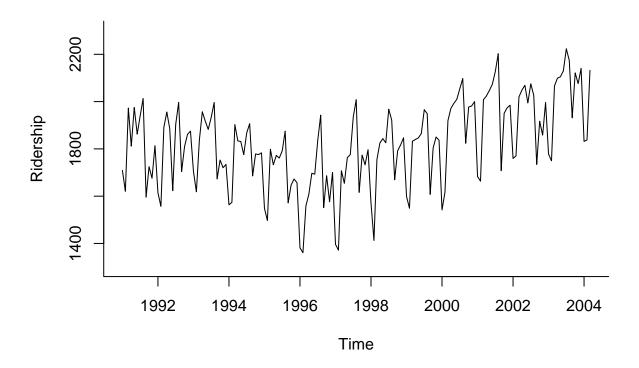
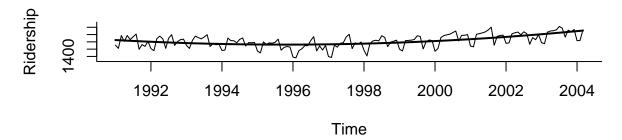
Amtrack Ridership Forecasting

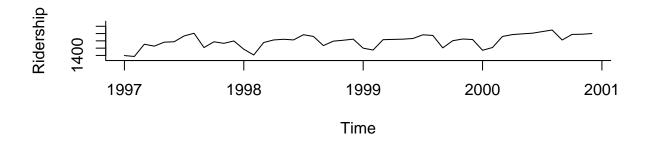


Line plot of Ridership - The dataset

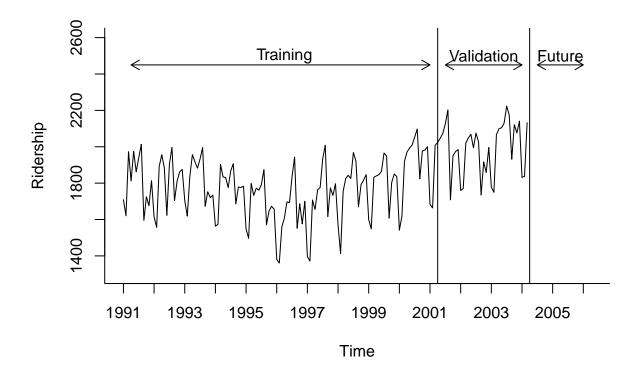
Linear Fitting and Smoothening

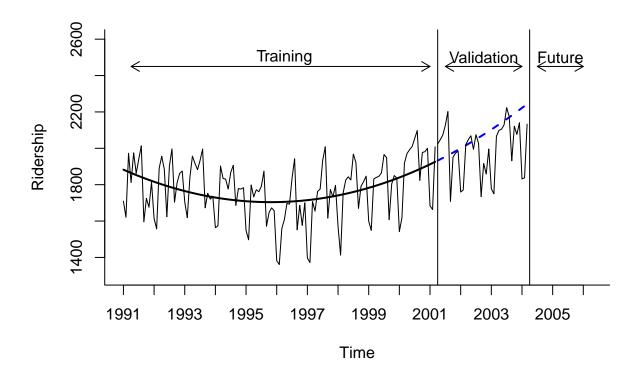
Fitted Trend to Timeseries

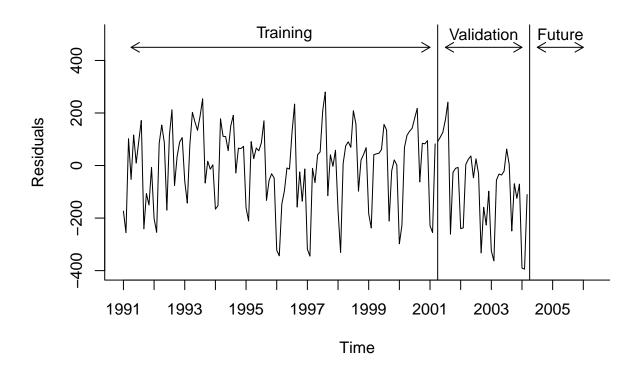


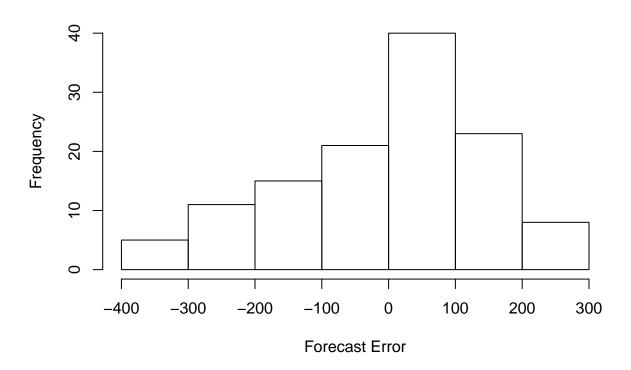


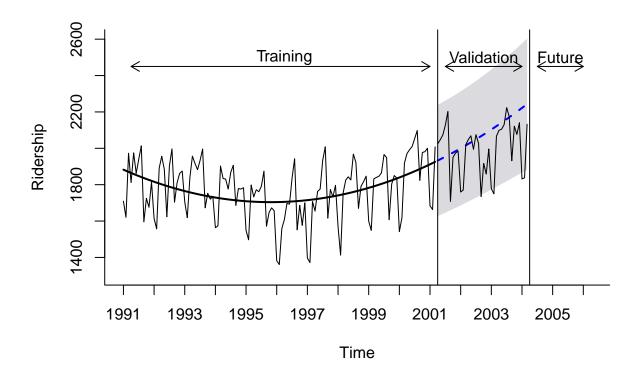
Partitioning

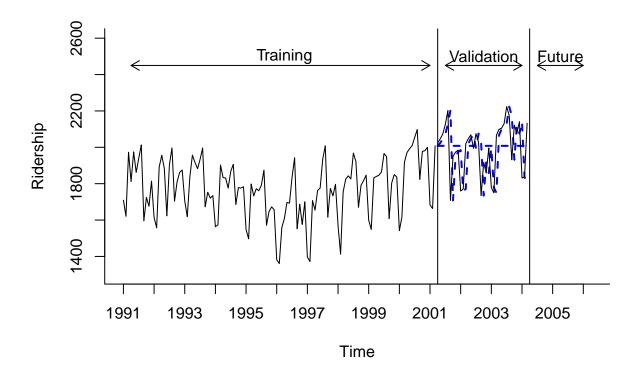




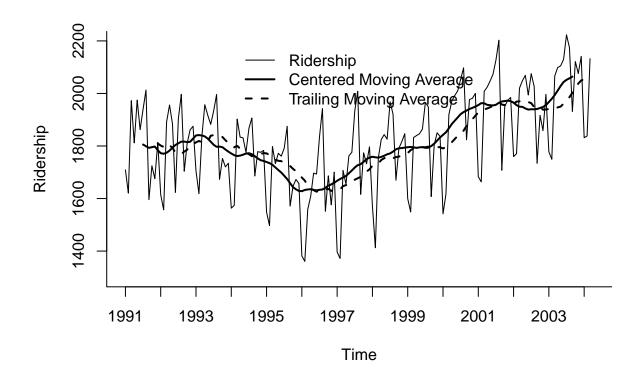


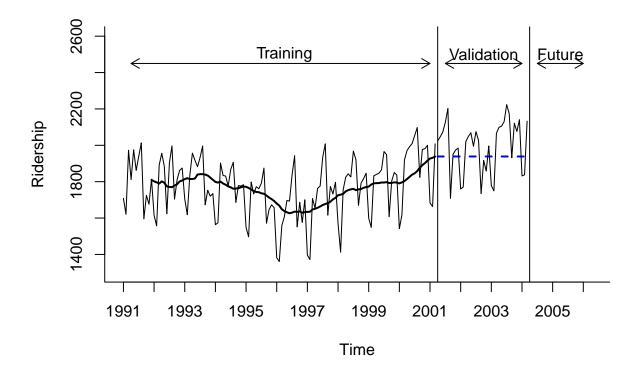


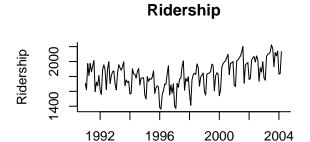




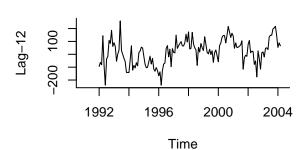
Predictions





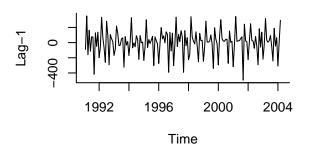


Lag-12 Difference

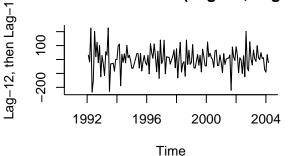




Time



Twice-Differenced (Lag-12, Lag-1)



```
## null device
##
##
## Call:
   tslm(formula = ridership.deseasonalized ~ trend)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    ЗQ
                                            Max
  -241.873 -56.022
                       -0.219
                                59.150
                                        284.792
##
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -40.3641
                           15.0455
                                   -2.683 0.00815 **
                                     4.702 5.93e-06 ***
## trend
                 0.8294
                            0.1764
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 90.74 on 145 degrees of freedom
## Multiple R-squared: 0.1323, Adjusted R-squared: 0.1263
## F-statistic: 22.11 on 1 and 145 DF, p-value: 5.935e-06
```

```
Training
                                                                                                 Future
                                                                                Validation
Ridership (Twice-Differenced)
       200
       100
       0
              1991
                          1993
                                      1995
                                                 1997
                                                             1999
                                                                         2001
                                                                                     2003
                                                                                                2005
                                                           Time
```

```
## null device
##
## ETS(A,N,N)
##
##
##
    ets(y = train.ts, model = "ANN")
##
##
     Smoothing parameters:
##
       alpha = 1e-04
##
##
     Initial states:
       1 = 1.6583
##
##
##
     sigma: 82.8209
##
        AIC
                AICc
                           BIC
##
   1494.723 1494.949 1502.824
##
##
                         ΜE
                                RMSE
                                           MAE
                                                     MPE
                                                             MAPE
                                                                        MASE
## Training set -0.9407425 90.82254 68.01782 181.35457 225.2854 0.6669040
##
   Test set
                  5.7226043 75.99033 54.88964 55.92139 178.3106 0.5381843
##
                       ACF1 Theil's U
## Training set -0.3678952
                                   NA
## Test set
                -0.3665235
                                1.113
                                  RMSE
                                             MAE
                                                      MPE
                                                                         MASE
##
                           ME
                                                               MAPE
## Training set -0.001116552 82.82094 62.90416 100.5652 106.3611 0.6167654
```

```
-2.280828663 75.80886 53.02528 111.5202 111.5202 0.5199045
##
                      ACF1 Theil's U
## Training set -0.3398588
## Test set
               -0.3665235 0.9627726
## Series: train.ts
## ARIMA(1,0,1)(0,0,1)[12] with non-zero mean
## Coefficients:
           ar1
##
                             sma1
                     ma1
                                     mean
##
         0.3850 -0.8181 -0.7545 1.3775
                0.1032
                          0.1100 0.7093
## s.e. 0.1529
##
## sigma^2 estimated as 3894: log likelihood=-614.1
## AIC=1238.2
               AICc=1238.78
                              BIC=1251.7
## ETS(M,N,A)
##
## Call:
##
   ets(y = rts)
##
##
    Smoothing parameters:
##
      alpha = 0.5199
##
      gamma = 1e-04
##
##
    Initial states:
##
      1 = 1811.2158
##
       s=30.8814 -12.3074 -2.7332 -120.1579 203.8979 150.6521
##
              37.2649 74.1158 47.518 36.5746 -245.4989 -200.2075
##
     sigma: 0.0328
##
##
##
        AIC
                AICc
                          BIC
## 1437.803 1442.909 1478.310
   [1] 56.89533 72.41222 47.58071 109.40784 105.01269 70.84465 64.63404
   [8] 65.44567 80.81070 134.14835 132.05848 103.71279 106.18907 107.98966
## [15] 109.53008 110.97033 112.37201 113.75885 115.13997 116.51889 117.89696
## [22] 119.27470 120.65232 122.02989 123.40744 124.78498 126.16252 127.54006
## [29] 128.91760 130.29514 131.67268 133.05022 134.42776 135.80530 137.18284
## [36] 138.56038
  [1] 1971.493 1992.301 2009.763 2053.996 2097.471 1823.706 1976.997
## [8] 1981.408 2000.153 1683.148 1663.404 2007.928 2028.388 2064.713
## [15] 2057.344 2163.404 2202.484 1894.551 2041.631 2046.854 2080.964
## [22] 1817.296 1795.462 2111.641 2134.577 2172.703 2166.874 2274.374
## [29] 2314.856 2008.310 2156.771 2163.373 2198.861 1936.571 1916.115
## [36] 2233.671 2257.985 2297.488 2293.036 2401.914 2443.773 2138.605
## [43] 2288.444 2296.423 2333.288 2072.376 2053.298 2372.231
   [1] 2028.388 2064.713 2057.344 2163.404 2202.484 1894.551 2041.631
## [8] 2046.854 2080.964 1817.296 1795.462 2111.641 2134.577 2172.703
## [15] 2166.874 2274.374 2314.856 2008.310 2156.771 2163.373 2198.861
## [22] 1936.571 1916.115 2233.671 2257.985 2297.488 2293.036 2401.914
## [29] 2443.773 2138.605 2288.444 2296.423 2333.288 2072.376 2053.298
## [36] 2372.231
```

```
##
                          RMSE
                                    MAE
                   ME
                                              MPE
## Test set -152.0855 174.9945 152.959 -7.714254 7.75637
                   1
                                           s2
                                                       s3
                               s1
## Dec 1990 1813.648
                       29.568977
                                   -15.787980
                                                -3.331059
                                                          -140.301977
## Jan 1991 1871.621 -208.468368
                                    29.568977
                                               -15.787980
                                                            -3.331059
## Feb 1991 1868.567 -245.569948 -208.468368
                                                29.568977
                                                           -15.787980
## Mar 1991 1898.002
                       51.477534 -245.569948 -208.468368
                                                            29.568977
## Apr 1991 1812.936
                       65.880755
                                   51.477534 -245.569948 -208.468368
## May 1991 1858.762
                       80.026058
                                    65.880755
                                                51.477534 -245.569948
## Jun 1991 1832.873
                       49.919811
                                    80.026058
                                                65.880755
                                                            51.477534
                                                            65.880755
## Jul 1991 1808.081
                      151.350043
                                    49.919811
                                                80.026058
                      185.237516
## Aug 1991 1819.227
                                  151.350043
                                                49.919811
                                                            80.026058
## Sep 1991 1772.700 -140.313343
                                  185.237516
                                               151.350043
                                                            49.919811
## Oct 1991 1747.865
                       -3.337125 -140.313343
                                               185.237516
                                                           151.350043
## Nov 1991 1716.345
                      -15.795680
                                   -3.337125
                                              -140.313343
                                                           185.237516
                                  -15.795680
## Dec 1991 1754.313
                       29.578252
                                                -3.337125
                                                          -140.313343
## Jan 1992 1792.858 -208.458951
                                    29.578252
                                               -15.795680
                                                            -3.337125
## Feb 1992 1798.334 -245.568610 -208.458951
                                                29.578252
                                                           -15.795680
## Mar 1992 1821.473
                       51.483186 -245.568610 -208.458951
                                                            29.578252
## Apr 1992 1859.820
                       65.890123
                                    51.483186 -245.568610 -208.458951
## May 1992 1829.014
                       80.018533
                                    65.890123
                                                51.483186 -245.568610
## Jun 1992 1686.030
                       49.884881
                                    80.018533
                                                65.890123
                                                            51.483186
## Jul 1992 1722.869
                      151.359043
                                   49.884881
                                                80.018533
                                                            65.890123
## Aug 1992 1772.379
                      185.249611
                                 151.359043
                                                49.884881
                                                            80.018533
## Sep 1992 1812.516 -140.303538
                                  185.249611
                                               151.359043
                                                            49.884881
## Oct 1992 1812.975
                       -3.337013 -140.303538
                                               185.249611
                                                           151.359043
## Nov 1992 1848.972
                      -15.786887
                                    -3.337013 -140.303538
                                                           185.249611
## Dec 1992 1847.056
                       29.577784
                                  -15.786887
                                                -3.337013 -140.303538
## Jan 1993 1884.305 -208.449852
                                    29.577784
                                               -15.786887
                                                            -3.337013
## Feb 1993 1873.017 -245.571368 -208.449852
                                                29.577784
