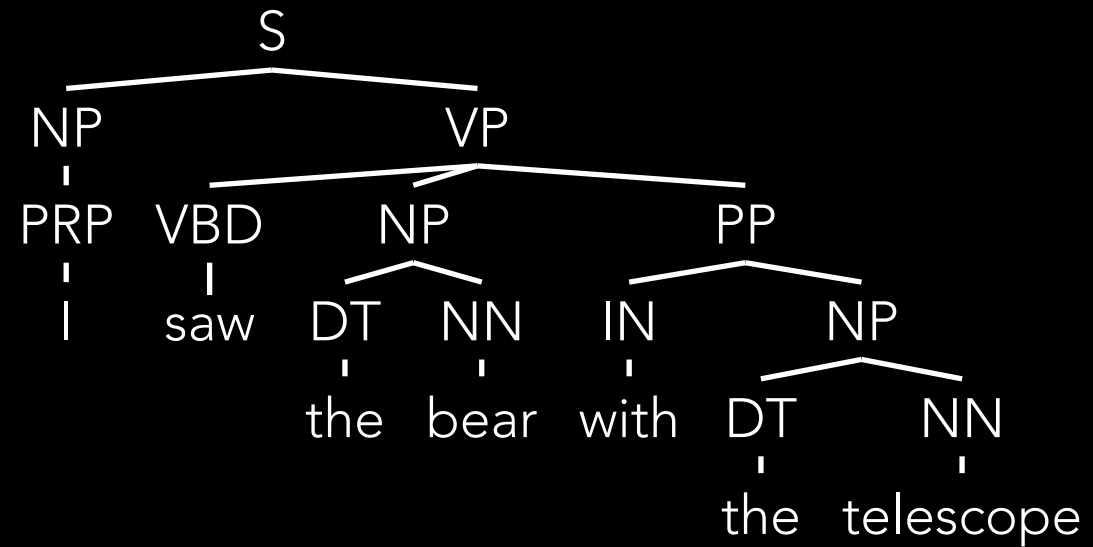
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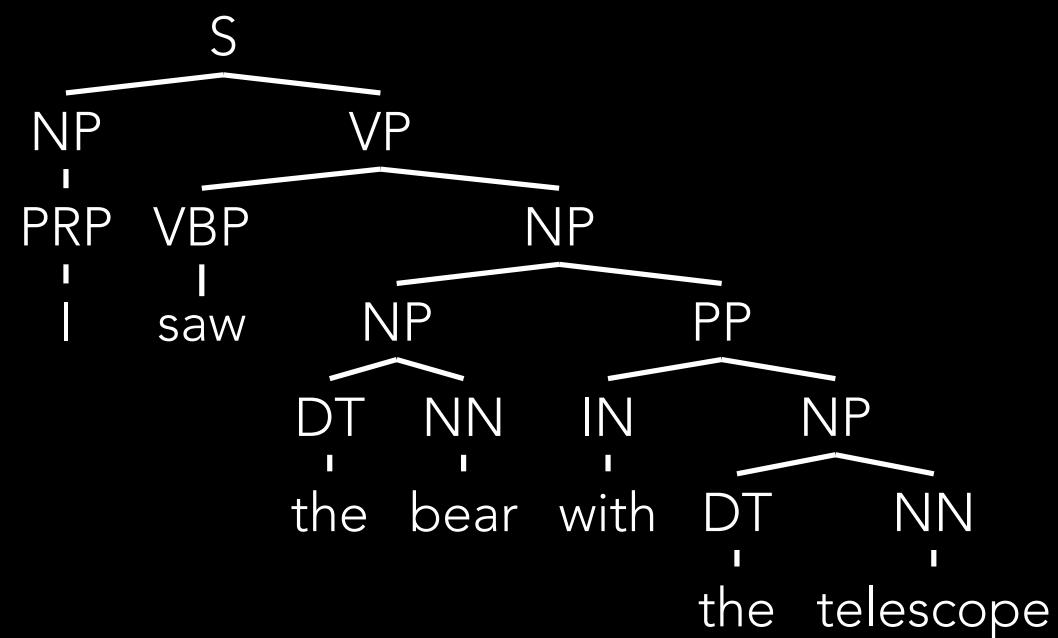
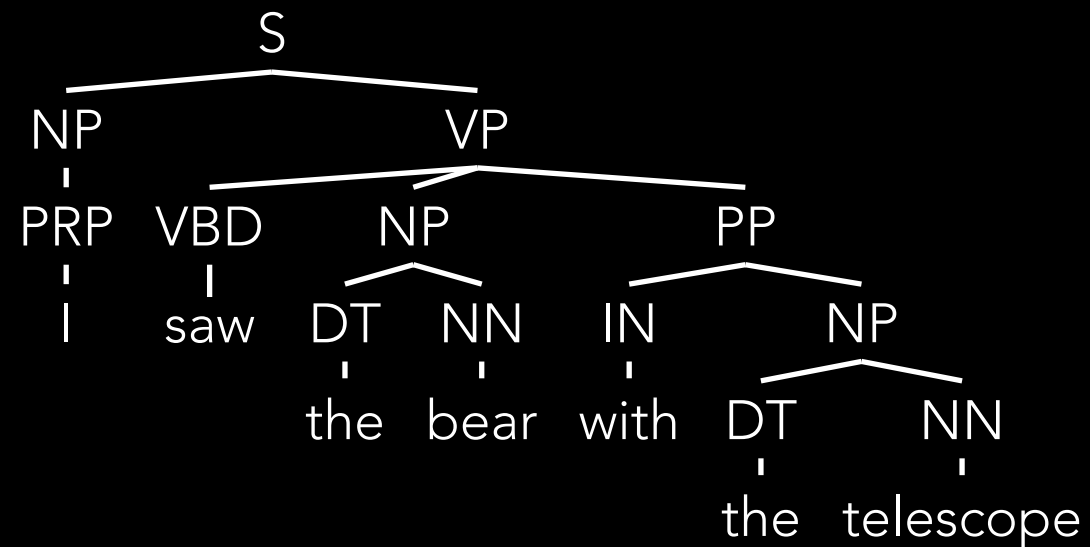
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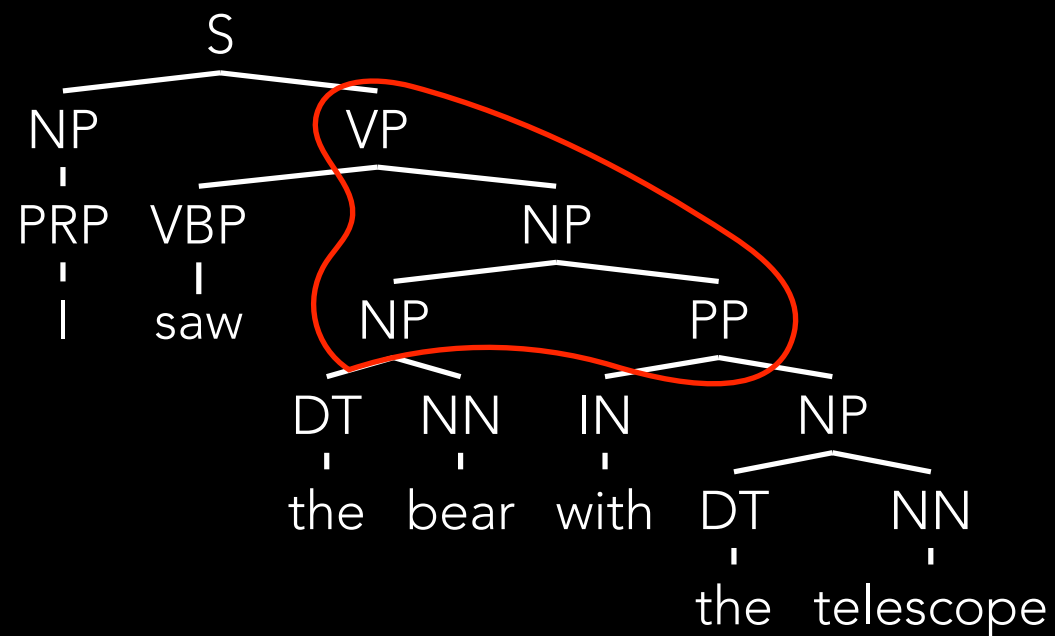
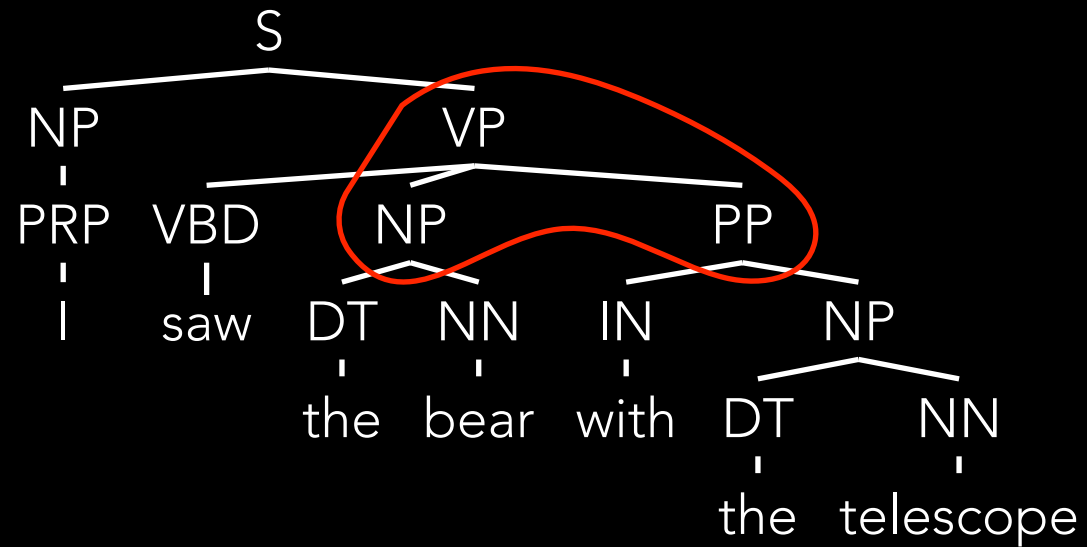
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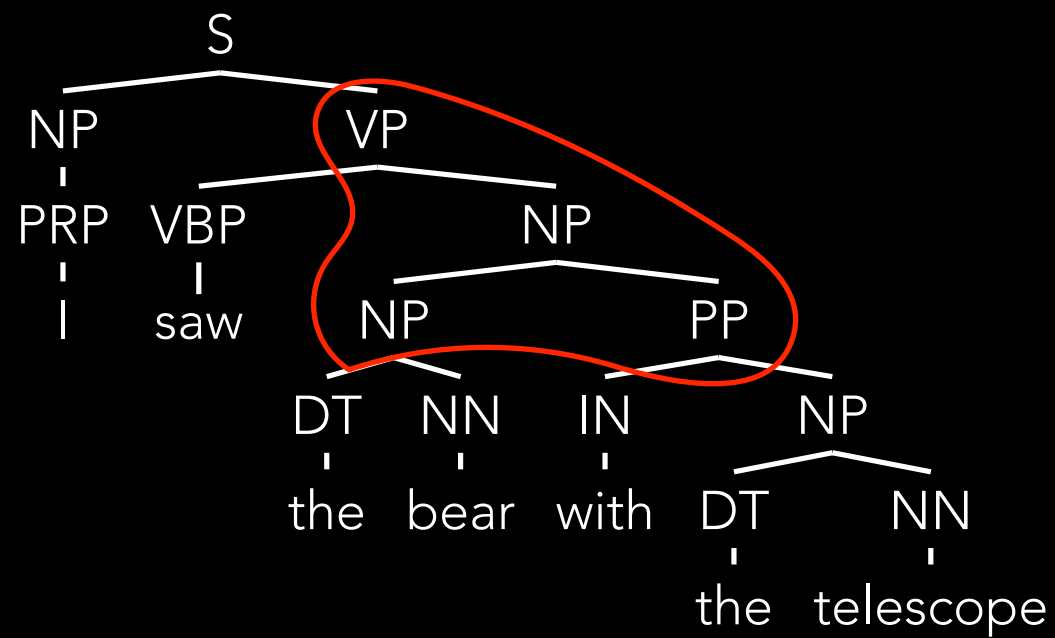
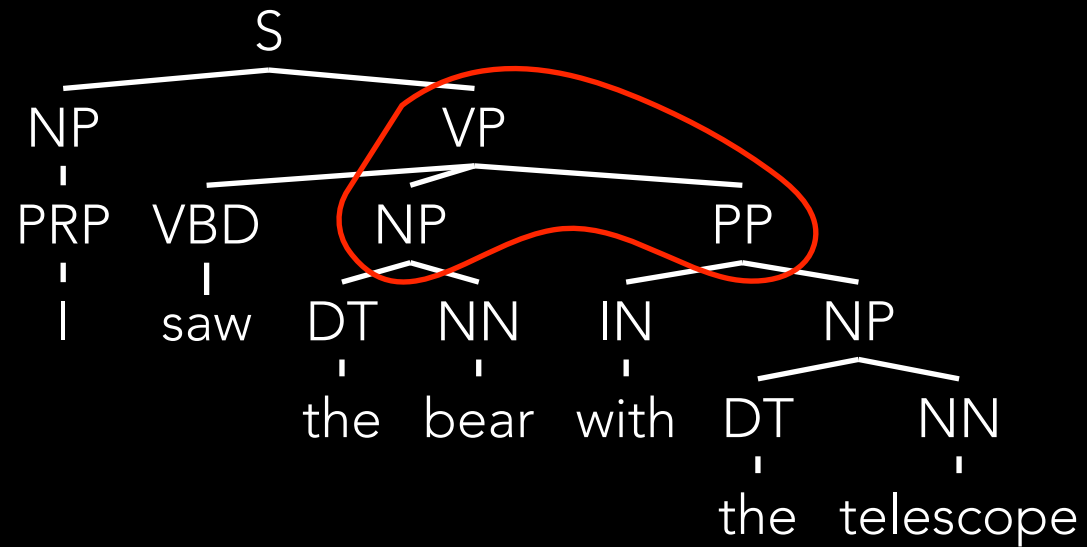
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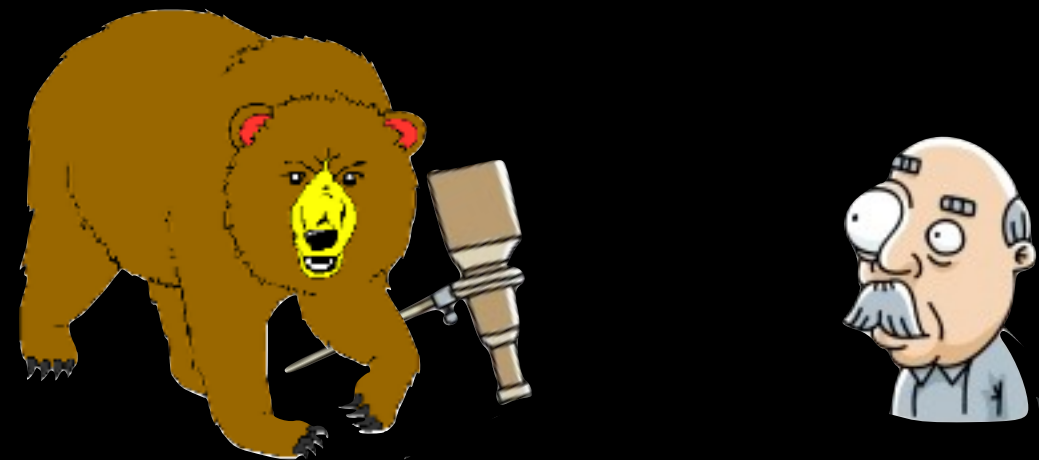
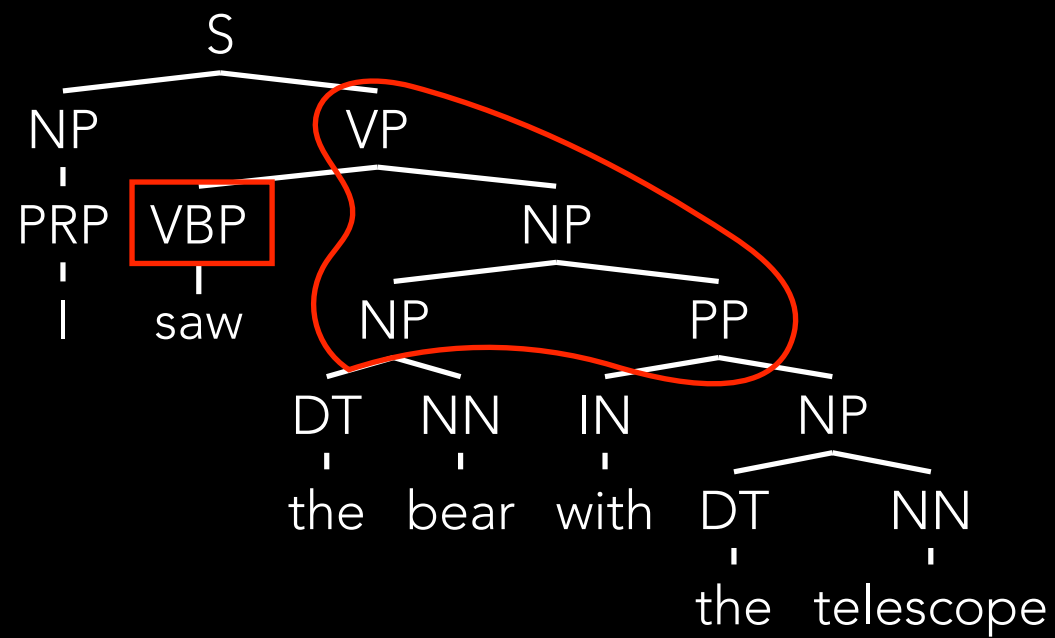
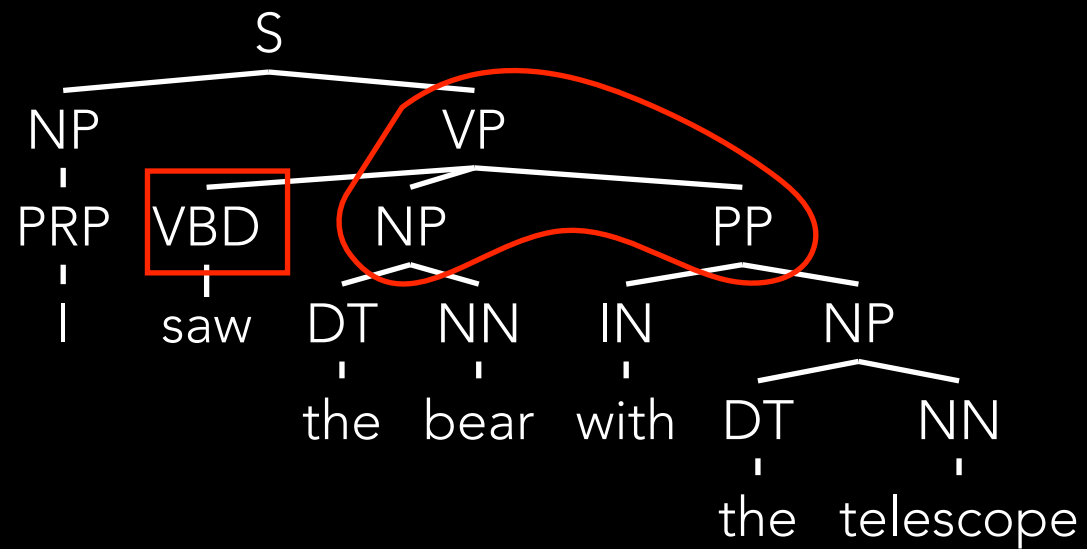
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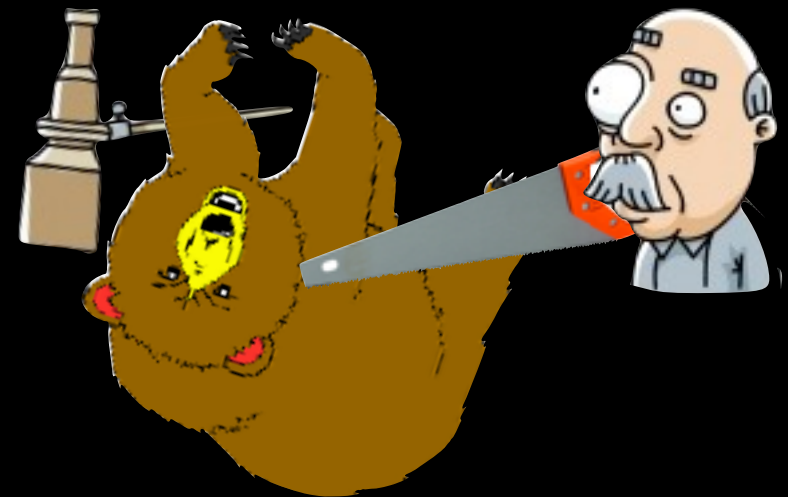
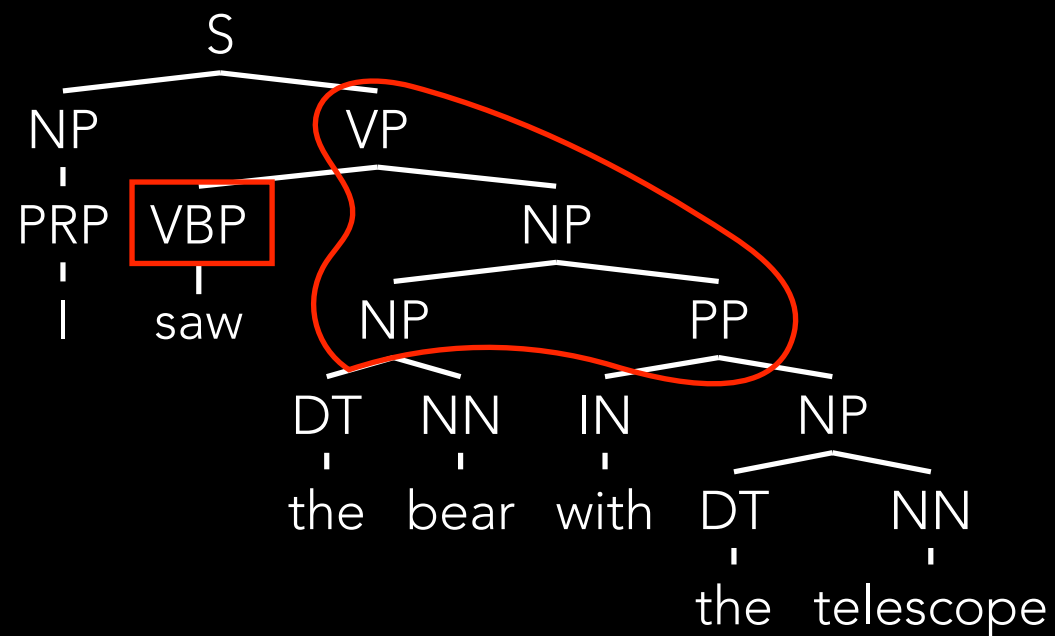
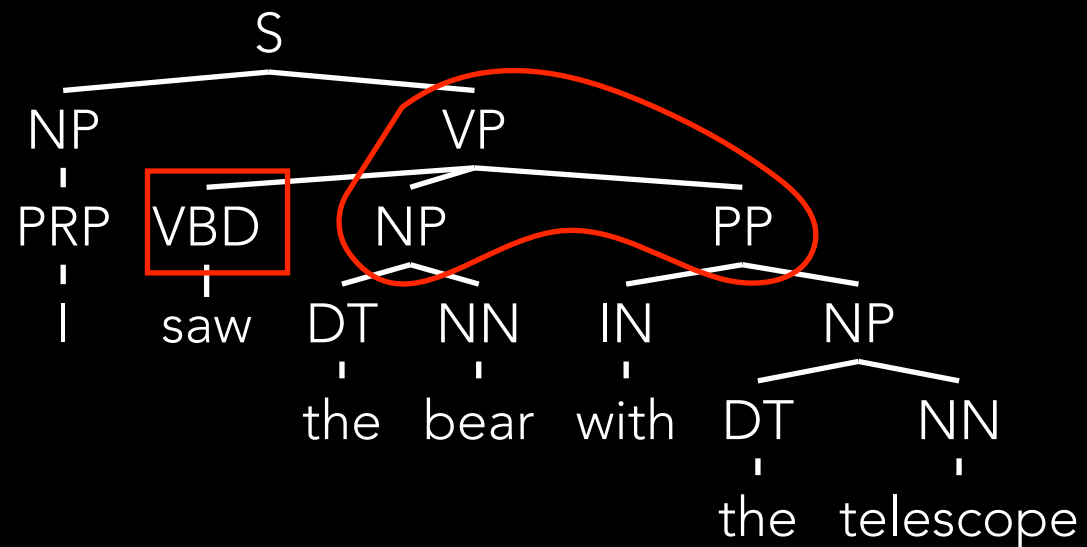
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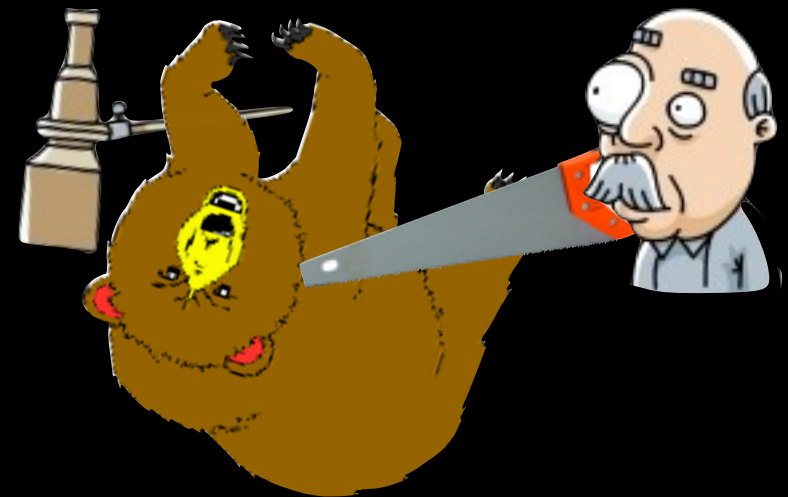
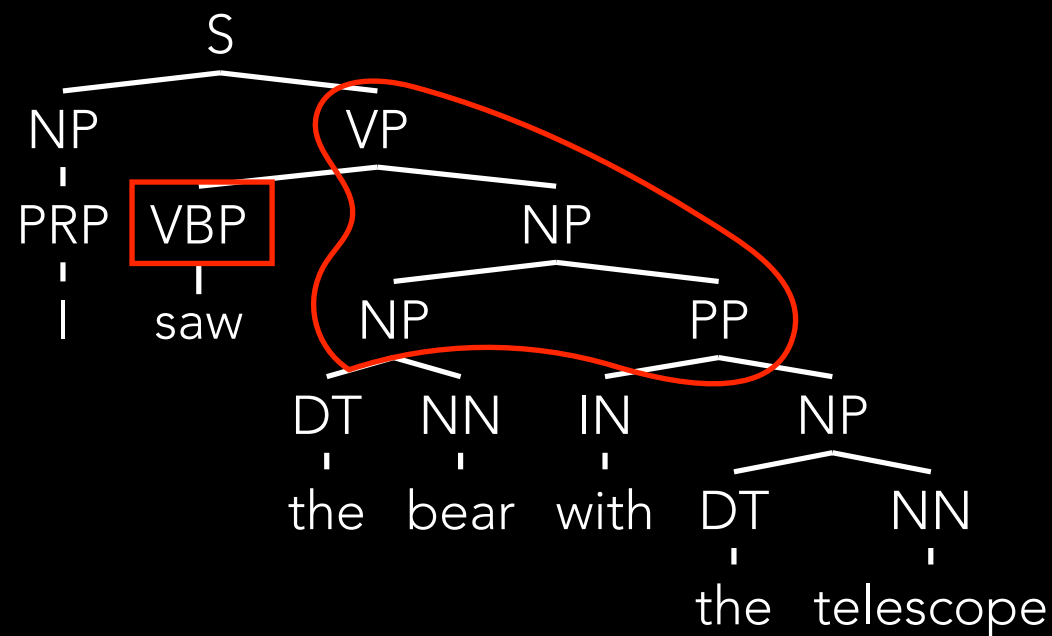
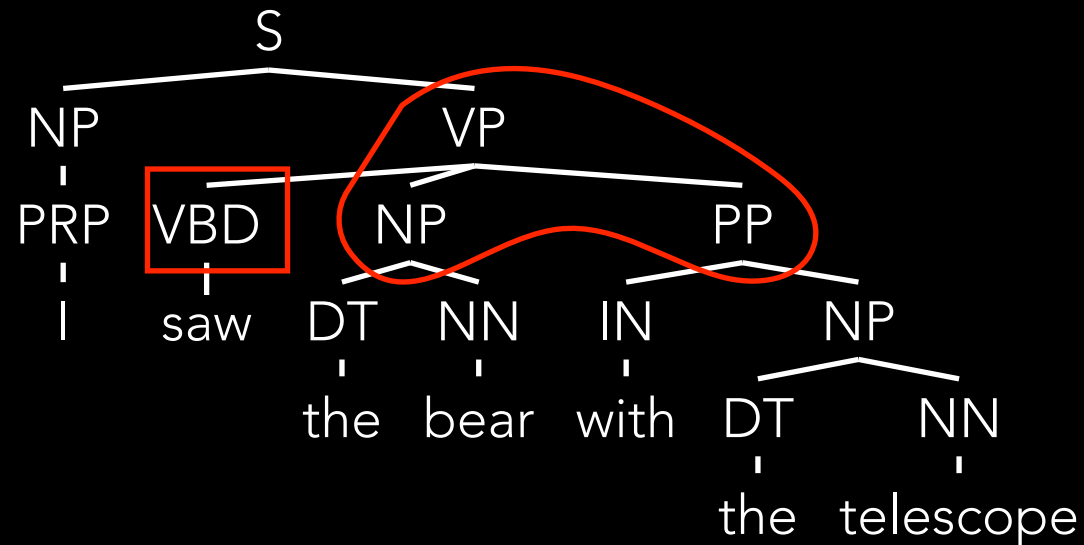
# Parser Evaluation



# Parser Evaluation



# Parser Evaluation



How do we quantify parse errors?



# Parser Evaluation

Parseval (Black et al. '91)

# Parser Evaluation

Parseval (Black et al. '91)

1. Decompose tree into labeled *constituent* spans  
(note: POS tags not considered!)

# Parser Evaluation

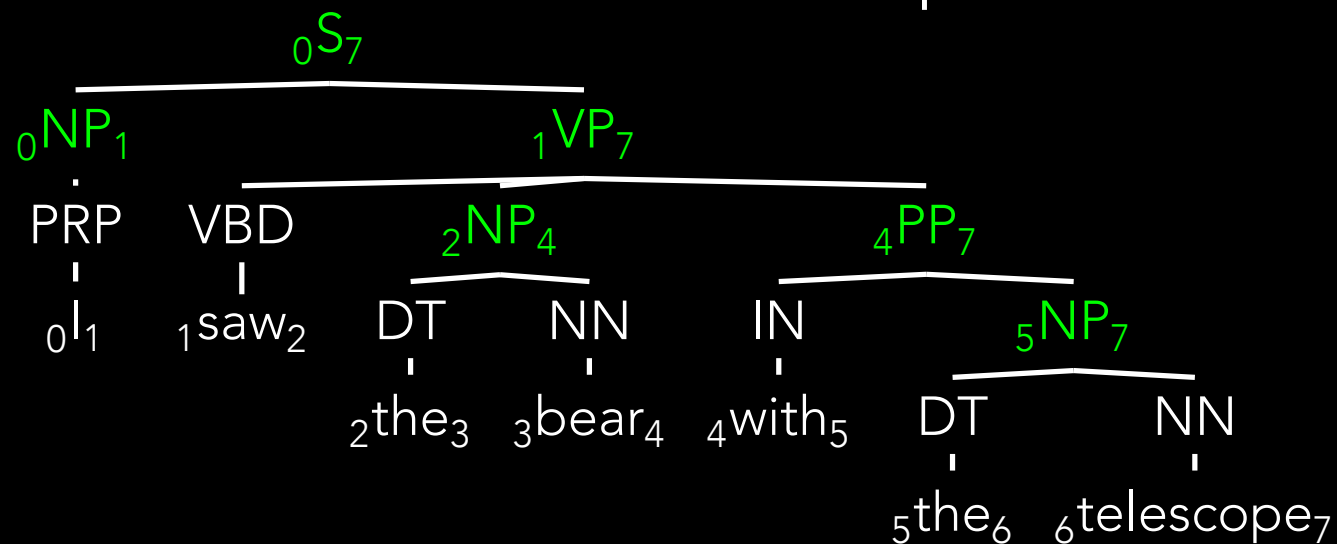
Parseval (Black et al. '91)

1. Decompose tree into labeled *constituent* spans  
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2. Calculate balanced precision and recall (f-measure)

# Parser Evaluation

Parseval (Black et al. '91)

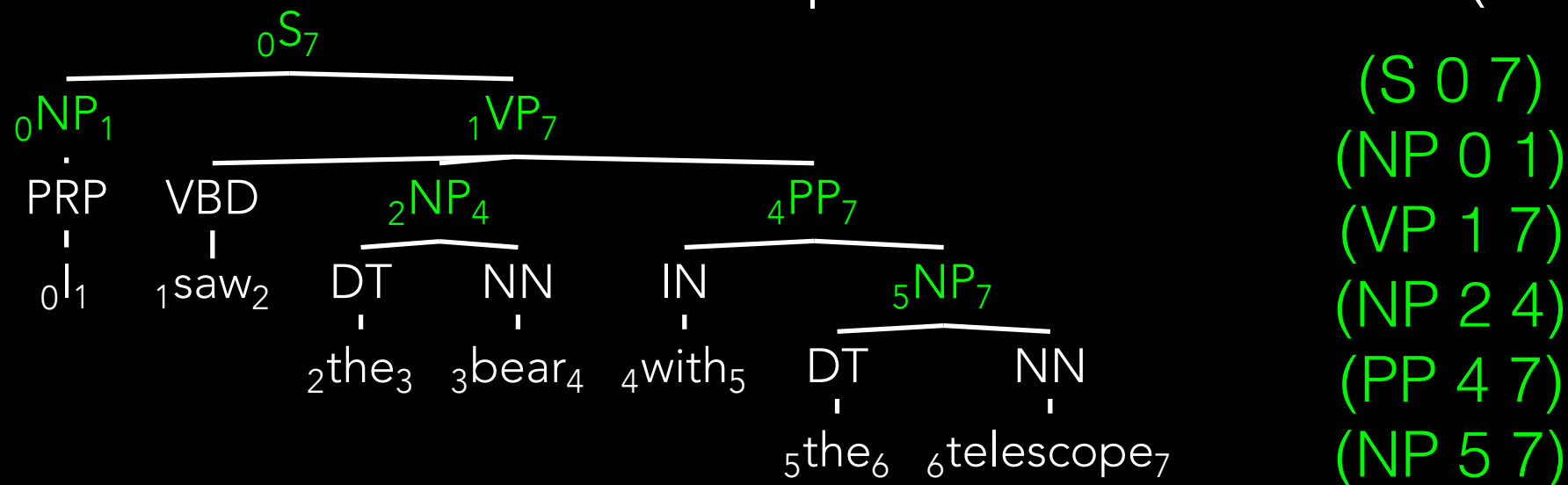
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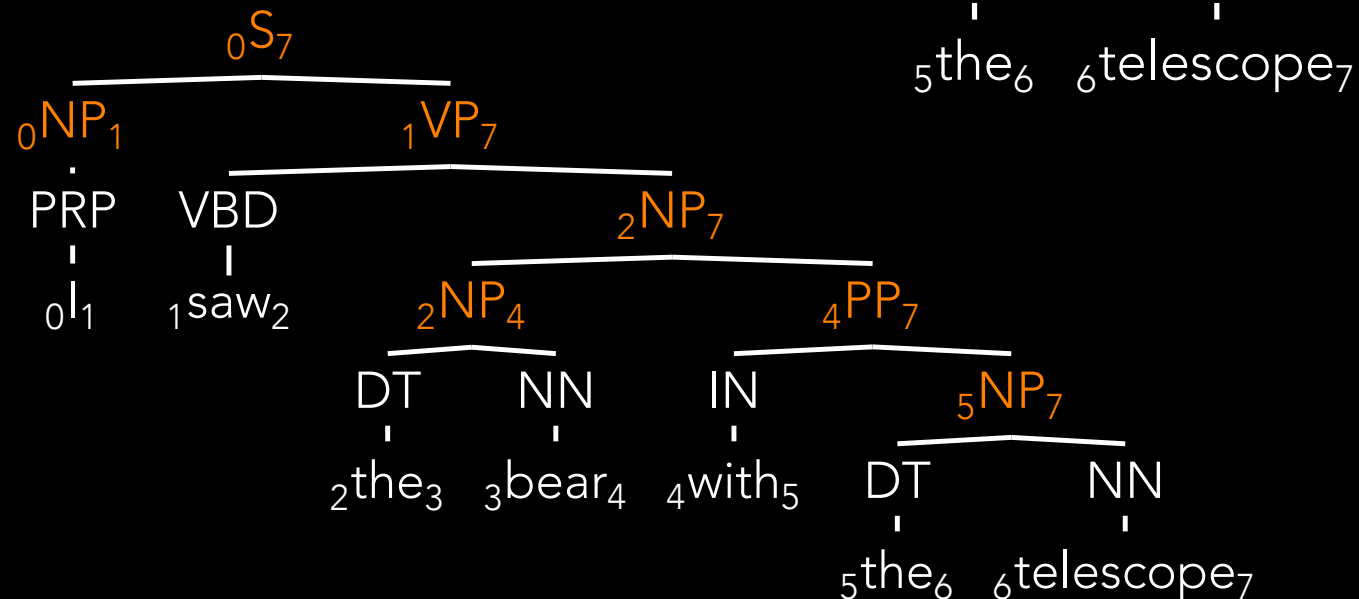
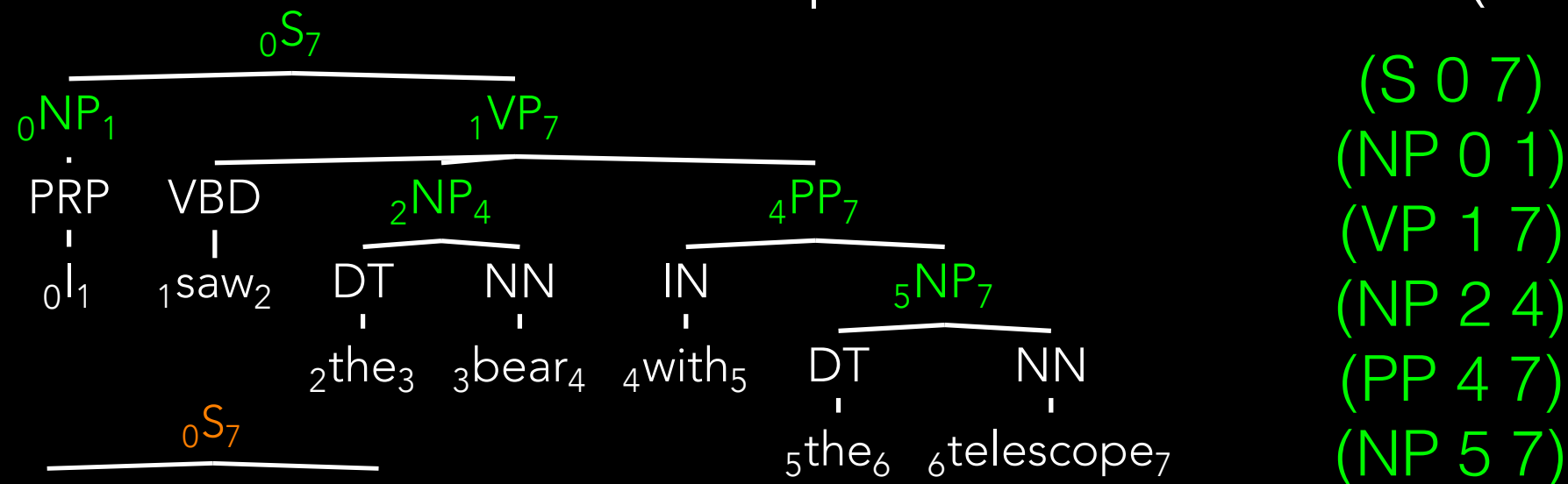
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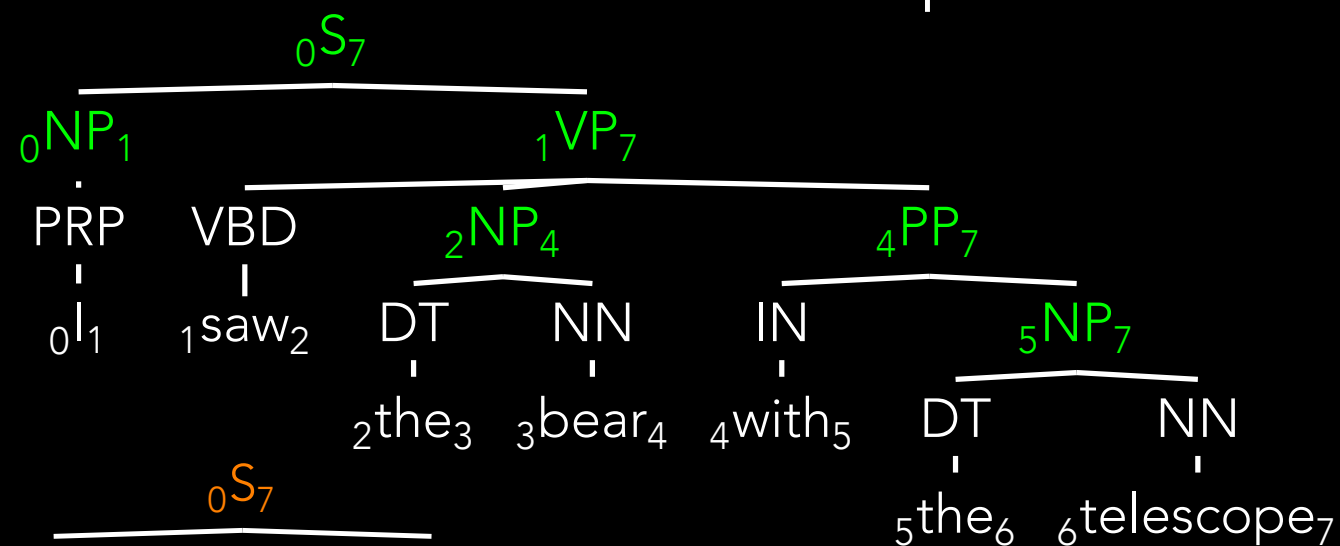
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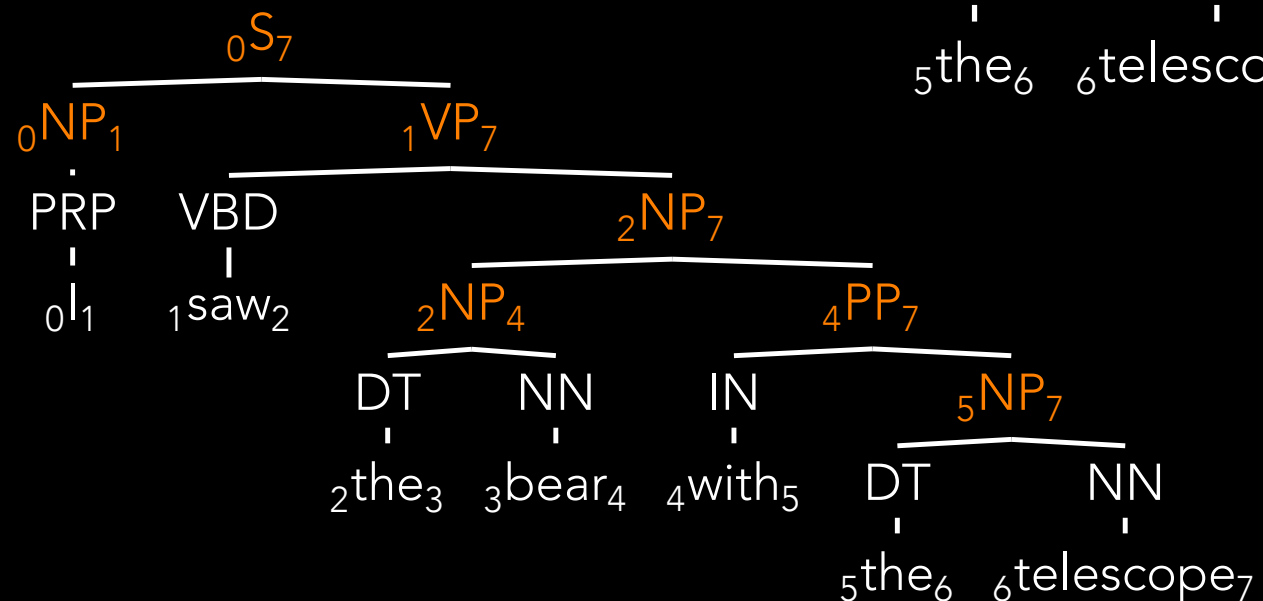
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Parseval (Black et al. '91)

1. Decompose tree into labeled *constituent* spans  
(note: POS tags not considered!)
2. Calculate balanced precision and recall (f-measure)



(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)



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(VP 1 7)  
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(NP 2 4)  
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(NP 5 7)

# Parser Evaluation

(S 0 7)  
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(VP 1 7)  
(NP 2 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

A = answers

C = correct

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# Parser Evaluation

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Precision: Of the answers I gave, what percent were correct?

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Precision: Of the answers I gave, what percent were correct?

$$\frac{|A \cap C|}{|A|}$$

# Parser Evaluation

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Recall: What percent of the correct answers did I give?

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# Parser Evaluation

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(NP 2 4)  
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Recall: What percent of the correct answers did I give?

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F1: Harmonic mean of Precision and Recall (reciprocal of mean of reciprocals)

# Parser Evaluation

(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

A = answers

C = correct

(S 0 7)  
(NP 0 1)  
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Precision: Of the answers I gave, what percent were correct?

$$\frac{|A \cap C|}{|A|}$$

Recall: What percent of the correct answers did I give?

$$\frac{|A \cap C|}{|C|}$$

F1: Harmonic mean of Precision and Recall (reciprocal of mean of reciprocals)

$$\frac{2|A \cap C|}{|C| + |A|}$$

# Parser Evaluation

A = answers

(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

$|A| = 7$

C = correct

(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

$|C| = 6$

# Parser Evaluation

A = answers

C = correct

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|A| = 7$

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|C| = 6$

$|A \cap C| = 6$



# Parser Evaluation

A = answers

C = correct

extra!

(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

$|A| = 7$

(S 0 7)  
(NP 0 1)  
(VP 1 7)  
(NP 2 4)  
(PP 4 7)  
(NP 5 7)

$|C| = 6$

$|A \cap C| = 6$

# Parser Evaluation

A = answers

C = correct

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

|A| = 7

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

|C| = 6

|A ∩ C| = 6

$$R = \frac{|A \cap C|}{|C|} = 1.0$$

# Parser Evaluation

A = answers

C = correct

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|A| = 7$

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|C| = 6$

$|A \cap C| = 6$

$$R = \frac{|A \cap C|}{|C|} = 1.0$$

$$P = \frac{|A \cap C|}{|A|} = .857$$

# Parser Evaluation

A = answers

C = correct

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|A| = 7$

(S 0 7)

(NP 0 1)

(VP 1 7)

(NP 2 4)

(PP 4 7)

(NP 5 7)

$|C| = 6$

$|A \cap C| = 6$

$$R = \frac{|A \cap C|}{|C|} = 1.0 \quad P = \frac{|A \cap C|}{|A|} = .857$$

$$F1 = \frac{2|A \cap C|}{|C| + |A|} = .923$$

# How to parse a sentence?

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- Input: word-separated sentence

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- Output: syntactic tree with POS tag/word labels

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- How you get there is up to you!



# How to parse a sentence?

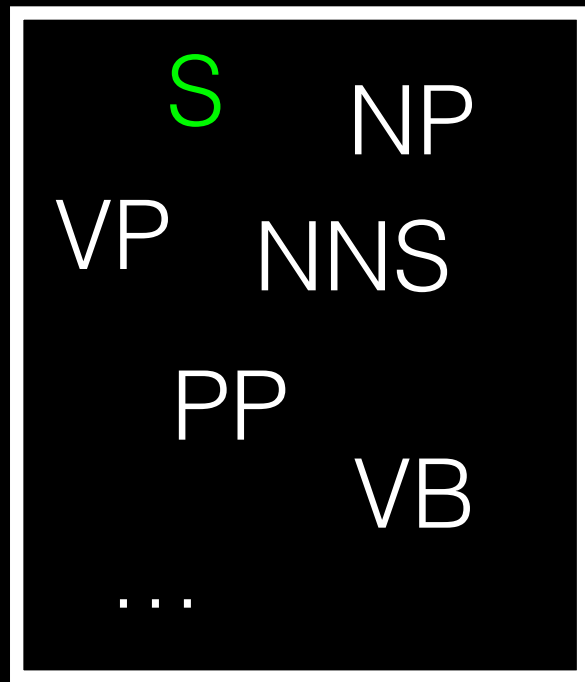
- Input: word-separated sentence
- Output: syntactic tree with POS tag/word labels
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- So far in this class we've used wFSAs and wFSTs. Can we keep using them?

# How to parse a sentence?

- Input: word-separated sentence
- Output: syntactic tree with POS tag/word labels
- How you get there is up to you!
- So far in this class we've used wFSAs and wFSTs. Can we keep using them?
- NO! (Why?)

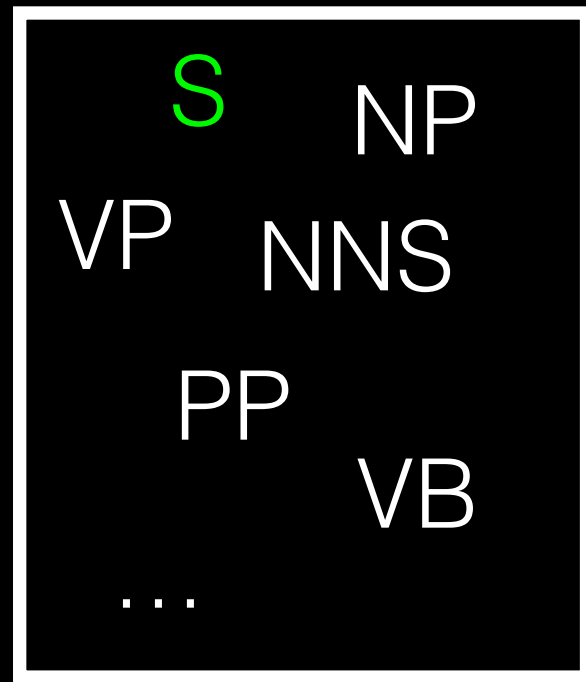
# Context-Free Grammars

# Context-Free Grammars



Nonterminals  
(start)

# Context-Free Grammars



Nonterminals  
(start)



Terminals

# Context-Free Grammars

$S$  NP  
VP NNS  
PP VB  
...

Nonterminals  
( $S$  start)

cats I  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$   
 $VP \rightarrow VB NP$   
 $NP \rightarrow NNS$   
 $NNS \rightarrow \text{cats}$   
 $NNS \rightarrow \text{mice}$   
 $VB \rightarrow \text{eat}$

Rules

# Context-Free Grammars

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Rules  
 $S$

Extend leftmost  
nonterminal  
by RHS of matching  
rule until done

# Context-Free Grammars

**S** NP  
VP NNS  
PP VB  
...

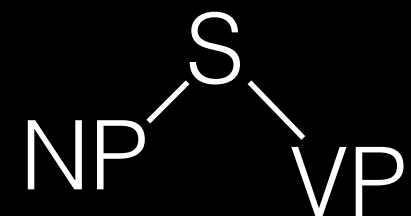
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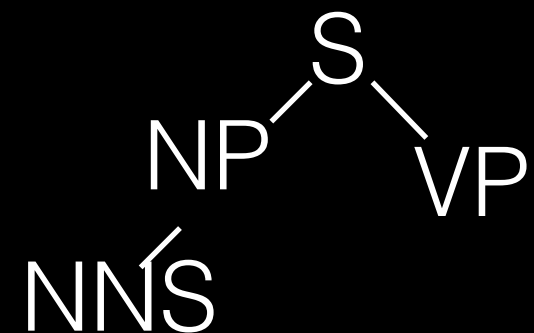
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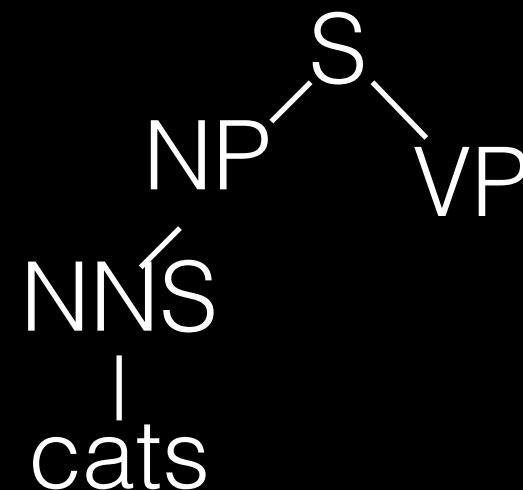
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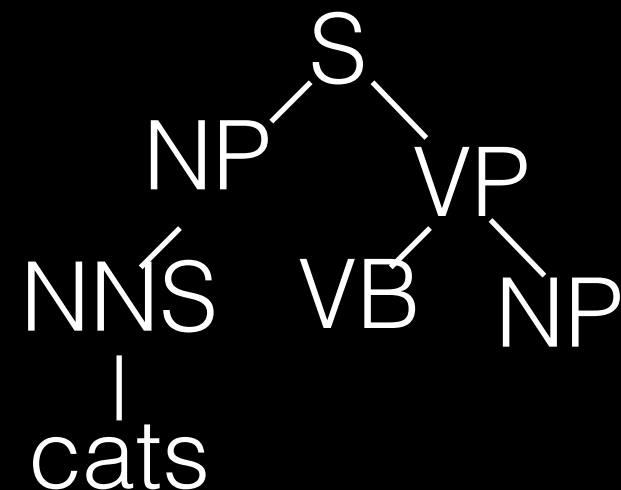
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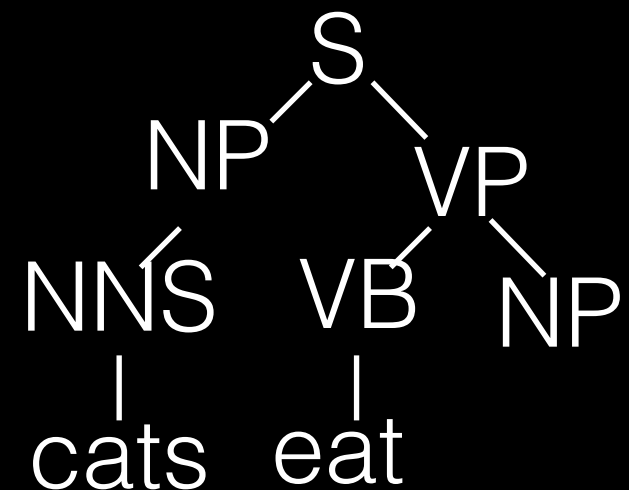
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...

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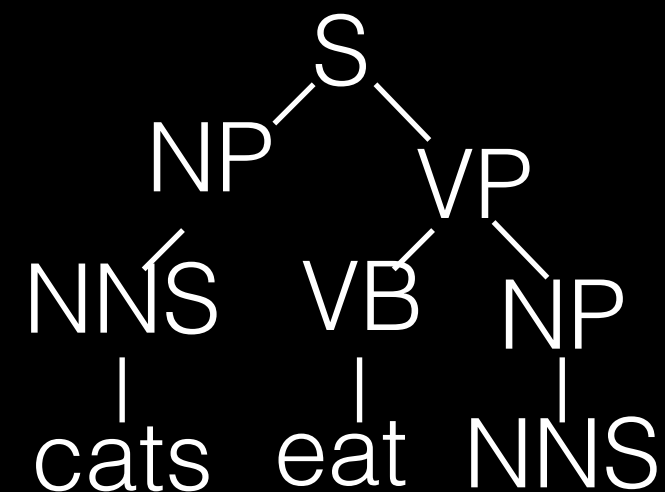
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...

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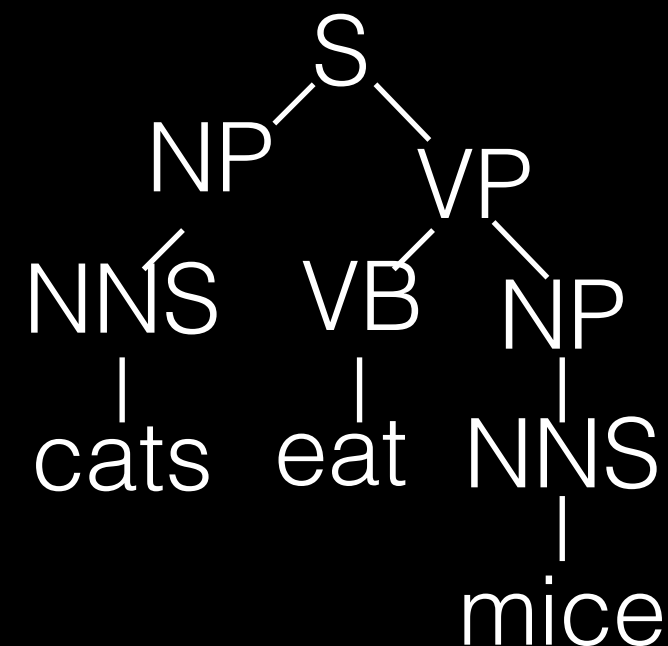
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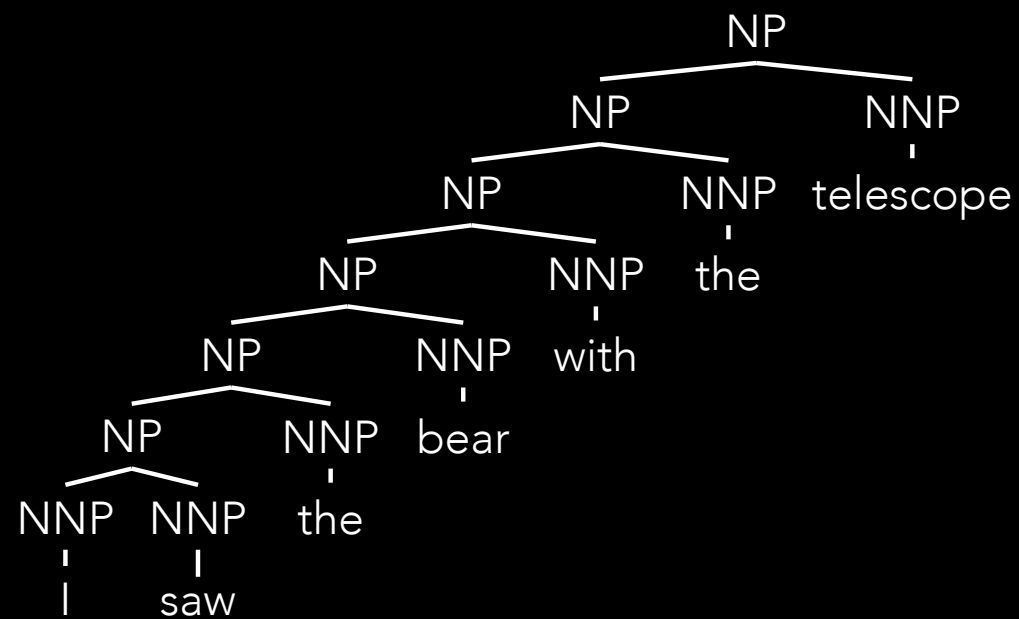


# Baseline Parser

Left-branching chain of NPs

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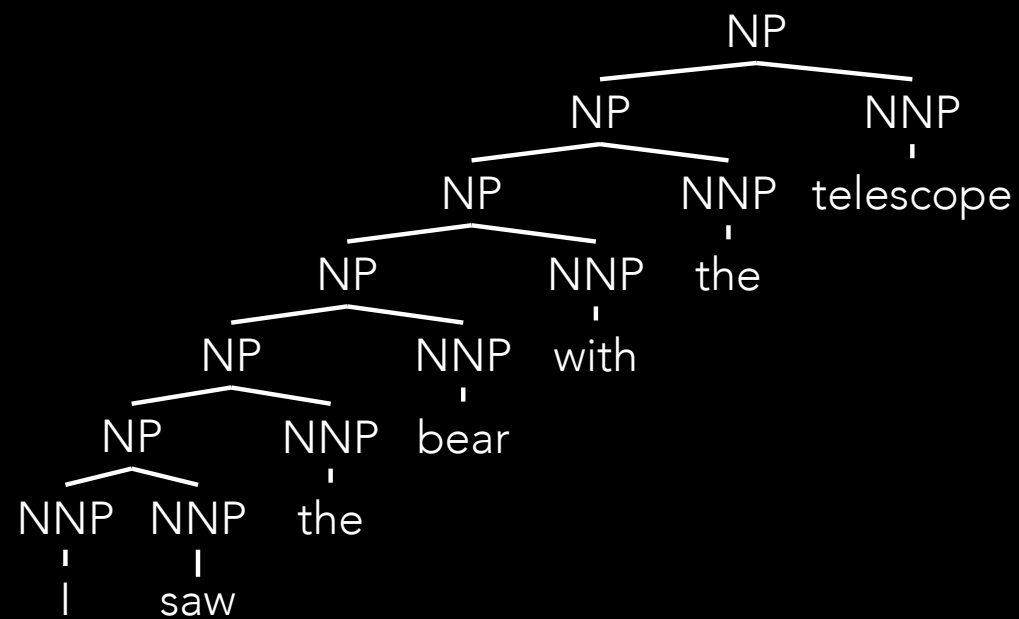
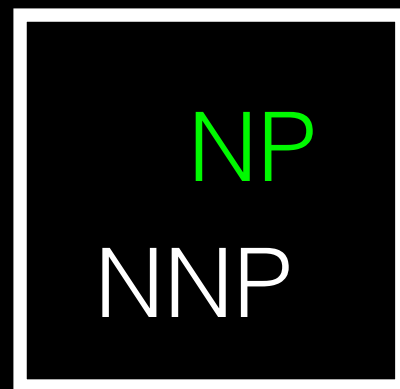
Left-branching chain of NPs





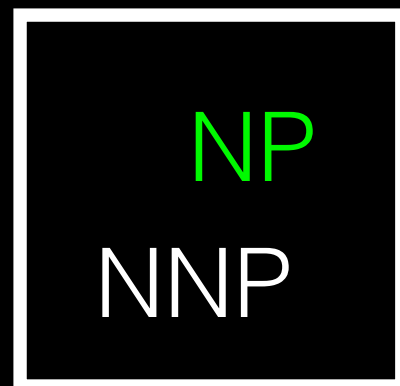
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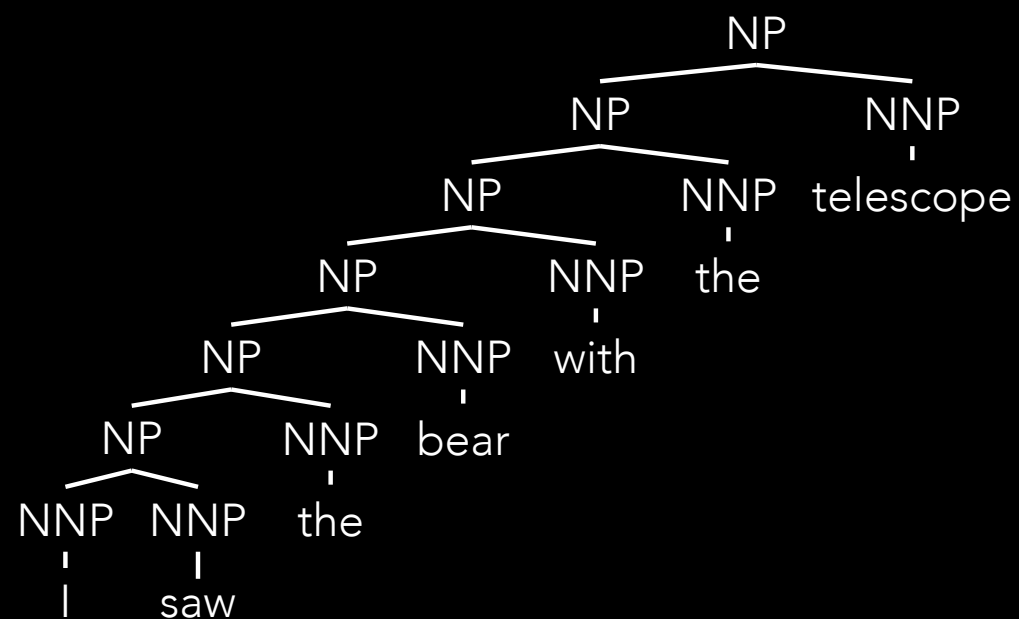


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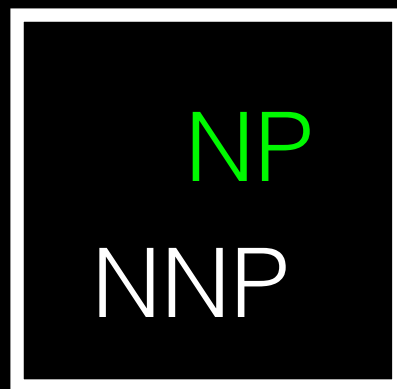


NP  $\rightarrow$  NP NNP  
NP  $\rightarrow$  NNP NNP  
NNP  $\rightarrow$  I/saw/the/...

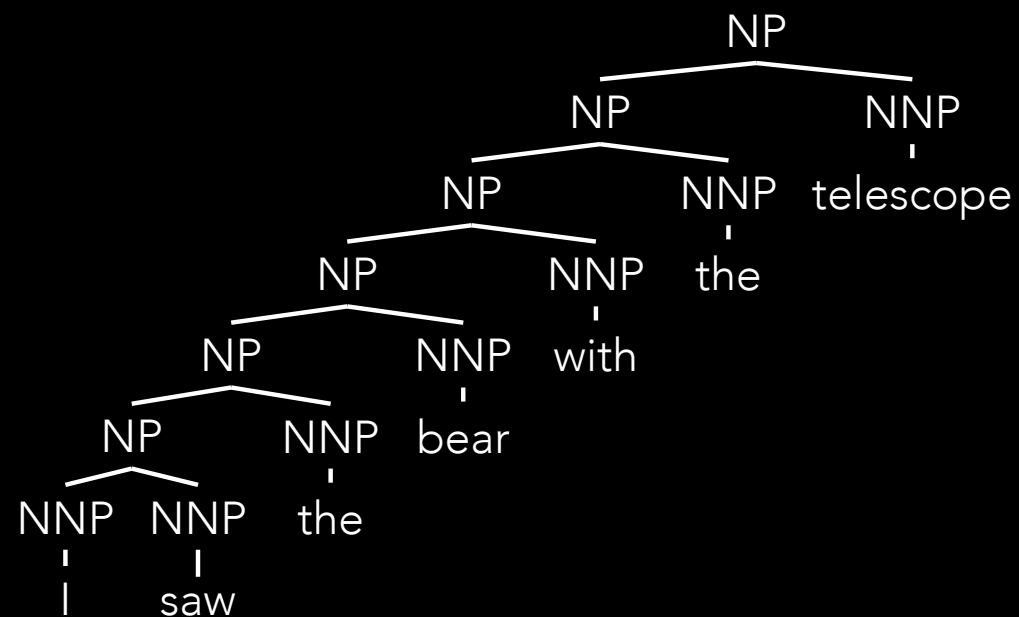


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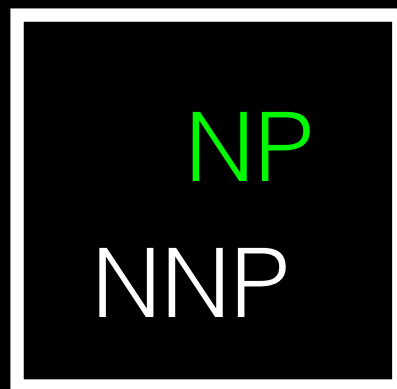
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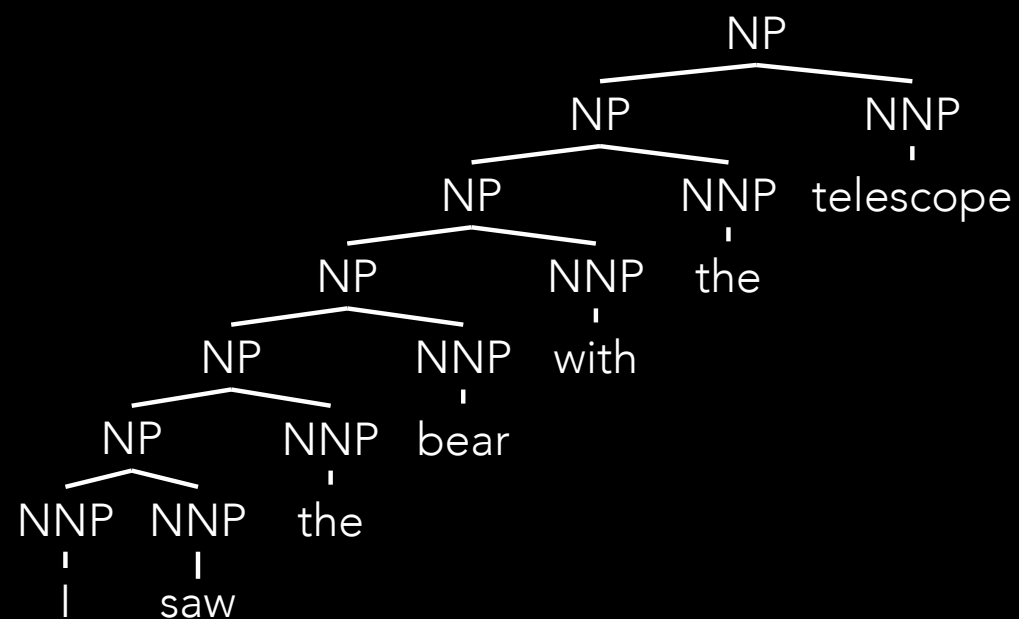
- Data-driven! (Most popular tag/constituent in PTB)

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Left-branching chain of NPs



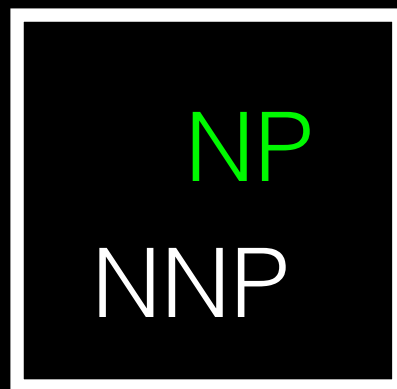
NP → NP NNP  
NP → NNP NNP  
NNP → I/saw/the/...



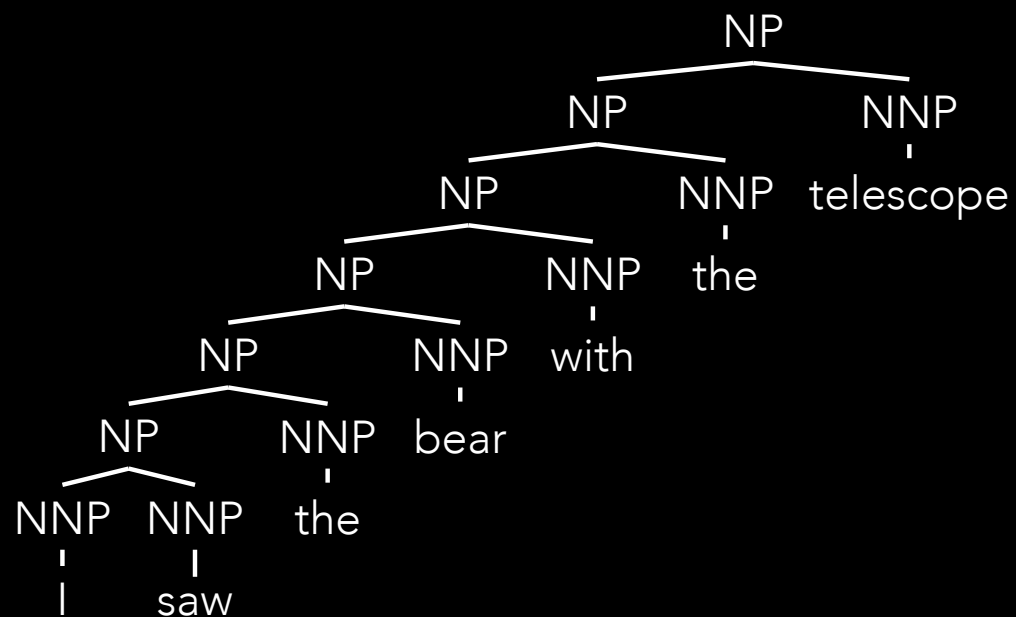
- Data-driven! (Most popular tag/constituent in PTB)
- Easy!

# Baseline Parser

Left-branching chain of NPs



NP → NP NNP  
NP → NNP NNP  
NNP → I/saw/the/...



- Data-driven! (Most popular tag/constituent in PTB)
- Easy!
- F1 of around 0.03

But how do you actually  
*parse*?

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$NP \rightarrow NP\ NNP$   
 $NP \rightarrow NNP\ NNP$   
 $NNP \rightarrow I \mid \text{ saw } \mid \text{ the } \mid \text{ bear }$

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I saw the bear

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NNP  $\rightarrow$  I | saw | the | bear

I saw the bear  
0 1 2 3

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- We're intersecting two languages, so we can use the *Bar-Hillel* construction: annotate the CFG rules with indices corresponding to the words in the string.

$NP \rightarrow NP\ NNP$   
 $NP \rightarrow NNP\ NNP$   
 $NNP \rightarrow I \mid \text{ saw } \mid \text{ the } \mid \text{ bear }$

I saw the bear  
0 1 2 3

$NNP_0 \rightarrow I$

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$NNP_0 \rightarrow I$   
 $NNP_1 \rightarrow \text{saw}$

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$$NP_{i:j} \rightarrow NP_{i:j-1}\ NNP_j$$

$NNP_0 \rightarrow I$	$NNP_2 \rightarrow \text{the}$
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0 1 2 3

$NP_{i\_j} \rightarrow NP_{i\_j-1}\ NNP_j$

$NP_{i\_j+1} \rightarrow NNP_i\ NNP_{i+1}$

$NNP_0 \rightarrow I$        $NNP_2 \rightarrow \text{the}$

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$$0 \leq i < j \leq 3$$

$NP \rightarrow NP \ NNP$   
 $NP \rightarrow NNP \ NNP$   
 $NNP \rightarrow I \mid \text{ saw } \mid \text{ the } \mid \text{ bear }$

I saw the bear  
0 1 2 3

$NP_{i_j} \rightarrow NP_{i_{j-1}} \ NNP_j$

$NP_{i_{j+1}} \rightarrow NNP_i \ NNP_{i+1}$

$NNP_0 \rightarrow I$        $NNP_2 \rightarrow \text{the}$

$NNP_1 \rightarrow \text{saw}$        $NNP_3 \rightarrow \text{bear}$

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 $NP \rightarrow NNP\ NNP$   
 $NNP \rightarrow I \mid \text{ saw } \mid \text{ the } \mid \text{ bear }$

I saw the bear  
0 1 2 3

$NP_{0..3}$   $0 \leq i < j \leq 3$

$NP_{i..j} \rightarrow NP_{i..j-1}\ NNP_j$

$NP_{i..j+1} \rightarrow NNP_i\ NNP_{i+1}$

$NNP_0 \rightarrow I$   $NNP_2 \rightarrow \text{the}$

$NNP_1 \rightarrow \text{saw}$   $NNP_3 \rightarrow \text{bear}$

# CKY Parsing

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$X \rightarrow YZ$   
nonterminal rule

$X \rightarrow x$   
terminal rule

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- Input: sentence of length  $n+1 = \langle w_0, w_1 \dots w_n \rangle$ ,  
CFG

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- Build states of the form  $[X, i, j] = \text{“I can cover from words } i \text{ through } j \text{ with at least one tree rooted in } X\text{”}$

# CKY Parsing

- Input: sentence of length  $n+1 = \langle w_0, w_1 \dots w_n \rangle$ , CFG
- Build states of the form  $[X, i, j]$  = “I can cover from words  $i$  through  $j$  with at least one tree rooted in  $X$ ”
- States contain backpointers of the form  $\{R, k\}$  = “To satisfy my state I will use  $R$  ( $X \rightarrow YZ$ ) and states  $[Y, i, k]$  and  $[Z, k, j]$ ”

# CKY Parsing

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- Initialize: build  $[X, i, i+1]$  for every lexical rule  $R = X \rightarrow w_i$ ; add backpointer  $\{R, ()\}$



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- If state is already built, just add backpointer
- Goal: build  $[X, 0, n+1]$  for start symbol  $X$

	time	flies	like	an	arrow
	[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP					
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time   fruit					
NP → NN NNS					
VP → VBP NP			[2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP				[3,4]	[3,5]
DT → a   an					
NN → time   fruit   arrow   banana					[4,5]
NNS → flies					
VBP → like					
IN → like					

time

flies

like

an

arrow

[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	[1,2]	[1,3]	[1,4]	[1,5]
		[2,3]	[2,4]	[2,5]
			[3,4]	[3,5]
				[4,5]



$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$NP \rightarrow \text{time} \mid \text{fruit}$

$NP \rightarrow NN NNS$

$VP \rightarrow VBP NP$

$VP \rightarrow \text{flies}$

$VP \rightarrow VP PP$

$PP \rightarrow IN NP$

$DT \rightarrow a \mid an$

$NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$

$NNS \rightarrow \text{flies}$

$VBP \rightarrow \text{like}$

$IN \rightarrow \text{like}$

time

flies

like

an

arrow

[0,1]

[0,2]

[0,3]

[0,4]

[0,5]

 $S \rightarrow NP VP$  $NP \rightarrow DT NN$  $NP \rightarrow \text{time} \mid \text{fruit}$  $NP \rightarrow NN NNS$  $VP \rightarrow VBP NP$  $VP \rightarrow \text{flies}$  $VP \rightarrow VP PP$  $PP \rightarrow IN NP$  $DT \rightarrow a \mid an$  $NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$  $NNS \rightarrow \text{flies}$  $VBP \rightarrow \text{like}$  $IN \rightarrow \text{like}$ 

[1,2]

[1,3]

[1,4]

[1,5]

[2,3]

[2,4]

[2,5]

[3,4]

[3,5]

[4,5]

Length 2

time

flies

like

an

arrow

[0,1]

[0,2]

[0,3]

[0,4]

[0,5]

 $S \rightarrow NP VP$  $NP \rightarrow DT NN$ 

[1,2]

[1,3]

[1,4]

[1,5]

 $NP \rightarrow \text{time} \mid \text{fruit}$  $NP \rightarrow NN NNS$  $VP \rightarrow VBP NP$ 

[2,3]

[2,4]

[2,5]

 $VP \rightarrow \text{flies}$  $VP \rightarrow VP PP$  $PP \rightarrow IN NP$  $DT \rightarrow a \mid an$  $NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$ 

[4,5]

 $NNS \rightarrow \text{flies}$  $VBP \rightarrow \text{like}$  $IN \rightarrow \text{like}$ 

Length 3





	time	flies	like	an	arrow
	[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP					
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time   fruit					
NP → NN NNS					
VP → VBP NP			[2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP				[3,4]	[3,5]
DT → a   an					
NN → time   fruit   arrow   banana					[4,5]
NNS → flies					
VBP → like					
IN → like					



	time	flies	like	an	arrow
	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP					
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time   fruit					
NP → NN NNS					
VP → VBP NP		[2,3]	[2,4]	[2,5]	
VP → flies					
VP → VP PP				[3,4]	[3,5]
PP → IN NP					
DT → a   an					
NN → time   fruit   arrow   banana					[4,5]

NNS → flies

VBP → like

IN → like

Seed length-1 cells  
with lexical coverage

	time	flies	like	an	arrow
	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			[2,3]	[2,4]	[2,5]
				[3,4]	[3,5]
					[4,5]

- S → NP VP
- NP → DT NN
- NP → time | fruit
- NP → NN NNS
- VP → VBP NP
- VP → flies
- VP → VP PP
- PP → IN NP
- DT → a | an
- NN → time | fruit | arrow | banana
- NNS → flies
- VBP → like
- IN → like

Seed length-1 cells  
with lexical coverage

	time	flies	like	an	arrow
<p> <math>S \rightarrow NP\ VP</math>  <math>NP \rightarrow DT\ NN</math>  <math>NP \rightarrow time \mid fruit</math>  <math>NP \rightarrow NN\ NNS</math>  <math>VP \rightarrow VBP\ NP</math>  <math>VP \rightarrow flies</math>  <math>VP \rightarrow VP\ PP</math>  <math>PP \rightarrow IN\ NP</math>  <math>DT \rightarrow a \mid an</math>  <math>NN \rightarrow time \mid fruit \mid arrow \mid banana</math>  <math>NNS \rightarrow flies</math> </p>	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	VP NNS [1,2]	[1,3]	[1,4]	[1,5]	
			IN VBP [2,3]	[2,4]	[2,5]
				[3,4]	[3,5]
					[4,5]

- $VBP \rightarrow like$
- $IN \rightarrow like$

Seed length-1 cells  
with lexical coverage



	time	flies	like	an	arrow
S → NP VP NP → DT NN NP → time   fruit NP → NN NNS VP → VBP NP VP → flies VP → VP PP PP → IN NP DT → a   an NN → time   fruit   <span style="border: 2px solid red;">arrow</span>   banana NNS → flies VBP → like IN → like	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	VP NNS [1,2]	[1,3]	[1,4]	[1,5]	
		IN VBP [2,3]	[2,4]	[2,5]	
			DT [3,4]	[3,5]	
				NN [4,5]	
Seed length-1 cells with lexical coverage					

	time	flies	like	an	arrow
	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NN [4,5]

- S → NP VP
- NP → DT NN
- NP → time | fruit
- NP → NN NNS
- VP → VBP NP
- VP → flies
- VP → VP PP
- PP → IN NP
- DT → a | an
- NN → time | fruit | arrow | banana
- NNS → flies
- VBP → like
- IN → like

Now check length-2 spans.  
Match rules to subspans

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NN [4,5]

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$NP \rightarrow \text{time} \mid \text{fruit}$

$NP \rightarrow NN NNS$

$VP \rightarrow VBP NP$

$VP \rightarrow \text{flies}$

$VP \rightarrow VP PP$

$PP \rightarrow IN NP$

$DT \rightarrow a \mid an$

$NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$

$NNS \rightarrow \text{flies}$

$VBP \rightarrow \text{like}$

$IN \rightarrow \text{like}$

Two new states!



	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NN [4,5]

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$NP \rightarrow \text{time} \mid \text{fruit}$

$NP \rightarrow NN NNS$

$VP \rightarrow VBP NP$

$VP \rightarrow \text{flies}$

$VP \rightarrow VP PP$

$PP \rightarrow IN NP$

$DT \rightarrow a \mid an$

$NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$

$NNS \rightarrow \text{flies}$

$VBP \rightarrow \text{like}$

$IN \rightarrow \text{like}$

Annotate with backpointer

for future reconstruction (not part of state)

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NN [4,5]

- S → NP VP
- NP → DT NN
- NP → time | fruit
- NP → NN NNS
- VP → VBP NP
- VP → flies
- VP → VP PP
- PP → IN NP
- DT → a | an
- NN → time | fruit | arrow | banana
- NNS → flies
- VBP → like
- IN → like

No matching rule



	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → DT NN					
NP → time   fruit					
NP → NN NNS					
VP → VBP NP			IN VBP [2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP					
DT → a   an					
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					

New state!

