Assignment 13: Spectral Imaging

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Github Link: https://github.com/pratheepkumar1/Principles-of-Color-Science

Question 1

In the m-file there is an "example" matrix to convert from 7-channel image to an approximation of XYZ. You should replace that matrix with a least-squares fit matrix (use the \ \text{operator}) that gives a better estimate of XYZ. Include your matrix in your PDF, and report the min, max, and mean Δ E00 between your estimate and the actual CCSG.

For the best fit of XYZ of the estimated image, we are using least-square fit matrix using the image pixel data and the XYZ of the reference CCSG data.

```
% Least Square Fit matrix calculation
M = (patchC\SGXYZ)';
```

| Channel 1 | -0.5039378219 | -0.4703246654 | -0.3161626315 |
|-----------|---------------|----------------|---------------|
| Channel 2 | 1.595858712 | 1.027126592 | 3.390678762 |
| Channel 3 | -2.070452355 | -1.05903866 | -2.901959291 |
| Channel 4 | 1.795691372 | 2.083162193 | 1.882669594 |
| Channel 5 | 0.4704275409 | -0.01280549722 | -0.7031008878 |
| Channel 6 | 0.4633836608 | 0.3640982394 | 0.5534212 |
| Channel 7 | -0.1844813795 | -0.1678184518 | -0.219808447 |

```
% ΔΕΘΘ between estimate and the actual CCSG and min, mean and mean value
SGDE = deltaEΘΘ(SGEstLab', SGLab')';

min_SDGE = min(SGDE);
max_SDGE = max(SGDE);
mean_SDGE = mean(SGDE);
```

| | Min | Mean | Max |
|-------|---------|--------|--------|
| ΔE*00 | 0.65033 | 1.2531 | 4.2787 |

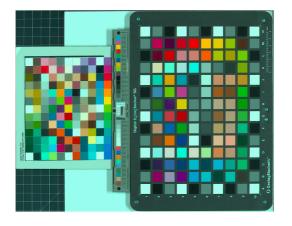
Question 2

Generate an sRGB image from the XYZ pixel data and save it as a JPG.

After applying the matrix calculated the from the previous question, we get a better color corrected sRGB image.

```
% go from Cam Signals to XYZ to sRGB
pixXYZ = (pixels)*M';
pixRGB = xyz2rgb(pixXYZ);
imgRGB = reshape(pixRGB,[nr nc 3]);
figure
imshow(imgRGB)
imwrite(imgRGB,'ImageOutput_sRGB.jpg');
```





After applying the Least Square Fit matrix

Before applying the Least Square Fit matrix

Question 3

Create a matrix to estimate spectra for each of the 140 CCSG patches. Make a plot of your matrix, like Fig. 6.42 in the book. And, make a plot of the actual and estimated spectra for the 6 patches near the middle of the CCSG: blue, green, red, yellow, magenta, cyan.

The following equation is used to calculate the transformation matrix using the spectral reflectance data of the reference and the pixel data of the Image.

$$\mathbf{M} = \begin{pmatrix} R_{\lambda=380 \text{ nm},1} & \cdots & R_{\lambda=380 \text{ nm},24} \\ \vdots & \cdots & \vdots \\ R_{\lambda=730 \text{ nm},1} & \cdots & R_{\lambda=730 \text{ nm},24} \end{pmatrix} \begin{pmatrix} C_{370 \text{ nm},1} & \cdots & C_{370 \text{ nm},24} \\ C_{450 \text{ nm},1} & \cdots & C_{450 \text{ nm},24} \\ C_{520 \text{ nm},1} & \cdots & C_{520 \text{ nm},24} \\ C_{550 \text{ nm},1} & \cdots & C_{550 \text{ nm},24} \\ C_{580 \text{ nm},1} & \cdots & C_{580 \text{ nm},24} \\ C_{600 \text{ nm},1} & \cdots & C_{600 \text{ nm},24} \\ C_{710 \text{ nm},1} & \cdots & C_{710 \text{ nm},24} \end{pmatrix}$$

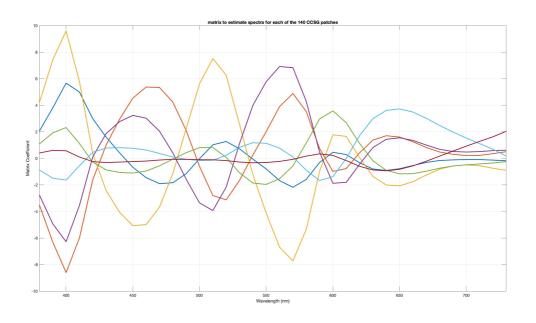
$$(6.27)$$

```
% Matrix to estimate spectra for each of the 140 CCSG patches
M_Trans = SGref*pinv(patchC');

% Plot of the Matrix
figure;
plot(SGwl,M_Trans,'LineWidth',2);
xlim([380,730]);
grid on;
xlabel('Wavelength (nm)'); ylabel('Matrix Coefficient');
title('matrix to estimate spectra for each of the 140 CCSG patches');
```

