Machine Learning Lab 10

Dimensionality Reduction

Dimensionality reduction is the process of reducing the number of random variables under consideration, by obtaining a set of principal variables. It can be divided into feature selection and feature extraction. There are two components of dimensionality reduction, the first one being feature selection, in which, we try to find a subset of the original set of variables, or features, to get a smaller subset which can be used to model the problem. It is usually done using filtered, wrapped and embedded, the second one is feature extraction. This reduces the data in a high dimensional space to a lower dimension space, i.e. a space with lesser no. of dimensions.

In this experiment we use three methods for dimensionality reduction namely:

- * Principal Component Analysis (PCA)
- * Linear Discriminant Analysis (LDA)
- * Kernel Principal Component Analysis (KPCA)

The dataset

The dataset used to perform this experiment is the wine quality dataset, it is a combination of data on two types of wine variants, namely red wine and white wine, of the portuguese "Vinho Verde" wine. The dataset contains information on the parameters for fixed acidity, volatile acidity, citric acid, residual sugar, chlorides, free sulfur dioxide, total sulfur dioxide, density, pH, sulphates, alcohol.

Experiment

In this experiment I used the sklearn's PCA(principal component analysis), LDA(linear discriminant analysis) and KPCA algorithms to predict the quality of a wine.

Using the pandas library in I loaded the red wine and white wine datasets into the memory from their respective csv files and then merged the two datasets into one single pandas dataframe. Then I bin the data points into good and bad wine quality data points this is done to reduce the skewness of the dataset, with the original quality classes (i.e. from 3 to 9 the dataset was very skewed). The criterion used for binning is the wine quality. A quality of above and equal to 6 is considered good, where as that below 6 is bad. Thus instead of 6 now I am left with just two categories in my dataset.

Using the standard scaler in sklearn I scaled the all the features of the dataset so as to avoid any feature to dominate while the algorithm is learning on the data.

For performing the experiment I started applying just a logistic regression to my dataset followed by applying a PCA and then applying a logistic regression again. And

after applying the PCA, there was a 0.02 increase in the score of the logistic regression model from 0.96 to 0.98 on the training set.

Next I used a scatter plot to visualize the dataset with reduced dimensions and from the graph it is evident that with reduced dimensions the data points corresponding to the good wine and bad wine samples cluster together.

Next I reduced my data with the LDA algorithm however, with my data it always reduced the dimensions to 1 no matter what, and hence it wasn't useful for any interpretations in my case.

Finally I applied the KPCA with rbf (Radial Basis Function) as the kernel for my PCA and then used a scatter plot to visualize the data and the results were similar, the similar data points clustered together.

This is because once the dimensionality is reduced, the new dimensions contain much more information as compared to the previous dimensions and thus are much better representative of the data than randomly selecting any same number of dimensions from the data. Thus we observe the clustering when we plot the data.

The code and plots can be found in the accompanying jupyter notebook.