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

- S → NP VP
- NP → DT NN
- NP → time | fruit
- NP → NN NNS
- VP → VBP NP
- VP → flies
- VP → VP PP
- PP → IN NP
- DT → a | an
- NN → time | fruit | arrow | banana
- NNS → flies
- VBP → like
- IN → like

Check every split point for rule

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → DT NN					
NP → time   fruit					
NP → NN NNS					
VP → VBP NP					
VP → flies					
VP → VP PP					
PP → IN NP					
DT → a   an					
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					

Empty cell

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → DT NN					
NP → time   fruit					
NP → NN NNS					
VP → VBP NP			IN VBP [2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP				DT [3,4]	NP [3,5]
DT → a   an					NN [4,5]
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					
			No matching rule		

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN NP → time   fruit NP → NN NNS VP → VBP NP VP → flies VP → VP PP PP → IN NP DT → a   an NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

(Skipping)



	time	flies	like	an	arrow
<p> <math>S \rightarrow NP VP</math>  <math>NP \rightarrow DT NN</math>  <math>NP \rightarrow time \mid fruit</math>  <math>NP \rightarrow NN NNS</math>  <math>VP \rightarrow VBP NP</math>  <math>VP \rightarrow flies</math>  <math>VP \rightarrow VP PP</math>  <math>PP \rightarrow IN NP</math>  <math>DT \rightarrow a \mid an</math>  <math>NN \rightarrow time \mid fruit \mid arrow \mid banana</math>  <math>NNS \rightarrow flies</math>  <math>VBP \rightarrow like</math>  <math>IN \rightarrow like</math> </p>	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

Two new states!

	time	flies	like	an	arrow
<div> <div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → time   fruit</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div> </div>	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]
Empty cell					

	time	flies	like	an	arrow
<div> <div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → time   fruit</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div> </div>	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]
(Skipping)					

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

- S → NP VP
- NP → DT NN
- NP → time | fruit
- NP → NN NNS
- VP → VBP NP
- VP → flies
- VP → VP PP
- PP → IN NP
- DT → a | an
- NN → time | fruit | arrow | banana
- NNS → flies
- VBP → like
- IN → like

New state!

	time	flies	like	an	arrow
	<div>NP</div> <div>NN</div> <div>[0,1]</div>	<div>S</div> <div>NP</div> <div>[0,2]</div>	<div></div> <div>[0,3]</div>	<div></div> <div>[0,4]</div>	<div></div> <div>[0,5]</div>
<div>S → NP VP</div>		<div>VP</div> <div>NNS</div> <div>[1,2]</div>	<div></div> <div>[1,3]</div>	<div></div> <div>[1,4]</div>	<div>VP</div> <div>[1,5]</div>
<div>NP → DT NN</div>			<div></div> <div>[2,3]</div>	<div></div> <div>[2,4]</div>	<div></div> <div>[2,5]</div>
<div>NP → time   fruit</div>			<div>IN</div> <div>VBP</div>		<div>PP</div> <div>VP</div>
<div>NP → NN NNS</div>					
<div>VP → VBP NP</div>					
<div>VP → flies</div>					
<div>VP → VP PP</div>				<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>[3,5]</div>
<div>PP → IN NP</div>					
<div>DT → a   an</div>					<div>NN</div> <div>[4,5]</div>
<div>NN → time   fruit   arrow   banana</div>					
<div>NNS → flies</div>					
<div>VBP → like</div>					
<div>IN → like</div>					

Empty Cell

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → DT NN					
NP → time   fruit			IN VBP [2,3]	[2,4]	[2,5]
NP → NN NNS					
VP → VBP NP					
VP → flies					
VP → VP PP				DT [3,4]	NP [3,5]
PP → IN NP					
DT → a   an					NN [4,5]
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					
			Empty Cell		

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
		VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$NP \rightarrow \text{time} \mid \text{fruit}$

$NP \rightarrow NN NNS$

$VP \rightarrow VBP NP$

$VP \rightarrow \text{flies}$

$VP \rightarrow VP PP$

$PP \rightarrow IN NP$

$DT \rightarrow a \mid an$

$NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$

$NNS \rightarrow \text{flies}$

$VBP \rightarrow \text{like}$

$IN \rightarrow \text{like}$

New state!

	time	flies	like	an	arrow
	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
		VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]

S → NP VP

NP → DT NN

NP → time | fruit

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

Alternate (no new state)



	time	flies	like	an	arrow
<div> <div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → time   fruit</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div> </div>	NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
		VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
			IN VBP [2,3]	[2,4]	PP VP [2,5]
				DT [3,4]	NP [3,5]
					NN [4,5]
Empty Cell					

	time	flies	like	an	arrow
<div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → time   fruit</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div>	<div>NP</div> <div>NN</div> <div>[0,1]</div>	<div>S</div> <div>NP</div> <div>[0,2]</div>	<div></div> <div>[0,3]</div>	<div></div> <div>[0,4]</div>	<div>S</div> <div></div> <div>[0,5]</div>
		<div>VP</div> <div>NNS</div> <div>[1,2]</div>	<div></div> <div>[1,3]</div>	<div></div> <div>[1,4]</div>	<div>VP</div> <div></div> <div>[1,5]</div>
			<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div></div> <div>[2,4]</div>	<div>PP</div> <div>VP</div> <div>[2,5]</div>
				<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>[3,5]</div>
					<div>NN</div> <div>[4,5]</div>

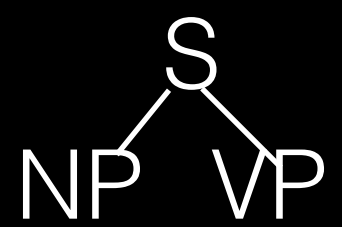
Empty Cell

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]

Start at top of the chart  
Follow backpointers  
to build tree

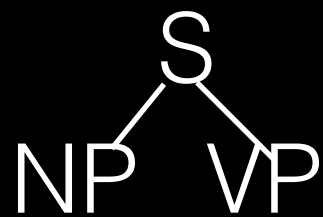
time	flies	like	an	arrow
<div>NP</div> <div>NN</div> <div>[0,1]</div>	<div>S</div> <div>NP</div> <div>[0,2]</div>	<div>[0,3]</div>	<div>[0,4]</div>	<div>S</div> <div>[0,5]</div>
<div>S</div>	<div>VP</div> <div>NNS</div> <div>[1,2]</div>	<div>[1,3]</div>	<div>[1,4]</div>	<div>VP</div> <div>[1,5]</div>
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div>[2,4]</div>	<div>PP</div> <div>VP</div> <div>[2,5]</div>
			<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>[3,5]</div>
				<div>NN</div> <div>[4,5]</div>

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



Backpointer: S → NP VP ,1

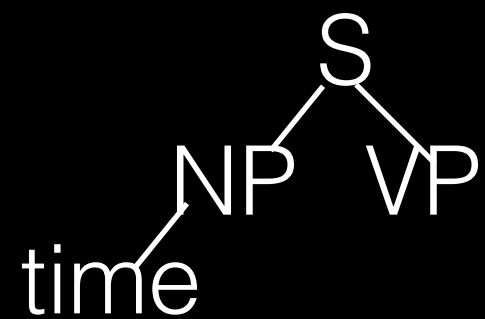
time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



(could have used  $S \rightarrow NP VP$  ,2  
to generate the other tree)

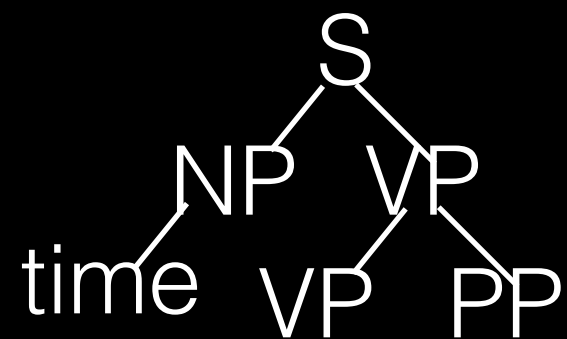
Backpointer:  $S \rightarrow NP VP$  ,1

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



Backpointer: NP → time

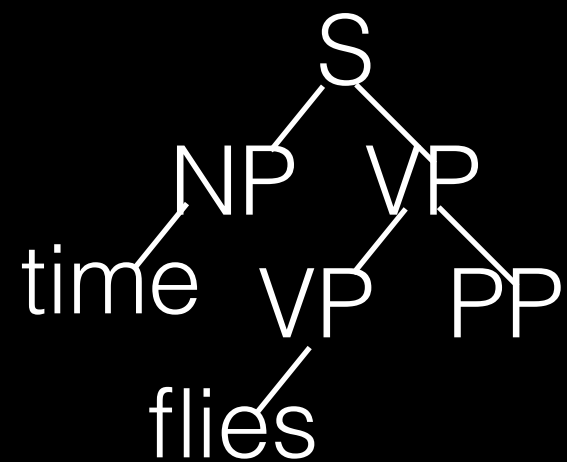
time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



Backpointer: VP → VP PP ,2

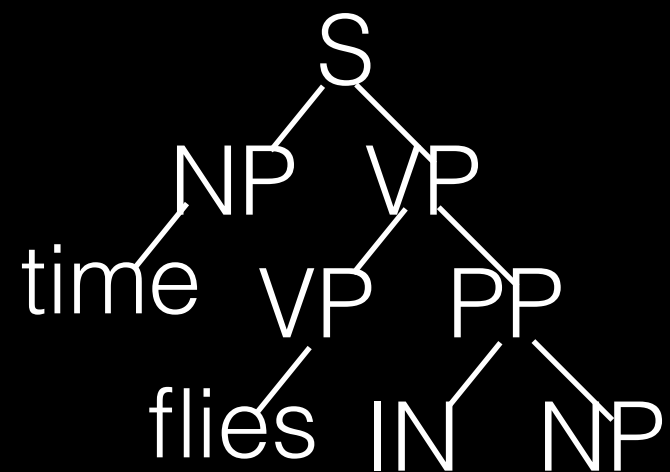


time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



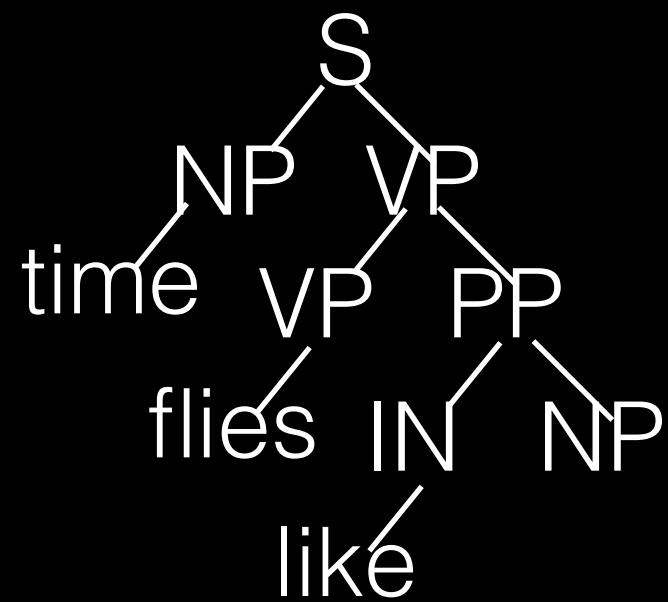
Backpointer: VP → flies

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



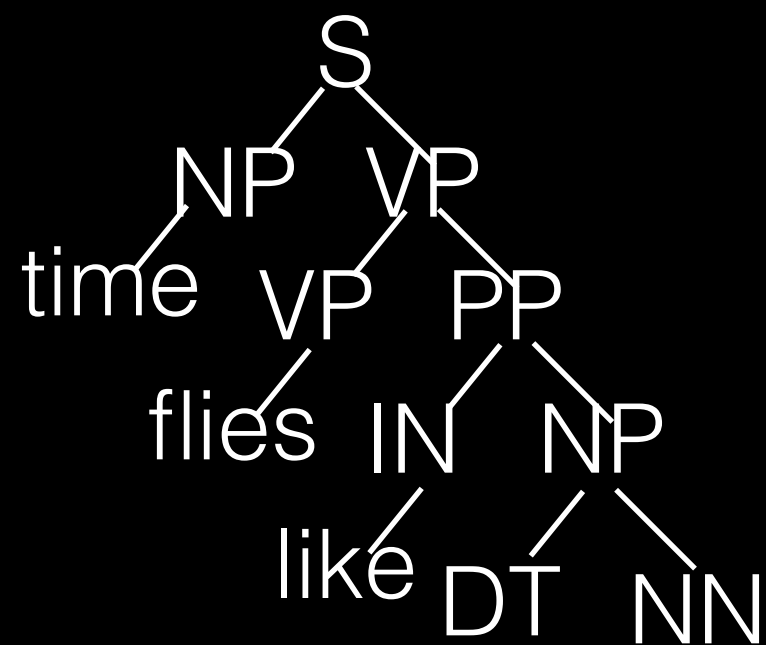
Backpointer: PP → IN NP ,3

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



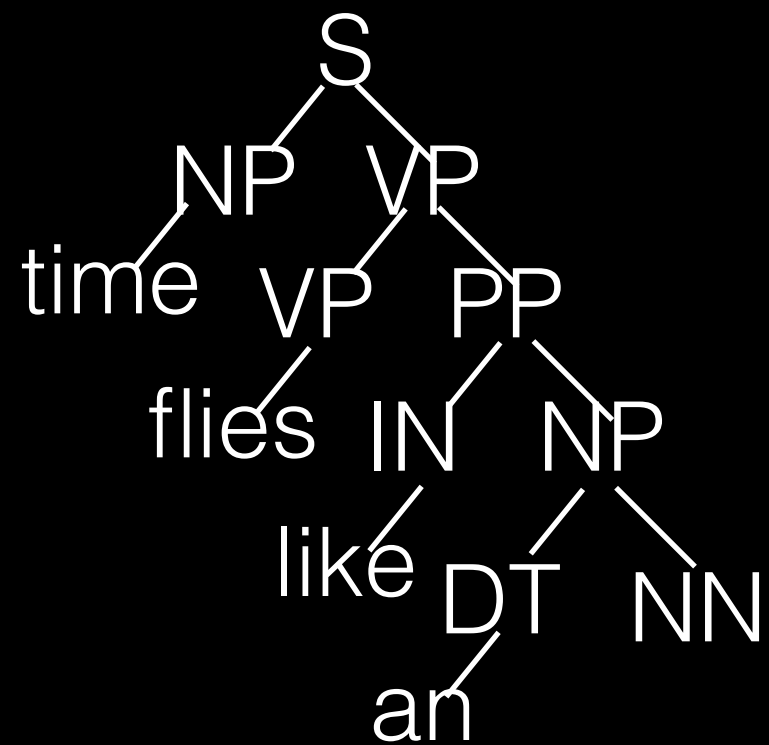
Backpointer: IN → like

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



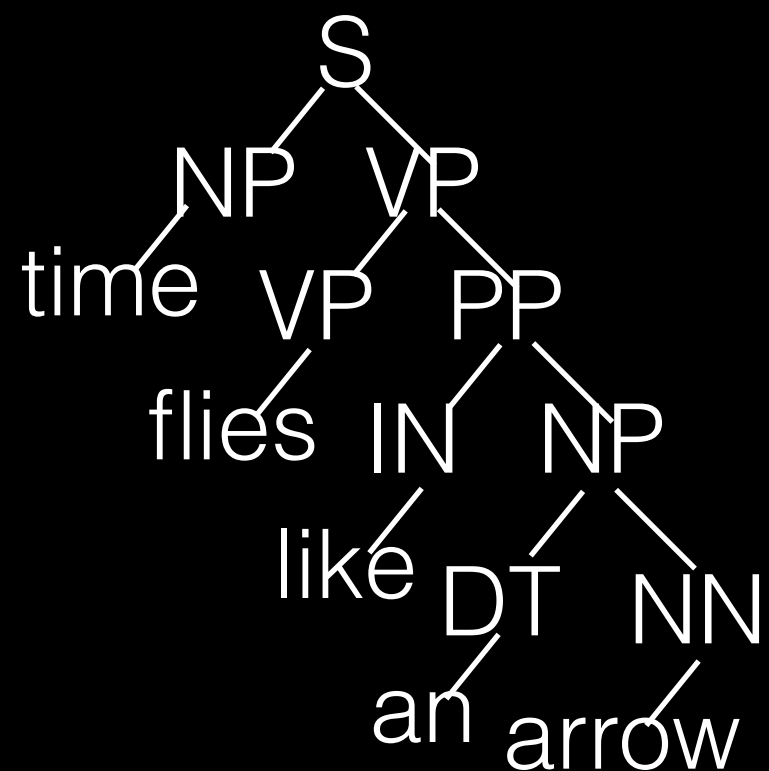
Backpointer: NP→DT NN ,4

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



Backpointer: DT → an

time	flies	like	an	arrow
NP NN [0,1]	S NP [0,2]	[0,3]	[0,4]	S [0,5]
	VP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP VP [2,5]
			DT [3,4]	NP [3,5]
				NN [4,5]



Backpointer: NN → arrow

# Other things to do with CKY

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$$C(X[i : i + 1]) = |X \rightarrow w_i|$$

$$C(X[i : j]) = \sum_{k=i+1}^{j-1} \sum_{X \rightarrow YZ} C(Y[i : k]) \times C(Z[k : j])$$

Where do grammars come  
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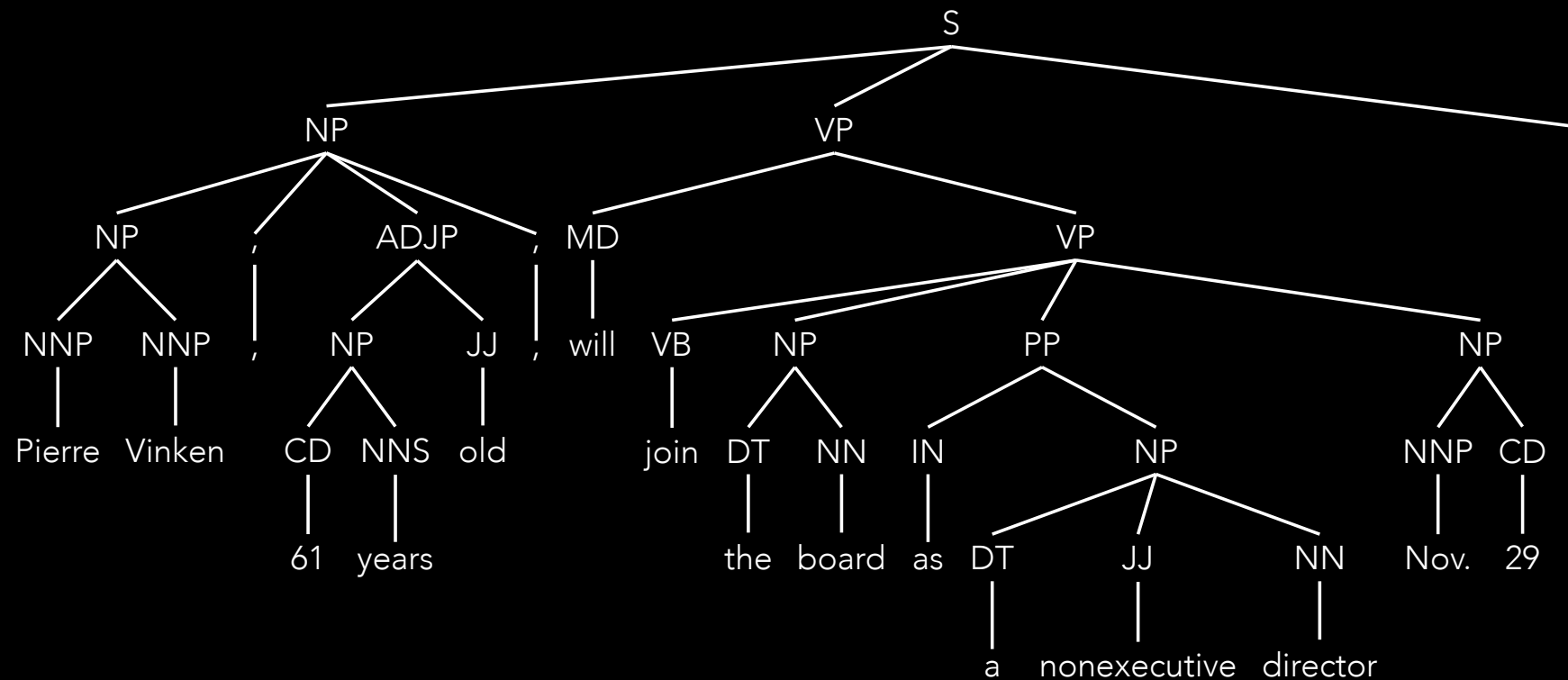
- You could write them by hand...

# Where do grammars come from?

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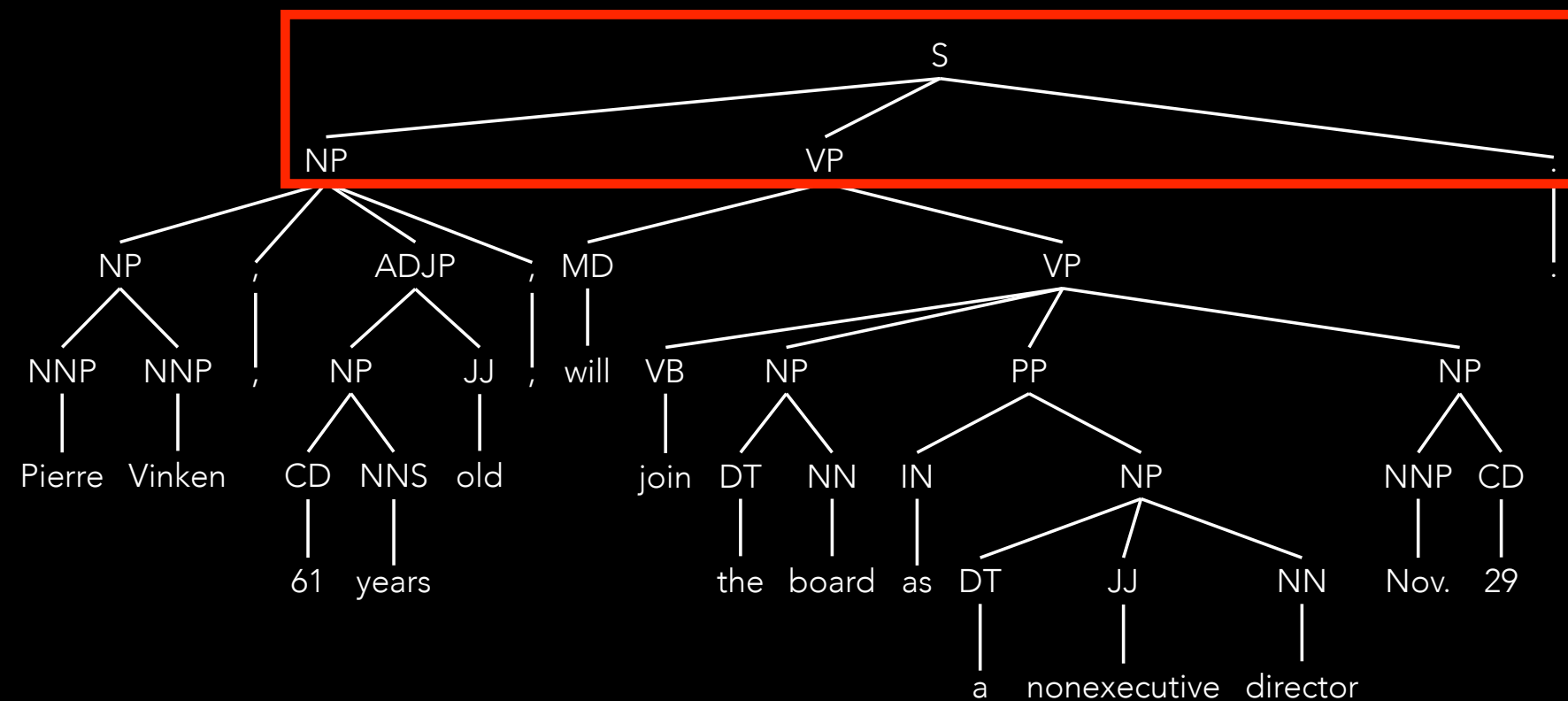
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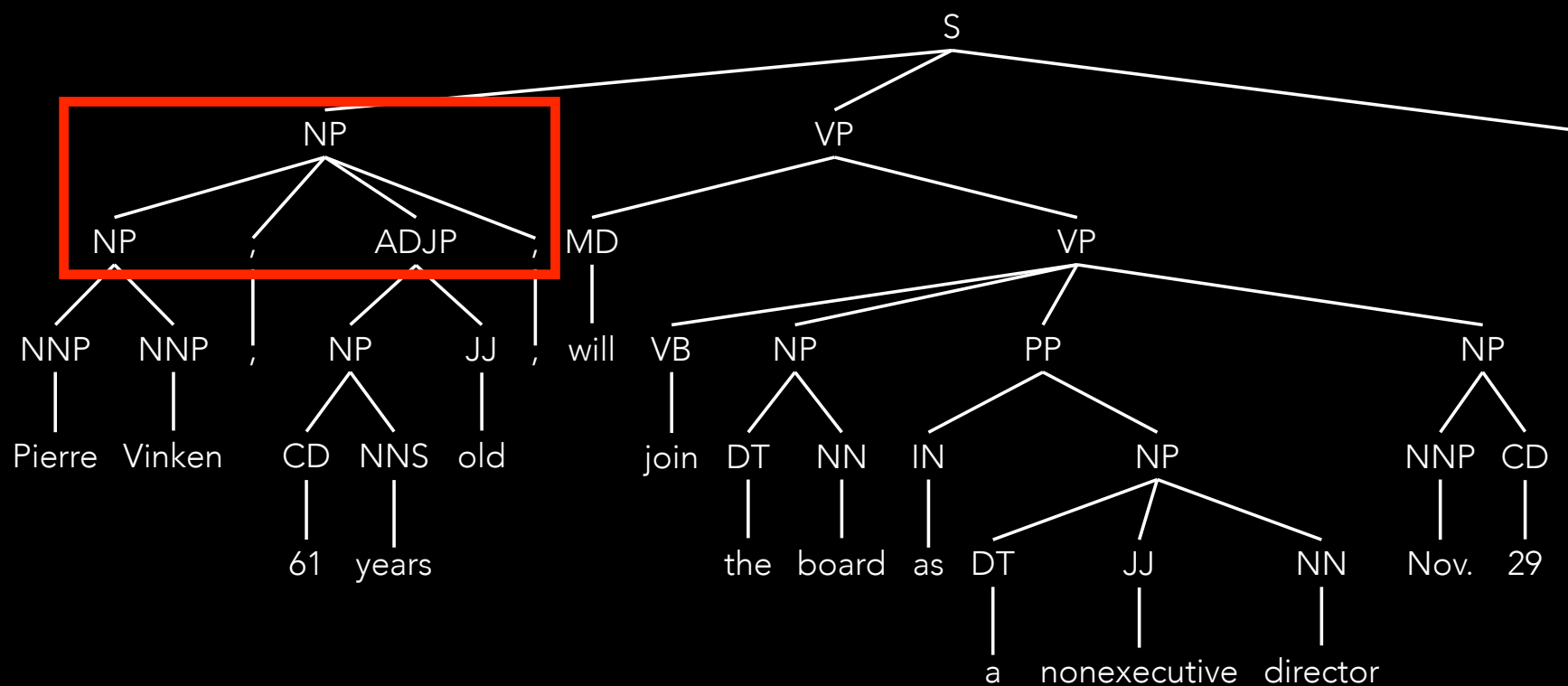
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$S \rightarrow NP VP .$

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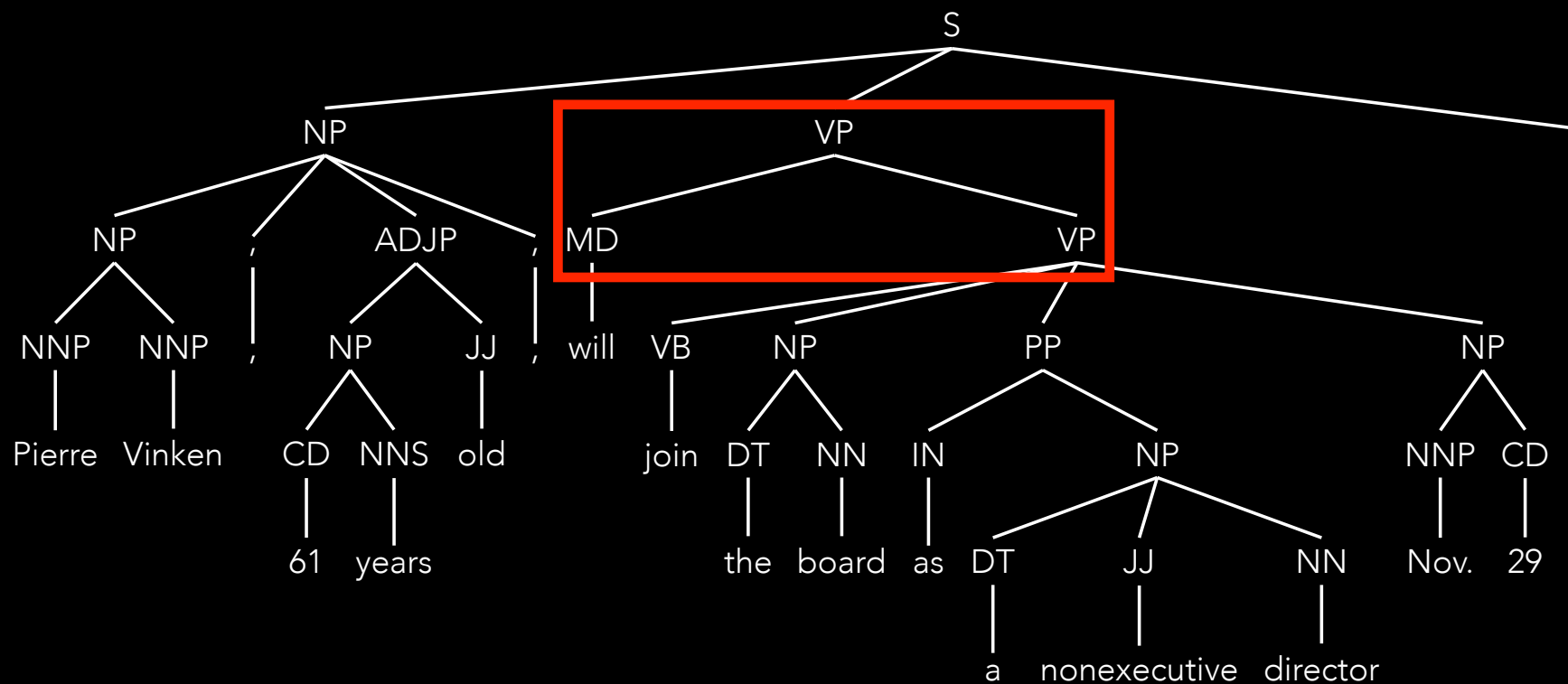
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$S \rightarrow NP VP .$   
 $NP \rightarrow NP , ADJP ,$

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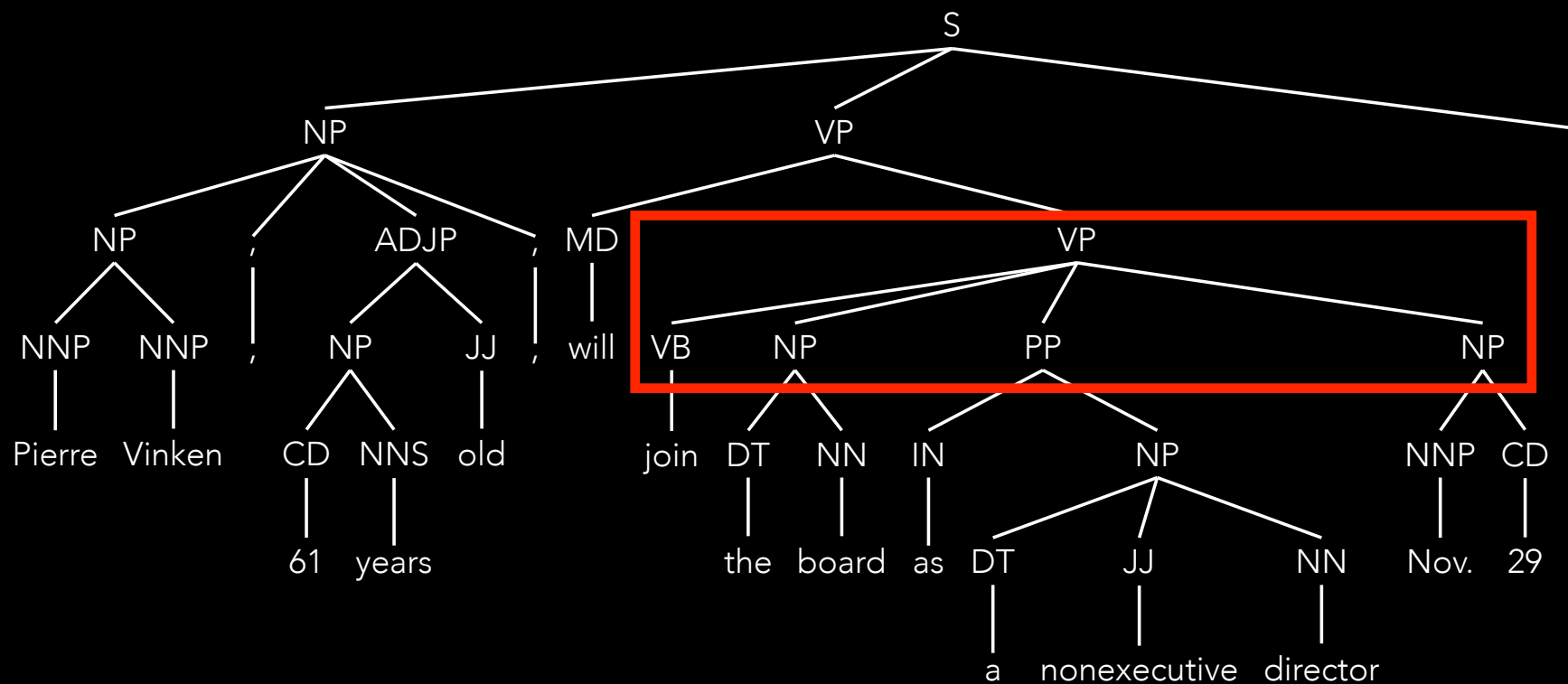
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$S \rightarrow NP VP .$   
 $NP \rightarrow NP , ADJP ,$   
 $VP \rightarrow MD VP$

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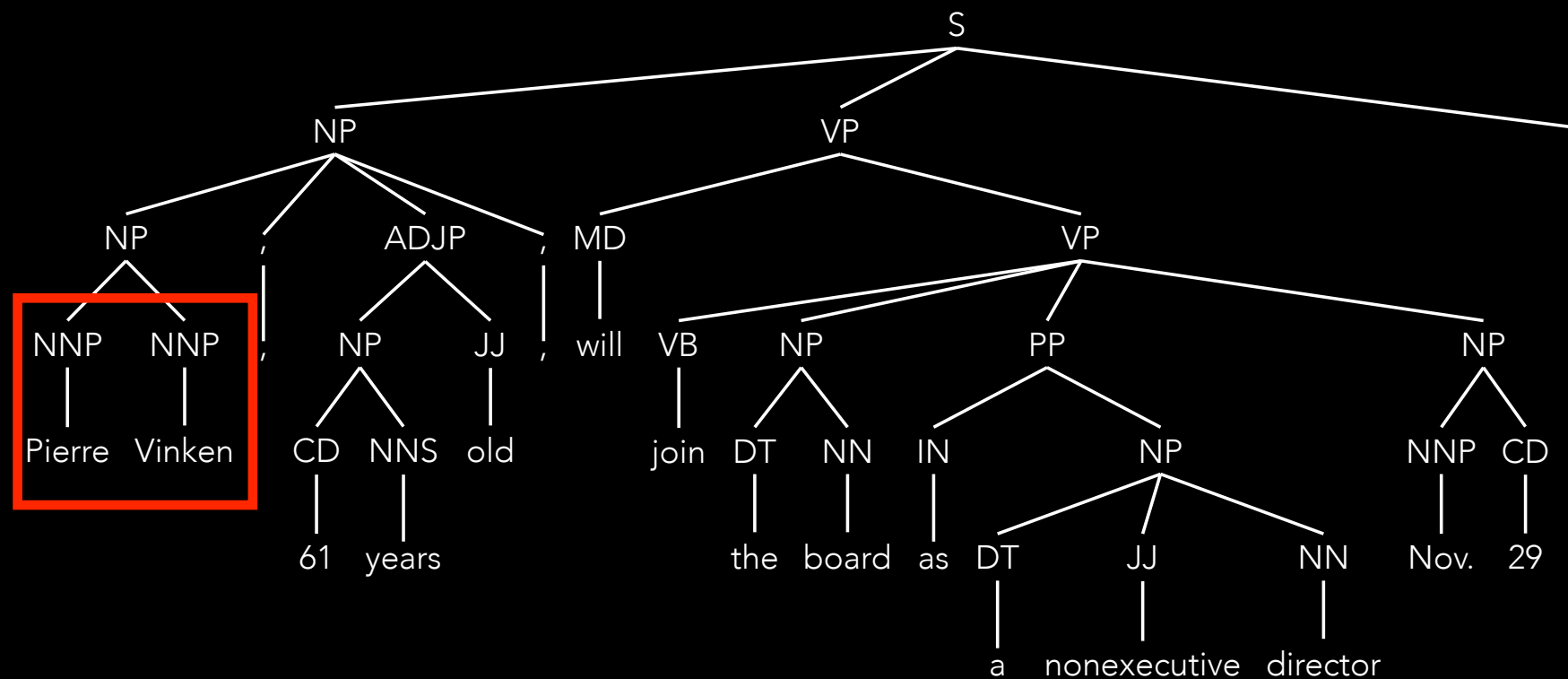
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$S \rightarrow NP VP .$   
 $NP \rightarrow NP , ADJP ,$   
 $VP \rightarrow MD VP$   
 $VP \rightarrow VB NP PP NP$

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$S \rightarrow NP VP .$

$NP \rightarrow NP , ADJP ,$

$VP \rightarrow MD VP$

$VP \rightarrow VB NP PP NP$

...

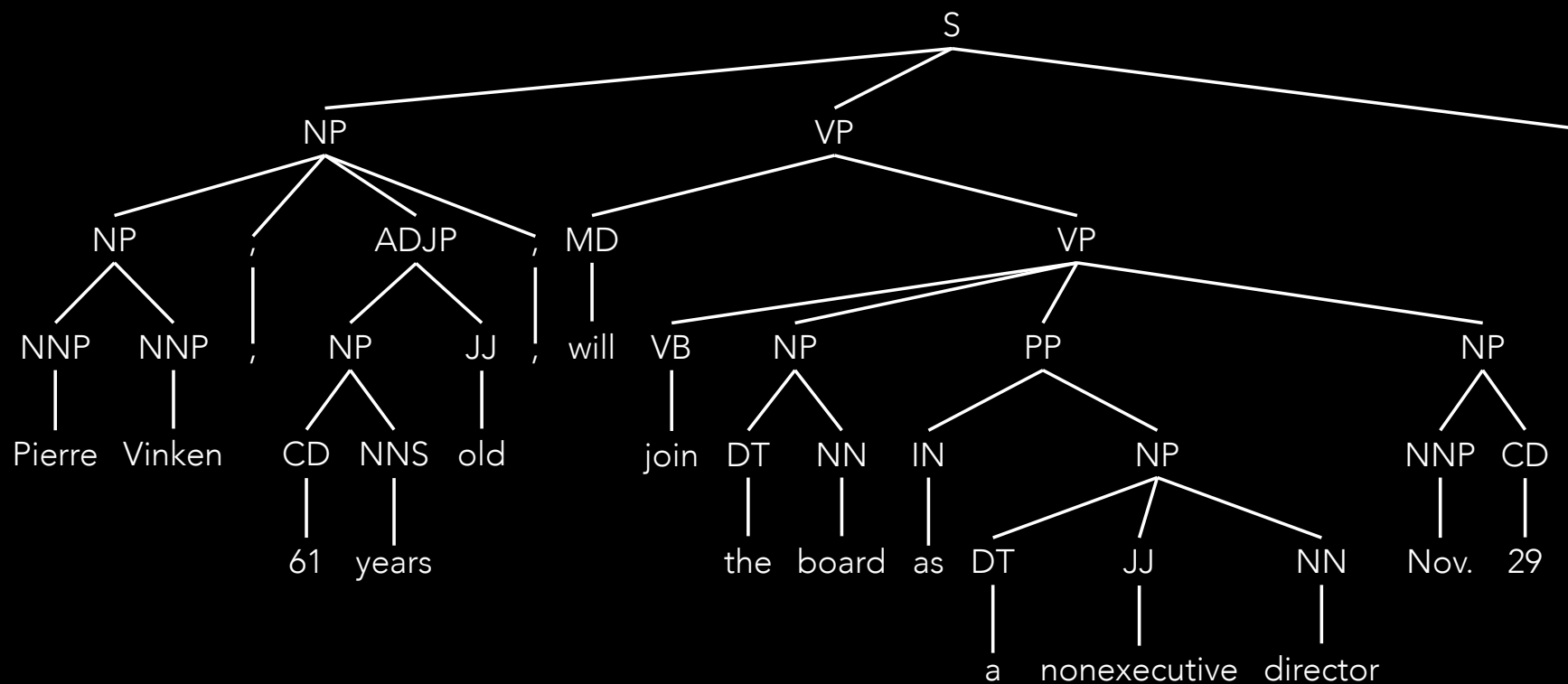
$NNP \rightarrow \text{Pierre}$

$NNP \rightarrow \text{Vinken}$

...

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$S \rightarrow NP VP .$   
 $NP \rightarrow NP , ADJP ,$   
 $VP \rightarrow MD VP$   
 $VP \rightarrow VB NP PP NP$   
...  
 $NNP \rightarrow \text{Pierre}$   
 $NNP \rightarrow \text{Vinken}$   
...

Chomsky Normal Form Violation!

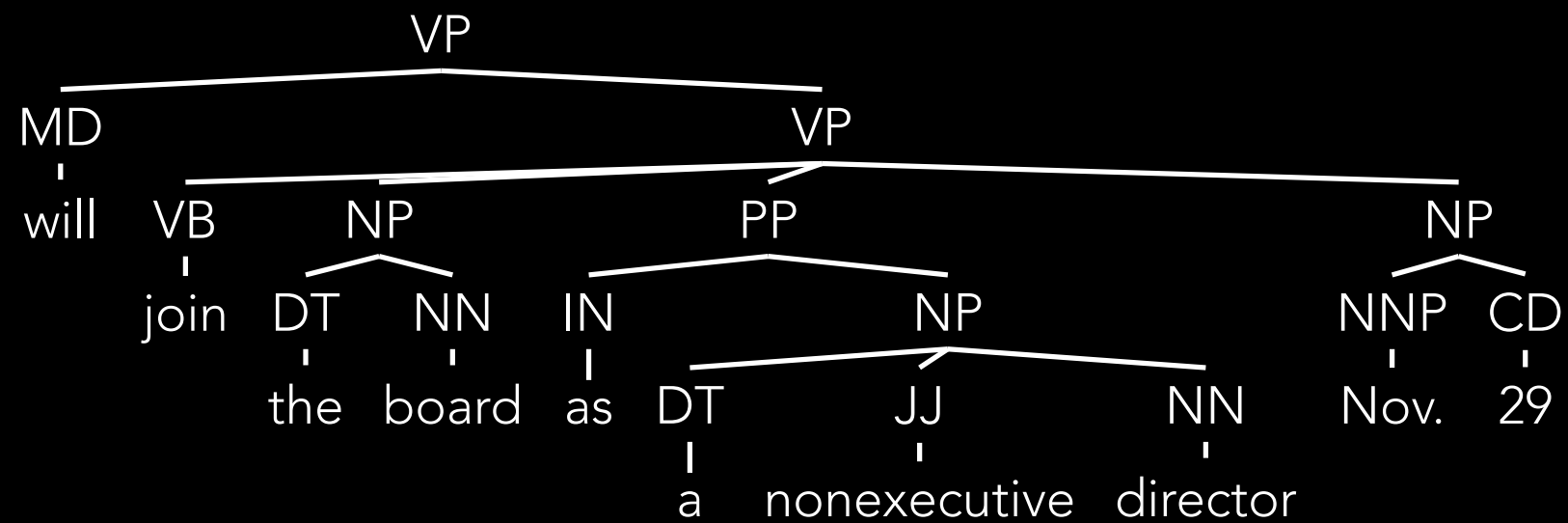
# CFG Normalization?

- There are well known approaches to normalizing CFGs into CNF
- However, it's far simpler to just modify the *trees*

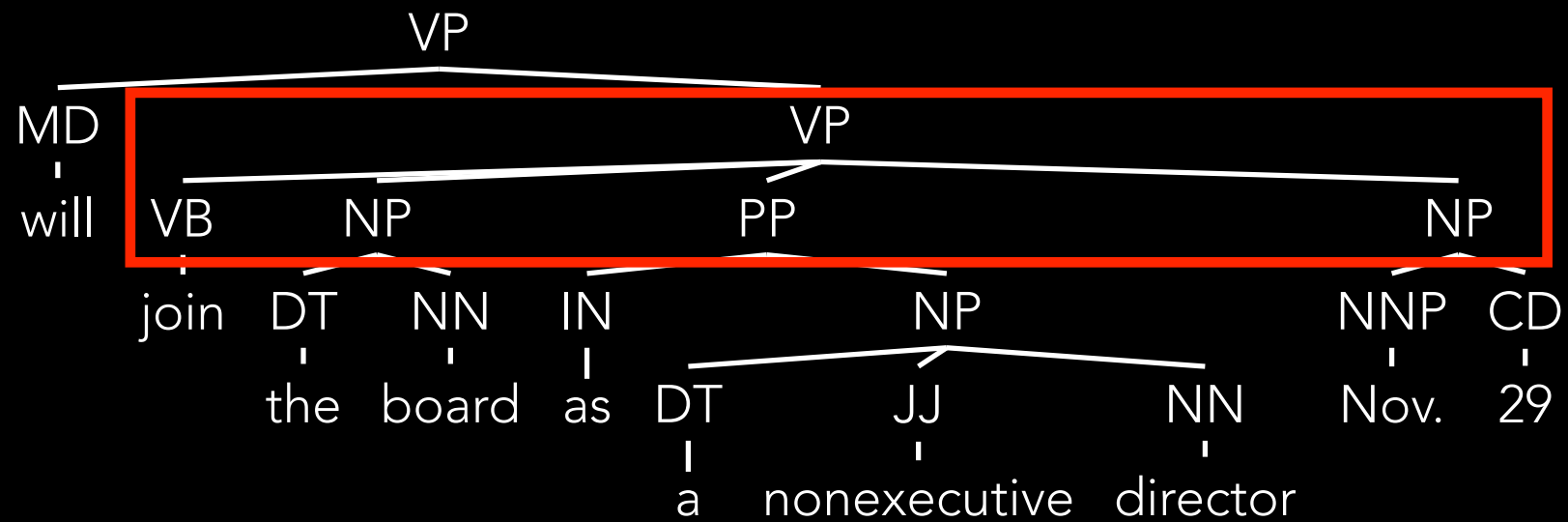
# CFG Normalization



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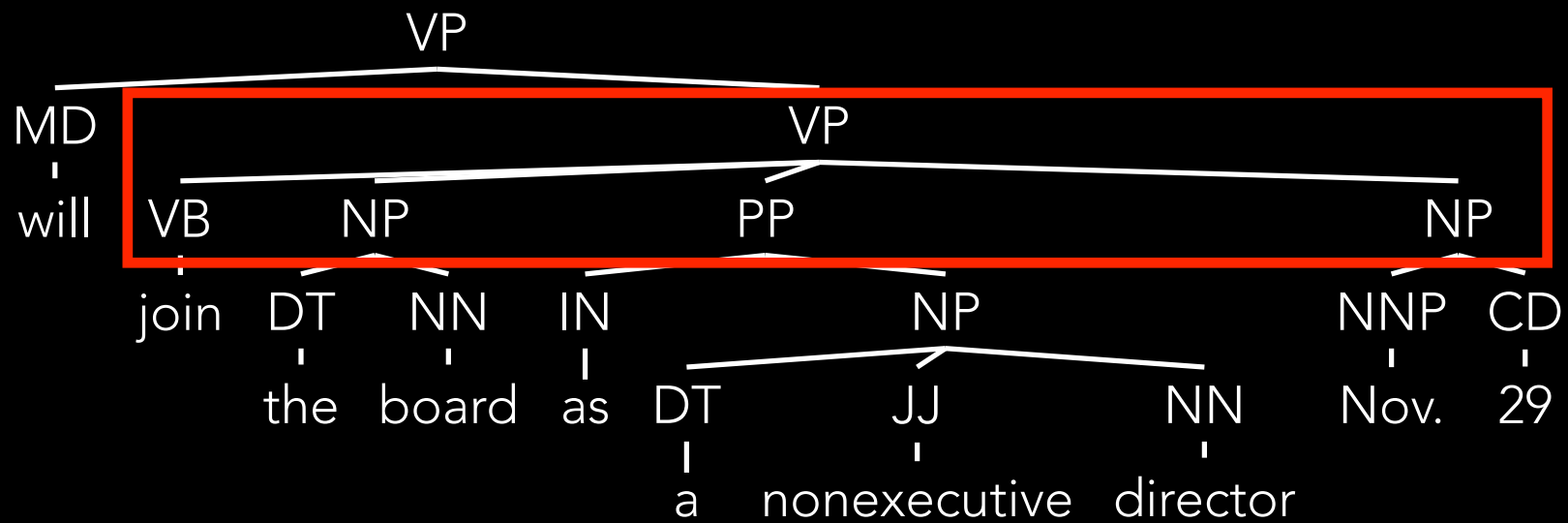


# CFG Normalization

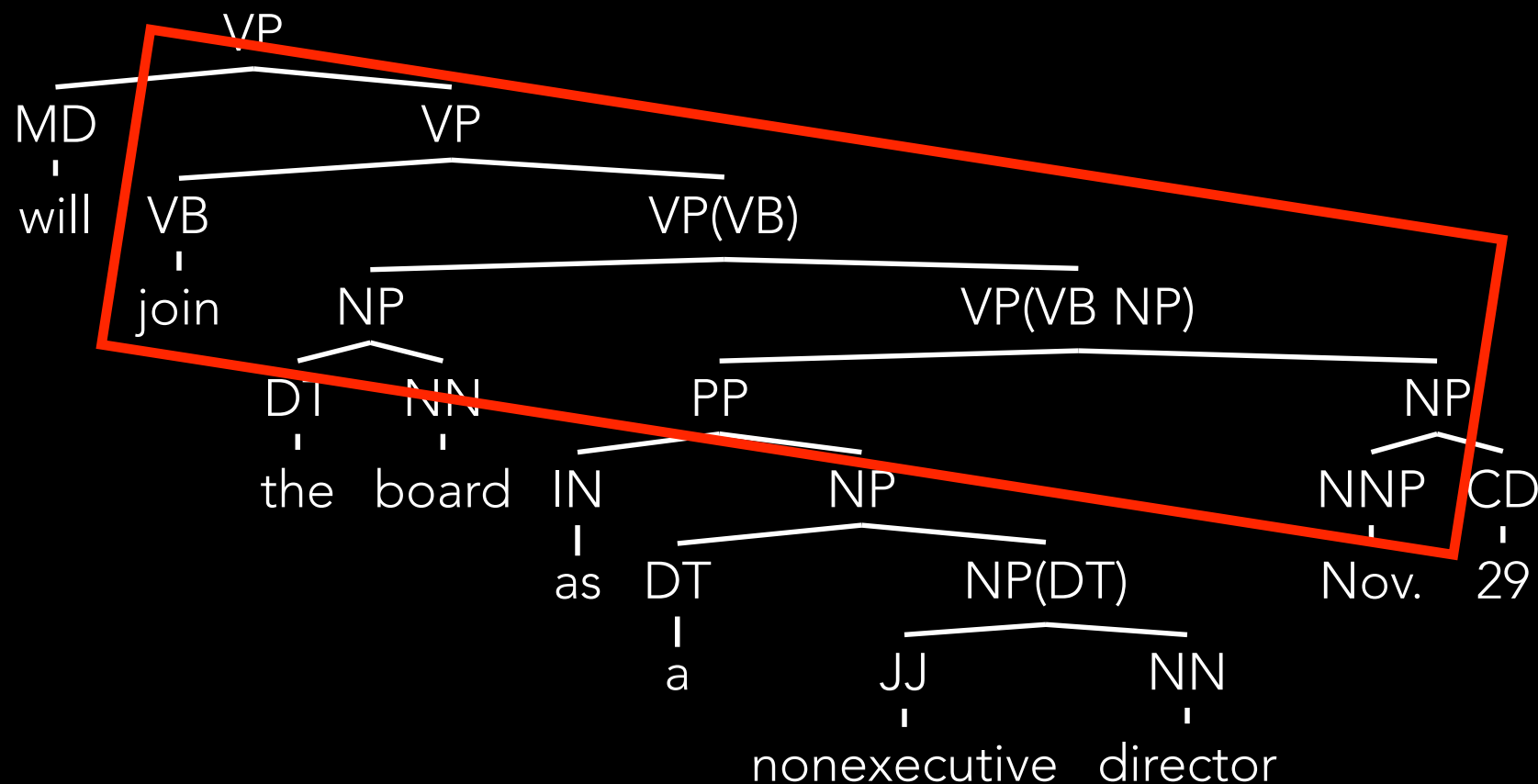


VP → VB NP PP NP  
not ok for CKY

# CFG Normalization

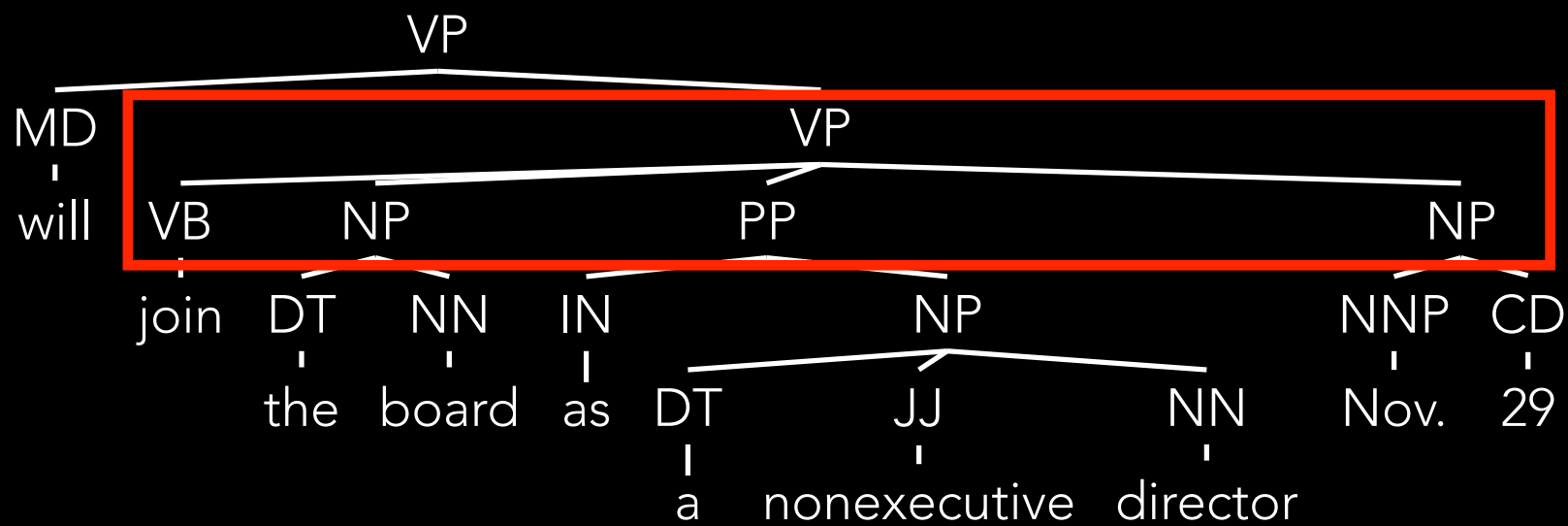


VP  $\rightarrow$  VB NP PP NP  
not ok for CKY

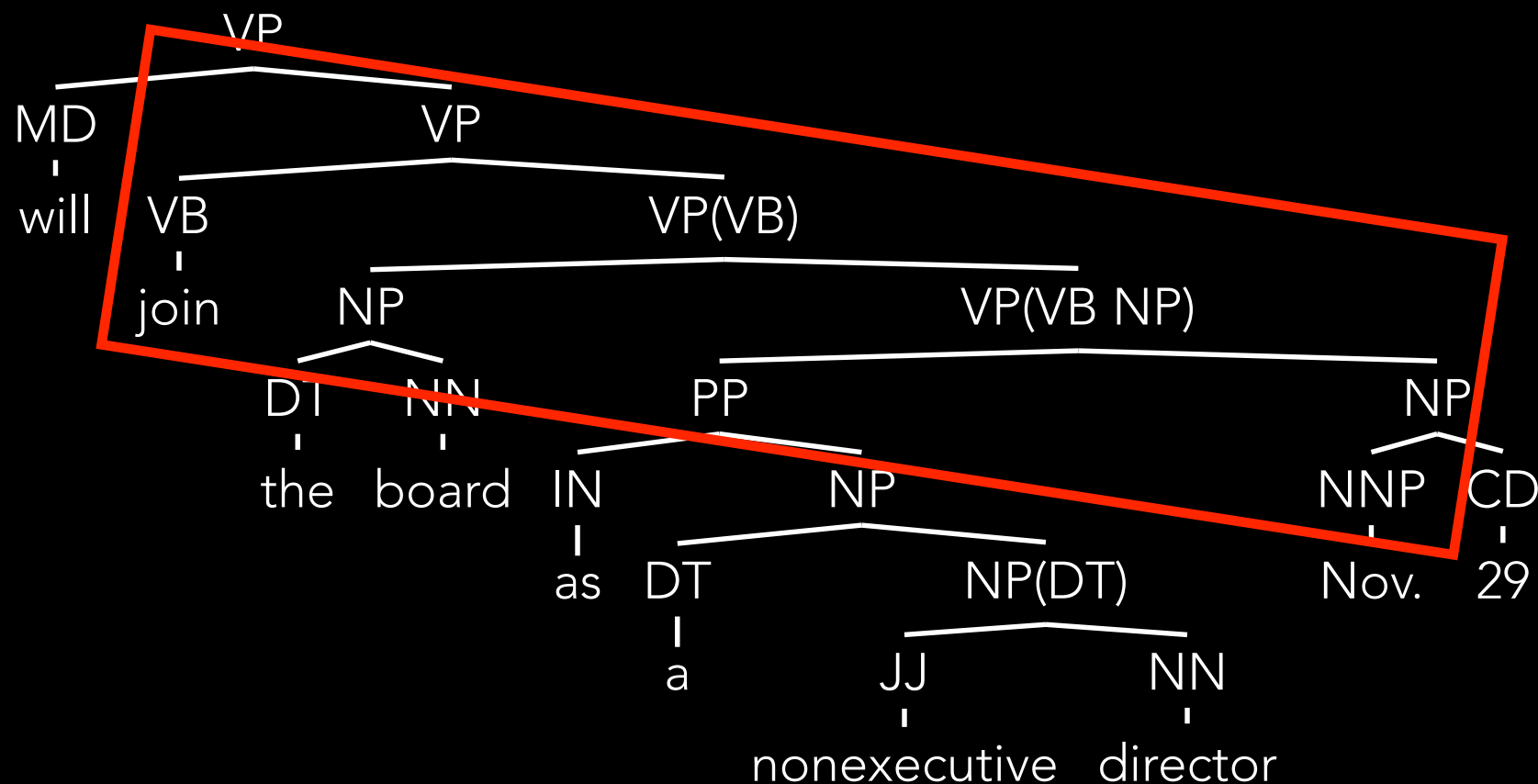


Three binary rules  
ok for CKY

# CFG Normalization



VP  $\rightarrow$  VB NP PP NP  
not ok for CKY

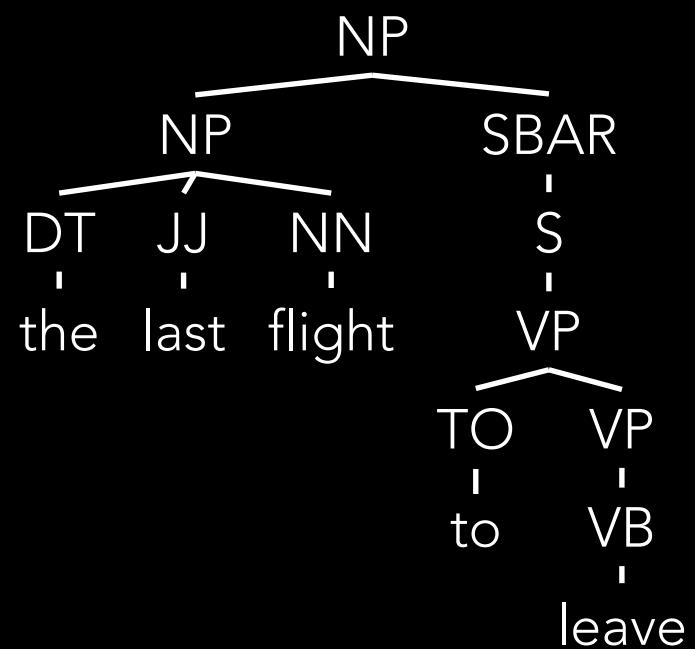


Three binary rules  
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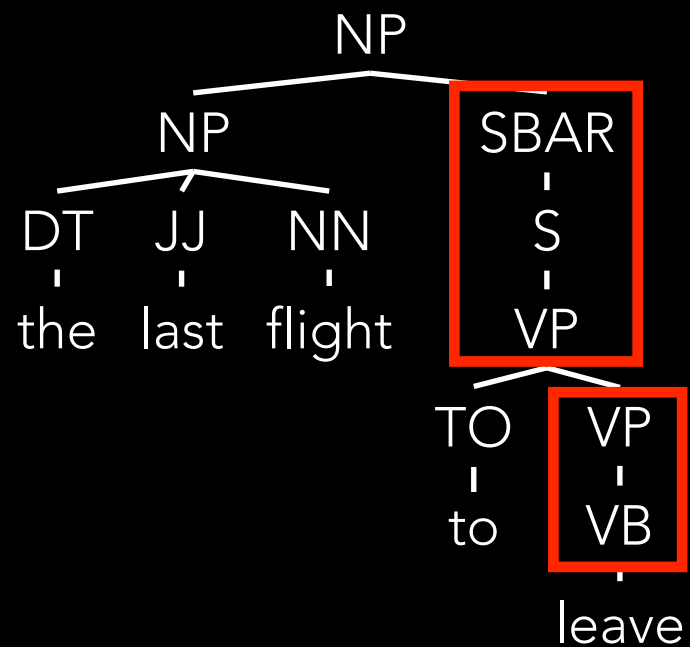
Why are the labels  
important?

# What about unary trees?

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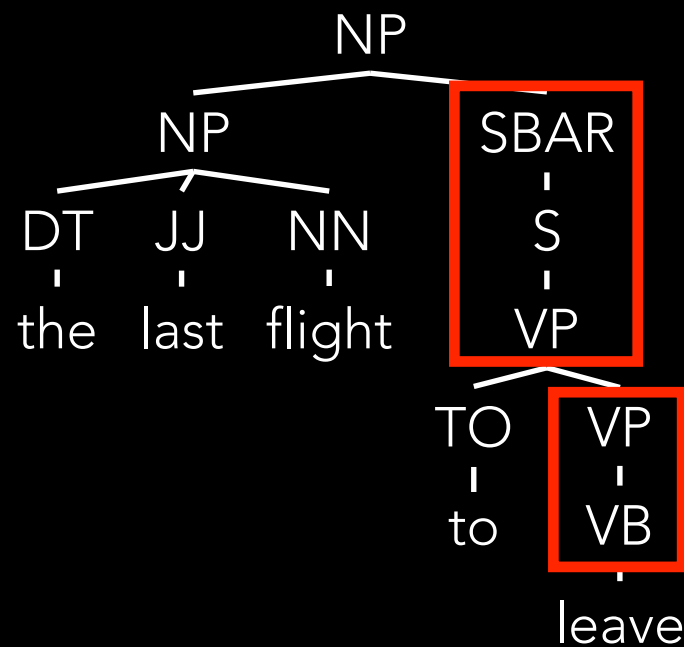


# What about unary trees?

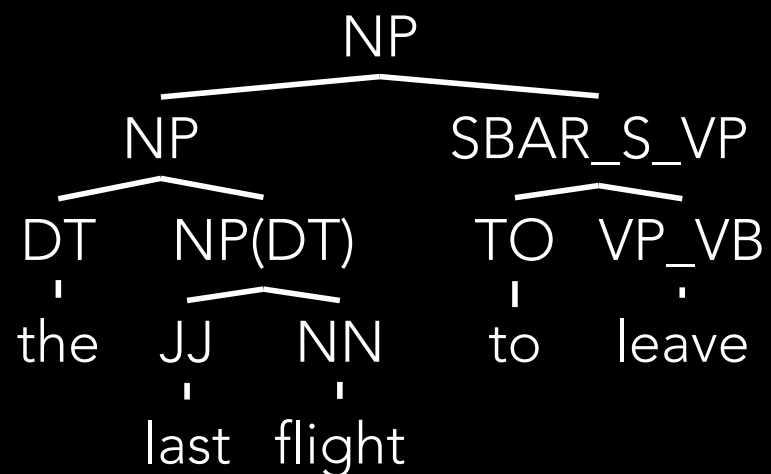


SBAR  $\rightarrow$  S, S  $\rightarrow$  VP,  
VP  $\rightarrow$  VB  
not good for CKY

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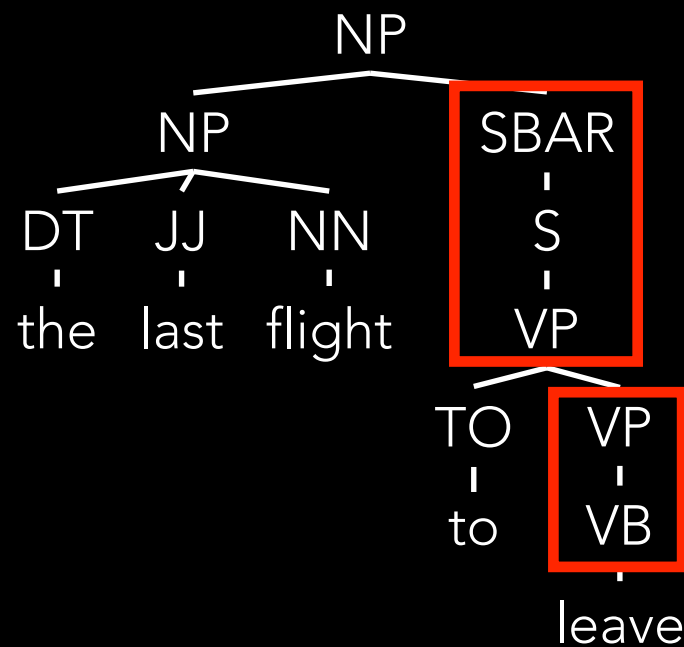


SBAR  $\rightarrow$  S, S  $\rightarrow$  VP,  
VP  $\rightarrow$  VB  
not good for CKY

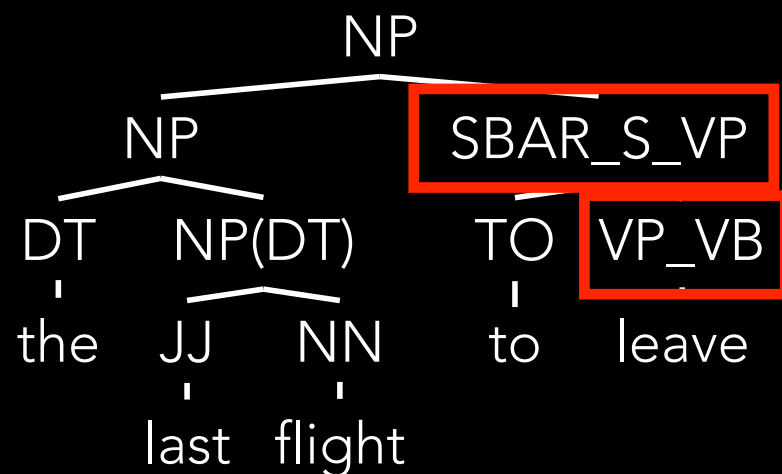




# What about unary trees?



SBAR  $\rightarrow$  S, S  $\rightarrow$  VP,  
VP  $\rightarrow$  VB  
not good for CKY



Collapse into single label

# Review

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- Tree normalization
- CKY extension to unary nonterminal rules

# Alternate: Modify CKY!

- Initialize: build  $[X, i, i+1]$  for every lexical rule  $R = X \rightarrow w_i$ ; add backpointer  $\{R, ()\}$
- Recursively: build  $[X, i, j]$  for every nonlexical rule  $R = X \rightarrow Y Z$  and pair of states  $([Y, i, k], [Z, k, j])$  where  $i < k < j$ ; add backpointer  $\{R, k\}$
- If state is already built, just add backpointer

# Alternate: Modify CKY!

- Initialize: build  $[X, i, i+1]$  for every lexical rule  $R = X \rightarrow w_i$ ; add backpointer  $\{R, ()\}$
- Recursively:
  - build  $[X, i, j]$  for every nonlexical rule  $R = X \rightarrow Y Z$  and pair of states  $([Y, i, k], [Z, k, j])$  where  $i < k < j$ ; add backpointer  $\{R, k\}$
  - build  $[X, i, j]$  for every nonlexical rule  $R = X \rightarrow Y$  and state  $[Y, i, j]$  **if  $[X, i, j]$  does not exist**; add backpointer  $\{R, ()\}$
- If state is already built, just add backpointer

	time	flies	like	an	arrow
	[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP					
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time   fruit					
NP → NN NNS					
VP → VBP NP			[2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP				[3,4]	[3,5]
DT → a   an					
NN → time   fruit   arrow   banana					[4,5]
NNS → flies					
VBP → like					
IN → like					

time

flies

like

an

arrow

[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP				
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]
NP → NN				
NP → NN NNS				
VP → VBP NP		[2,3]	[2,4]	[2,5]
VP → flies				
VP → VP PP				
PP → IN NP			[3,4]	[3,5]
DT → a   an				
NN → time   fruit   arrow   banana				[4,5]
NNS → flies				
VBP → like				
IN → like				

More realistic!

	time	flies	like	an	arrow
	[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP					
NP → DT NN	[1,2]	[1,3]	[1,4]	[1,5]	
NP → NN					
NP → NN NNS					
VP → VBP NP			[2,3]	[2,4]	[2,5]
VP → flies					
VP → VP PP					
PP → IN NP				[3,4]	[3,5]
DT → a   an					
NN → time   fruit   arrow   banana					[4,5]
NNS → flies					
VBP → like					
IN → like					

Not typical, but for illustration.



	time	flies	like	an	arrow
	<div>NN</div> <div>[0,1]</div>	<div>[0,2]</div>	<div>[0,3]</div>	<div>[0,4]</div>	<div>[0,5]</div>
<div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → NN</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div>	<div>VP</div> <div>NNS</div> <div>[1,2]</div>	<div>[1,3]</div>	<div>[1,4]</div>	<div>[1,5]</div>	
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div>[2,4]</div>	<div>[2,5]</div>	
	<div>PP → NP</div> <div>VP → PP</div> <div>NP → VP</div>		<div>DT</div> <div>[3,4]</div>	<div>[3,5]</div>	
				<div>NN</div> <div>[4,5]</div>	

After seeding the chart.  
 We need to check length-1 spans  
 for nonlexical rules

	time	flies	like	an	arrow
	NP NN [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → NN NP → NN NNS VP → VBP NP VP → flies VP → VP PP PP → IN NP DT → a   an NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NN [4,5]

New state!

	time	flies	like	an	arrow
	<div>NP PP</div> <div>NN</div> <div>[0,1]</div>	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		<div>VP</div> <div>NNS</div> <div>[1,2]</div>	[1,3]	[1,4]	[1,5]
NP → DT NN					
NP → NN			<div>IN</div> <div>VBP</div> <div>[2,3]</div>	[2,4]	[2,5]
NP → NN NNS					
VP → VBP NP					
VP → flies				<div>DT</div> <div>[3,4]</div>	[3,5]
VP → VP PP					
PP → IN NP					
DT → a   an					<div>NN</div> <div>[4,5]</div>
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					

New state!

New state!

	time	flies	like	an	arrow
	<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	[0,2]	[0,3]	[0,4]	[0,5]
<div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → NN</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div>	<div>VP</div> <div>NNS</div> <div>[1,2]</div>	[1,3]	[1,4]	[1,5]	
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	[2,4]	[2,5]	
	<div>PP → NP</div> <div>VP → PP</div> <div>NP → VP</div>		<div>DT</div> <div>[3,4]</div>	[3,5]	
				<div>NN</div> <div>[4,5]</div>	

New state!

New state!

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN		VP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → NN NP → NN NNS VP → VBP NP			IN VBP [2,3]	[2,4]	[2,5]
VP → flies VP → VP PP PP → IN NP				DT [3,4]	[3,5]
DT → a   an NN → time   fruit   arrow   banana					NN [4,5]
NNS → flies VBP → like IN → like					

PP → NP  
 VP → PP  
 NP → VP

No new state, and no backpointer  
(would lead to infinite loop)

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN NP → NN NP → NN NNS VP → VBP NP VP → flies VP → VP PP PP → IN NP DT → a   an NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like		PP VP NP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
		PP → NP VP → PP NP → VP		DT [3,4]	[3,5]
					NN [4,5]

Two new states!

time

flies

like

an

arrow

<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div></div> <div>[0,2]</div>	<div></div> <div>[0,3]</div>	<div></div> <div>[0,4]</div>	<div></div> <div>[0,5]</div>
<div></div>	<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	<div></div> <div>[1,3]</div>	<div></div> <div>[1,4]</div>	<div></div> <div>[1,5]</div>
<div></div>	<div></div>	<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div></div> <div>[2,4]</div>	<div></div> <div>[2,5]</div>
<div></div>	<div></div>	<div></div>	<div>DT</div> <div>[3,4]</div>	<div></div> <div>[3,5]</div>
<div></div>	<div></div>	<div></div>	<div></div>	<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

S → NP VP

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

PP → NP

VP → PP

NP → VP

Three new states!

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP [0,2]	[0,3]	[0,4]	[0,5]
		PP VP NP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NP PP NN VP [4,5]

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$NP \rightarrow NN$

$NP \rightarrow NN NNS$

$VP \rightarrow VBP NP$

$VP \rightarrow \text{flies}$

$VP \rightarrow VP PP$

$PP \rightarrow IN NP$

$DT \rightarrow a \mid an$

$NN \rightarrow \text{time} \mid \text{fruit} \mid \text{arrow} \mid \text{banana}$

$NNS \rightarrow \text{flies}$

$VBP \rightarrow \text{like}$

$IN \rightarrow \text{like}$

$PP \rightarrow NP$

$VP \rightarrow PP$

$NP \rightarrow VP$

This is what we had before...



	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP [0,2]	[0,3]	[0,4]	[0,5]
		PP VP NP NNS [1,2]	[1,3]	[1,4]	[1,5]
			IN VBP [2,3]	[2,4]	[2,5]
				DT [3,4]	[3,5]
					NP PP NN VP [4,5]

S → NP VP

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

PP → NP

VP → PP

NP → VP

...but now we can add one more  
with a binary rule

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN		PP VP NP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → NN NP → NN NNS VP → VBP NP			IN VBP [2,3]	[2,4]	[2,5]
VP → flies VP → VP PP PP → IN NP DT → a   an		PP → NP VP → PP NP → VP		DT [3,4]	[3,5]
NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like					NP PP NN VP [4,5]

...and can take a unary step

time

flies

like

an

arrow

<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div>S NP</div> <div>VP PP</div> <div>[0,2]</div>	<div>[0,3]</div>	<div>[0,4]</div>	<div>[0,5]</div>
	<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	<div>[1,3]</div>	<div>[1,4]</div>	<div>[1,5]</div>
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div>[2,4]</div>	<div>[2,5]</div>
			<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>[3,5]</div>
				<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

S → NP VP

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

PP → NP

VP → PP

NP → VP

This is what we had before

time

flies

like

an

arrow

<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div>S NP</div> <div>VP PP</div> <div>[0,2]</div>	<div>[0,3]</div>	<div>[0,4]</div>	<div>[0,5]</div>
	<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	<div>[1,3]</div>	<div>[1,4]</div>	<div>[1,5]</div>
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div>[2,4]</div>	<div>[2,5]</div>
			<div>DT</div> <div>[3,4]</div>	<div>NP PP VP</div> <div>[3,5]</div>
				<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

S → NP VP

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

PP → NP

VP → PP

NP → VP

Now we have two more

time

flies

like

an

arrow

<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div>S NP</div> <div>VP PP</div> <div>[0,2]</div>	<div>[0,3]</div>	<div>[0,4]</div>	<div>[0,5]</div>
<div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → NN</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div>	<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	<div>[1,3]</div>	<div>[1,4]</div>	<div>[1,5]</div>
		<div>IN</div> <div>VBP</div> <div>[2,3]</div>	<div>[2,4]</div>	<div>PP</div> <div>VP</div> <div>[2,5]</div>
			<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>PP VP</div> <div>[3,5]</div>
				<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

This is what we had before

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP NP → DT NN		PP VP NP NNS [1,2]	[1,3]	[1,4]	[1,5]
NP → NN NP → NN NNS VP → VBP NP VP → flies			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
VP → VP PP PP → IN NP DT → a   an	PP → NP VP → PP NP → VP		DT [3,4]	[3,5]	NP PP VP [4,5]
NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like					

Can add one from unary step

time

flies

like

an

arrow

NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	[0,5]
	PP VP NP NNS [1,2]	[1,3]	[1,4]	VP [1,5]
		IN VBP [2,3]	[2,4]	PP NP VP [2,5]
			DT [3,4]	NP PP VP [3,5]
				NP PP NN VP [4,5]

S → NP VP

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like

PP → NP

VP → PP

NP → VP

This is what we had before

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	[0,5]
<b>S → NP VP</b>		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S [1,5]
NP → DT NN			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
NP → NN					
NP → NN NNS					
VP → VBP NP					
VP → flies		PP → NP			
VP → VP PP		VP → PP		DT [3,4]	NP PP VP [3,5]
PP → IN NP		NP → VP			
DT → a   an					NP PP NN VP [4,5]
NN → time   fruit   arrow   banana					
NNS → flies					
VBP → like					
IN → like					

We can add one more non-unary now



	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	[0,5]
S → NP VP		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S PP NP [1,5]
NP → DT NN					
NP → NN					
NP → NN NNS					
VP → VBP NP			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
VP → flies		PP → NP			
VP → VP PP		VP → PP		DT [3,4]	NP PP VP [3,5]
PP → IN NP		NP → VP			
DT → a   an					
NN → time   fruit   arrow   banana					NP PP NN VP [4,5]
NNS → flies					
VBP → like					
IN → like					

And two more with unary steps.

	time	flies	like	an	arrow
	<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div>S NP</div> <div>VP PP</div> <div>[0,2]</div>	[0,3]	[0,4]	<div>S</div> <div>[0,5]</div>
<div>S → NP VP</div> <div>NP → DT NN</div> <div>NP → NN NNS</div> <div>VP → VBP NP</div> <div>VP → flies</div> <div>VP → VP PP</div> <div>PP → IN NP</div> <div>DT → a   an</div> <div>NN → time   fruit   arrow   banana</div> <div>NNS → flies</div> <div>VBP → like</div> <div>IN → like</div>		<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	[1,3]	[1,4]	<div>VP S</div> <div>PP NP</div> <div>[1,5]</div>
			<div>IN</div> <div>VBP</div> <div>[2,3]</div>	[2,4]	<div>PP NP</div> <div>VP</div> <div>[2,5]</div>
				<div>DT</div> <div>[3,4]</div>	<div>NP PP VP</div> <div>[3,5]</div>
					<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

We built S this way before

	time	flies	like	an	arrow
	<div>NP PP</div> <div>NN VP</div> <div>[0,1]</div>	<div>S NP</div> <div>VP PP</div> <div>[0,2]</div>	[0,3]	[0,4]	<div>S VP</div> <div>[0,5]</div>
		<div>PP VP NP</div> <div>NNS</div> <div>[1,2]</div>	[1,3]	[1,4]	<div>VP S</div> <div>PP NP</div> <div>[1,5]</div>
			<div>IN</div> <div>VBP</div> <div>[2,3]</div>	[2,4]	<div>PP NP</div> <div>VP</div> <div>[2,5]</div>
				<div>DT</div> <div>[3,4]</div>	<div>NP</div> <div>PP VP</div> <div>[3,5]</div>
					<div>NP PP</div> <div>NN VP</div> <div>[4,5]</div>

S → NP VP  
 NP → DT NN  
 NP → NN  
 NP → NN NNS  
 VP → VBP NP  
 VP → flies  
 VP → VP PP  
 PP → IN NP  
 DT → a | an

PP → NP  
 VP → PP  
 NP → VP

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like      We can also build a VP at this split point.

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	S VP [0,5]
		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S PP NP [1,5]
			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
				DT [3,4]	NP PP VP [3,5]
					NP PP NN VP [4,5]

**S → NP VP**

NP → DT NN

NP → NN

NP → NN NNS

VP → VBP NP

VP → flies

VP → VP PP

PP → IN NP

DT → a | an

NN → time | fruit | arrow | banana

NNS → flies

VBP → like

IN → like Before, we built a second backpointer to S

PP → NP

VP → PP

NP → VP

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	S VP [0,5]
S → NP VP NP → DT NN		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S PP NP [1,5]
NP → NN NP → NN NNS VP → VBP NP VP → flies			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
VP → VP PP PP → IN NP DT → a   an				DT [3,4]	NP PP VP [3,5]
NN → time   fruit   arrow   banana					NP PP NN VP [4,5]
NNS → flies					
VBP → like					
IN → like					

Now we have a second  
backpointer to VP, too

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	S VP NP PP [0,5]
S → NP VP NP → DT NN		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S PP NP [1,5]
NP → NN NP → NN NNS VP → VBP NP			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
VP → flies VP → VP PP PP → IN NP DT → a   an	PP → NP VP → PP NP → VP			DT [3,4]	NP PP VP [3,5]
NN → time   fruit   arrow   banana NNS → flies VBP → like IN → like					NP PP NN VP [4,5]

Finally, we have new states from unary steps.

	time	flies	like	an	arrow
	NP PP NN VP [0,1]	S NP VP PP [0,2]	[0,3]	[0,4]	S VP NP PP [0,5]
S → NP VP NP → DT NN		PP VP NP NNS [1,2]	[1,3]	[1,4]	VP S PP NP [1,5]
NP → NN NP → NN NNS VP → VBP NP VP → flies			IN VBP [2,3]	[2,4]	PP NP VP [2,5]
VP → VP PP PP → IN NP DT → a   an	PP → NP VP → PP NP → VP			DT [3,4]	NP PP VP [3,5]
NN → time   fruit   arrow   banana					NP PP NN VP [4,5]

NNS → flies

VBP → like

IN → like

Do we have any new trees?  
Actually, no,  
because S is the only start symbol.

But Which Parse Is Best?

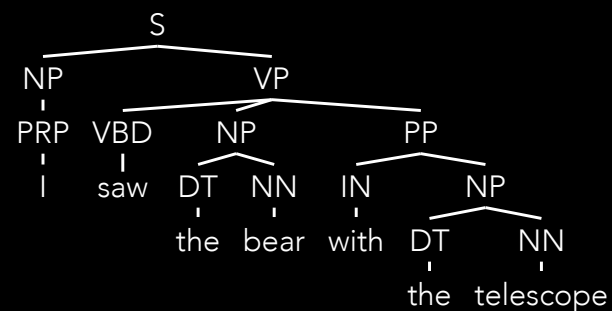


# But Which Parse Is Best?

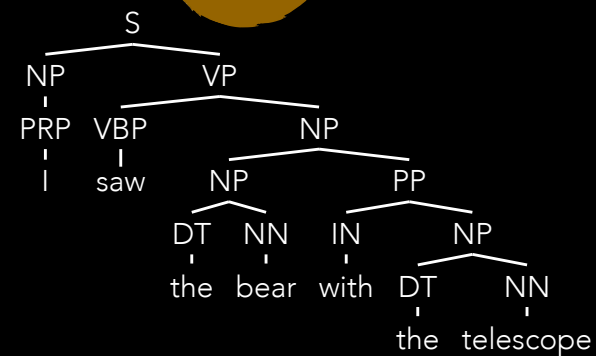
- How does our parser make decisions about which tree to produce?

# But Which Parse Is Best?

- How does our parser make decisions about which tree to produce?

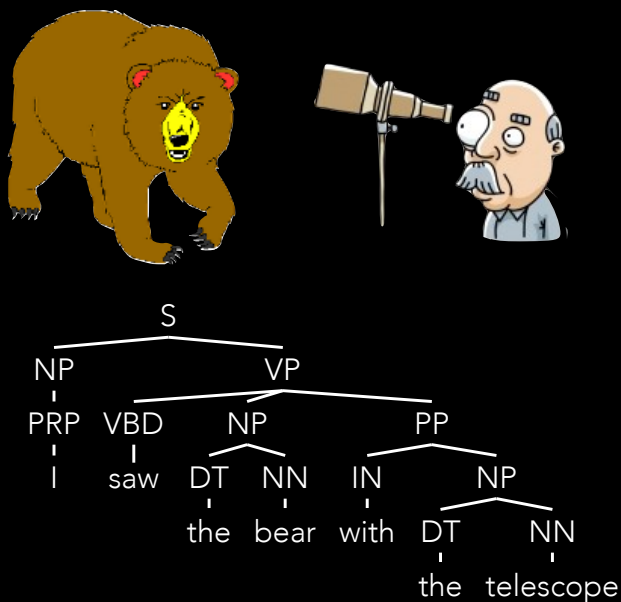


VS

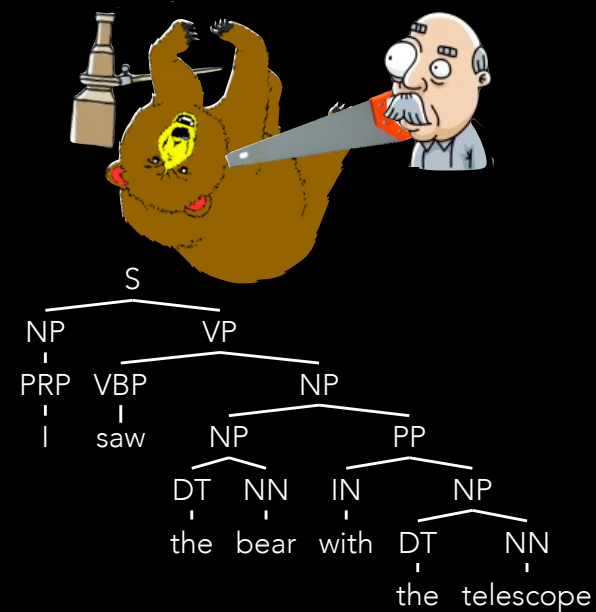


# But Which Parse Is Best?

- How does our parser make decisions about which tree to produce?



VS



- We need a probabilistic CFG and a probability model of trees

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(**start**)

cats I  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$   
 $VP \rightarrow VB NP$   
 $NP \rightarrow NNS$   
 $NP \rightarrow DT NNS$   
 $NNS \rightarrow \text{cats}$   
 $NNS \rightarrow \text{mice}$   
 $VB \rightarrow \text{eat}$

Rules

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(**start**)

cats I  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(**start**)

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mice the  
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$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules

Each rule has a weight  $w$ ,  $0 < w \leq 1$

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(**start**)

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... eat

Terminals

$S \rightarrow NP VP$	1.0
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$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules

Each rule has a weight  $w$ ,  $0 < w \leq 1$

Weights of all rules with the same LHS sum to 1

# Probabilistic Context-Free Grammars

<b>S</b>	NP
VP	NNS
	PP
	DT VB
...	