                                                           -15.786887
## Mar 1993 1823.962
                       51.471203 -245.571368 -208.449852
                                                            29.577784
## Apr 1993 1861.506
                       65.899295
                                    51.471203 -245.571368 -208.449852
## May 1993 1847.906
                       80.015210
                                    65.899295
                                                51.471203 -245.571368
## Jun 1993 1839.305
                       49.882780
                                    80.015210
                                                65.899295
                                                            51.471203
## Jul 1993 1807.089
                      151.351173
                                    49.882780
                                                80.015210
                                                            65.899295
## Aug 1993 1809.228
                                                49.882780
                                                            80.015210
                      185.250134
                                  151.351173
## Sep 1993 1811.417 -140.303003
                                  185.250134
                                               151.351173
                                                            49.882780
## Oct 1993 1780.543
                       -3.344556 -140.303003
                                               185.250134
                                                           151.351173
## Nov 1993 1755.745
                      -15.792945
                                    -3.344556 -140.303003
                                                           185.250134
## Dec 1993 1727.231
                       29.570818
                                  -15.792945
                                                -3.344556
                                                          -140.303003
## Jan 1994 1752.143 -208.443766
                                    29.570818
                                               -15.792945
                                                            -3.344556
## Feb 1994 1789.797 -245.562169 -208.443766
                                                29.570818
                                                           -15.792945
## Mar 1994 1824.089
                       51.479580 -245.562169 -208.443766
                                                             29.570818
## Apr 1994 1792.742
                       65.891637
                                    51.479580 -245.562169 -208.443766
## May 1994 1769.437
                       80.009517
                                    65.891637
                                                51.479580 -245.562169
## Jun 1994 1745.094
                       49.876833
                                    80.009517
                                                65.891637
                                                            51.479580
## Jul 1994 1728.925
                      151.347223
                                    49.876833
                                                80.009517
                                                            65.891637
## Aug 1994 1724.697
                      185.249101
                                  151.347223
                                                49.876833
                                                            80.009517
## Sep 1994 1781.265 -140.289184
                                   185.249101
                                               151.347223
                                                            49.876833
## Oct 1994 1781.615
                       -3.344470 -140.289184
                                               185.249101
                                                           151.347223
## Nov 1994 1787.299
                      -15.791556
                                   -3.344470 -140.289184
                                                           185.249101
## Dec 1994 1768.569
                       29.566242
                                  -15.791556
                                                -3.344470 -140.289184
## Jan 1995 1762.026 -208.445365
                                   29.566242 -15.791556
                                                            -3.344470
```

```
## Feb 1995 1751.108 -245.564836 -208.445365
                                                 29.566242
                                                            -15.791556
## Mar 1995 1748.721
                       51.478997 -245.564836 -208.445365
                                                             29.566242
## Apr 1995 1703.060
                        65.880482
                                    51.478997 -245.564836 -208.445365
## May 1995 1697.067
                       80.008053
                                    65.880482
                                                51.478997 -245.564836
## Jun 1995 1705.037
                       49.878780
                                    80.008053
                                                 65.880482
                                                             51.478997
## Jul 1995 1668.868
                                    49.878780
                                                 80.008053
                                                             65.880482
                      151.338387
## Aug 1995 1680.436
                       185.251927
                                   151.338387
                                                 49.878780
                                                             80.008053
## Sep 1995 1697.849 -140.284930
                                   185.251927
                                               151.338387
                                                             49.878780
## Oct 1995 1671.276
                       -3.350962 -140.284930
                                               185.251927
                                                            151.338387
## Nov 1995 1680.857
                      -15.789215
                                    -3.350962
                                              -140.284930
                                                            185.251927
## Dec 1995 1650.919
                        29.558929
                                   -15.789215
                                                 -3.350962
                                                           -140.284930
## Jan 1996 1616.993 -208.453652
                                    29.558929
                                               -15.789215
                                                             -3.350962
## Feb 1996 1611.083 -245.566280 -208.453652
                                                 29.558929
                                                            -15.789215
## Mar 1996 1552.979
                        51.464802 -245.566280 -208.453652
                                                             29.558929
## Apr 1996 1547.146
                        65.879057
                                    51.464802 -245.566280 -208.453652
## May 1996 1586.004
                       80.017546
                                    65.879057
                                                 51.464802 -245.566280
## Jun 1996 1618.021
                        49.886602
                                                 65.879057
                                    80.017546
                                                             51.464802
## Jul 1996 1654.987
                       151.347418
                                                             65.879057
                                    49.886602
                                                 80.017546
## Aug 1996 1712.168
                      185.265895
                                   151.347418
                                                 49.886602
                                                             80.017546
## Sep 1996 1700.723
                     -140.287726
                                   185.265895
                                               151.347418
                                                             49.886602
## Oct 1996 1694.653
                       -3.352445
                                  -140.287726
                                               185.265895
                                                            151.347418
## Nov 1996 1637.290
                       -15.803229
                                    -3.352445
                                              -140.287726
                                                            185.265895
## Dec 1996 1656.056
                                   -15.803229
                        29.563513
                                                 -3.352445
                                                           -140.287726
## Jan 1997 1627.551 -208.460616
                                    29.563513
                                               -15.803229
                                                             -3.352445
## Feb 1997 1621.799 -245.567685 -208.460616
                                                 29.563513
                                                            -15.803229
## Mar 1997 1640.941
                       51.469479 -245.567685 -208.460616
                                                             29.563513
## Apr 1997 1611.764
                        65.871929
                                    51.469479
                                              -245.567685
                                                           -208.460616
## May 1997 1651.505
                       80.027254
                                    65.871929
                                                 51.469479
                                                          -245.567685
## Jun 1997 1693.082
                        49.896759
                                    80.027254
                                                 65.871929
                                                             51.469479
## Jul 1997 1743.253
                                    49.896759
                                                             65.871929
                       151.359674
                                                 80.027254
## Aug 1997 1787.695
                       185.276752
                                   151.359674
                                                 49.896759
                                                             80.027254
## Sep 1997 1770.103 -140.292024
                                   185.276752
                                               151.359674
                                                             49.896759
## Oct 1997 1774.104
                        -3.351468
                                  -140.292024
                                                185.276752
                                                            151.359674
## Nov 1997 1759.613
                       -15.806768
                                    -3.351468
                                               -140.292024
                                                            185.276752
## Dec 1997 1763.776
                        29.564530
                                   -15.806768
                                                 -3.351468
                                                            -140.292024