PCA + LDA + KPCA

November 1, 2018

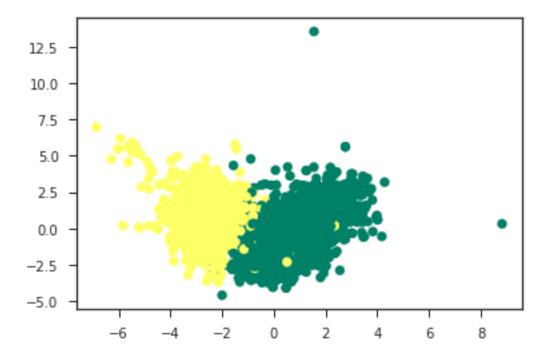
- 1 Lab 10
- 2 Dimensionality Reduction
- 2.1 Submitted to: Prof. Sweetlin Hemlatha
- 2.2 Submitted by: Prateek Singh (15BCE1091)

```
In [2]: import random
        import numpy as np
        import pandas as pd
        import seaborn as sn
        from sklearn.linear_model import LogisticRegression
        from sklearn.model_selection import train_test_split
        from sklearn.metrics import precision_score, recall_score
        from sklearn.preprocessing import StandardScaler
        from sklearn.decomposition import PCA, KernelPCA
        from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
        import matplotlib.pyplot as plt
        from matplotlib.colors import ListedColormap
        %matplotlib inline
In [3]: sn.set(style='ticks', color_codes=True, font_scale=1)
        white_wine = pd.read_csv('../Dataset/winequality-white.csv', sep=';')
        white_wine['wine_type'] = 0
        red_wine = pd.read_csv('../Dataset/winequality-red.csv', sep=';')
        red_wine['wine_type'] = 1
        wine_data = pd.concat([white_wine, red_wine])
        wine_data.tail()
Out[3]:
              fixed acidity volatile acidity citric acid residual sugar chlorides \
                                                                       2.0
        1594
                        6.2
                                        0.600
                                                      0.08
                                                                                0.090
        1595
                        5.9
                                        0.550
                                                      0.10
                                                                       2.2
                                                                                0.062
        1596
                        6.3
                                        0.510
                                                      0.13
                                                                       2.3
                                                                                0.076
        1597
                        5.9
                                        0.645
                                                      0.12
                                                                       2.0
                                                                                0.075
```

```
6.0
                   1598
                                                                                                0.310
                                                                                                                                  0.47
                                                                                                                                                                           3.6
                                                                                                                                                                                                 0.067
                                 free sulfur dioxide total sulfur dioxide density
                                                                                                                                                                   pH sulphates \
                   1594
                                                                      32.0
                                                                                                                           44.0 0.99490 3.45
                                                                                                                                                                                          0.58
                                                                      39.0
                                                                                                                           51.0 0.99512 3.52
                   1595
                                                                                                                                                                                          0.76
                                                                      29.0
                                                                                                                           40.0 0.99574 3.42
                                                                                                                                                                                          0.75
                   1596
                   1597
                                                                      32.0
                                                                                                                           44.0 0.99547 3.57
                                                                                                                                                                                          0.71
                   1598
                                                                      18.0
                                                                                                                           42.0 0.99549 3.39
                                                                                                                                                                                          0.66
                                 alcohol quality wine_type
                   1594
                                         10.5
                                                                      5
                                        11.2
                                                                      6
                   1595
                                                                                                 1
                                         11.0
                                                                      6
                   1596
                                                                                                 1
                                        10.2
                                                                      5
                   1597
                                                                                                1
                   1598
                                        11.0
                                                                      6
In [4]: scaler = StandardScaler()
                   data = wine_data.iloc[:,:11].values
                   scaled_features = scaler.fit_transform(data)
                   wine_data_scaled = pd.DataFrame(scaled_features, index=wine_data.index, columns=wine_data_scaled_scaled_scaled_features, index=wine_data_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scaled_scale
                   wine_data_scaled.head()
Out [4]:
                          fixed acidity volatile acidity citric acid residual sugar
                                                                                                                                                                                chlorides
                   0
                                    -0.166089
                                                                               -0.423183
                                                                                                                 0.284686
                                                                                                                                                        3.206929
                                                                                                                                                                                -0.314975
                                                                                                                                                     -0.807837
                   1
                                    -0.706073
                                                                               -0.240949
                                                                                                                 0.147046
                                                                                                                                                                                -0.200790
                   2
                                     0.682458
                                                                               -0.362438
                                                                                                                 0.559966
                                                                                                                                                        0.306208
                                                                                                                                                                                -0.172244
                   3
                                    -0.011808
                                                                               -0.666161
                                                                                                                 0.009406
                                                                                                                                                        0.642523
                                                                                                                                                                                   0.056126
                   4
                                                                               -0.666161
                                    -0.011808
                                                                                                                 0.009406
                                                                                                                                                        0.642523
                                                                                                                                                                                  0.056126
                          free sulfur dioxide total sulfur dioxide density
                                                                                                                                                                         pH sulphates \
                   0
                                                    0.815565
                                                                                                          0.959976 2.102214 -1.359049 -0.546178
                   1
                                                   -0.931107
                                                                                                          0.287618 -0.232332 0.506915 -0.277351
                   2
                                                   -0.029599
                                                                                                        -0.331660 0.134525 0.258120 -0.613385
                   3
                                                     0.928254
                                                                                                          1.243074 0.301278 -0.177272 -0.882212
                   4
                                                     0.928254
                                                                                                          1.243074 0.301278 -0.177272 -0.882212
                             alcohol
                   0 -1.418558
                   1 -0.831615
                   2 -0.328521
                   3 -0.496219
                   4 -0.496219
In [5]: X_train, X_test, Y_train, Y_test = train_test_split(wine_data_scaled,
                                                                                                                                                 wine_data.iloc[:, 12],
                                                                                                                                                 test_size=0.2,
                                                                                                                                                 random_state=42)
```