Nonterminals  
(**start**)

cats	
mice	the
telescope	
...	eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow cats$	0.6
$NNS \rightarrow mice$	0.4
$VB \rightarrow eat$	1.0

Rules

Each rule has a weight  $w$ ,  $0 < w \leq 1$

Weights of all rules with the same LHS sum to 1

Probability of tree is product of  
probability of rules in its derivation



# Probabilistic Context-Free Grammars

S NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(start)

cats I  
mice the  
telescope  
... eat

Terminals  
S

S → NP VP	1.0
VP → VB NP	1.0
NP → NNS	0.2
NP → DT NNS	0.8
NNS → cats	0.6
NNS → mice	0.4
VB → eat	1.0

Rules

1.0

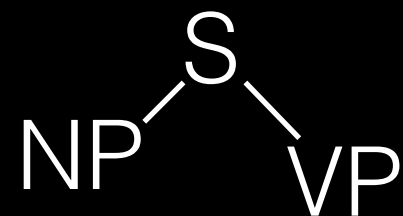
# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

Nonterminals  
(**start**)

cats I  
mice the  
telescope  
... eat

Terminals



<b>S → NP VP</b>	<b>1.0</b>
VP → VB NP	1.0
NP → NNS	0.2
NP → DT NNS	0.8
NNS → cats	0.6
NNS → mice	0.4
VB → eat	1.0

Rules

1.0

# Probabilistic Context-Free Grammars

$S$  NP  
 VP NNS  
 PP  
 ... DT VB

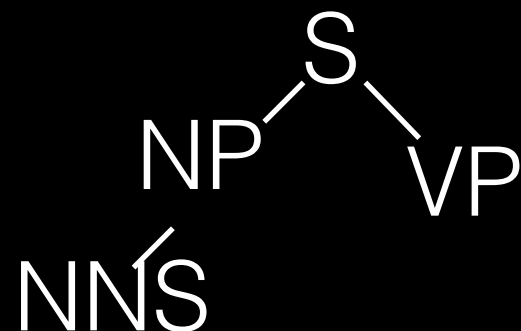
Nonterminals  
( $S$  start)

cats I  
 mice the  
 telescope  
 ... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules



0.2

# Probabilistic Context-Free Grammars

$S$  NP  
 VP NNS  
 PP  
 ... DT VB

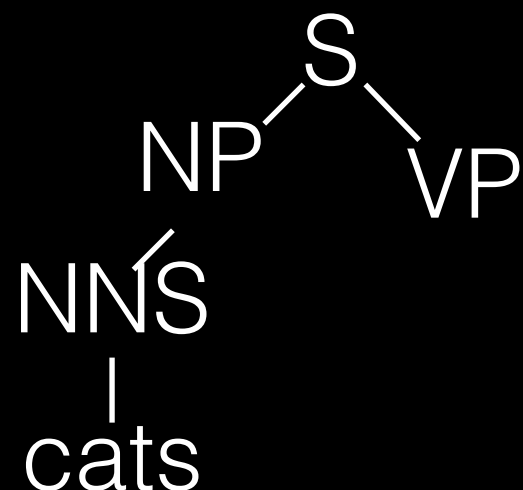
Nonterminals  
(start)

cats |  
 mice the  
 telescope  
 ... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow cats$	0.6
$NNS \rightarrow mice$	0.4
$VB \rightarrow eat$	1.0

Rules



0.12

# Probabilistic Context-Free Grammars

$S$  NP  
 VP NNS  
 PP  
 ... DT VB

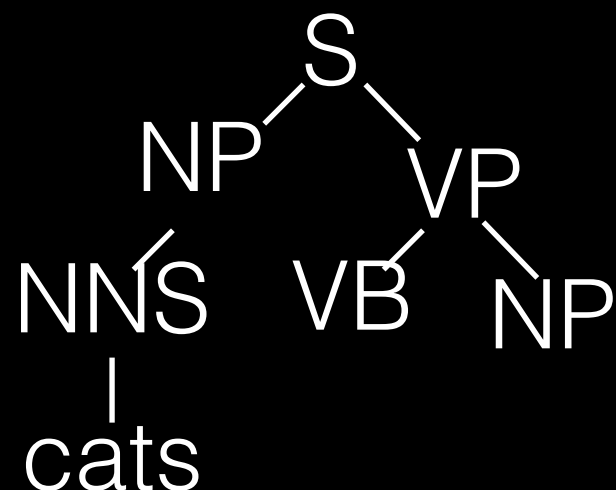
Nonterminals  
(start)

cats I  
 mice the  
 telescope  
 ... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules



0.12

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

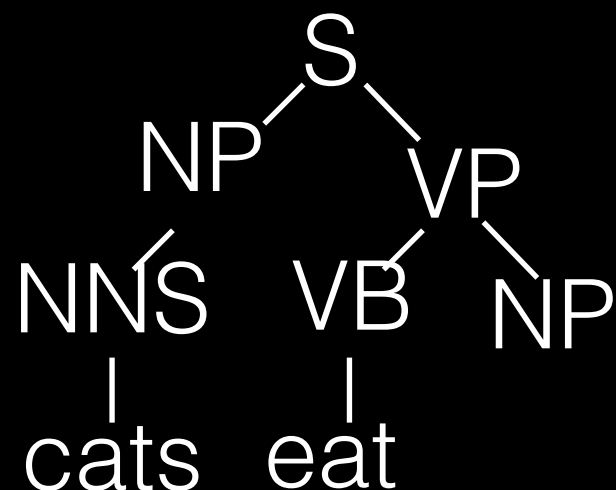
Nonterminals  
(**start**)

cats |  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow cats$	0.6
$NNS \rightarrow mice$	0.4
$VB \rightarrow eat$	1.0

Rules



# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

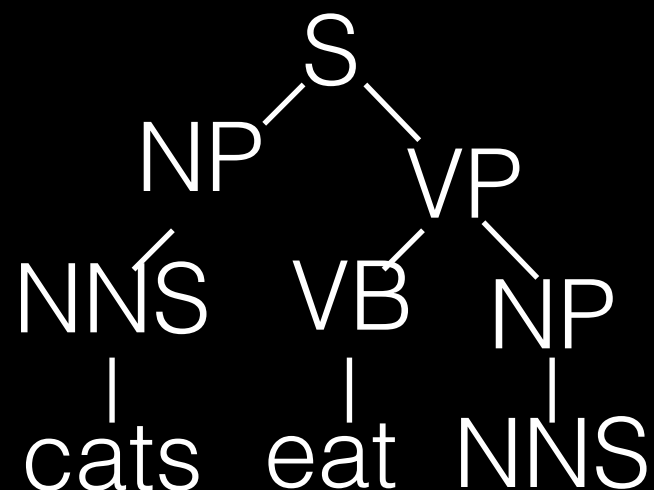
Nonterminals  
(**start**)

cats |  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow \text{cats}$	0.6
$NNS \rightarrow \text{mice}$	0.4
$VB \rightarrow \text{eat}$	1.0

Rules



0.024

# Probabilistic Context-Free Grammars

**S** NP  
VP NNS  
PP  
... DT VB

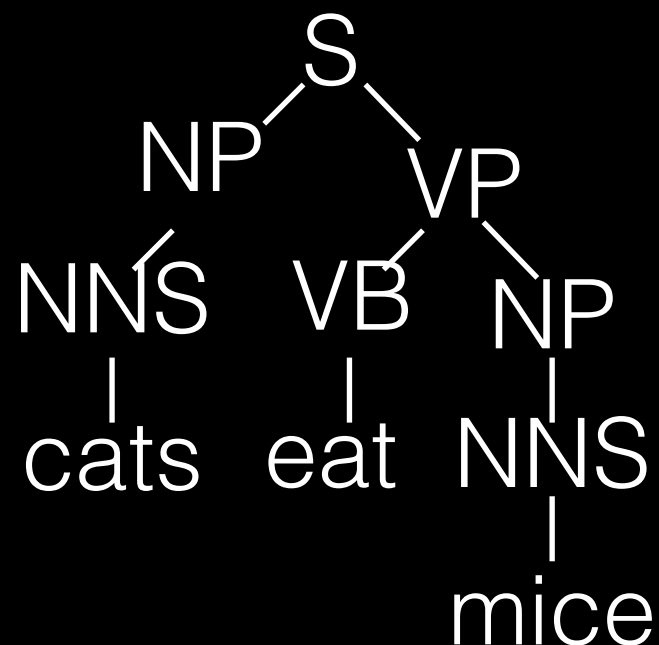
Nonterminals  
(**start**)

cats |  
mice the  
telescope  
... eat

Terminals

$S \rightarrow NP VP$	1.0
$VP \rightarrow VB NP$	1.0
$NP \rightarrow NNS$	0.2
$NP \rightarrow DT NNS$	0.8
$NNS \rightarrow cats$	0.6
$NNS \rightarrow mice$	0.4
$VB \rightarrow eat$	1.0

Rules





# Viterbi (one-best) CKY for PCFG

# Viterbi (one-best) CKY for PCFG

- Before:
  - we built states  $[X, i, j]$  denoting coverage of span from  $i$  to  $j$  with symbol  $X$
  - we stored all  $\{X \rightarrow YZ, k\}$  backpointer

# Viterbi (one-best) CKY for PCFG

- Before:
  - we built states  $[X, i, j]$  denoting coverage of span from  $i$  to  $j$  with symbol  $X$
  - we stored all  $\{X \rightarrow YZ, k\}$  backpointer
- New:
  - when deriving via  $\{R, k\}$ , set  $\text{best}([X, i, j]) = p(R) * \text{best}([Y, i, k]) * \text{best}([Z, k, j])$  if this is greater than current value for  $\text{best}([X, i, j])$
  - only keep backpointer if best is updated
  - chart contains only the best derivation at end of algorithm

	time	flies	like	an	arrow
	[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP <sup>1.0</sup>					
NP → DT NN <sup>0.3</sup>	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time <sup>0.05</sup>   fruit <sup>0.05</sup>					
NP → NN NNS <sup>0.6</sup>			[2,3]	[2,4]	[2,5]
VP → VBP NP <sup>0.7</sup>					
VP → flies <sup>0.1</sup>					
VP → VP PP <sup>0.2</sup>				[3,4]	[3,5]
PP → IN NP <sup>1.0</sup>					
DT → a <sup>0.5</sup>   an <sup>0.5</sup>					
NN → time <sup>0.25</sup>   fruit <sup>0.25</sup>   arrow <sup>0.25</sup>   banana <sup>0.25</sup>					[4,5]
NNS → flies <sup>1.0</sup>					
VBP → like <sup>1.0</sup>					
IN → like <sup>1.0</sup>					

	time	flies	like	an	arrow
	<div>NP 0.05</div> <div>NN 0.25</div> <div>[0,1]</div>	[0,2]	[0,3]	[0,4]	[0,5]
S → NP VP 1.0					
NP → DT NN 0.3	[1,2]	[1,3]	[1,4]	[1,5]	
NP → time 0.05 fruit 0.05					
NP → NN NNS 0.6		[2,3]	[2,4]	[2,5]	
VP → VBP NP 0.7					
VP → flies 0.1					
VP → VP PP 0.2			[3,4]	[3,5]	
PP → IN NP 1.0					
DT → a 0.5 an 0.5					
NN → time 0.25 fruit 0.25 arrow 0.25 banana 0.25					[4,5]

NNS → flies 1.0  
 VBP → like 1.0  
 IN → like 1.0

best() for bottom of the chart  
 is simply the rule probability

	time	flies	like	an	arrow
	NP <sup>0.05</sup> NN <sup>0.25</sup> [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
		VP <sup>0.1</sup> NNS <sup>1.0</sup> [1,2]	[1,3]	[1,4]	[1,5]
			[2,3]	[2,4]	[2,5]
				[3,4]	[3,5]
					[4,5]

- S → NP VP<sup>1.0</sup>
- NP → DT NN<sup>0.3</sup>
- NP → time<sup>0.05</sup> | fruit<sup>0.05</sup>
- NP → NN NNS<sup>0.6</sup>
- VP → VBP NP<sup>0.7</sup>
- VP → flies<sup>0.1</sup>
- VP → VP PP<sup>0.2</sup>
- PP → IN NP<sup>1.0</sup>
- DT → a<sup>0.5</sup> | an<sup>0.5</sup>
- NN → time<sup>0.25</sup> | fruit<sup>0.25</sup> | arrow<sup>0.25</sup> | banana<sup>0.25</sup>
- NNS → flies<sup>1.0</sup>
- VBP → like<sup>1.0</sup>
- IN → like<sup>1.0</sup>

best() for bottom of the chart  
is simply the rule probability

	time	flies	like	an	arrow
<p> <math>S \rightarrow NP VP</math> 1.0  <math>NP \rightarrow DT NN</math> 0.3  <math>NP \rightarrow time   fruit</math> 0.05 0.05  <math>NP \rightarrow NN NNS</math> 0.6  <math>VP \rightarrow VBP NP</math> 0.7  <math>VP \rightarrow flies</math> 0.1  <math>VP \rightarrow VP PP</math> 0.2  <math>PP \rightarrow IN NP</math> 1.0  <math>DT \rightarrow a   an</math> 0.5 0.5  <math>NN \rightarrow time   fruit   arrow   banana</math> 0.25 0.25 0.25 0.25  <math>NNS \rightarrow flies</math> 1.0  <math>VBP \rightarrow like</math> 1.0  <math>IN \rightarrow like</math> 1.0 </p>	$NP$ 0.05 $NN$ 0.25 [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	$VP$ 0.1 $NNS$ 1.0 [1,2]	[1,3]	[1,4]	[1,5]	
		$IN$ 1.0 $VBP$ 1.0 [2,3]	[2,4]	[2,5]	
			[3,4]	[3,5]	
					[4,5]

best() for bottom of the chart  
is simply the rule probability

	time	flies	like	an	arrow
<p> <math>S \rightarrow NP VP</math> 1.0  <math>NP \rightarrow DT NN</math> 0.3  <math>NP \rightarrow time   fruit</math> 0.05 0.05  <math>NP \rightarrow NN NNS</math> 0.6  <math>VP \rightarrow VBP NP</math> 0.7  <math>VP \rightarrow flies</math> 0.1  <math>VP \rightarrow VP PP</math> 0.2  <math>PP \rightarrow IN NP</math> 1.0  <math>DT \rightarrow a   an</math> 0.5 0.5  <math>NN \rightarrow time   fruit   arrow   banana</math> 0.25 0.25 0.25 0.25  <math>NNS \rightarrow flies</math> 1.0  <math>VBP \rightarrow like</math> 1.0  <math>IN \rightarrow like</math> 1.0 </p>	$NP$ 0.05 $NN$ 0.25 [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	$VP$ 0.1 $NNS$ 1.0 [1,2]	[1,3]	[1,4]	[1,5]	
		$IN$ 1.0 $VBP$ 1.0 [2,3]	[2,4]	[2,5]	
			$DT$ 0.5 [3,4]	[3,5]	
					[4,5]

best() for bottom of the chart is simply the rule probability



time flies like an arrow

NP 0.05  
NN 0.25  
[0,1]

VP 0.1  
NNS 1.0  
[1,2]

IN 1.0  
VBP 1.0  
[2,3]

DT 0.5  
[3,4]

NN 0.25  
[4,5]

S → NP VP 1.0  
NP → DT NN 0.3  
NP → time | fruit 0.05  
NP → NN NNS 0.6  
VP → VBP NP 0.7  
VP → flies 0.1  
VP → VP PP 0.2  
PP → IN NP 1.0  
DT → a | an 0.5  
NN → time | fruit | arrow | banana 0.25  
NNS → flies 1.0  
VBP → like 1.0  
IN → like 1.0

best() for bottom of the chart is simply the rule probability

	time	flies	like	an	arrow
S → NP VP <sup>1.0</sup> NP → DT NN <sup>0.3</sup> NP → time <sup>0.05</sup>   fruit <sup>0.05</sup> NP → NN NNS <sup>0.6</sup> VP → VBP NP <sup>0.7</sup> VP → flies <sup>0.1</sup> VP → VP PP <sup>0.2</sup> PP → IN NP <sup>1.0</sup> DT → a <sup>0.5</sup>   an <sup>0.5</sup> NN → time <sup>0.25</sup>   fruit <sup>0.25</sup>   arrow <sup>0.25</sup>   banana <sup>0.25</sup> NNS → flies <sup>1.0</sup> VBP → like <sup>1.0</sup> IN → like <sup>1.0</sup>	NP <sup>0.05</sup> NN <sup>0.25</sup> [0,1]	[0,2]	[0,3]	[0,4]	[0,5]
		VP <sup>0.1</sup> NNS <sup>1.0</sup> [1,2]	[1,3]	[1,4]	[1,5]
			IN <sup>1.0</sup> VBP <sup>1.0</sup> [2,3]	[2,4]	[2,5]
				DT <sup>0.5</sup> [3,4]	[3,5]
					NN <sup>0.25</sup> [4,5]
Now multiply rule by best() of descendants					

	time	flies	like	an	arrow
	<div>NP<sup>0.05</sup></div> <div>NN<sup>0.25</sup></div> <div>[0,1]</div>	<div>S<sup>0.005</sup></div> <div>NP<sup>0.15</sup></div> <div>[0,2]</div>	[0,3]	[0,4]	[0,5]
<div>S → NP VP<sup>1.0</sup></div> <div>NP → DT NN<sup>0.3</sup></div> <div>NP → time<sup>0.05</sup>   fruit<sup>0.05</sup></div> <div>NP → NN NNS<sup>0.6</sup></div> <div>VP → VBP NP<sup>0.7</sup></div> <div>VP → flies<sup>0.1</sup></div> <div>VP → VP PP<sup>0.2</sup></div> <div>PP → IN NP<sup>1.0</sup></div> <div>DT → a<sup>0.5</sup>   an<sup>0.5</sup></div> <div>NN → time<sup>0.25</sup>   fruit<sup>0.25</sup>   arrow<sup>0.25</sup>   banana<sup>0.25</sup></div>	<div>VP<sup>0.1</sup></div> <div>NNS<sup>1.0</sup></div> <div>[1,2]</div>	[1,3]	[1,4]	[1,5]	
			<div>IN<sup>1.0</sup></div> <div>VBP<sup>1.0</sup></div> <div>[2,3]</div>	[2,4]	[2,5]
				<div>DT<sup>0.5</sup></div> <div>[3,4]</div>	[3,5]
					<div>NN<sup>0.25</sup></div> <div>[4,5]</div>

$1.0 \cdot .05 \cdot .1 = .005$   
 $.6 \cdot .25 \cdot 1.0 = .15$

	time	flies	like	an	arrow
	<div>NP<sup>0.05</sup></div> <div>NN<sup>0.25</sup></div> <div>[0,1]</div>	<div>S<sup>0.005</sup></div> <div>NP<sup>0.15</sup></div> <div>[0,2]</div>	[0,3]	[0,4]	<div>0.0000375</div> <div>S</div> <div>[0,5]</div>
<div>S → NP VP<sup>1.0</sup></div> <div>NP → DT NN<sup>0.3</sup></div> <div>NP → time<sup>0.05</sup>   fruit<sup>0.05</sup></div> <div>NP → NN NNS<sup>0.6</sup></div> <div>VP → VBP NP<sup>0.7</sup></div> <div>VP → flies<sup>0.1</sup></div> <div>VP → VP PP<sup>0.2</sup></div> <div>PP → IN NP<sup>1.0</sup></div> <div>DT → a<sup>0.5</sup>   an<sup>0.5</sup></div> <div>NN → time<sup>0.25</sup>   fruit<sup>0.25</sup>   arrow<sup>0.25</sup>   banana<sup>0.25</sup></div> <div>NNS → flies<sup>1.0</sup></div> <div>VBP → like<sup>1.0</sup></div> <div>IN → like<sup>1.0</sup></div>		<div>VP<sup>0.1</sup></div> <div>NNS<sup>1.0</sup></div> <div>[1,2]</div>	[1,3]	[1,4]	<div>0.00075</div> <div>VP</div> <div>[1,5]</div>
			<div>IN<sup>1.0</sup></div> <div>VBP<sup>1.0</sup></div> <div>[2,3]</div>	[2,4]	[2,5]
				<div>DT<sup>0.5</sup></div> <div>[3,4]</div>	<div>0.0375</div> <div>NP</div> <div>[3,5]</div>
					<div>NN<sup>0.25</sup></div> <div>[4,5]</div>

best(S) = 1\*.05\*.00075 = .0000375

	time	flies	like	an	arrow
	NP <sup>0.05</sup> NN <sup>0.25</sup> [0,1]	<div>S<sup>0.005</sup> NP<sup>0.15</sup> [0,2]</div>	[0,3]	[0,4]	<div>0.0039375 S [0,5]</div>
<div>S → NP VP<sup>1.0</sup></div>	NP → DT NN <sup>0.3</sup> NP → time <sup>0.05</sup>   fruit <sup>0.05</sup> NP → NN NNS <sup>0.6</sup> VP → VBP NP <sup>0.7</sup> VP → flies <sup>0.1</sup> VP → VP PP <sup>0.2</sup> PP → IN NP <sup>1.0</sup> DT → a <sup>0.5</sup>   an <sup>0.5</sup> NN → time <sup>0.25</sup>   fruit <sup>0.25</sup>   arrow <sup>0.25</sup>   banana <sup>0.25</sup>	VP <sup>0.1</sup> NNS <sup>1.0</sup> [1,2]	[1,3]	[1,4]	0.00075 VP [1,5]
			IN <sup>1.0</sup> VBP <sup>1.0</sup> [2,3]	[2,4]	<div>0.0375 PP<sup>0.0375</sup> VP<sup>0.02625</sup> [2,5]</div>
				DT <sup>0.5</sup> [3,4]	0.0375 NP [3,5]
					NN <sup>0.25</sup> [4,5]

NNS → flies<sup>1.0</sup>  
 VBP → like<sup>1.0</sup>  
 IN → like<sup>1.0</sup>

can also derive as  
 $1 * .15 * .02625 = .0039375$   
 so update best and change backpointer

	time	flies	like	an	arrow
	NP <sup>0.05</sup> NN <sup>0.25</sup> [0,1]	S <sup>0.005</sup> NP <sup>0.15</sup> [0,2]	[0,3]	[0,4]	0.0039375 S [0,5]
S → NP VP <sup>1.0</sup> NP → DT NN <sup>0.3</sup> NP → time <sup>0.05</sup>   fruit <sup>0.05</sup> NP → NN NNS <sup>0.6</sup> VP → VBP NP <sup>0.7</sup> VP → flies <sup>0.1</sup> VP → VP PP <sup>0.2</sup> PP → IN NP <sup>1.0</sup> DT → a <sup>0.5</sup>   an <sup>0.5</sup> NN → time <sup>0.25</sup>   fruit <sup>0.25</sup>   arrow <sup>0.25</sup>   banana <sup>0.25</sup> NNS → flies <sup>1.0</sup> VBP → like <sup>1.0</sup> IN → like <sup>1.0</sup>		VP <sup>0.1</sup> NNS <sup>1.0</sup> [1,2]	[1,3]	[1,4]	0.00075 VP [1,5]
			IN <sup>1.0</sup> VBP <sup>1.0</sup> [2,3]	[2,4]	PP <sup>0.0375</sup> VP <sup>0.02625</sup> [2,5]
				DT <sup>0.5</sup> [3,4]	0.0375 NP [3,5]
					NN <sup>0.25</sup> [4,5]

If we wanted the probability of ALL parses of this sentence, sum multiple derivations instead of max (= .0039375+ .0000375)

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- We discovered our rule set by reading training trees.
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- Maximum likelihood estimate = fancy name for count and divide
- If we see NP 1000 times in training, and we see NP -> DT NN 150 times, then  $p(\text{NP} \rightarrow \text{DT NN}) = 150/1000 = .15$

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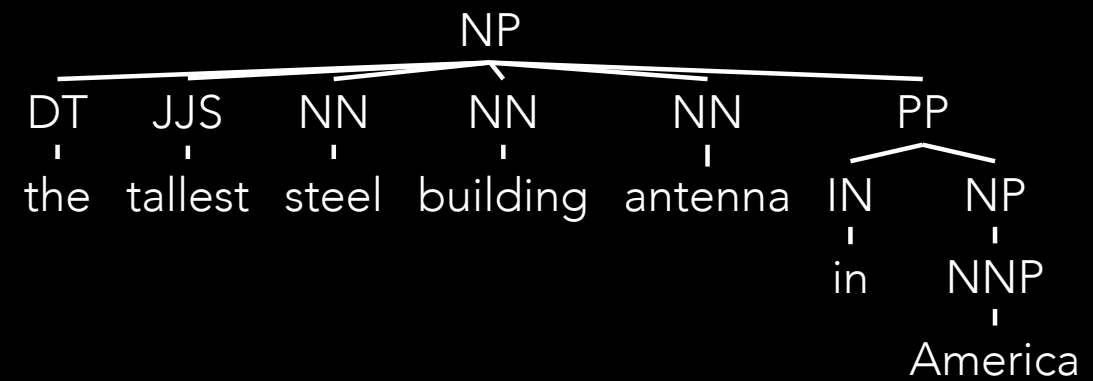
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- Using the approach just described (“vanilla PCFG”), a CKY parser scores about 73% F1. State of the art parsers are in the mid-90s
- Why so bad?
  - Rules are too specific
  - Rules are not specific enough

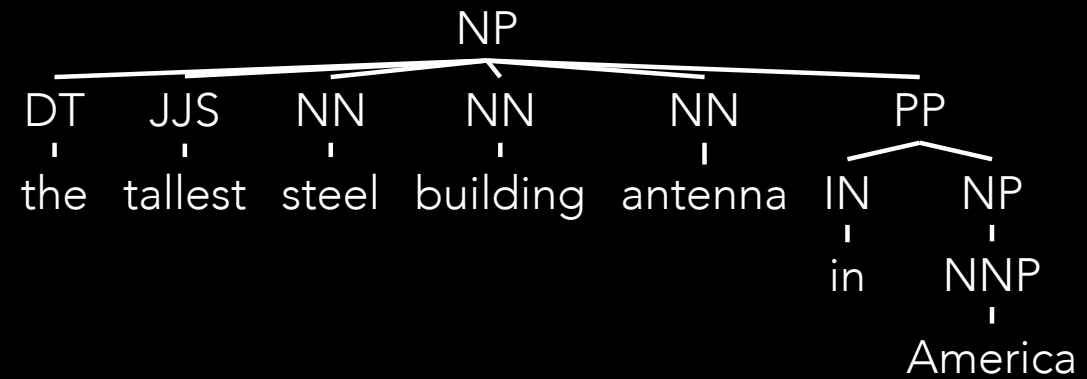


# Too Specific



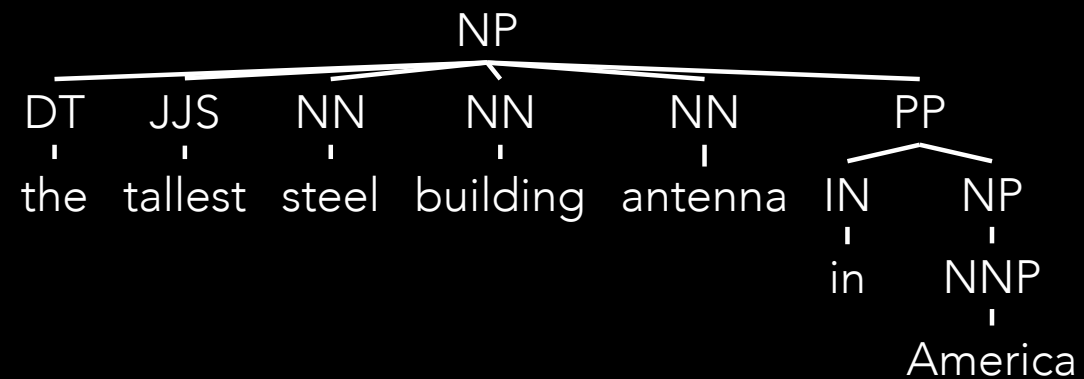
# Too Specific

If we see this  
tree:



# Too Specific

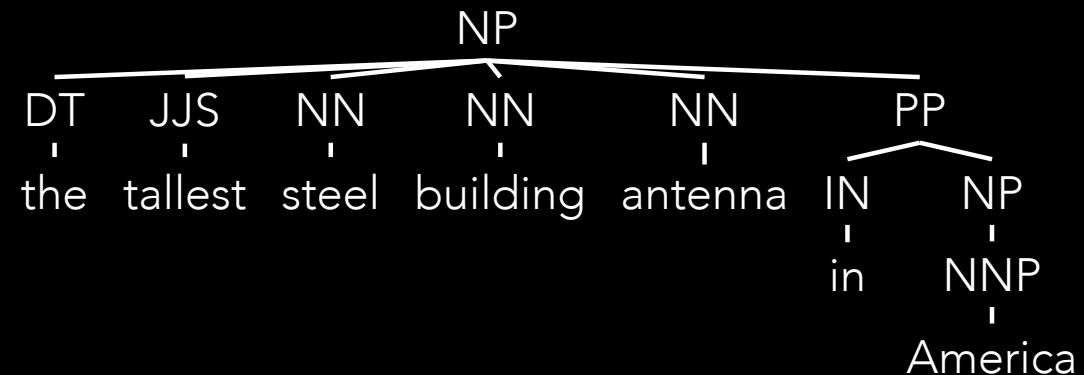
If we see this  
tree:



We get this rule:  $NP \rightarrow DT\ JJS\ NN\ NN\ NN\ PP$

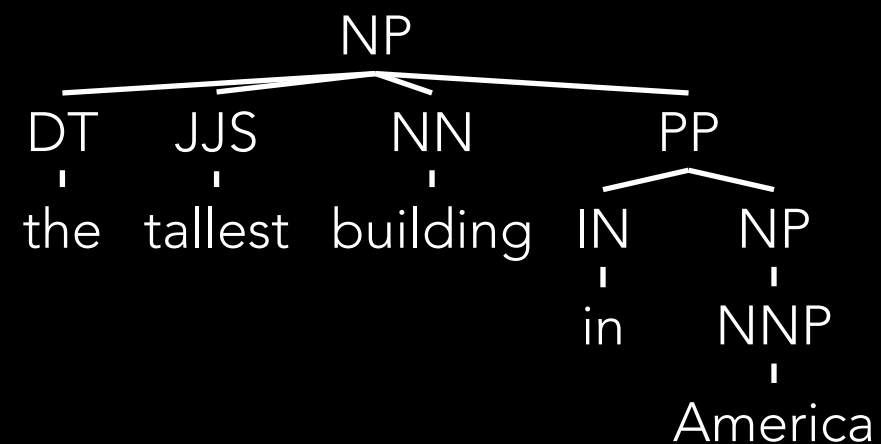
# Too Specific

If we see this  
tree:



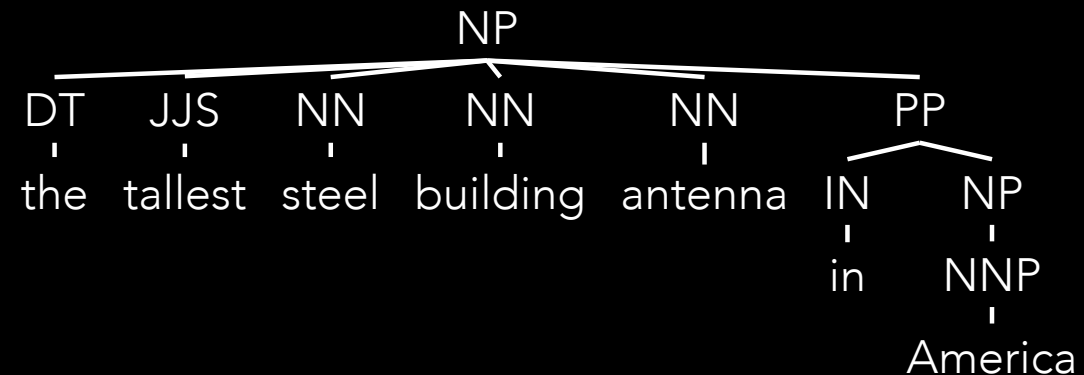
We get this rule: NP -> DT JJS NN NN NN PP

But we can't parse  
this tree:



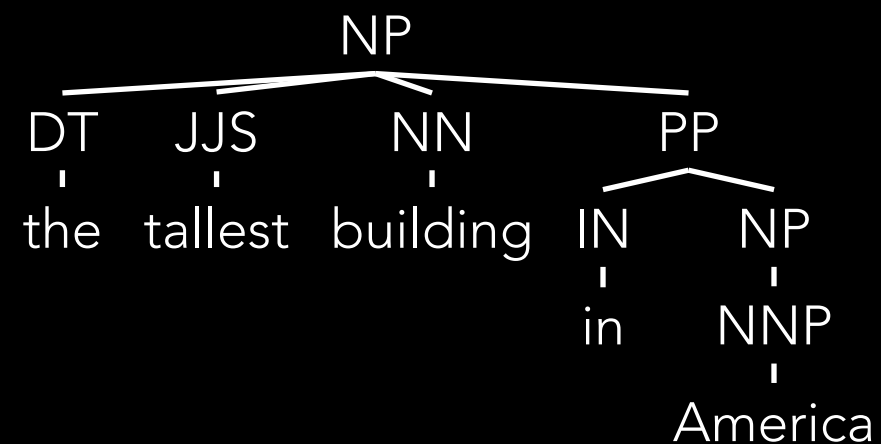
# Too Specific

If we see this  
tree:



We get this rule: NP -> DT JJS NN NN NN PP

But we can't parse  
this tree:



without this rule: NP -> DT JJS NN PP

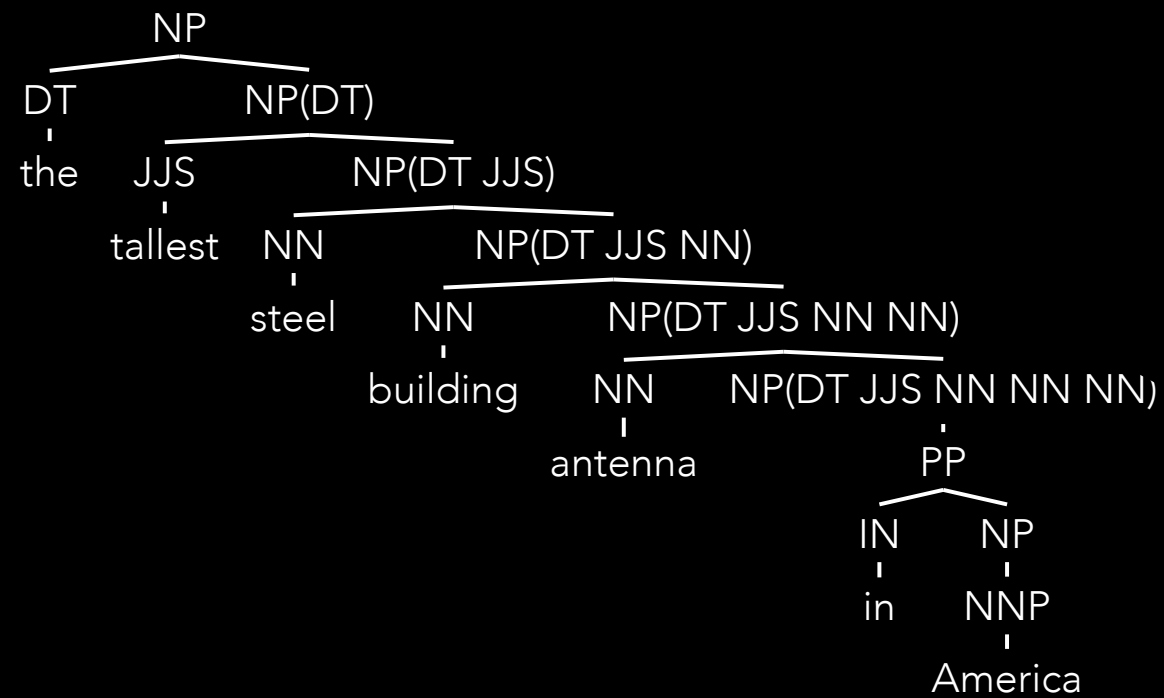
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Recall that for  
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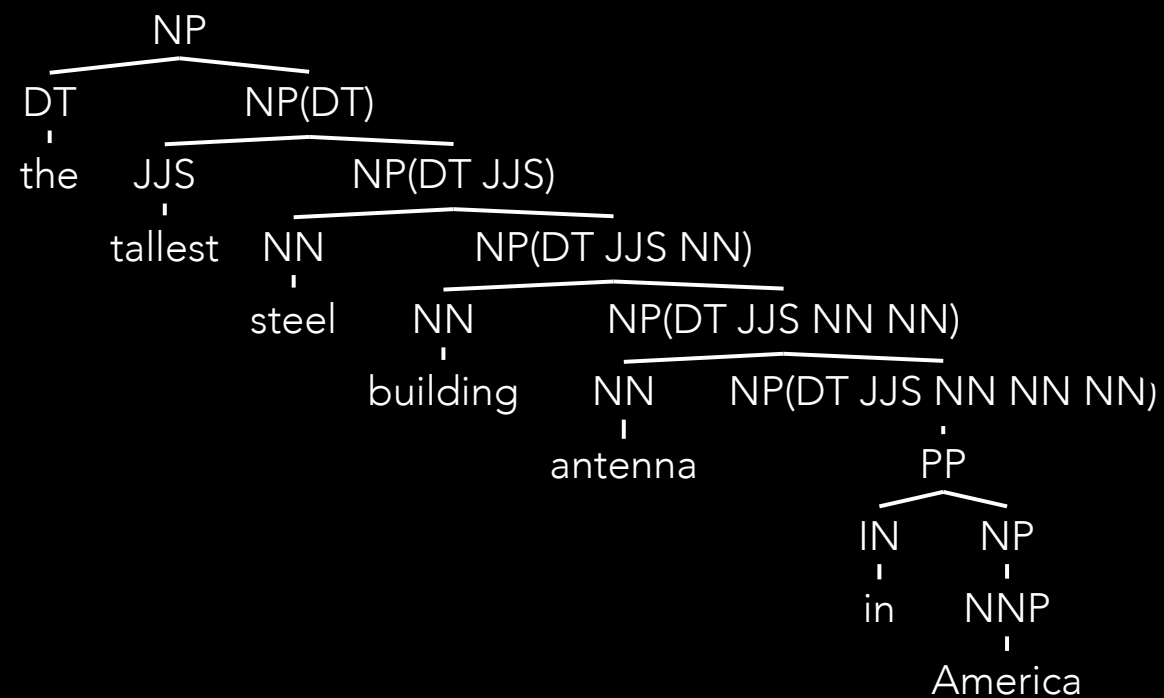




# Too Specific

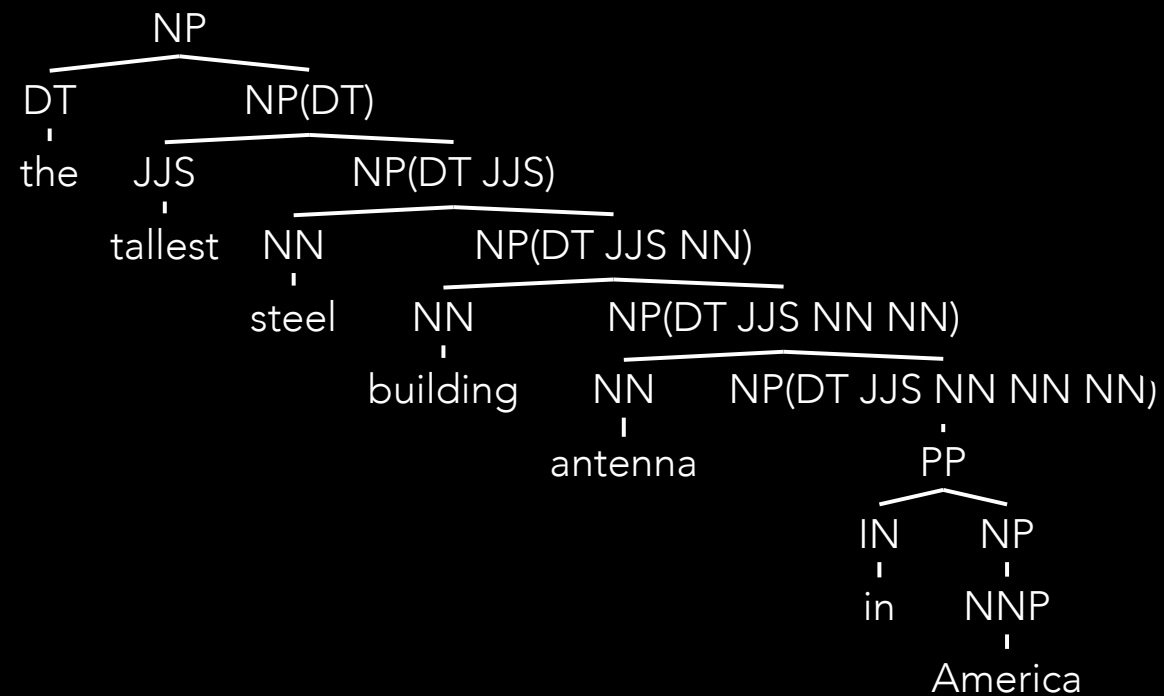
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That still doesn't help!



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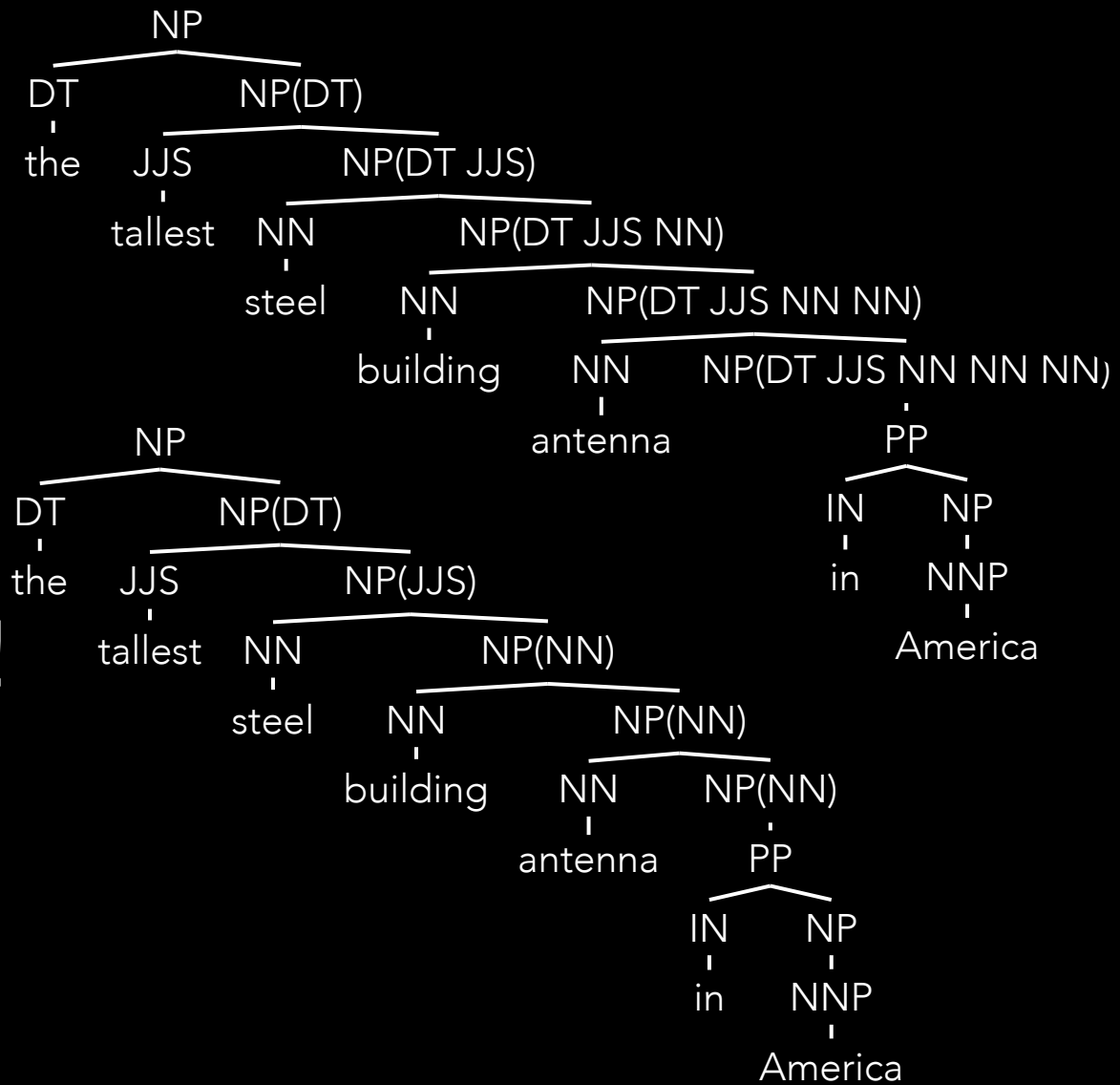
What if we only  
remembered one  
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CKY purposes  
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# That still doesn't help!

What if we only remembered one sibling?

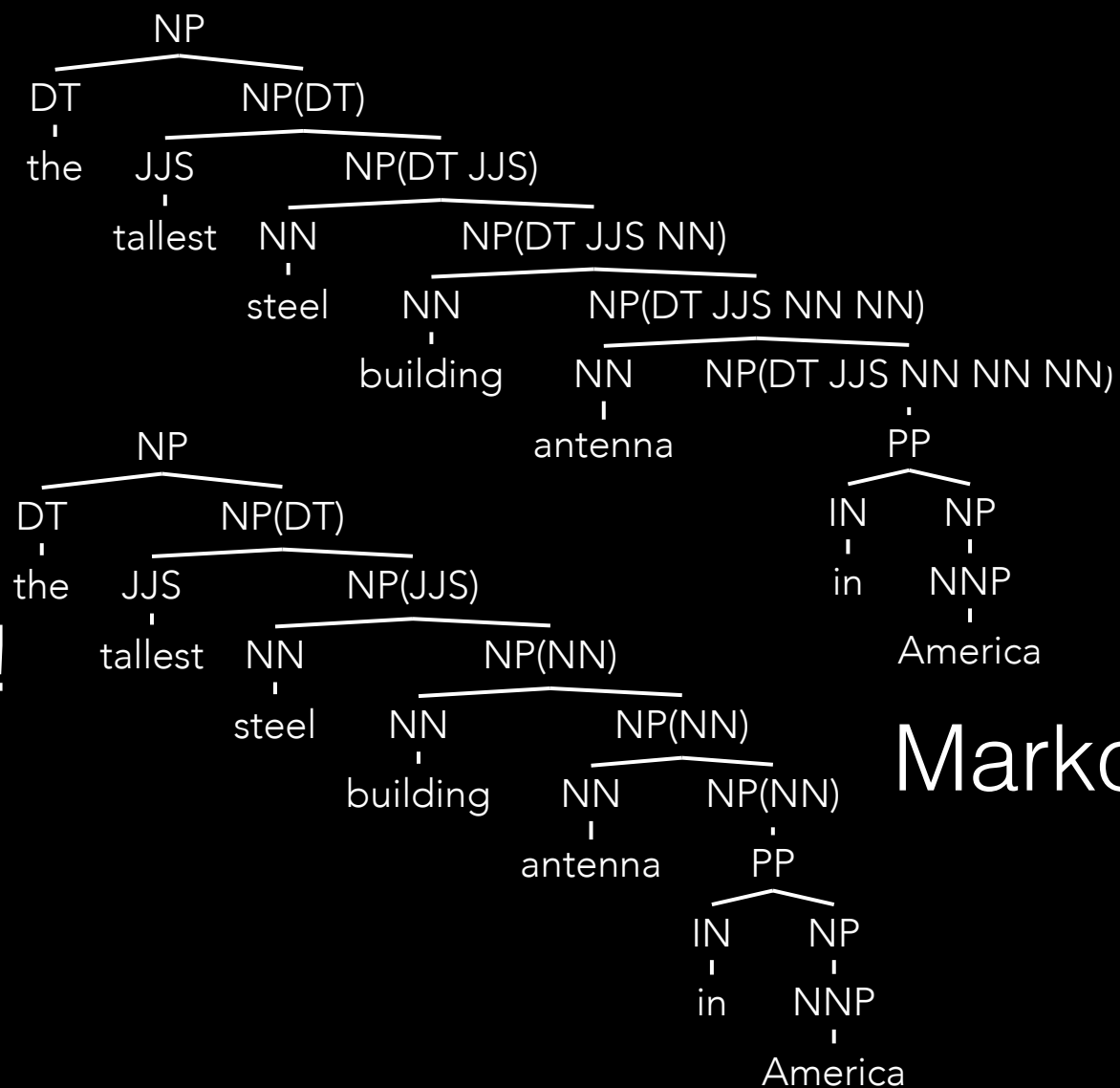


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CKY purposes  
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That still doesn't help!

What if we only  
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Markovization!

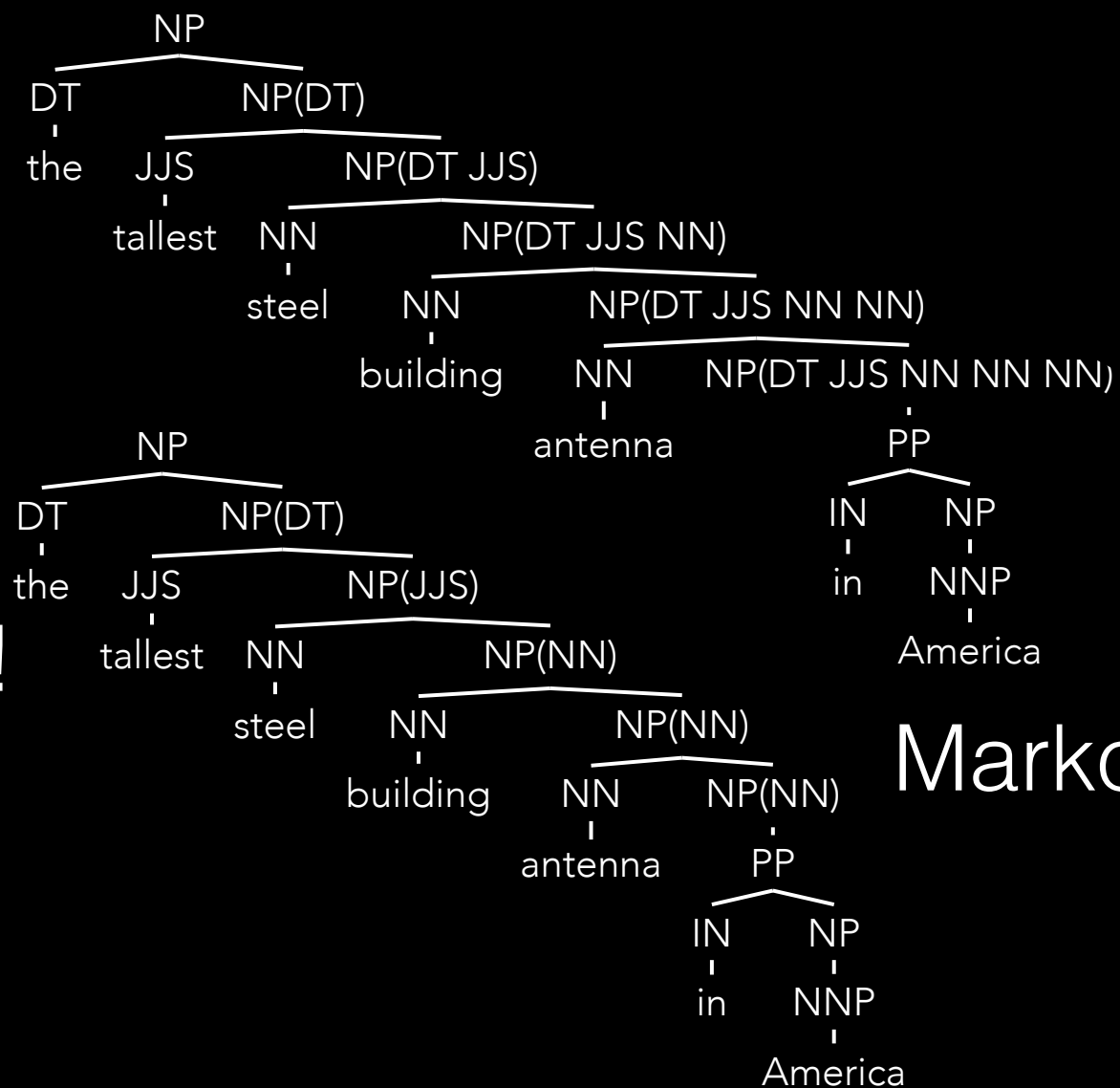
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What if we only remembered one sibling?

Now we have the rules we need



Markovization!

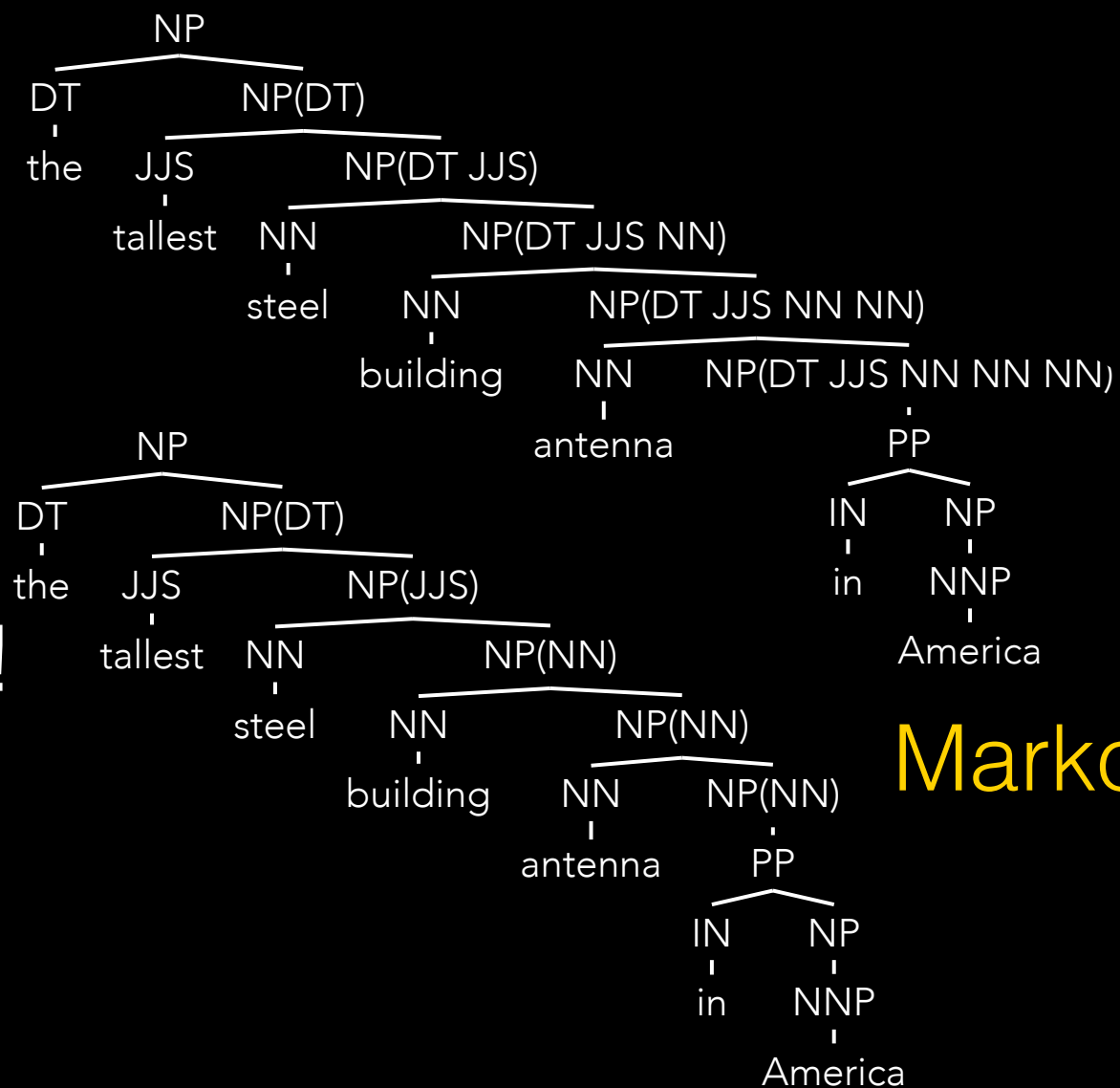
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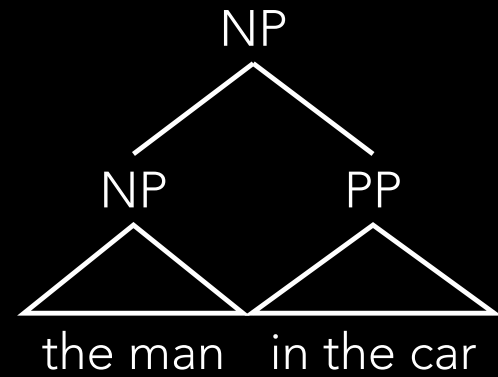
Markovization!

Can experiment with keeping more or less context

# Not Specific Enough (I)

If we saw

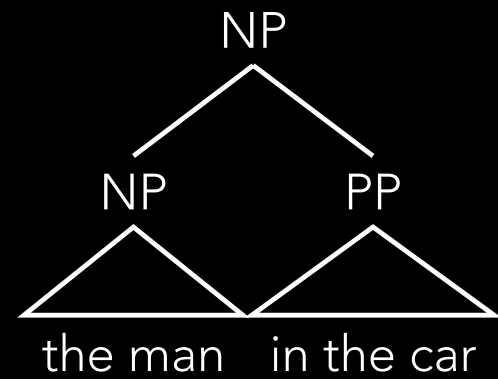
# Not Specific Enough (I)



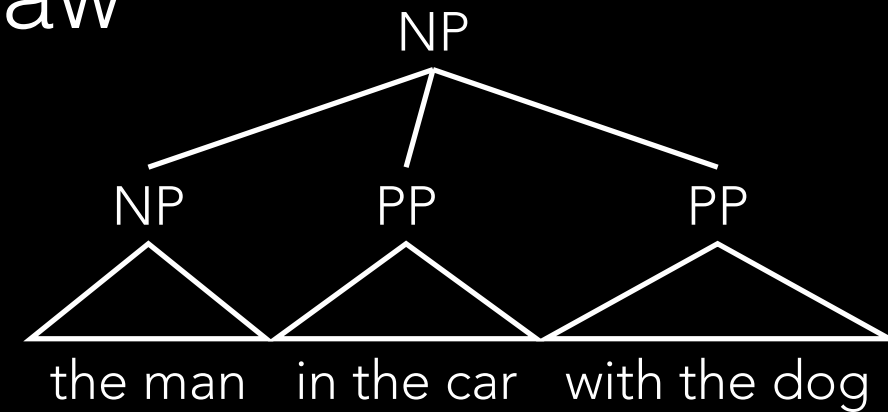
If we saw  
90  
times



# Not Specific Enough (I)

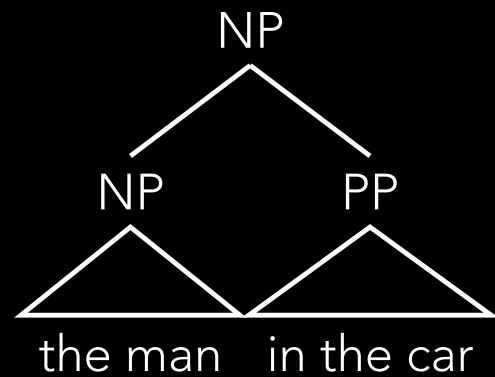


If we saw  
90  
times

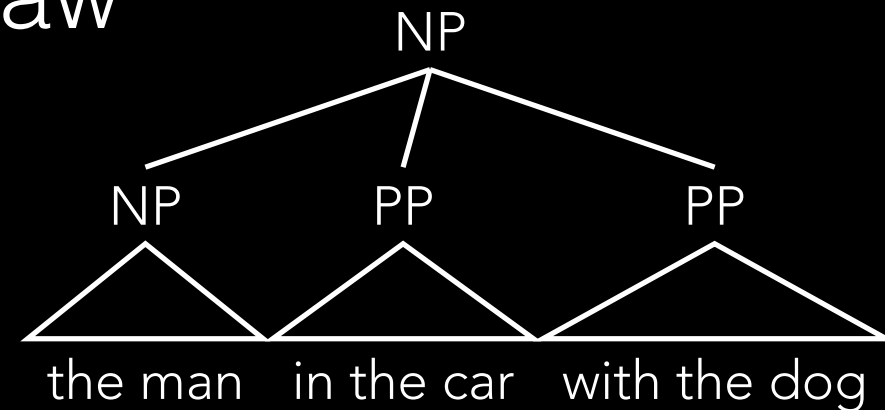


10  
times

# Not Specific Enough (I)



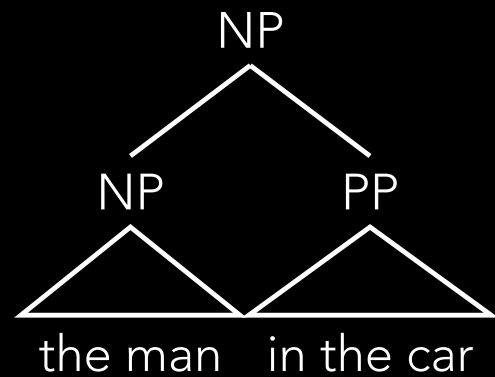
If we saw  
90  
times



10  
times

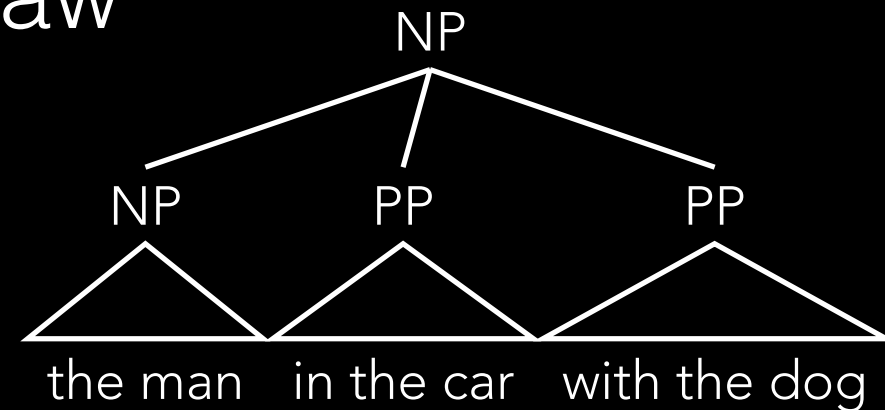
$$p(\text{NP} \rightarrow \text{NP PP}) \\ = 90/200 = .45$$

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90  
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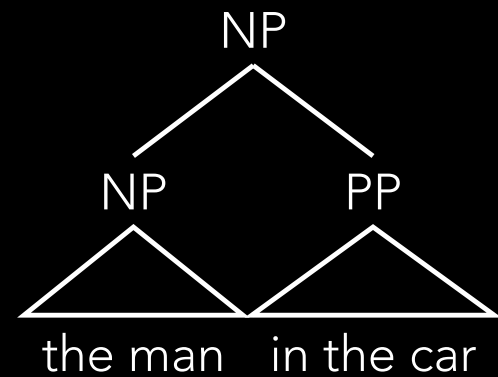
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10  
times

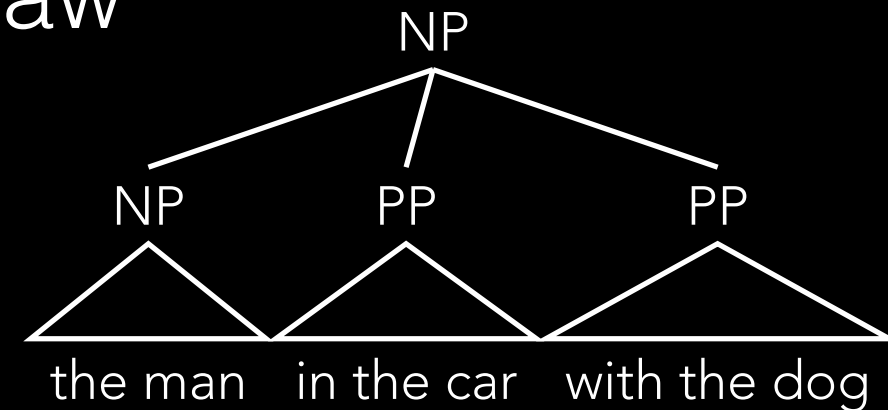
$$p(\text{NP} \rightarrow \text{NP PP PP}) \\ = 10/200 = .05$$

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90  
times

$$p(\text{NP} \rightarrow \text{NP PP}) \\ = 90/200 = .45$$

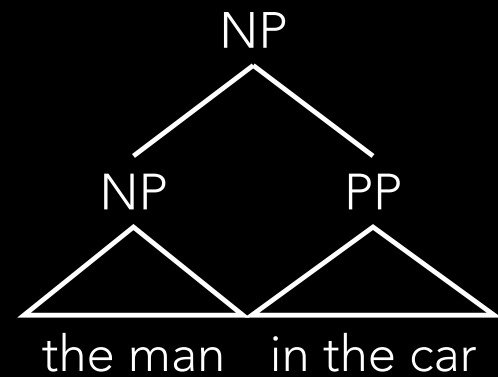


10  
times

$$p(\text{NP} \rightarrow \text{NP PP PP}) \\ = 10/200 = .05$$

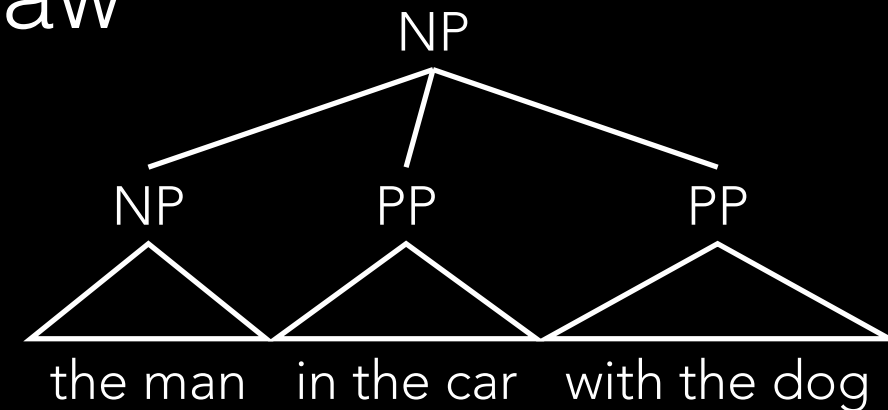
How would we score parses of “the man in the car with the dog”?

# Not Specific Enough (I)



If we saw  
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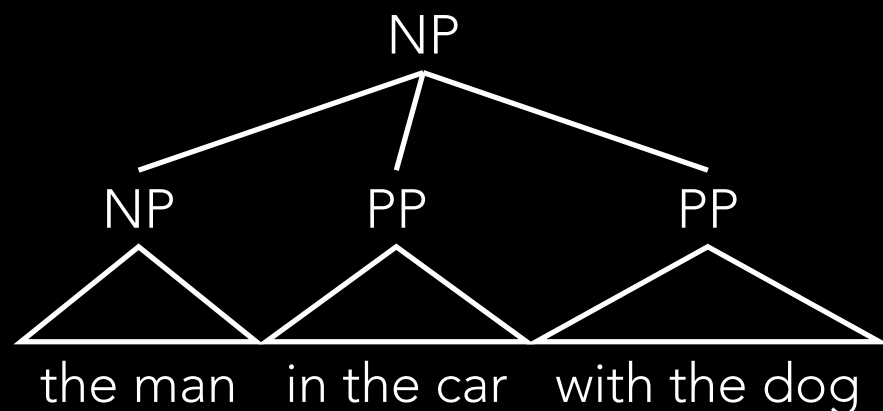
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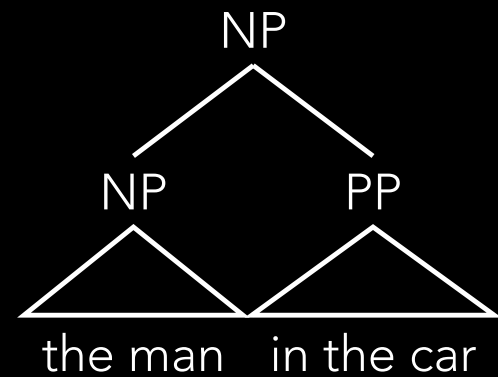
10  
times

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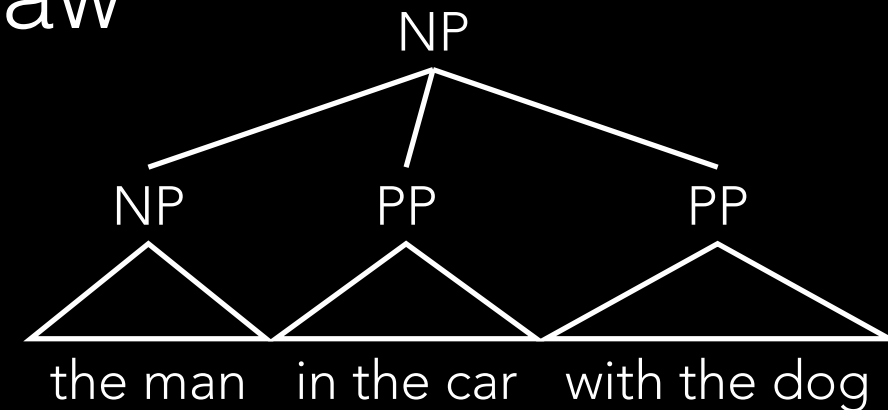
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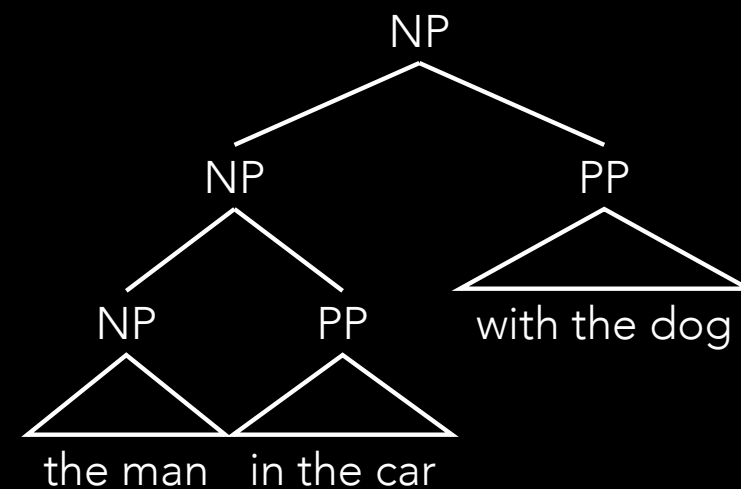
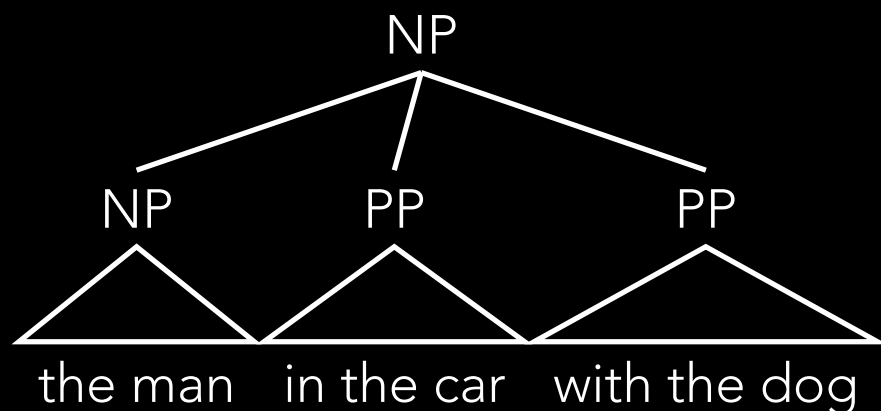


10  
times

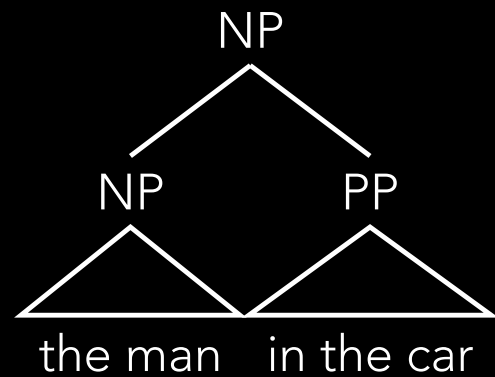
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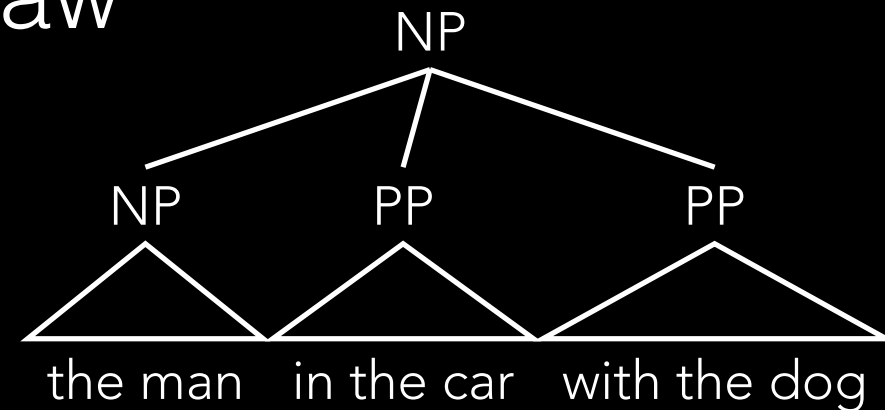


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If we saw  
90  
times

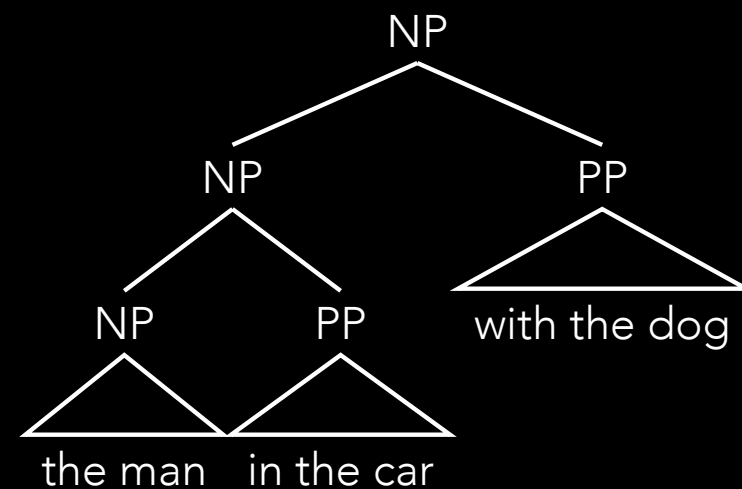
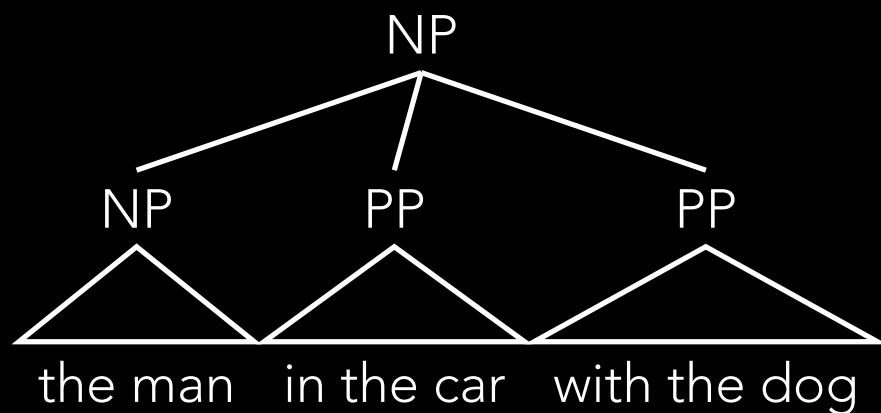
$$p(\text{NP} \rightarrow \text{NP PP}) \\ = 90/200 = .45$$



10  
times

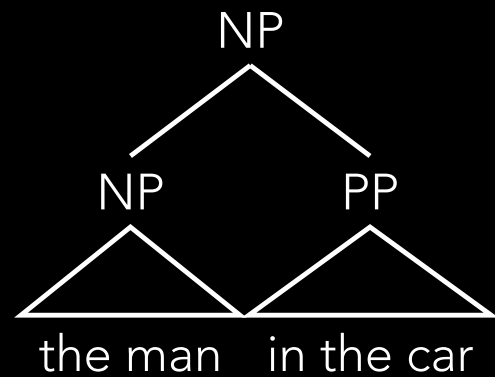
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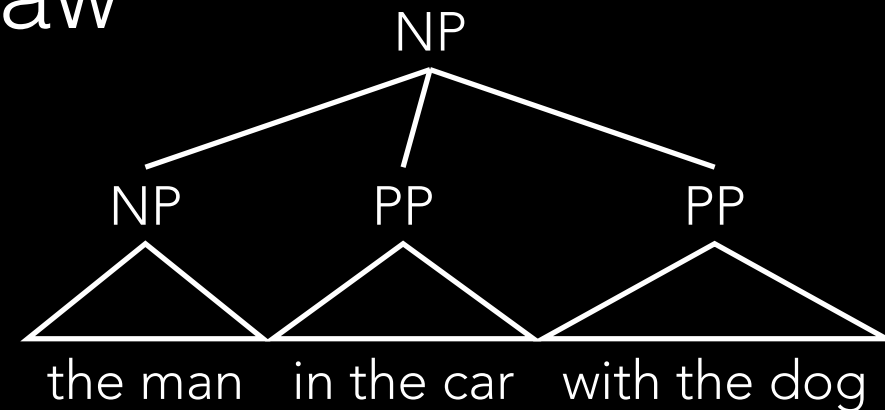
.05x...

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If we saw  
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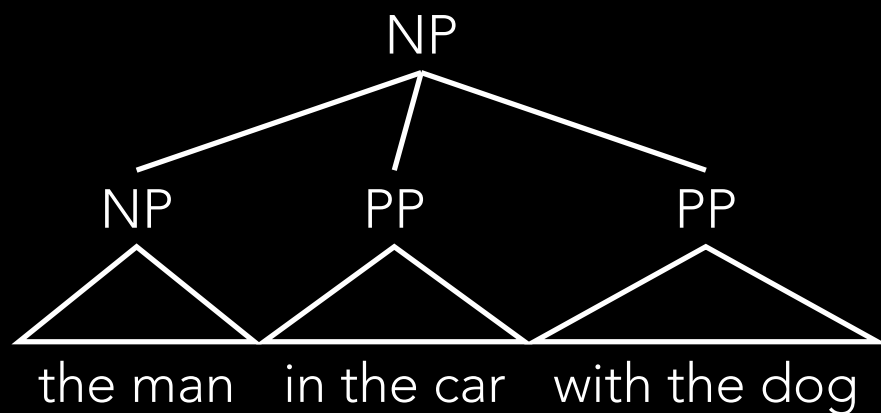
$$p(\text{NP} \rightarrow \text{NP PP}) \\ = 90/200 = .45$$



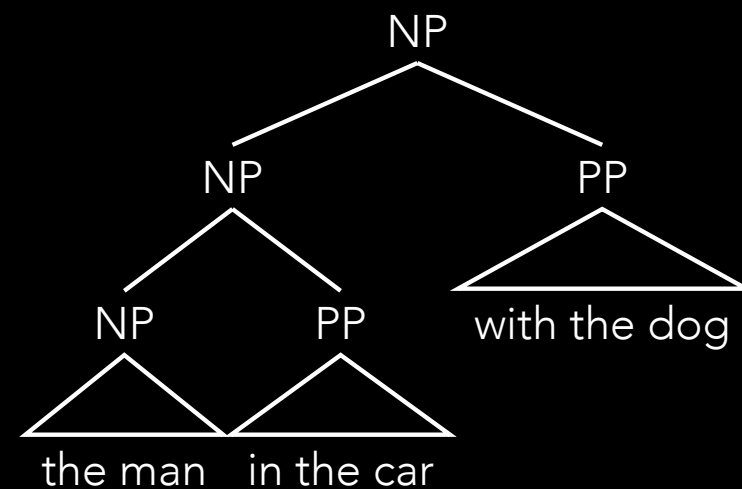
10  
times

$$p(\text{NP} \rightarrow \text{NP PP PP}) \\ = 10/200 = .05$$

How would we score parses of "the man in the car with the dog"?



$$.05 \times \dots$$

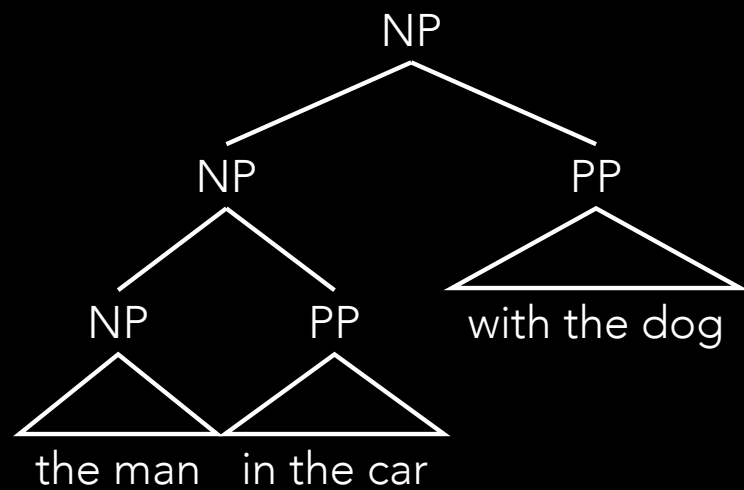


$$.45 \times .45 \times \dots = .2025 \times \dots$$



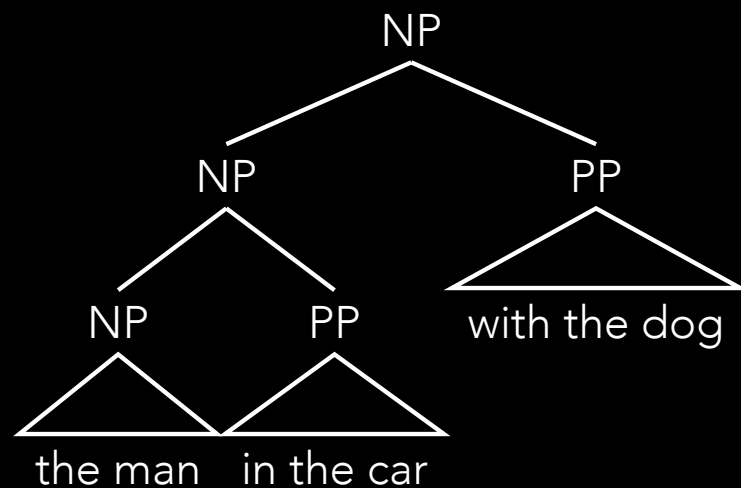
# Not Specific Enough (I)

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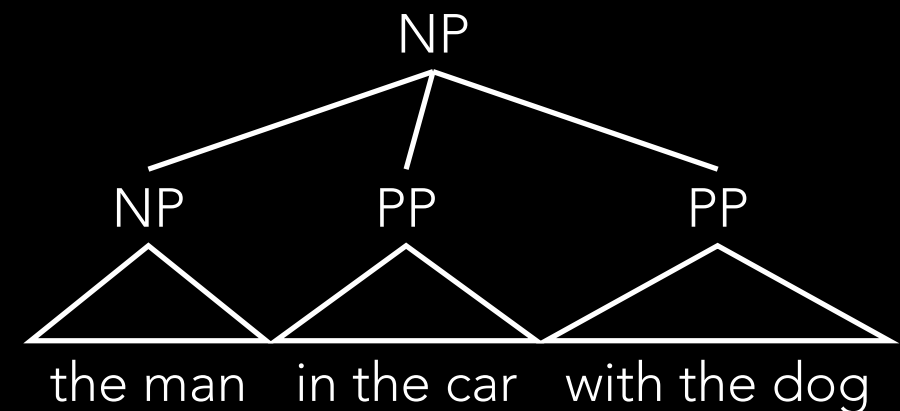


This was never  
seen in training

# Not Specific Enough (I)

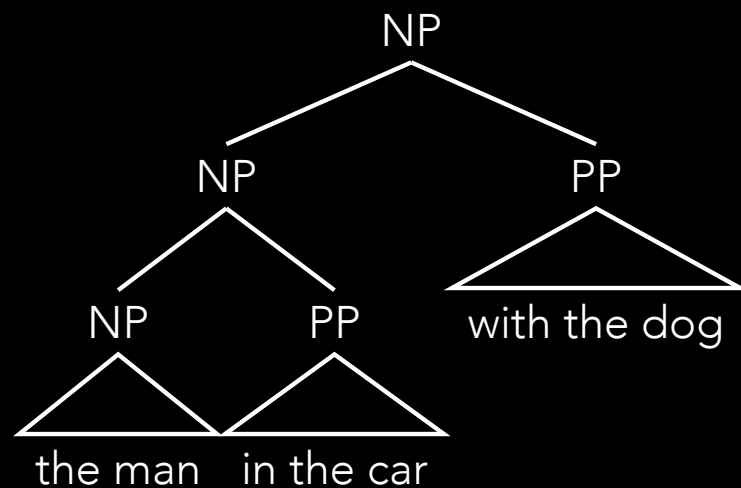


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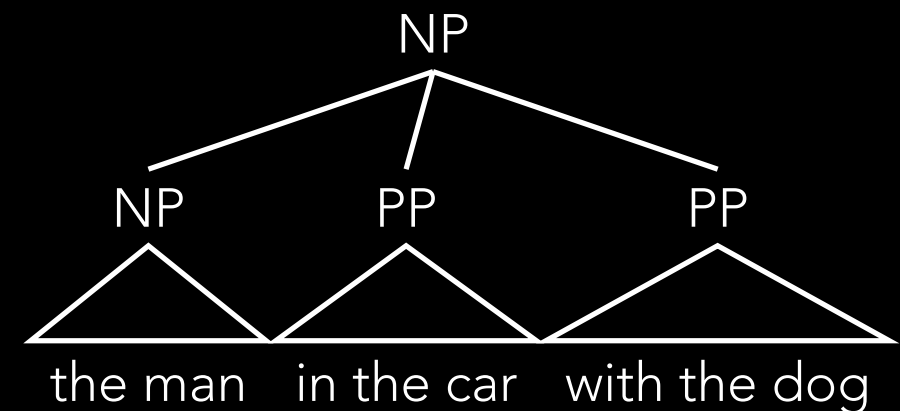
This was!

# Not Specific Enough (I)



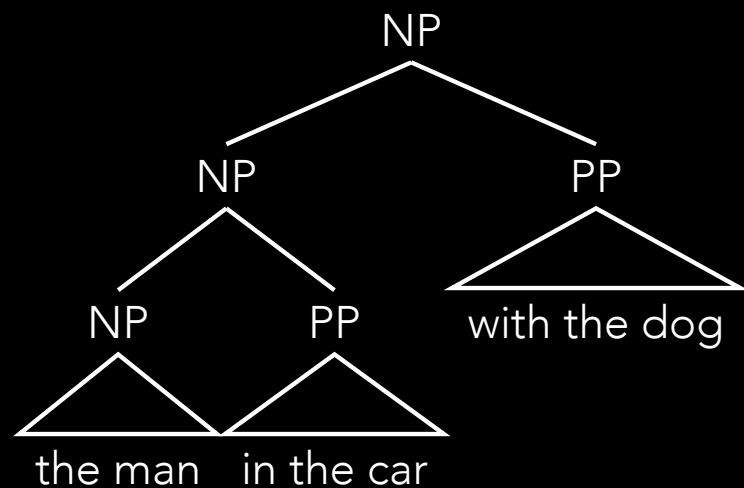
.2025

This was never  
seen in training



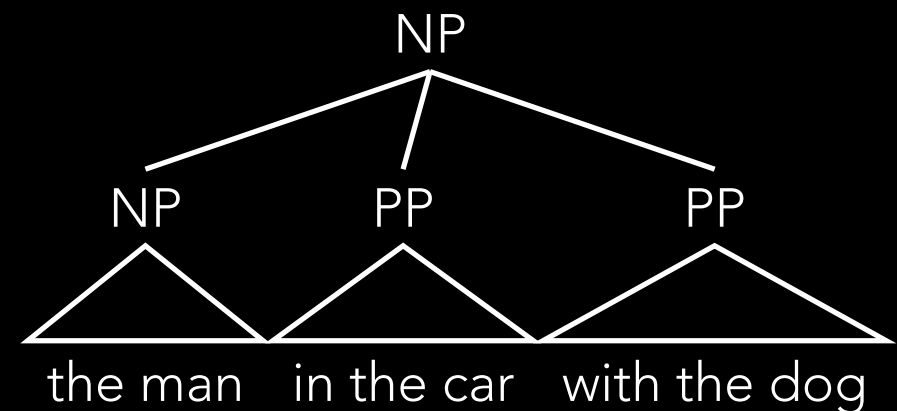
This was!