## Jan 1998 1772.166 -208.458566
                                    29.564530
                                               -15.806768
                                                             -3.351468
## Feb 1998 1708.518 -245.583234 -208.458566
                                                 29.564530
                                                            -15.806768
## Mar 1998 1705.531
                       51.468749 -245.583234 -208.458566
                                                             29.564530
## Apr 1998 1735.441
                        65.879236
                                    51.468749 -245.583234 -208.458566
## May 1998 1750.986
                        80.031052
                                    65.879236
                                                 51.468749
                                                           -245.583234
## Jun 1998 1765.001
                       49.900183
                                    80.031052
                                                 65.879236
                                                             51.468749
## Jul 1998 1793.951
                       151.366747
                                    49.900183
                                                 80.031052
                                                             65.879236
## Aug 1998 1761.776
                      185.268892
                                   151.366747
                                                 49.900183
                                                             80.031052
## Sep 1998 1788.660 -140.285456
                                   185.268892
                                               151.366747
                                                             49.900183
## Oct 1998 1792.105
                        -3.350626 -140.285456
                                               185.268892
                                                            151.366747
## Nov 1998 1814.688
                      -15.801252
                                    -3.350626
                                              -140.285456
                                                            185.268892
## Dec 1998 1816.086
                       29.564871
                                   -15.801252
                                                 -3.350626 -140.285456
## Jan 1999 1811.504 -208.459686
                                    29.564871
                                               -15.801252
                                                             -3.350626
## Feb 1999 1801.940 -245.585570 -208.459686
                                                 29.564871
                                                            -15.801252
## Mar 1999 1790.163
                       51.465872 -245.585570 -208.459686
                                                             29.564871
## Apr 1999 1781.043
                        65.877008
                                    51.465872 -245.585570 -208.459686
## May 1999 1772.898
                       80.029062
                                    65.877008
                                                 51.465872 -245.585570
## Jun 1999 1796.396
                        49.905923
                                    80.029062
                                                 65.877008
                                                             51.465872
## Jul 1999 1806.443 151.369201
                                    49.905923
                                                80.029062
                                                             65.877008
```

```
## Aug 1999 1782.578 185.263062 151.369201
                                                49.905923
                                                             80.029062
## Sep 1999 1763.066 -140.290223
                                                             49.905923
                                  185.263062
                                               151.369201
## Oct 1999 1787.623
                       -3.344627 -140.290223
                                               185.263062
                                                            151.369201
## Nov 1999 1831.479
                      -15.790538
                                    -3.344627 -140.290223
                                                            185.263062
## Dec 1999 1817.728
                       29.561512
                                   -15.790538
                                                -3.344627
                                                           -140.290223
## Jan 2000 1779.951 -208.468915
                                    29.561512
                                               -15.790538
                                                             -3.344627
                                                29.561512
                                                            -15.790538
## Feb 2000 1826.084 -245.574300 -208.468915
## Mar 2000 1849.546
                       51.471603 -245.574300 -208.468915
                                                             29.561512
## Apr 2000 1880.876
                       65.884662
                                    51.471603 -245.574300 -208.468915
## May 2000 1898.419
                       80.033348
                                    65.884662
                                                51.471603 -245.574300
## Jun 2000 1932.749
                       49.914310
                                    80.033348
                                                65.884662
                                                             51.471603
## Jul 2000 1915.918
                      151.365089
                                    49.914310
                                                80.033348
                                                             65.884662
## Aug 2000 1913.845
                      185.262556
                                   151.365089
                                                49.914310
                                                             80.033348
                                               151.365089
## Sep 2000 1941.868
                     -140.283377
                                   185.262556
                                                             49.914310
## Oct 2000 1963.366
                       -3.339375 -140.283377
                                               185.262556
                                                            151.365089
## Nov 2000 1982.270
                      -15.785920
                                    -3.339375
                                              -140.283377
                                                            185.262556
## Dec 2000 1975.745
                       29.559918
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## Jul 2002
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## Aug 2002
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## Sep 2002
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## Nov 2002
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## Sep 2003
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## Nov 2003
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## Dec 2003
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## Jan 2004 -140.299207
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## Feb 2004
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## Mar 1991
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## Apr 1991
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## May 1991
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## Jul 1997
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## Jul 2003
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## Sep 2003
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## Nov 2003 -245.565467 -208.471780
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## Dec 2003
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## Jan 2004
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                           51.478186 -245.565467
## Feb 2004
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                           65.892146
                                       51.478186
## Mar 2004
              49.925277
                           80.037625
                                       65.892146
```

```
Ridership Walidation Future 1991 1993 1995 1997 1999 2001 2003 2005

Time
```

```
## ETS(M,A,A)
##
## Call:
##
    ets(y = train.ts, model = "MAA")
##
##
     Smoothing parameters:
       alpha = 0.5483
##
##
       beta = 1e-04
##
       gamma = 1e-04
##
##
     Initial states:
##
       1 = 1881.6423
##
       b = 0.4164
##
       s=27.1143 -10.6847 -2.9465 -121.1763 201.1625 147.3359
              37.6688 75.8711 60.4021 44.4779 -252.047 -207.1783
##
##
##
     sigma: 0.0317
##
##
        AIC
                 AICc
                           BIC
   1616.219 1622.048 1664.027
##
##
              1
                            b
                                                       s2
                                                                     s3
                                         s1
##
  1881.6422674
                    0.4164294
                                 27.1143232
                                             -10.6847219
                                                            -2.9464535
##
             s4
                           ธ5
                                         s6
                                                       s7
                                                                     s8
##
   -121.1762908
                  201.1625434
                                147.3359163
                                              37.6688093
                                                            75.8711436
##
                          s10
             s9
                                        s11
                                                      s12
##
     60.4021324
                   44.4778868 -252.0469570 -207.1783318
```

```
b
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                                        s1
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                   0.4191293
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##
             s4
                          s5
                                        s6
                                                     s7
##
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##
             s9
                         s10
                                       s11
                                                    s12
##
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##
                             b
                                                     s2
                                                                 s3
                   1
                                         s1
## Dec 1990 1881.642 0.4164294
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## Jan 1991 1900.721 0.4198334 -207.174926
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## Mar 1991 1909.126 0.4212138
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## Apr 1991 1822.760 0.4053837
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## May 1991 1864.796 0.4129773
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## Jun 1991 1842.991 0.4089247
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## Jul 1991 1815.505 0.4038365
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## Aug 1991 1813.821 0.4034558
