$feature_selection$

May 15, 2020

```
[1]: # store start time to get execution time of entire script
     import time
     start_time = time.time()
[2]: import pandas as pd
     pd.set_option('display.max_rows', 500)
     pd.set_option('display.max_columns', 500)
     import csv
     df = pd.read_csv('data/data_superset.csv')
     df = df.sample(frac=1).reset_index(drop=True)
     df.head()
[2]:
        Unnamed: 0 Unnamed: 0.1 Unnamed: 0.1.1
                                                       ID State
                                                                    City \
     0
              2427
                            7157
                                             7161 16820
                                                             TX Houston
     1
              9953
                           21076
                                            21090 17753
                                                             ΑZ
                                                                  Tucson
     2
              5602
                           12216
                                            12224 19420
                                                             TX
                                                                  Laredo
     3
              3165
                             8711
                                                   11503
                                                             TX
                                                                  Laredo
                                             8717
     4
              6540
                            14056
                                            14066
                                                  18639
                                                             CA
                                                                  Downey
                                           xobsyr_0 Illicit_Days5
                                  agyaddr
                                                                    Illicit_Cens5
     0
                237 Social Work Building
                                               2011
                                                                196
                                                                                 0
        3130 E. Broadway Blvd, Suite 180
                                               2011
                                                                176
     1
                                                                                  0
     2
                        2387 E. Saunders
                                               2011
                                                                123
                                                                                  1
     3
               2386 E. Saunders, Suite 2
                                               2008
                                                                 30
                                                                                  1
     4
                    11500 Paramount Blvd
                                               2010
                                                                365
        female_cd nonwhite_cd unemplmt_cd prsatx_cd gvsg_cd CWSg_0_cd
     0
                0
                              1
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                0
                              1
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        srprobg_cd dssg_0_cd epsg_0_cd adhdg_0_cd cdsg_0_cd cjsig_0_cd \
     0
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     1
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2
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   lrig_0_cd srig_0_cd SESg_0_cd r4ag_0_cd primsev_cd_1 primsev_cd_2
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   primsev_cd_3 primsev_cd_4 primsev_cd_5 primsev_cd_6
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                                                                   2
              1
                                          Address
                                                          lat
                                                                      lng
          237 Social Work Building, Houston, TX 29.948496
                                                              -95.470979
0
   3130 E. Broadway Blvd, Suite 180, Tucson, AZ
1
                                                   32.221465 -110.926070
2
                    2387 E. Saunders, Laredo, TX
                                                   27.530458 -99.472336
3
          2386 E. Saunders, Suite 2, Laredo, TX
                                                  27.530608 -99.472335
4
                11500 Paramount Blvd, Downey, CA 33.930804 -118.146842
   state name
               county FIPS
                               block_FIPS murder_numg %_dropoutg %_povertyg
        Texas
                    48201.0 4.820155e+14
                                                                 0.0
0
                                                                              0.0
1
      Arizona
                     4019.0 4.019002e+13
                                                                 0.0
                                                                              0.0
2
        Texas
                    48479.0 4.847900e+14
                                                       0
                                                                 0.0
                                                                              1.0
                    48479.0 4.847900e+14
                                                       0
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                                                                              1.0
3
        Texas
   California
                     6037.0 6.037552e+13
                                                       0
                                                                 0.0
                                                                              0.0
   %_public_assistanceg %_unemployedg
                                                               closest
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                                                                   NaN
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3
                     0.0
                                    0.0
                                          ('27.530608', '-99.472335')
                                                                         2.0
                     0.0
                                    0.0
                                                                   NaN
                                                                         1.0
                                    point
                                            pop_deng
    ('29.94849600000002', '-95.470979')
0
1
   ('32.2214651', '-110.92607029999999')
                                                 0.0
2
    ('27.530458000000003', '-99.472336')
                                                 0.0
3
             ('27.530608', '-99.472335')
                                                 0.0
  ('33.9308039', '-118.14684199999999')
                                                 0.0
```

```
[3]: # drop unnecessary columns
     cols_to_drop = ['Address','lat','lng','xobsyr_0','Unnamed: 0','Unnamed: 0.
      \hookrightarrow1', 'Unnamed: 0.1.1',
      →'ID', 'State', 'City', 'agyaddr', 'state_name', 'gran', 'srprobg_cd', 'county_FIPS', 'block_FIPS',
                       'point','closest','SUDSy_0']
     df.drop(columns=cols_to_drop, inplace=True)
     df.head()
[3]:
        Illicit_Days5
                         Illicit_Cens5
                                         female_cd nonwhite_cd unemplmt_cd
     0
                   196
                                      0
                                                  0
                                                                               0
     1
                   176
                                      0
                                                  1
                                                                 1
                                                                               0
     2
                   123
                                      1
                                                  0
                                                                 1
                                                                               1
     3
                    30
                                                  0
                                                                               0
                                      1
                   365
        prsatx_cd
                   gvsg_cd CWSg_0_cd dssg_0_cd epsg_0_cd adhdg_0_cd cdsg_0_cd
     0
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     4
                 0
                           1
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        cjsig_0_cd lrig_0_cd srig_0_cd SESg_0_cd r4ag_0_cd primsev_cd_1
     0
                              2
                                          2
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                                                                                  0
                  1
     1
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                              1
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                  2
                               1
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                               2
                  0
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        primsev_cd_2 primsev_cd_3 primsev_cd_4 primsev_cd_5
                                                                      primsev_cd_6
     0
                                    1
     1
                    0
                                    1
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                                                                   0
                                                                                  0
     2
                    0
                                    0
                                                   0
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                                                                                  0
     3
                    1
                    0
     4
                                    1
                                                   0
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                                                                                  0
                 murder_numg %_dropoutg %_povertyg %_public_assistanceg
     0
                                       0.0
                                                    0.0
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              1
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              1
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     1
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                                                     1.0
                                                                             0.0
              2
                                       0.0
                                                    0.0
                                                                             0.0
        %_unemployedg pop_deng
```