# Not Specific Enough (I)



.2025

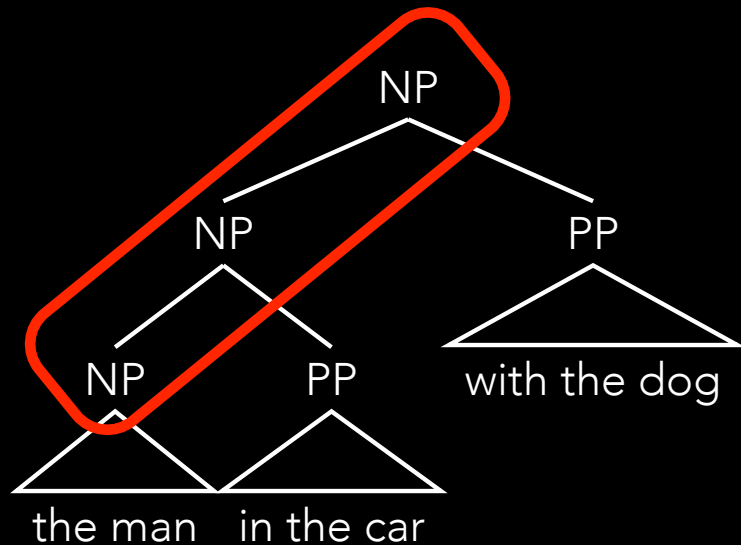
This was never  
seen in training



.05

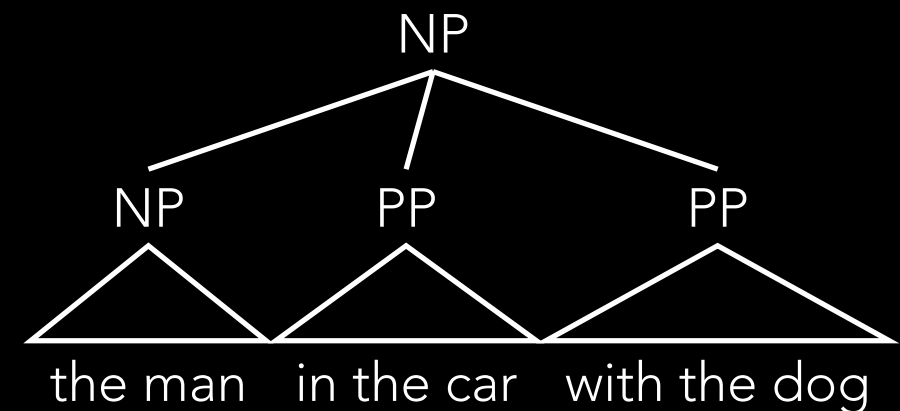
This was!

# Not Specific Enough (I)



.2025

This was never  
seen in training



.05

This was!

We should model parent-child behavior

# Not Specific Enough (I)

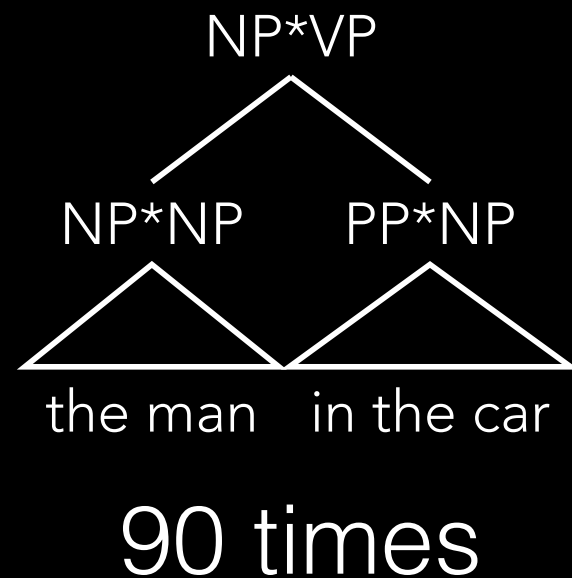
# Not Specific Enough (I)

Add parent symbol annotation



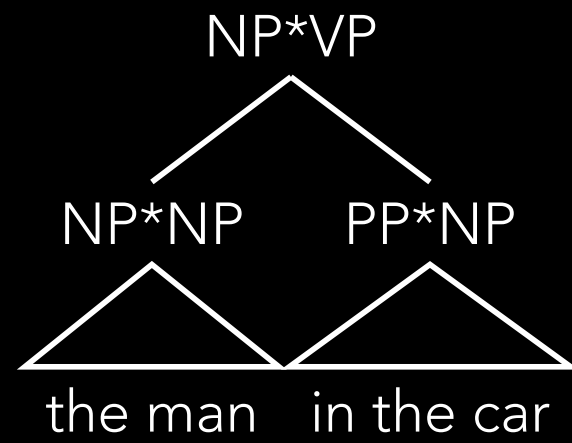
# Not Specific Enough (I)

Add parent symbol annotation

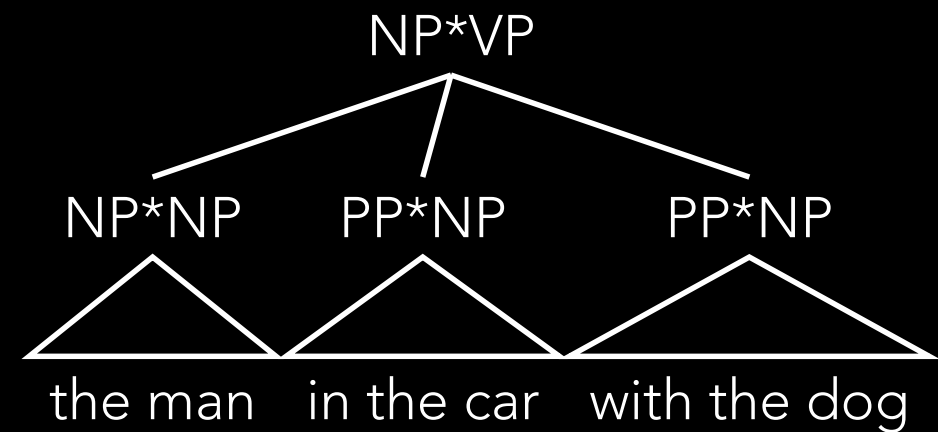


# Not Specific Enough (I)

Add parent symbol annotation



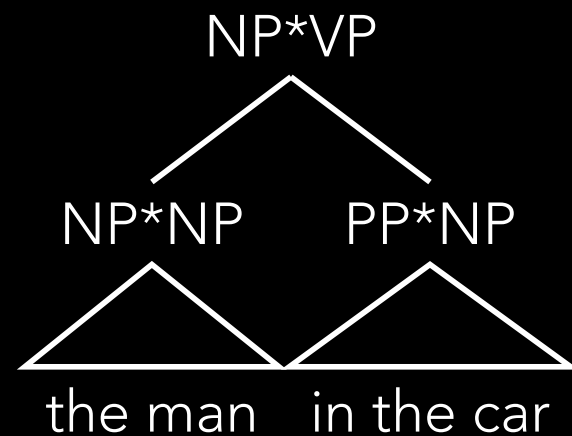
90 times



10 times

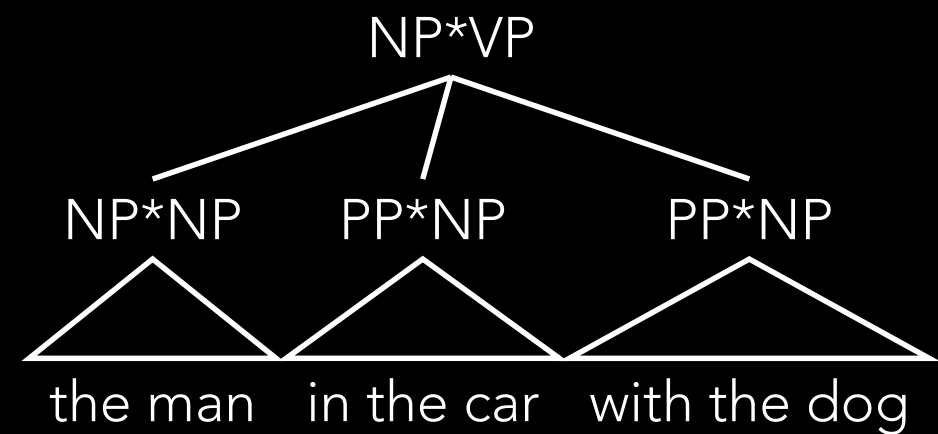
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Add parent symbol annotation



90 times

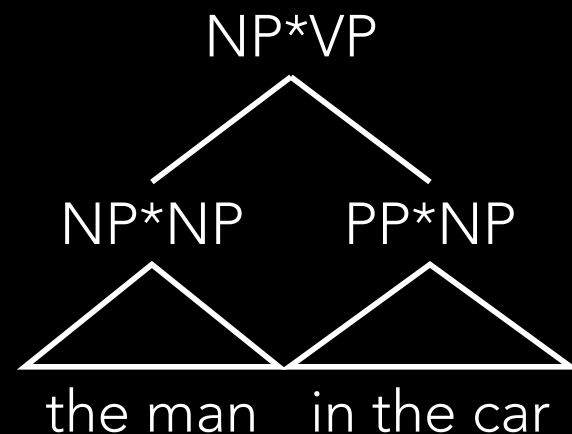
$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$



10 times

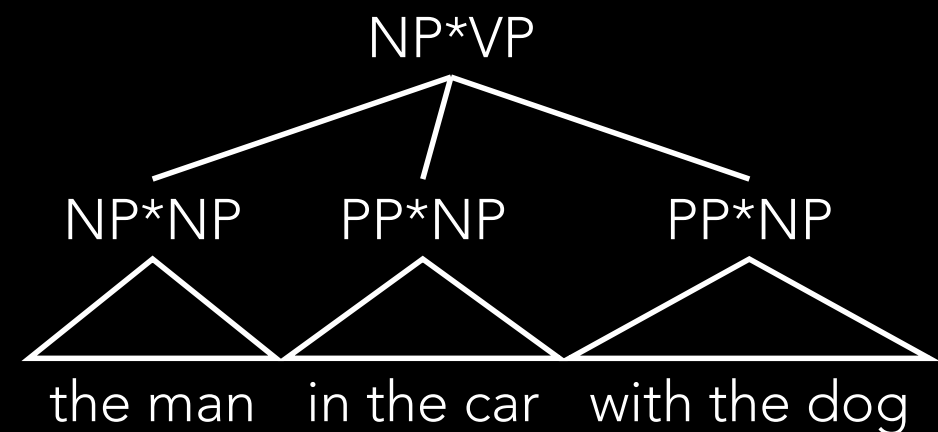
# Not Specific Enough (I)

Add parent symbol annotation



90 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$

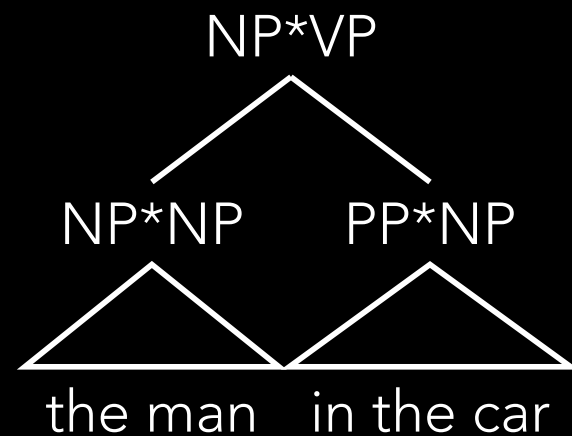


10 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP PP*NP}) \\ = 10/200 = .05$$

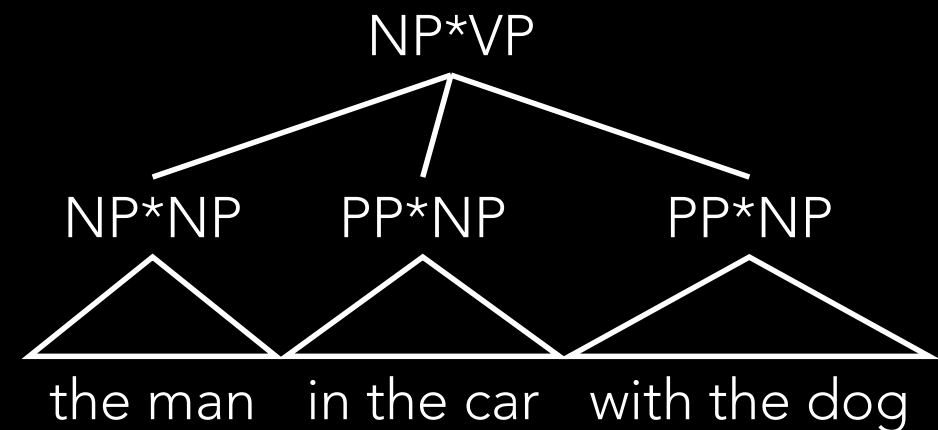
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Add parent symbol annotation



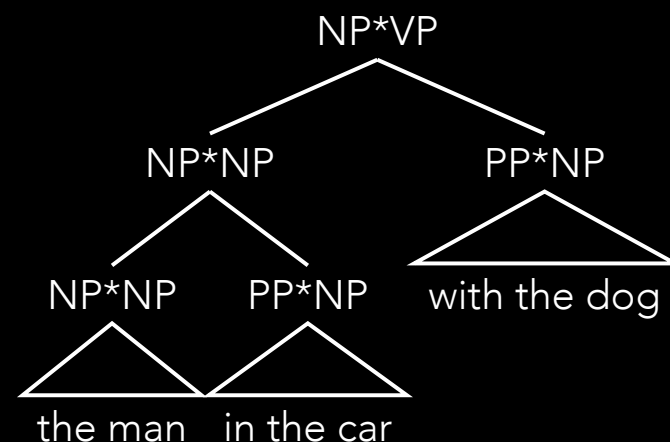
90 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$



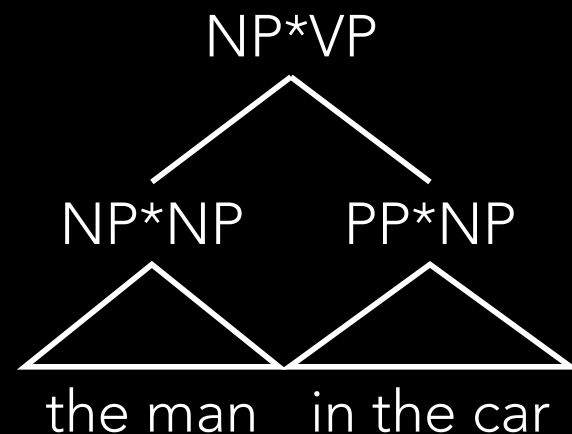
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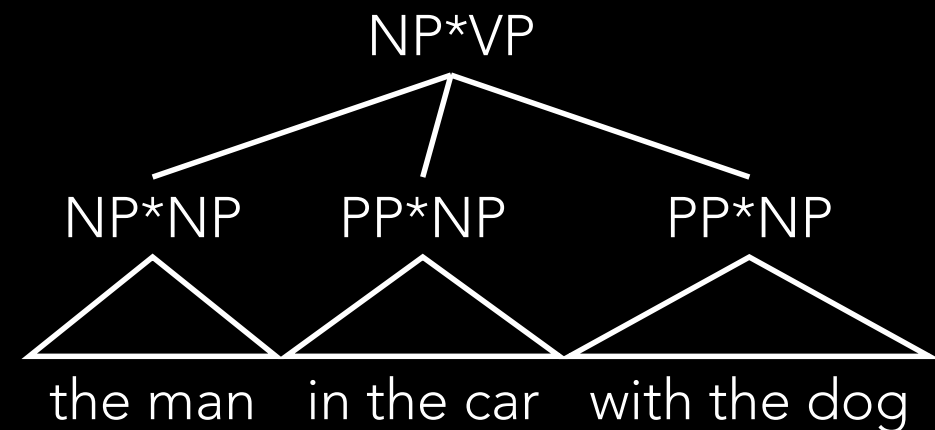
# Not Specific Enough (I)

Add parent symbol annotation



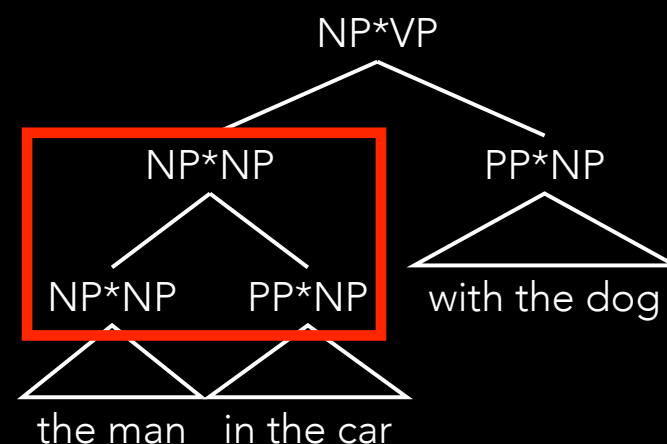
90 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$



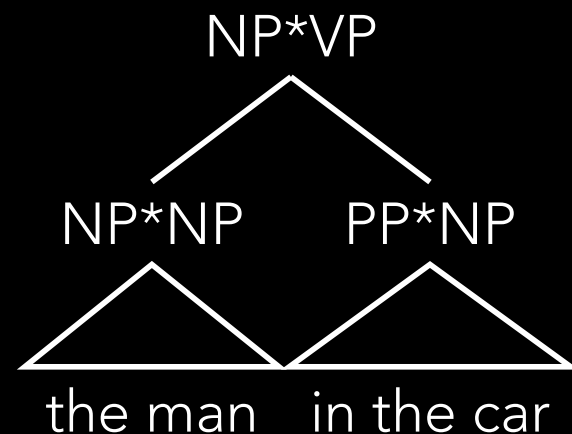
10 times

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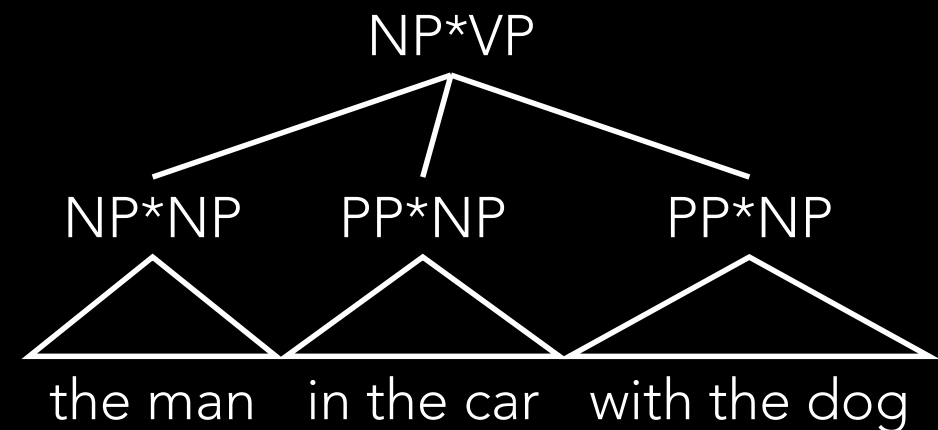
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90 times

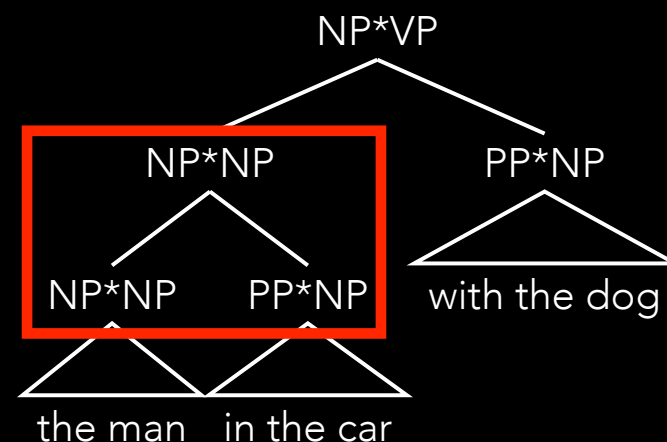
$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$



10 times

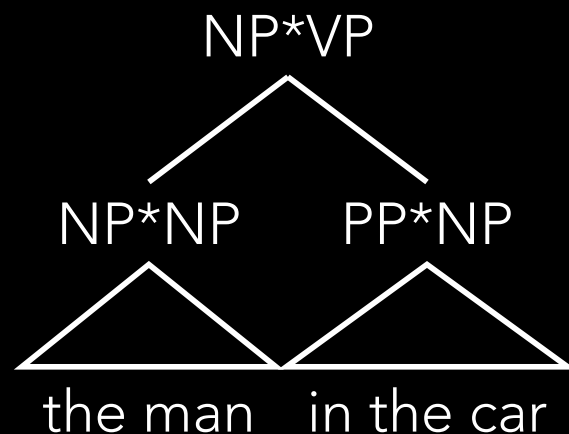
$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP PP*NP}) \\ = 10/200 = .05$$

$$p(\text{NP*NP} \rightarrow \text{NP*NP PP*NP}) = 0$$



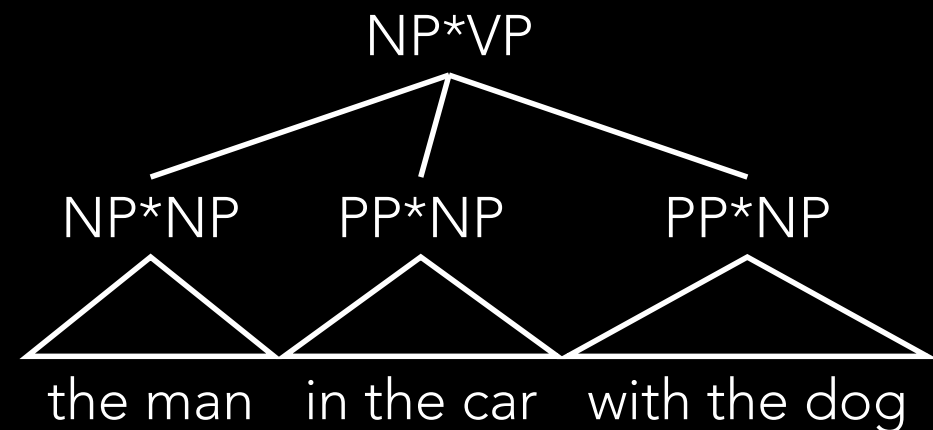
# Not Specific Enough (I)

Add parent symbol annotation



90 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP}) \\ = 90/200 = .45$$

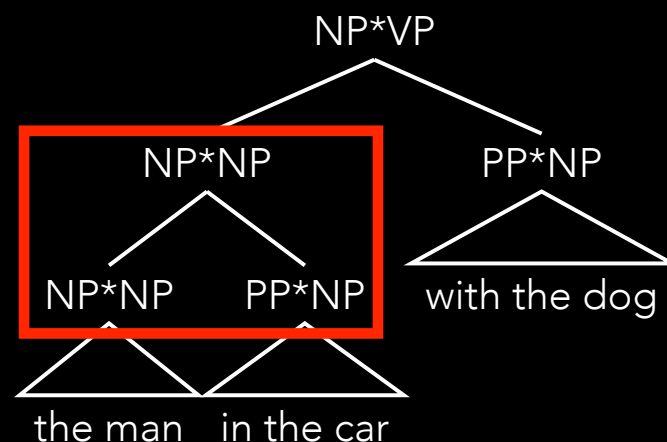


10 times

$$p(\text{NP*VP} \rightarrow \text{NP*NP PP*NP PP*NP}) \\ = 10/200 = .05$$

$$p(\text{NP*NP} \rightarrow \text{NP*NP PP*NP}) = 0$$

Not possible!





# Other Useful Category Splits

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- Mark base NPs (NPs that do not contain other NPs)

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- Mark base NPs (NPs that do not contain other NPs)
- Parent annotation on preterminals

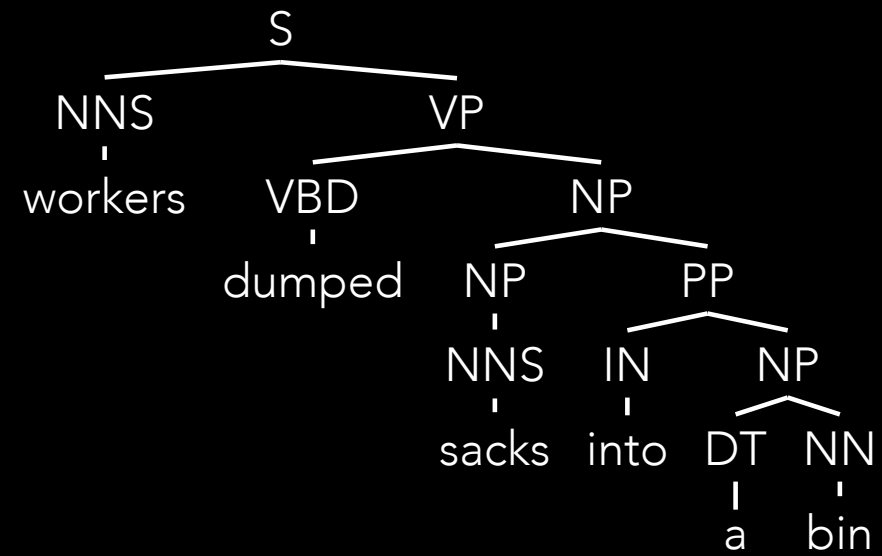
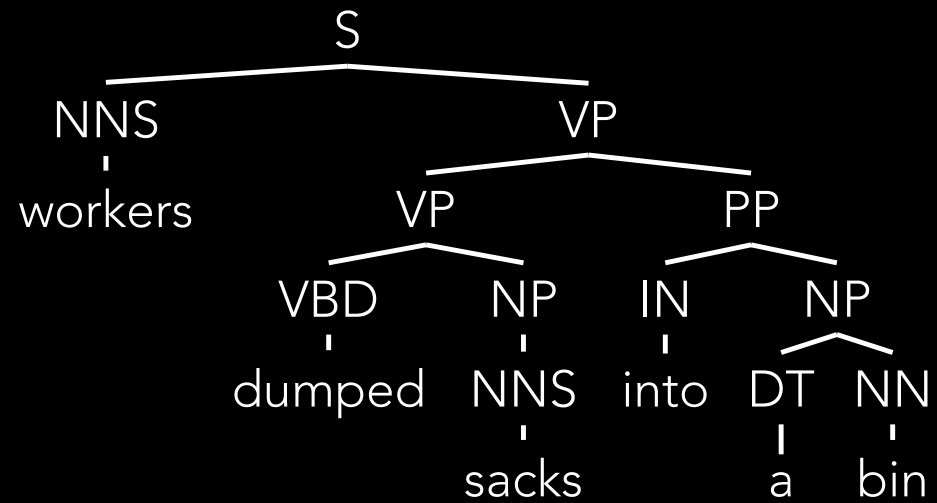
# Other Useful Category Splits

- Mark base NPs (NPs that do not contain other NPs)
- Parent annotation on preterminals
- Subdivide IN, CC, “have” vs “be” auxiliary

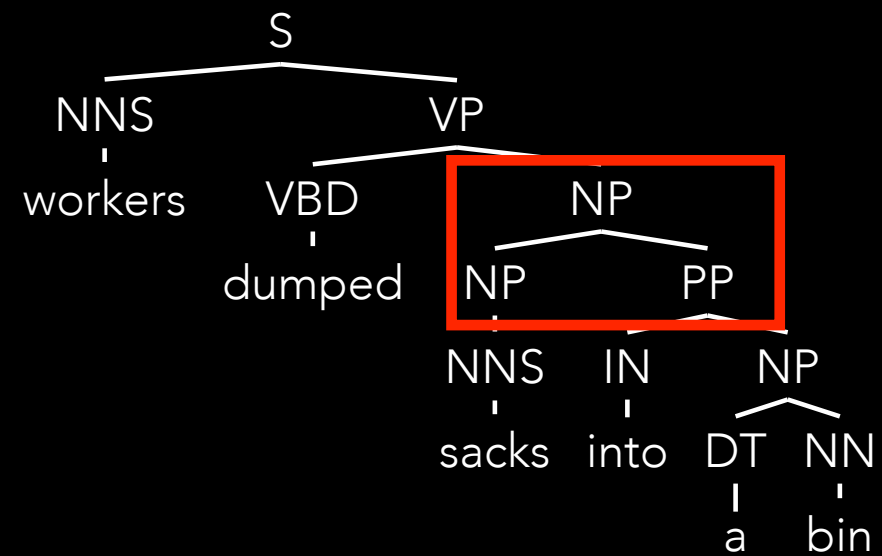
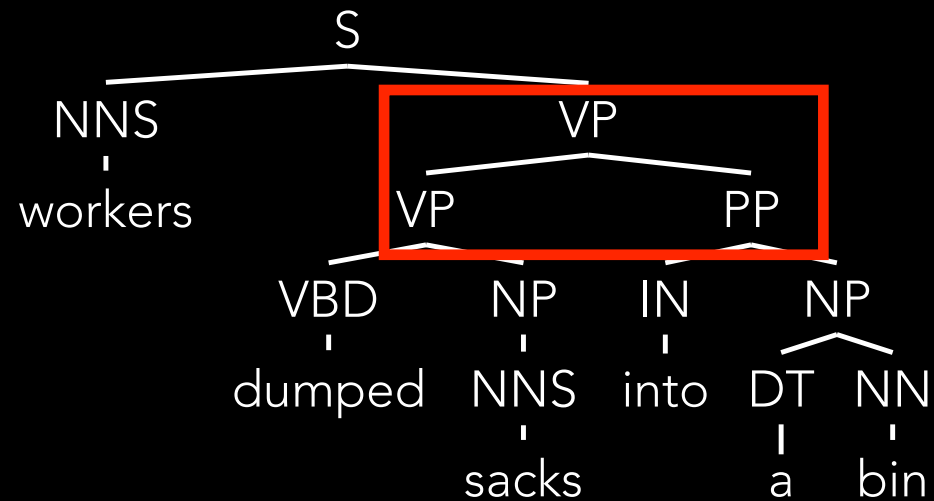
# Other Useful Category Splits

- Mark base NPs (NPs that do not contain other NPs)
- Parent annotation on preterminals
- Subdivide IN, CC, “have” vs “be” auxiliary
- See “Accurate Unlexicalized Parsing” (Klein & Manning, 2003)

# Not Specific Enough (II)

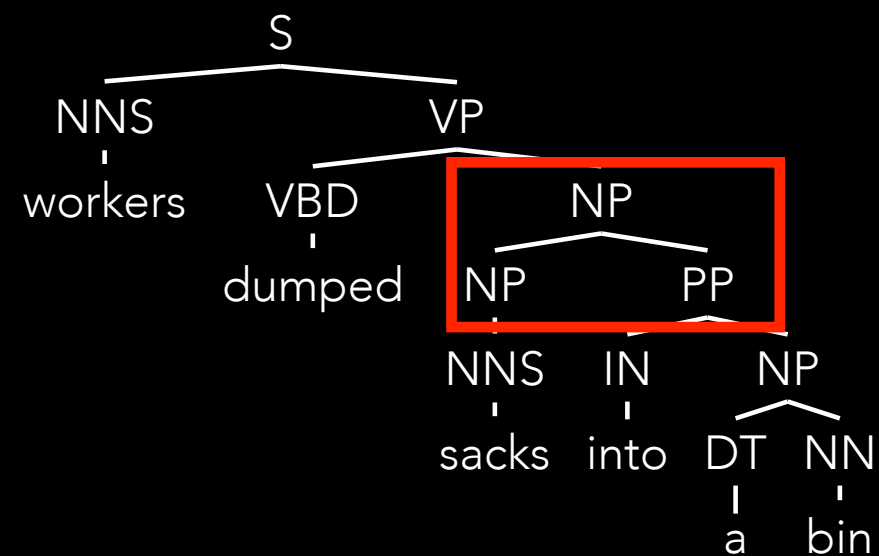
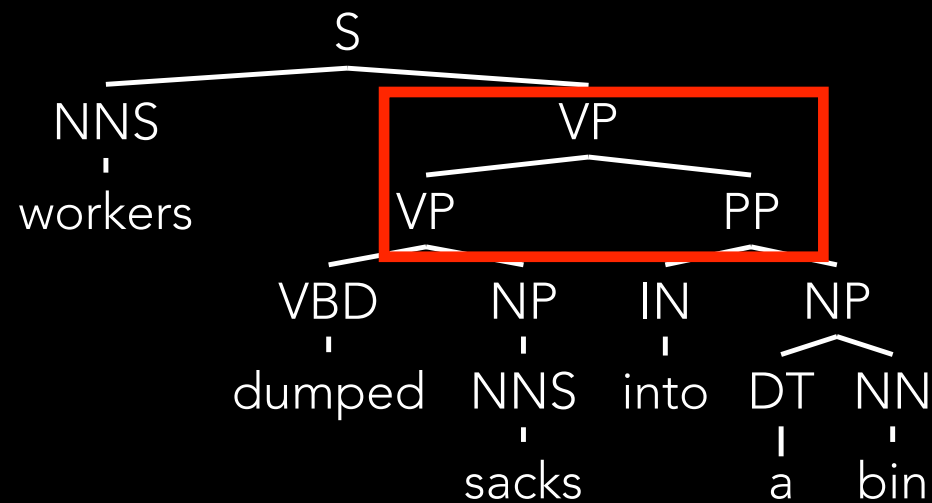


# Not Specific Enough (II)



These derivations only differ by the highlighted rules

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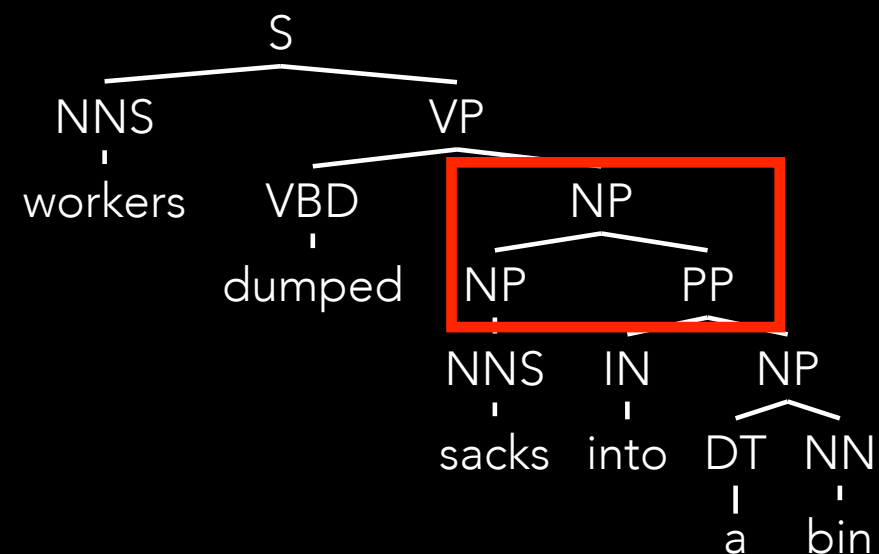
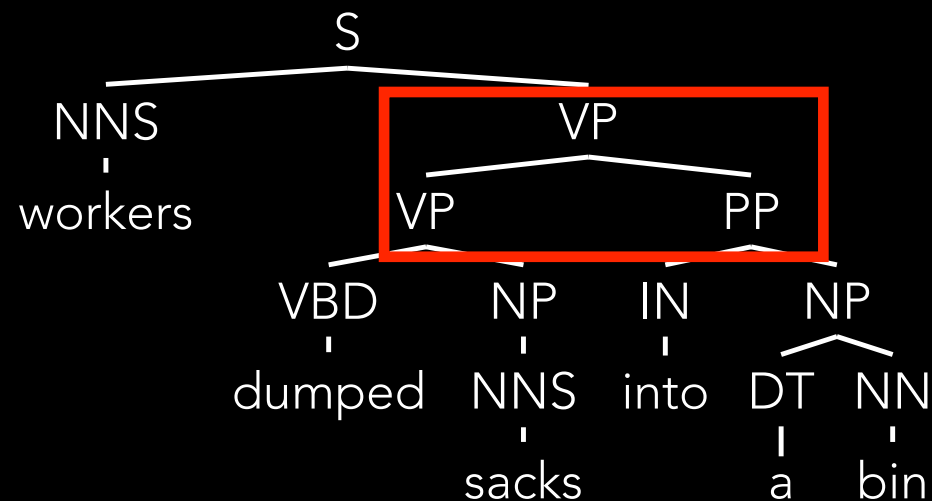


These derivations only differ by the highlighted rules

If  $p(\text{VP} \rightarrow \text{VP PP}) > p(\text{NP} \rightarrow \text{NP PP})$  then the left derivation wins. Else, the right derivation



# Not Specific Enough (II)



These derivations only differ by the highlighted rules

If  $p(\text{VP} \rightarrow \text{VP PP}) > p(\text{NP} \rightarrow \text{NP PP})$  then  
the left derivation wins. Else, the right derivation

The words (particularly “into”) are not considered. PPs  
with “into” are much more likely to attach to VP than NP.

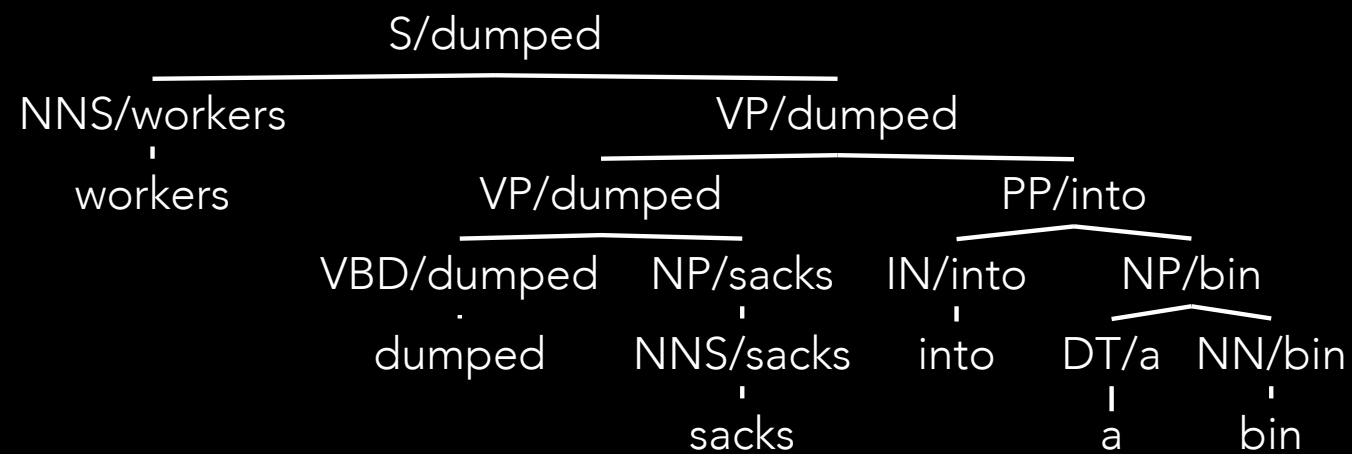
# Head lexicalization

# Head lexicalization

Annotate tree labels with their “head” word

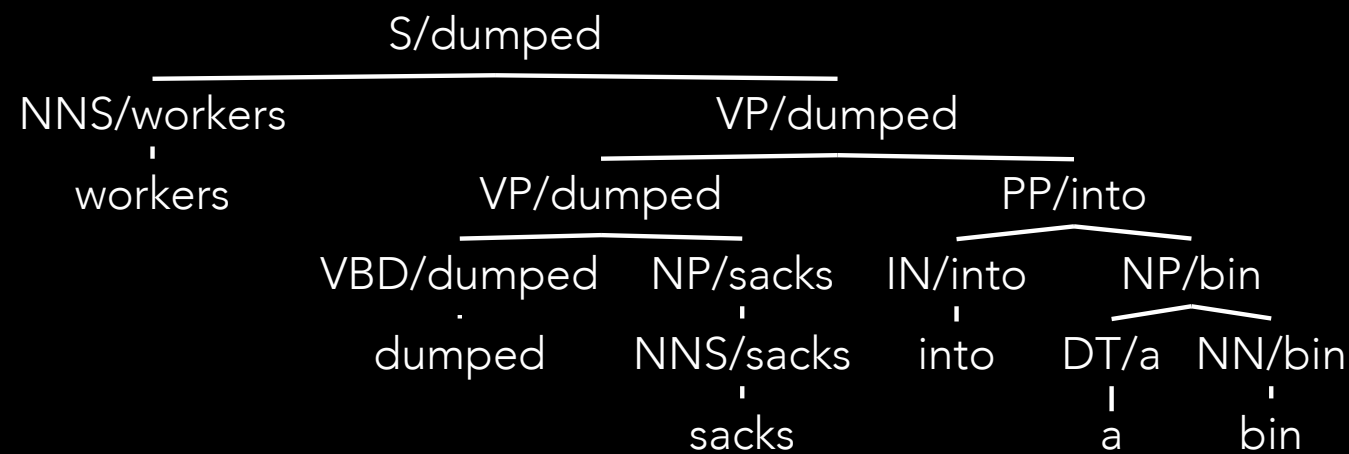
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# Head lexicalization

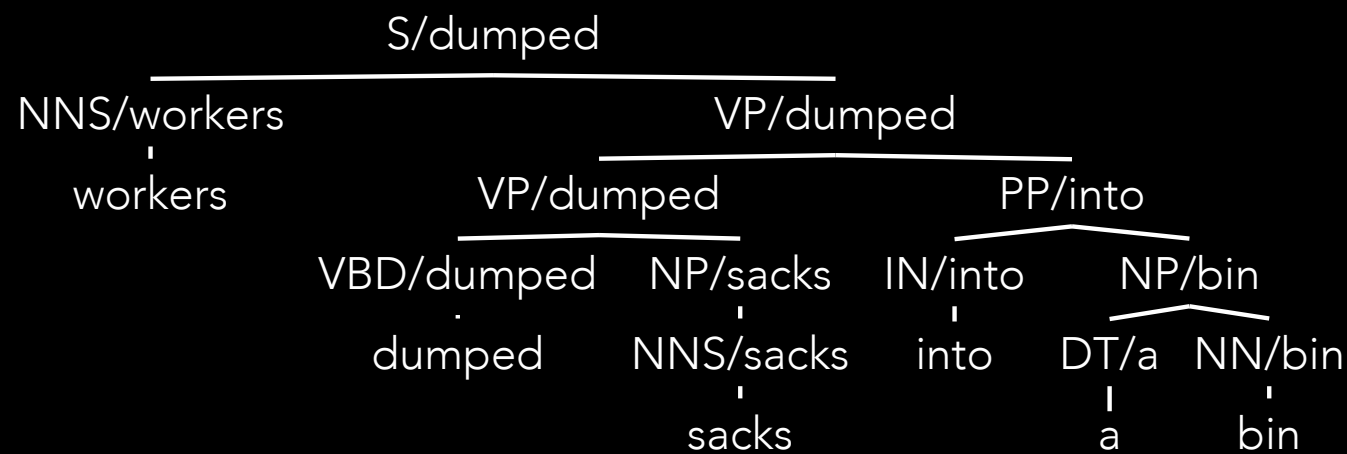
Annotate tree labels with their “head” word



Heads are the “important” word in a phrase

# Head lexicalization

Annotate tree labels with their “head” word

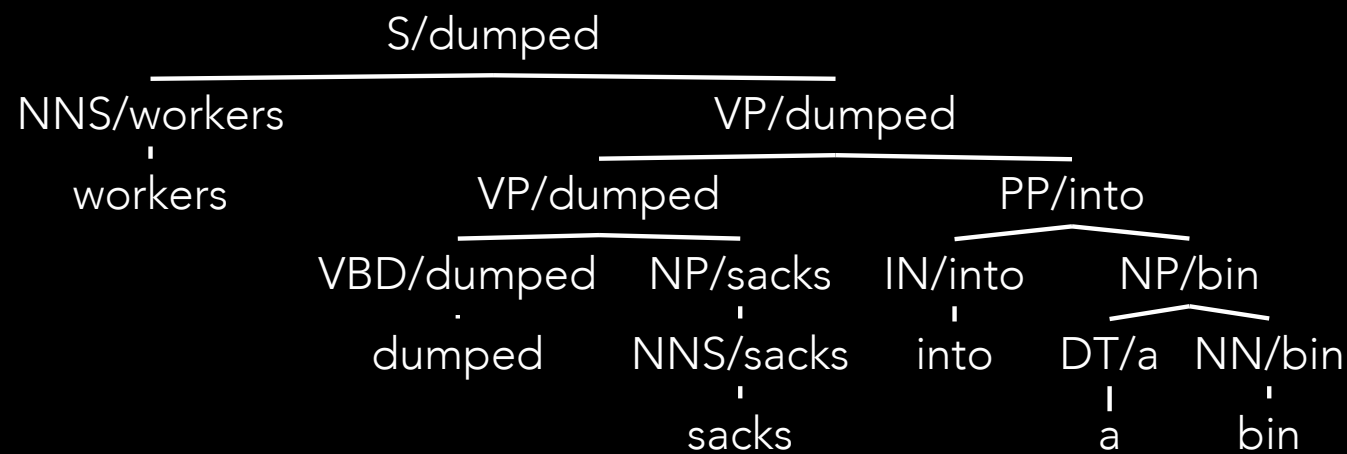


Heads are the “important” word in a phrase

They could be provided by annotators

# Head lexicalization

Annotate tree labels with their “head” word



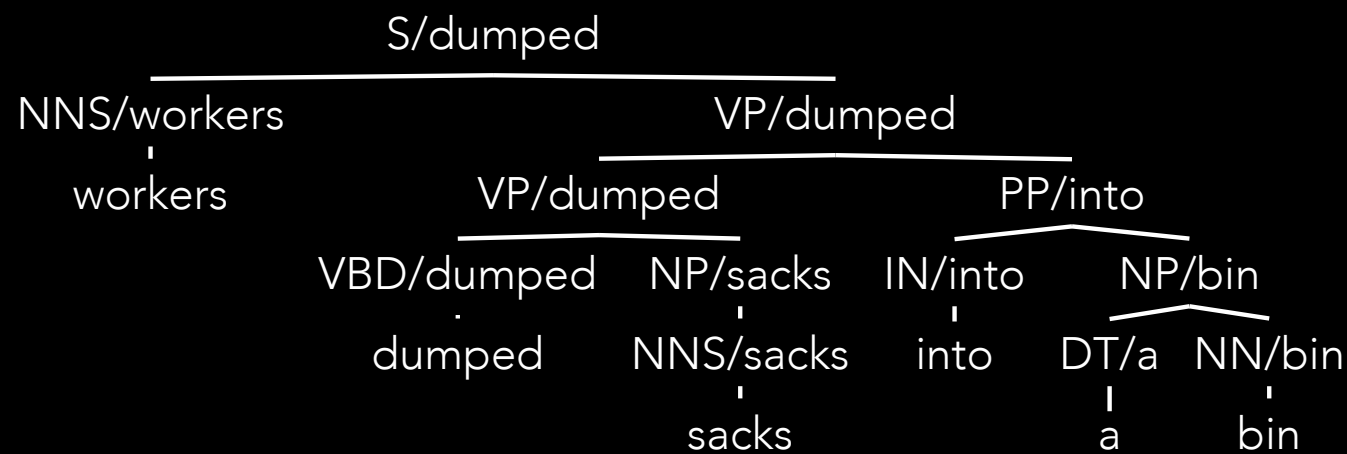
Heads are the “important” word in a phrase

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In practice, for English, some heuristics work well

# Head lexicalization

Annotate tree labels with their “head” word



Heads are the “important” word in a phrase

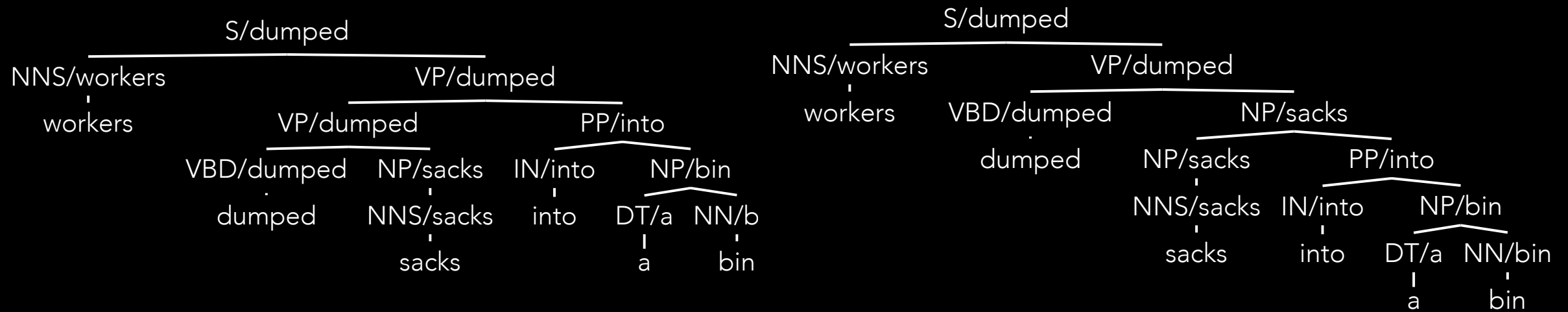
They could be provided by annotators

In practice, for English, some heuristics work well

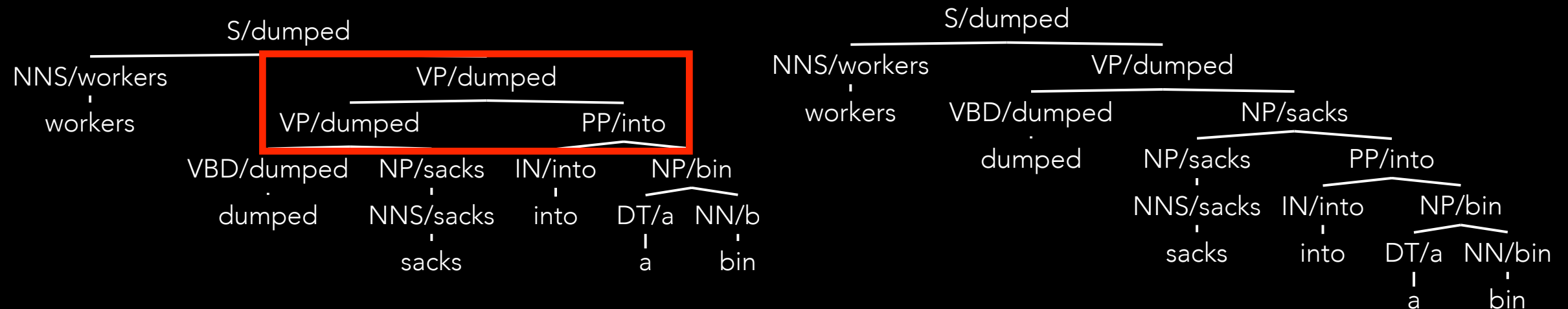
<http://www.cs.columbia.edu/~mcollins/papers/heads>



# Head lexicalization

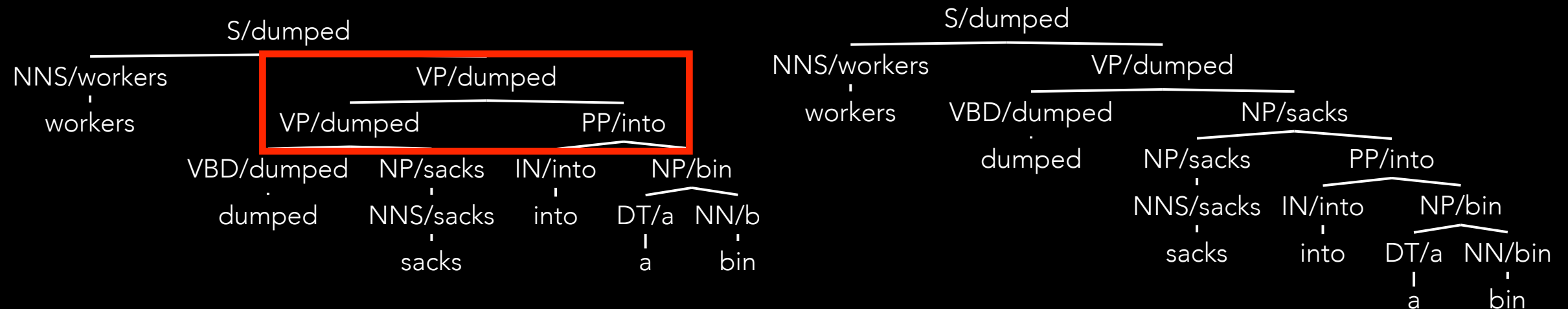


# Head lexicalization



VP/dumped -> VP/dumped PP/into

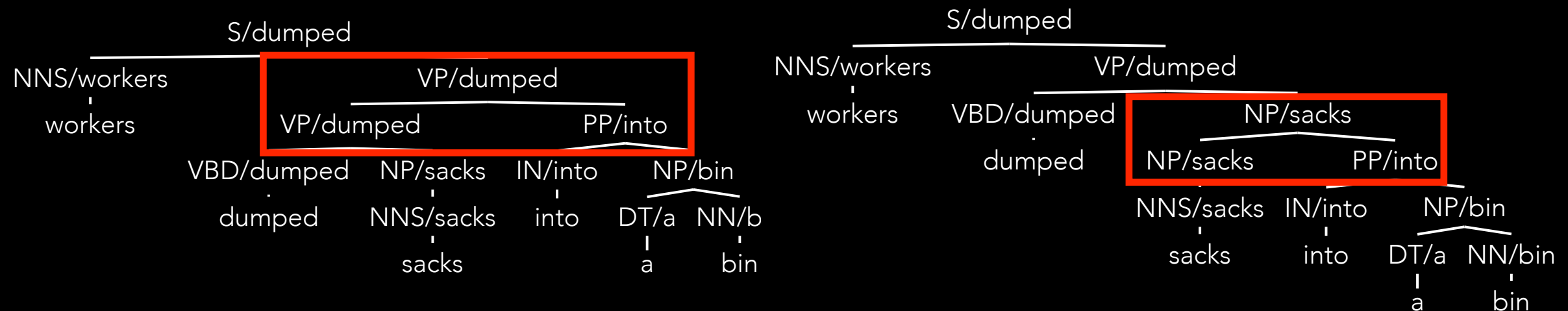
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VP/dumped -> VP/dumped PP/into

more likely than

# Head lexicalization



VP/dumped -> VP/dumped PP/into

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NP/sacks-> NP/sacks PP/into

# Lexicalization and Binarization

# Lexicalization and Binarization

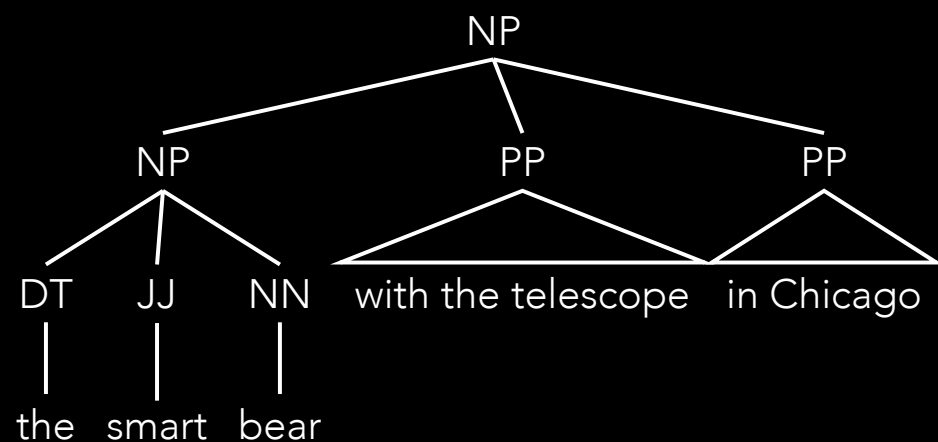
- Want to keep meaningful head at every point

# Lexicalization and Binarization

- Want to keep meaningful head at every point
- Need to make binarization head-aware

# Lexicalization and Binarization

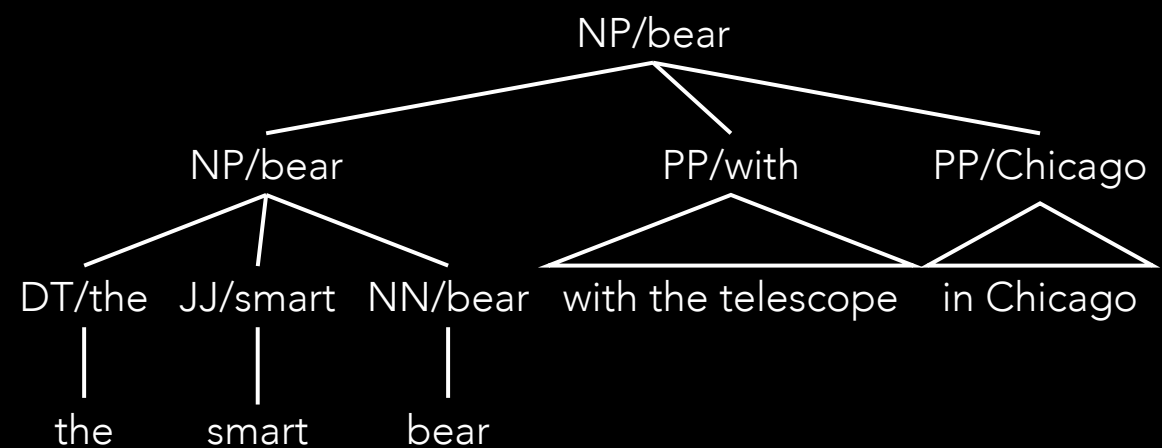
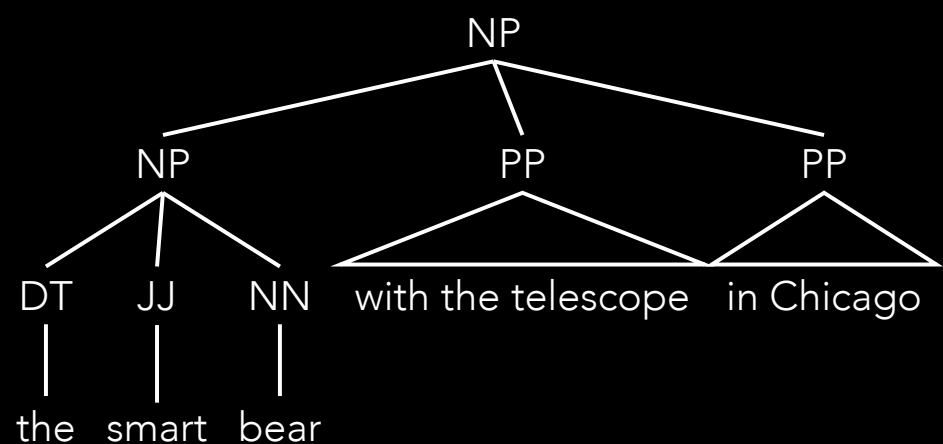
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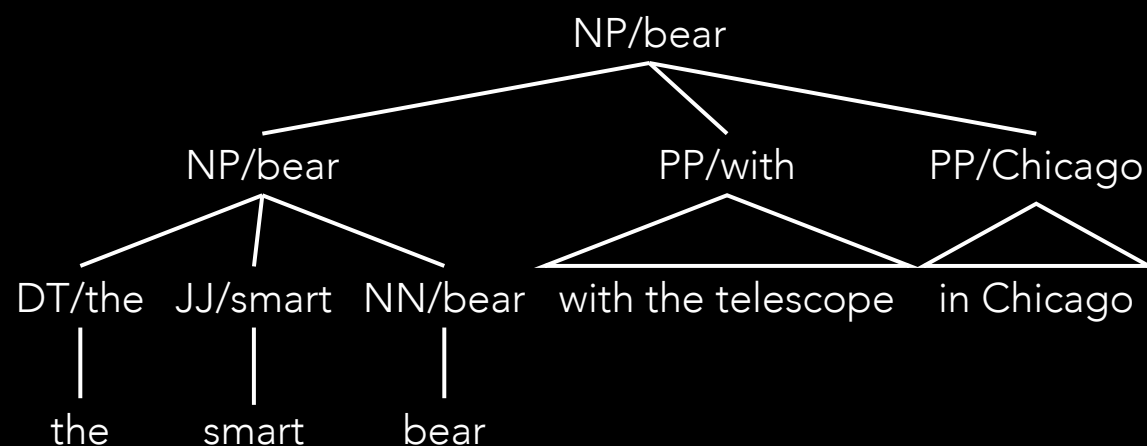
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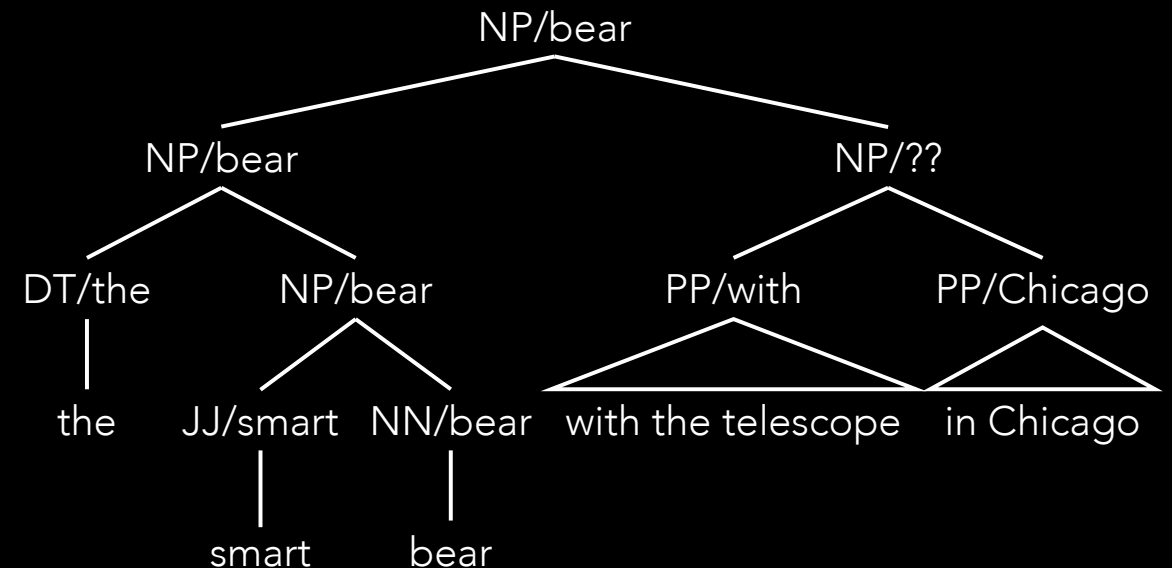
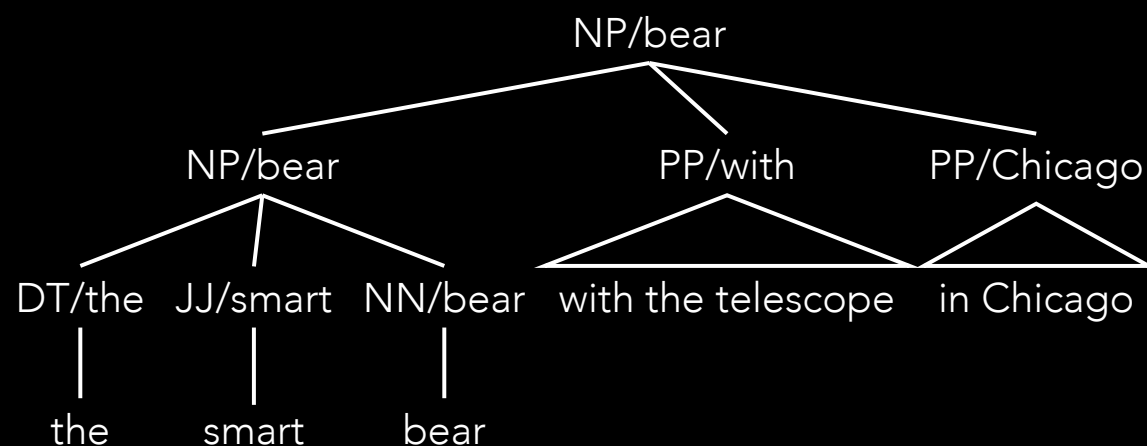
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# Lexicalization and Binarization

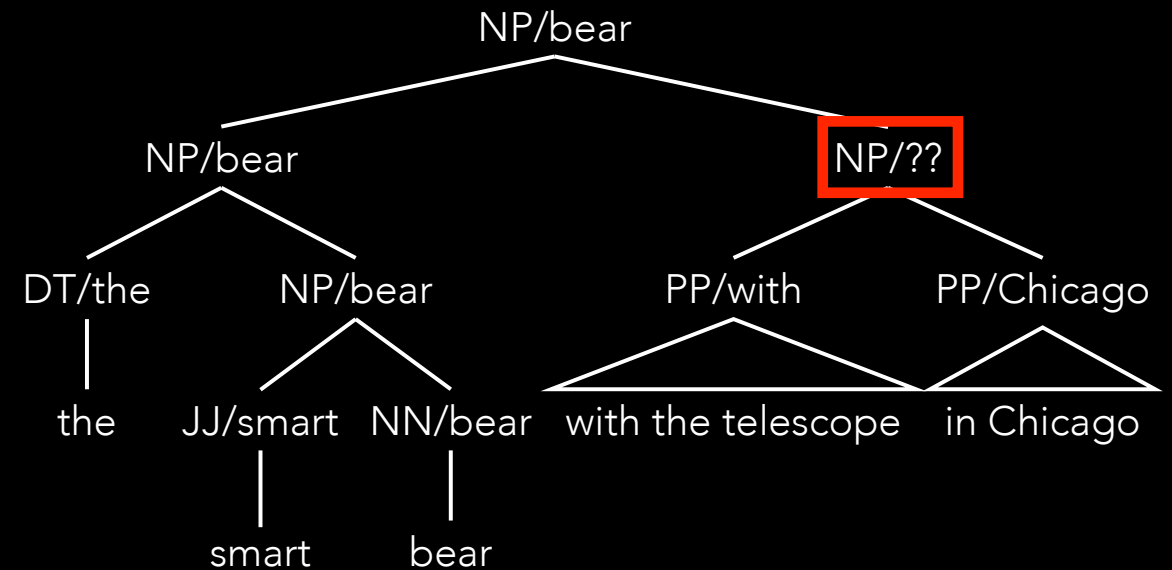
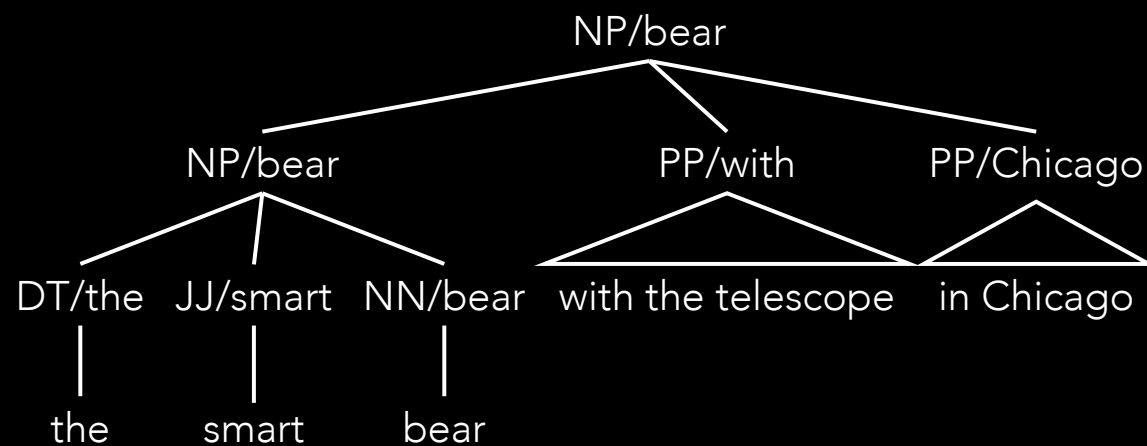
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Right binarization

# Lexicalization and Binarization

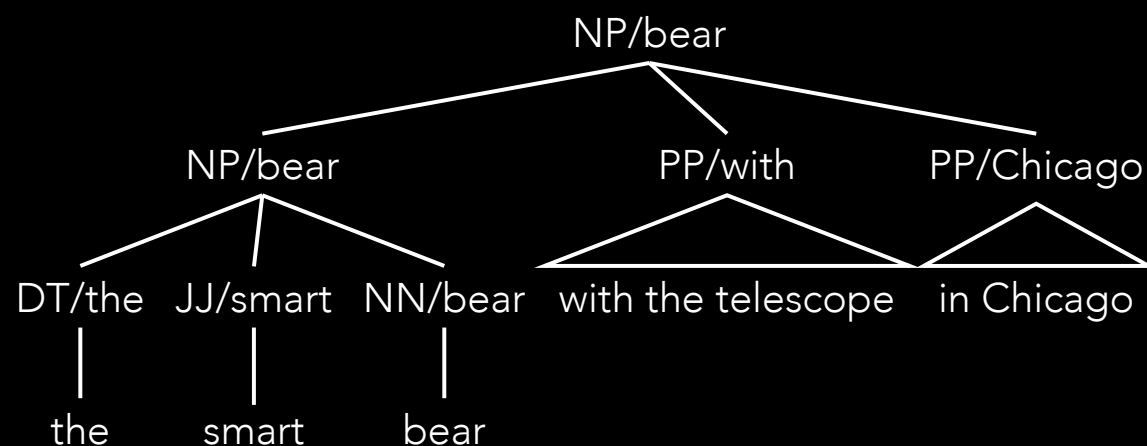
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Right binarization

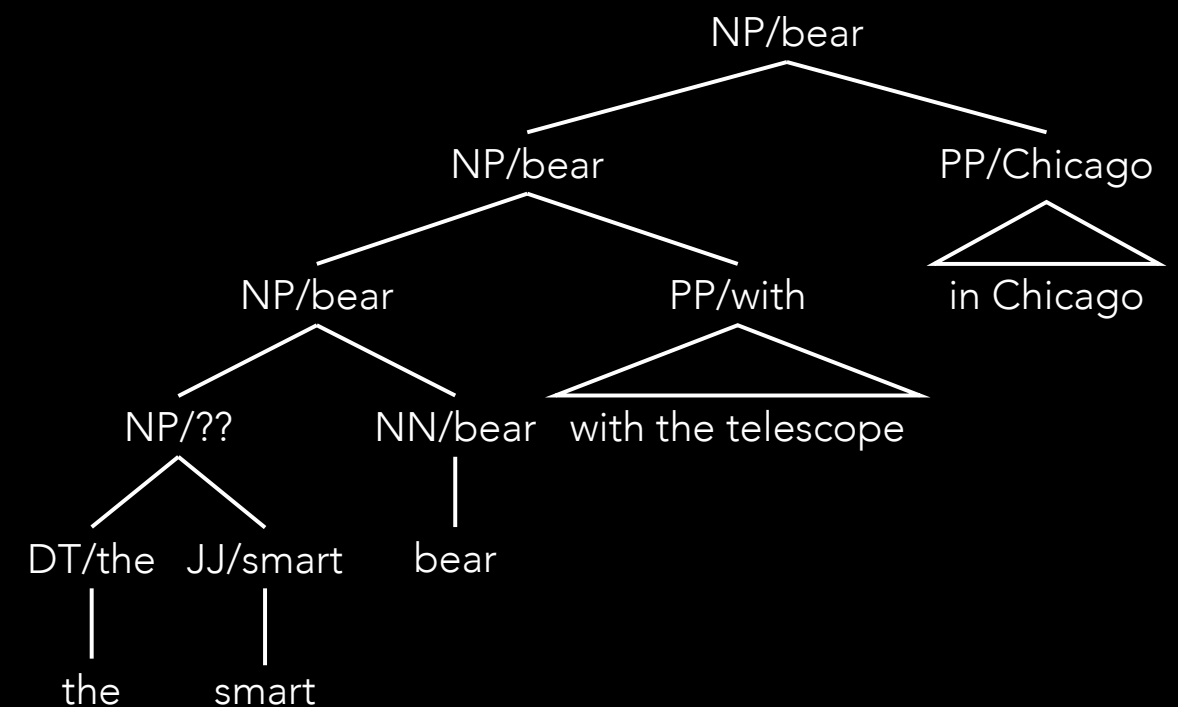
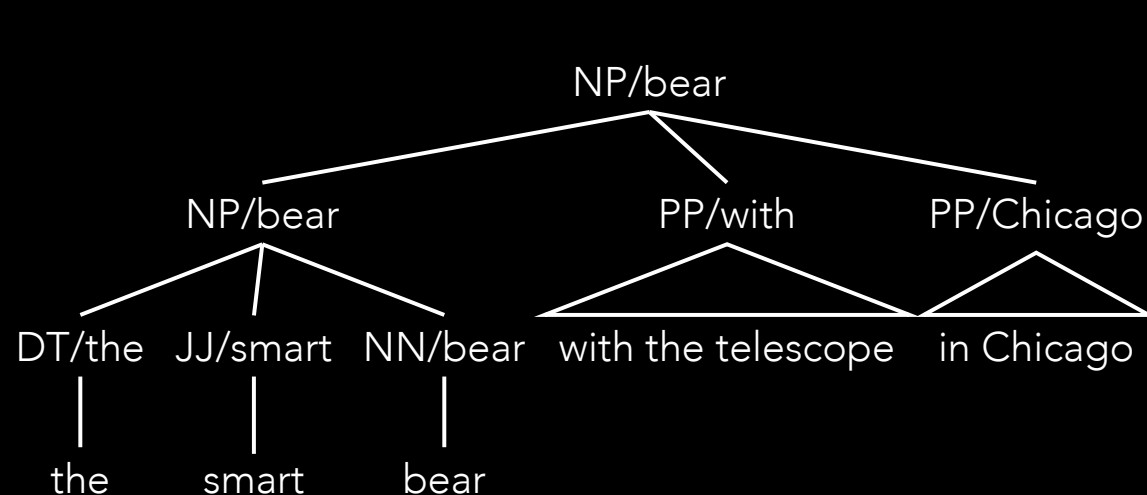
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# Lexicalization and Binarization

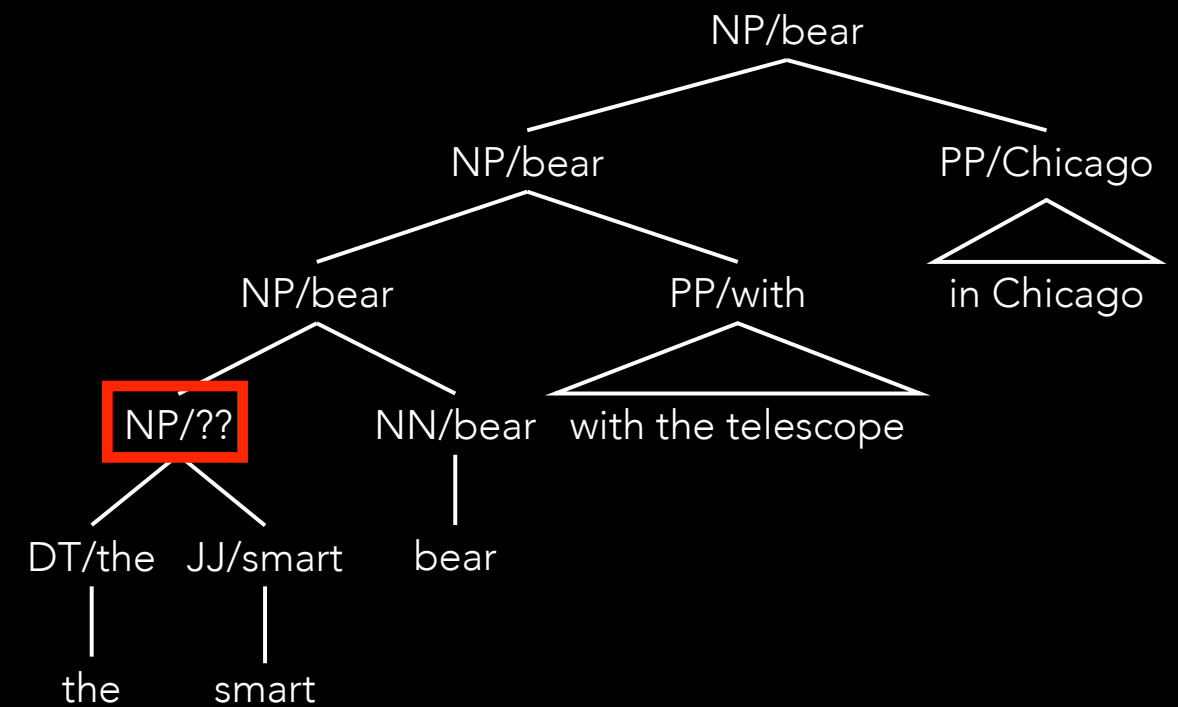
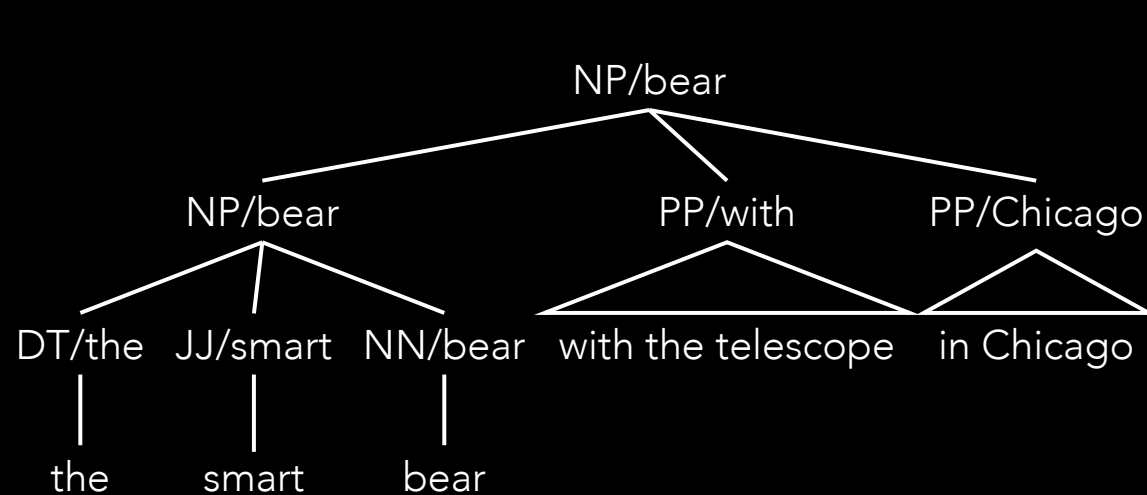
- Want to keep meaningful head at every point
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Left binarization

# Lexicalization and Binarization

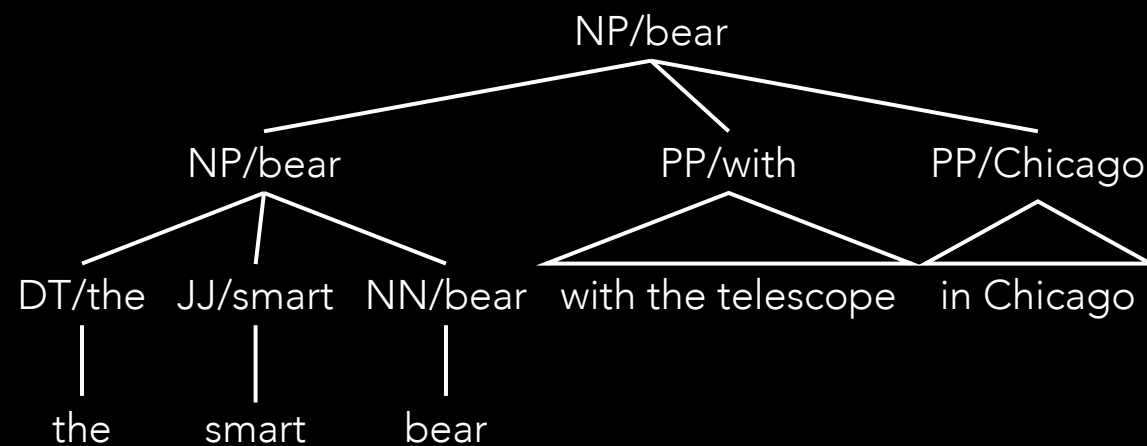
- Want to keep meaningful head at every point
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Left binarization

# Lexicalization and Binarization

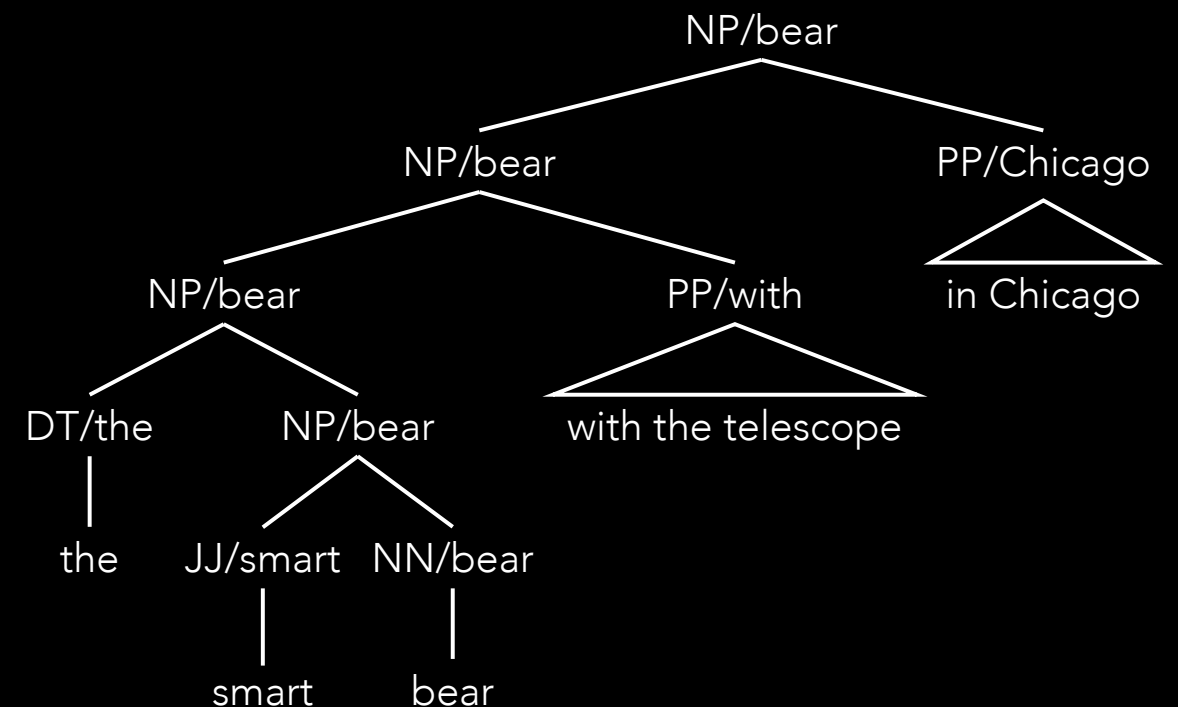
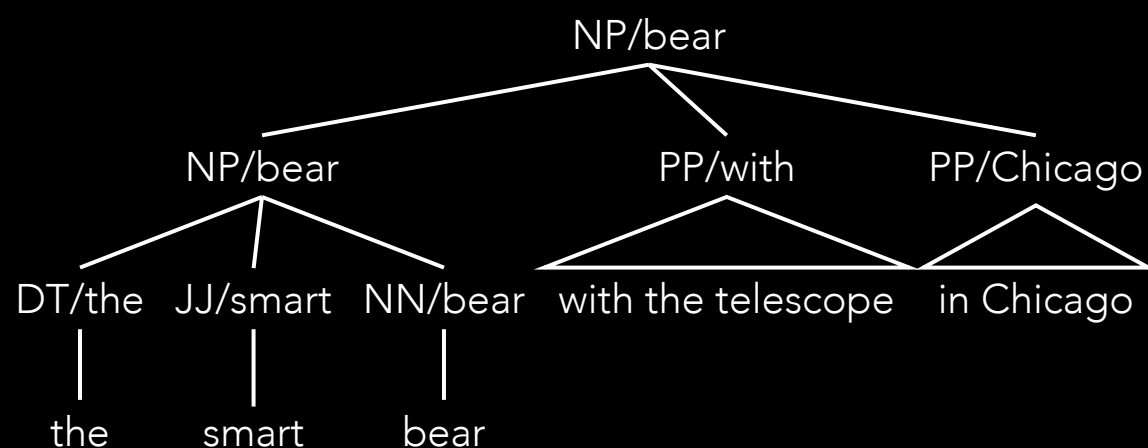
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# Lexicalization and Binarization

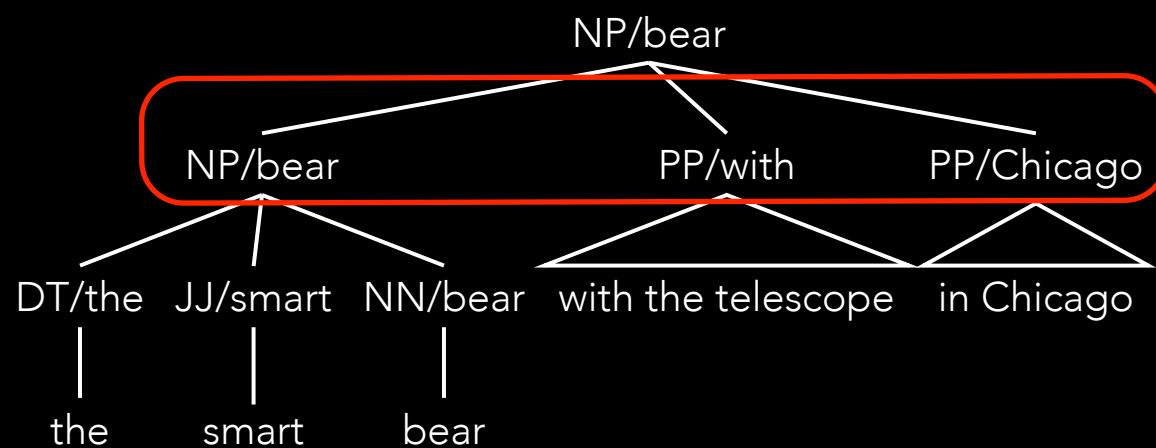
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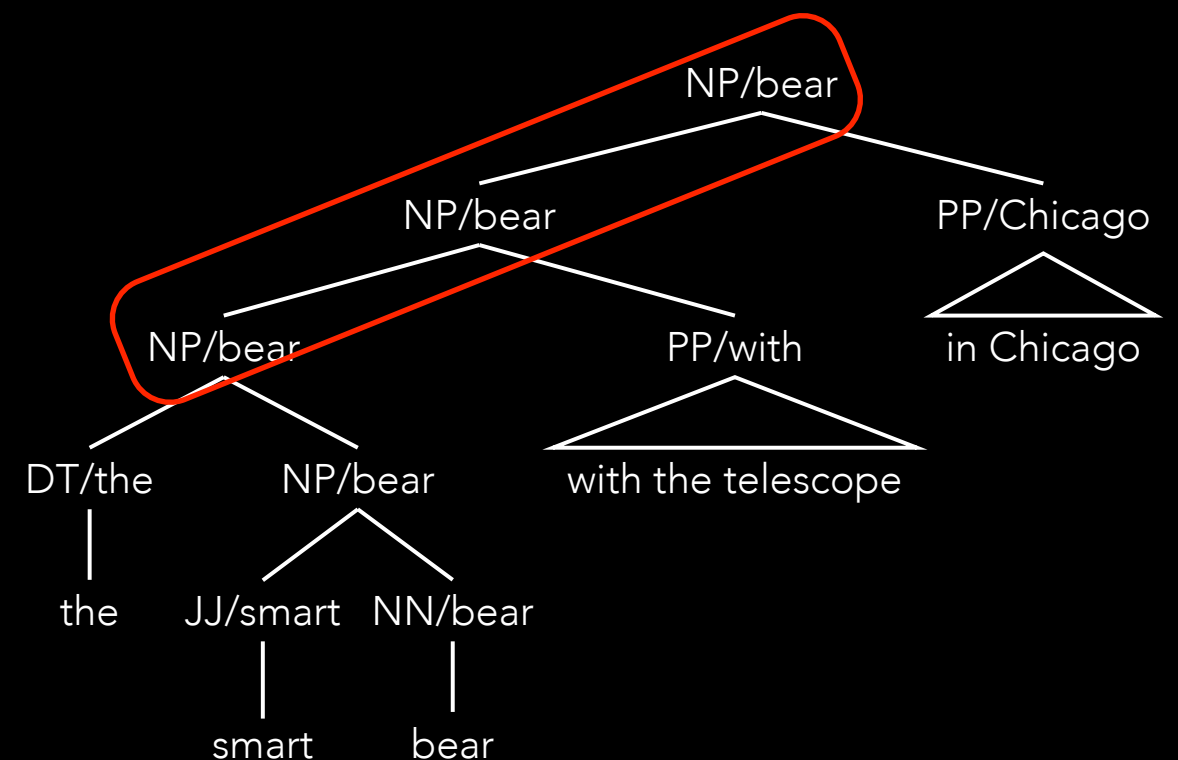
Head binarization!