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## Sep 1991 1760.825 0.3937156 -121.186036
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## Oct 1991 1742.934 0.3903804
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## Dec 1991 1753.197 0.3921111
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## Jan 1992 1791.100 0.3989531 -207.168081
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```
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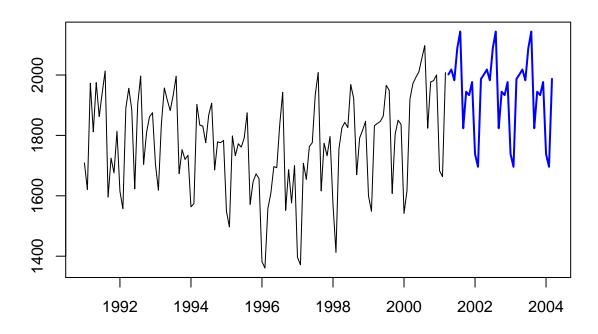
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                                      147.340338
                                                    37.660037
                                                                75.879318
## Jan 2000
              -2.945352 -121.179974
                                      201.162722
                                                   147.340338
                                                                37.660037
## Feb 2000
             -10.686305
                           -2.945352 -121.179974
                                                   201.162722
                                                               147.340338
## Mar 2000
              27.115419
                          -10.686305
                                       -2.945352
                                                  -121.179974
                                                               201.162722
## Apr 2000 -207.176137
                           27.115419
                                      -10.686305
                                                    -2.945352 -121.179974
## May 2000 -252.046726 -207.176137
                                       27.115419
                                                   -10.686305
                                                                -2.945352
## Jun 2000
              44.480688 -252.046726 -207.176137
                                                    27.115419
                                                               -10.686305
## Jul 2000
              60.388730
                           44.480688 -252.046726
                                                 -207.176137
                                                                27.115419
## Aug 2000
              75.882356
                           60.388730
                                       44.480688
                                                              -207.176137
                                                  -252.046726
## Sep 2000
              37.666939
                           75.882356
                                       60.388730
                                                    44.480688
                                                              -252.046726
## Oct 2000
             147.336865
                           37.666939
                                       75.882356
                                                    60.388730
                                                                44.480688
## Nov 2000
             201.160076
                          147.336865
                                       37.666939
                                                    75.882356
                                                                60.388730
## Dec 2000 -121.176350
                          201.160076
                                      147.336865
                                                    37.666939
                                                                75.882356
              -2.940249 -121.176350
## Jan 2001
                                      201.160076
                                                   147.336865
                                                                37.666939
## Feb 2001
             -10.682826
                           -2.940249 -121.176350
                                                   201.160076
                                                               147.336865
## Mar 2001
              27.115041
                          -10.682826
                                       -2.940249
                                                 -121.176350
                                                               201.160076
##
                     s9
                                 s10
                                              s11
                                                          s12
## Dec 1990
              60.402132
                           44.477887 -252.046957 -207.178332
## Jan 1991
              75.871144
                           60.402132
                                       44.477887 -252.046957
## Feb 1991
              37.668809
                           75.871144
                                       60.402132
                                                    44.477887
             147.335916
## Mar 1991
                           37.668809
                                       75.871144
                                                    60.402132
## Apr 1991
             201.162543
                          147.335916
                                       37.668809
                                                    75.871144
## May 1991 -121.176291
                          201.162543
                                      147.335916
                                                    37.668809
## Jun 1991
              -2.946453 -121.176291
                                      201.162543
                                                   147.335916
## Jul 1991
             -10.684722
                           -2.946453
                                     -121.176291
                                                   201.162543
                                       -2.946453
## Aug 1991
              27.114323
                          -10.684722
                                                  -121.176291
## Sep 1991 -207.174926
                           27.114323
                                      -10.684722
                                                    -2.946453
## Oct 1991 -252.049810 -207.174926
                                       27.114323
                                                   -10.684722
## Nov 1991
              44.482120 -252.049810 -207.174926
                                                    27.114323
```

```
## Dec 1991
              60.386294
                           44.482120 -252.049810 -207.174926
                                       44.482120 -252.049810
## Jan 1992
              75.878741
                           60.386294
## Feb 1992
              37.664755
                           75.878741
                                       60.386294
                                                    44.482120
## Mar 1992
             147.330826
                           37.664755
                                       75.878741
                                                   60.386294
## Apr 1992
             201.162162
                         147.330826
                                       37.664755
                                                   75.878741
## May 1992 -121.186036
                         201.162162
                                      147.330826
                                                   37.664755
## Jun 1992
              -2.949790 -121.186036
                                      201.162162
                                                   147.330826
                           -2.949790 -121.186036
## Jul 1992
             -10.690423
                                                   201.162162
## Aug 1992
              27.121756
                         -10.690423
                                       -2.949790 -121.186036
## Sep 1992 -207.168081
                           27.121756
                                      -10.690423
                                                    -2.949790
## Oct 1992 -252.048045 -207.168081
                                       27.121756
                                                  -10.690423
## Nov 1992
              44.486640 -252.048045 -207.168081
                                                    27.121756
## Dec 1992
              60.393184
                          44.486640 -252.048045 -207.168081
## Jan 1993
              75.873131
                           60.393184
                                       44.486640 -252.048045
## Feb 1993
              37.639820
                          75.873131
                                       60.393184
                                                    44.486640
## Mar 1993
             147.336595
                           37.639820
                                       75.873131
                                                   60.393184
## Apr 1993
                         147.336595
             201.168689
                                       37.639820
                                                   75.873131
## May 1993 -121.180172
                         201.168689
                                      147.336595
                                                   37.639820
## Jun 1993
              -2.948396 -121.180172
                                      201.168689
                                                   147.336595
## Jul 1993
             -10.683895
                           -2.948396 -121.180172
                                                   201.168689
## Aug 1993
              27.122233
                         -10.683895
                                       -2.948396
                                                 -121.180172
                                      -10.683895
                                                    -2.948396
## Sep 1993 -207.161459
                           27.122233
## Oct 1993 -252.049282 -207.161459
                                       27.122233
                                                   -10.683895
## Nov 1993
              44.478199 -252.049282 -207.161459
                                                    27.122233
## Dec 1993
              60.399779
                           44.478199 -252.049282 -207.161459
## Jan 1994
              75.870531
                           60.399779
                                       44.478199 -252.049282
                          75.870531
## Feb 1994
              37.638950
                                       60.399779
                                                   44.478199
## Mar 1994
             147.330249
                          37.638950
                                       75.870531
                                                   60.399779
## Apr 1994
             201.166716
                         147.330249
                                       37.638950
                                                   75.870531
## May 1994 -121.181201
                         201.166716
                                      147.330249
                                                   37.638950
## Jun 1994
              -2.952727 -121.181201
                                      201.166716
                                                   147.330249
## Jul 1994
             -10.688364
                           -2.952727 -121.181201
                                                   201.166716
## Aug 1994
              27.117784
                         -10.688364
                                       -2.952727
                                                 -121.181201
## Sep 1994 -207.157168
                           27.117784
                                      -10.688364
                                                    -2.952727
