# Social network Graph Link Prediction - Facebook Challenge

```
In [1]:
            #Importing Libraries
          2 | # please do go through this python notebook:
          3 import warnings
            warnings.filterwarnings("ignore")
          6
            import csv
          7
            import pandas as pd#pandas to create small dataframes
          8 import datetime #Convert to unix time
            import time #Convert to unix time
         10 | # if numpy is not installed already : pip3 install numpy
             import numpy as np#Do aritmetic operations on arrays
         11
         12 # matplotlib: used to plot graphs
         13 import matplotlib
         14
            import matplotlib.pylab as plt
         15 import seaborn as sns#Plots
         16 | from matplotlib import rcParams#Size of plots
         17 | from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
         18 import math
         19 import pickle
         20 import os
         21 | # to install xqboost: pip3 install xqboost
         22 import xgboost as xgb
         23 import warnings
         24 import networkx as nx
         25 import pdb
         26 import pickle
         27 from pandas import HDFStore, DataFrame
         28 from pandas import read hdf
         29 from scipy.sparse.linalg import svds, eigs
         30 import gc
         31 from tqdm import tqdm
```

# 1. Reading Data

In [ ]:

```
In [2]:
             if os.path.isfile('data/after eda/train pos after eda.csv'):
          2
                 train graph=nx.read edgelist('data/after eda/train pos after eda.csv',de
          3
                 print(nx.info(train_graph))
          4
            else:
          5
                 print("please run the FB_EDA.ipynb or download the files from drive")
        Name:
        Type: DiGraph
        Number of nodes: 1780722
        Number of edges: 7550015
        Average in degree:
                             4.2399
        Average out degree:
                              4.2399
```

In [7]:

0

```
In [ ]: 1
```

# 2. Similarity measures

#### 2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

```
In [3]:
             #for followees
          2
             def jaccard_for_followees(a,b):
          3
          4
                      if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(a)))
          5
                          return 0
                      sim = (len(set(train graph.successors(a)).intersection(set(train gra
          6
          7
                                                    (len(set(train_graph.successors(a)).unio
          8
                  except:
          9
                      return 0
         10
                  return sim
In [4]:
             #one test case
             print(jaccard_for_followees(273084,1505602))
        0.0
In [5]:
             #node 1635354 not in graph
             print(jaccard for followees(273084,1505602))
        0.0
In [6]:
          1
             #for followers
             def jaccard_for_followers(a,b):
          2
          3
                 try:
                      if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecess
          4
          5
                          return 0
                      sim = (len(set(train graph.predecessors(a)).intersection(set(train g
          6
          7
                                                 (len(set(train_graph.predecessors(a)).union
          8
                      return sim
                 except:
          9
         10
                      return 0
```

print(jaccard for followers(273084,470294))

# 2.2 Cosine distance

$$Cosine Distance = \frac{|X \cap Y|}{|X| \cdot |Y|}$$

```
In [9]:
                                                 #for followees
                                                  def cosine_for_followees(a,b):
                                        2
                                        3
                                                                try:
                                                                               if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(a)))
                                        4
                                        5
                                                                                              return 0
                                                                               sim = (len(set(train graph.successors(a)).intersection(set(train gra
                                        6
                                        7
                                                                                                                                                                                     (math.sqrt(len(set(train_graph.successor
                                        8
                                                                               return sim
                                        9
                                                                except:
                                     10
                                                                               return 0
In [10]:
                                                  print(cosine for followees(273084,1505602))
                                  0.0
                                                   print(cosine for followees(273084,1635354))
In [11]:
                                  0
In [12]:
                                        1
                                                   def cosine_for_followers(a,b):
                                        2
                                                                try:
                                        3
                                                                               if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph
                                        4
                                                                                              return 0
                                        5
                                                                               sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessors(a))).intersection(set(train_graph.predecessor
                                        6
                                        7
                                                                                                                                                                                         (math.sqrt(len(set(train_graph.predeces
                                        8
                                                                               return sim
                                        9
                                                                 except:
                                     10
                                                                               return 0
In [13]:
                                                  print(cosine_for_followers(2,470294))
                                  0.02886751345948129
In [14]:
                                                  print(cosine_for_followers(669354,1635354))
                                  0
```