# Lexicalization and Binarization

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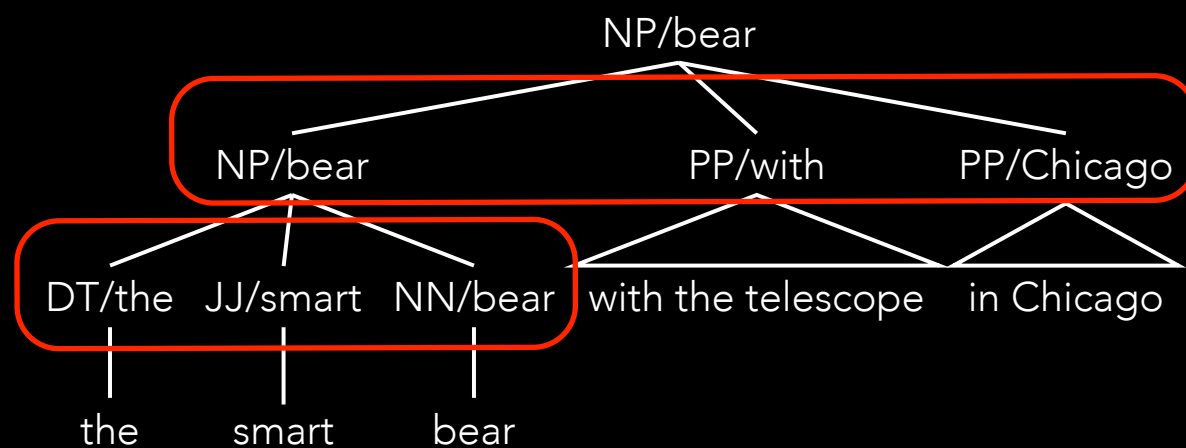
Left (for NP PP PP)



Head binarization!

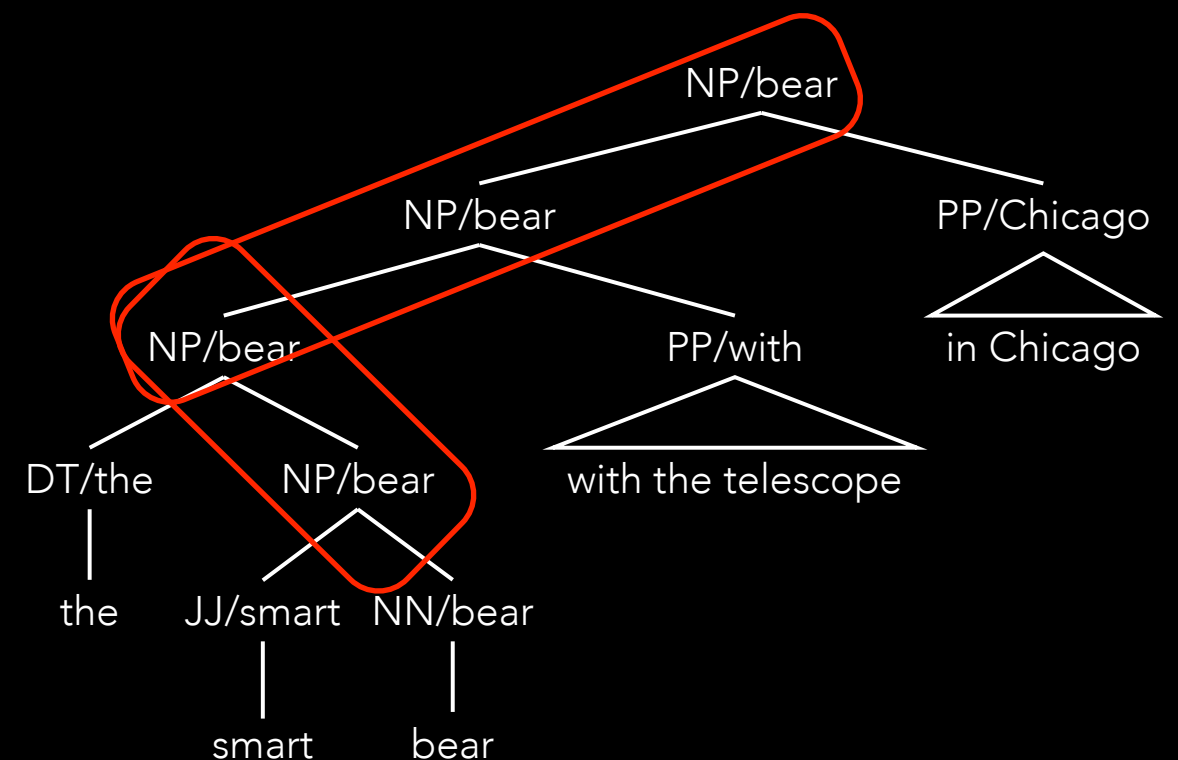
# Lexicalization and Binarization

- Want to keep meaningful head at every point
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Left (for NP PP PP)

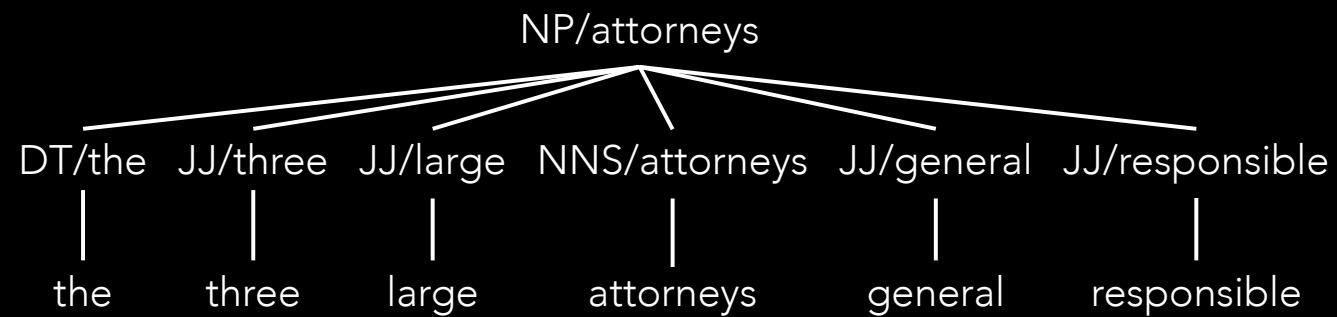
Right (for DT JJ NN)



Head binarization!

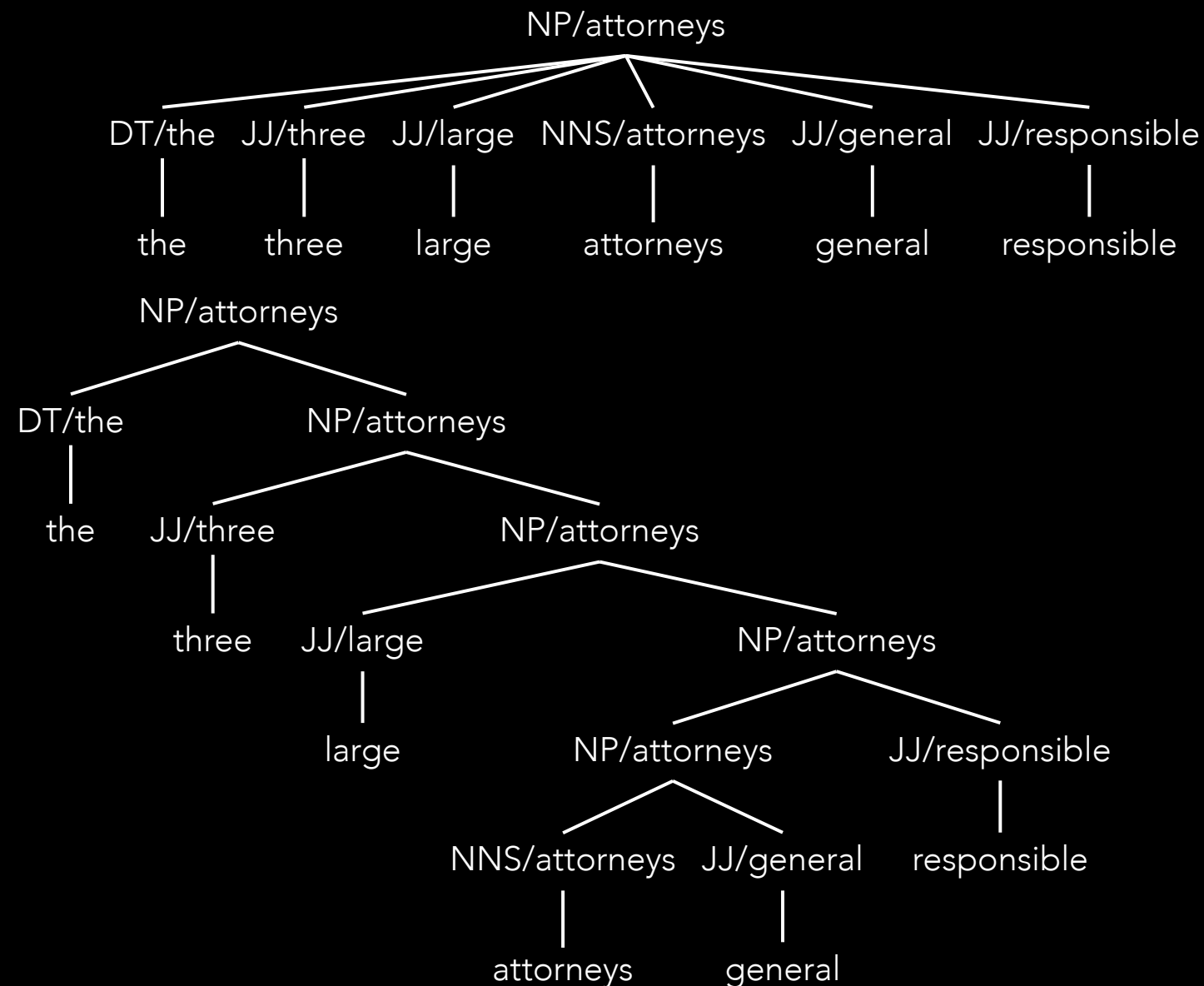
# Lexicalization and Binarization

More complicated example



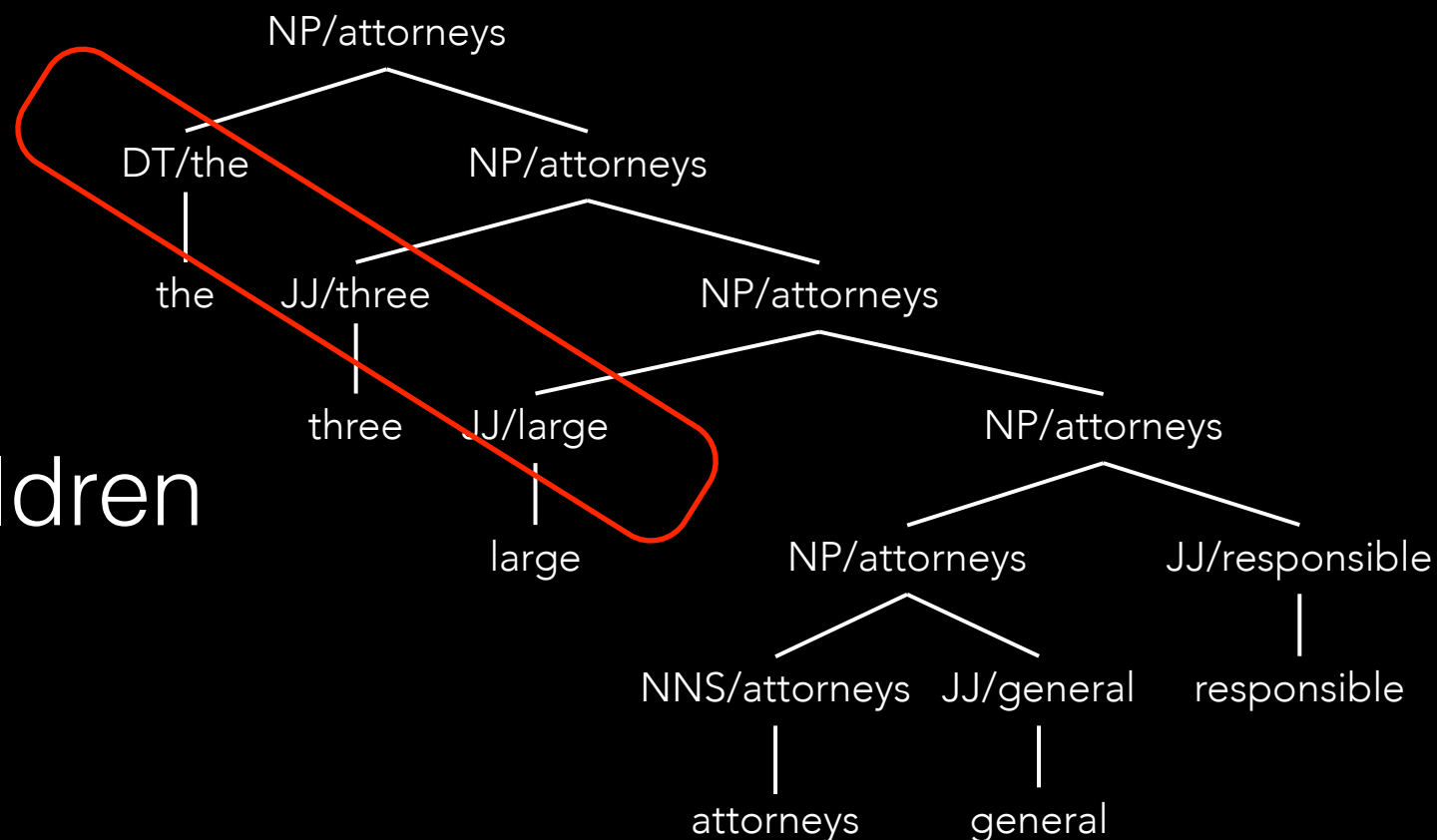
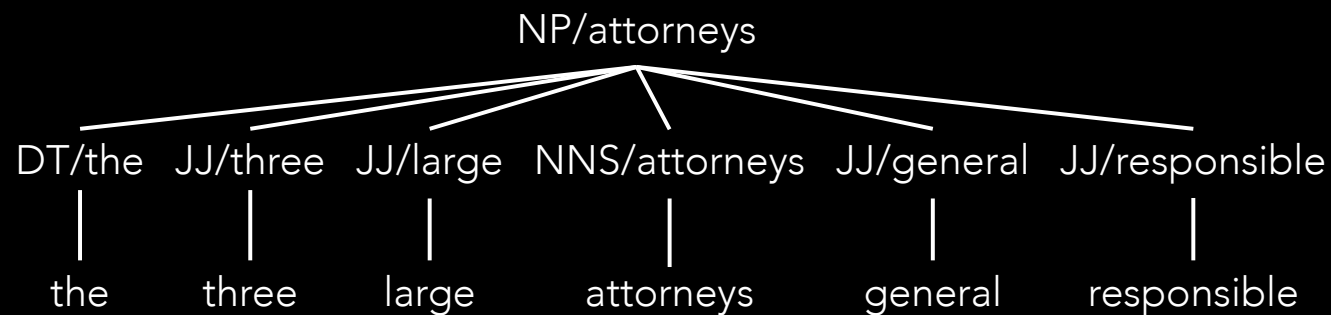
# Lexicalization and Binarization

More complicated example



# Lexicalization and Binarization

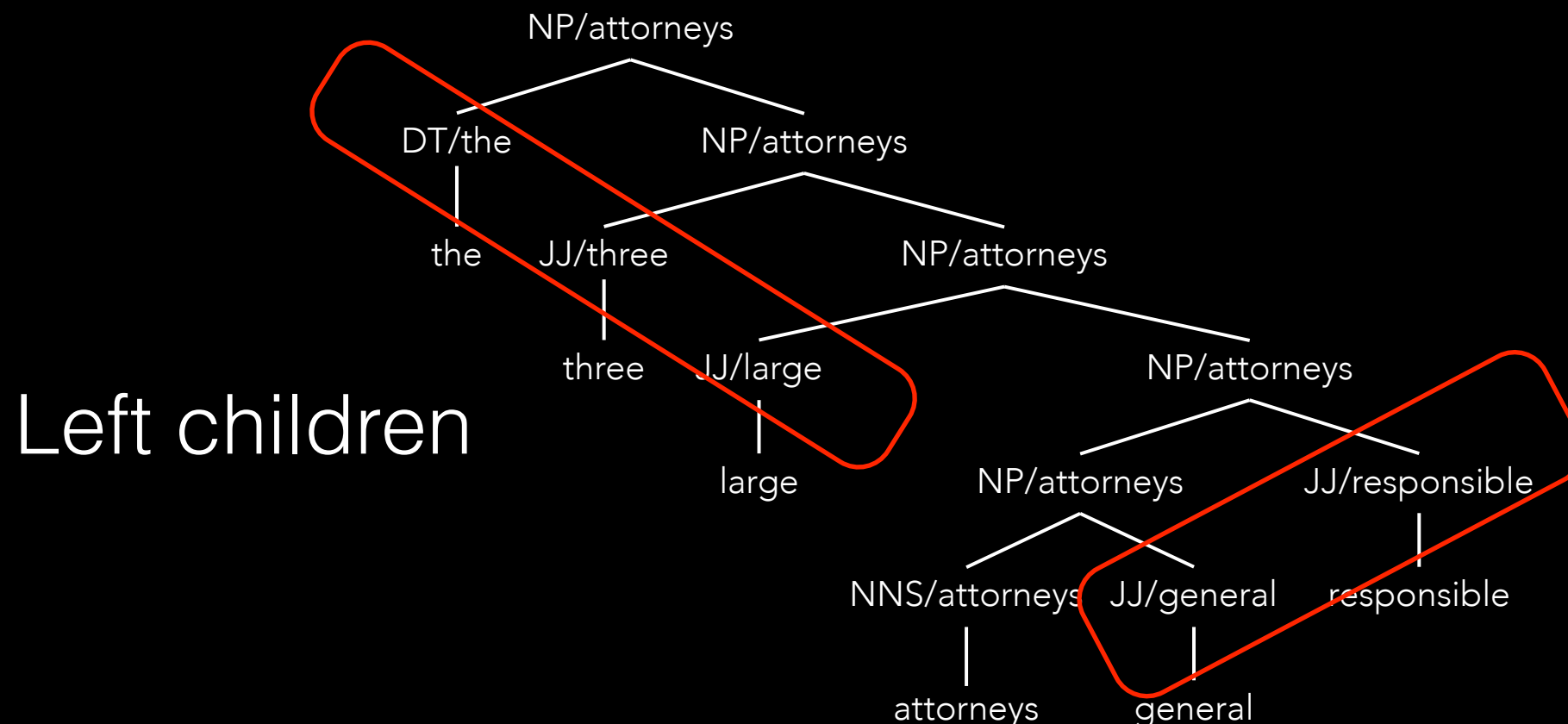
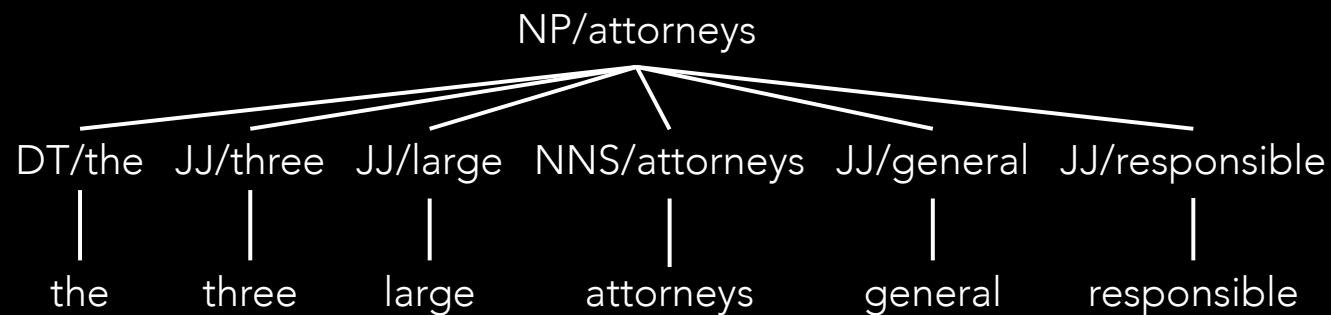
More complicated example



Left children

# Lexicalization and Binarization

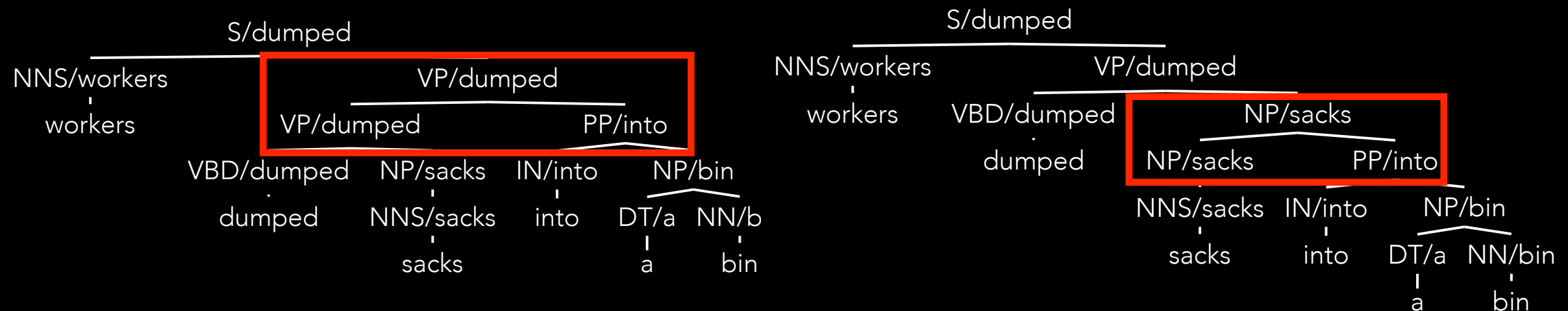
More complicated example



Left children

Right children

# Head lexicalization



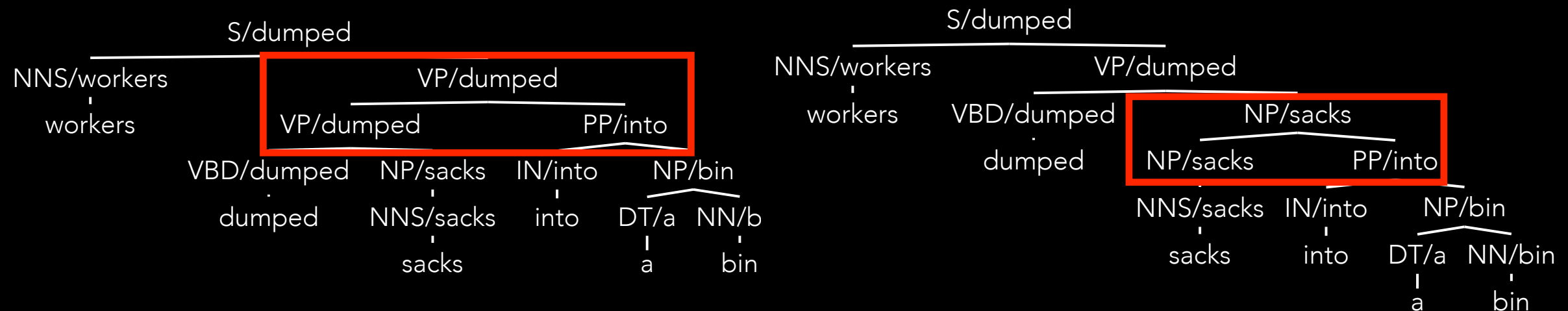
VP/dumped -> VP/dumped PP/into

more likely than

NP/sacks-> NP/sacks PP/into



# Head lexicalization



VP/dumped -> VP/dumped PP/into

more likely than

NP/sacks-> NP/sacks PP/into

But now our parameter space is getting very large  
and our estimates are going to be very poor!

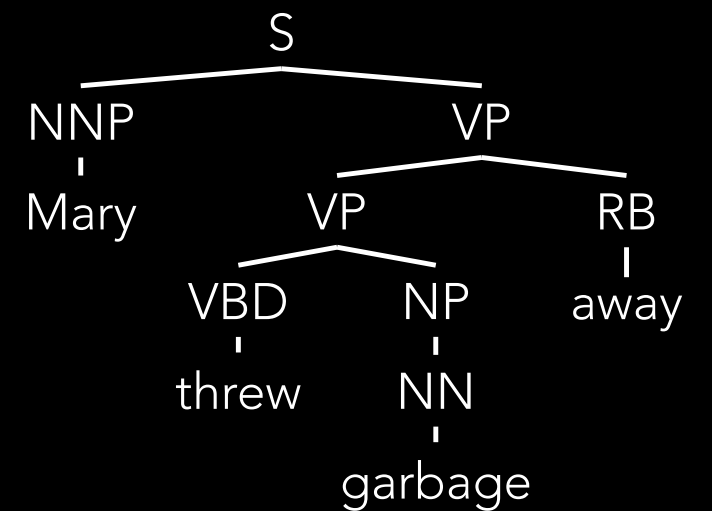
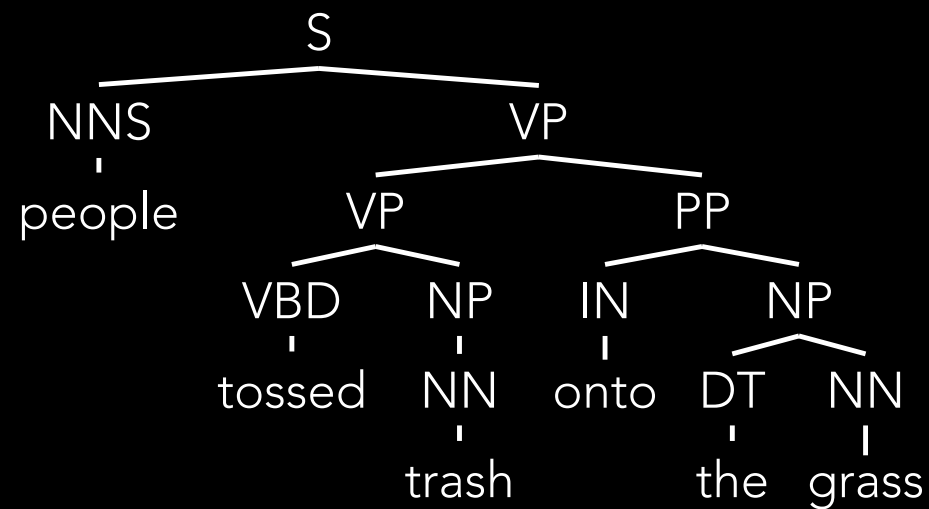
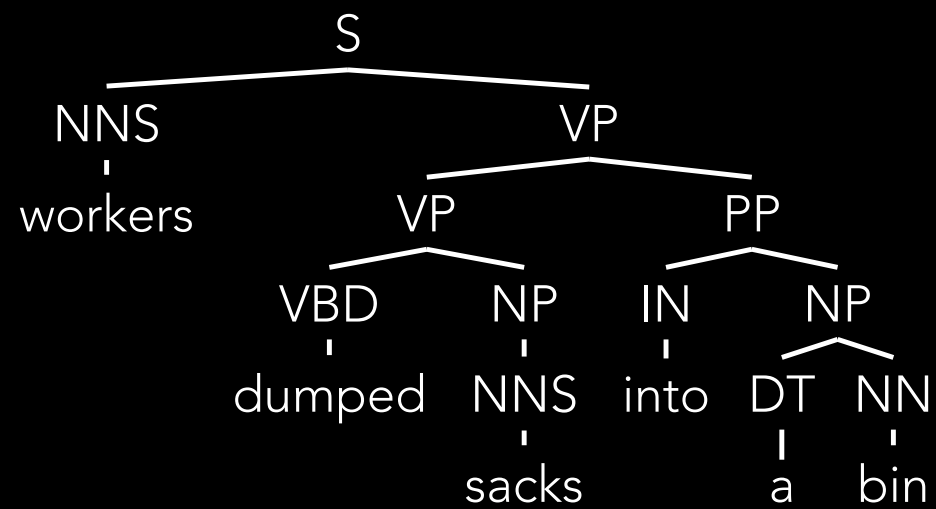
# Head lexicalization

# Head lexicalization

If your training data is

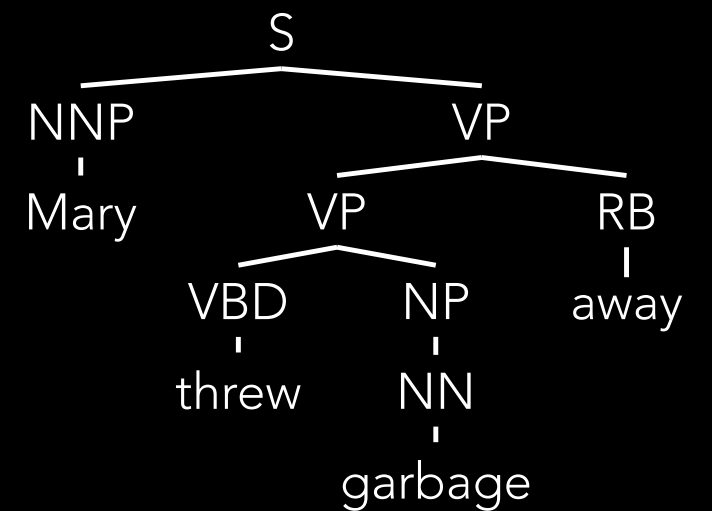
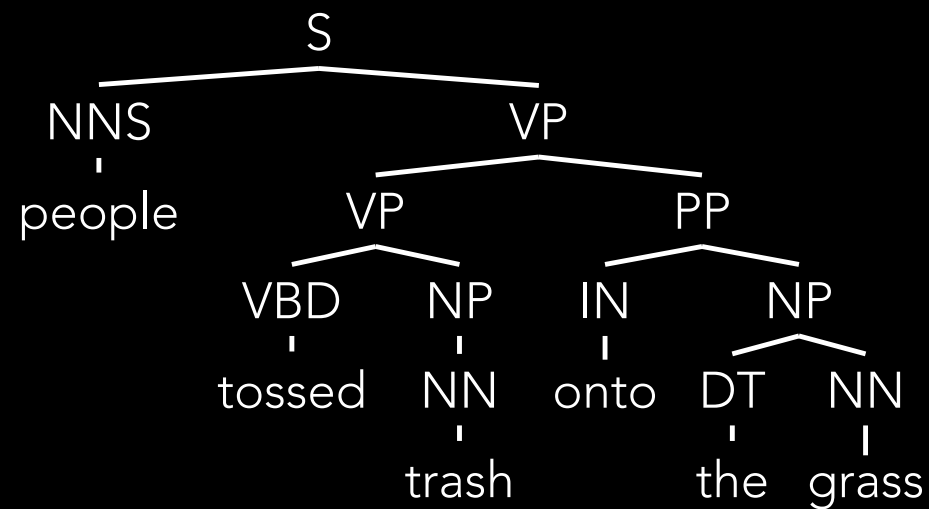
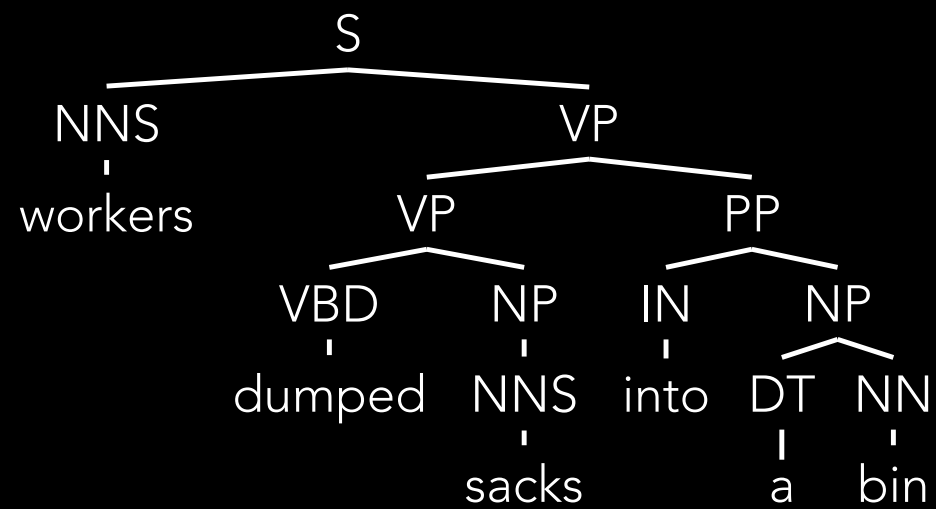
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# Head lexicalization

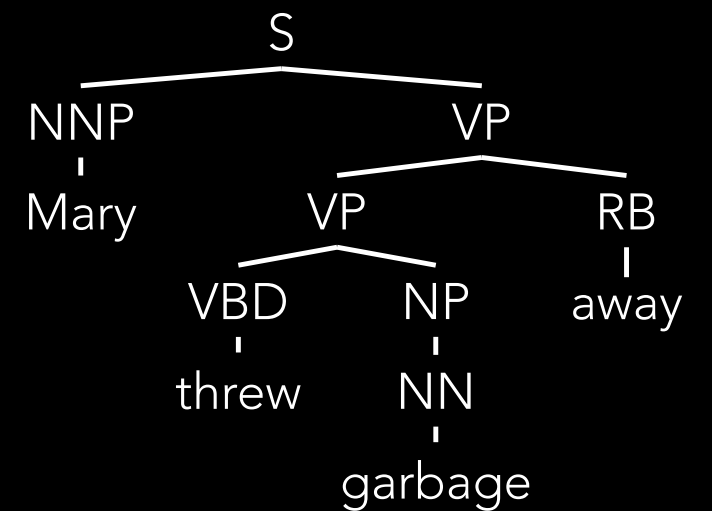
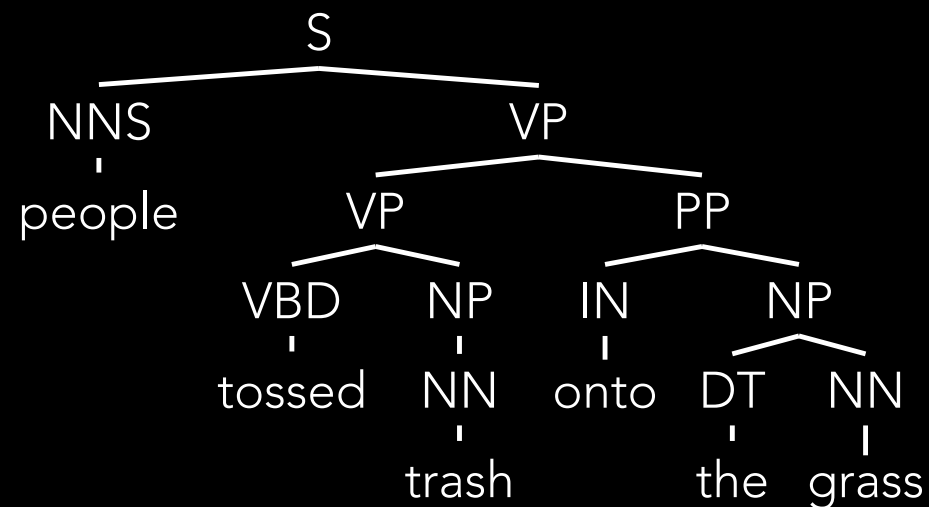
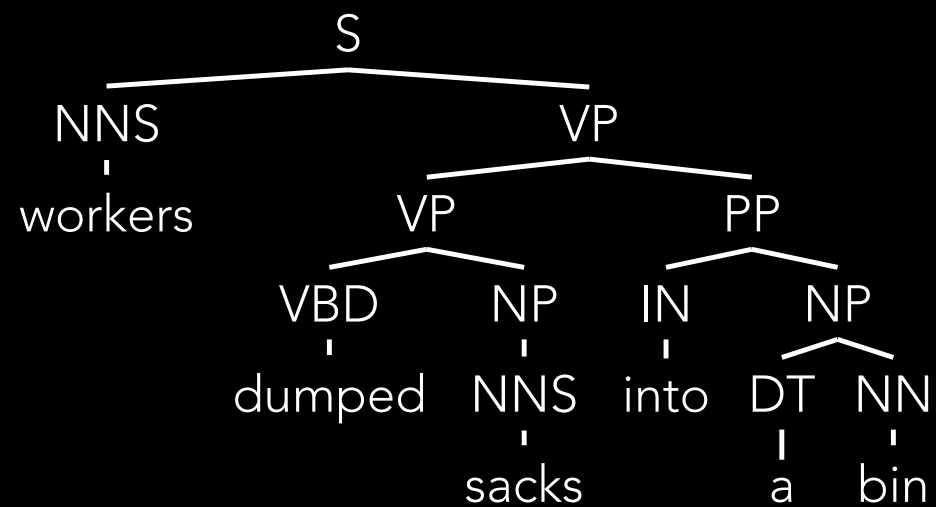
If your training data is



And you want to parse

# Head lexicalization

If your training data is

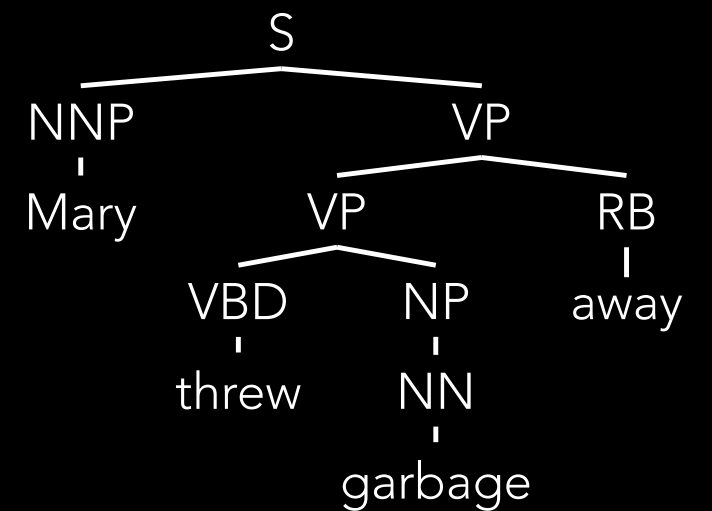
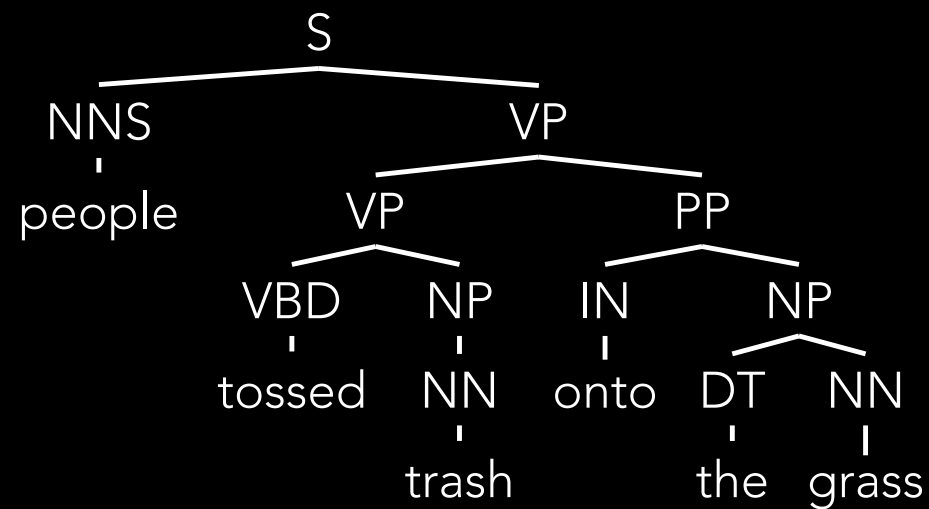
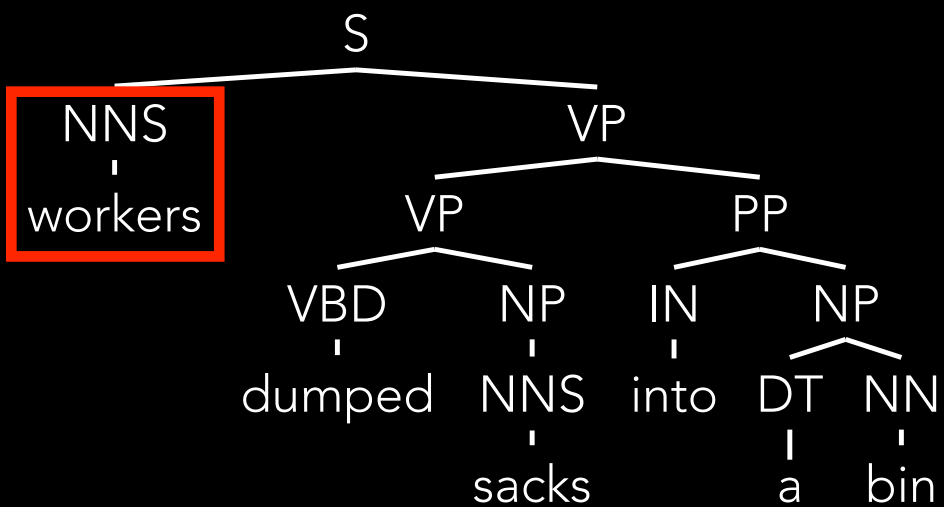


And you want to parse

workers threw trash  
onto the grass

# Head lexicalization

If your training data is



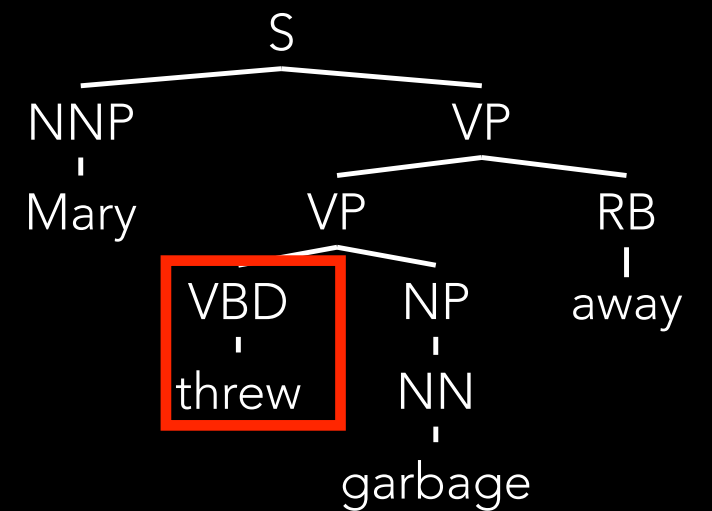
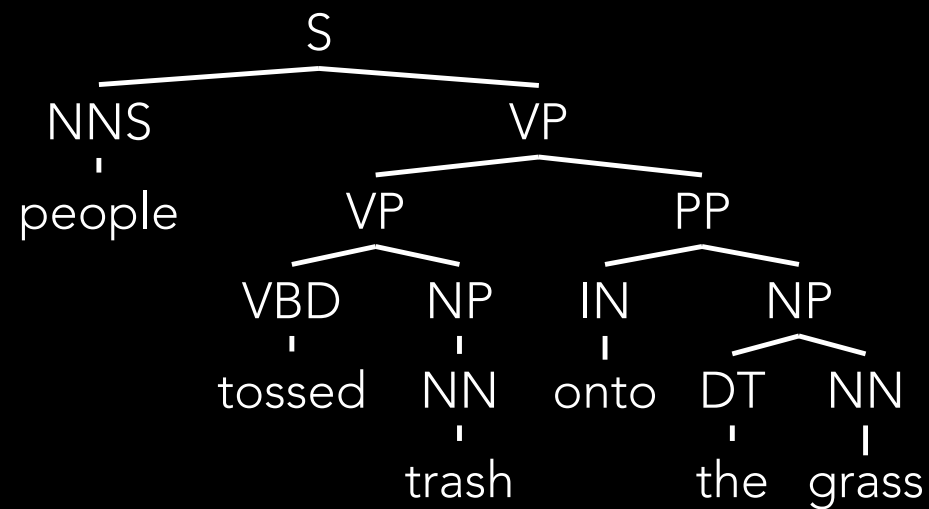
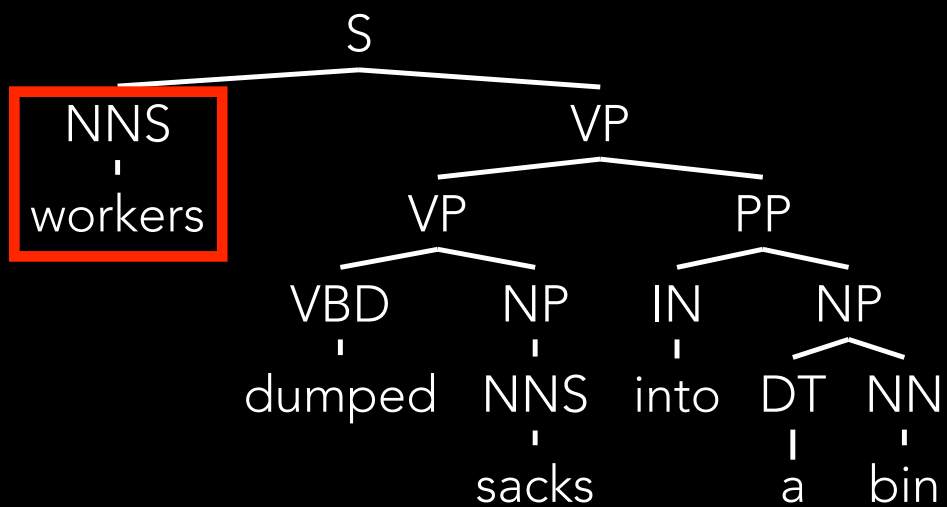
NNS  
workers

And you want to parse

workers threw trash  
onto the grass

# Head lexicalization

If your training data is



And you want to parse

workers threw trash  
onto the grass

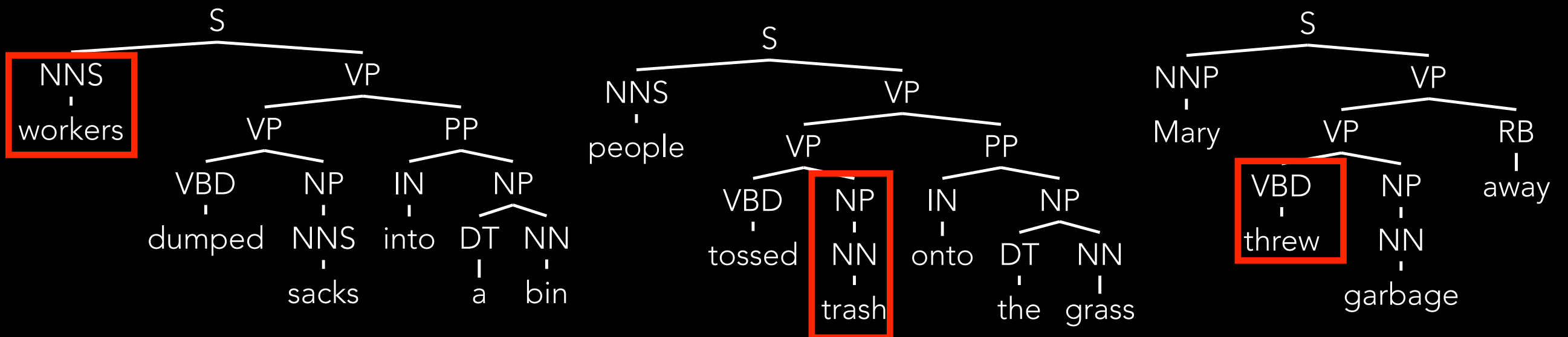
NNS  
|  
workers

VBD  
|  
threw



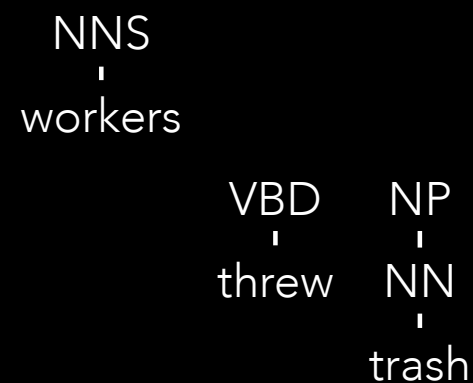
# Head lexicalization

If your training data is



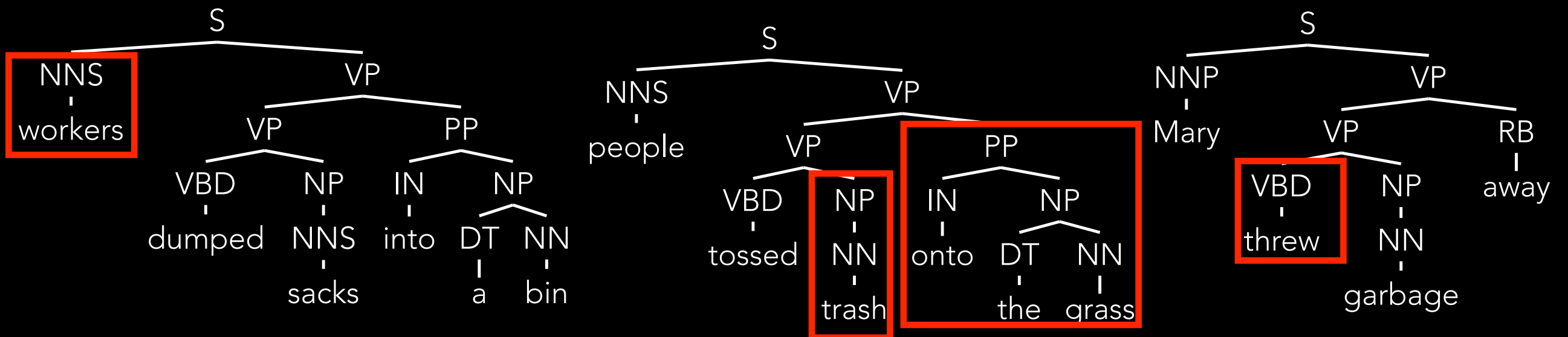
And you want to parse

workers threw trash  
onto the grass



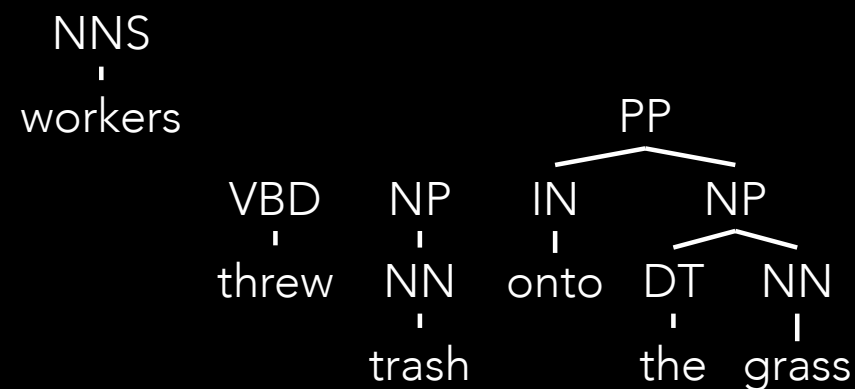
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If your training data is



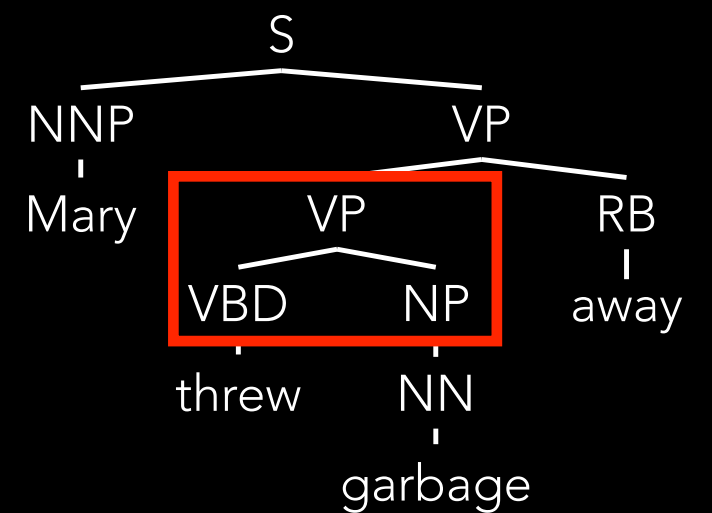
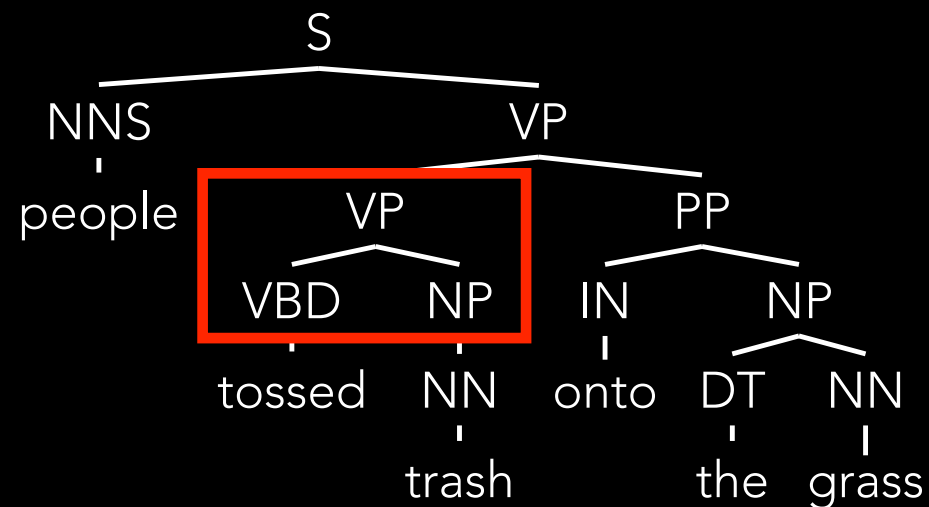
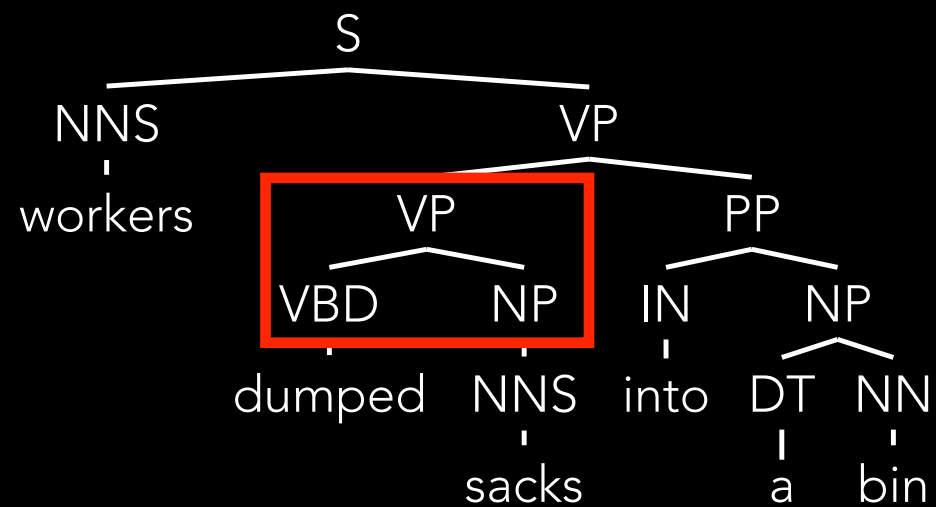
And you want to parse

workers threw trash  
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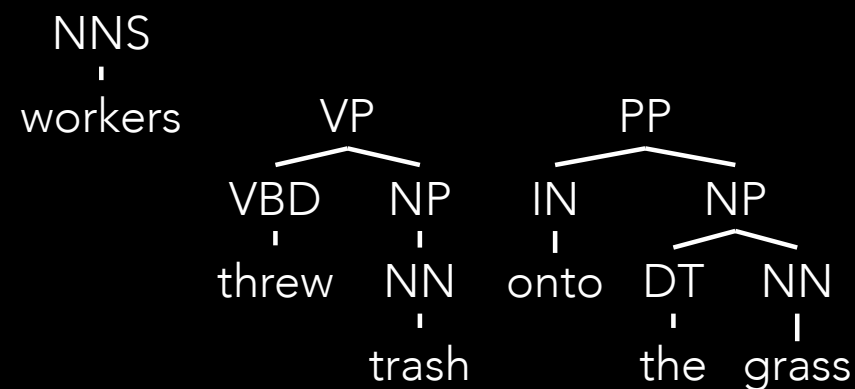
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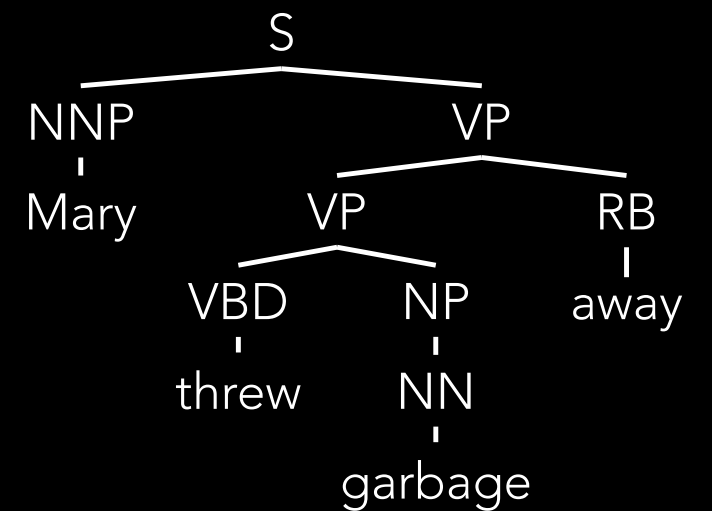
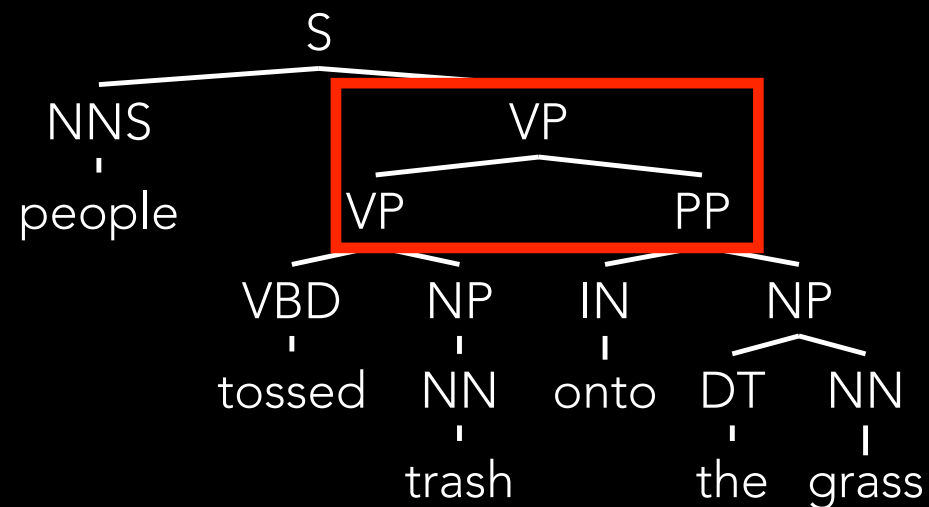
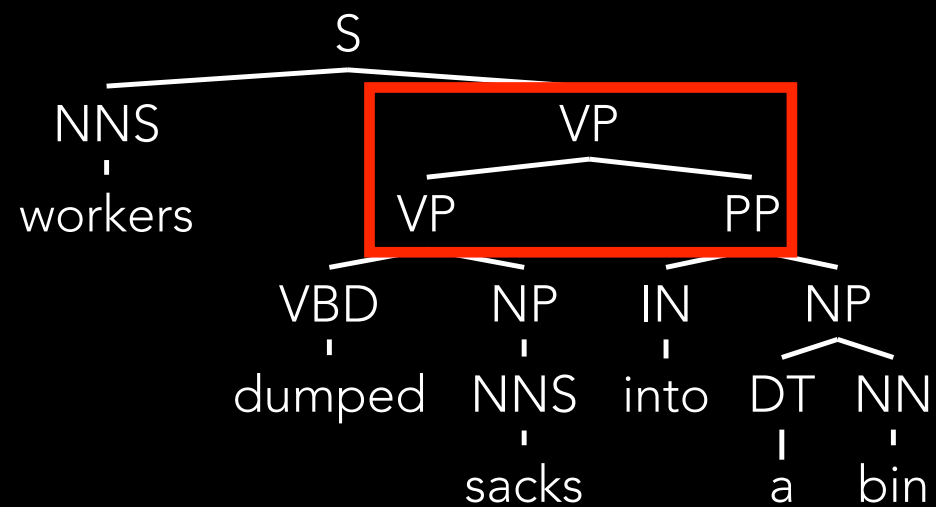
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workers threw trash  
onto the grass



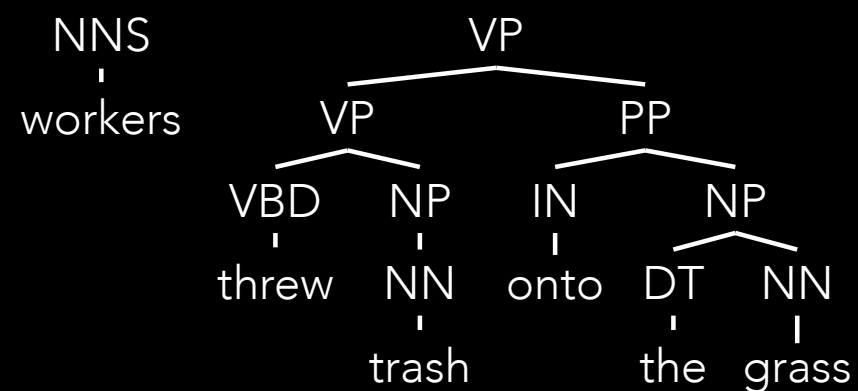
# Head lexicalization

If your training data is



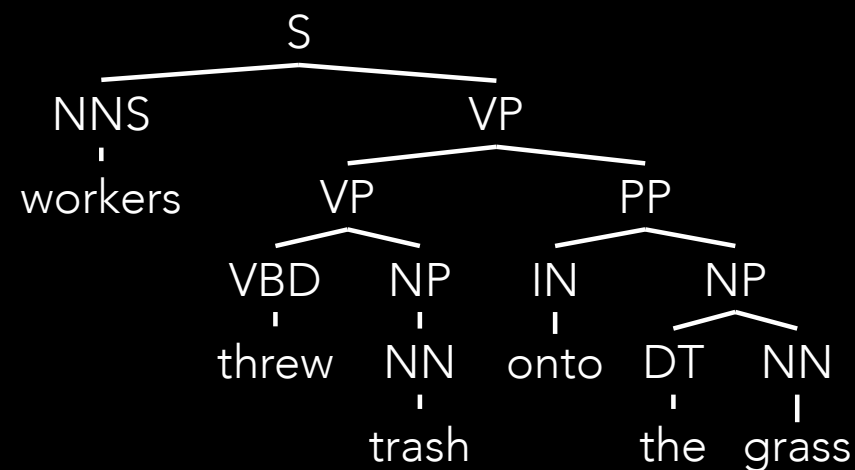
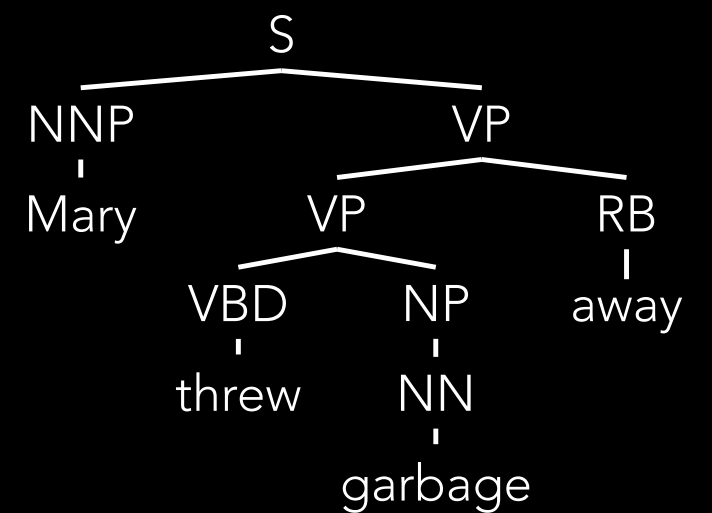
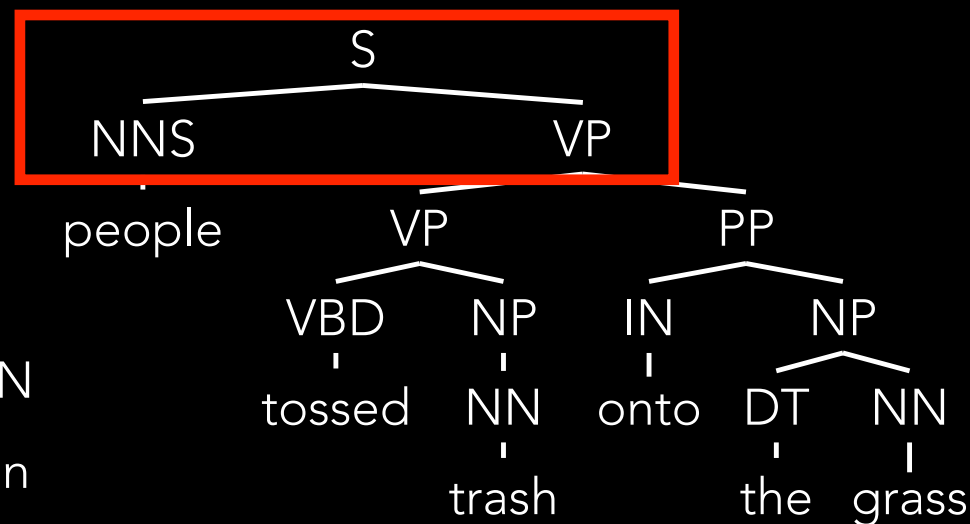
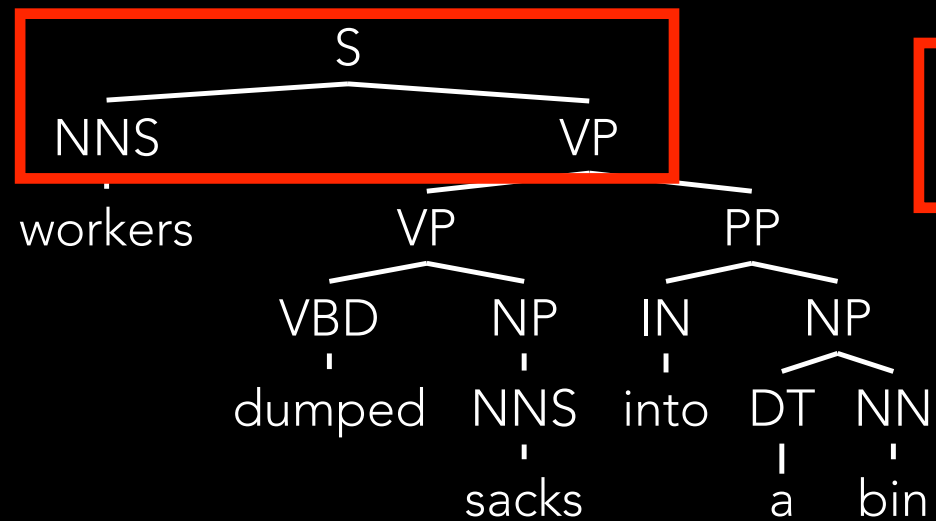
And you want to parse

workers threw trash  
onto the grass



# Head lexicalization

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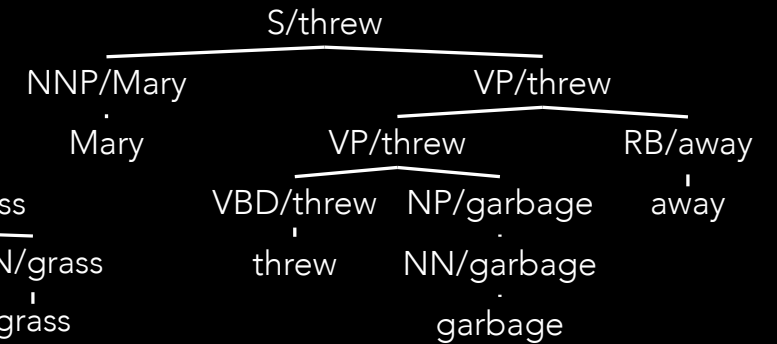
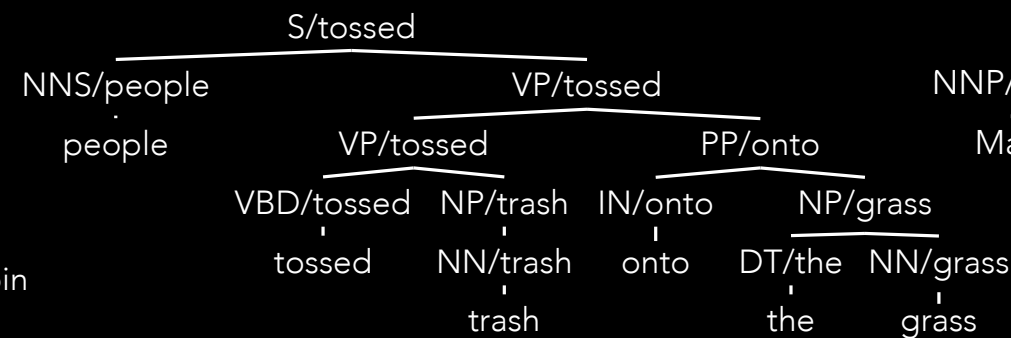
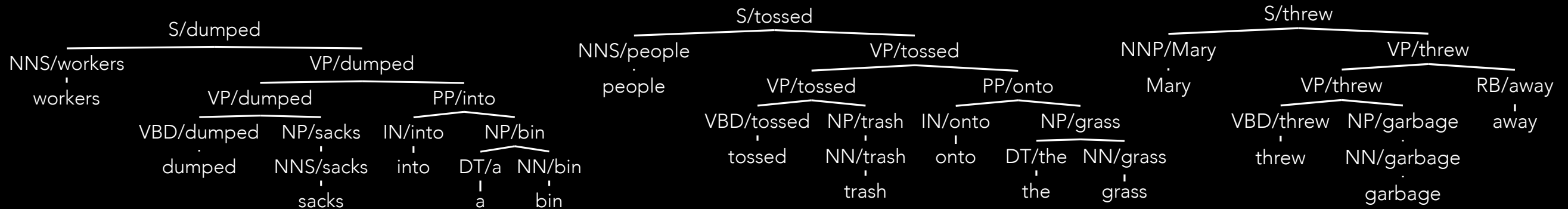
And you want to parse

workers threw trash  
onto the grass

You can!

# Head lexicalization

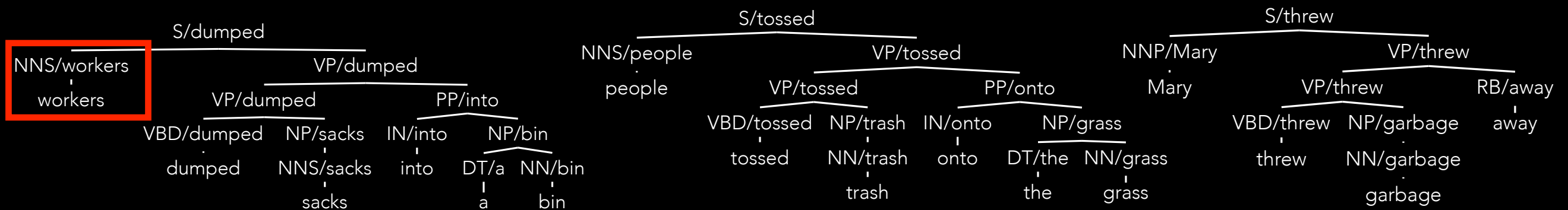
But if we lexicalize



workers threw trash  
onto the grass

# Head lexicalization

But if we lexicalize

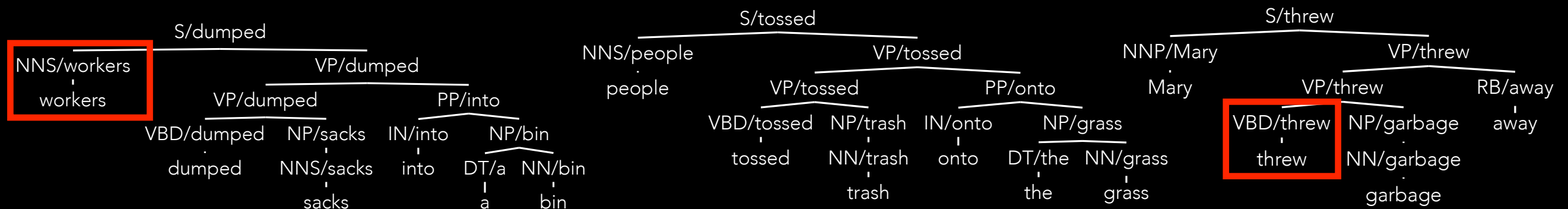


workers threw trash  
onto the grass

NNS/workers  
workers

# Head lexicalization

But if we lexicalize



workers threw trash  
onto the grass

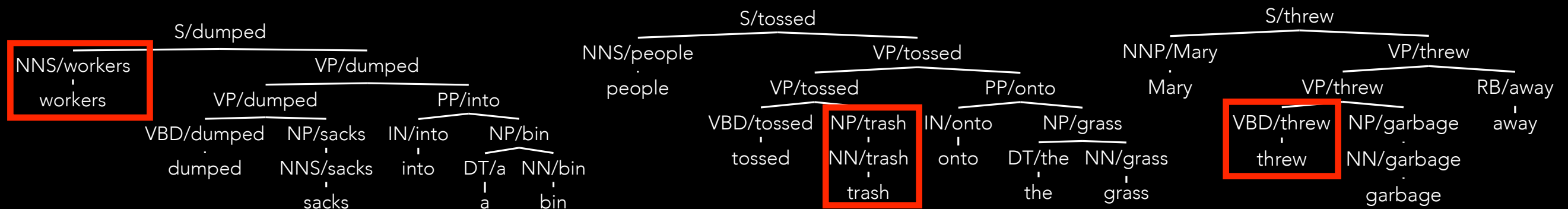
NNS/workers  
workers

VBD/threw  
threw



# Head lexicalization

But if we lexicalize



workers threw trash  
onto the grass

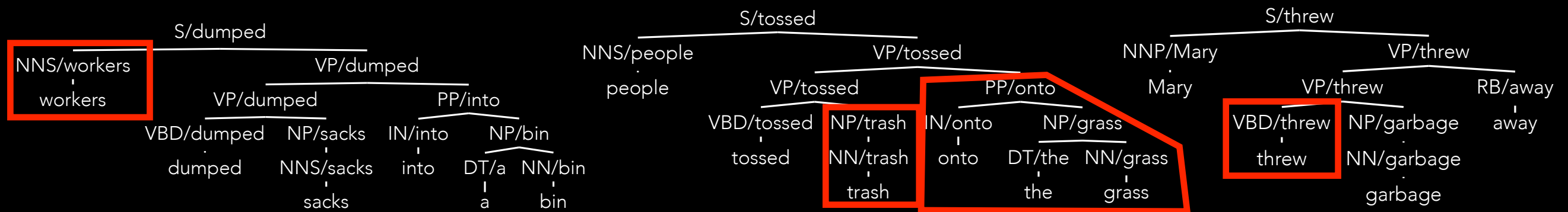
NNS/workers  
workers

VBD/threw  
threw

NP/trash  
NN/trash  
trash

# Head lexicalization

But if we lexicalize

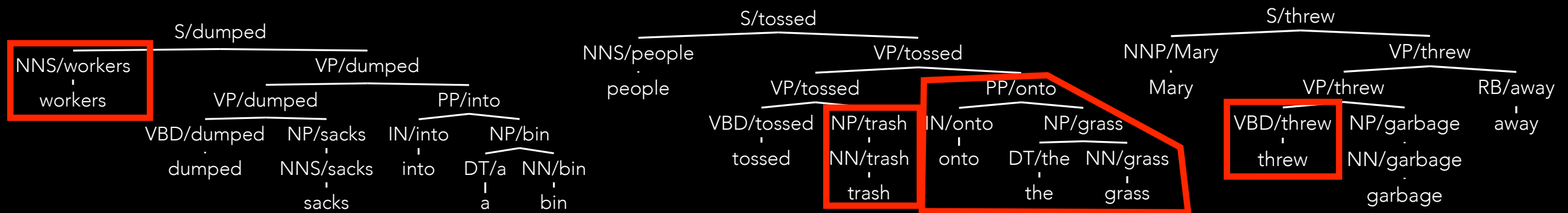


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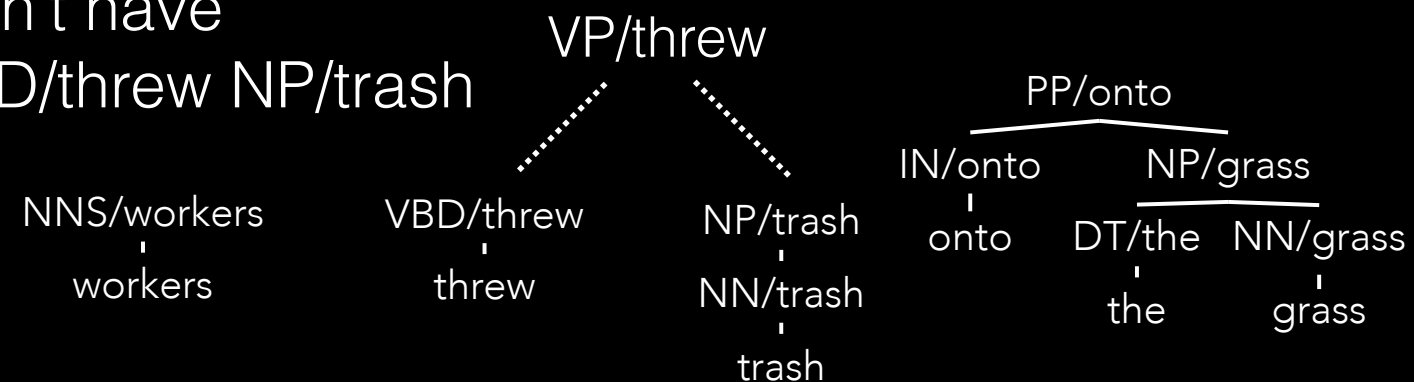
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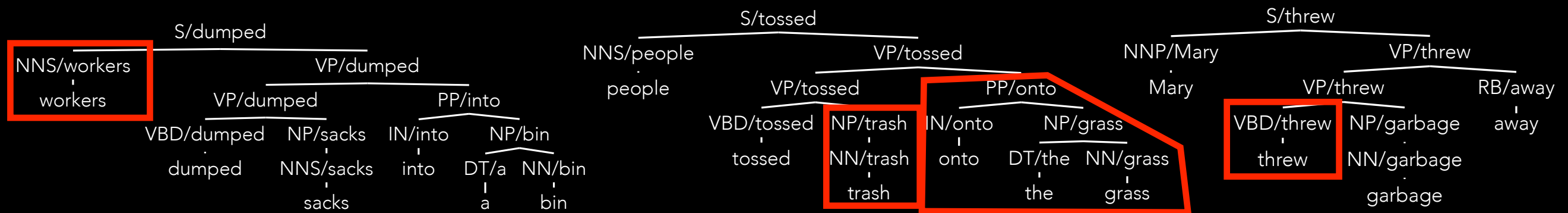
workers threw trash  
onto the grass

We don't have  
VP/threw -> VBD/threw NP/trash



# Head lexicalization

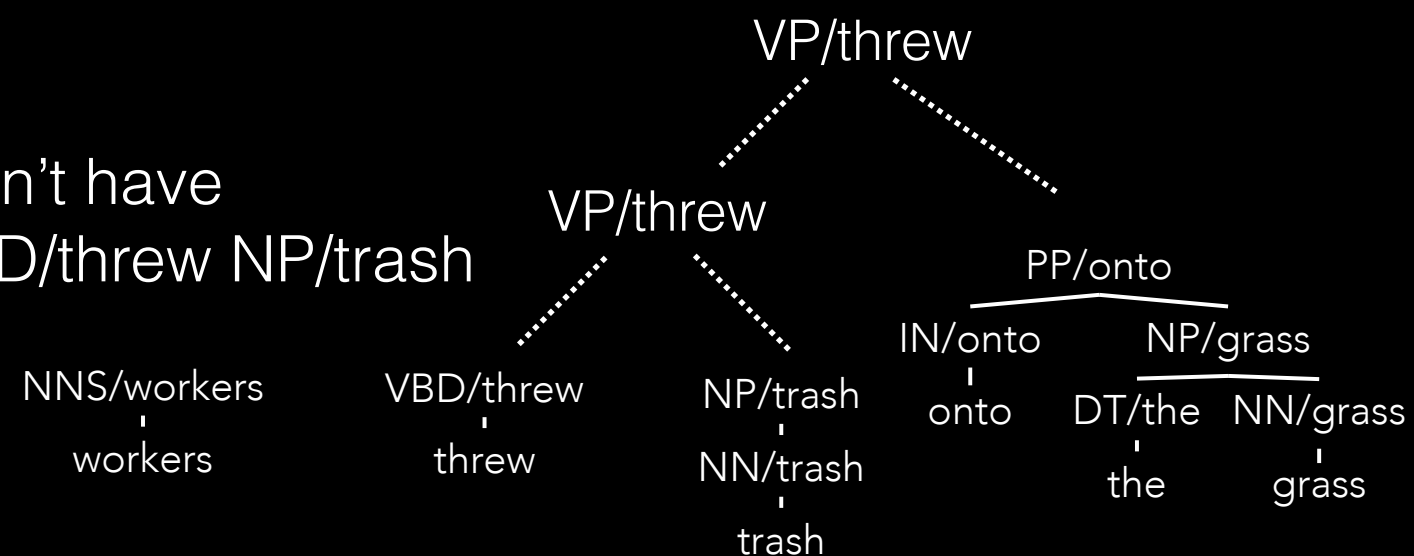
But if we lexicalize



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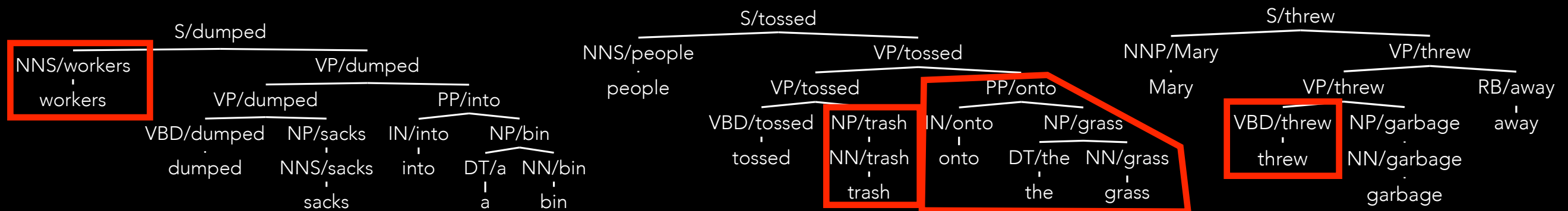
We don't have  
VP/threw → VP/threw PP/onto

We don't have  
VP/threw → VBD/threw NP/trash



# Head lexicalization

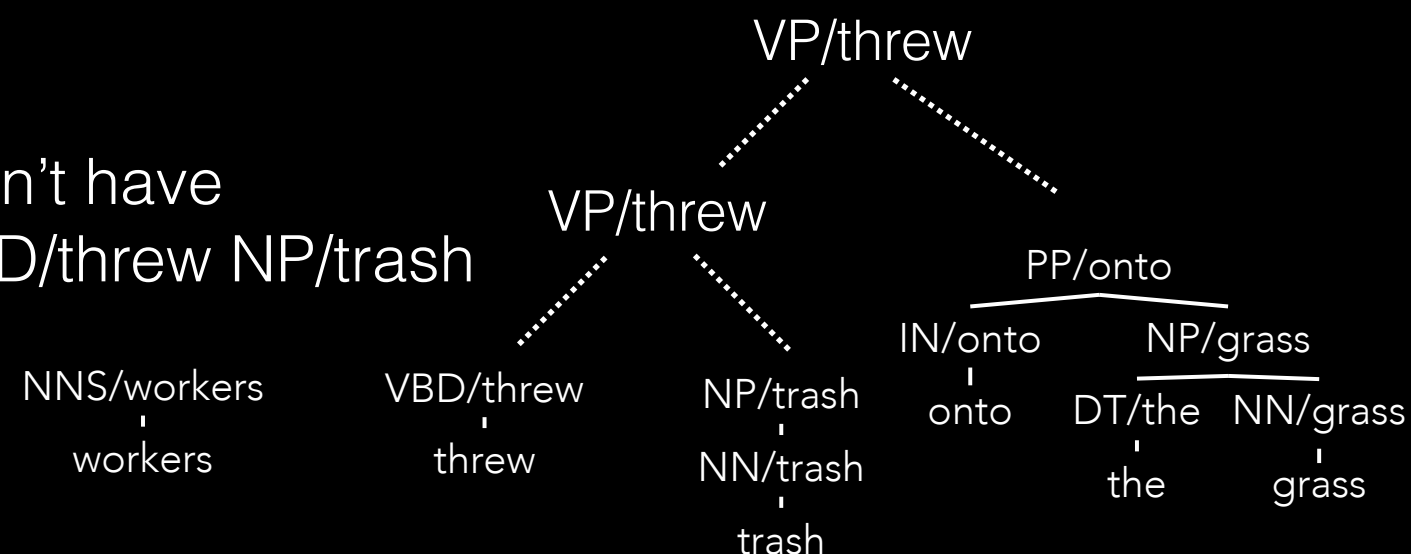
But if we lexicalize



workers threw trash  
onto the grass

We don't have  
VP/threw → VP/threw PP/onto

We don't have  
VP/threw → VBD/threw NP/trash



Now we have a problem!