## Oct 1994 -252.041831 -207.157168
                                                   -10.688364
                                       27.117784
## Nov 1994
              44.484742 -252.041831 -207.157168
                                                   27.117784
## Dec 1994
              60.394222
                           44.484742 -252.041831 -207.157168
## Jan 1995
              75.866149
                                       44.484742 -252.041831
                           60.394222
              37.635224
## Feb 1995
                           75.866149
                                                   44.484742
                                       60.394222
## Mar 1995
             147.326732
                           37.635224
                                       75.866149
                                                   60.394222
## Apr 1995
             201.163614
                         147.326732
                                       37.635224
                                                   75.866149
## May 1995 -121.172497
                         201.163614
                                      147.326732
                                                   37.635224
## Jun 1995
              -2.951368 -121.172497
                                      201.163614
                                                   147.326732
## Jul 1995
             -10.687271
                          -2.951368 -121.172497
                                                   201.163614
## Aug 1995
              27.115192
                         -10.687271
                                       -2.951368 -121.172497
## Sep 1995 -207.158444
                           27.115192
                                      -10.687271
                                                   -2.951368
                                                  -10.687271
## Oct 1995 -252.043108 -207.158444
                                       27.115192
## Nov 1995
              44.484613 -252.043108 -207.158444
                                                    27.115192
## Dec 1995
              60.385987
                           44.484613 -252.043108 -207.158444
## Jan 1996
              75.864790
                           60.385987
                                       44.484613 -252.043108
                          75.864790
## Feb 1996
              37.637283
                                       60.385987
                                                    44.484613
## Mar 1996
             147.319695
                           37.637283
                                       75.864790
                                                   60.385987
## Apr 1996
             201.163332
                         147.319695
                                       37.637283
                                                   75.864790
## May 1996 -121.170778
                         201.163332 147.319695
                                                   37.637283
```

```
## Jun 1996
              -2.954890 -121.170778 201.163332
                                                   147.319695
## Jul 1996
             -10.685555
                           -2.954890 -121.170778
                                                   201.163332
## Aug 1996
              27.110567
                          -10.685555
                                        -2.954890
                                                  -121.170778
## Sep 1996 -207.164654
                           27.110567
                                      -10.685555
                                                    -2.954890
## Oct 1996 -252.043550 -207.164654
                                       27.110567
                                                   -10.685555
## Nov 1996
              44.474491 -252.043550 -207.164654
                                                    27.110567
## Dec 1996
              60.384776
                           44.474491 -252.043550 -207.164654
## Jan 1997
              75.871492
                           60.384776
                                       44.474491 -252.043550
## Feb 1997
              37.643748
                           75.871492
                                       60.384776
                                                    44.474491
## Mar 1997
             147.325845
                           37.643748
                                       75.871492
                                                    60.384776
## Apr 1997
             201.171398
                          147.325845
                                        37.643748
                                                    75.871492
## May 1997 -121.174061
                          201.171398
                                      147.325845
                                                    37.643748
## Jun 1997
              -2.954720 -121.174061
                                      201.171398
                                                   147.325845
## Jul 1997
             -10.695780
                           -2.954720
                                     -121.174061
                                                   201.171398
## Aug 1997
              27.114561
                          -10.695780
                                        -2.954720
                                                  -121.174061
## Sep 1997 -207.169848
                           27.114561
                                      -10.695780
                                                    -2.954720
                                                   -10.695780
## Oct 1997 -252.043933 -207.169848
                                       27.114561
              44.478215 -252.043933 -207.169848
                                                    27.114561
## Nov 1997
## Dec 1997
              60.379534
                           44.478215 -252.043933
                                                  -207.169848
## Jan 1998
              75.878375
                           60.379534
                                       44.478215
                                                  -252.043933
## Feb 1998
              37.651936
                           75.878375
                                       60.379534
                                                    44.478215
## Mar 1998
             147.334383
                           37.651936
                                       75.878375
                                                    60.379534
## Apr 1998
             201.177216
                          147.334383
                                       37.651936
                                                    75.878375
## May 1998 -121.178455
                          201.177216
                                      147.334383
                                                    37.651936
## Jun 1998
              -2.952765
                        -121.178455
                                      201.177216
                                                   147.334383
## Jul 1998
             -10.698318
                           -2.952765
                                     -121.178455
                                                   201.177216
## Aug 1998
              27.116022
                          -10.698318
                                       -2.952765
                                                  -121.178455
## Sep 1998 -207.168428
                           27.116022
                                      -10.698318
                                                    -2.952765
## Oct 1998 -252.054614 -207.168428
                                        27.116022
                                                   -10.698318
## Nov 1998
              44.477898 -252.054614 -207.168428
                                                    27.116022
## Dec 1998
              60.384795
                           44.477898 -252.054614 -207.168428
## Jan 1999
              75.880999
                           60.384795
                                       44.477898 -252.054614
## Feb 1999
              37.655173
                           75.880999
                                        60.384795
                                                    44.477898
## Mar 1999
             147.339061
                           37.655173
                                       75.880999
                                                    60.384795
## Apr 1999
                          147.339061
                                                    75.880999
             201.169246
                                       37.655173
## May 1999 -121.175059
                          201.169246
                                      147.339061
                                                    37.655173
## Jun 1999
              -2.950905
                        -121.175059
                                      201.169246
                                                   147.339061
## Jul 1999
             -10.694216
                           -2.950905 -121.175059
                                                   201.169246
                          -10.694216
## Aug 1999
              27.117057
                                       -2.950905 -121.175059
## Sep 1999 -207.169305
                           27.117057
                                      -10.694216
                                                    -2.950905
## Oct 1999 -252.055624 -207.169305
                                        27.117057
                                                   -10.694216
## Nov 1999
              44.476101 -252.055624 -207.169305
                                                    27.117057
## Dec 1999
              60.383091
                           44.476101 -252.055624 -207.169305
              75.879318
## Jan 2000
                           60.383091
                                       44.476101 -252.055624
## Feb 2000
              37.660037
                           75.879318
                                        60.383091
                                                    44.476101
             147.340338
## Mar 2000
                           37.660037
                                       75.879318
                                                    60.383091
## Apr 2000
             201.162722
                          147.340338
                                        37.660037
                                                    75.879318
## May 2000 -121.179974
                          201.162722
                                      147.340338
                                                    37.660037
## Jun 2000
              -2.945352 -121.179974
                                      201.162722
                                                   147.340338
## Jul 2000
             -10.686305
                           -2.945352
                                     -121.179974
                                                   201.162722
## Aug 2000
                          -10.686305
              27.115419
                                       -2.945352
                                                  -121.179974
## Sep 2000 -207.176137
                           27.115419
                                      -10.686305
                                                    -2.945352
## Oct 2000 -252.046726 -207.176137
                                       27.115419
                                                   -10.686305
## Nov 2000
              44.480688 -252.046726 -207.176137
                                                    27.115419
```