Applying logistic regression without any dimensionality reduction

```
In [6]: model_ll = LogisticRegression(penalty='12', solver='saga', max_iter=10, multi_class='o'
        model_ll.fit(X_train, Y_train)
       print("Train Score: ", model_ll.score(X_train, Y_train))
        print("Test Score: ", model_ll.score(X_test, Y_test), '\n')
Train Score: 0.9926880892822783
Test Score: 0.9884615384615385
/home/prateek/anaconda3/envs/dltf/lib/python3.6/site-packages/sklearn/linear_model/sag.py:326:
  "the coef_ did not converge", ConvergenceWarning)
  Applying PCA over the dataset
In [7]: wine_data_vals = wine_data_scaled.values
       pca = PCA(n_components=2, svd_solver='full', random_state=42)
        reduced_wine_data = pca.fit_transform(X_train)
        reduced_wine_data.shape
Out[7]: (5197, 2)
In [8]: model_ll = LogisticRegression(penalty='12', solver='saga', max_iter=10000, multi_class
        model_ll.fit(reduced_wine_data, Y_train)
Out[8]: LogisticRegression(C=1.0, class_weight=None, dual=False, fit_intercept=True,
                  intercept_scaling=1, max_iter=10000, multi_class='multinomial',
                  n_jobs=1, penalty='12', random_state=None, solver='saga',
                  tol=0.0001, verbose=0, warm start=False)
In [1]: print(model_ll.score(reduced_wine_data, Y_train))
        print(model_ll.score(pca.transform(X_test), Y_test))
0.9659534346738503
0.9807692307692307
In [10]: plt.scatter(reduced_wine_data[:, 0], reduced_wine_data[:, 1], c=Y_train, cmap='summer
Out[10]: <matplotlib.collections.PathCollection at 0x7f442788de48>
```



Applying LDA over the dataset

```
In [11]: lda = LinearDiscriminantAnalysis(solver='eigen', n_components=3)
         wine_data_reduced = lda.fit_transform(X_train, Y_train)
In [12]: wine_data_reduced.shape
Out[12]: (5197, 1)
In [13]: wine_data_reduced
Out[13]: array([[-0.5634886],
                [-0.53612547],
                [-0.15322816],
                ...,
                [ 1.34187962],
                [ 1.35577714],
                [-0.22737771]])
  Applying KPCA on the dataset
In [14]: kpca = KernelPCA(n_components=2, kernel='rbf', random_state=42)
         wine_data_reduced = kpca.fit_transform(X_train)
In [15]: print(model_ll.score(reduced_wine_data, Y_train))
         print(model_ll.score(kpca.transform(X_test), Y_test))
```

- 0.9859534346738503
- 0.7584615384615384

In [16]: plt.scatter(reduced_wine_data[:, 0], reduced_wine_data[:, 1], c=Y_train, cmap='summer
Out[16]: <matplotlib.collections.PathCollection at 0x7f4425ac13c8>