# Smoothing Lexicalized PCFGs

We want to estimate

$$P(\text{VP/threw} \rightarrow \text{VP/threw PP/onto} \mid \text{VP/threw})$$

# Smoothing Lexicalized PCFGs

We want to estimate

$$\begin{aligned} &P(\text{VP/threw} \rightarrow \text{VP/threw PP/onto} \mid \text{VP/threw}) \\ &= P(\text{VP} \rightarrow \underline{\text{VP}} \text{ PP, onto} \mid \text{VP, threw}) \end{aligned}$$

# Smoothing Lexicalized PCFGs

We want to estimate

$$P(\text{VP/threw} \rightarrow \text{VP/threw PP/onto} \mid \text{VP/threw})$$

$$= P(\text{VP} \rightarrow \underline{\text{VP}} \text{ PP, onto} \mid \text{VP, threw})$$

or more generally

$$P(X \rightarrow YZ, m \mid X, h)$$



# Smoothing Lexicalized PCFGs

We want to estimate

$$P(\text{VP/threw} \rightarrow \text{VP/threw PP/onto} \mid \text{VP/threw})$$

$$= P(\text{VP} \rightarrow \underline{\text{VP}} \text{ PP, onto} \mid \text{VP, threw})$$

or more generally

$$P(X \rightarrow YZ, m \mid X, h)$$

since  $X$  and  $h$  were already chosen, leaving the rule and the lexicalization of the non-head path to choose.

# Smoothing Lexicalized PCFGs

First apply the chain rule

# Smoothing Lexicalized PCFGs

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$$P(X \rightarrow YZ, m \mid X, h) = P(X \rightarrow YZ \mid X, h) P(m \mid X \rightarrow YZ, X, h)$$

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Now we consider a means for smoothing  
each of these components

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Interpolate  $P(X \rightarrow YZ \mid X, h)$  with  $P(X \rightarrow YZ \mid X)$

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Interpolate  $P(X \rightarrow YZ \mid X, h)$  with  $P(X \rightarrow YZ \mid X)$

Interpolate  $P(m \mid X \rightarrow YZ, X, h)$  with  $P(m \mid X \rightarrow YZ)$



# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  
h be its head, and  $m$  be its modifier

# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  
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$$P(r, m \mid X, h) = P(r \mid X, h) P(m \mid r, X, h)$$

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rule model

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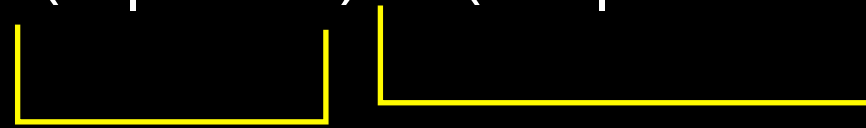


rule model   modifier model

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rule model   modifier model

Rule Model

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rule model    modifier model


## Rule Model

$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

# Smoothing Lexicalized PCFGs

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rule model    modifier model

## Rule Model

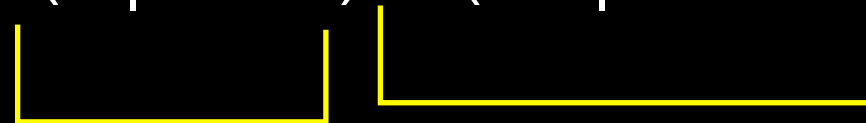
$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

$$P_{ML}(r \mid X, h) = \frac{\text{count}(r, h)}{\text{count}(X, h)}$$

# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  
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rule model    modifier model

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$$P_{ML}(r \mid X, h) = \frac{\text{count}(r, h)}{\text{count}(X, h)} \quad \begin{array}{l} X/h \rightarrow Y/h \ Z/^* \\ X/h \end{array}$$



# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  $h$  be its head, and  $m$  be its modifier

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# Smoothing Lexicalized PCFGs

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$$P_{ML}(r \mid X) = \frac{\text{count}(r)}{\text{count}(X)} \quad \begin{array}{c} X/^* \rightarrow Y/^* \ Z/^* \\ X/^* \end{array}$$

# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  $h$  be its head, and  $m$  be its modifier

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 rule model    modifier model

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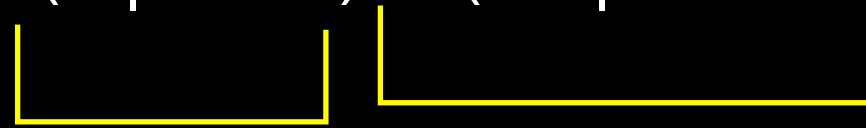
$$P_{ML}(r \mid X, h) = \frac{\text{count}(r, h)}{\text{count}(X, h)} \quad \begin{array}{c} X/h \rightarrow Y/h \ Z/^* \\ X/h \end{array}$$

$$P_{ML}(r \mid X) = \frac{\text{count}(r)}{\text{count}(X)} \quad \begin{array}{c} X/^* \rightarrow Y/^* \ Z/^* \\ X/^* \end{array} \quad \begin{array}{l} \text{Vanilla} \\ \text{PCFG!} \end{array}$$

# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  
 $h$  be its head, and  $m$  be its modifier

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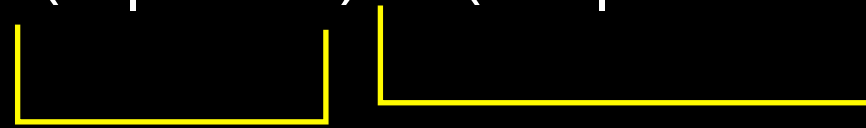
rule model   modifier model

Modifier Model

# Smoothing Lexicalized PCFGs

Let  $r$  be a vanilla rule (e.g.  $X \rightarrow YZ$ ),  $X$  be its root symbol,  
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$$P(r, m \mid X, h) = P(r \mid X, h) P(m \mid r, X, h)$$



rule model   modifier model


## Modifier Model

$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

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rule model   modifier model

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$$P_{ML}(m \mid r) = \frac{\text{count}(m, r)}{\text{count}(r)}$$



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# Head lexicalization

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By decomposing we can estimate unseen lexicalized rules

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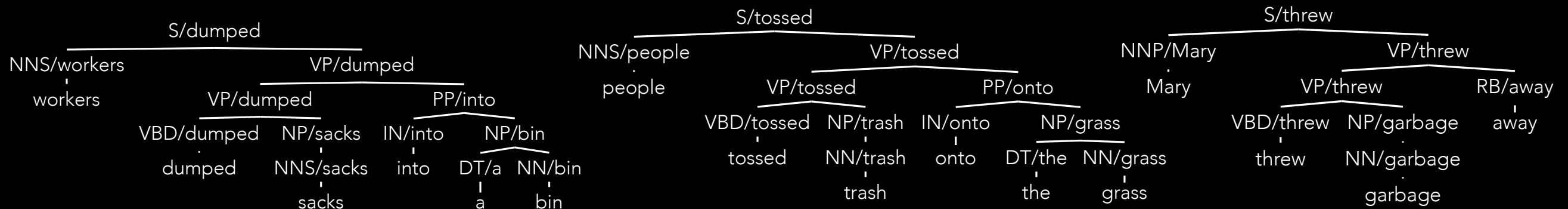
By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times

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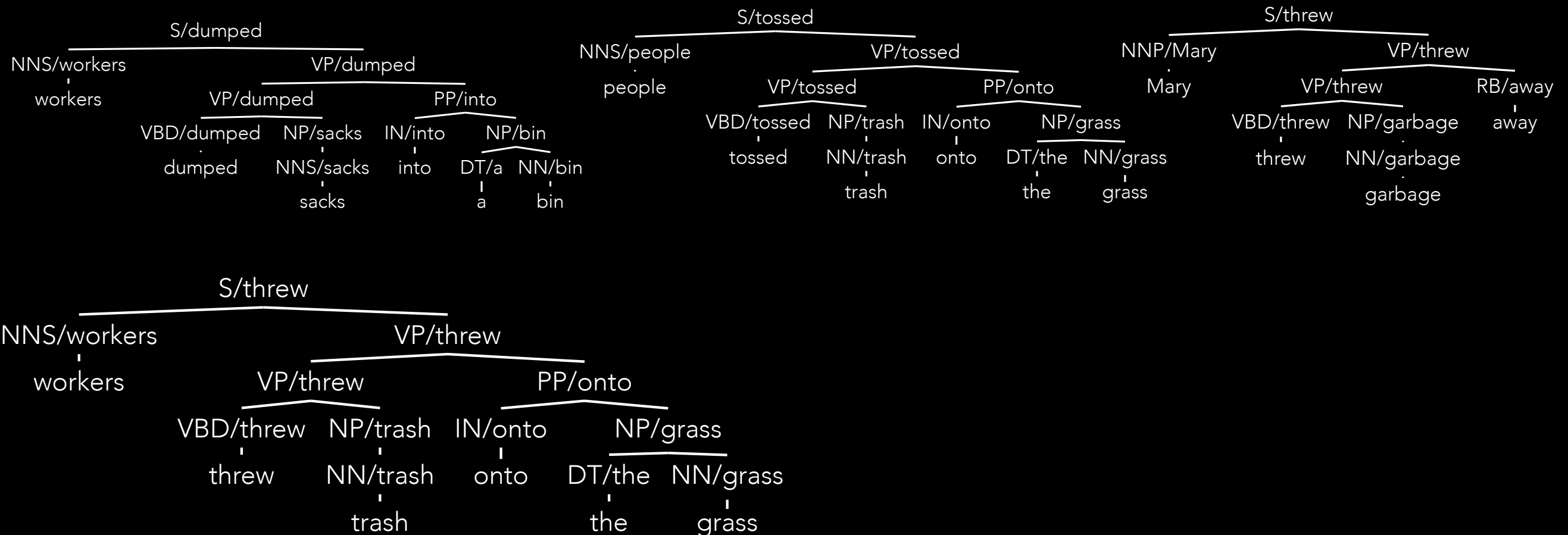
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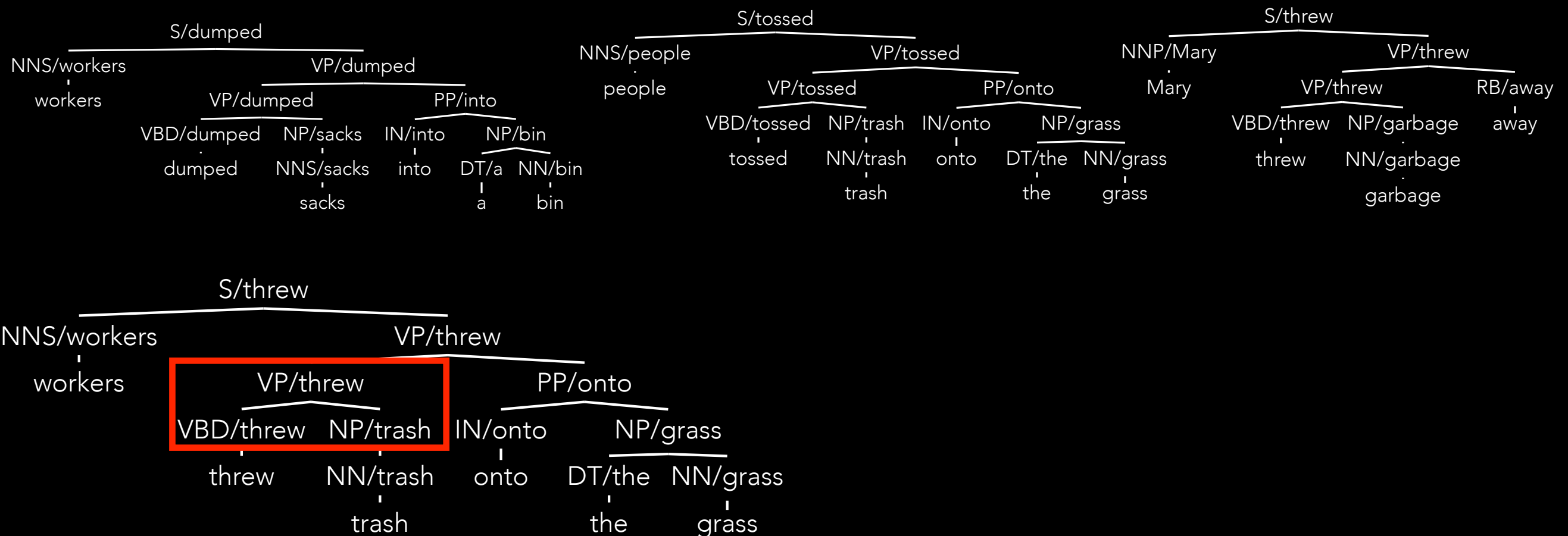
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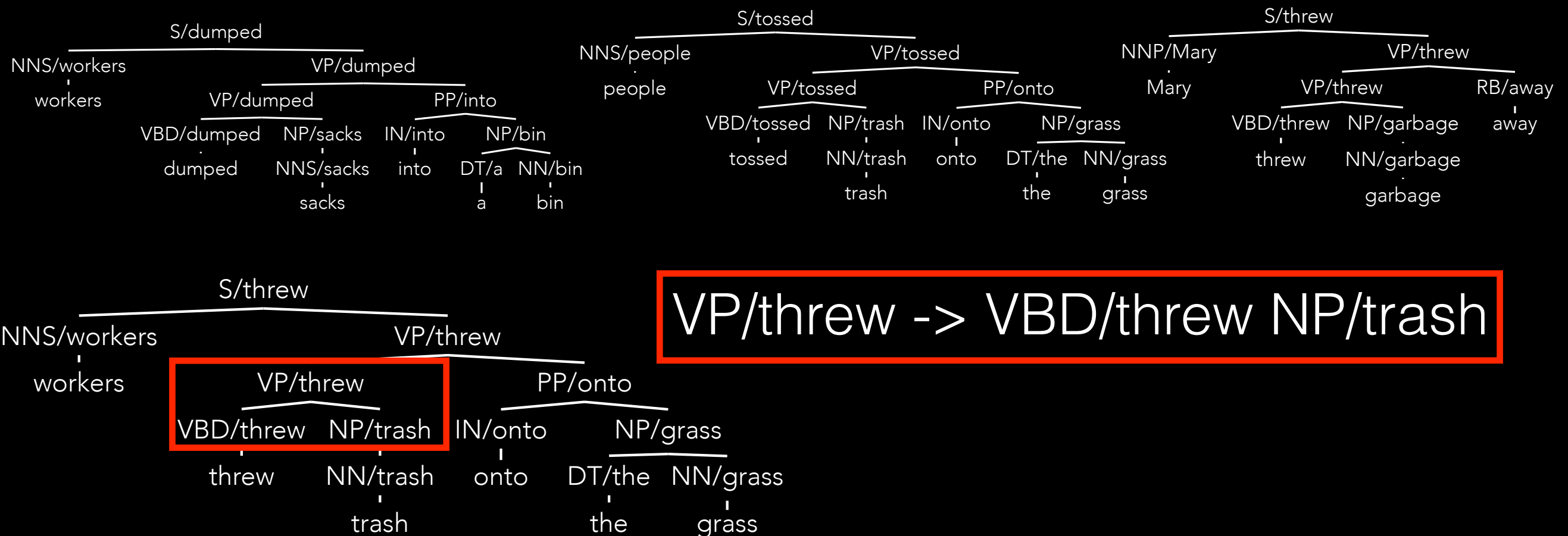
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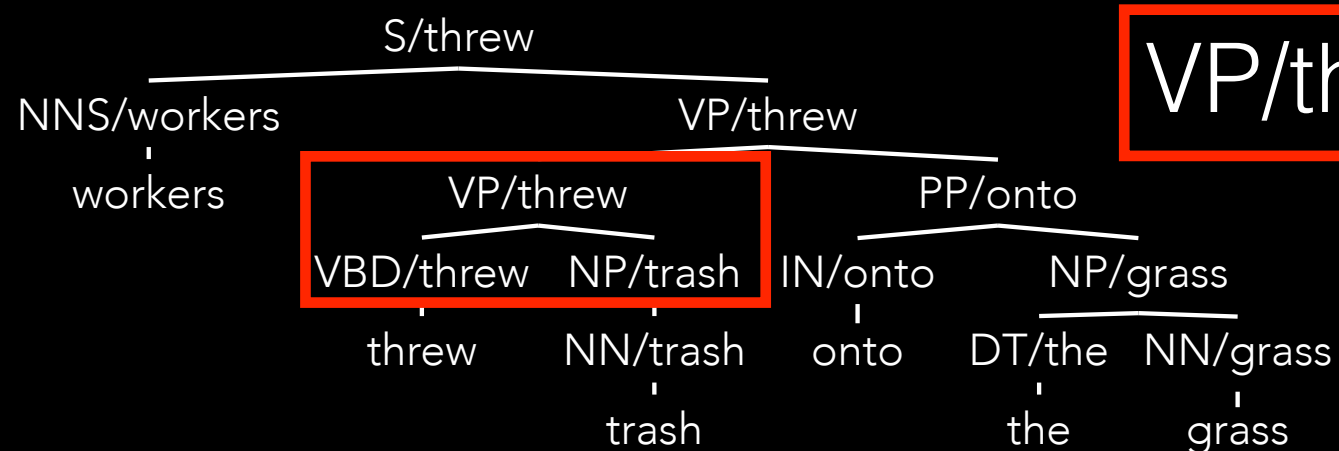
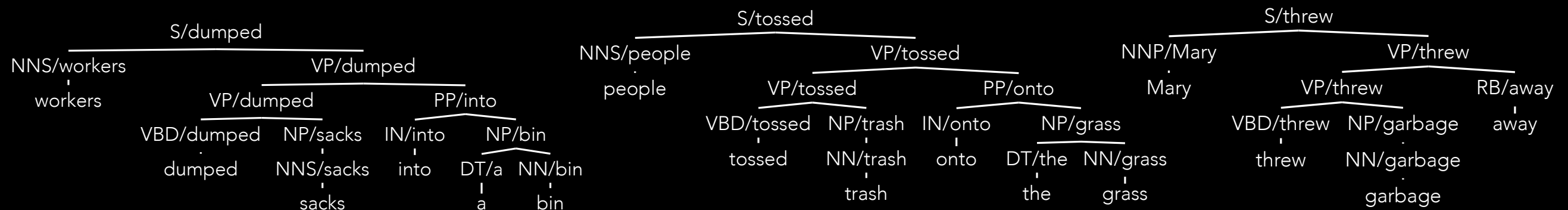




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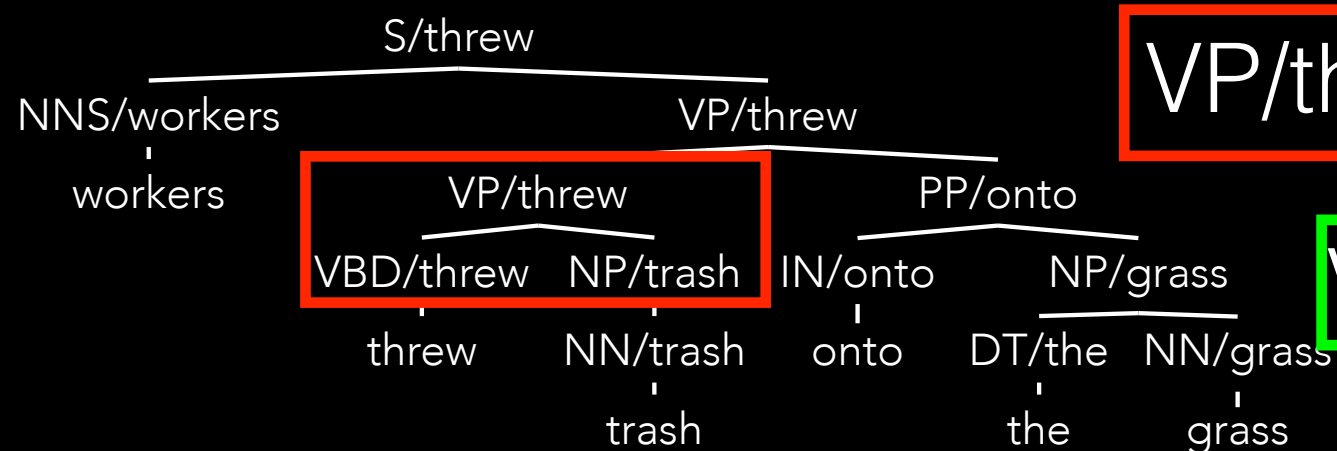
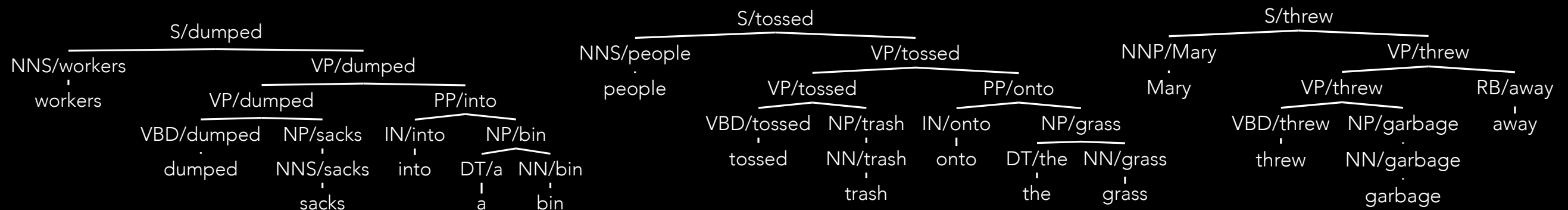
VP/threw → VBD/threw NP/trash

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VP/threw -> VBD/threw NP/trash

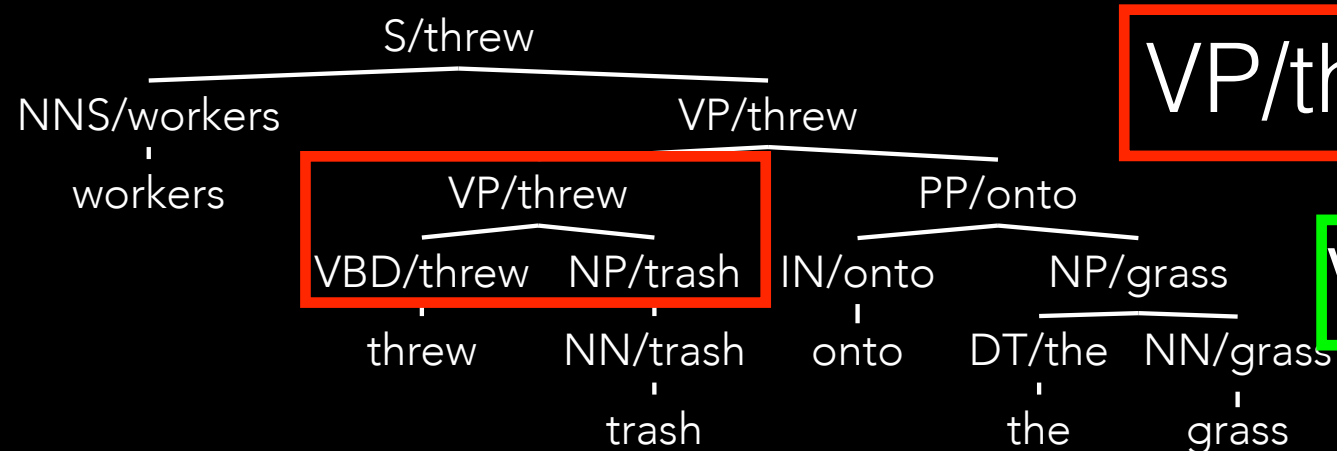
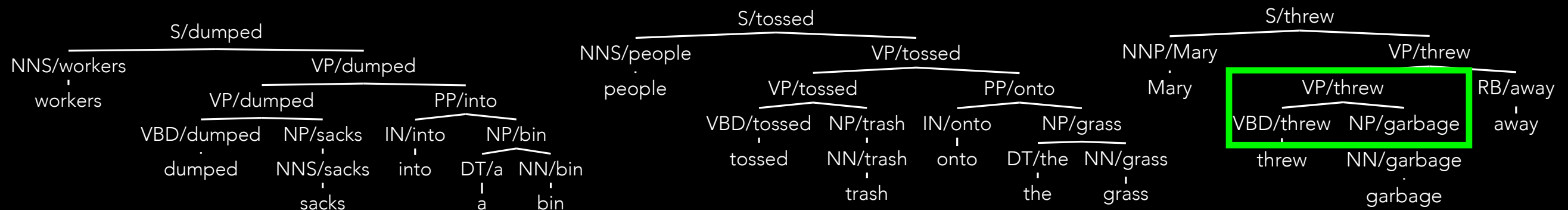
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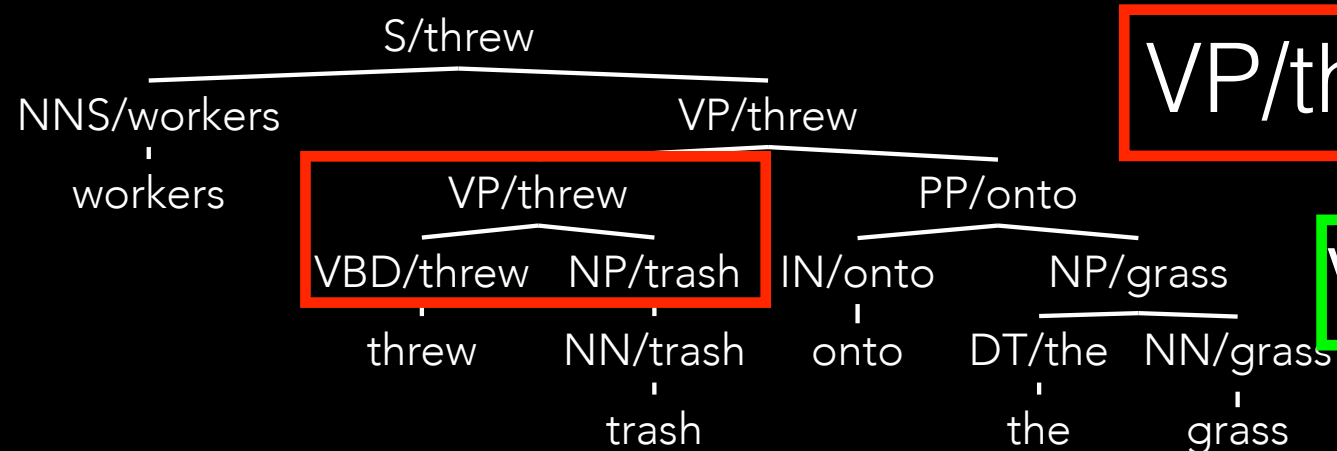
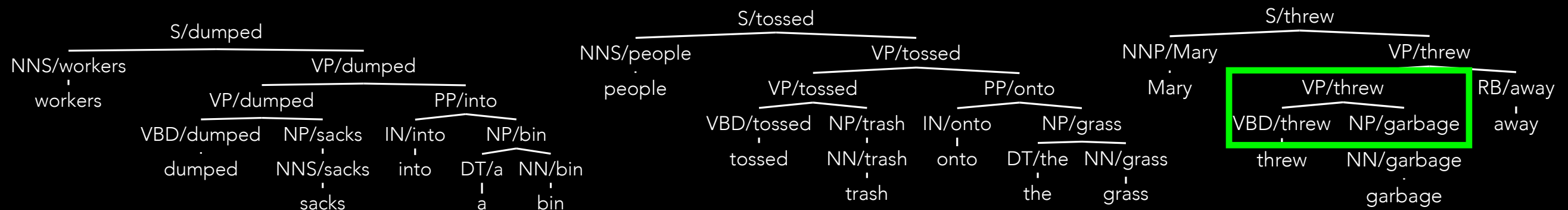
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VP/threw -> VBD/threw NP/trash

VP/threw -> VBD/threw NP

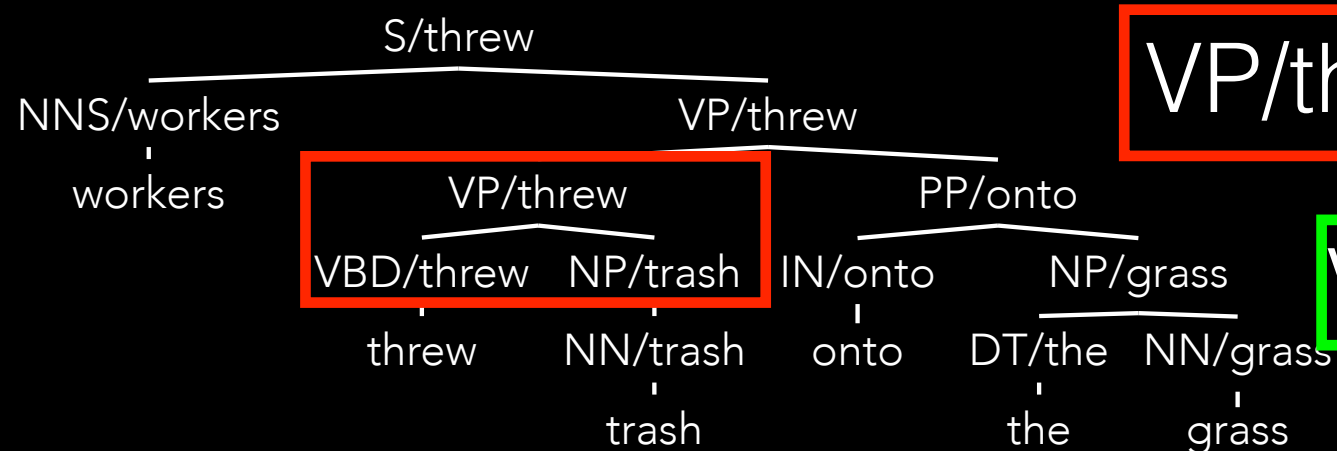
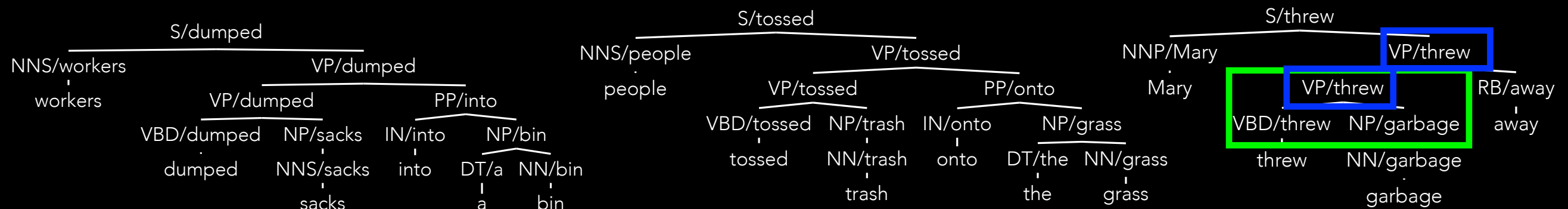
VP/threw -> ...

$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP/threw -> VBD/threw NP

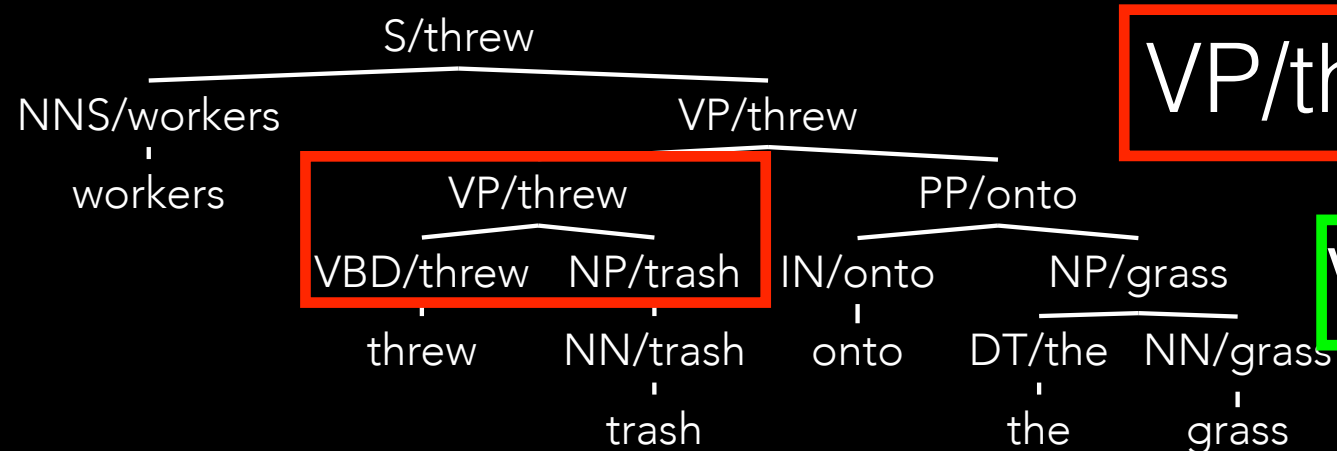
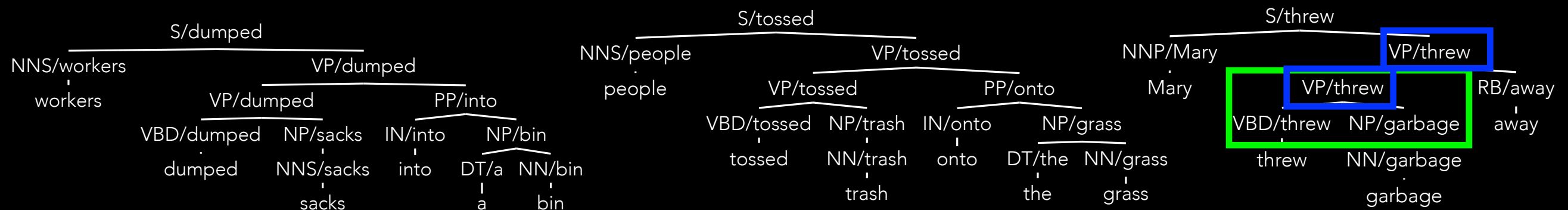
VP/threw -> ...

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP/threw -> VBD/threw NP

VP/threw -> ...

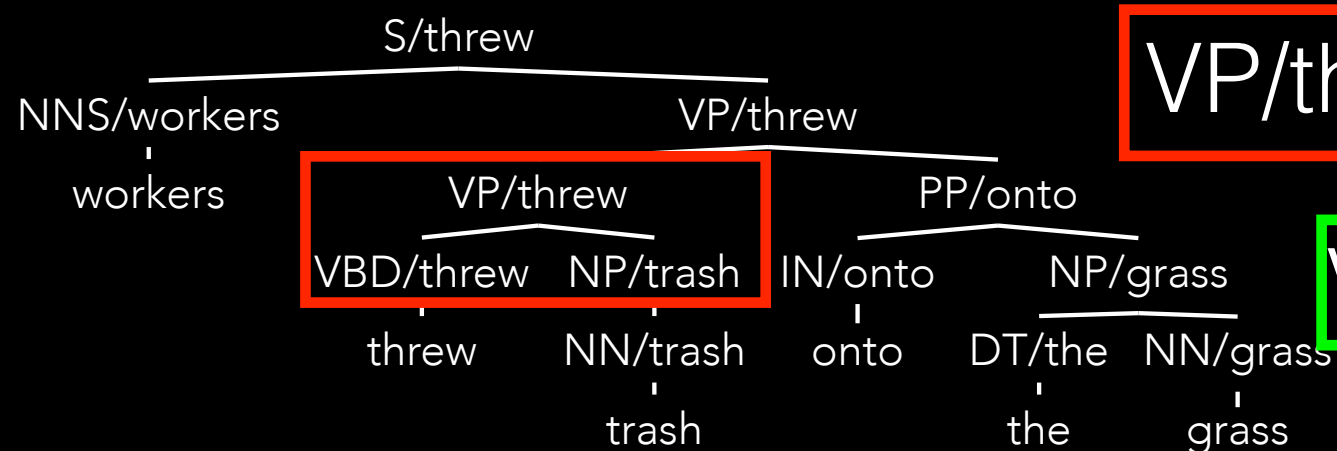
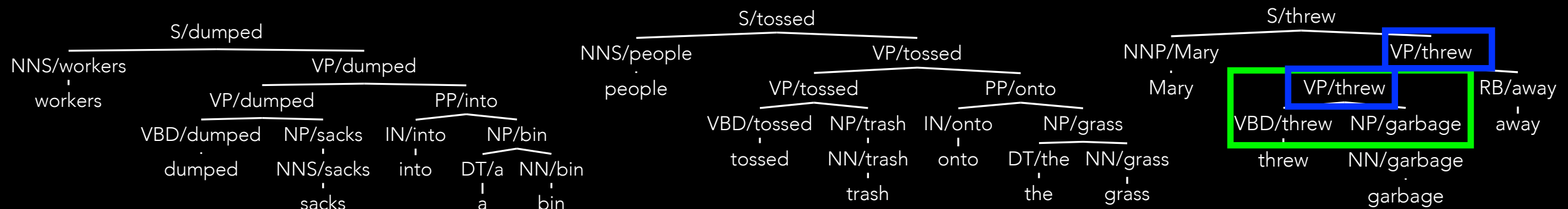
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20/40

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP/threw -> VBD/threw NP

VP/threw -> ...

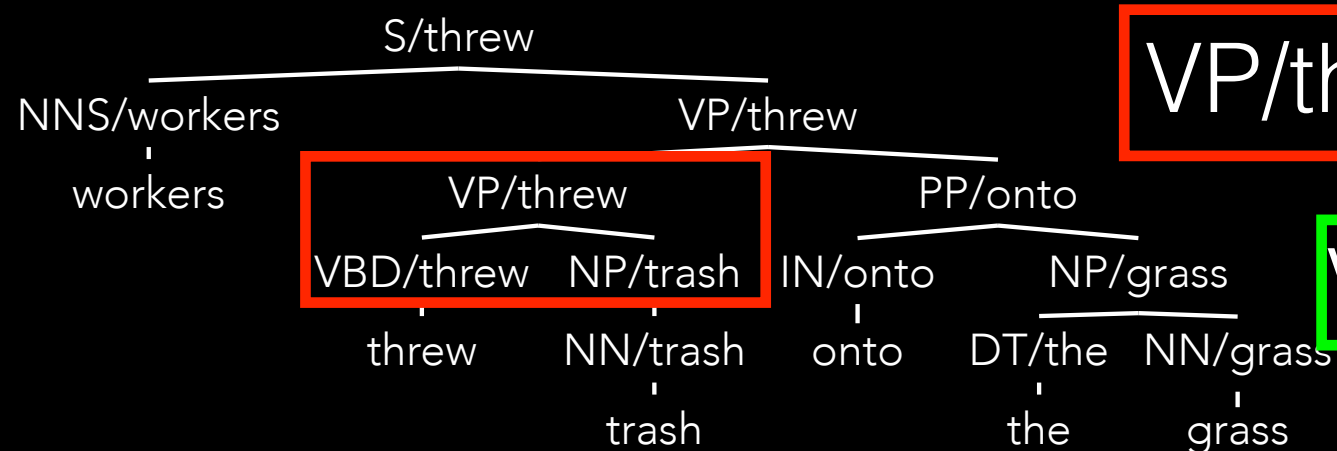
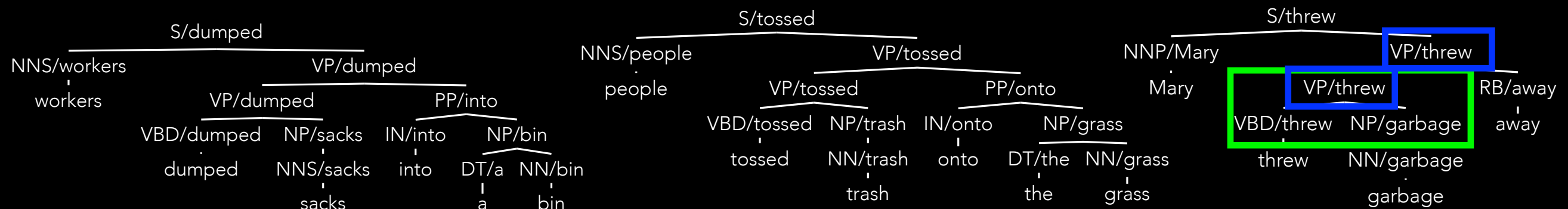
$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

20/40

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP/threw -> VBD/threw NP

VP/threw -> ...

$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

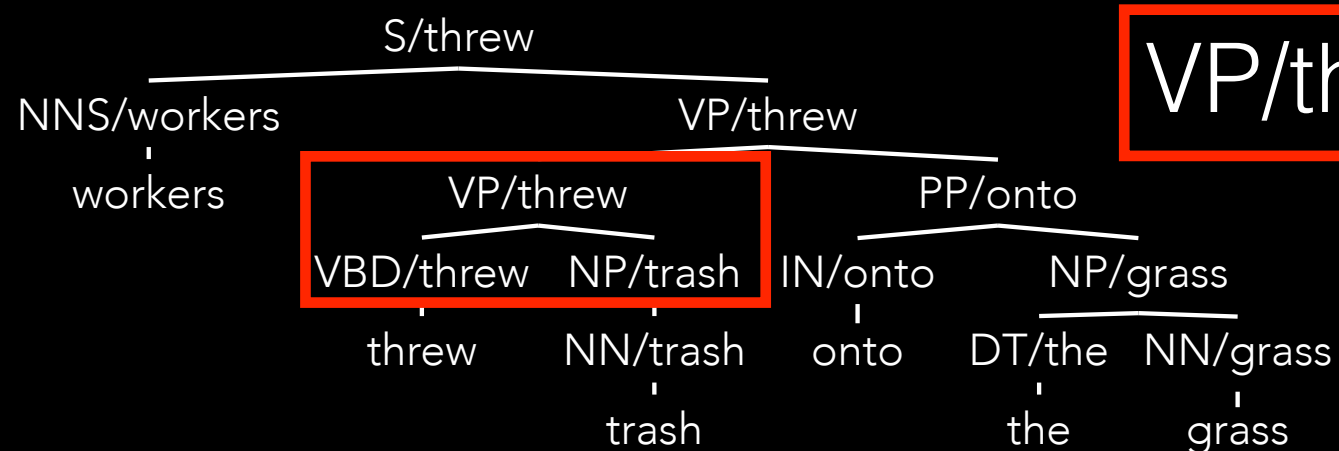
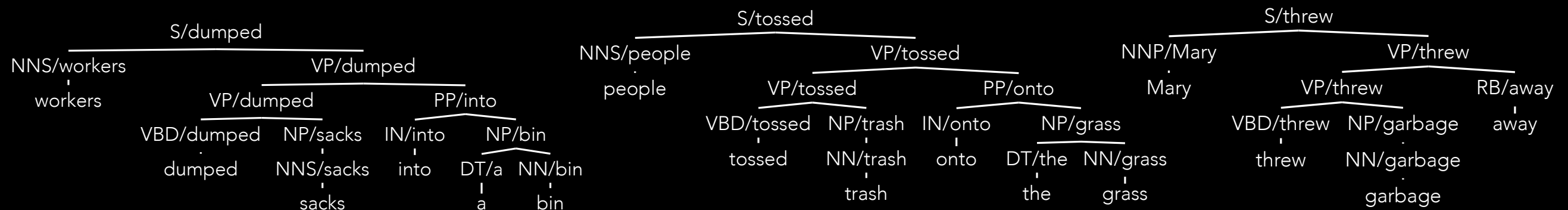
20/40



# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



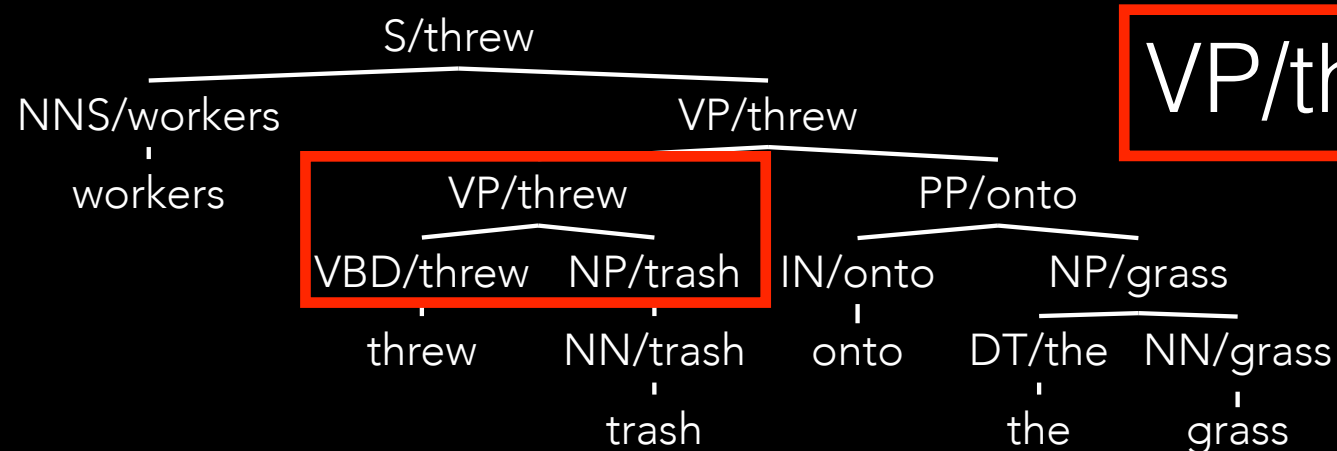
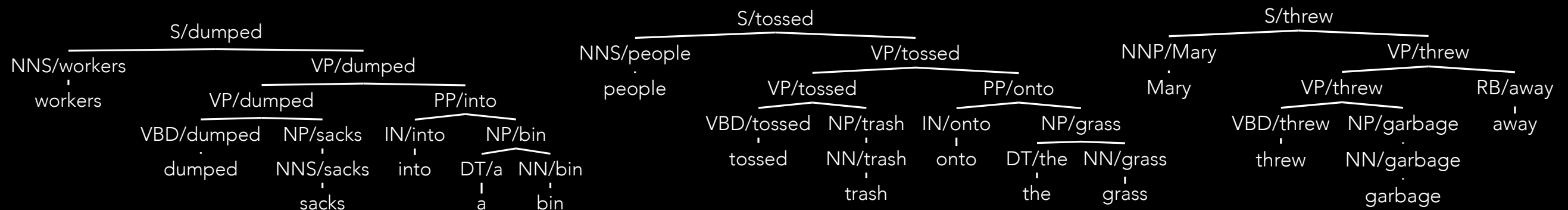
VP/threw -> VBD/threw NP/trash

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

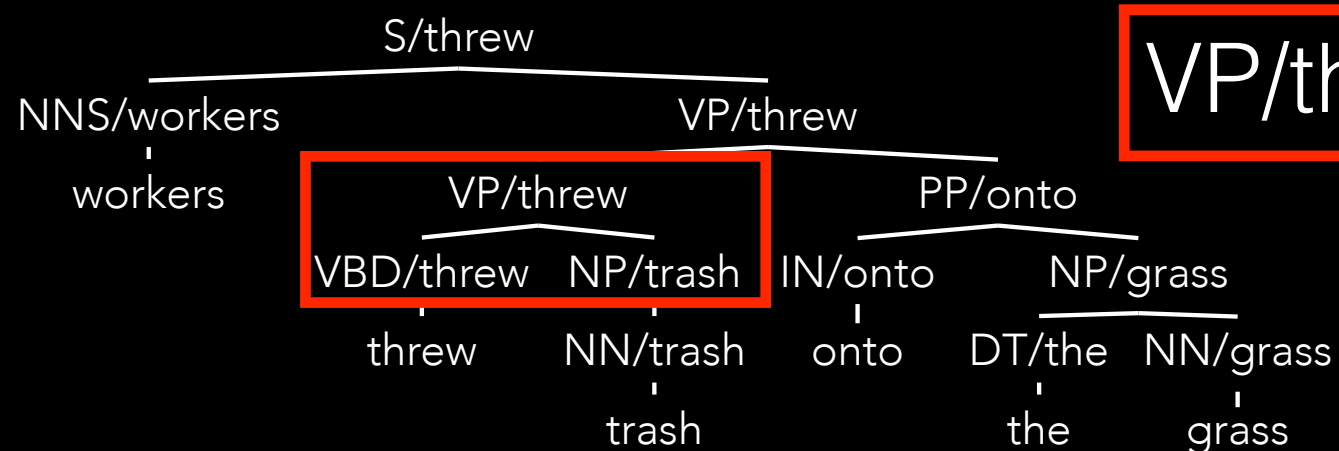
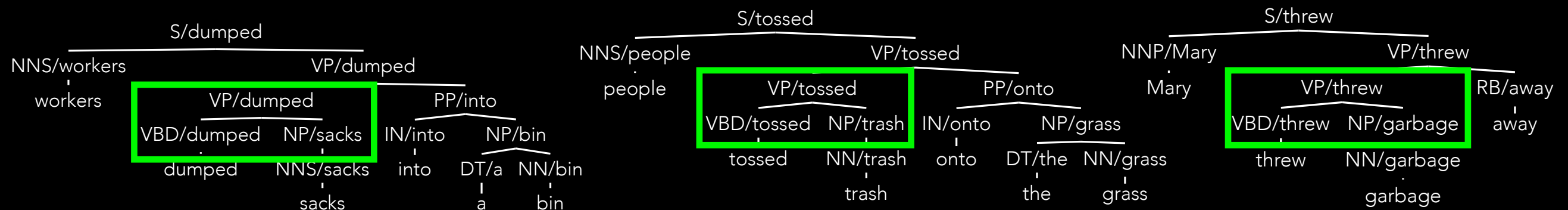
VP -> VBD NP

$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

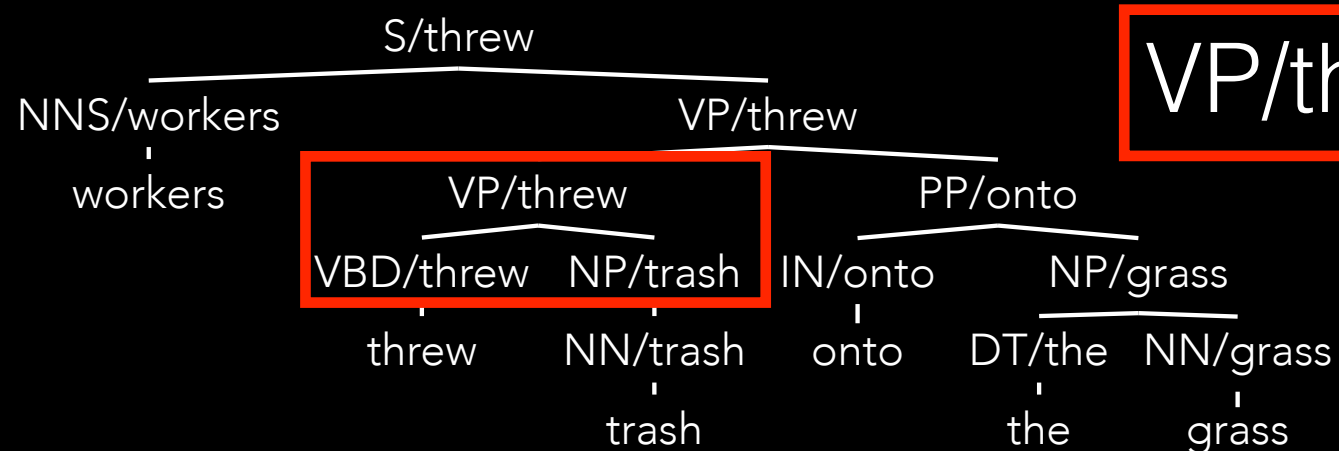
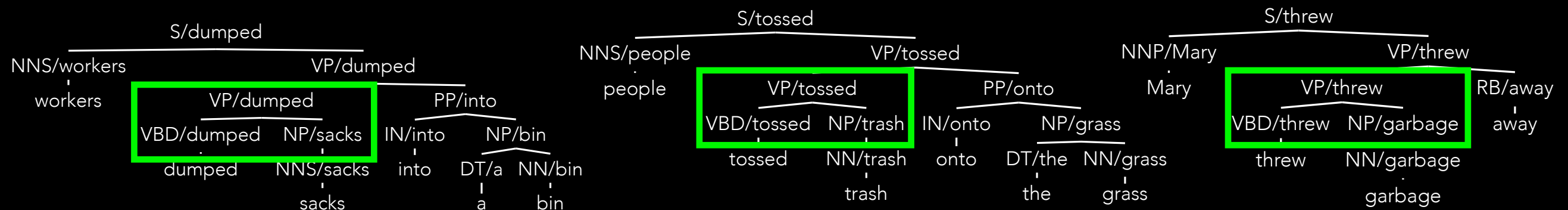
VP -> VBD NP

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP

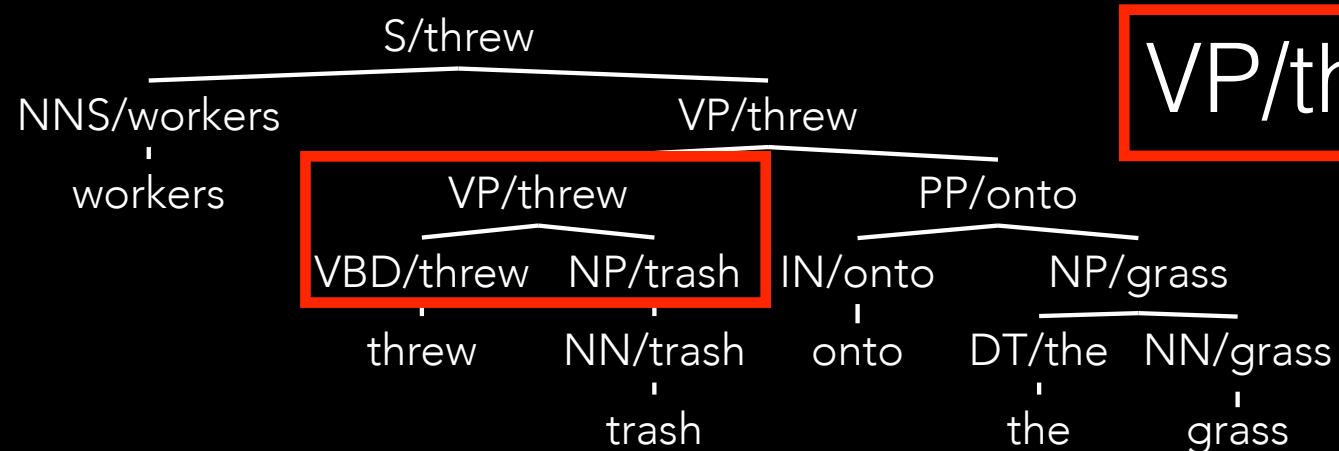
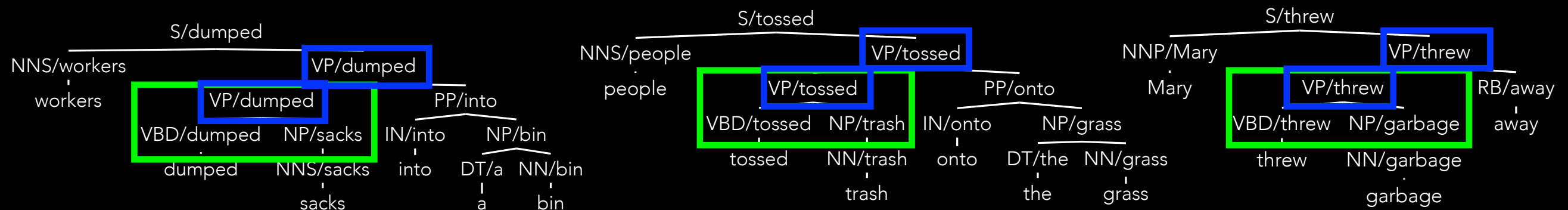
VP -> ...

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP

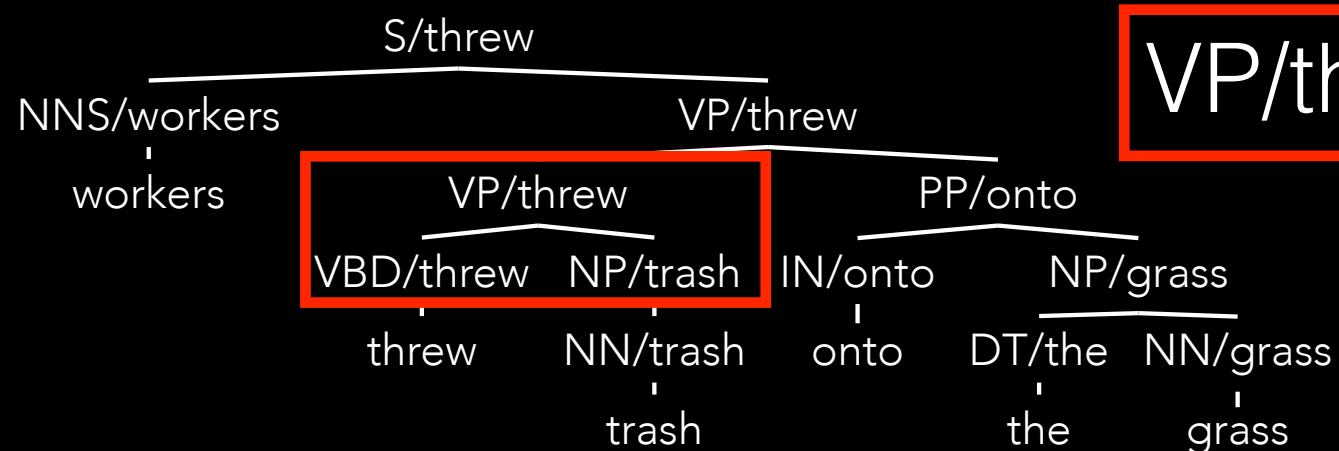
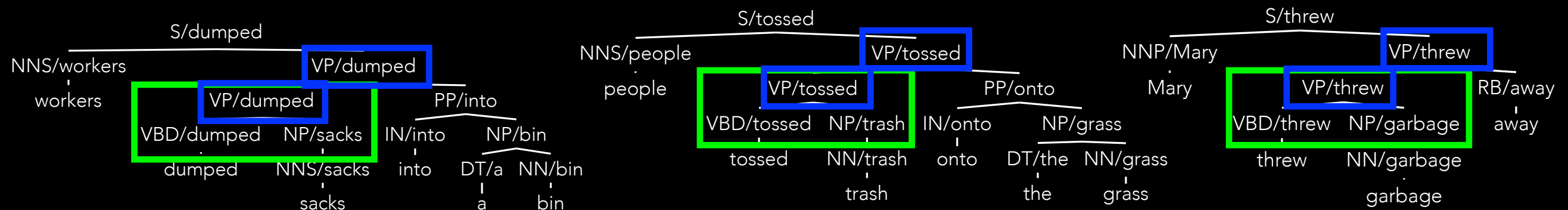
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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP

VP -> ...

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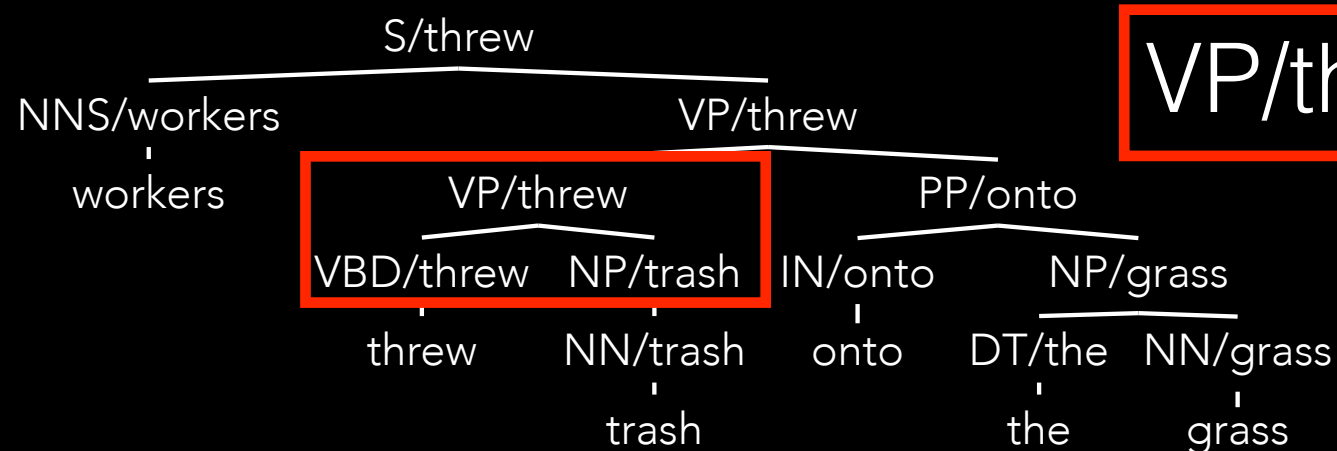
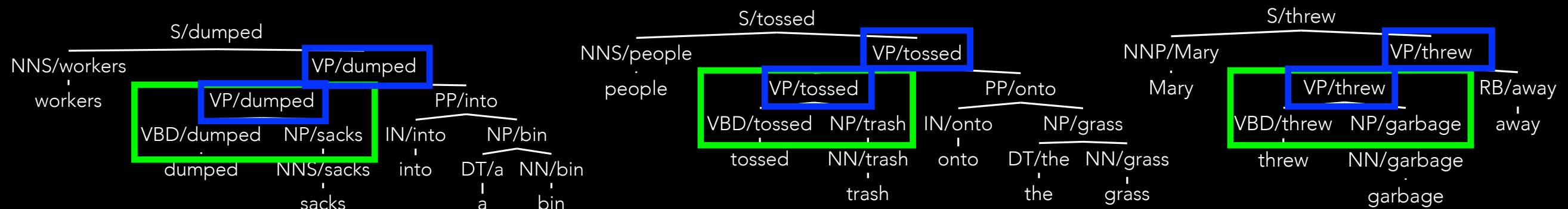
20/40

60/120

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP

VP -> ...

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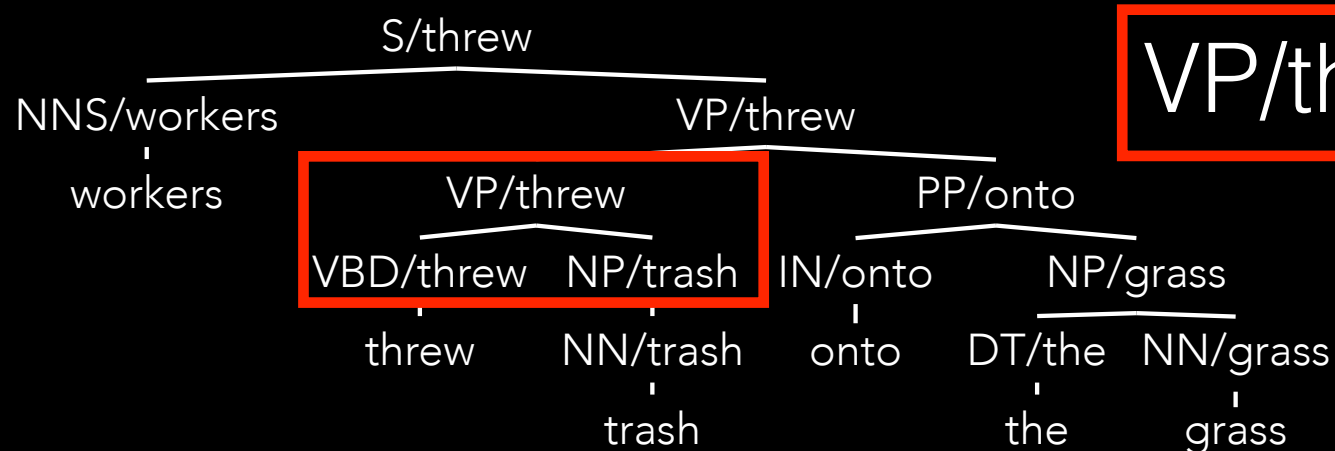
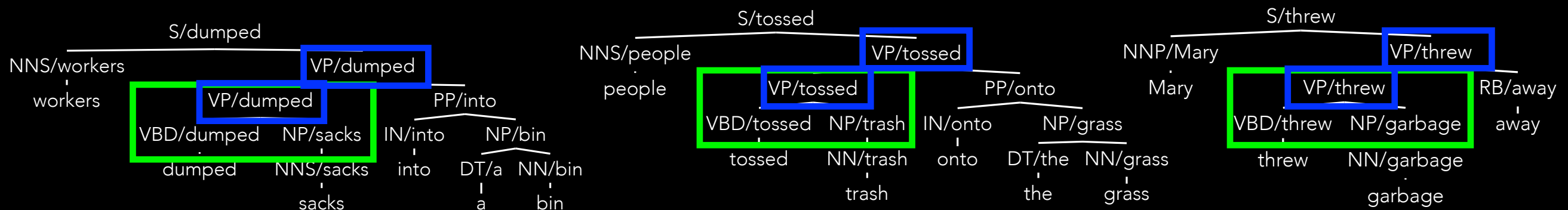
20/40

60/120

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP

VP -> ...

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20/40

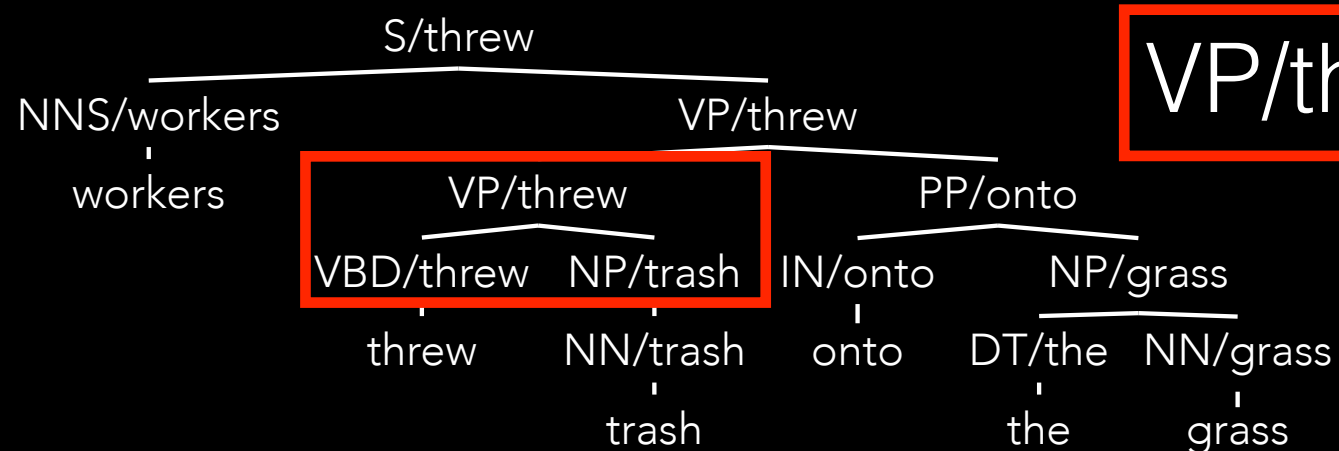
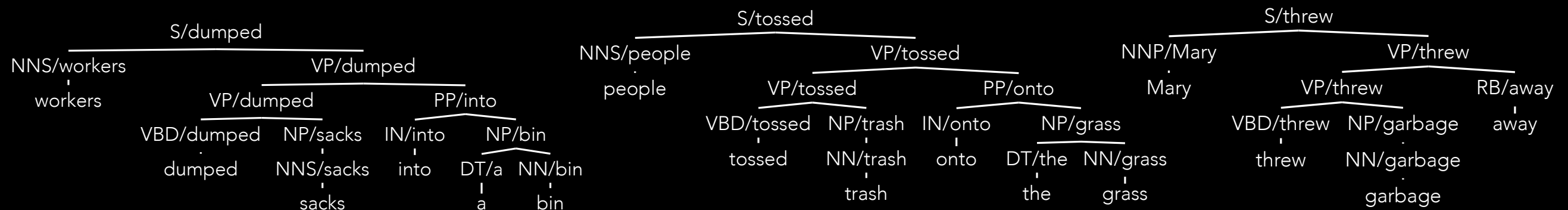
60/120



# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



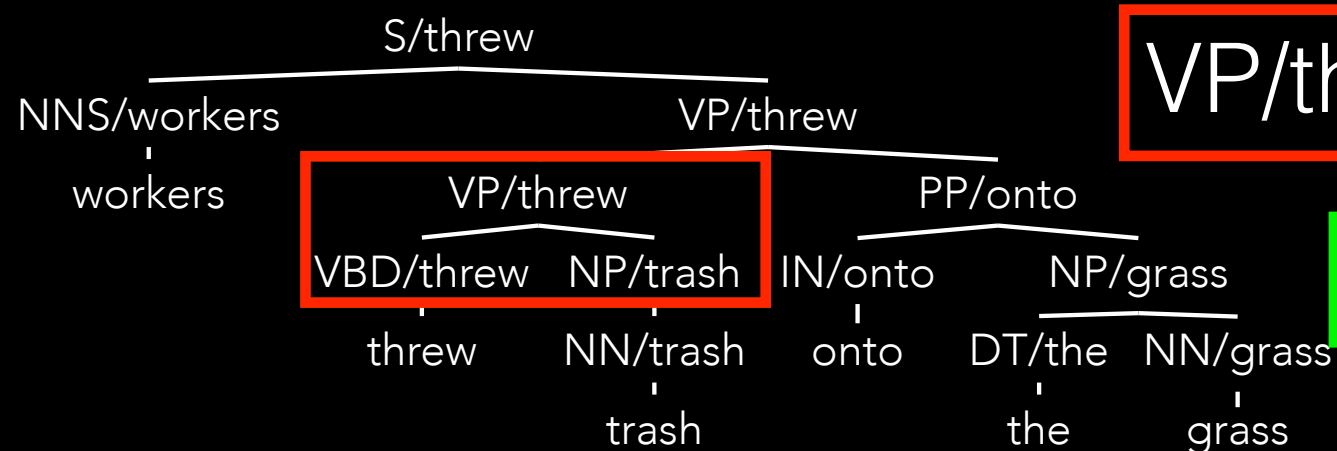
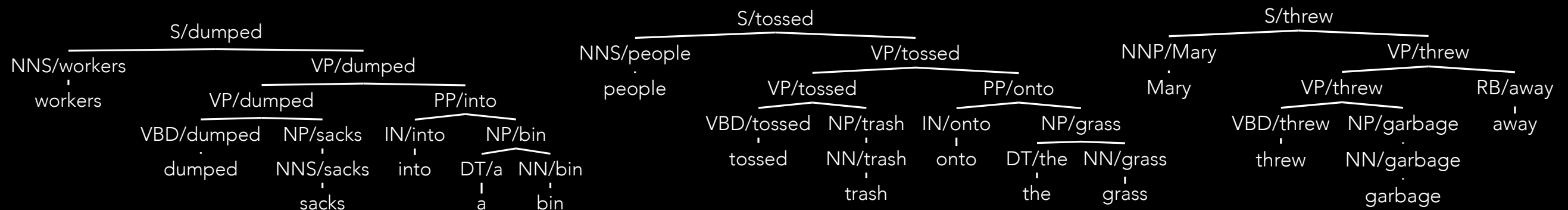
VP/threw -> VBD/threw NP/trash

$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

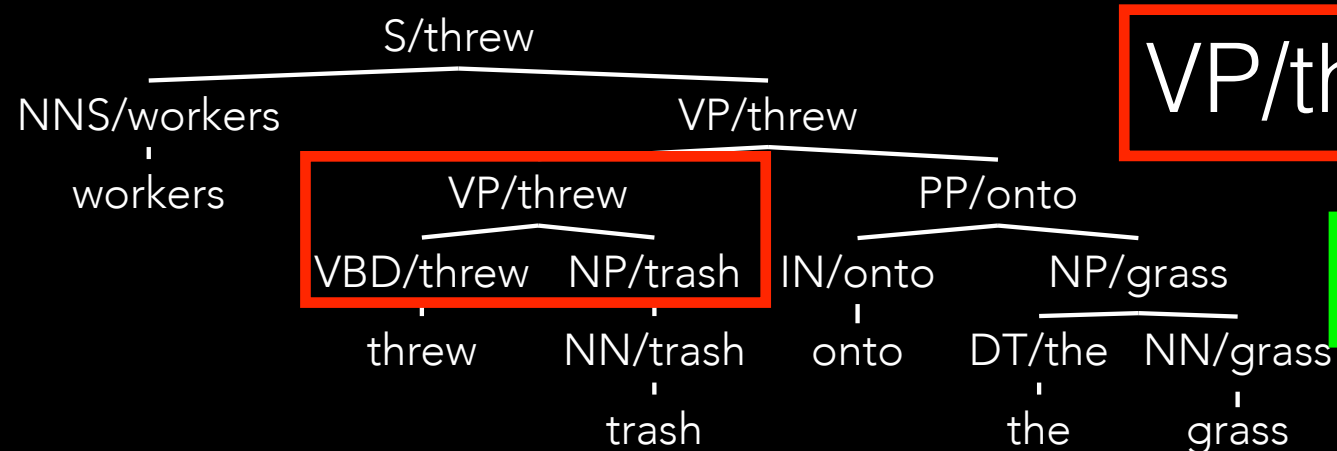
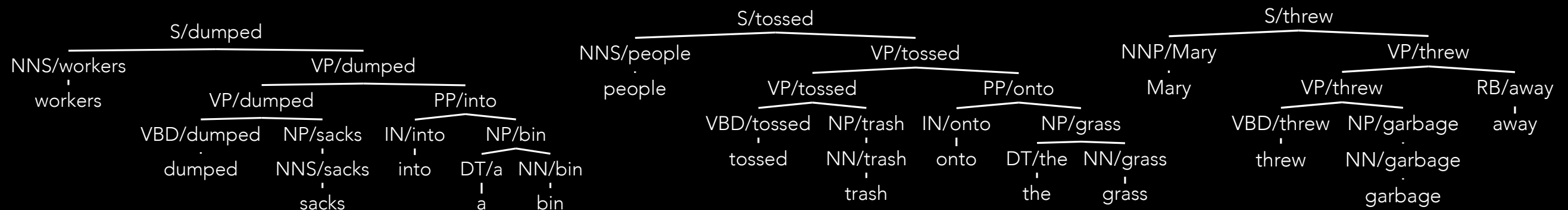
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By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



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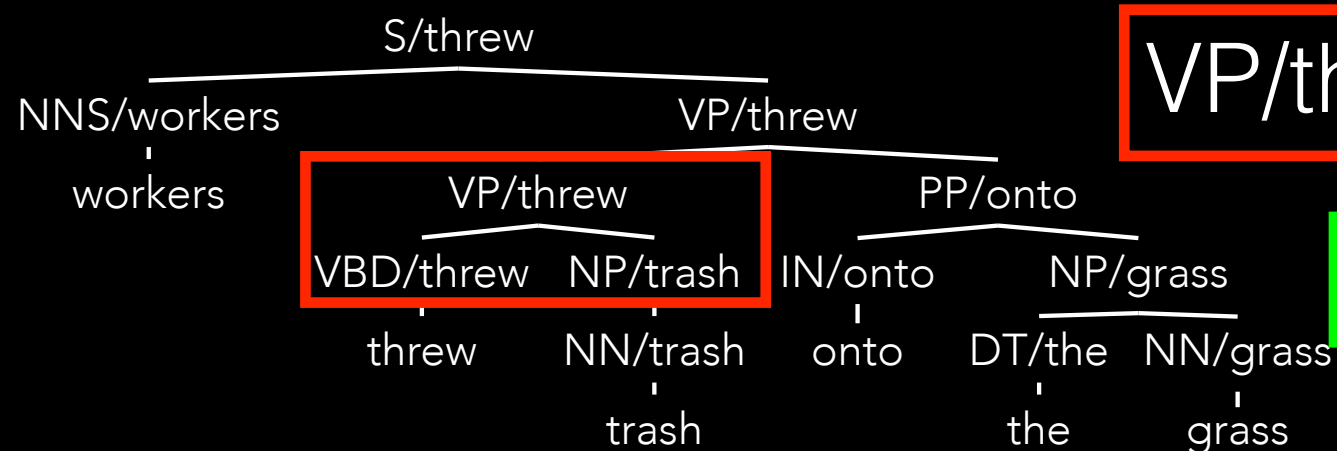
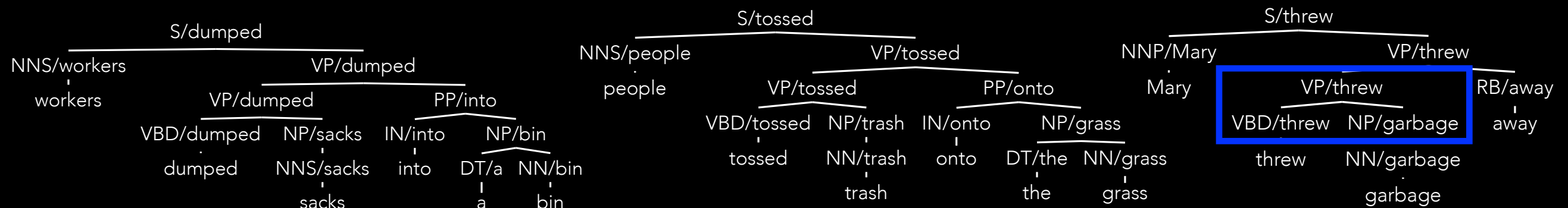
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By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



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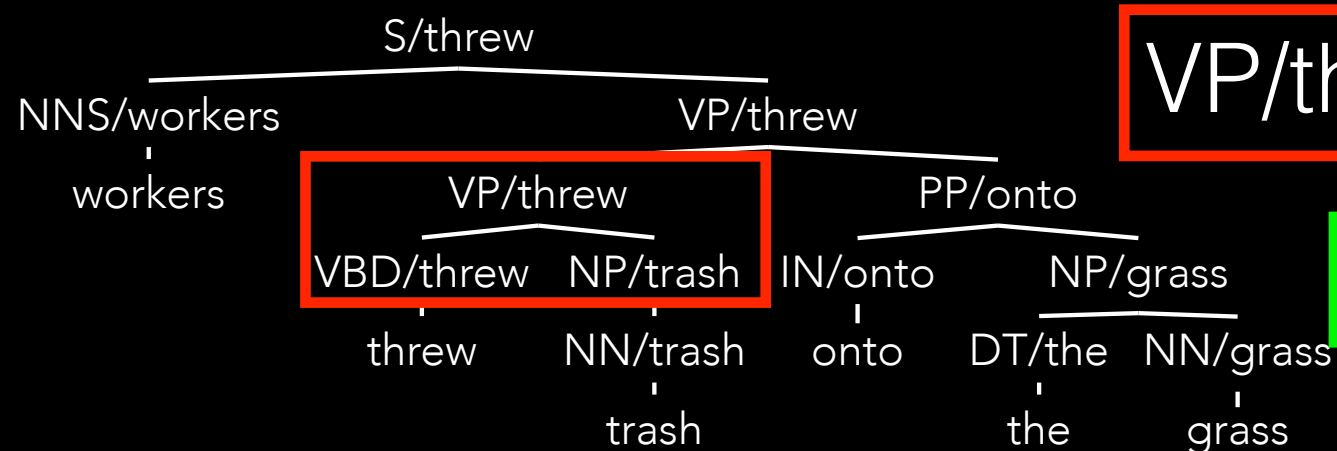
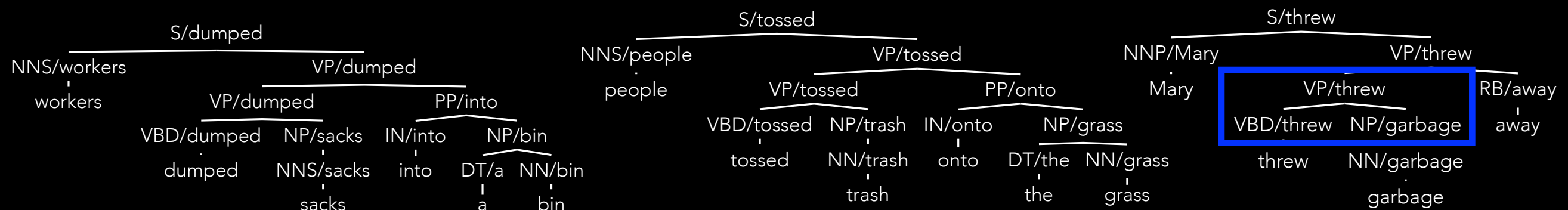
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By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



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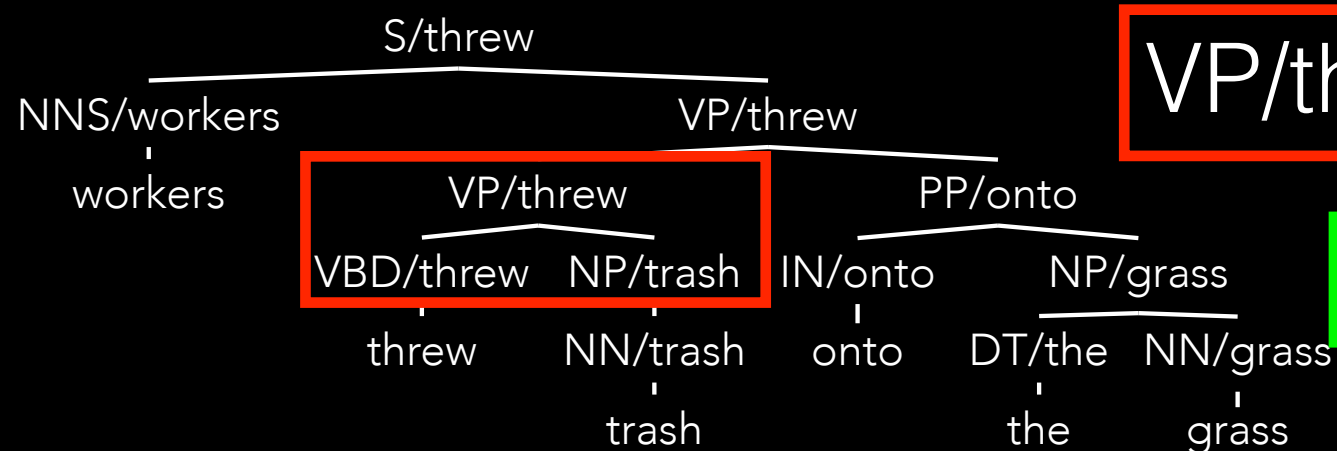
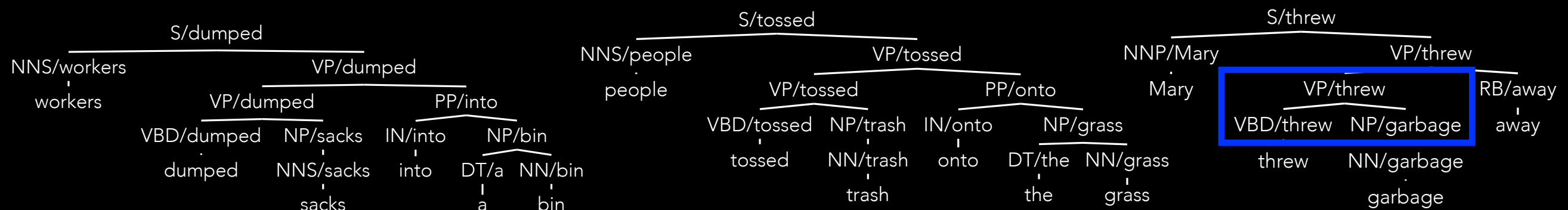
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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

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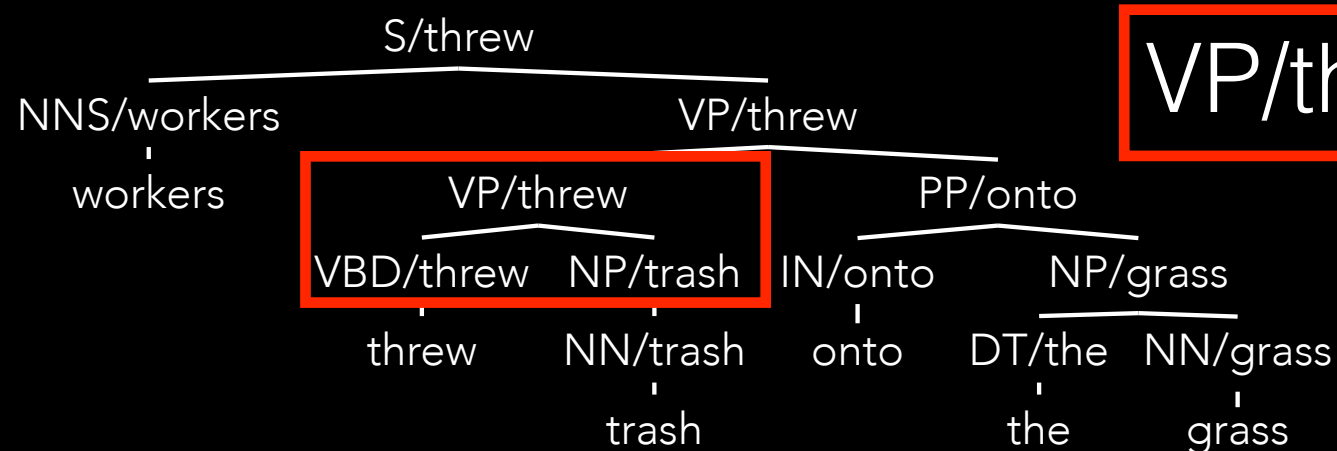
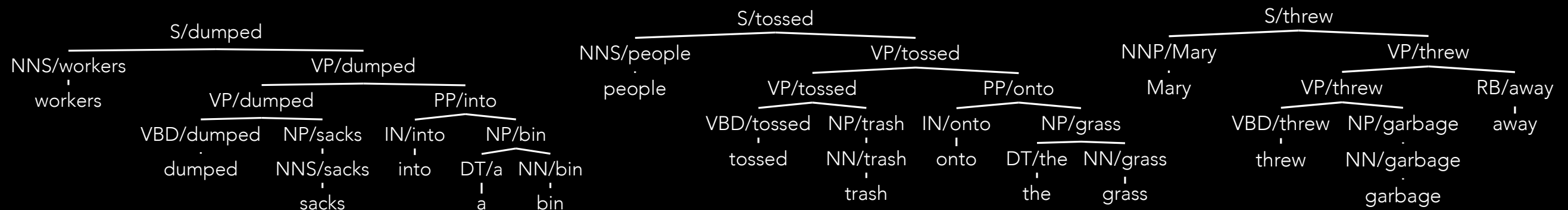
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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