## **Preferential attachment**

```
In [15]:
           1
              def preferential attachment followers(a,b):
            2
                   try:
           3
                       if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.pr
           4
                           return 0
           5
                       p_a = len(set(train_graph.successors(a)).intersection(set(train_grap
           6
                   except:
            7
                       return 0
           8
                   return p_a
           9
In [16]:
               def preferential attachment followees(a,b):
           1
           2
                   try:
           3
                       if len(set(train graph.successors(a))) == 0 | len(set(train graph.pr
           4
                           return 0
                       p_a = len(set(train_graph.predecessors(a)).intersection(set(train_gr
            5
           6
                   except:
            7
                       return 0
           8
                   return p_a
           9
 In [ ]:
           1
 In [ ]:
 In [ ]:
           1
 In [ ]:
```

# 3. Ranking Measures

https://networkx.github.io/documentation/networkx-

- <u>1.10/reference/generated/networkx.algorithms.link\_analysis.pagerank\_alg.pagerank.html</u> (https://networkx.github.io/documentation/networkx-
- 1.10/reference/generated/networkx.algorithms.link\_analysis.pagerank\_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

## 3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

```
In [17]:
              if not os.path.isfile('data/fea sample/page rank.p'):
           2
                  pr = nx.pagerank(train_graph, alpha=0.85)
           3
                  pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
           4
              else:
                  pr = pickle.load(open('data/fea sample/page rank.p','rb'))
In [18]:
              print('min',pr[min(pr, key=pr.get)])
              print('max',pr[max(pr, key=pr.get)])
              print('mean',float(sum(pr.values())) / len(pr))
         min 1.6556497245737814e-07
         max 2.7098251341935827e-05
         mean 5.615699699389075e-07
In [19]:
           1 | #for imputing to nodes which are not there in Train data
             mean_pr = float(sum(pr.values())) / len(pr)
           3 print(mean pr)
```

5.615699699389075e-07

# 4. Other Graph Features

## 4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [20]:
              #if has direct edge then deleting that edge and calculating shortest path
              def compute_shortest_path_length(a,b):
           2
                  p=-1
           3
           4
                  try:
           5
                      if train_graph.has_edge(a,b):
           6
                          train_graph.remove_edge(a,b)
                           p= nx.shortest_path_length(train_graph,source=a,target=b)
           7
                          train_graph.add_edge(a,b)
           8
           9
                      else:
                          p= nx.shortest_path_length(train_graph,source=a,target=b)
          10
          11
                      return p
                  except:
          12
          13
                      return -1
In [21]:
              #testing
              compute shortest path length(77697, 826021)
Out[21]: 10
In [22]:
           1
              #testing
              compute_shortest_path_length(669354,1635354)
Out[22]: -1
```

# 4.2 Checking for same community

```
In [23]:
              #getting weekly connected edges from graph
              wcc=list(nx.weakly connected components(train graph))
              def belongs_to_same_wcc(a,b):
            3
           4
                   index = []
                   if train_graph.has_edge(b,a):
           5
           6
                       return 1
            7
                   if train_graph.has_edge(a,b):
                           for i in wcc:
           8
                                if a in i:
           9
                                    index= i
          10
          11
                                    break
                           if (b in index):
          12
                                train_graph.remove_edge(a,b)
          13
                                if compute_shortest_path_length(a,b)==-1:
          14
                                    train graph.add edge(a,b)
          15
          16
                                    return 0
          17
                                else:
          18
                                    train_graph.add_edge(a,b)
          19
                                    return 1
          20
                           else:
          21
                                return 0
          22
                   else:
                           for i in wcc:
          23
          24
                                if a in i:
          25
                                    index= i
          26
                                    break
          27
                           if(b in index):
          28
                                return 1
          29
                           else:
          30
                                return 0
In [24]:
              belongs to same wcc(861, 1659750)
Out[24]: 0
In [25]:
              belongs_to_same_wcc(669354,1635354)
```

## 4.3 Adamic/Adar Index:

Out[25]: 0

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x, y) = \sum_{u \in N(x) \cap N(y)} \frac{1}{log(|N(u)|)}$$