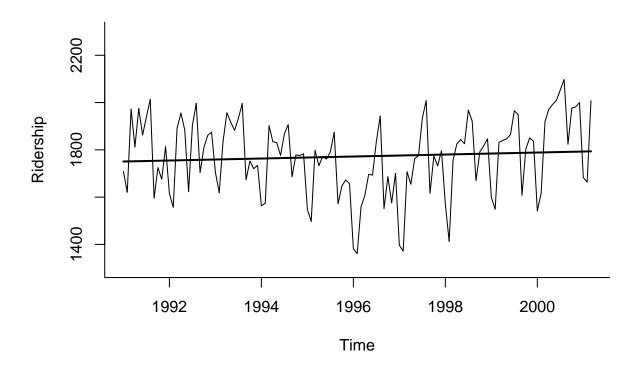
```
## Dec 2000
              60.388730
                          44.480688 -252.046726 -207.176137
## Jan 2001
             75.882356
                          60.388730
                                      44.480688 -252.046726
## Feb 2001
              37.666939
                          75.882356
                                      60.388730
                                                  44.480688
## Mar 2001 147.336865
                          37.666939
                                      75.882356
                                                  60.388730
```

Forecasts from ETS(M,N,A)



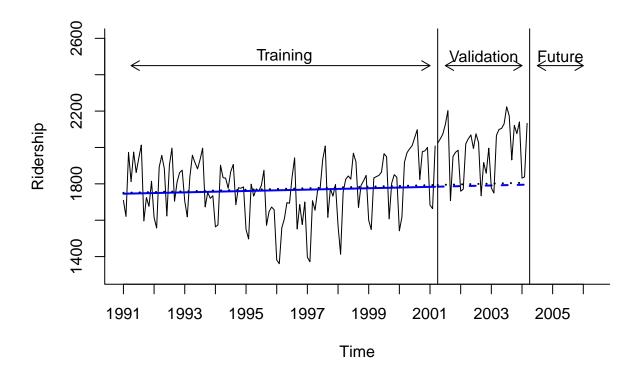
```
RMSE
##
                       ME
                                        MAE
                                                    MPE
                                                            MAPE
                                                                      MASE
## Training set 0.219486 56.24056 44.98047 -0.07430418 2.564691 0.5452709
                40.723759 82.11922 67.52209 1.93604797 3.388343 0.8185293
## Test set
                      ACF1 Theil's U
## Training set 0.06506553
## Test set
                0.62663295 0.4755131
                       ME
                              RMSE
                                        MAE
                                                   MPE
                                                           MAPE
                                                                     MASE
## Training set 1.947578 56.88865 45.33644 0.02337148 2.582187 0.5495861
## Test set
                48.667558 88.01624 73.05445 2.33048701 3.656759 0.8855948
##
                      ACF1 Theil's U
## Training set 0.05514443
                0.65275454 0.5098143
## Test set
```

Smoothening



```
##
## Call:
## tslm(formula = train.ts ~ trend)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
                    16.06 129.28 306.35
## -411.29 -114.02
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1750.3595
                           29.0729 60.206
                                            <2e-16 ***
                                     0.864
                                               0.39
## trend
                 0.3514
                            0.4069
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 160.2 on 121 degrees of freedom
## Multiple R-squared: 0.006125, Adjusted R-squared: -0.002089
## F-statistic: 0.7456 on 1 and 121 DF, p-value: 0.3896
```