0.0

0.0

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    1
    0.0
    0.0

    2
    0.0
    0.0

    3
    0.0
    0.0

    4
    0.0
    0.0
```

(10068, 28) (10068,)

```
[5]: import numpy as np
     from sklearn.model_selection import cross_validate
     def forward_feature_selection(model, X, y):
         selected_features = []
         score = -1
         while (True):
             temp score = -1
             next feature = None
             for f in X.columns:
                 if f not in selected_features:
                     selected_features.append(f)
                     temp = X[selected_features]
                     scores = cross_validate(model, temp, y, cv=5)
                     s = scores['test_score'].mean()
                     #print(selected_features, '->', s)
                     if s > temp_score:
                         temp_score = s
                         next_feature = f
                     selected_features.pop()
             if temp_score <= score: # stop if no more change in improvement</pre>
                 print('Optimal Features:', selected_features)
                 print('Optimal Score:', score)
```

```
break
else:
    selected_features.append(next_feature)
    score = temp_score
print('Added Feature:', next_feature)
print('Score:', score)

return selected_features
```

```
[6]: def backward_feature_selection(model, X, y):
         selected_features = list(X.columns)
         score = -1
         while (True):
             temp_score = -1
             worst_feature = None
             for i in range(len(selected features)):
                 f = selected_features.pop()
                 temp = X[selected_features]
                 scores = cross_validate(model, temp, y, cv=5)
                 s = scores['test_score'].mean()
                 #print(selected_features, '->', s)
                 if s > temp_score:
                     temp_score = s
                     worst_feature = f
                 selected_features.insert(0, f)
             if temp_score <= score: # stop if no more change in improvement</pre>
                 print('Optimal Features:', selected_features)
                 print('Optimal Score:', score)
                 break
             else:
                 selected_features.remove(worst_feature)
                 score = temp_score
             print('Dropped Feature:', worst_feature)
             print('Score:', score)
         return selected_features
```