```
In [26]:
              #adar index
              def calc adar in(a,b):
           2
           3
                   sum=0
           4
                  try:
                       n=list(set(train graph.successors(a)).intersection(set(train graph.s
           5
           6
                       if len(n)!=0:
           7
                           for i in n:
           8
                               sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
           9
                           return sum
          10
                       else:
          11
                           return 0
          12
                  except:
          13
                       return 0
In [27]:
              calc_adar_in(1,189226)
Out[27]: 0
           1 calc_adar_in(669354,1635354)
In [28]:
Out[28]: 0
```

# 4.4 Is the person following back:

```
In [29]:
              def follows_back(a,b):
           1
           2
                   if train graph.has edge(b,a):
           3
                       return 1
           4
                  else:
                       return 0
In [30]:
              follows_back(1,189226)
Out[30]: 1
In [31]:
              follows_back(669354,1635354)
Out[31]: 0
```

## 4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz\_centrality (https://en.wikipedia.org/wiki/Katz\_centrality)

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/
(https://www.geeksforgeeks.org/katz-centrality-centrality-measure/)
Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

$$x_i = \alpha \sum_j A_{ij} x_j + \beta,$$

where A is the adjacency matrix of the graph G with eigenvalues

λ

.

The parameter

controls the initial centrality and

β

```
\alpha < \frac{1}{\lambda_{max}}.
```

```
In [32]:
              if not os.path.isfile('data/fea_sample/katz.p'):
                  katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
           2
           3
                  pickle.dump(katz,open('data/fea sample/katz.p','wb'))
           4
              else:
                  katz = pickle.load(open('data/fea_sample/katz.p','rb'))
In [33]:
              print('min',katz[min(katz, key=katz.get)])
              print('max',katz[max(katz, key=katz.get)])
              print('mean',float(sum(katz.values())) / len(katz))
         min 0.0007313532484065916
         max 0.003394554981699122
         mean 0.0007483800935562018
```

mean\_katz = float(sum(katz.values())) / len(katz)

0.0007483800935562018

print(mean katz)

In [34]:

#### 4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS\_algorithm (https://en.wikipedia.org/wiki/HITS\_algorithm)

```
In [35]:
           1
              if not os.path.isfile('data/fea sample/hits.p'):
                  hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normal
           2
           3
                  pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
           4
              else:
           5
                  hits = pickle.load(open('data/fea sample/hits.p','rb'))
In [36]:
              print('min',hits[0][min(hits[0], key=hits[0].get)])
              print('max',hits[0][max(hits[0], key=hits[0].get)])
              print('mean',float(sum(hits[0].values())) / len(hits[0]))
         min 0.0
         max 0.004868653378780953
         mean 5.615699699344123e-07
```

# 5. Featurization

#### 5. 1 Reading a sample of Data from both train and test

