

## Assignment No. 2

Q.1. Explain Chomsky's classification of grammar.  
 → Chomsky has classified formal grammar in 4 categories:

- i) Type 3 grammar ( $T_3$ )
- ii) Type 2 grammar ( $T_2$ )
- iii) Type 1 grammar ( $T_1$ )
- iv) Type 0 grammar ( $T_0$ )

i) Type 3 grammar ( $T_3$ ) -

It is also called as regular grammar.

If every production of a grammar is in the form  $A \rightarrow \alpha B / B$

where  $A, B \in V$

&  $\beta, \alpha \in \Sigma^*$

then such grammar known as regular grammar.

The language generated by regular grammar is a regular language.

Or type 3 language which is further processed by finite automata.

Regular grammars are further classified into two types:

① RLG (Right linear grammar)

② LLG (Left linear grammar)

Every LLG can be converted into RLG. & every RLG can be converted into LLG.

∴ Their expressive power is identical.

cal.

For example, consider following grammar

$$A \longrightarrow Ba$$

$$A \longrightarrow \epsilon$$

② Type 2 grammar (context free grammar)

A grammar 'G' is context free grammar if & only if all the productions of that grammar are in the form

$$A \longrightarrow \alpha$$

where 'A' is variable

$$\& \alpha \in (V+T)^*$$

Context free grammar generate context free language of type 2 language.

which is further processed by push down automata i.e. PDA.

push-down automata is a subform of parser. ~~For~~ Following are some of the IMP properties of CFG.

① Context free grammar ambiguous or unambiguous.

② Context free grammar either deterministic or non-deterministic.

- ~~context free~~ grammars Deterministic grammar generate deterministic CFL (CFL), which is further processed by deterministic push down automata.
- If, the language generated by non-deterministic CFG is known as NCFL, which is further processed by non-deterministic push down automata.
- Context free grammar are left recursive or right recursive.

### ③ Type 1 grammar-

This is type of grammar is also known as context sensitive grammar.

If all the productions of the grammar is in the form  $\alpha \rightarrow \gamma$ .

where  $\alpha \in (V+T)^*$  &  $\gamma \in (V+T)^*$  and more over length of  $\alpha$  length of  $\gamma \leq \gamma$ , then this grammar is known as context sensitive grammar (CSG).

one fact can be worth noted regarding CSG that CSG is non contracting grammar.

In the sense, the length of head is atmost equal to length of body.

### ④ Type 0 grammar-

It is also called as unrestricted grammar.

This type of grammar is supp.

used to generate recursive language as well as recursive innumerable. ~~ER~~

Both of recursive as well as recursive innumerable is commonly called as type 0 language further processed by Turing machine.

2. Write a grammar for

1.  $L = \{ a^m b^n \mid m < n \}$

2.  $L = \{ a^m b^n \mid m > n \}$

→ 1.  $L = \{ a^m b^n \mid m < n \}$   
 $m < n$   
 $m + p = n$

Rewrite the grammar

$$L = \{ a^{m+p} b^{m+p} \mid m \geq 0, p \geq 1 \}$$

$$= \{ a^m b^m \cdot b^p \mid m \geq 0, p \geq 1 \}$$

$$S \longrightarrow S_m \cdot S_p$$

$$S_m \longrightarrow a S_m \cdot b \mid \epsilon$$

$$S_p \longrightarrow b S_p \mid b$$

2.  $L = \{ a^m b^n \mid m > n \}$   
 $m > n$

$$m = n + q$$

Rewrite the grammar

$$L = \{ a^m b^n \mid m \geq 0, n \geq 1 \}$$

$$L = \{ a^n \cdot a^q \cdot b^n \mid n \geq 0, q \geq 1 \}$$

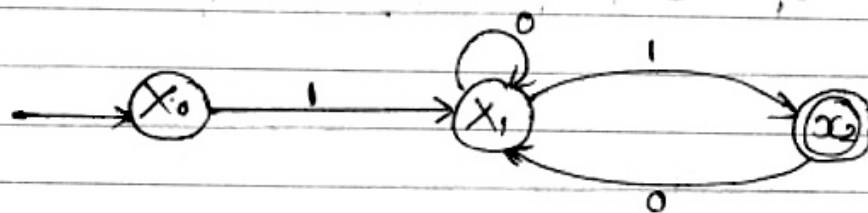
$$= \{ a^q a^n b^n \mid n \geq 0, q \geq 1 \}$$