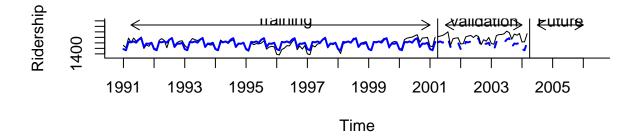
Box-Cox Transformation

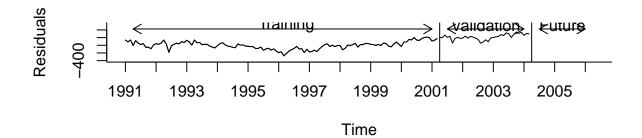


```
Feb
##
             Jan
                               Mar
                                                           Jun
                                                                    Jul
                                        Apr
                                                 May
## 1991 7.443615 7.390543 7.587166 7.502002 7.588305 7.529598 7.570371
## 1992 7.386983 7.350573 7.544979 7.578647 7.541531 7.392057 7.551349
## 1993 7.441472 7.389277 7.515731 7.579190 7.558613 7.540302 7.566833
## 1994 7.354596 7.361349 7.550997 7.514194 7.512644 7.481981 7.532360
## 1995 7.344987 7.311168 7.494606 7.457549 7.480059 7.473755 7.490895
## 1996 7.231112 7.215866 7.351527 7.383008 7.436438 7.434365 7.515081
## 1997 7.241787 7.223799 7.442798 7.411317 7.474717 7.482006 7.567459
## 1998 7.359041 7.253252 7.470020 7.509298 7.519307 7.509863 7.584860
## 1999 7.377401 7.345238 7.513345 7.517369 7.521046 7.530937 7.583626
## 2000 7.340615 7.388283 7.559840 7.586546 7.597046 7.605772 7.627542
## 2001 7.428421 7.416621 7.604859
##
             Aug
                      Sep
                               Oct
                                        Nov
## 1991 7.607513 7.375041 7.452938 7.423967 7.503214
## 1992 7.599257 7.440673 7.501082 7.529192 7.536429
## 1993 7.598984 7.422279 7.468985 7.450299 7.458355
## 1994 7.553081 7.429896 7.483551 7.482116 7.486249
## 1995 7.536268 7.359664 7.406679 7.422153 7.412670
## 1996 7.571769 7.346914 7.430415 7.362775 7.438638
## 1997 7.604922 7.387662 7.480941 7.457245 7.493666
## 1998 7.560937 7.420338 7.490794 7.504785 7.521185
## 1999 7.575073 7.382356 7.497575 7.523108 7.515581
## 2000 7.648488 7.508626 7.589334 7.591563 7.600979
## 2001
```

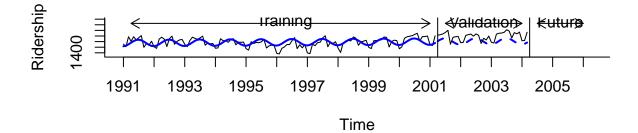
Smoothening with various Permuations of Interaction Terms

```
## Call:
## tslm(formula = train.ts ~ trend + I(trend^2))
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -344.79 -101.86
                    40.89
                            98.54
                                   279.81
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1888.88401
                          40.91521 46.166 < 2e-16 ***
## trend
                -6.29780
                            1.52327 -4.134 6.63e-05 ***
## I(trend^2)
                 0.05362
                            0.01190
                                      4.506 1.55e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 148.8 on 120 degrees of freedom
## Multiple R-squared: 0.1499, Adjusted R-squared: 0.1358
## F-statistic: 10.58 on 2 and 120 DF, p-value: 5.844e-05
##
## Call:
## tslm(formula = train.ts ~ season)
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
## -276.165 -52.934
                       5.868
                               54.544
                                      215.081
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                            30.58 51.475 < 2e-16 ***
## (Intercept) 1573.97
## season2
                -42.93
                            43.24 -0.993
                                            0.3230
                260.77
                            43.24
                                   6.030 2.19e-08 ***
## season3
## season4
                245.09
                            44.31
                                   5.531 2.14e-07 ***
## season5
                278.22
                            44.31 6.279 6.81e-09 ***
## season6
                233.46
                            44.31 5.269 6.82e-07 ***
## season7
                345.33
                            44.31
                                   7.793 3.79e-12 ***
## season8
                396.66
                            44.31
                                  8.952 9.19e-15 ***
## season9
                 75.76
                            44.31
                                   1.710 0.0901 .
                            44.31 4.527 1.51e-05 ***
## season10
                200.61
## season11
                192.36
                            44.31 4.341 3.14e-05 ***
## season12
                230.42
                            44.31 5.200 9.18e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 101.4 on 111 degrees of freedom
## Multiple R-squared: 0.6348, Adjusted R-squared: 0.5986
## F-statistic: 17.54 on 11 and 111 DF, p-value: < 2.2e-16
```





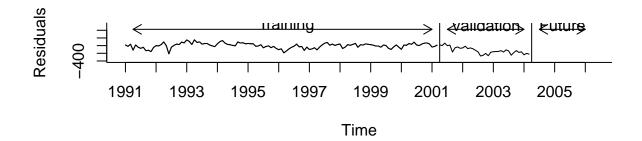
```
##
## Call:
## tslm(formula = train.ts ~ trend + I(sin(2 * pi * trend/12)) +
       I(cos(2 * pi * trend/12)))
##
##
## Residuals:
##
       Min
                1Q
                    Median
                                       Max
   -318.34
           -96.30
                      8.04
                             89.73
                                   307.89
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
                                                   69.788 < 2e-16 ***
## (Intercept)
                             1748.0335
                                          25.0477
## trend
                                0.4229
                                           0.3507
                                                    1.206 0.23015
## I(sin(2 * pi * trend/12)) -48.2666
                                          17.5260
                                                   -2.754 0.00681 **
## I(cos(2 * pi * trend/12)) -106.5245
                                          17.6773
                                                   -6.026 1.93e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 137.9 on 119 degrees of freedom
## Multiple R-squared: 0.2762, Adjusted R-squared: 0.2579
## F-statistic: 15.14 on 3 and 119 DF, p-value: 2.088e-08
```



```
##
## Call:
## tslm(formula = train.ts ~ trend + I(trend^2) + season)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
##
  -213.775 -39.363
                        9.711
                                 42.422
                                        152.187
##
##
  Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
              1.697e+03
                          2.768e+01
                                       61.318
                                              < 2e-16 ***
                                               < 2e-16 ***
## trend
               -7.156e+00
                           7.293e-01
                                       -9.812
## I(trend^2)
                6.074e-02
                           5.698e-03
                                       10.660
                                               < 2e-16 ***
## season2
               -4.325e+01
                           3.024e+01
                                       -1.430 0.15556
## season3
                2.600e+02
                           3.024e+01
                                        8.598 6.60e-14 ***
                2.606e+02
                                        8.401 1.83e-13 ***
## season4
                           3.102e+01
                2.938e+02
                           3.102e+01
                                        9.471 6.89e-16 ***
## season5
## season6
                2.490e+02
                           3.102e+01
                                        8.026 1.26e-12 ***
## season7
                3.606e+02
                           3.102e+01
                                       11.626 < 2e-16 ***
                                       13.270
                                               < 2e-16 ***
## season8
                4.117e+02
                           3.102e+01
                9.032e+01
                                        2.911 0.00437 **
## season9
                           3.102e+01
                           3.102e+01
                2.146e+02
                                        6.917 3.29e-10 ***
## season10
## season11
                2.057e+02
                           3.103e+01
                                        6.629 1.34e-09 ***
## season12
                2.429e+02
                           3.103e+01
                                        7.829 3.44e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

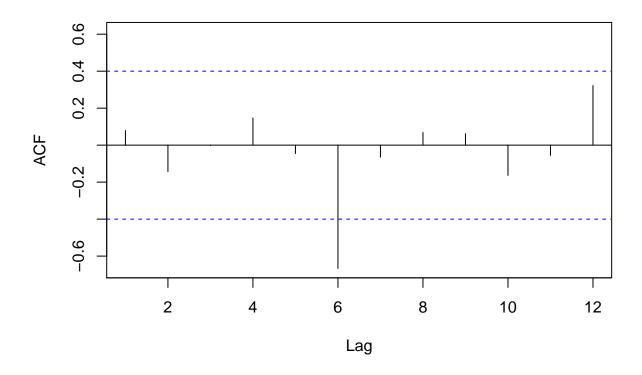
##
Residual standard error: 70.92 on 109 degrees of freedom
Multiple R-squared: 0.8246, Adjusted R-squared: 0.8037
F-statistic: 39.42 on 13 and 109 DF, p-value: < 2.2e-16</pre>

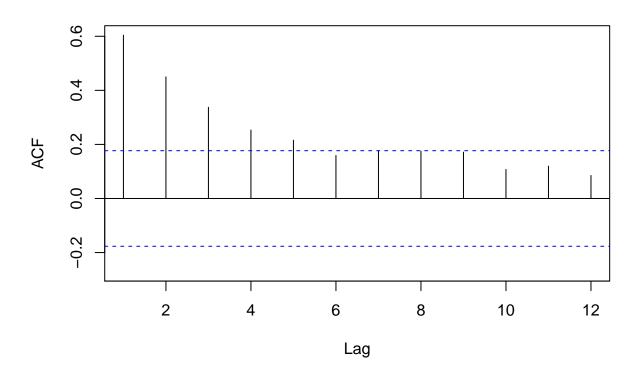




null device
1

Auto Correlations Plot and Treatment

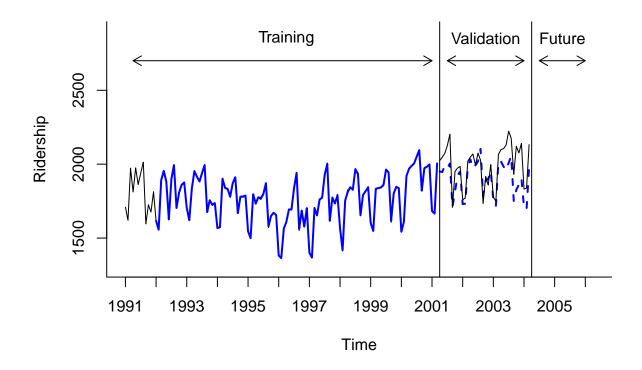