| 2.0527 | -3.5204 | 4.2005 | -2.7725 | 1.0807 | -0.8910 | 0.3985 |
|---------|---------|---------|---------|---------|---------|---------|
| 3.7974 | -6.3022 | 7.4089 | -4.9336 | 1.9132 | -1.4936 | 0.5984 |
| 5.6622 | -8.6090 | 9.5931 | -6.2856 | 2.3145 | -1.6413 | 0.5650 |
| 4.9874 | -6.0035 | 5.7814 | -3.5560 | 1.1136 | -0.5685 | 0.0953 |
| 2.9805 | -1.6176 | 0.3553 | 0.1105 | -0.2946 | 0.4533 | -0.2516 |
| 1.5973 | 0.9940 | -2.4257 | 1.8619 | -0.8717 | 0.7711 | -0.3174 |
| 0.4210 | 2.9280 | -4.0520 | 2.7522 | -1.0672 | 0.7979 | -0.2856 |
| -0.6740 | 4.5313 | -5.0743 | 3.2312 | -1.1157 | 0.7543 | -0.2486 |
| -1.4598 | 5.3648 | -4.9951 | 3.0212 | -0.9583 | 0.6249 | -0.2085 |

| -1.9102 | 5.3359 | -3.6786 | 2.0440 | -0.5736 | 0.3677 | -0.1330 |
|---------|---------|---------|---------|---------|---------|---------|
| -1.8405 | 4.2338 | -1.1472 | 0.4090 | -0.0631 | 0.0946 | -0.0746 |
| -1.1648 | 2.0962 | 2.2267 | -1.5671 | 0.4219 | -0.0691 | -0.0836 |
| -0.0348 | -0.6043 | 5.6066 | -3.3572 | 0.7987 | -0.1659 | -0.1089 |
| 1.0132 | -2.8032 | 7.5084 | -3.9364 | 0.8141 | -0.1523 | -0.1135 |
| 1.2666 | -3.1317 | 6.2579 | -2.1796 | 0.0679 | 0.2278 | -0.1734 |
| 0.7110 | -1.6673 | 2.5531 | 1.1080 | -1.0900 | 0.8206 | -0.2824 |
| -0.0614 | 0.2467 | -1.2150 | 3.9810 | -1.8640 | 1.1729 | -0.3401 |
| -0.8026 | 2.0072 | -4.1368 | 5.7718 | -1.9661 | 1.1298 | -0.3187 |
| -1.6791 | 3.8842 | -6.6889 | 6.9095 | -1.5431 | 0.7700 | -0.2367 |
| -2.1877 | 4.8814 | -7.7301 | 6.8258 | -0.5764 | 0.1038 | -0.0801 |
| -1.5935 | 3.5284 | -5.3671 | 4.3029 | 1.1478 | -0.8950 | 0.1627 |
| -0.3218 | 0.7366 | -0.9848 | 0.4681 | 2.9645 | -1.6728 | 0.3340 |
| 0.4490 | -0.9910 | 1.7693 | -1.8834 | 3.5678 | -1.3852 | 0.2147 |
| 0.2831 | -0.7722 | 1.6508 | -1.8100 | 2.6803 | -0.0081 | -0.1719 |
| -0.3402 | 0.4117 | 0.0540 | -0.4493 | 1.1221 | 1.7024 | -0.6042 |
| -0.8059 | 1.3670 | -1.3637 | 0.8097 | -0.1857 | 2.9830 | -0.8800 |
| -0.9138 | 1.6996 | -2.0118 | 1.4290 | -0.9057 | 3.6070 | -0.9438 |
| -0.7856 | 1.5971 | -2.0743 | 1.5421 | -1.1722 | 3.7190 | -0.8304 |
| -0.5478 | 1.2461 | -1.7630 | 1.3455 | -1.1588 | 3.4817 | -0.5735 |
| -0.3128 | 0.8121 | -1.2630 | 0.9959 | -0.9753 | 3.0114 | -0.2207 |
| -0.1678 | 0.4721 | -0.8178 | 0.6767 | -0.7479 | 2.4731 | 0.1622 |
| -0.1197 | 0.2980 | -0.5785 | 0.5106 | -0.5834 | 1.9744 | 0.5408 |
| -0.0955 | 0.2066 | -0.4962 | 0.4701 | -0.4932 | 1.5267 | 0.9143 |
| -0.0977 | 0.2184 | -0.5599 | 0.5033 | -0.4251 | 1.1028 | 1.2734 |
| -0.1376 | 0.3498 | -0.7517 | 0.5772 | -0.3544 | 0.6799 | 1.6201 |
| -0.1890 | 0.4978 | -0.9079 | 0.6097 | -0.2485 | 0.1632 | 2.0338 |
| | | | | | | |



```
% A plot of the actual and estimated spectra for the 6 patches
% near the middle of the CCSG: blue, green, red, yellow, magenta, cyan.

figure;
SGEst = (M_Trans*patchC');
plot(SGwl,SGEst(:,47:52),'LineWidth',2);
hold on
plot(SGwl,SGref(:,47:52),'LineWidth',0.5);
xlim[[380,730]];
xlabel('Wavelength (nm)'); ylabel('Reflectance Factor')
title('Estimated (thick lines) and Reference (thin lines) spectral reflectance')
subtitle('6 patches near the middle of the CCSG')
```