```
In [37]:
              import random
              if os.path.isfile('data/after eda/train after eda.csv'):
           2
           3
                  filename = "data/after eda/train after eda.csv"
                  # you uncomment this line, if you don't know the lentgh of the file name
           4
                  # here we have hardcoded the number of lines as 15100030
           5
                  # n train = sum(1 for line in open(filename)) #number of records in file
           6
           7
                  n train = 15100028
           8
                  s = 100000 #desired sample size
           9
                  skip train = sorted(random.sample(range(1,n train+1),n train-s))
          10
                  #https://stackoverflow.com/a/22259008/4084039
In [38]:
              if os.path.isfile('data/after eda/train after eda.csv'):
                  filename = "data/after eda/test after eda.csv"
           2
           3
                  # you uncomment this line, if you dont know the lentqh of the file name
                  # here we have hardcoded the number of lines as 3775008
           4
                  # n test = sum(1 for line in open(filename)) #number of records in file
           5
           6
                  n test = 3775006
           7
                  s = 50000 #desired sample size
           8
                  skip test = sorted(random.sample(range(1,n test+1),n test-s))
                  #https://stackoverflow.com/a/22259008/4084039
In [39]:
           1 print("Number of rows in the train data file:", n_train)
           2 print("Number of rows we are going to elimiate in train data are",len(skip t
           3 print("Number of rows in the test data file:", n_test)
              print("Number of rows we are going to elimiate in test data are",len(skip te
         Number of rows in the train data file: 15100028
         Number of rows we are going to elimiate in train data are 15000028
         Number of rows in the test data file: 3775006
         Number of rows we are going to elimiate in test data are 3725006
In [40]:
           1 | df_final_train = pd.read_csv('data/after_eda/train_after_eda.csv', skiprows=
           2 df_final_train['indicator_link'] = pd.read_csv('data/train_y.csv', skiprows=
           3 print("Our train matrix size ",df final train.shape)
           4 df final train.head(2)
         Our train matrix size (100002, 3)
Out[40]:
             source node destination node indicator link
```

	source_noue	destination_node	indicator_iiik
0	273084	1505602	1
1	1814537	613441	1

Our test matrix size (50002, 3)

#### Out[41]:

	source_node	destination_node	indicator_link
0	848424	784690	1
1	548473	1721521	1

# 5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard followees
- 3. cosine followers
- 4. cosine followees
- 5. num\_followers\_s
- 6. num followees s
- 7. num\_followers\_d
- 8. num\_followees\_d
- 9. inter followers
- 10. inter followees

```
In [46]:
           1
              if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
           2
                  #mapping jaccrd followers to train and test data
           3
                  df final train['jaccard followers'] = df final train.apply(lambda row:
           4
                                                           jaccard for followers(row['sourc
                  df final test['jaccard followers'] = df final test.apply(lambda row:
           5
           6
                                                           jaccard for followers(row['sourc
           7
           8
                  #mapping jaccrd followees to train and test data
           9
                  df final train['jaccard followees'] = df final train.apply(lambda row:
                                                           jaccard_for_followees(row['sourc
          10
          11
                  df final test['jaccard followees'] = df final test.apply(lambda row:
          12
                                                           jaccard for followees(row['sourc
          13
          14
          15
                      #mapping jaccrd followers to train and test data
          16
                  df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
          17
                                                           cosine for followers(row['source
          18
                  df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
          19
                                                           cosine_for_followers(row['source
          20
          21
                  #mapping jaccrd followees to train and test data
          22
                  df_final_train['cosine_followees'] = df_final_train.apply(lambda row:
          23
                                                           cosine for followees(row['source
          24
                  df_final_test['cosine_followees'] = df_final_test.apply(lambda row:
          25
                                                           cosine for followees(row['source
In [60]:
              asdad = df final train.apply(lambda row:jaccard for followers(row['source no
           2
In [47]:
              # #if anything not there in train graph then adding mean page rank
              # df_final_train['preferential_attachment_s'] = df_final_train.source_node.a
              # df final train['preferential attachment d'] = df final train.destination n
           3
           4
              # df final test['preferential attachment s'] = df final test.source node.app
           5
              # df final test['preferential attachment d'] = df final test.destination nod
```