```
##
   , , 1
##
   [,1]
[1,] 1.00000000
##
    [2,] 0.60405883
##
    [3,] 0.44983171
##
##
    [4,] 0.33730830
    [5,] 0.25329034
    [6,] 0.21565844
##
##
    [7,] 0.15901326
    [8,] 0.17676683
   [9,] 0.17553762
## [10,] 0.17140882
## [11,] 0.10739472
## [12,] 0.11976519
## [13,] 0.08512942
```

```
## null device
##
## Series: train.lm.trend.season$residuals
  ARIMA(1,0,0) with non-zero mean
##
##
  Coefficients:
##
            ar1
                    mean
         0.5998
##
                  0.3728
## s.e. 0.0712 11.8408
##
## sigma^2 estimated as 2876: log likelihood=-663.54
## AIC=1333.08
                 AICc=1333.29
                                BIC=1341.52
##
## Training set error measures:
##
                        ME
                                \mathtt{RMSE}
                                         MAE
                                                  MPE
                                                          MAPE
                                                                     MASE
## Training set -0.1223159 53.19141 39.8277 103.3885 175.2219 0.5721356
##
                        ACF1
## Training set -0.07509305
## [1] 159
## a 12-7-1 network with 99 weights
  options were - linear output units
                                     i4->h1 i5->h1
##
     b->h1 i1->h1 i2->h1 i3->h1
                                                     i6->h1 i7->h1
                                                                      i8->h1
##
      7.62
              3.26
                     -0.51
                             -7.79
                                      -0.40
                                               4.18
                                                      -3.67
                                                                4.26
                                                                      -6.99
##
    i9->h1 i10->h1 i11->h1 i12->h1
##
      4.26
            -0.37
                      1.22
                              4.58
```

```
b->h2 i1->h2 i2->h2 i3->h2 i4->h2 i5->h2 i6->h2 i7->h2 i8->h2
##
    0.84 -0.47 4.11 -6.37 -7.74 8.22 -6.46 2.65 -6.84
  i9->h2 i10->h2 i11->h2 i12->h2
##
          1.42 5.43 -0.05
##
    8.29
    b->h3 i1->h3 i2->h3 i3->h3 i4->h3 i5->h3 i6->h3 i7->h3 i8->h3
##
##
    7.45 \quad -7.59 \quad -4.51 \quad 5.28 \quad -2.60 \quad -2.31 \quad -7.64 \quad 1.37 \quad -1.36
   i9->h3 i10->h3 i11->h3 i12->h3
##
    3.91
          4.33 -1.65
                        0.83
##
    b->h4 i1->h4 i2->h4 i3->h4 i4->h4 i5->h4 i6->h4 i7->h4 i8->h4
##
   -4.48 1.53 -1.92 -1.55 -6.22 8.73 -2.41 -1.68 -0.84
  i9->h4 i10->h4 i11->h4 i12->h4
    9.37 -10.92 5.00 4.68
##
   b->h5 i1->h5 i2->h5 i3->h5 i4->h5 i5->h5 i6->h5 i7->h5 i8->h5
    0.27 -2.11 -3.05 -3.50
                               -5.15 0.64 8.94 -6.71 -0.37
##
## i9->h5 i10->h5 i11->h5 i12->h5
   12.48 -2.84 -0.30 -0.55
##
##
    b->h6 i1->h6 i2->h6 i3->h6 i4->h6 i5->h6 i6->h6 i7->h6 i8->h6
   -6.31
         -4.68 1.54 -7.47 3.65 3.42 4.15 0.39 0.70
##
## i9->h6 i10->h6 i11->h6 i12->h6
    0.28 -5.94 -4.73 -0.23
##
##
   b->h7 i1->h7 i2->h7 i3->h7 i4->h7 i5->h7 i6->h7 i7->h7 i8->h7
##
    0.70
          7.03 -8.27 2.06 -13.59 -0.39 8.68 2.16 3.89
## i9->h7 i10->h7 i11->h7 i12->h7
    9.90 -1.84 -4.01 -4.10
    b->o h1->o h2->o h3->o h4->o h5->o h6->o h7->o
##
   0.60 1.05 -1.05 -1.11 1.33 -1.64 -1.58 1.28
                    ME
                           RMSE
                                    MAE
## Training set 0.1345029 4.60624 3.355614 0.001476058 0.1921153
## Test set 87.7655536 121.60742 97.251127 4.250144613 4.7525810
                  MASE ACF1 Theil's U
## Training set 0.04067807 -0.03689506 NA
## Test set 1.17891637 0.62628789 0.6955393
```



```
## Series: train.ts
## Model: NNAR(2,1,2)[12]
          nnetar(y = train.ts)
## Call:
##
## Average of 20 networks, each of which is
## a 3-2-1 network with 11 weights
## options were - linear output units
##
## sigma^2 estimated as 6766
##
                         ME
                                 RMSE
                                            MAE
                                                       MPE
                                                               MAPE
                                                                         MASE
## Training set -0.3492673 82.25378 67.07129 -0.2610314 3.875977 0.8130646
                -37.1540134 130.87578 100.48248 -2.2095656 5.236845 1.2180881
## Test set
                     ACF1 Theil's U
## Training set 0.3979050
                                 NA
## Test set
                0.3529398 0.762112
```