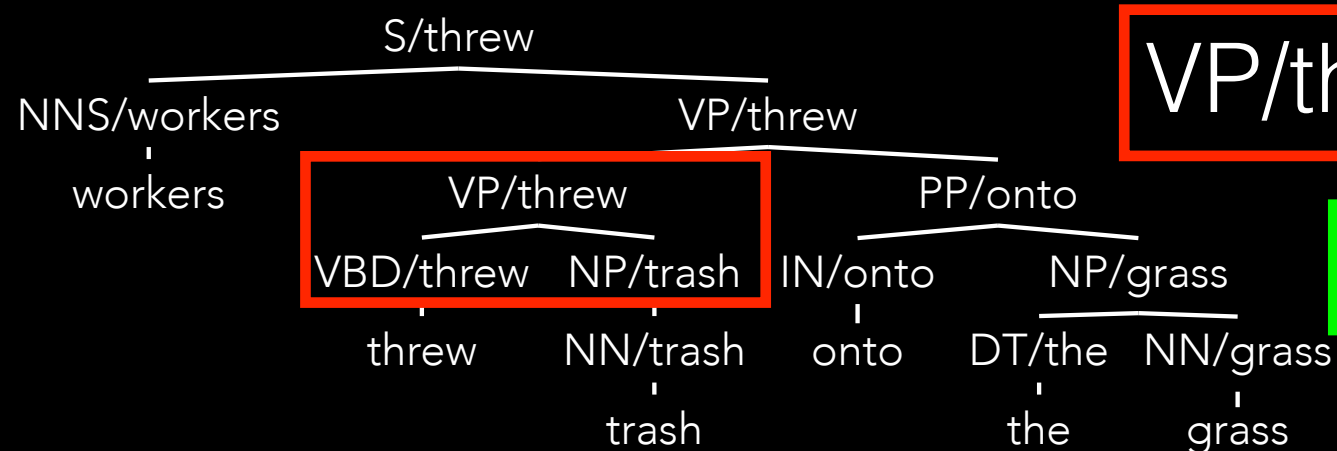
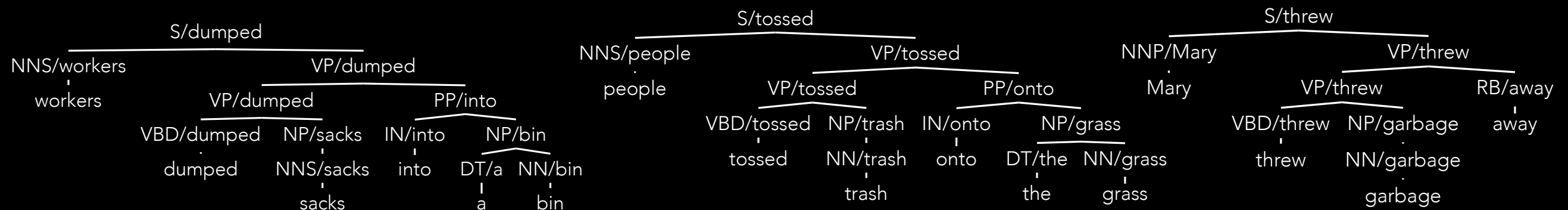
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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP/trash

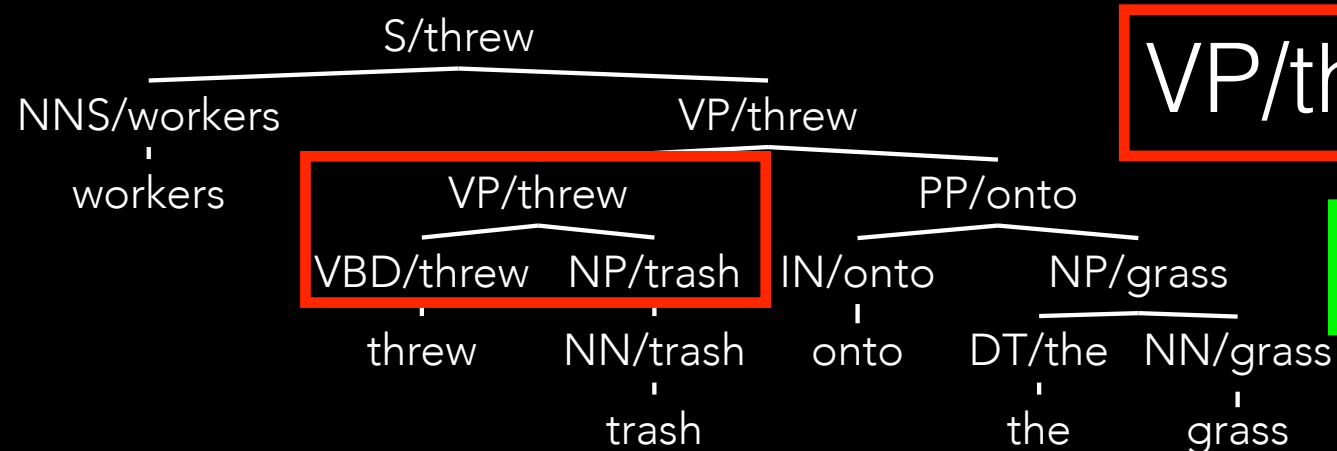
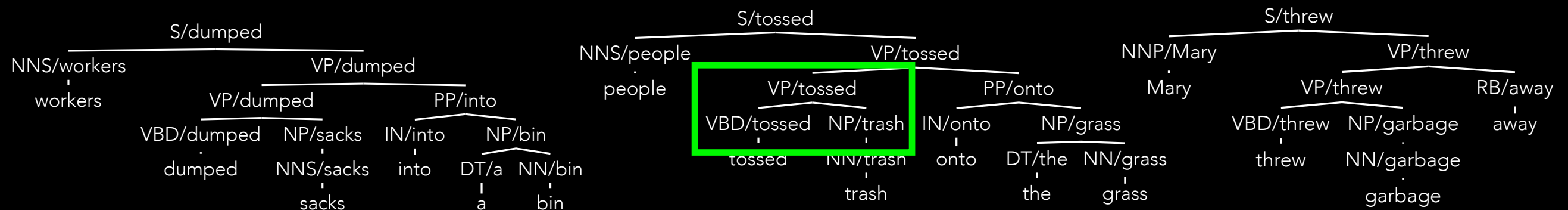
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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



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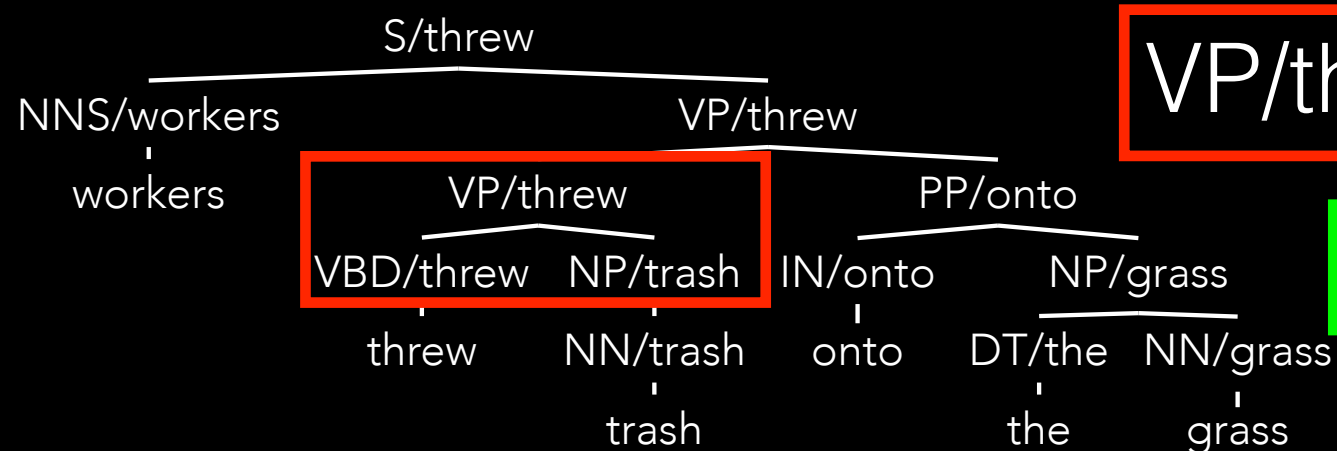
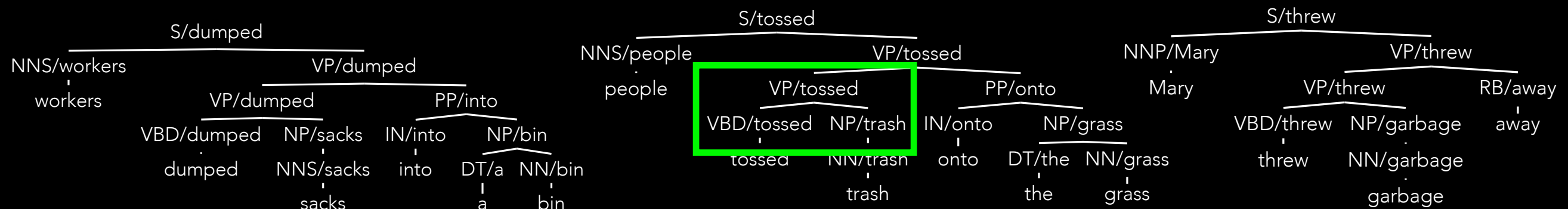
VP -> VBD NP/trash

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

VP → VBD NP/trash

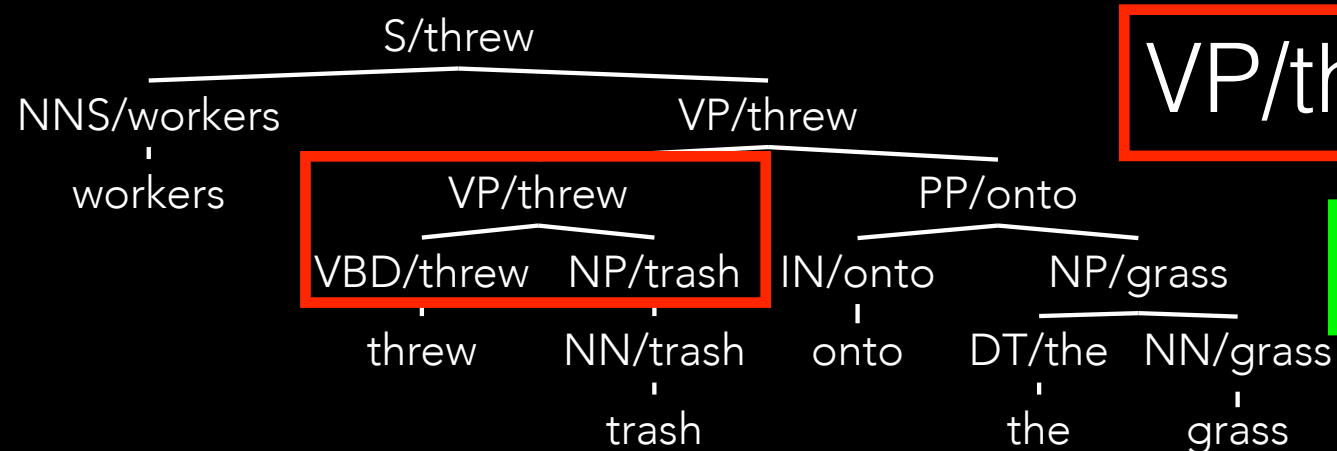
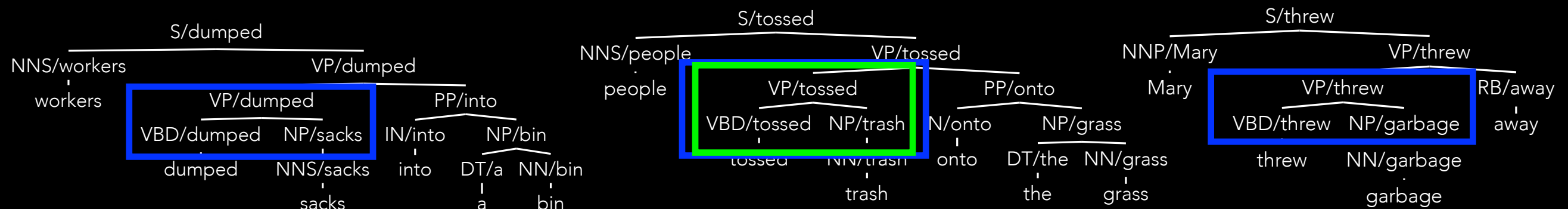
VP → VBD NP

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# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP/trash

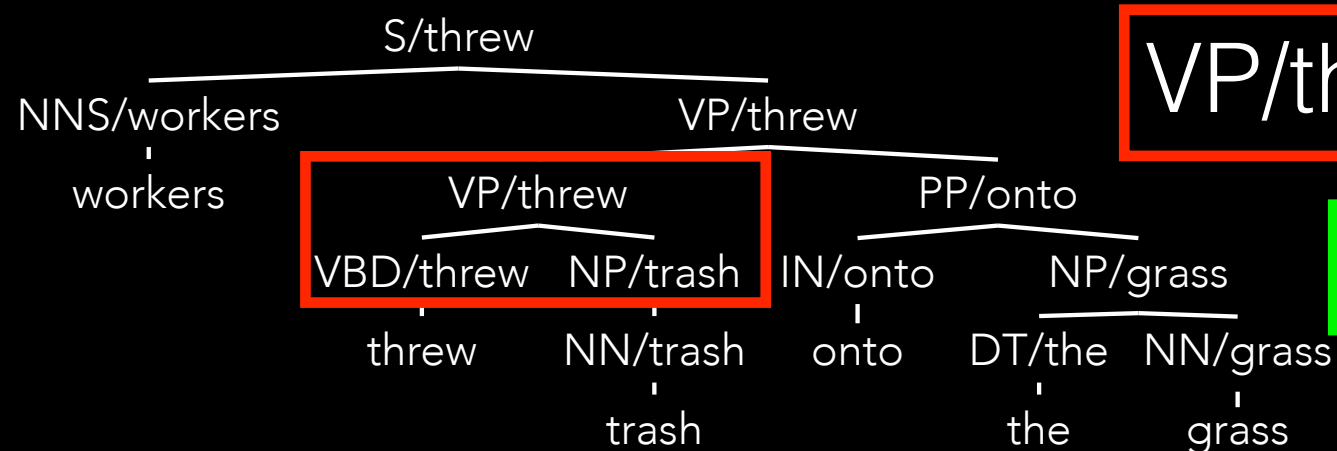
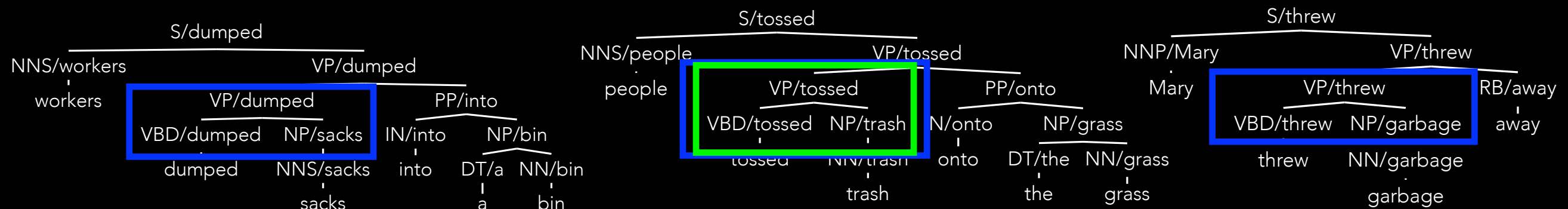
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By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



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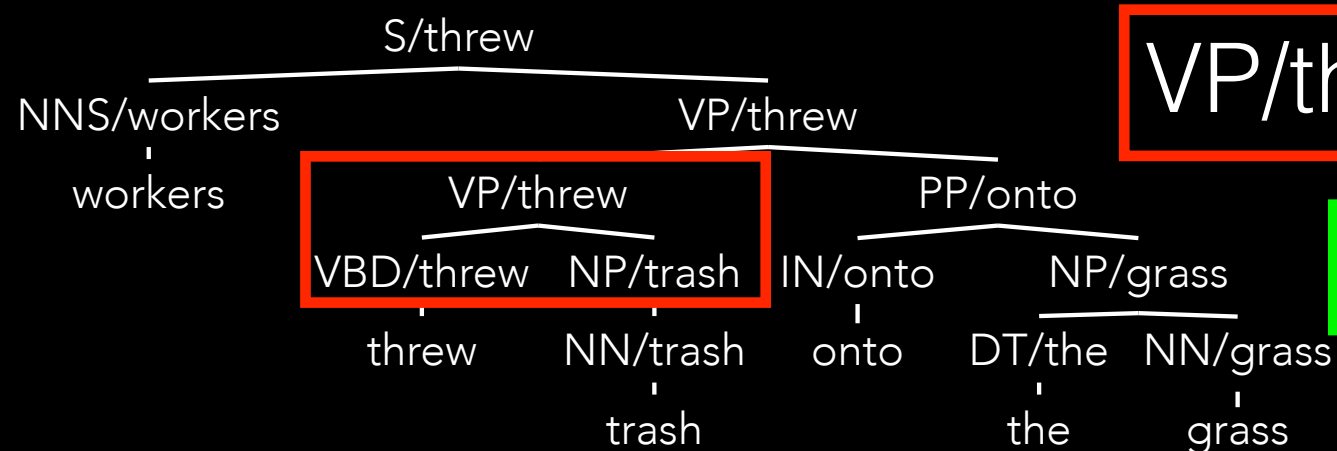
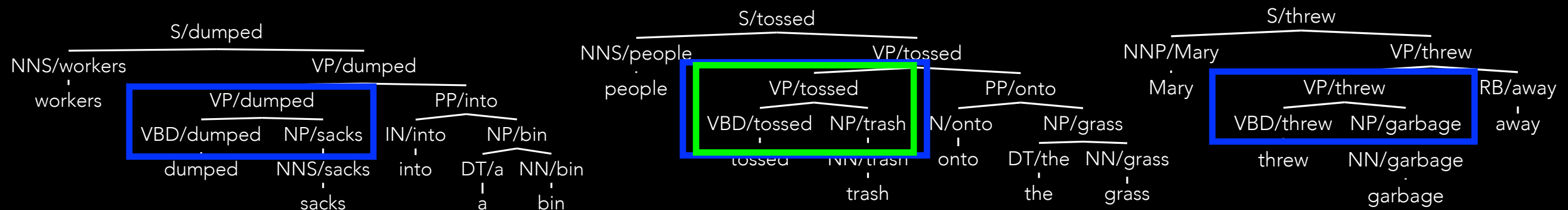
0/20

20/60

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP/trash

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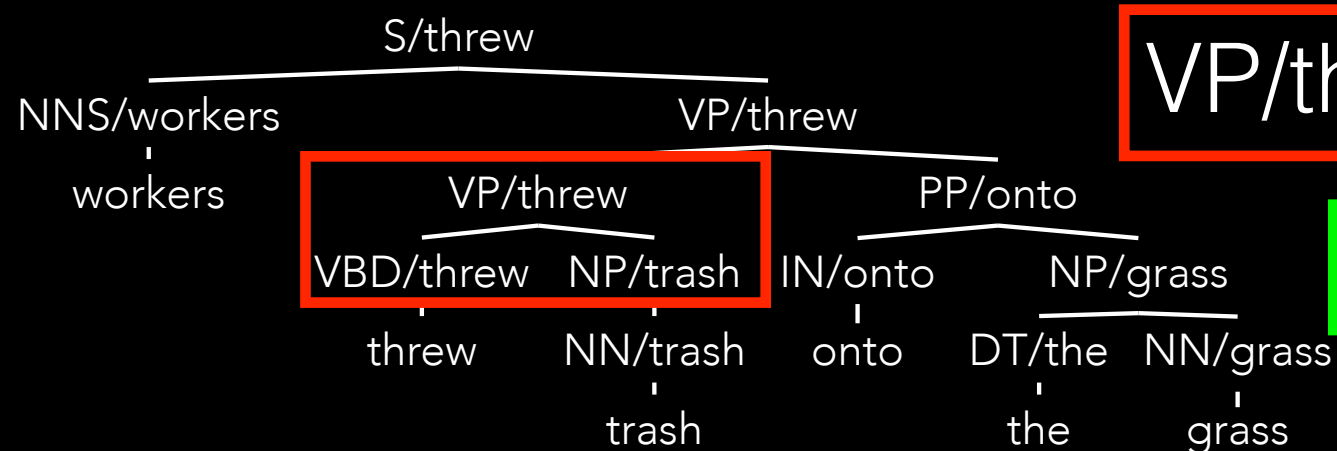
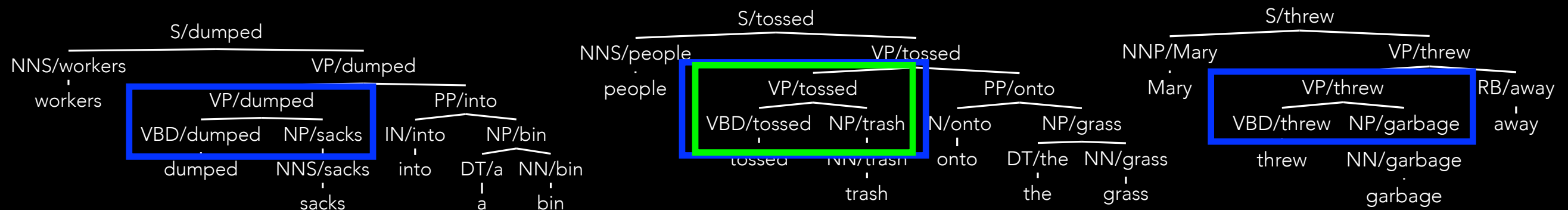
0/20

20/60

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

VP -> VBD NP/trash

VP -> VBD NP

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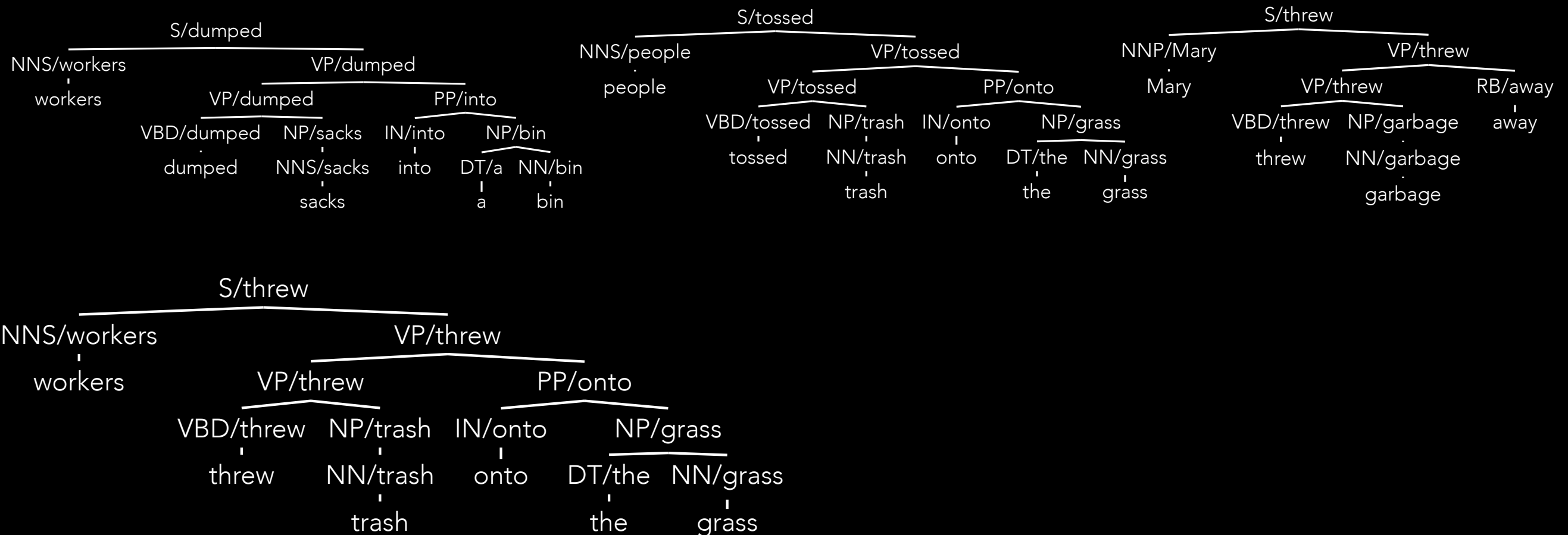
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20/60

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

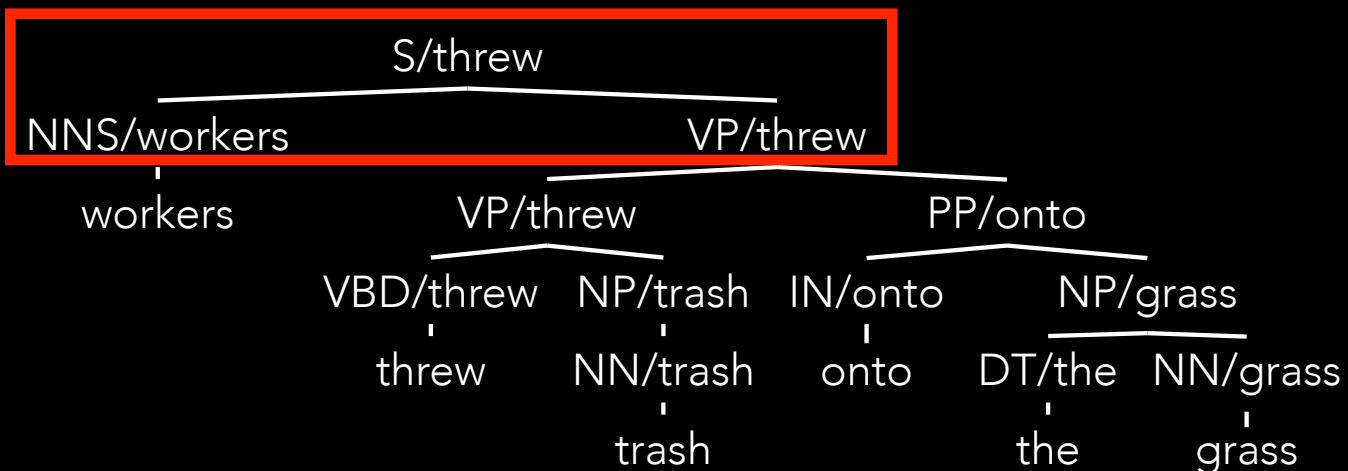
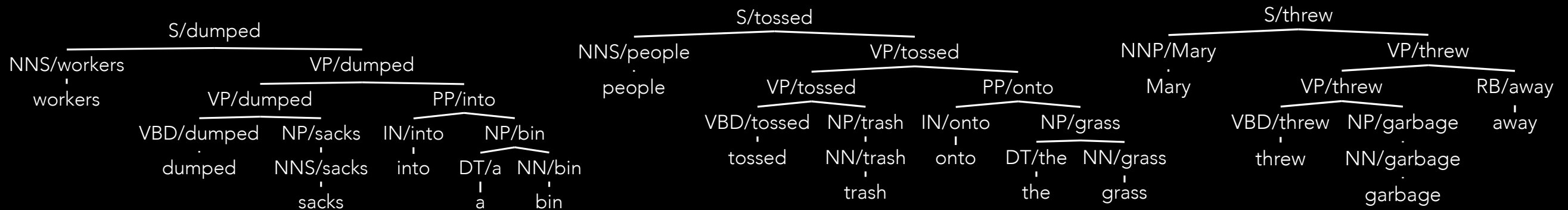
Assume we saw each training tree 20 times



# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times

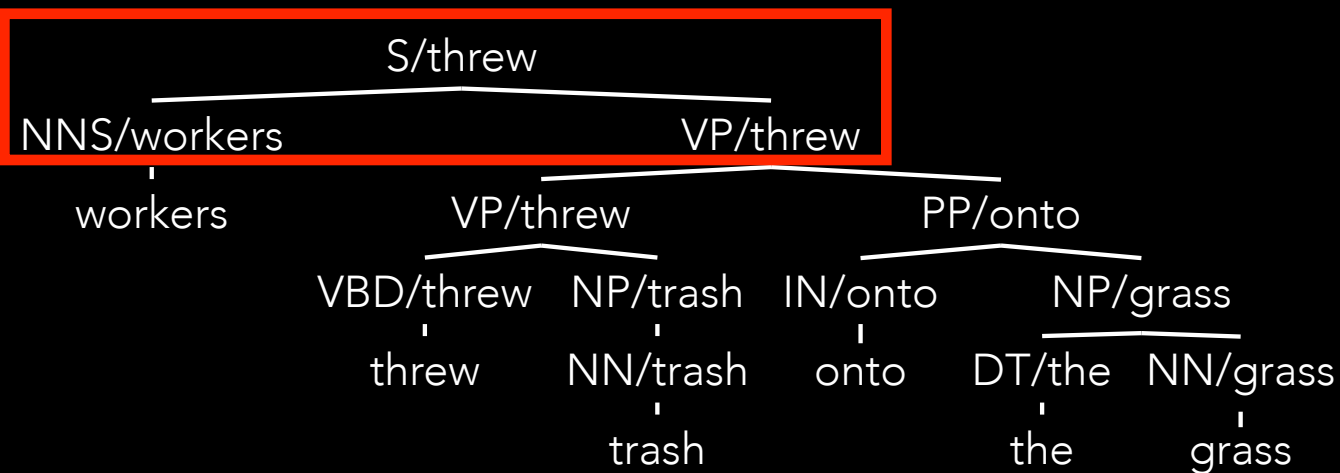
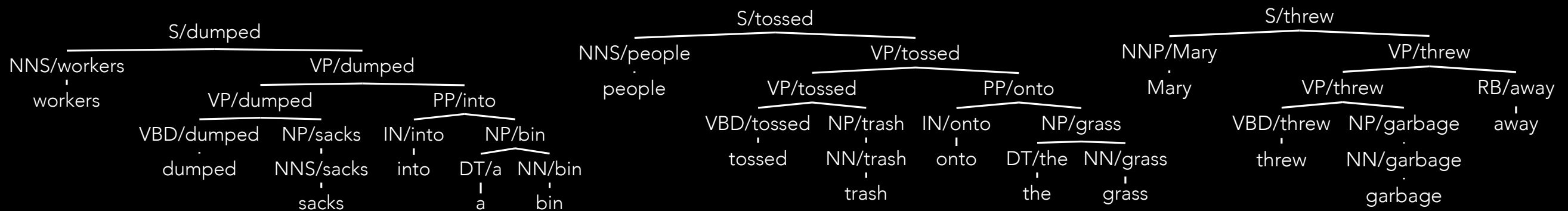




# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times

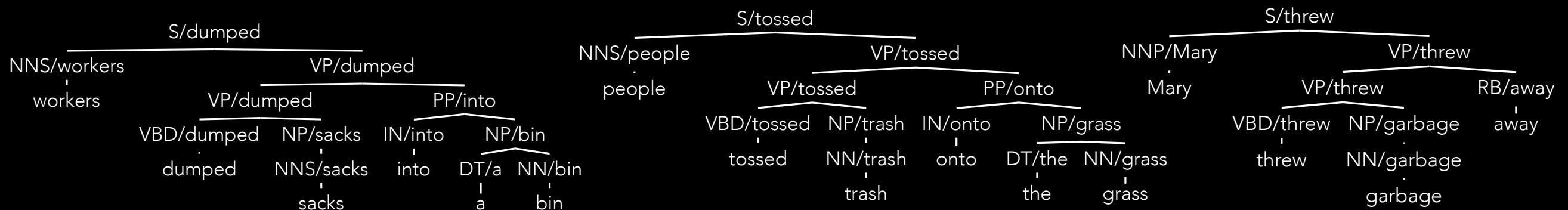


$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

Assume we saw each training tree 20 times



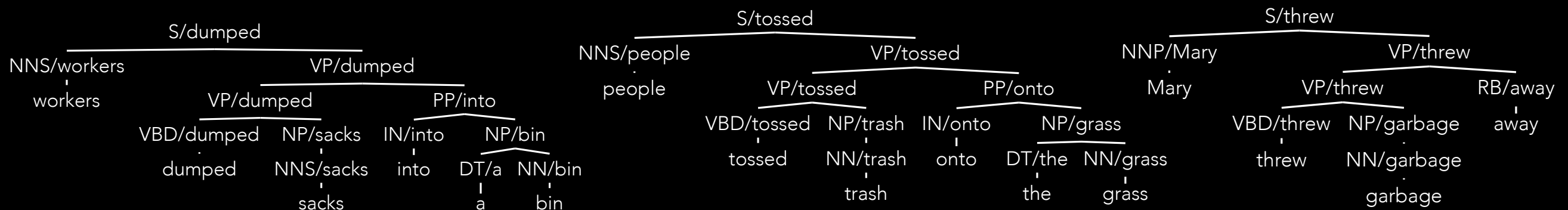
**S/threw -> NNS/workers VP/threw**

$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

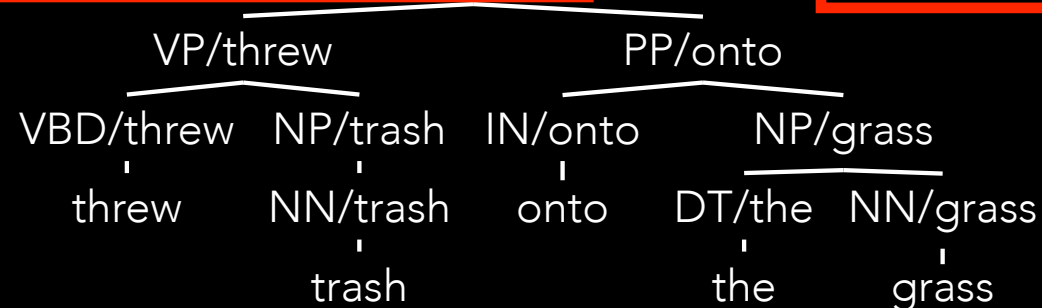
# Head lexicalization

By decomposing we can estimate unseen lexicalized rules

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**S/threw -> NNS/workers VP/threw**



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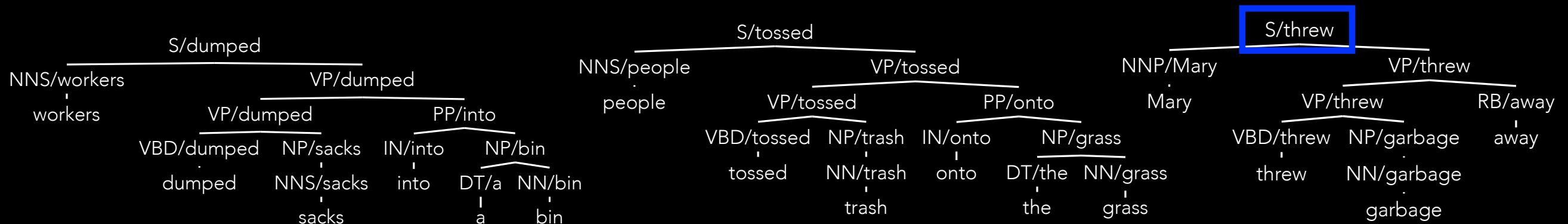
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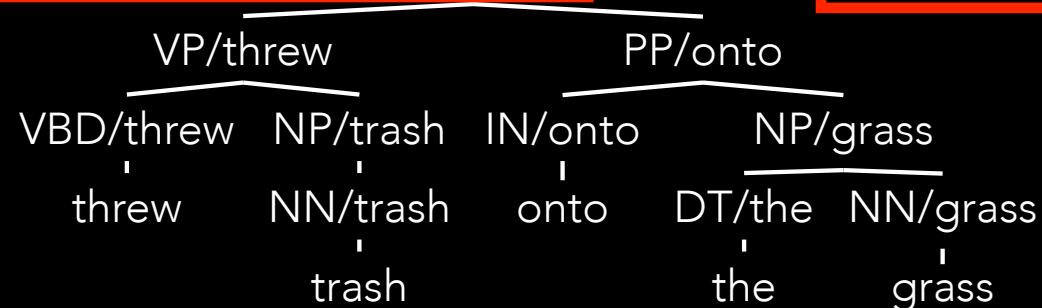
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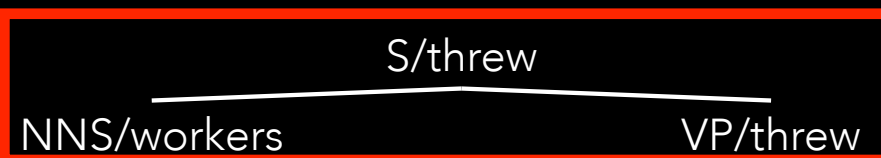
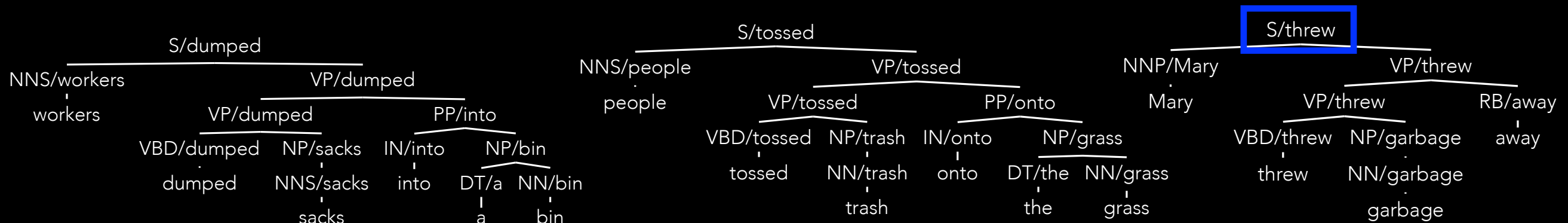
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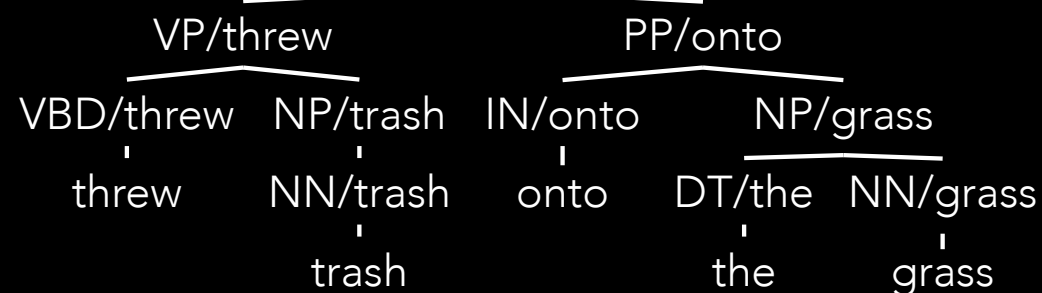
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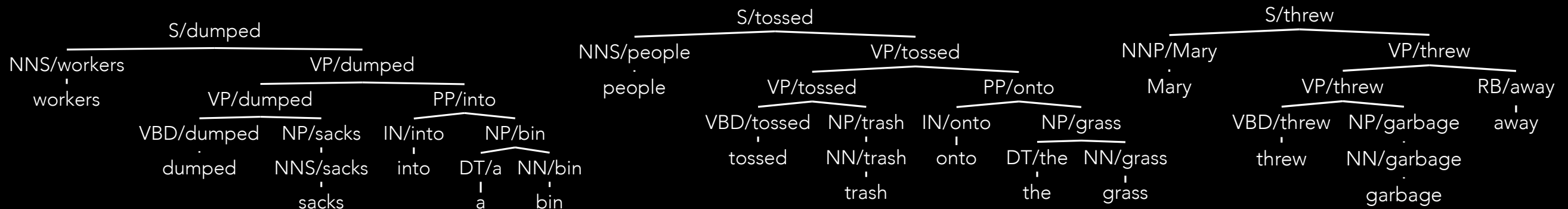
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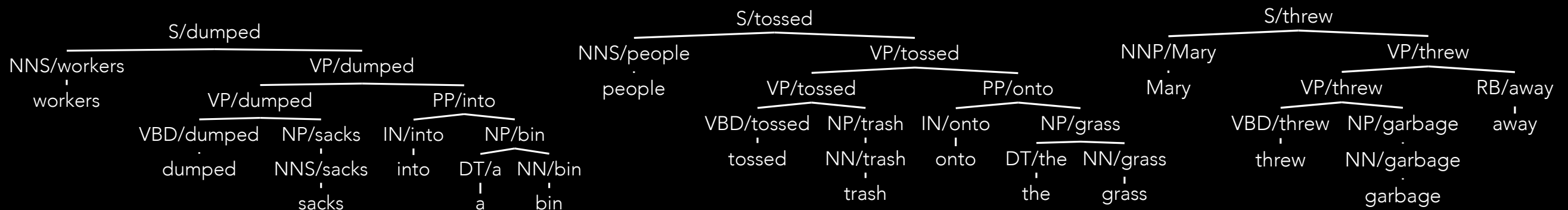
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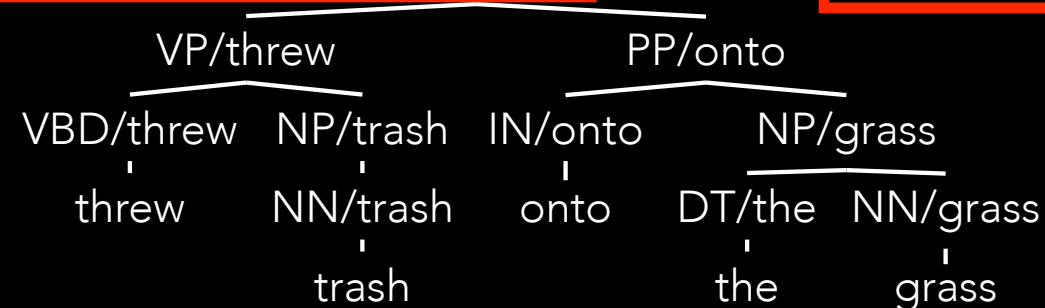
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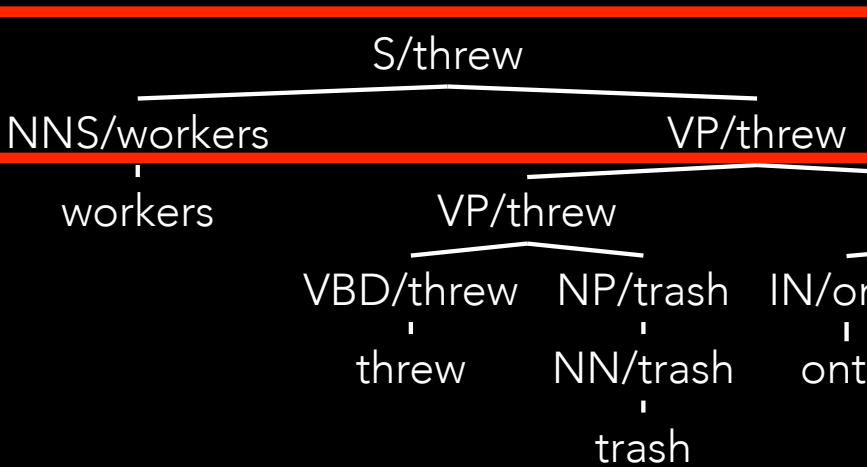
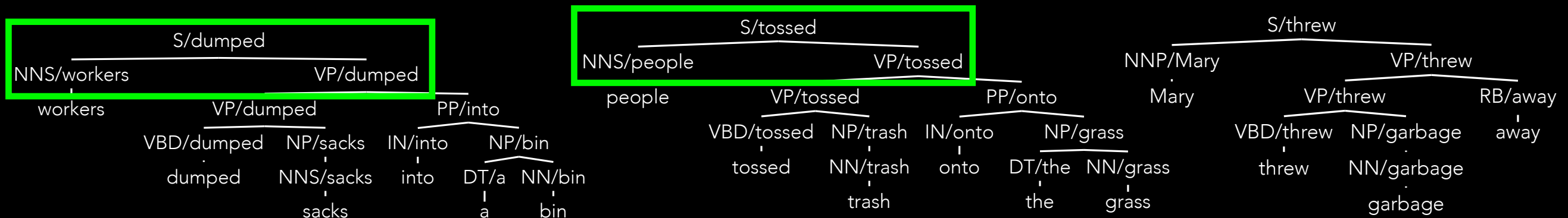
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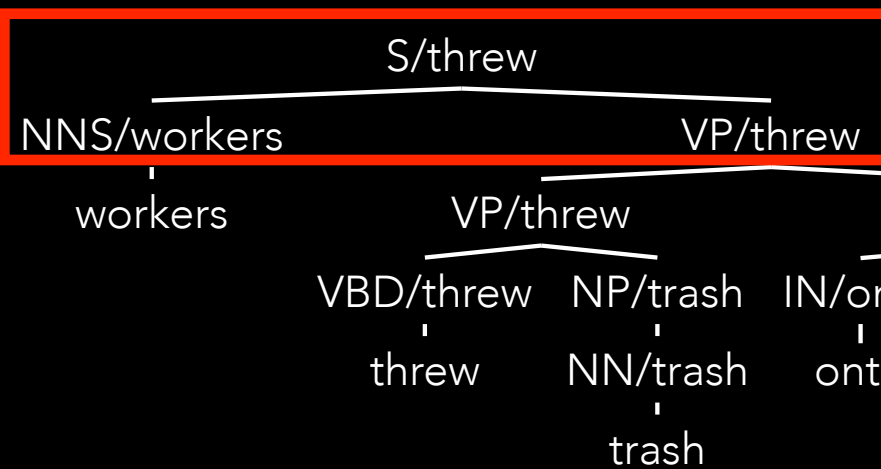
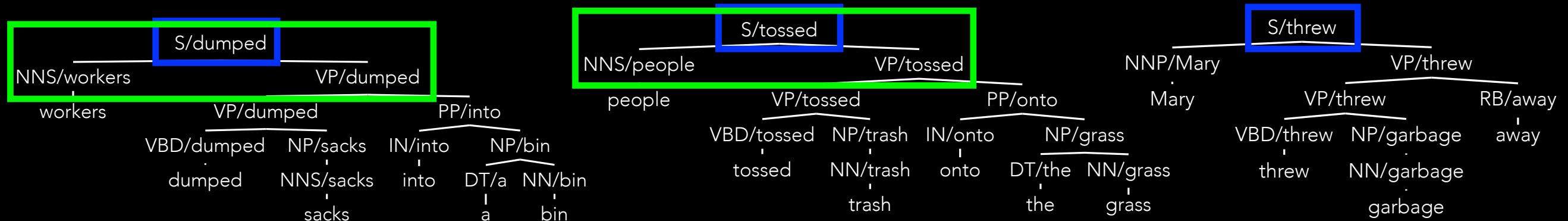
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$S/threw \rightarrow NNS/workers \ VP/threw$

$S \rightarrow NNS \ VP$

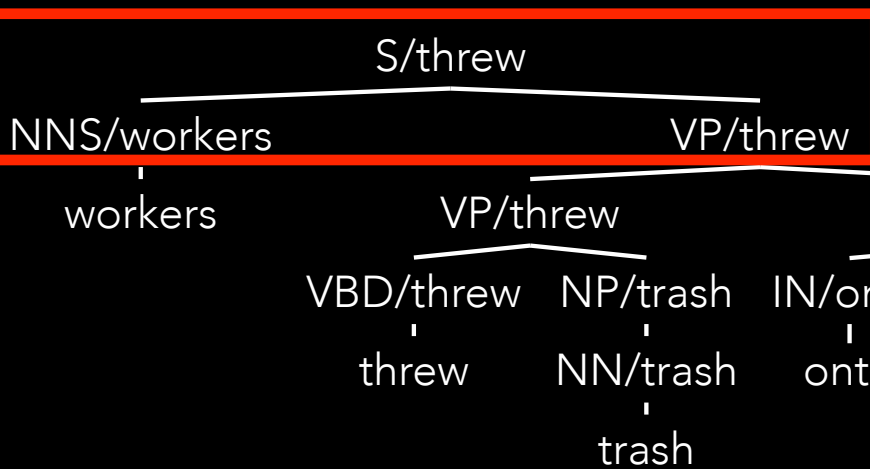
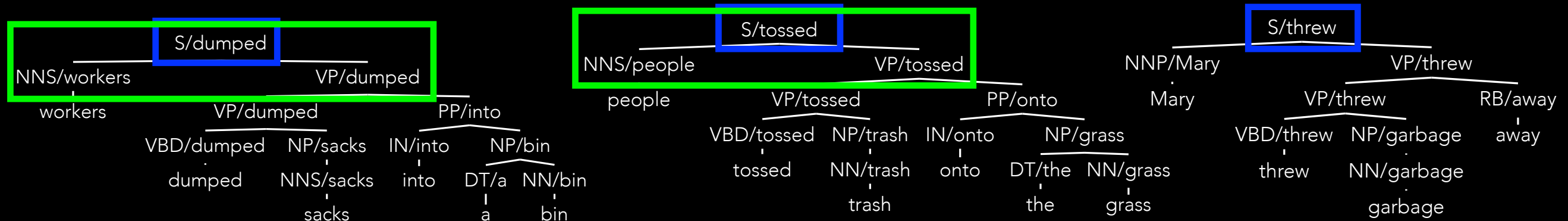
$S \rightarrow \dots$

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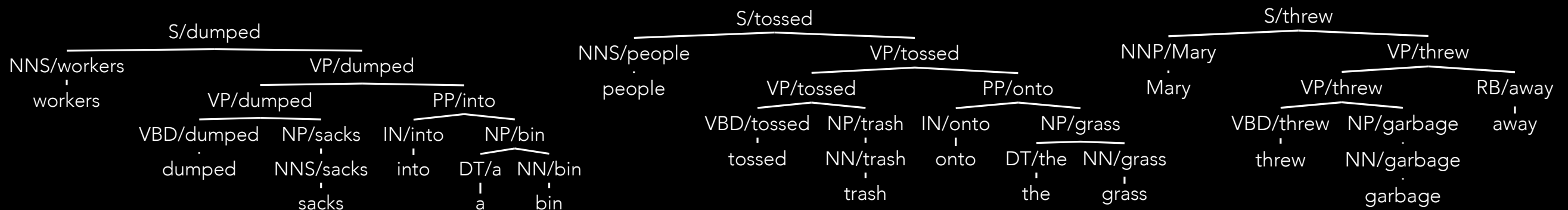
0/20

40/60

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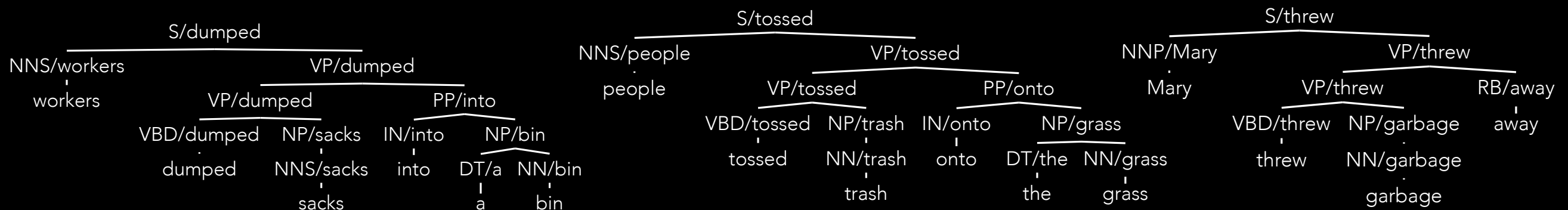
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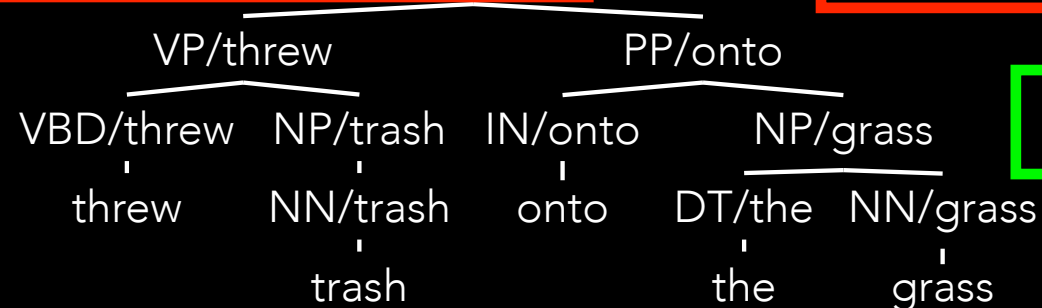
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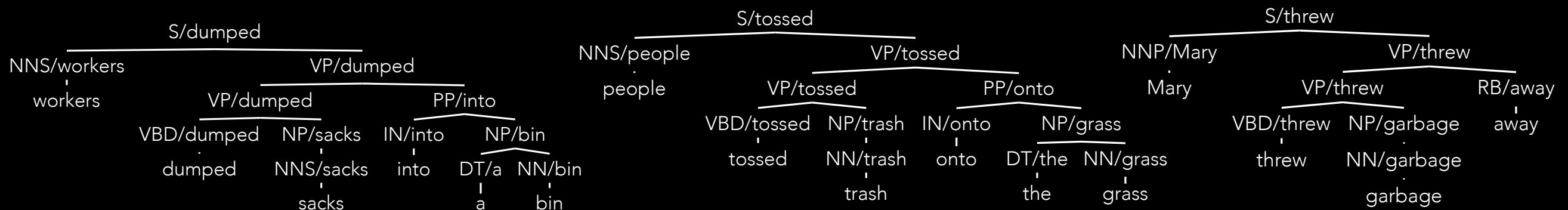
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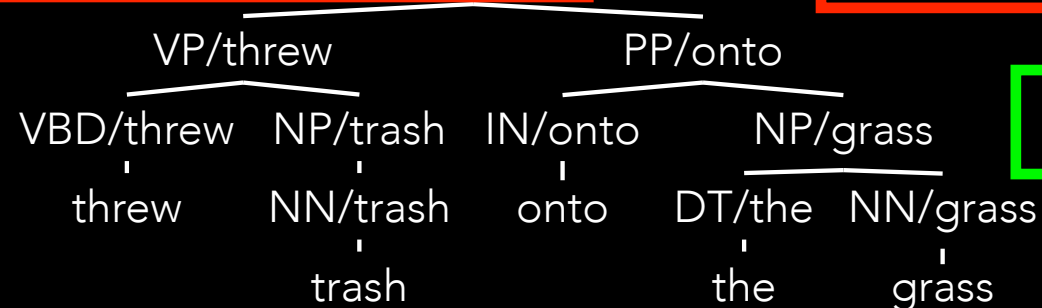
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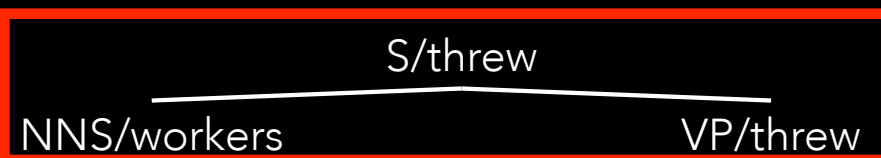
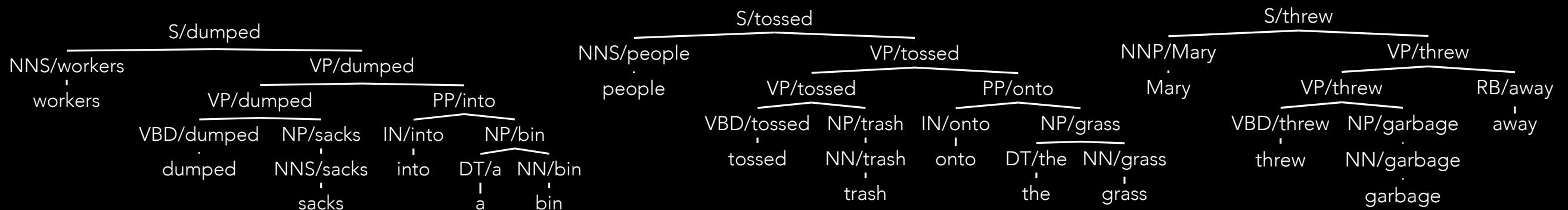
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0/0

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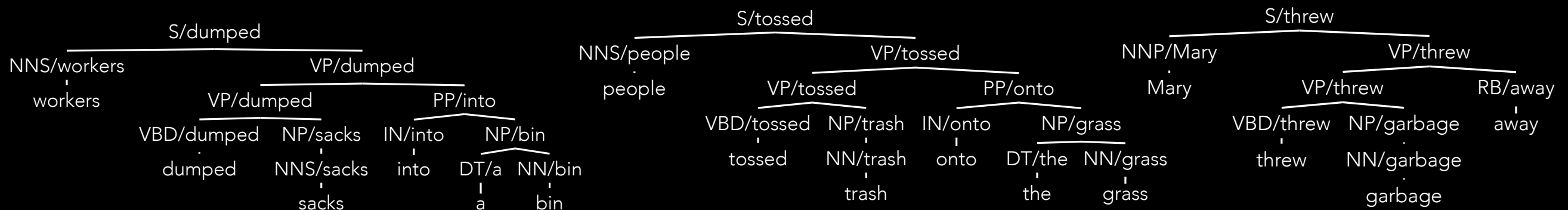
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0/0

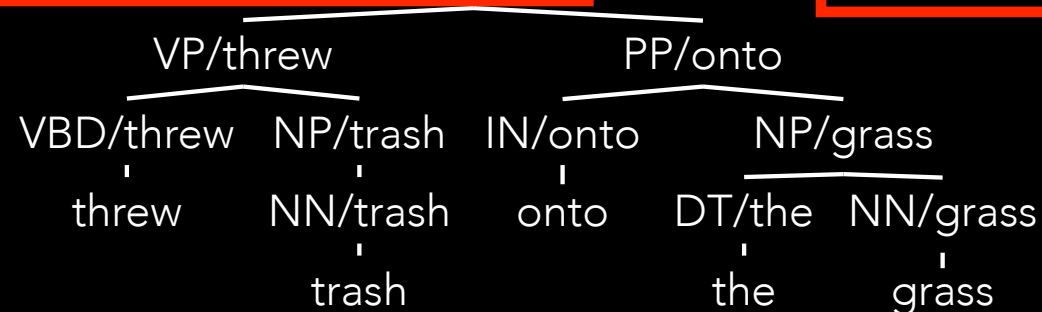
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**S -> NNS/workers VP**

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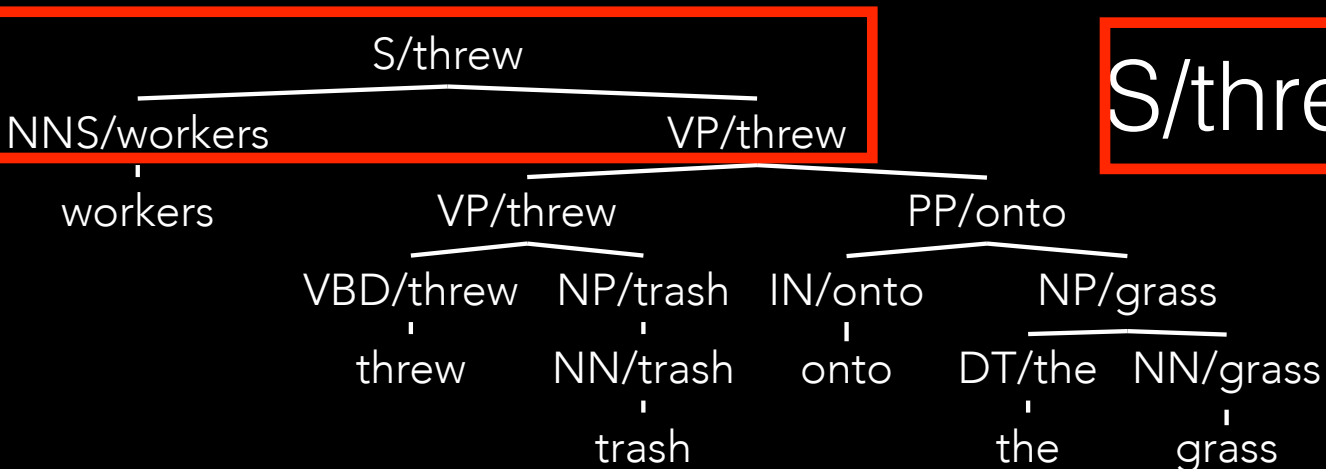
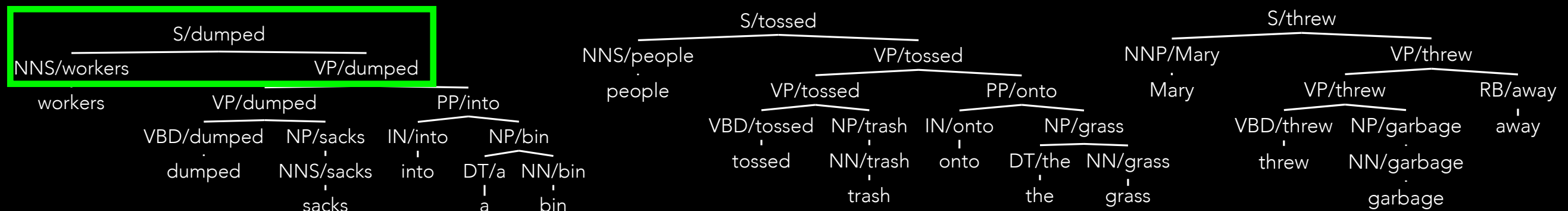
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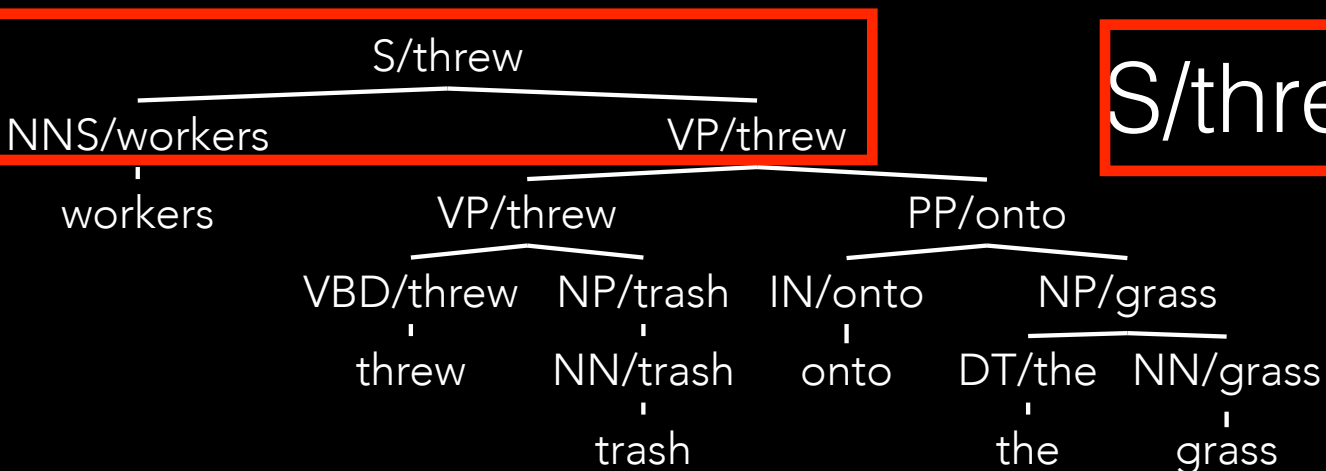
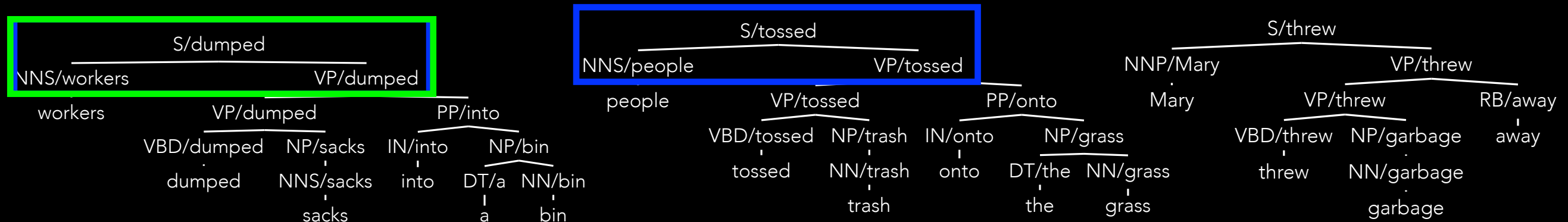
0/0



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*S/threw* -> *NNS/workers* *VP/threw*

*S* -> *NNS/workers* *VP*

*S* -> *NNS* *VP*

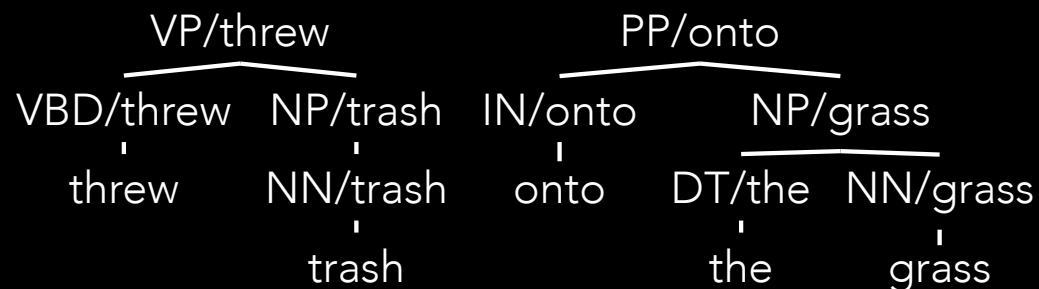
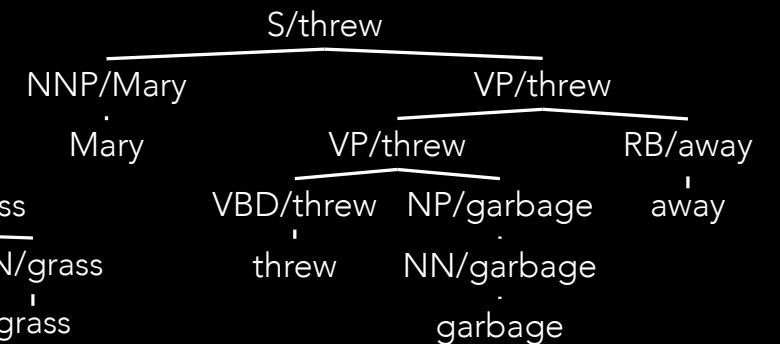
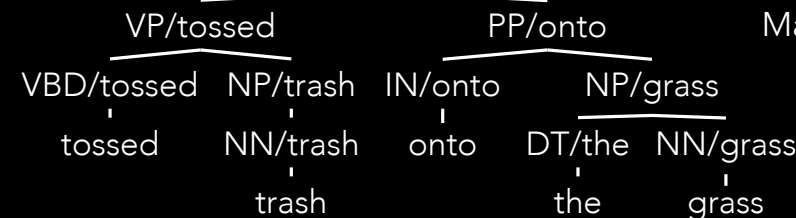
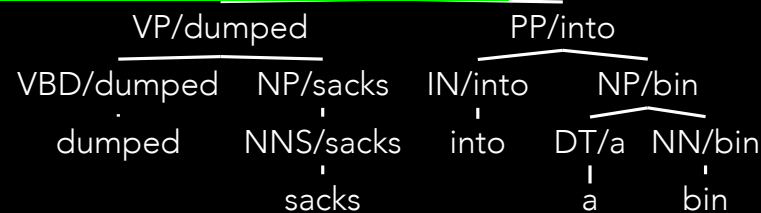
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0/0

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0/0                      20/40

# Smoothing Lexicalized PCFGs

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- Here we'll apply it to lexicalization, e.g.:  
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# Witten-Bell Smoothing

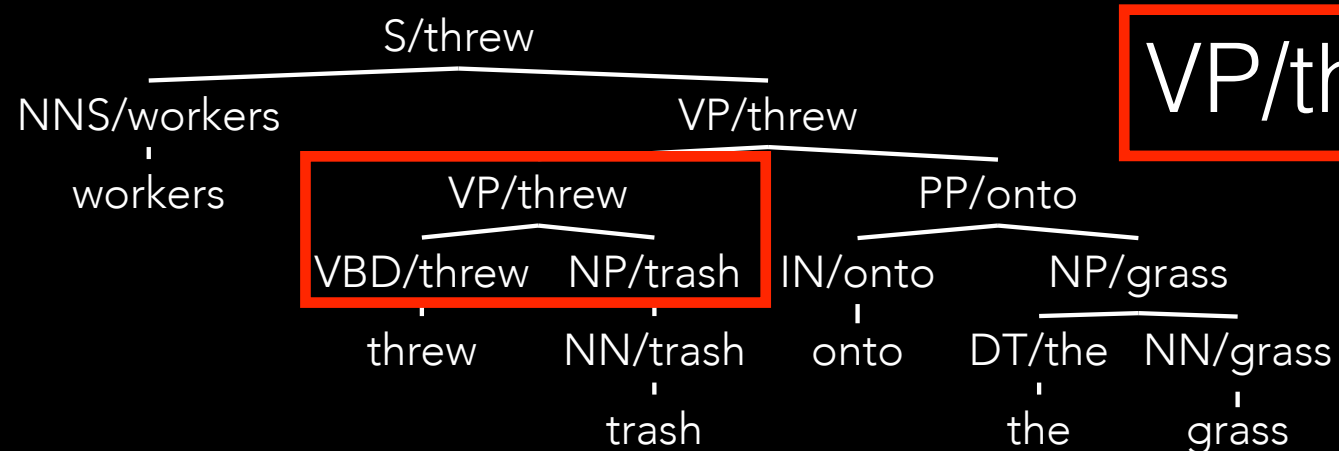
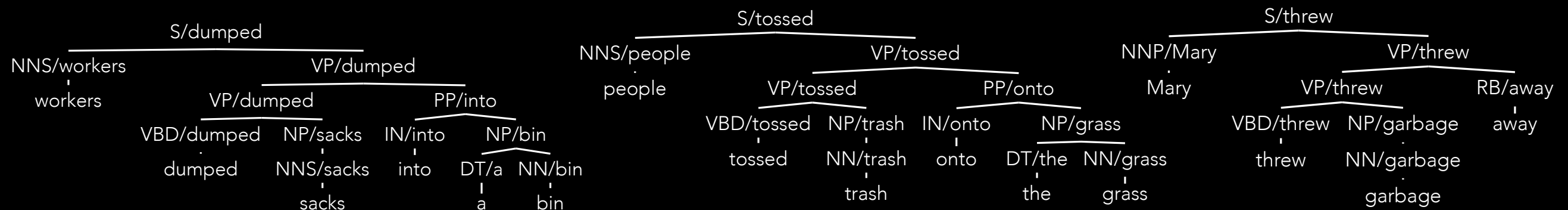
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- $\lambda_C = 0$  if  $C$  never seen

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

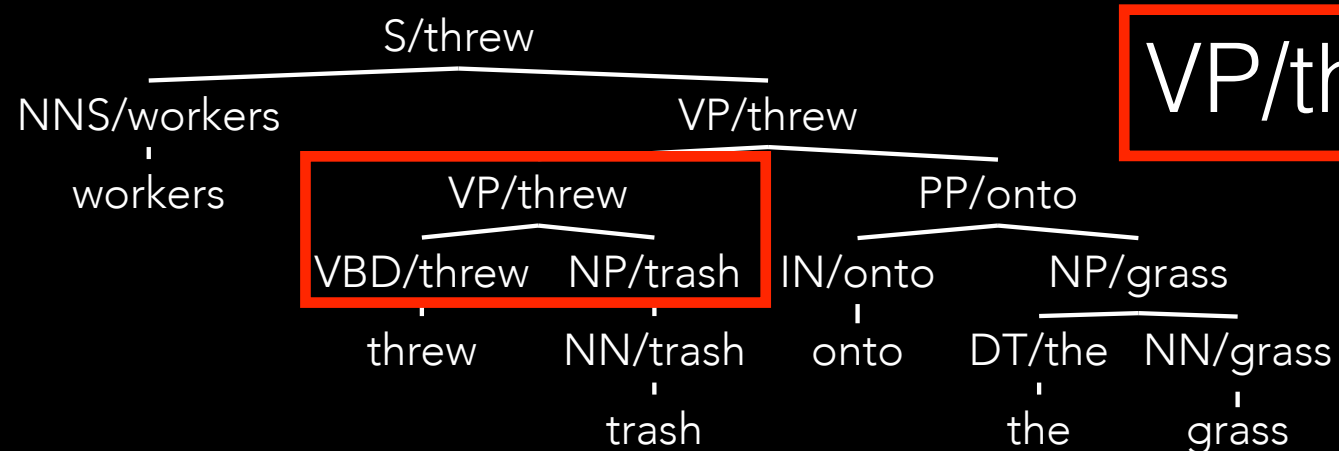
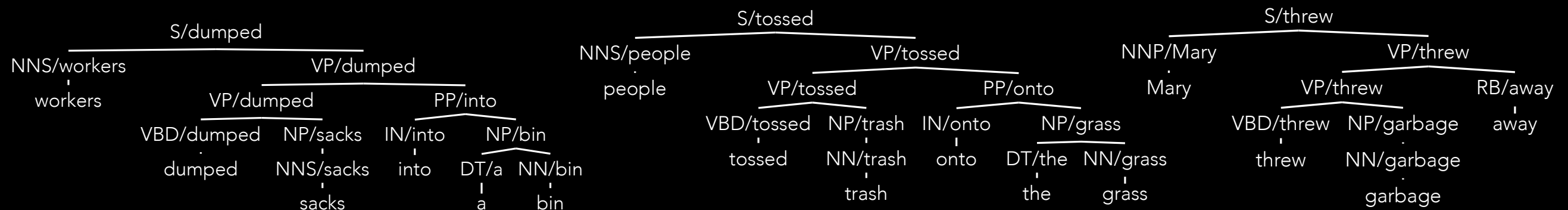
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20/40

60/120

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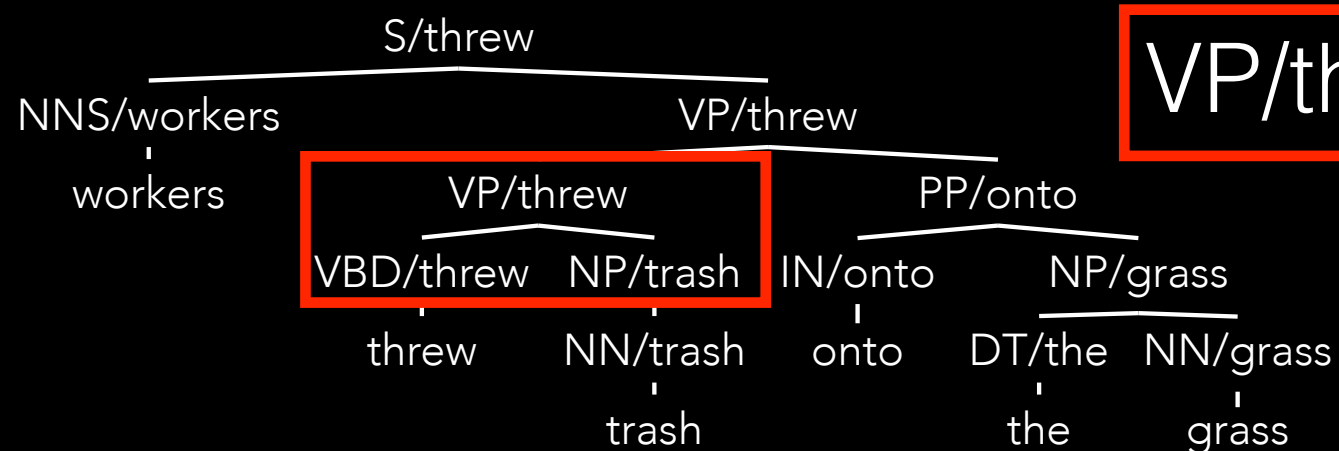
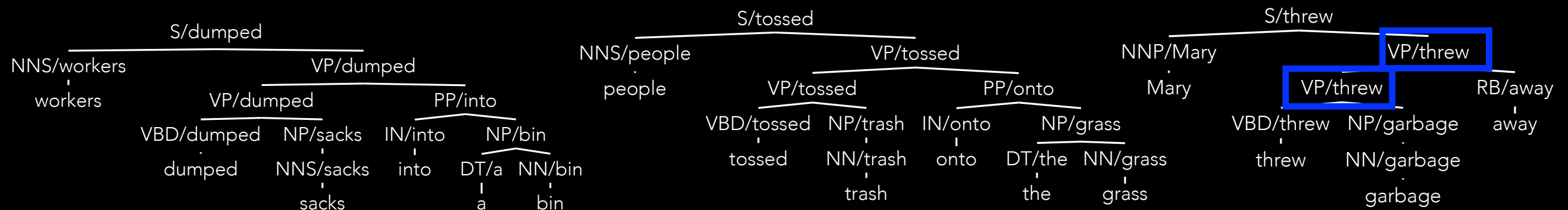
VP/threw → VBD/threw NP/trash

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20/40 60/120

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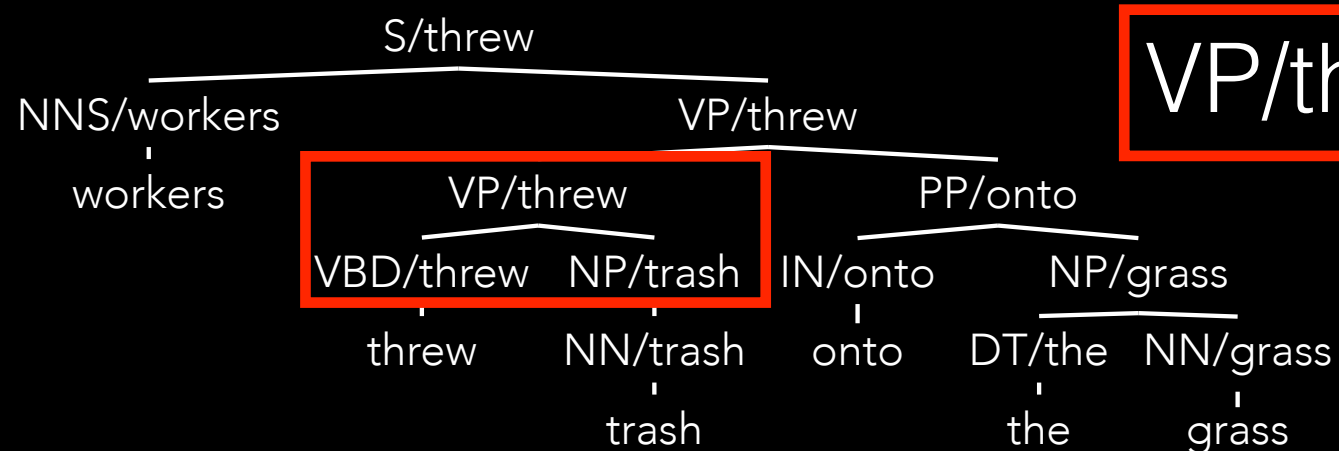
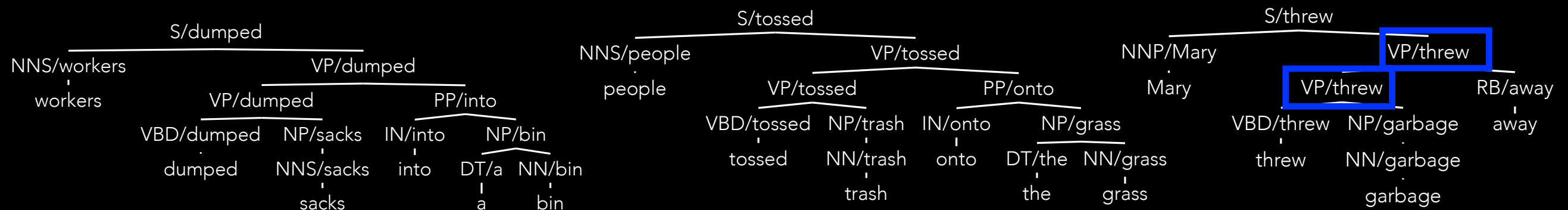
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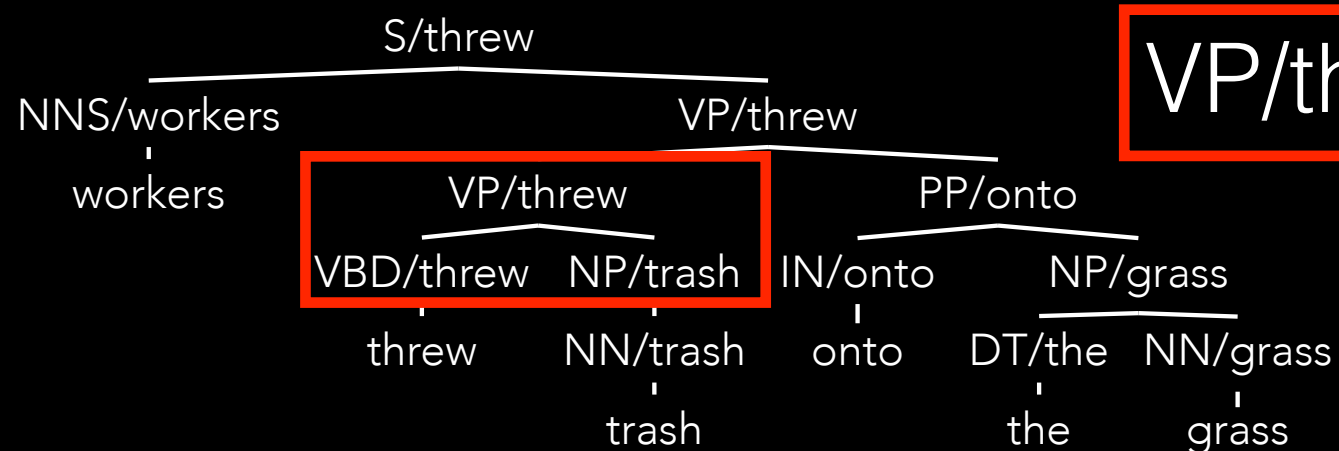
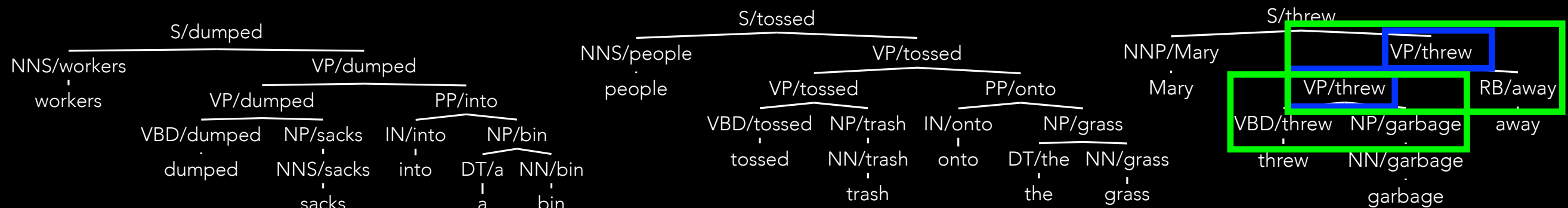
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20/40                      60/120



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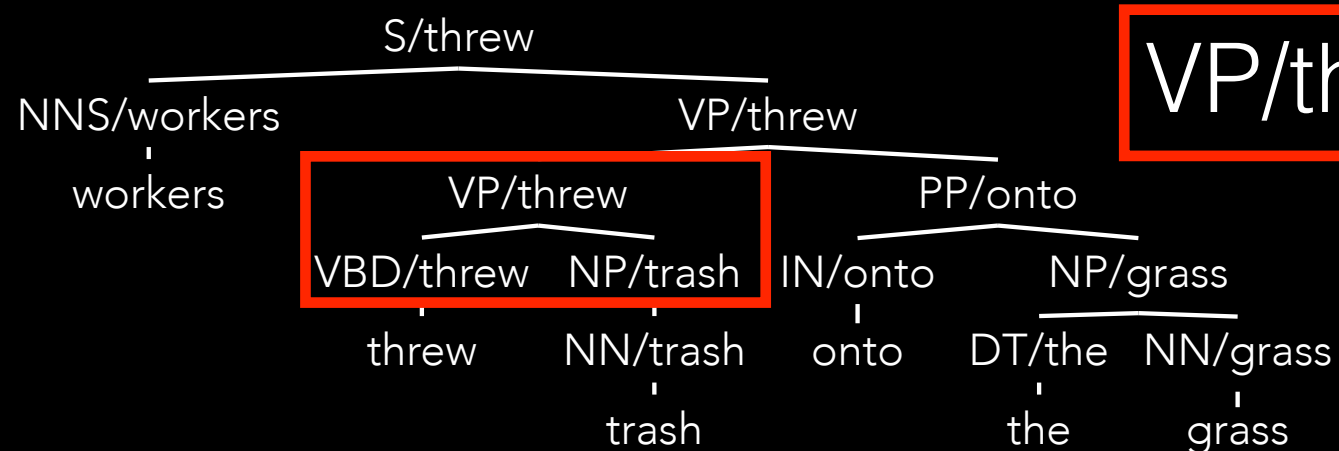
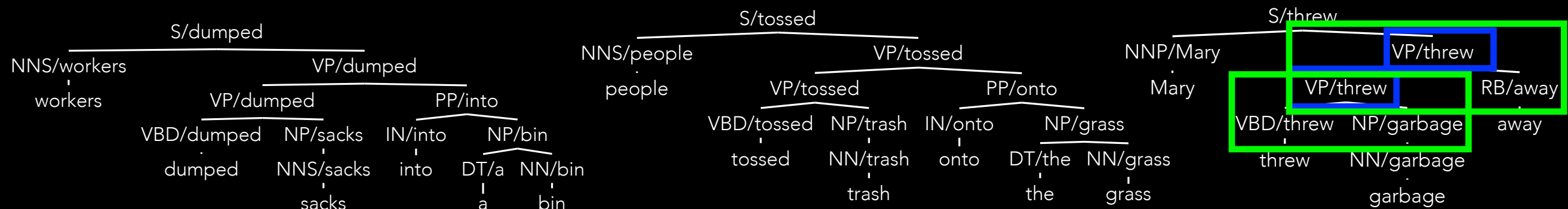
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20/40
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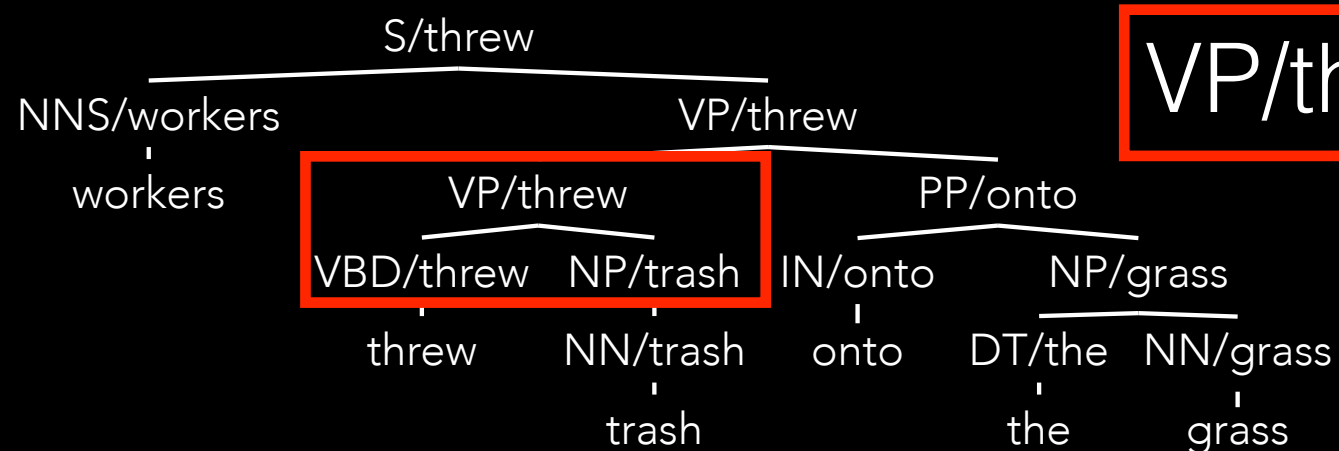
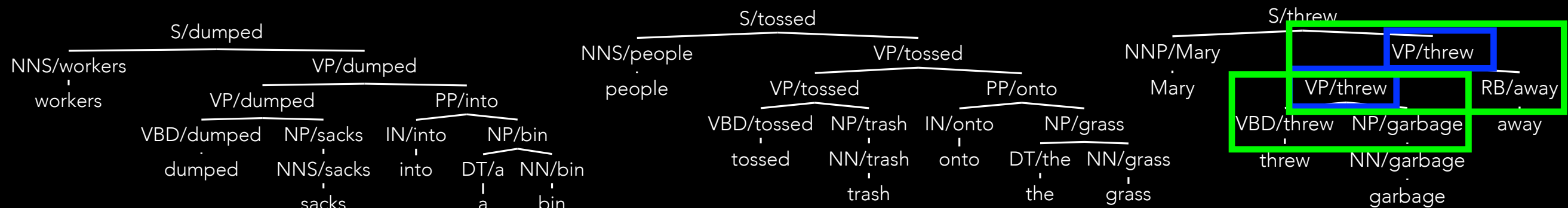
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$\frac{40}{42} \times \frac{20}{40}$ 
 $\frac{60}{120}$