```
In [48]:
           1
              def compute features stage1(df final):
           2
                  #calculating no of followers followees for source and destination
           3
                  #calculating intersection of followers and followees for source and dest
           4
                  num followers s=[]
           5
                  num followees s=[]
           6
                  num_followers_d=[]
           7
                  num followees d=[]
           8
                  inter followers=[]
           9
                  inter followees=[]
                  for i,row in df_final.iterrows():
          10
                      try:
          11
                          s1=set(train_graph.predecessors(row['source_node']))
          12
          13
                          s2=set(train_graph.successors(row['source_node']))
          14
                      except:
          15
                          s1 = set()
                          s2 = set()
          16
          17
                      try:
          18
                          d1=set(train_graph.predecessors(row['destination_node']))
          19
                          d2=set(train_graph.successors(row['destination_node']))
          20
          21
                          d1 = set()
          22
                          d2 = set()
          23
                      num followers s.append(len(s1))
                      num_followees_s.append(len(s2))
          24
          25
                      num followers d.append(len(d1))
          26
          27
                      num followees d.append(len(d2))
          28
          29
                      inter followers.append(len(s1.intersection(d1)))
                      inter_followees.append(len(s2.intersection(d2)))
          30
          31
          32
                  return num_followers_s, num_followers_d, num_followees_s, num_followees_
In [49]:
           1
              if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
                  df final train['num followers s'], df final train['num followers d'], \
           2
                  df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
           3
           4
                  df_final_train['inter_followers'], df_final_train['inter_followees']= co
           5
           6
                  df final test['num followers s'], df final test['num followers d'], \
           7
                  df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
           8
                  df_final_test['inter_followers'], df_final_test['inter_followees']= comp
           9
          10
                  hdf = HDFStore('data/fea_sample/storage_sample_stage1.h5')
          11
                  hdf.put('train_df',df_final_train, format='table', data_columns=True)
                  hdf.put('test df',df final test, format='table', data columns=True)
          12
          13
                  hdf.close()
          14
              else:
                  df final train = read hdf('data/fea sample/storage sample stage1.h5', 't
          15
          16
                  df_final_test = read_hdf('data/fea_sample/storage_sample_stage1.h5',
```

# 5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [50]:
           1
              if not os.path.isfile('data/fea sample/storage sample stage2.h5'):
           2
                  #mapping adar index on train
           3
                  df final train['adar index'] = df final train.apply(lambda row: calc ada
           4
                  #mapping adar index on test
           5
                  df final test['adar index'] = df final test.apply(lambda row: calc adar
           6
           7
           8
                  #mapping followback or not on train
           9
                  df final train['follows back'] = df final train.apply(lambda row: follow
          10
          11
                  #mapping followback or not on test
          12
                  df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_
          13
          14
          15
                  #mapping same component of wcc or not on train
                  df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_t
          16
          17
          18
                  ##mapping same component of wcc or not on train
          19
                  df final test['same comp'] = df final test.apply(lambda row: belongs to
          20
          21
          22
                  #mapping shortest path on train
                  df final train['shortest path'] = df final train.apply(lambda row: compu
          23
          24
                  #mapping shortest path on test
          25
                  df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute
          26
          27
                  hdf = HDFStore('data/fea sample/storage sample stage2.h5')
          28
                  hdf.put('train_df',df_final_train, format='table', data_columns=True)
          29
                  hdf.put('test_df',df_final_test, format='table', data_columns=True)
          30
                  hdf.close()
          31
              else:
                  df final train = read hdf('data/fea sample/storage sample stage2.h5',
          32
                  df final test = read hdf('data/fea sample/storage sample stage2.h5', 'te
          33
```

#### 5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
  - · weight of incoming edges
  - · weight of outgoing edges
  - · weight of incoming edges + weight of outgoing edges
  - · weight of incoming edges \* weight of outgoing edges
  - 2\*weight of incoming edges + weight of outgoing edges
  - · weight of incoming edges + 2\*weight of outgoing edges
- 2. Page Ranking of source
- Page Ranking of dest

- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities\_s of dest

#### **Weight Features**

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. <code>credit</code> - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1 + |X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
In [54]:
              #weight for source and destination of each link
           2 Weight in = {}
              Weight out = {}
              for i in tqdm(train_graph.nodes()):
           5
                  s1=set(train graph.predecessors(i))
           6
                  w in = 1.0/(np.sqrt(1+len(s1)))
           7
                  Weight in[i]=w in
           8
           9
                  s2=set(train graph.successors(i))
          10
                  w_{out} = 1.0/(np.sqrt(1+len(s2)))
          11
                  Weight out[i]=w out
          12
          13
              #for imputing with mean
              mean_weight_in = np.mean(list(Weight_in.values()))
          14
              mean weight out = np.mean(list(Weight out.values()))
          15
```