```
[7]: def feature_selection_statistics(FFS, BFS, features):
    stats = {}

    FFS = np.array(FFS)
    BFS = np.array(BFS)
    features = np.array(features)
```

```
stats['Both_Used'] = list(np.intersect1d(FFS, BFS))
stats['FFS_Used'] = list(np.setdiff1d(FFS, stats['Both_Used']))
stats['BFS_Used'] = list(np.setdiff1d(BFS, stats['Both_Used']))
stats['Both_Dropped'] = list(np.setdiff1d(features, np.union1d(FFS, BFS)))
stats['FFS_Dropped'] = list(np.setdiff1d(features, np.union1d(FFS, u)))
stats['Both_Dropped'])))
stats['BFS_Dropped'] = list(np.setdiff1d(features, np.union1d(BFS, u)))
stats['Both_Dropped'])))
```

[8]: %%time from sksurv.linear_model import CoxnetSurvivalAnalysis # l1_ratio = 1 adjusts model to implement LASSO method for penalties rcr = CoxnetSurvivalAnalysis(l1_ratio=1) rcr_BFS = backward_feature_selection(rcr, X, y)

Dropped Feature: pop_deng Score: 0.6760885893770648 Dropped Feature: B2a_0g Score: 0.676574105529251 Dropped Feature: female cd Score: 0.6768420522968134 Dropped Feature: murder_numg Score: 0.677134228100414 Dropped Feature: lrig 0 cd Score: 0.6773121646009029 Dropped Feature: primsev cd 1 Score: 0.6774121386230144 Dropped Feature: primsev cd 2 Score: 0.6775436141724663 Dropped Feature: unemplmt_cd Score: 0.6775989077777093 Dropped Feature: gvsg_cd Score: 0.6776179053764813 Dropped Feature: primsev_cd_3 Score: 0.6776434242487729 Dropped Feature: %_dropoutg Score: 0.6776588129011195 Optimal Features: ['nonwhite_cd', 'prsatx_cd', 'CWSg_0_cd', 'dssg_0_cd', 'epsg_0_cd', 'adhdg_0_cd', 'cdsg_0_cd', 'cjsig_0_cd', 'srig_0_cd', 'SESg_0_cd', 'r4ag_0_cd', 'primsev_cd_4', 'primsev_cd_5', 'primsev_cd_6', '%_povertyg', '% public assistanceg', '% unemployedg'] Optimal Score: 0.6776588129011195 CPU times: user 4min 18s, sys: 18.5 s, total: 4min 37s Wall time: 2min 48s

```
[9]: %%time
     rcr_FFS = forward_feature_selection(rcr, X, y)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
      estimator.fit(X_train, y_train, **fit_params)
    //anaconda3/lib/python3.7/site-
    packages/sklearn/model_selection/_validation.py:514: UserWarning: all
    coefficients are zero, consider decreasing alpha.
```