$$S \longrightarrow S_q S_n$$

$$S_q \longrightarrow a S_q \mid a$$

$$S_n \longrightarrow a S_n b \mid \epsilon$$

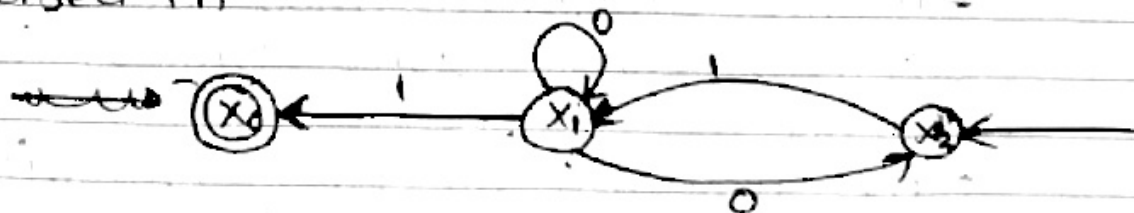
3. obtain left linear grammar for language accepted by following FA.



→ step 1 - 1<sup>st</sup> fall, we shall reverse given FA.

Remainder to reverse the FA, swap the initial & final state only & after wards swap the direction of all transition.

Reversed FA -



From this reversed FA, we can write RLG as follows

$$X_2 \longrightarrow X_1$$

$$X_1 \longrightarrow 0X_1 \mid 0X_2 \mid 1X_0$$

$x_0 \longrightarrow \epsilon$   
 upon eliminating the  $\epsilon$  production  
 grammar becomes

$$\begin{aligned}
 x_2 &\longrightarrow 1x_1 \\
 x_1 &\longrightarrow 0x_1 \mid 0x_2 \mid 1x_0 \mid 1
 \end{aligned}$$

Now, to obtain the LLG, we can reverse  
 all the productions of that rule.  
 So, the final LLG be,

$$\begin{aligned}
 x_2 &\longrightarrow x_1 1 \\
 x_1 &\longrightarrow x_1 0 \mid x_2 0 \mid x_0 1 \mid 1
 \end{aligned}$$

Q.4) Explain the concept of ambiguous grammar with example.

- - Ambiguity is one kind of impurity.
- If a grammar is contain in ambiguity then parser can't understand a grammar.
  - Such kinds of grammars can't be processed by the system.
  - The grammar must be clean & fine system can easily process of that grammar.
  - By removing all the ambiguity of the grammar, grammar become clean & fine, so, that system can easily process it.



## Concept of Ambiguous Grammar -

If a grammar has more than one LMD or more than one RMD to derive same I/p string, then such grammar is known as ambiguous grammar.

- Ambiguous grammar is always unwanted. Since, system cannot accept that grammar. In fact, system can't understand that grammar, hence system can't process the grammar.

Consider the grammar as -

$$\begin{aligned} E &\longrightarrow E + E \\ E &\longrightarrow E * E \\ E &\longrightarrow id \end{aligned}$$

with respect to this grammar  $V = \{E\}$ ,  $\Sigma = \{id, +, *\}$ ,  $S = \{E\}$ ,  $P = \{E \rightarrow E + E, E \rightarrow E * E, E \rightarrow id\}$

- Now, suppose the I/p string  $id + id * id$  is derived from this grammar.

- The grammar has more than one LMD as well as more than one RMD to derive the same I/p string  $id + id * id$ . These all derivations are expressed below.

$$\begin{aligned} \text{LMD 1: } E &\Rightarrow E + E \\ &\Rightarrow id + E \\ &\Rightarrow id + E * E \\ &\Rightarrow id + id * E \\ &\Rightarrow id + id * id \end{aligned}$$

LMD<sub>2</sub> :  $E \Rightarrow E * E$   
 $\Rightarrow E + E * E$   
 $\Rightarrow id * E * E$   
 $\Rightarrow id + id * E$   
 $\Rightarrow id + id * E$   
 $\Rightarrow id + id * id$

RMD<sub>1</sub> :  $E \Rightarrow E + E$   
 $\Rightarrow E + E * E$   
 $\Rightarrow E + E * id$   
 $\Rightarrow E + id * id$   
 $\Rightarrow id + id * id$

RMD<sub>2</sub> :  $E \Rightarrow E * E$   
 $\Rightarrow E * E$   
 $\Rightarrow E + E * id$   
 $\Rightarrow E + id * id$   
 $\Rightarrow id + id * id$

As this grammar having multiple LMD or RMD, the grammar is ambiguous.

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