```
In [0]:
          1
             if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
          2
                 #mapping to pandas train
                 df final train['weight in'] = df final train.destination node.apply(lamb
          3
          4
                 df final train['weight out'] = df final train.source node.apply(lambda x
          5
          6
                 #mapping to pandas test
          7
                 df final test['weight in'] = df final test.destination node.apply(lambda
          8
                 df final test['weight out'] = df final test.source node.apply(lambda x:
          9
         10
         11
                 #some features engineerings on the in and out weights
         12
                 df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.
                 df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.
         13
                 df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_t
         14
                 df final train['weight f4'] = (1*df final train.weight in + 2*df final t
         15
         16
         17
                 #some features engineerings on the in and out weights
         18
                 df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_
         19
                 df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.wei
                 df final test['weight f3'] = (2*df final test.weight in + 1*df final test
         20
         21
                 df final test['weight f4'] = (1*df final test.weight in + 2*df final test
```

```
In [0]:
         1
           if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
         2
         3
               #page rank for source and destination in Train and Test
         4
               #if anything not there in train graph then adding mean page rank
         5
               df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda
         6
               df_final_train['page_rank_d'] = df_final_train.destination_node.apply(la
         7
         8
               df final test['page rank s'] = df final test.source node.apply(lambda x:
               df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lamb
         9
               10
        11
        12
               #Katz centrality score for source and destination in Train and test
        13
               #if anything not there in train graph then adding mean katz score
               df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: ka
        14
        15
               df final train['katz d'] = df final train.destination node.apply(lambda
        16
        17
               df final test['katz s'] = df final test.source node.apply(lambda x: katz
        18
               df_final_test['katz_d'] = df_final_test.destination_node.apply(lambda x:
        19
               20
        21
               #Hits algorithm score for source and destination in Train and test
        22
               #if anything not there in train graph then adding 0
               df final train['hubs s'] = df final train.source node.apply(lambda x: hi
        23
        24
               df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda
        25
        26
               df final test['hubs s'] = df final test.source node.apply(lambda x: hits
        27
               df final test['hubs d'] = df final test.destination node.apply(lambda x:
        28
               29
        30
               #Hits algorithm score for source and destination in Train and Test
        31
               #if anything not there in train graph then adding 0
               df final train['authorities s'] = df final train.source node.apply(lambd
        32
               df final train['authorities d'] = df final train.destination node.apply(
        33
        34
        35
               df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda
        36
               df_final_test['authorities_d'] = df_final_test.destination_node.apply(la
        37
               38
        39
               hdf = HDFStore('data/fea sample/storage sample stage3.h5')
        40
               hdf.put('train df',df final train, format='table', data columns=True)
        41
               hdf.put('test_df',df_final_test, format='table', data_columns=True)
               hdf.close()
        42
        43
           else:
               df final train = read hdf('data/fea sample/storage sample stage3.h5', 't
        44
        45
               df final test = read hdf('data/fea sample/storage sample stage3.h5', 'te
```

#### 5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [42]:
           1
              def svd(x, S):
           2
                  try:
                      z = sadj_dict[x]
           3
           4
                      return S[z]
           5
                  except:
           6
                      return [0,0,0,0,0,0]
In [43]:
             #for svd features to get feature vector creating a dict node val and inedx i
              sadj_col = sorted(train_graph.nodes())
              sadj dict = { val:idx for idx,val in enumerate(sadj col)}
In [44]:
              Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes()))
In [45]:
              U, s, V = svds(Adj, k = 6)
             print('Adjacency matrix Shape',Adj.shape)
           3 print('U Shape',U.shape)
             print('V Shape', V.shape)
              print('s Shape',s.shape)
         Adjacency matrix Shape (1780722, 1780722)
         U Shape (1780722, 6)
         V Shape (6, 1780722)
         s Shape (6,)
```

```
In [0]:
                     1
                           if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
                     2
                                  3
                     4
                                 df final train[['svd u s 1', 'svd u s 2','svd u s 3', 'svd u s 4', 'svd
                     5
                                 df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
                     6
                     7
                                 df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd
                     8
                                  df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Seri
                     9
                                  10
                    11
                                 df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_1', 'sv
                    12
                                 df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
                    13
                                 df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd
                    14
                   15
                                 df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Se
                    16
                                  17
                    18
                                 df_final_test[['svd_u_s_1', 'svd_u_s_2','svd_u_s_3', 'svd_u_s_4', 'svd_u
                    19
                                 df_final_test.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
                    20
                    21
                                 df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_
                    22
                                 df_final_test.destination_node.apply(lambda x: svd(x, U)).apply(pd.Serie
                    23
                    24
                                  25
                    26
                                  df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v
                    27
                                  df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
                    28
                    29
                                 df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd
                    30
                                 df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Ser
                    31
                                  32
                    33
                                 hdf = HDFStore('data/fea sample/storage sample stage4.h5')
                    34
                                 hdf.put('train_df',df_final_train, format='table', data_columns=True)
                                 hdf.put('test_df',df_final_test, format='table', data_columns=True)
                    35
                    36
                                 hdf.close()
   In [ ]:
                     1
   In [ ]:
                     1
   In [ ]:
   In [ ]:
                     1
In [104]:
                        from pandas import read hdf
                          df_final_train = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'train')
                          df_final_test = read_hdf('data/fea_sample/storage_sample_stage4.h5', 'test_d
```

```
In [105]: 1 df_final_train.describe()
```