```
estimator.fit(X_train, y_train, **fit_params)
//anaconda3/lib/python3.7/site-
packages/sklearn/model_selection/_validation.py:514: UserWarning: all
coefficients are zero, consider decreasing alpha.
  estimator.fit(X train, y train, **fit params)
//anaconda3/lib/python3.7/site-
packages/sklearn/model selection/ validation.py:514: UserWarning: all
coefficients are zero, consider decreasing alpha.
  estimator.fit(X_train, y_train, **fit_params)
//anaconda3/lib/python3.7/site-
packages/sklearn/model_selection/validation.py:514: UserWarning: all
coefficients are zero, consider decreasing alpha.
  estimator.fit(X_train, y_train, **fit_params)
//anaconda3/lib/python3.7/site-
packages/sklearn/model_selection/_validation.py:514: UserWarning: all
coefficients are zero, consider decreasing alpha.
  estimator.fit(X_train, y_train, **fit_params)
Added Feature: dssg_0_cd
Score: 0.600963905872708
Added Feature: r4ag_0_cd
Score: 0.6345411519078523
Added Feature: prsatx cd
Score: 0.6437760250287912
Added Feature: SESg 0 cd
Score: 0.6529195463131539
Added Feature: cdsg_0_cd
Score: 0.6597671702588404
Added Feature: primsev_cd_5
Score: 0.6647272241326584
Added Feature: %_povertyg
Score: 0.669344880133808
Added Feature: srig_0_cd
Score: 0.6717639311559671
Added Feature: nonwhite_cd
Score: 0.6737998469686873
Added Feature: cjsig_0_cd
Score: 0.6751984384041073
Added Feature: primsev_cd_6
Score: 0.6764908552122334
Added Feature: adhdg 0 cd
Score: 0.676991134853712
Added Feature: primsev_cd_4
Score: 0.6773298106150195
Added Feature: CWSg_0_cd
Score: 0.6775957246817649
Added Feature: epsg_0_cd
Score: 0.6776605413963954
```

```
Added Feature: primsev_cd_2
     Score: 0.6777095112305578
     Optimal Features: ['dssg_0_cd', 'r4ag_0_cd', 'prsatx_cd', 'SESg_0_cd',
     'cdsg_0_cd', 'primsev_cd_5', '%_povertyg', 'srig_0_cd', 'nonwhite_cd',
     'cjsig_0_cd', 'primsev_cd_6', 'adhdg_0_cd', 'primsev_cd_4', 'CWSg_0_cd',
     'epsg_0_cd', 'primsev_cd_2']
     Optimal Score: 0.6777095112305578
     CPU times: user 3min 6s, sys: 12.3 s, total: 3min 19s
     Wall time: 2min 4s
[10]: import json
      stats = feature_selection_statistics(rcr_FFS, rcr_BFS, X.columns)
      print(json.dumps(stats, indent=1))
     {
      "Both_Used": [
       "%_povertyg",
       "CWSg_0_cd",
       "SESg_0_cd",
       "adhdg_0_cd",
       "cdsg_0_cd",
       "cjsig_0_cd",
       "dssg_0_cd",
       "epsg_0_cd",
       "nonwhite_cd",
       "primsev_cd_4",
       "primsev_cd_5",
       "primsev_cd_6",
       "prsatx_cd",
       "r4ag_0_cd",
       "srig_0_cd"
      ],
      "FFS_Used": [
       "primsev_cd_2"
      ],
      "BFS_Used": [
       "%_public_assistanceg",
       "%_unemployedg"
      ],
      "Both_Dropped": [
       "%_dropoutg",
       "B2a 0g",
       "female_cd",
       "gvsg_cd",
       "lrig_0_cd",
       "murder_numg",
       "pop_deng",
```