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Assume we saw each training tree 20 times



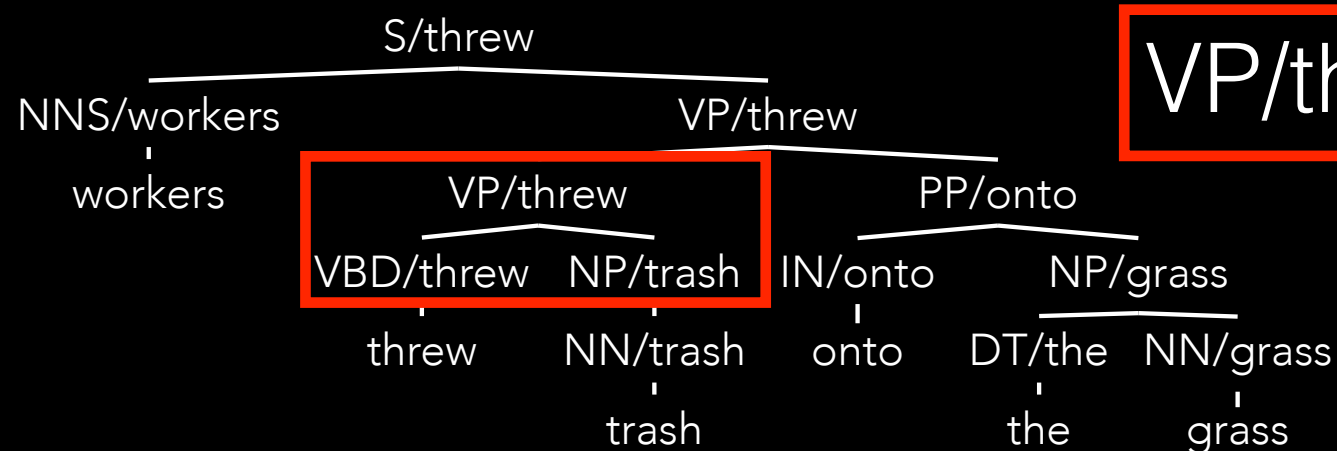
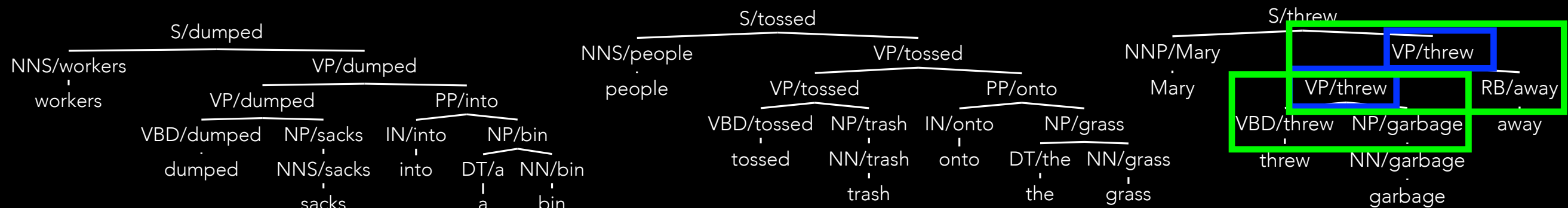
VP/threw → VBD/threw NP/trash

$$P(r | X, h) = \lambda_1 P_{ML}(r | X, h) + (1 - \lambda_1) P_{ML}(r | X)$$

$\frac{40}{42} \times \frac{20}{40}$ 
 $\frac{2}{42} \times \frac{60}{120}$

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

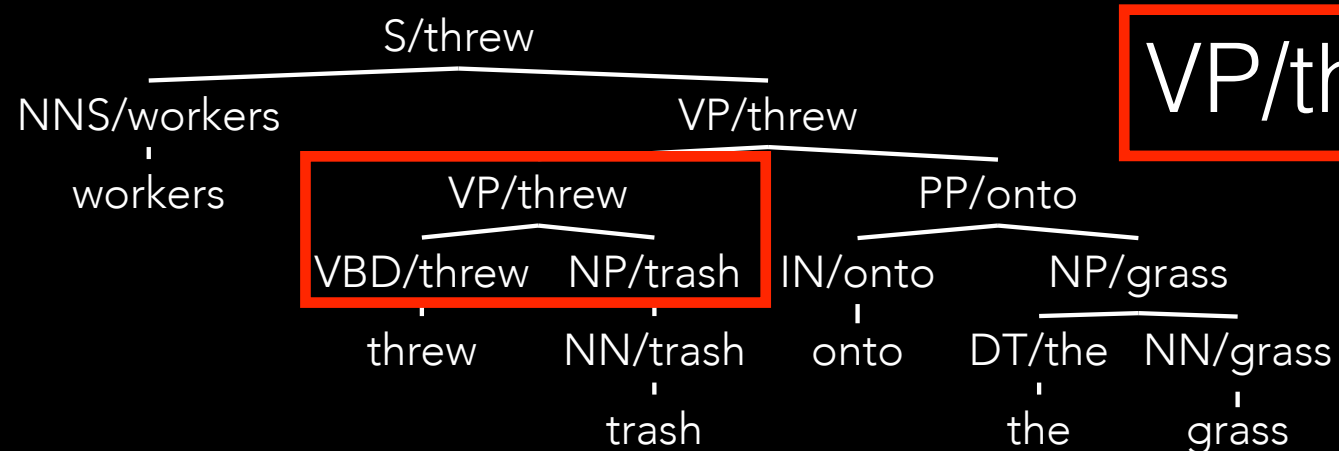
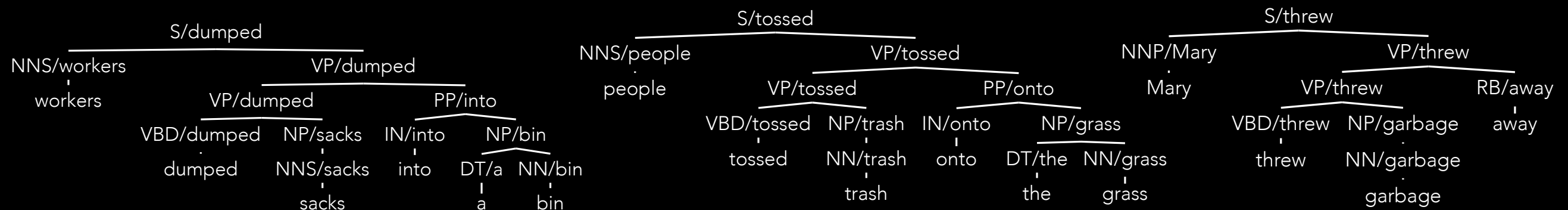
$$P(r | X, h) = \lambda_1 P_{ML}(r | X, h) + (1 - \lambda_1) P_{ML}(r | X)$$

$$40/42 \times 20/40 \quad 2/42 \times 60/120$$

=0.5

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

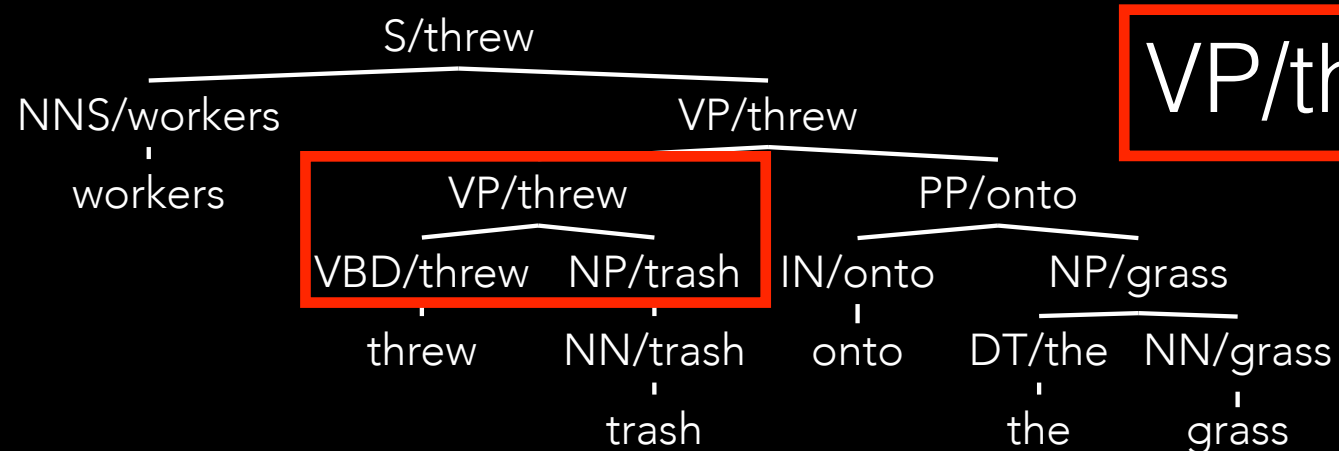
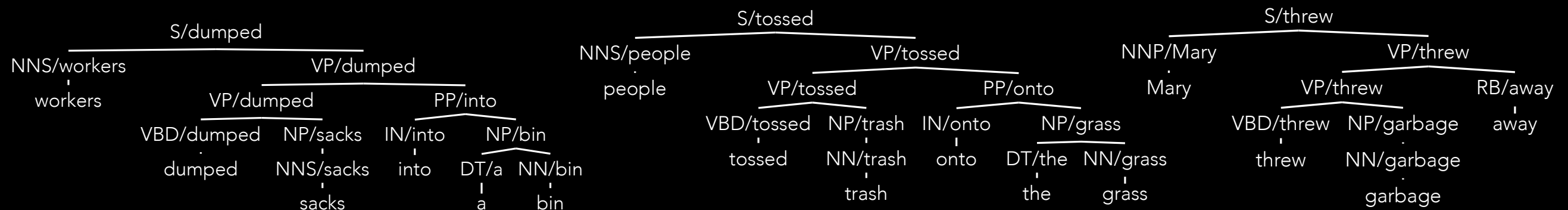
$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

0/20

20/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

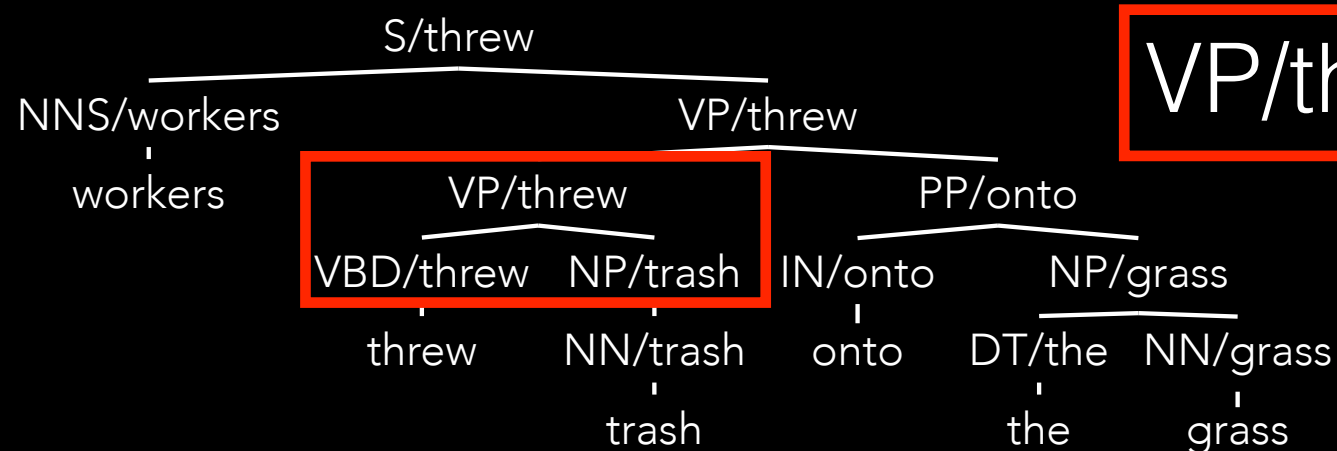
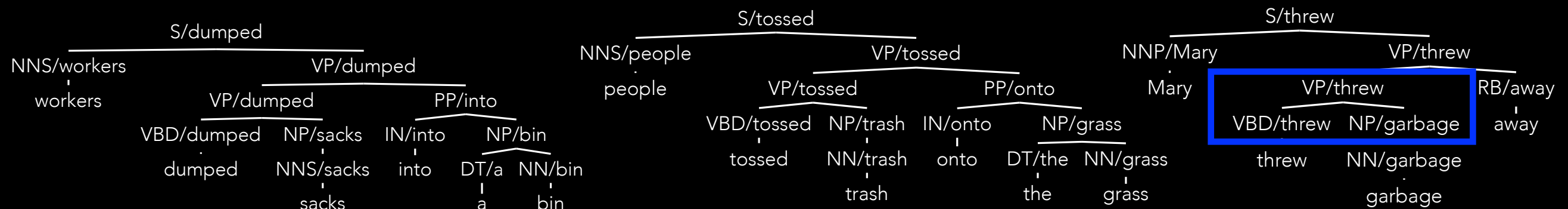
$$P(m \mid \boxed{r, X, h}) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

0/20

20/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw  $\rightarrow$  VBD/threw NP/trash

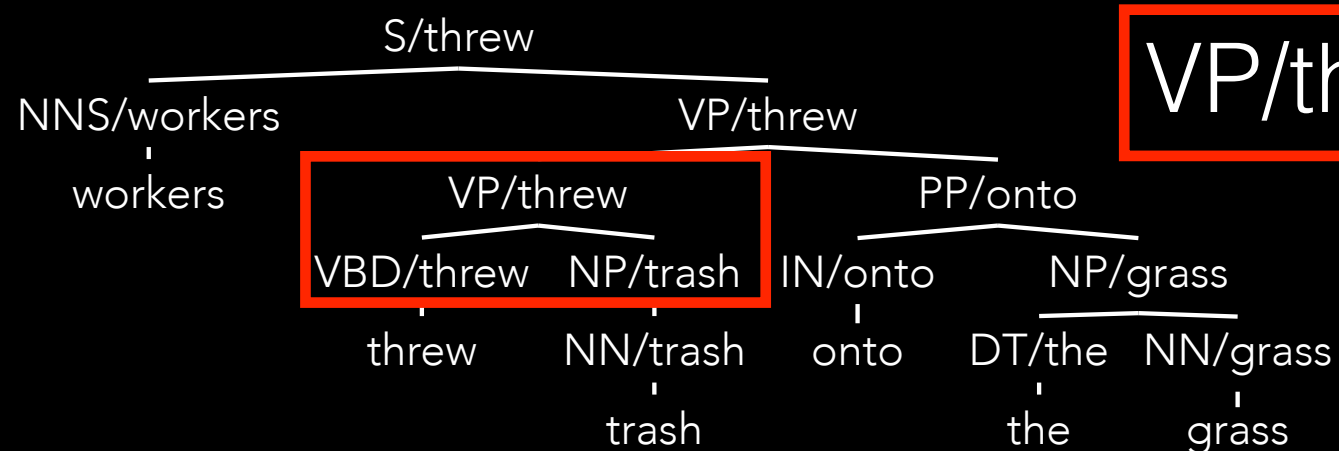
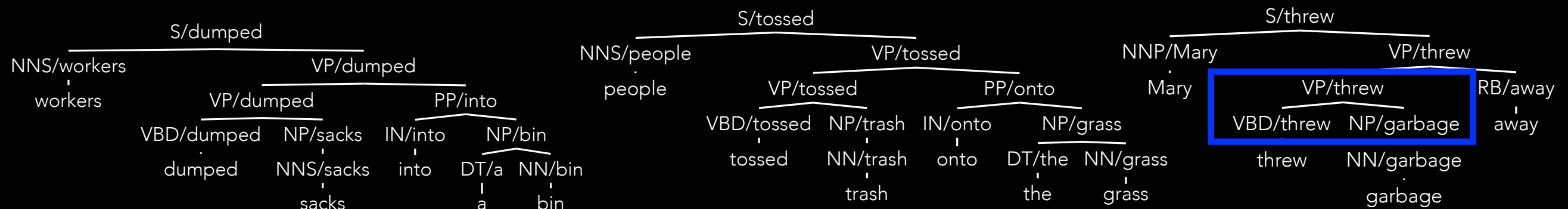
$$P(m \mid \boxed{r, X, h}) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

0/20

20/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

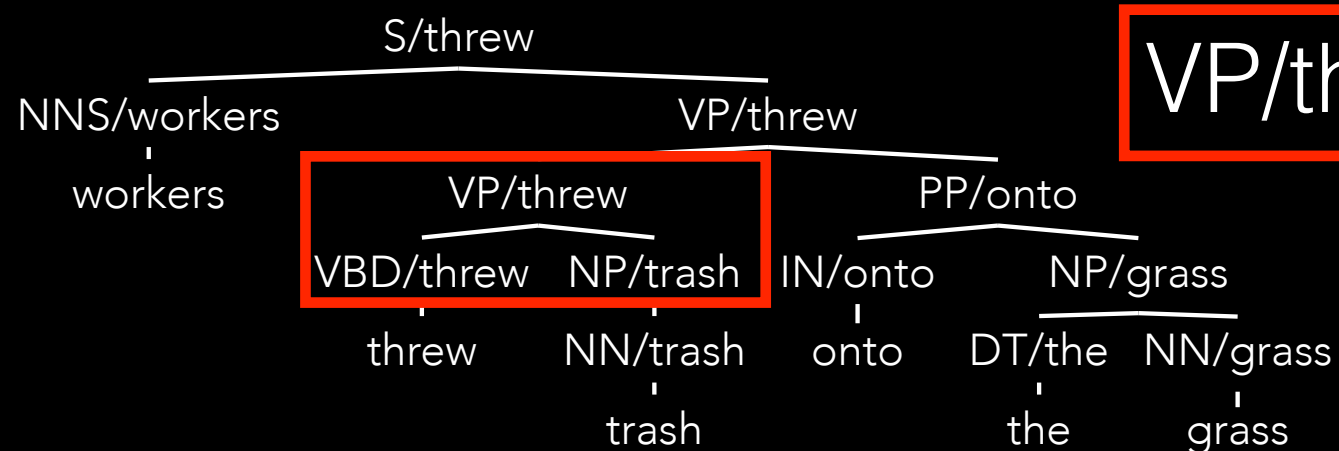
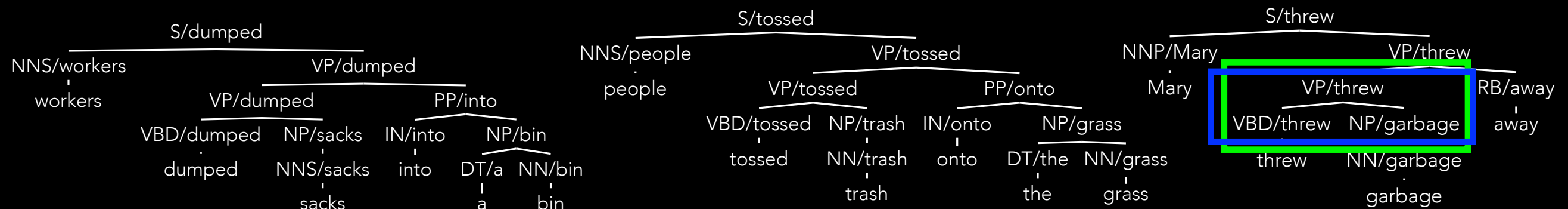
$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

0/20                      20/60



# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw -> VBD/threw NP/trash

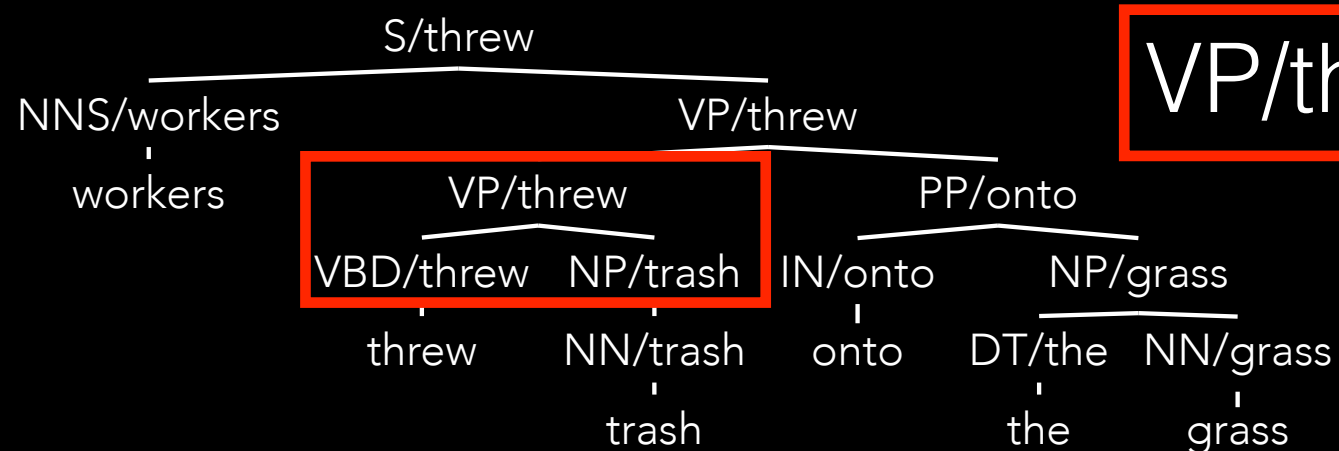
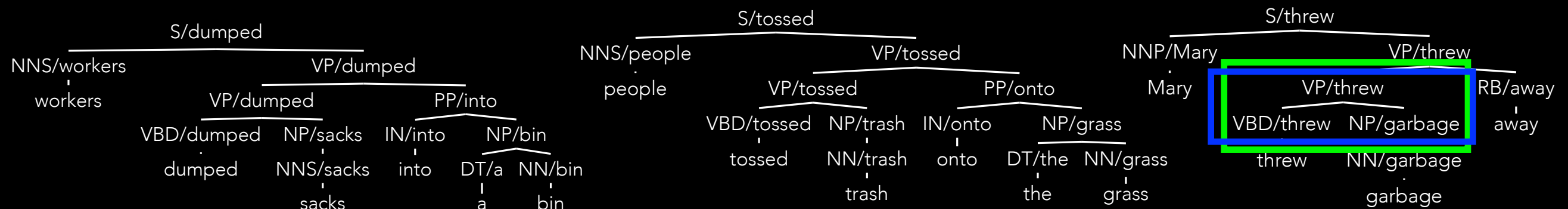
$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

0/20

20/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



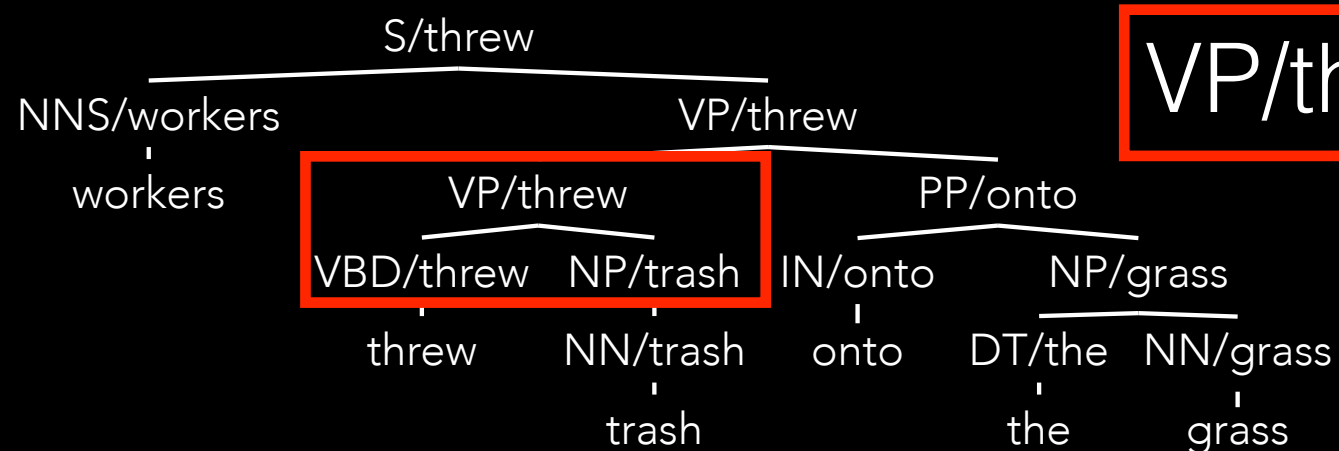
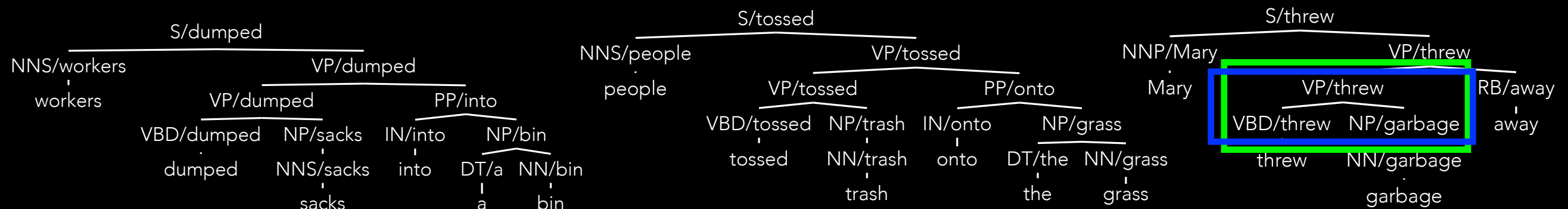
VP/threw → VBD/threw NP/trash

$$P(\boxed{m} \mid \boxed{r, X, h}) = \lambda_2 P_{\text{ML}}(m \mid r, X, h) + (1 - \lambda_2) P_{\text{ML}}(m \mid r)$$

$20/21 \times 0/20$ 
 $20/60$

# Incorporating Smoothing

Assume we saw each training tree 20 times



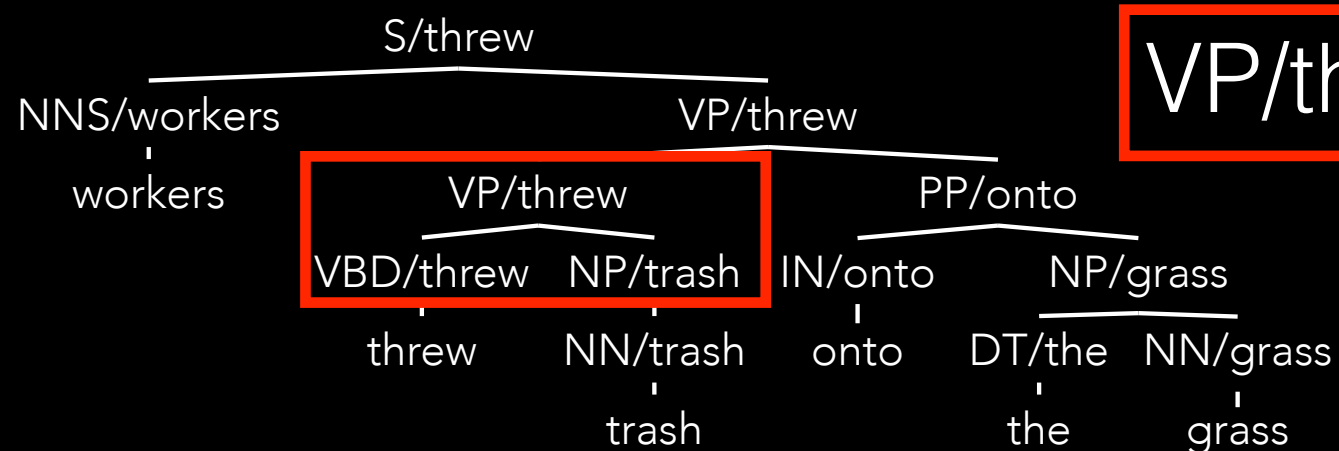
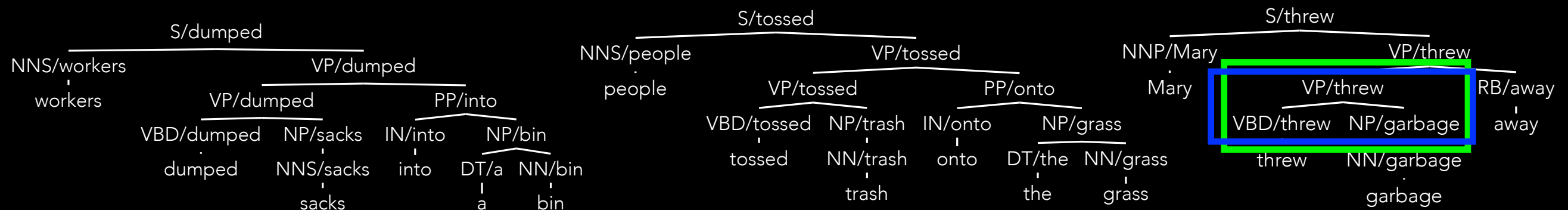
VP/threw → VBD/threw NP/trash

$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

$\frac{20}{21} \times \frac{0}{20}$ 
 $\frac{1}{21} \times \frac{20}{60}$

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

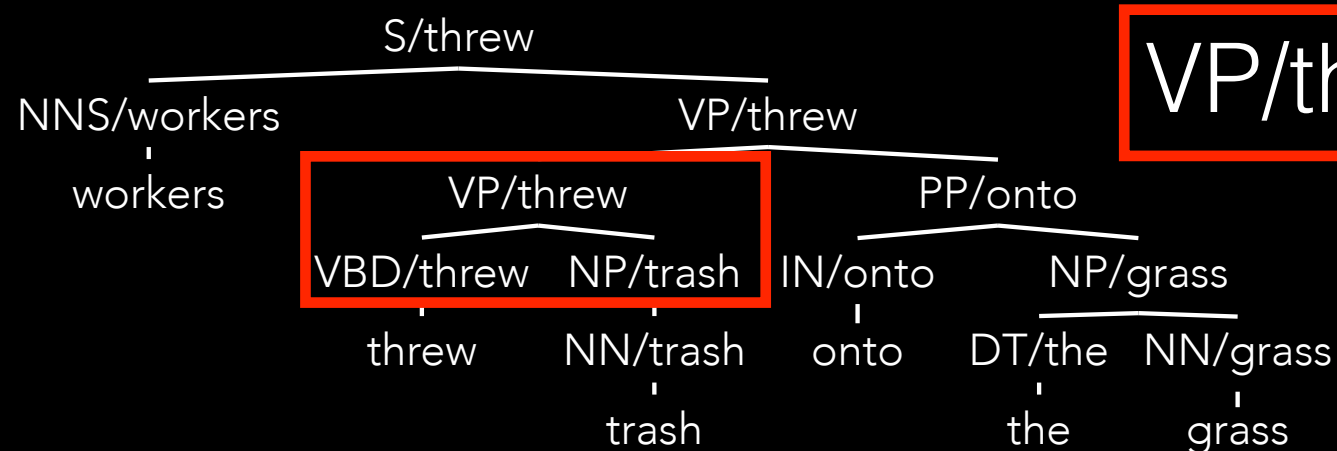
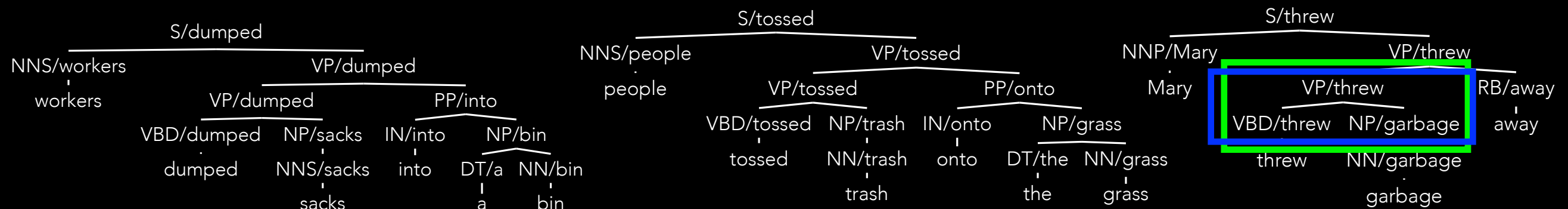
$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

$\frac{20}{21} \times \frac{0}{20} \qquad \frac{1}{21} \times \frac{20}{60}$

=.016

# Incorporating Smoothing

Assume we saw each training tree 20 times



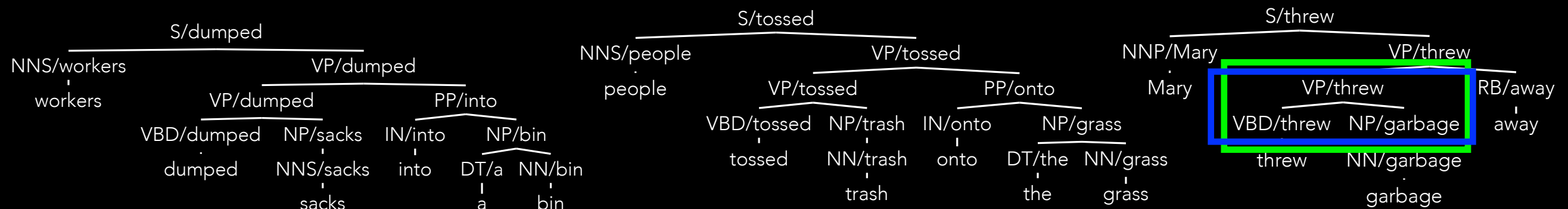
VP/threw -> VBD/threw NP/trash

$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

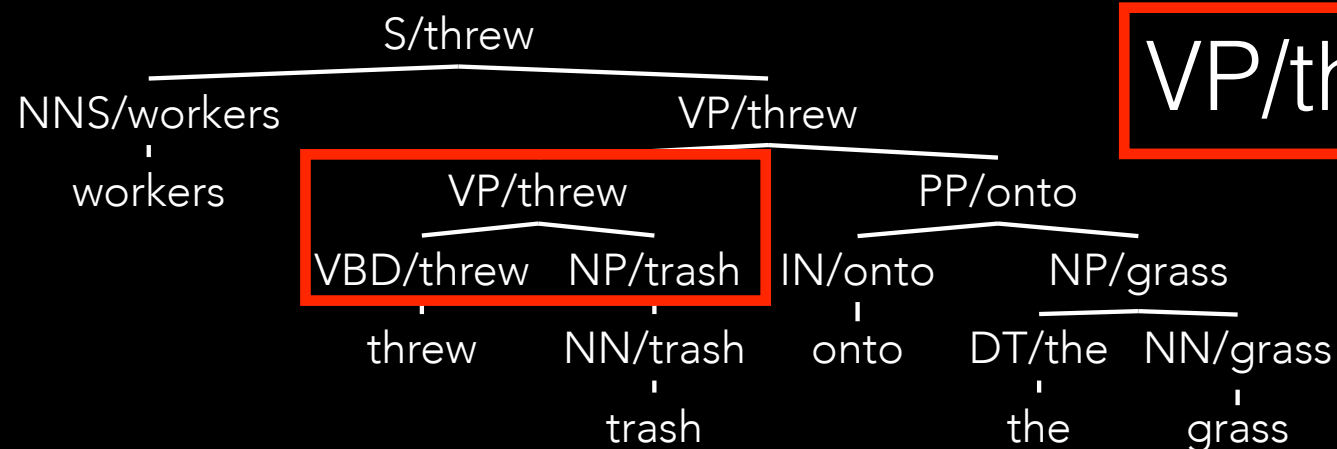
$$=.016 \quad \frac{20/21 \times 0/20}{VP/threw \rightarrow VBD/threw \ NP/trash} + \frac{1/21 \times 20/60}{}$$

# Incorporating Smoothing

Assume we saw each training tree 20 times



VP/threw → VBD/threw NP/trash

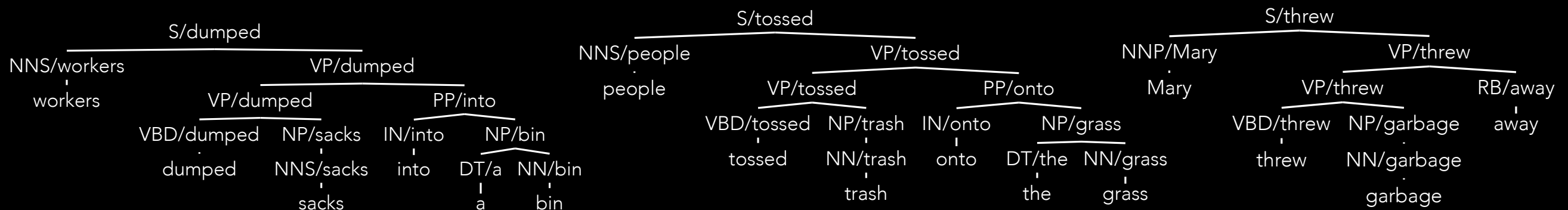


$$P(m | r, X, h) = \lambda_2 P_{ML}(m | r, X, h) + (1 - \lambda_2) P_{ML}(m | r)$$

$$=.016 \quad \text{VP/threw} \rightarrow \text{VBD/threw NP/trash} = .5 \times \frac{20}{21} \times \frac{0}{20} + .5 \times \frac{1}{21} \times \frac{20}{60} = .5 \times .016 = .008$$

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw -> NNS/workers VP/threw

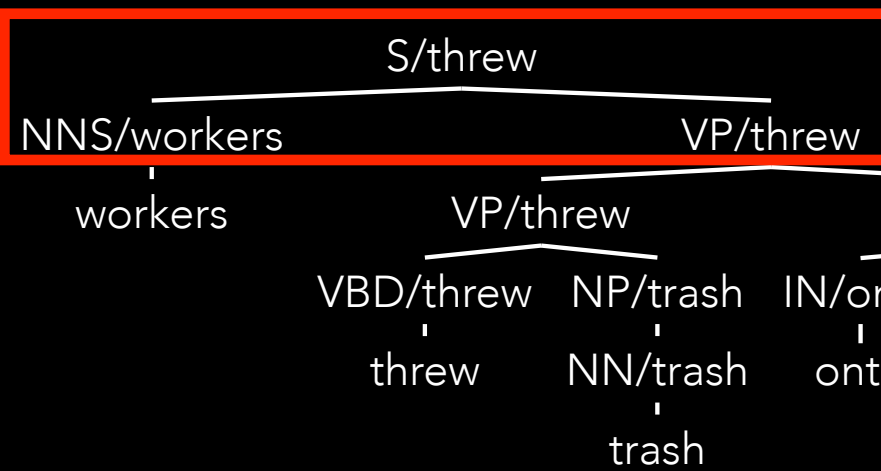
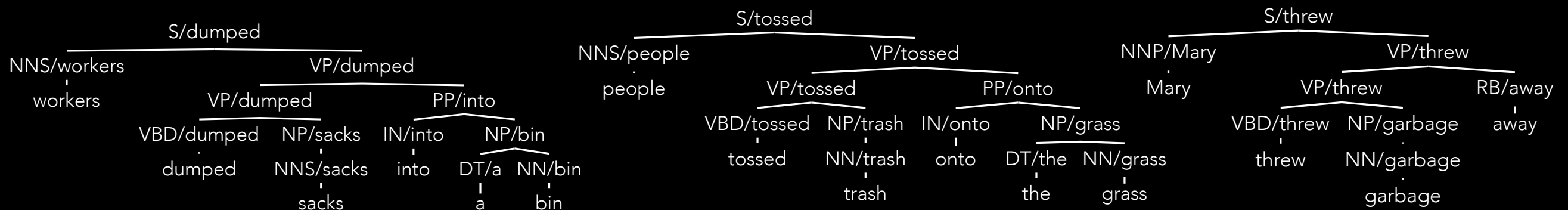
$$P(r \mid X, h) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

0/20

40/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw → NNS/workers VP/threw

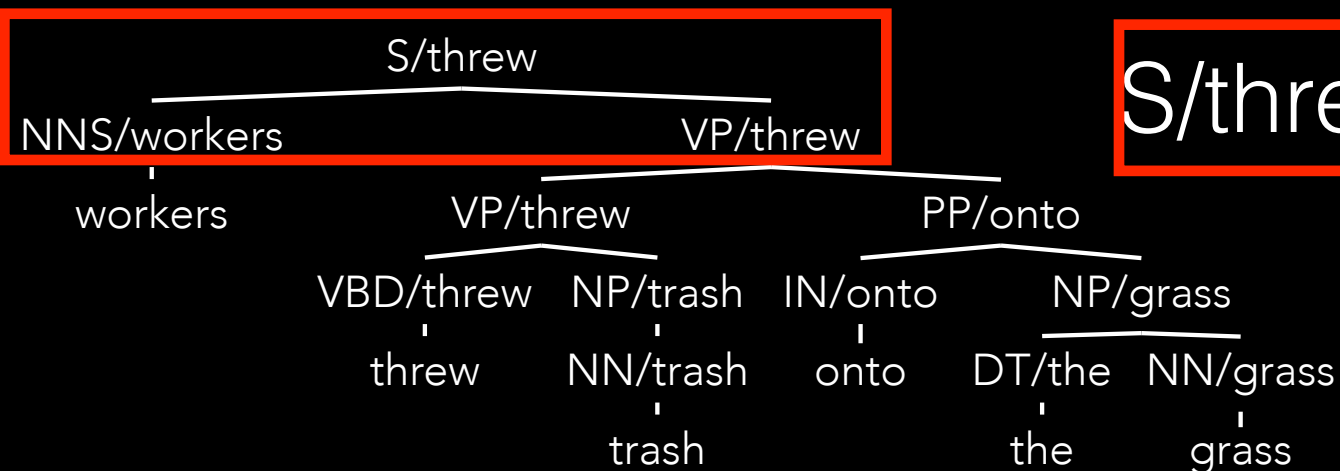
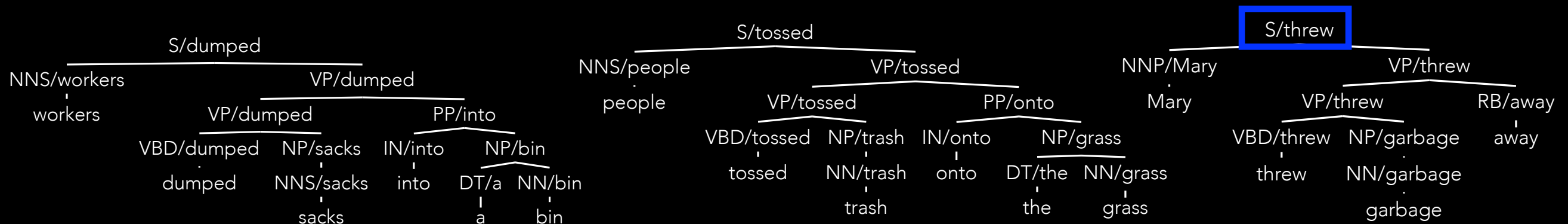
$$P(r \mid \boxed{X, h}) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

0/20                      40/60



# Incorporating Smoothing

Assume we saw each training tree 20 times



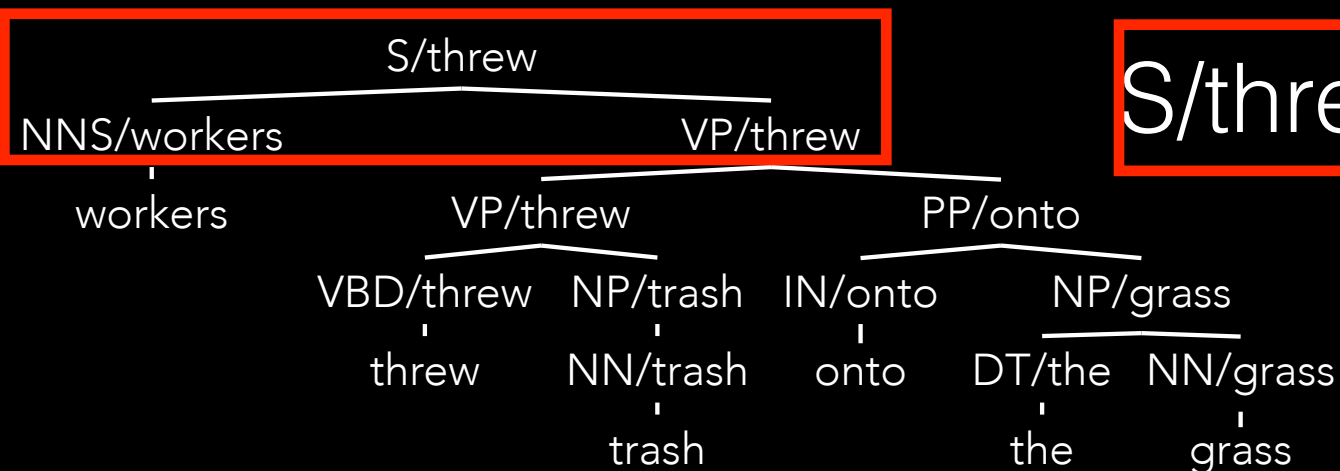
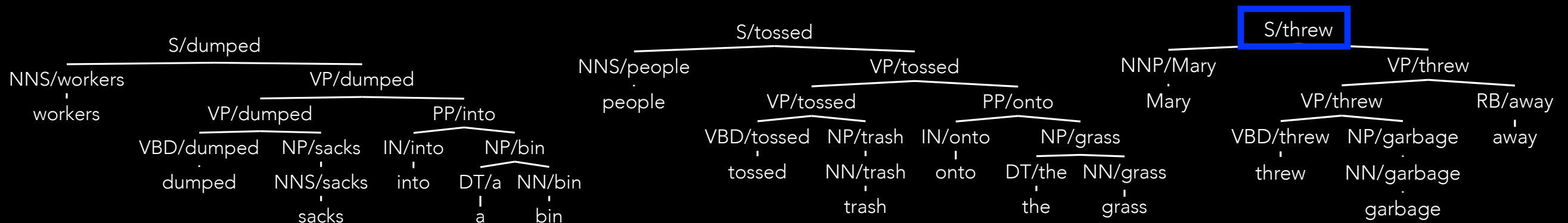
*S/threw* → *NNS/workers* *VP/threw*

$$P(r \mid \boxed{X, h}) = \lambda_1 P_{ML}(r \mid X, h) + (1 - \lambda_1) P_{ML}(r \mid X)$$

0/20                      40/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



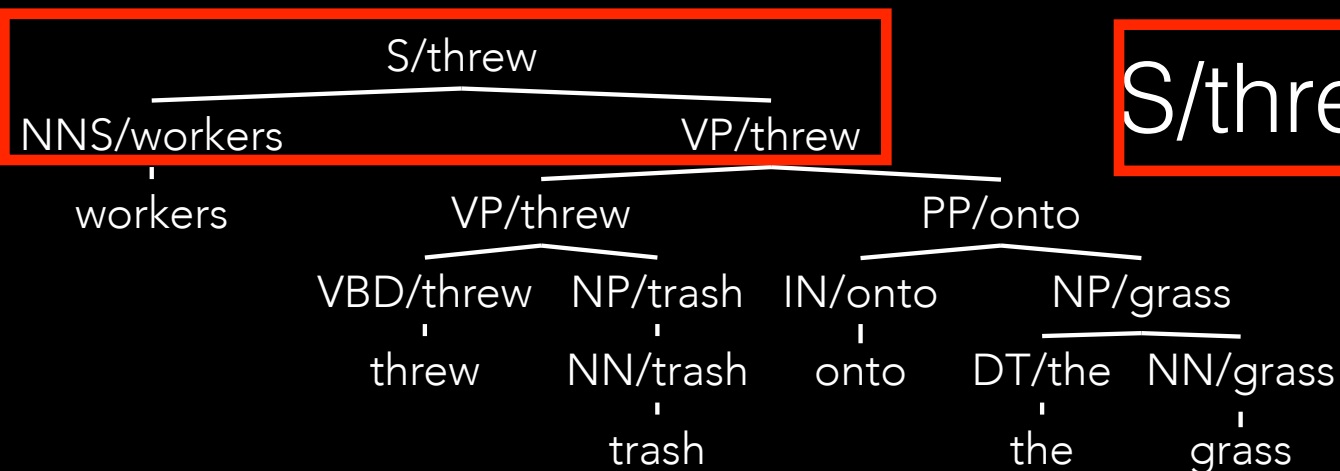
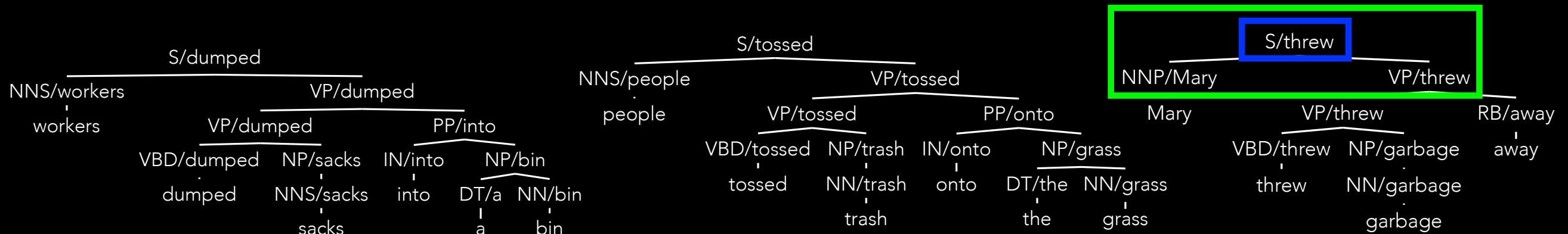
*S/threw* → *NNS/workers* *VP/threw*

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0/20                      40/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



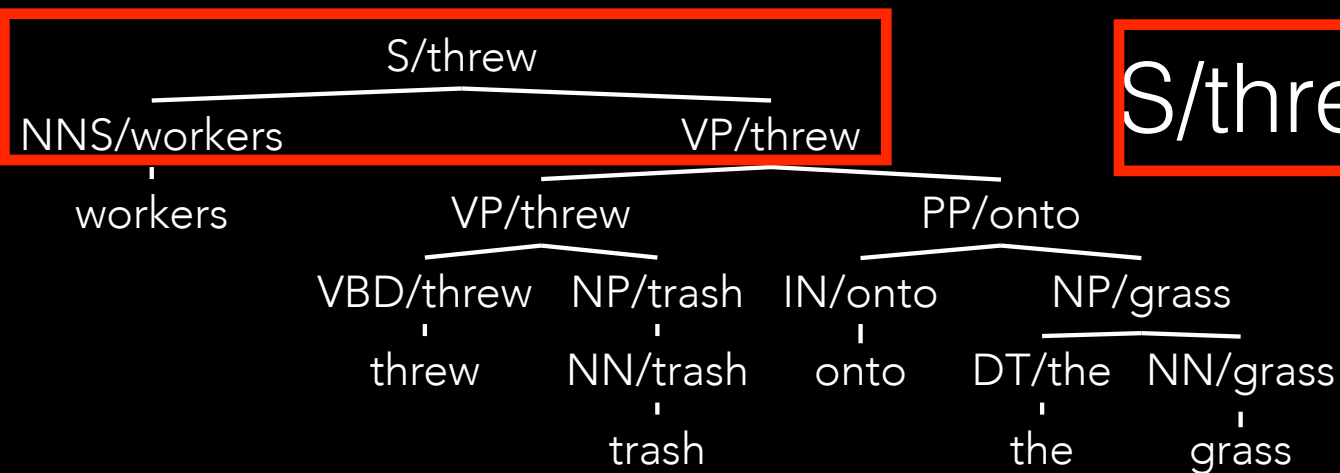
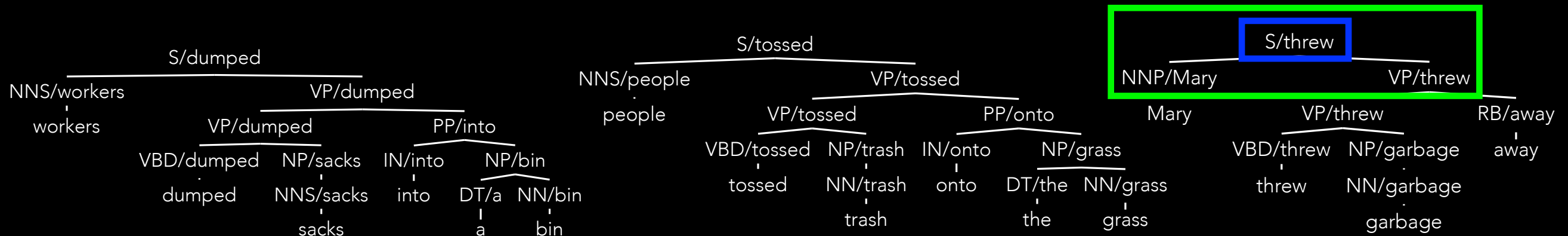
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0/20                      40/60

# Incorporating Smoothing

Assume we saw each training tree 20 times



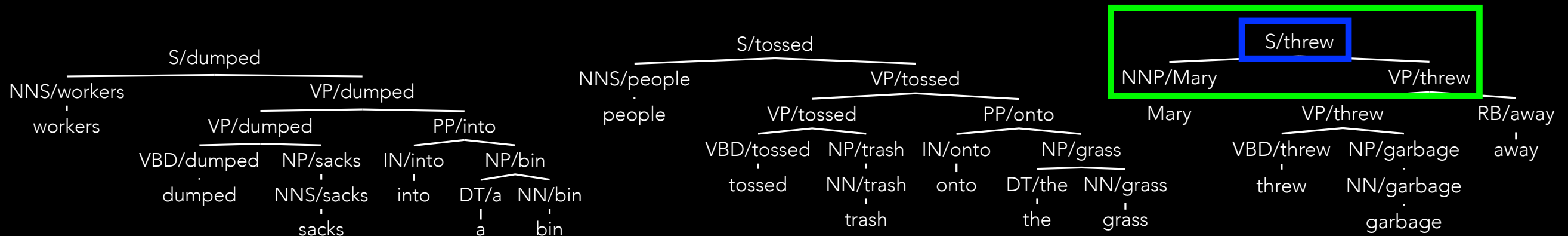
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$$P(r | X, h) = \lambda_1 P_{ML}(r | X, h) + (1 - \lambda_1) P_{ML}(r | X)$$

$\frac{20}{21} \times \frac{0}{20}$ 
 $\frac{40}{60}$

# Incorporating Smoothing

Assume we saw each training tree 20 times



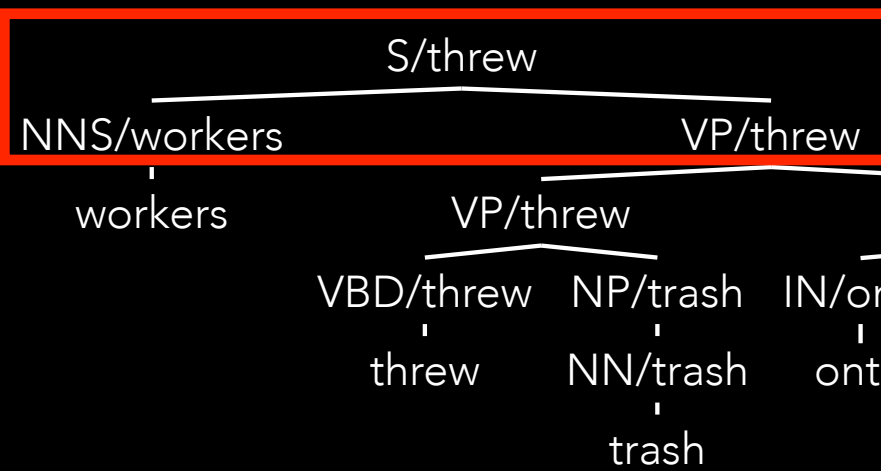
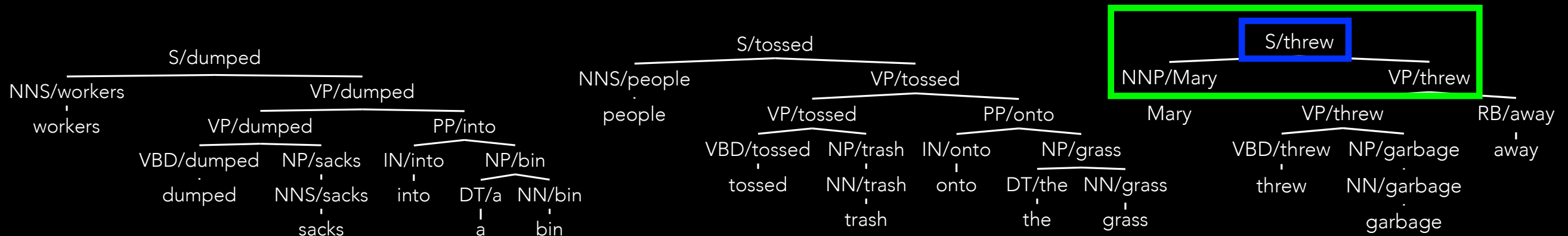
S/threw → NNS/workers VP/threw

$$P(r | X, h) = \lambda_1 P_{ML}(r | X, h) + (1 - \lambda_1) P_{ML}(r | X)$$

$\frac{20}{21} \times \frac{0}{20} \quad \frac{1}{21} \times \frac{40}{60}$

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw -> NNS/workers VP/threw

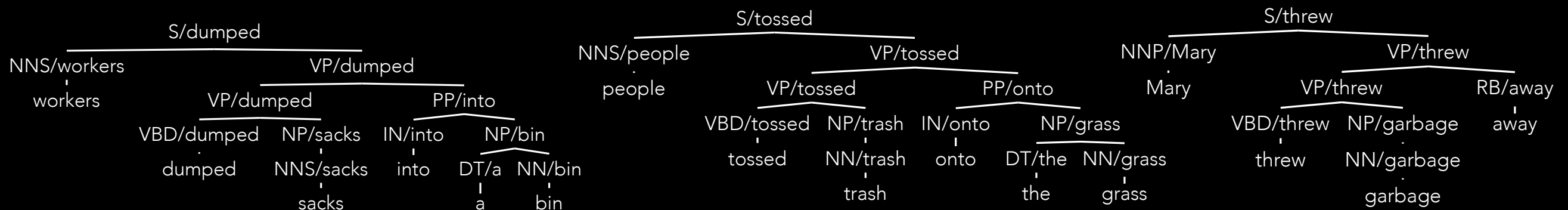
$$P(r | X, h) = \lambda_1 P_{ML}(r | X, h) + (1 - \lambda_1) P_{ML}(r | X)$$

20/21 x 0/20      1/21 x 40/60

=.032

# Incorporating Smoothing

Assume we saw each training tree 20 times



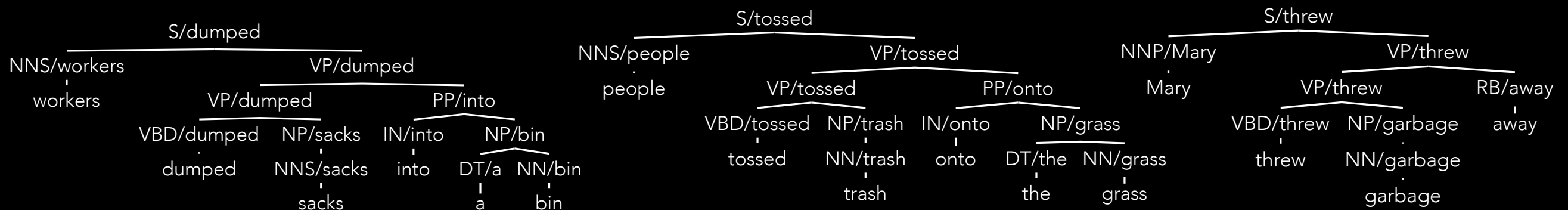
*S/threw* -> *NNS/workers* *VP/threw*

$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

0/0 20/40

# Incorporating Smoothing

Assume we saw each training tree 20 times



$S/threw \rightarrow NNS/workers \ VP/threw$

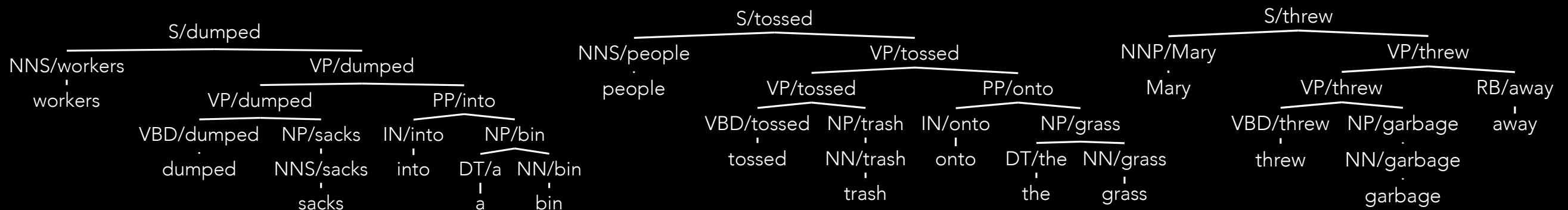
$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

$0 \times 0/0$ 
 $20/40$



# Incorporating Smoothing

Assume we saw each training tree 20 times



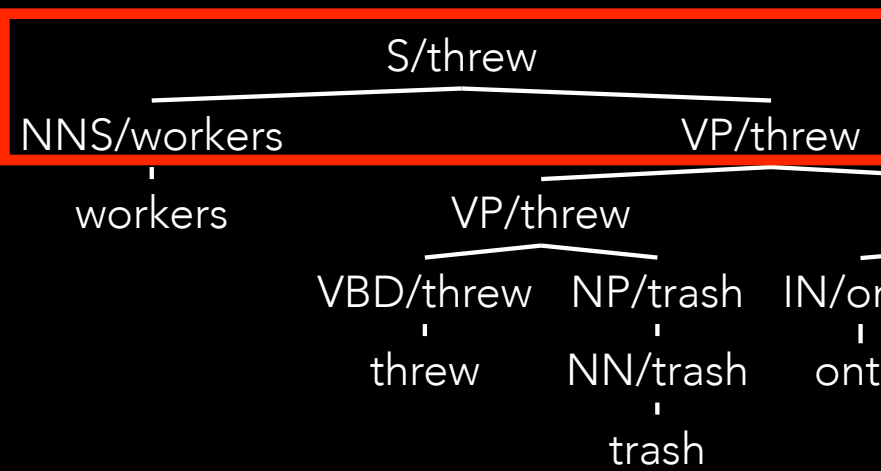
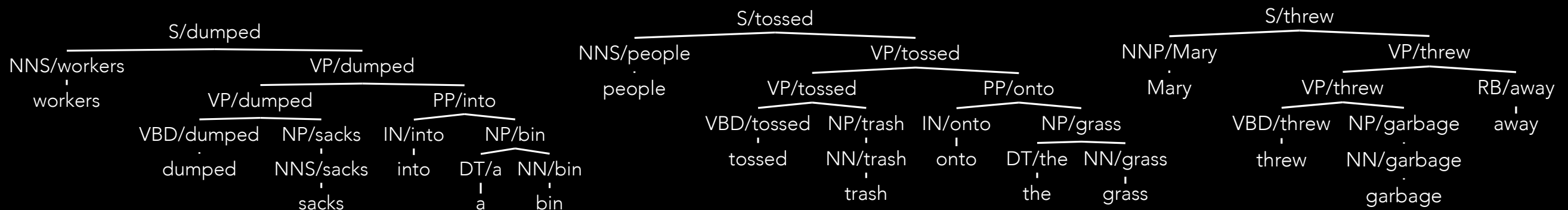
S/threw  $\rightarrow$  NNS/workers VP/threw

$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

$0 \times 0/0$ 
 $1 \times 20/40$

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw -> NNS/workers VP/threw

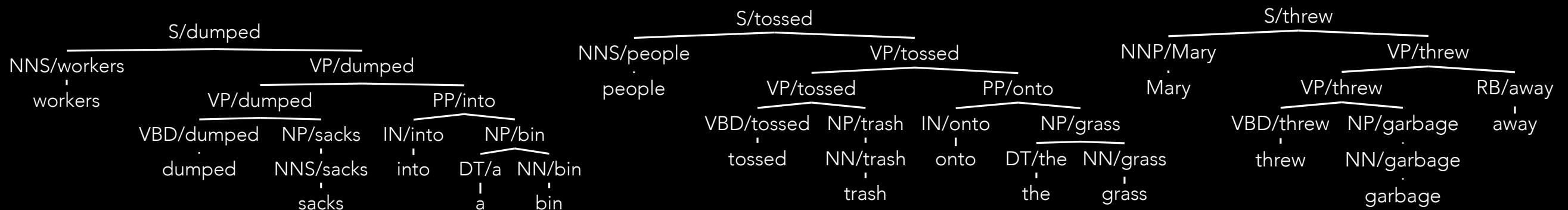
$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

$0 \times 0/0$ 
 $1 \times 20/40$

=0.5

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw -> NNS/workers VP/threw

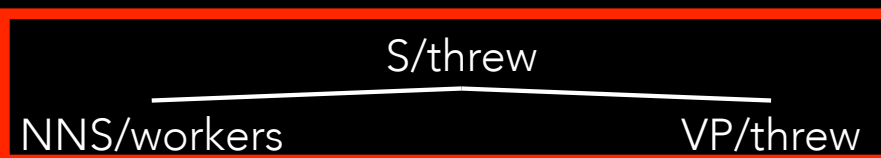
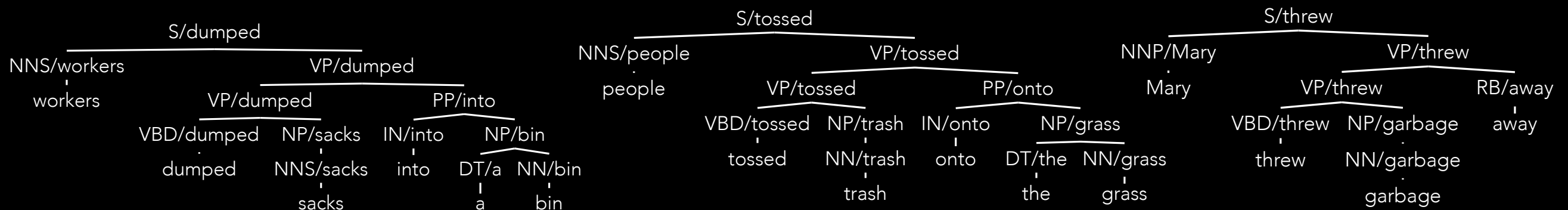
$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

0 x 0/0
1 x 20/40

=0.5      S/threw -> NNS/workers VP/threw

# Incorporating Smoothing

Assume we saw each training tree 20 times



S/threw -> NNS/workers VP/threw

$$P(m \mid r, X, h) = \lambda_2 P_{ML}(m \mid r, X, h) + (1 - \lambda_2) P_{ML}(m \mid r)$$

$0 \times 0/0$ 
 $1 \times 20/40$

=0.5      S/threw -> NNS/workers VP/threw = .032 \* .5 = .016

# Other Ways To Smooth

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- Replace infrequently seen words with <unk> in training; map unseen words to <unk> when parsing

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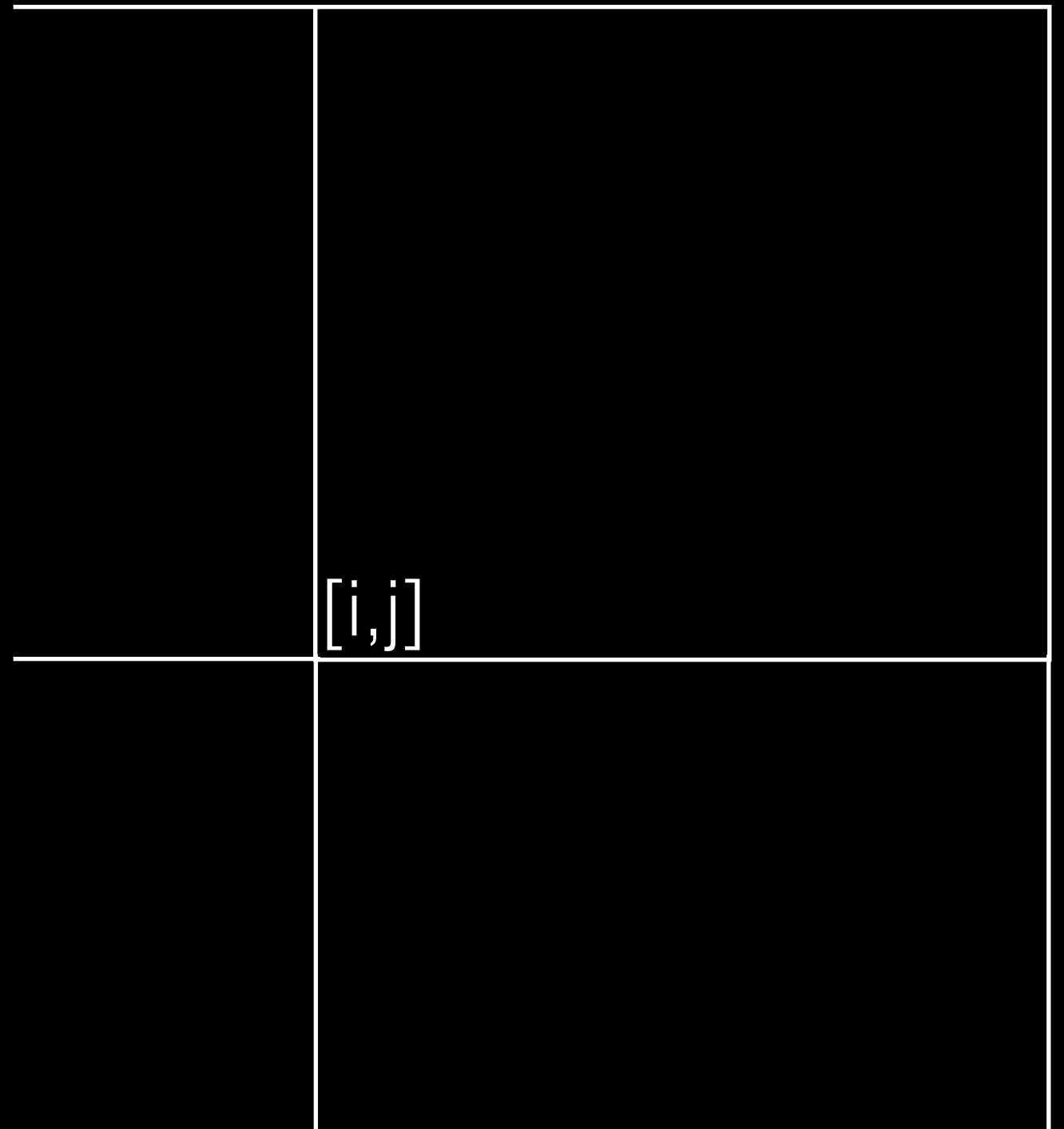
- Replace infrequently seen words with <unk> in training; map unseen words to <unk> when parsing
- For interesting suffixes, stem infrequent words instead of replacing them; “working” becomes <unk>-ing

# Other Ways To Smooth

- Replace infrequently seen words with <unk> in training; map unseen words to <unk> when parsing
- For interesting suffixes, stem infrequent words instead of replacing them; “working” becomes <unk>-ing
- POS-tag ‘lexicalization’ instead of/in addition to true lexicalization

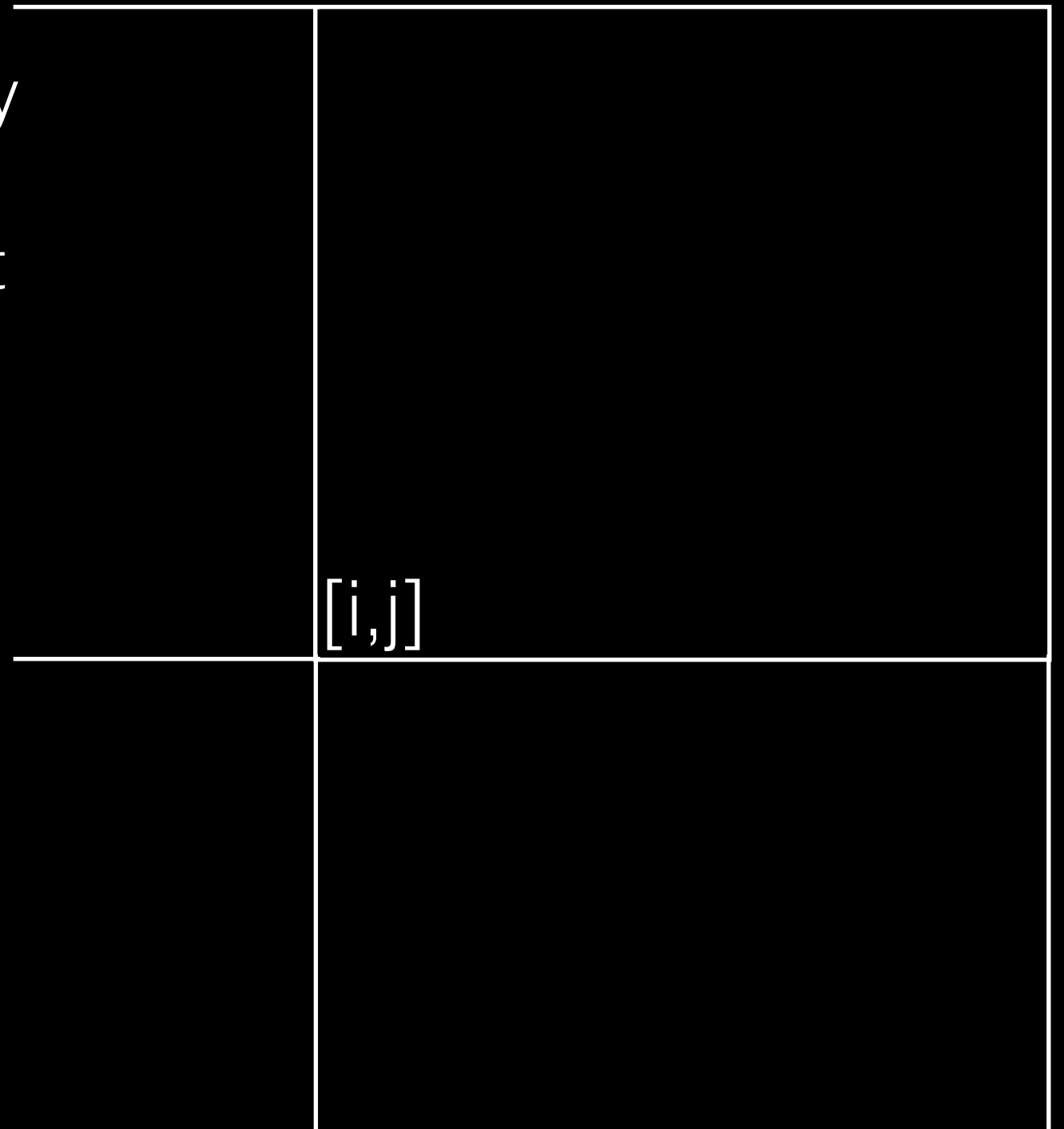


# Beaming



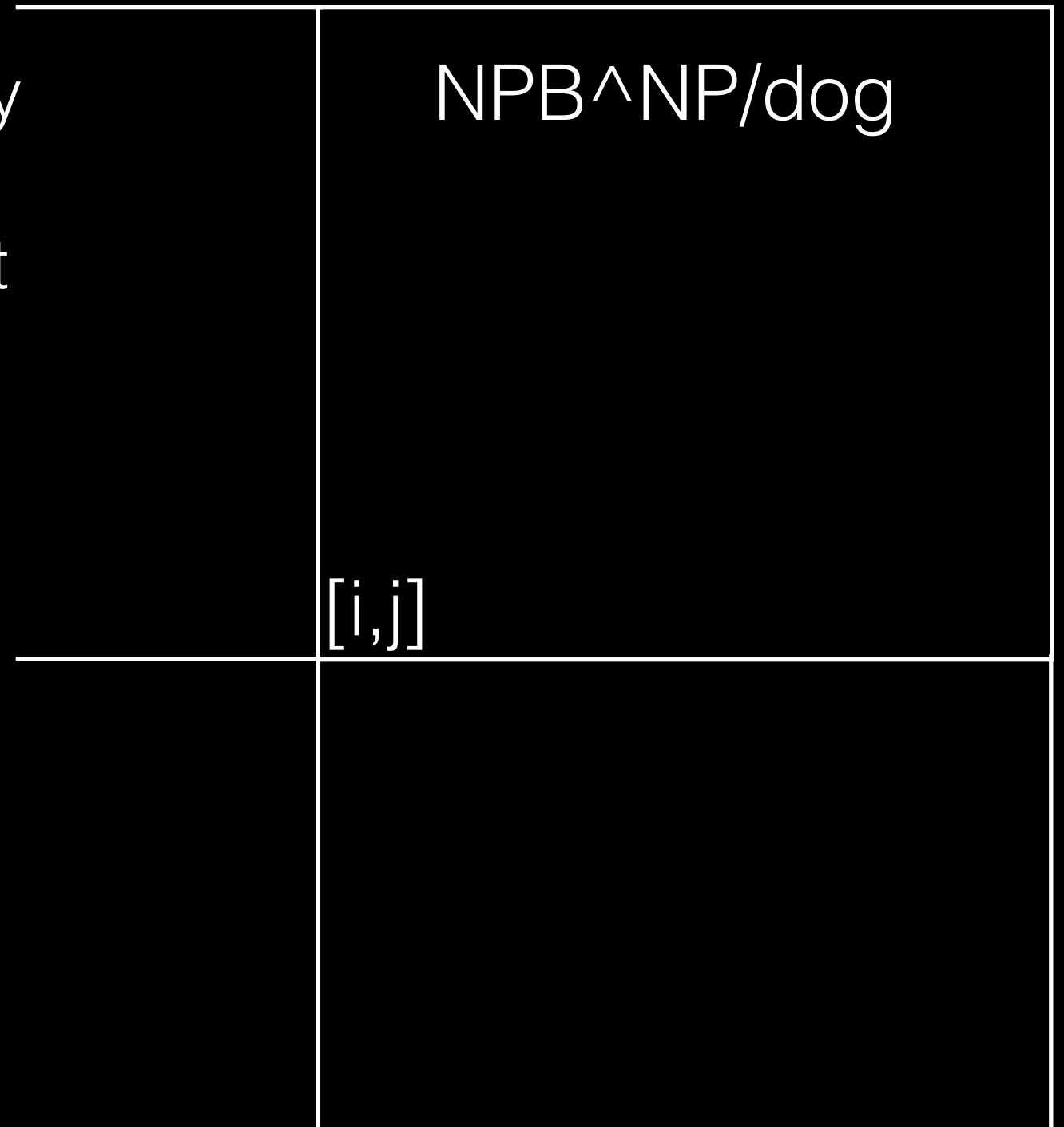
# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart



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	$NPB \wedge NP / \text{dog}$ $NPB \wedge NP / \text{cat}$
	$[i, j]$

# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart

	$NPB \wedge NP / \text{dog}$ $NPB \wedge NP / \text{cat}$ $NP \wedge NP / \text{dog}$
	$[i, j]$

# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart

	$NPB \wedge NP / \text{dog}$ $NPB \wedge NP / \text{cat}$ $NP \wedge NP / \text{dog}$ $NP \wedge NP / \text{cat}$
	$[i, j]$

# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart

	<div>NPB^NP/dog NPB^NP/cat NP^NP/dog NP^NP/cat NP_JJ^NP/cat</div>
	[i,j]

# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart

	<div>NPB^NP/dog NPB^NP/cat NP^NP/dog NP^NP/cat NP_JJ^NP/cat ...</div>
	[i,j]



# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart
- As grammars get more complex, number of states per span can grow

	<div>NPB^NP/dog</div> <div>NPB^NP/cat</div> <div>NP^NP/dog</div> <div>NP^NP/cat</div> <div>NP_JJ^NP/cat</div> <div>[i,j] ...</div>

# Beaming

- Every state that gets created can be potentially combined to form new states higher up the chart
- As grammars get more complex, number of states per span can grow
- Parsing will start to get slow unless something is done

	<div>NPB^NP/dog</div> <div>NPB^NP/cat</div> <div>NP^NP/dog</div> <div>NP^NP/cat</div> <div>NP_JJ^NP/cat</div> <div>[i,j] ...</div>

# Beaming

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- Can cause search errors = best parse found is suboptimal

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- Beam search eliminates part of the chart as it is constructed
- Can cause search errors = best parse found is suboptimal
- Basic idea: Using heuristic score of partial parse, eliminate states

# Beaming

Done		
	NP .00005	
	VP .000093	
Done	S .00034	
	ADVP .0021	
	SQ .0008	
	[i,j]	
Done	Done	Next

# Beaming

- Before moving to  $[i+1, j+1]$ , throw out some states

Done		
	NP .00005	
	VP .000093	
Done	S .00034	
	ADVP .0021	
	SQ .0008	
	$[i,j]$	
Done	Done	Next



# Beaming

- Before moving to  $[i+1, j+1]$ , throw out some states
- Scores are *inside costs* = probability of subtree rooted in X

Done		
	NP .00005	
	VP .000093	
Done	S .00034	
	ADVP .0021	
	SQ .0008	
	$[i,j]$	
Done	Done	Next

# Beaming

- Before moving to  $[i+1, j+1]$ , throw out some states
- Scores are *inside costs* = probability of subtree rooted in  $X$
- We want the state most likely to be used in a *successful* parse

Done		
	NP .00005	
	VP .000093	
Done	S .00034	
	ADVP .0021	
	SQ .0008	
	$[i,j]$	
Done	Done	Next

# Beaming

- Before moving to  $[i+1, j+1]$ , throw out some states
- Scores are *inside costs* = probability of subtree rooted in X
- We want the state most likely to be used in a *successful* parse
- What makes the state likely?

Done		
	NP .00005	
	VP .000093	
Done	S .00034	
	ADVP .0021	
	SQ .0008	
	$[i,j]$	
Done	Done	Next

# Beaming

Done		
Done	ADVP .002 VP .0009 SQ .0008 NP .0005 S .0003 [i,j]	
Done	Done	Next

# Beaming

- Incorporate *heuristic* of completion (note:  $A^*$  search!)

Done		
Done	ADVP .002 VP .0009 SQ .0008 NP .0005 S .0003 [i,j]	
Done	Done	Next

# Beaming

- Incorporate *heuristic* of completion (note:  $A^*$  search!)

Done		
	ADVP .002 x h(ADVP) VP .0009 x h(VP) SQ .0008 x h(SQ) NP .0005 x h(NP) S .0003 x h(S)	
Done	[i,j]	
Done	Done	Next

# Beaming

- Incorporate *heuristic* of completion (note:  $A^*$  search!)
- $p(X)$  = prior probability of seeing  $X$  (count nonterminals in corpus)

Done		
	ADVP .002 x h(ADVP)	
	VP .0009 x h(VP)	
Done	SQ .0008 x h(SQ)	
	NP .0005 x h(NP)	
	S .0003 x h(S)	
	[i,j]	
Done	Done	Next

# Beaming

- Incorporate *heuristic* of completion (note:  $A^*$  search!)
- $p(X)$  = prior probability of seeing  $X$  (count nonterminals in corpus)
- could subdivide by span size ( $p(X|j-i)$ )

Done		
	ADVP .002 x h(ADVP)	
	VP .0009 x h(VP)	
	SQ .0008 x h(SQ)	
Done	NP .0005 x h(NP)	
	S .0003 x h(S)	
	[i,j]	
Done	Done	Next



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	[i,j]	
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Done		
	ADVP .002 x .03 = .00006	
	VP .0009 x .2 = .00018	
	SQ .0008 x .0004 = .00000032	
Done	NP .0005 x .4 = .0002	
	S .0003 x .13 = .00004	
	[i,j]	
Done	Done	Next

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- Incorporate *heuristic* of completion (note:  $A^*$  search!)
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	ADVP .002 x .03 = .00006	
	VP .0009 x .2 = .00018	
	<del>SQ .0008 x .0004 = .00000032</del>	
Done	NP .0005 x .4 = .0002	
	S .0003 x .13 = .00004	
	[i,j]	
Done	Done	Next

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	[i,j]	
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	<del>SQ .0008 x .0004 = .00000032</del>	
Done	NP .0005 x .4 = .0002	
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	[i,j]	
Done	Done	Next

# Summary

# Summary

- PCFG parsing

# Summary

- PCFG parsing
- Estimating Vanilla PCFGs



# Summary

- PCFG parsing
- Estimating Vanilla PCFGs
- Markovization

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- Lexicalization

# Summary

- PCFG parsing
- Estimating Vanilla PCFGs
- Markovization
- Parent Annotation
- Lexicalization
- Head binarization

# Summary

- PCFG parsing
- Estimating Vanilla PCFGs
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- Smoothing rich models

# Summary

- PCFG parsing
- Estimating Vanilla PCFGs
- Markovization
- Parent Annotation
- Lexicalization
- Head binarization
- Smoothing rich models
- Beaming the search