#### Out[105]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_
count	1.000020e+05	1.000020e+05	100002.000000	100002.0	100002.000000	1000
mean	9.305942e+05	9.280010e+05	0.500490	0.0	0.040088	
std	5.376040e+05	5.383887e+05	0.500002	0.0	0.104141	
min	3.000000e+00	7.000000e+00	0.000000	0.0	0.000000	
25%	4.654765e+05	4.598682e+05	0.000000	0.0	0.000000	
50%	9.309050e+05	9.290790e+05	1.000000	0.0	0.000000	
75%	1.395303e+06	1.392905e+06	1.000000	0.0	0.000000	
max	1.862198e+06	1.862218e+06	1.000000	0.0	0.833333	

#### 8 rows × 54 columns

```
In [96]: 1 # prepared and stored the data from machine learning models
2 # pelase check the FB_Models.ipynbb
```

```
In [97]:
              svd dot train U U = []
           2
              for i,a in tqdm(df_final_train.iterrows(), total = df_final_train.shape[0]):
                  s = sadj_dict.get(a.source_node, 'NA')
           3
                  d = sadj dict.get(a.destination node, 'NA')
           4
           5
                  if (s!='NA') and (d!='NA'):
           6
                      aaa = np.dot(U[s,:], U[d,:])
           7
                      svd dot train U U.append(aaa)
           8
                  else:
           9
                      svd_dot_train_U_U.append(0)
```