```
"primsev_cd_1",
       "primsev_cd_3",
       "unemplmt_cd"
      ],
      "FFS Dropped": [
       "%_public_assistanceg",
       "% unemployedg"
      ],
      "BFS Dropped": [
       "primsev_cd_2"
      ]
     }
[11]: %%time
      from sksurv.ensemble import RandomSurvivalForest
      rsf = RandomSurvivalForest()
      rsf_BFS = backward_feature_selection(rsf, X, y)
     //anaconda3/lib/python3.7/importlib/_bootstrap.py:219: RuntimeWarning:
     sklearn.tree._splitter.Splitter size changed, may indicate binary
     incompatibility. Expected 360 from C header, got 368 from PyObject
       return f(*args, **kwds)
     Dropped Feature: %_dropoutg
     Score: 0.6708214947596508
     Optimal Features: ['female_cd', 'nonwhite_cd', 'unemplmt_cd', 'prsatx_cd',
     'gvsg_cd', 'CWSg_0_cd', 'dssg_0_cd', 'epsg_0_cd', 'adhdg_0_cd', 'cdsg_0_cd',
     'cjsig_0_cd', 'lrig_0_cd', 'srig_0_cd', 'SESg_0_cd', 'r4ag_0_cd',
     'primsev_cd_1', 'primsev_cd_2', 'primsev_cd_3', 'primsev_cd_4', 'primsev_cd_5',
     'primsev_cd_6', 'B2a_0g', 'murder_numg', '%_povertyg', '%_public_assistanceg',
     '%_unemployedg', 'pop_deng']
     Optimal Score: 0.6708214947596508
     CPU times: user 16min 38s, sys: 1min 56s, total: 18min 35s
     Wall time: 19min 39s
[12]: %%time
      rsf_FFS = forward_feature_selection(rsf, X, y)
     Added Feature: dssg_0_cd
     Score: 0.600963905872708
     Added Feature: r4ag_0_cd
     Score: 0.6346451627823293
     Added Feature: SESg_0_cd
     Score: 0.6457088110003675
     Added Feature: prsatx cd
     Score: 0.6508620358535185
```

```
Added Feature: primsev_cd_5
     Score: 0.6531618457422678
     Added Feature: primsev_cd_6
     Score: 0.6559288379752741
     Added Feature: murder numg
     Score: 0.6593064367668062
     Added Feature: % unemployedg
     Score: 0.6593630386617033
     Added Feature: %_public_assistanceg
     Score: 0.6597501463910019
     Optimal Features: ['dssg_0_cd', 'r4ag_0_cd', 'SESg_0_cd', 'prsatx_cd',
     'primsev_cd_5', 'primsev_cd_6', 'murder_numg', '%_unemployedg',
     '%_public_assistanceg']
     Optimal Score: 0.6597501463910019
     CPU times: user 21min 27s, sys: 1min 1s, total: 22min 29s
     Wall time: 23min 30s
[13]: stats = feature_selection_statistics(rsf_FFS, rsf_BFS, X.columns)
      print(json.dumps(stats, indent=1))
     {
      "Both_Used": [
       "% public assistanceg",
       "%_unemployedg",
       "SESg_0_cd",
       "dssg_0_cd",
       "murder_numg",
       "primsev_cd_5",
       "primsev_cd_6",
       "prsatx_cd",
       "r4ag_0_cd"
      ],
      "FFS_Used": [],
      "BFS_Used": [
       "%_povertyg",
       "B2a_0g",
       "CWSg_0_cd",
       "adhdg_0_cd",
       "cdsg_0_cd",
       "cjsig_0_cd",
       "epsg_0_cd",
       "female_cd",
       "gvsg_cd",
       "lrig_0_cd",
       "nonwhite_cd",
       "pop_deng",
       "primsev_cd_1",
       "primsev_cd_2",
```

```
"primsev_cd_3",
       "primsev_cd_4",
       "srig_0_cd",
       "unemplmt_cd"
      ],
      "Both_Dropped": [
       "%_dropoutg"
      ],
      "FFS_Dropped": [
       "%_povertyg",
       "B2a_0g",
       "CWSg_0_cd",
       "adhdg_0_cd",
       "cdsg_0_cd",
       "cjsig_0_cd",
       "epsg_0_cd",
       "female_cd",
       "gvsg_cd",
       "lrig_0_cd",
       "nonwhite_cd",
       "pop_deng",
       "primsev_cd_1",
       "primsev_cd_2",
       "primsev_cd_3",
       "primsev_cd_4",
       "srig_0_cd",
       "unemplmt_cd"
      ],
      "BFS_Dropped": []
     }
[14]: # print out total notebook execution time
      total_seconds = int(time.time() - start_time)
      minutes = total_seconds // 60
      seconds = total_seconds % 60
      print("--- " + str(minutes) + " minutes " + str(seconds) + " seconds ---")
     --- 48 minutes 5 seconds ---
```