100%| 100%| 100002 [00:07<00:00, 14036.04it/s]

```
In [98]:
              svd dot train U V = []
              for i,a in tqdm(df final train.iterrows(), total = df final train.shape[0]):
           2
           3
                  s = sadj_dict.get(a.source_node, 'NA')
           4
                  d = sadj dict.get(a.destination node, 'NA')
           5
                  if (s!='NA') and (d!='NA'):
           6
                      aaa = np.dot(U[s,:], V[:,d])
           7
                       svd_dot_train_U_V.append(aaa)
           8
                  else:
           9
                      svd_dot_train_U_V.append(0)
```

```
100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%| 100%|
```

```
In [99]:
            1
               svd dot train V V = []
               for i,a in tqdm(df_final_train.iterrows(), total = df_final_train.shape[0]):
            2
            3
                   s = sadj dict.get(a.source node, 'NA')
                   d = sadj dict.get(a.destination node, 'NA')
            4
                   if (s!='NA') and (d!='NA'):
            5
            6
                       aaa = np.dot(V[:,s], V[:,d])
            7
                        svd dot train V V.append(aaa)
            8
                   else:
            9
                        svd dot train V V.append(0)
          100%
          00002/100002 [00:07<00:00, 13043.87it/s]
In [100]:
               svd dot test U U = []
               for i,a in tqdm(df final test.iterrows(), total = df final test.shape[0]):
            2
            3
                   s = sadj dict.get(a.source node, 'NA')
            4
                   d = sadj dict.get(a.destination node, 'NA')
                   if (s!='NA') and (d!='NA'):
            5
                       aaa = np.dot(U[s,:], U[d,:])
            6
            7
                        svd_dot_test_U_U.append(aaa)
            8
                   else:
            9
                        svd dot test U U.append(0)
          100%
          50002/50002 [00:03<00:00, 13228.33it/s]
In [101]:
               svd dot test U V = []
               for i,a in tqdm(df_final_test.iterrows(), total = df_final_test.shape[0]):
            2
            3
                   s = sadj dict.get(a.source node, 'NA')
            4
                   d = sadj dict.get(a.destination node, 'NA')
            5
                   if (s!='NA') and (d!='NA'):
            6
                       aaa = np.dot(U[s,:], V[:,d])
            7
                        svd dot test U V.append(aaa)
            8
                   else:
                        svd dot test U V.append(0)
            9
          100%
          50002/50002 [00:03<00:00, 14008.32it/s]
In [102]:
               svd dot test V V = []
            1
               for i,a in tqdm(df_final_test.iterrows(), total = df_final_test.shape[0]):
            2
            3
                   s = sadj dict.get(a.source node, 'NA')
                   d = sadj dict.get(a.destination node, 'NA')
            4
            5
                   if (s!='NA') and (d!='NA'):
                       aaa = np.dot(V[:,s], V[:,d])
            6
            7
                        svd_dot_test_V_V.append(aaa)
            8
                   else:
                        svd_dot_test_V_V.append(0)
            9
          100%
          50002/50002 [00:03<00:00, 14118.65it/s]
```

```
In [106]:
           1
              if not os.path.isfile('data/fea sample/storage sample stage5.h5'):
            2
                  3
           4
                  df final train['svd dot U U'] = svd dot train U U
            5
                  df final train['svd dot U V'] = svd dot train U V
           6
                  df_final_train['svd_dot_V_V'] = svd_dot_train_V_V
           7
                  df final test['svd dot U U'] = svd dot test U U
                  df final test['svd_dot_U_V'] = svd_dot_test_U_V
           8
                  df final test['svd dot V V'] = svd dot test V V
           9
                  df_final_train['preferential_attachment_followers'] = df_final_train.app
           10
           11
                      lambda row:preferential attachment followers(row['source node'], row
           12
                  df_final_train['preferential_attachment_followees'] = df_final_train.app
                      lambda row:preferential attachment followees(row['source node'], row
           13
                  df_final_test['preferential_attachment_followers'] = df_final_test.apply
           14
                      lambda row:preferential attachment followers(row['source node'], row
          15
           16
                  df_final_test['preferential_attachment_followees'] = df_final_test.apply
          17
                      lambda row:preferential attachment followees(row['source node'], row
           18
                  hdf = HDFStore('data/fea sample/storage sample stage5.h5')
                  hdf.put('train_df',df_final_train, format='table', data_columns=True)
           19
                  hdf.put('test df',df final test, format='table', data columns=True)
           20
           21
                  hdf.close()
  In [ ]:
           1
  In [ ]:
           1
  In [ ]:
  In [ ]:
           1
  In [ ]:
```