

* Interference of Light

The phenomenon in which two coherent light waves combine to form a resultant wave of greater or lower amplitude.

Types

- a) Constructive interference : If a crest of one wave .

Introduction :

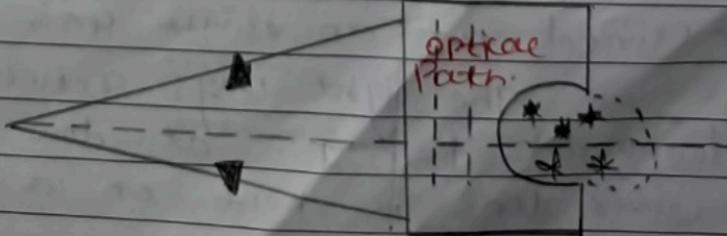
Optics is one of the special branch in Physics which deals with the study of Behaviour & Properties of light.

There are two types of optics light as a collection of rays that travel in a straight line.

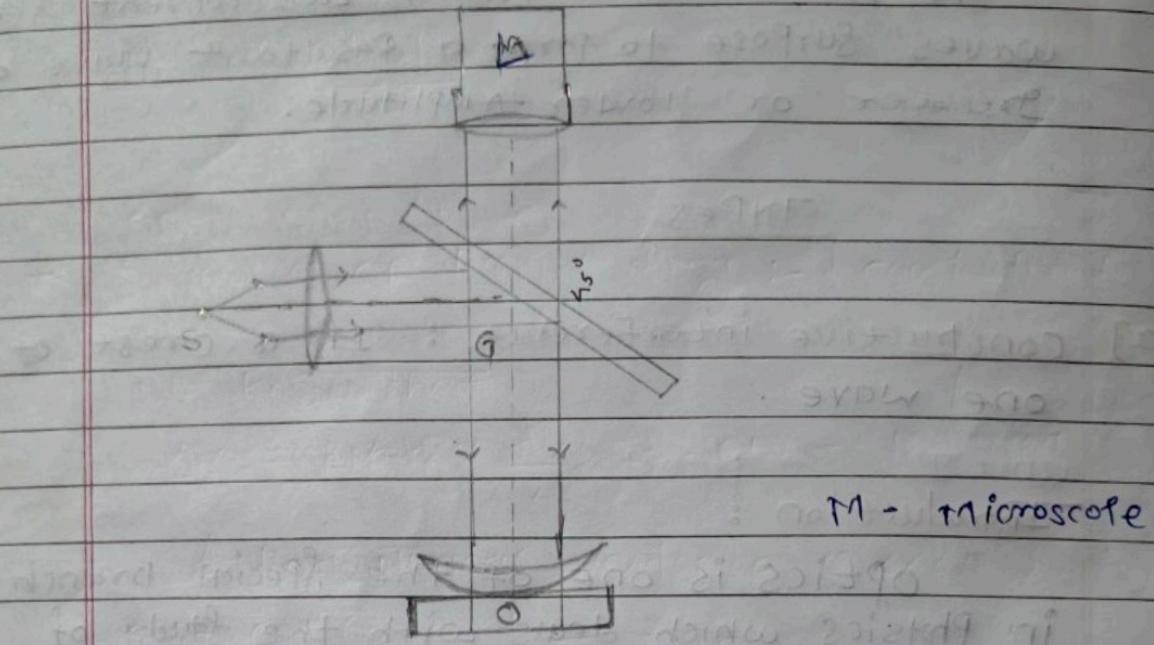
In Physical optics light travel as a wave.

Optical Path ::

Optical Path is a optical medium path where light can travel.



* Newton's Ring :



In above diagram experimental arrangement of newton's ring is shown in diagram

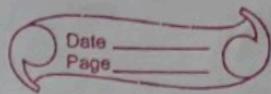
- S is source of monochromatic light.
 - L is converging lens / convex
 - G is glass plate
 - O is centre of plane-convex lens
- are arranged neatly.

A parallel beam of monochromatic light is incident on lens L, the light ray travelling as a wave ~~light~~ guide.

It fall on glass plate (G) which is inclined at an angle 45° .

The light rays reflected towards downwards from G. at downward plane-convex lens is kept on a glass plate.

bright - constructive interference
dark - destructive interference.



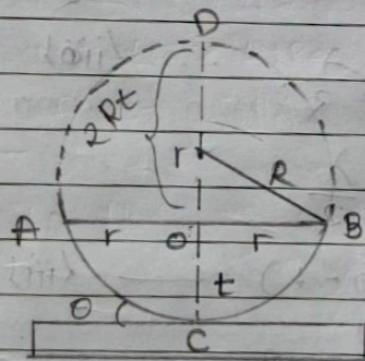
After falling light rays on plano-convex lens, it gets back reflected to upward direction. where microscope is arranged.

the

the two light rays produced upper & lower constructive and destructive interference due to plano-convex lens.

It is observed that the dark & bright concentric rings at point of contact O this is called as newton's ring.

Diameter of Newton's Ring ::



AB - length of planoconvex lens

OC - thickness of planoconvex lens.

from property of circle

$$\text{AO} \times \text{OB} = \text{OC} \times \text{OD}$$

$$r \times r = t \times 2R - t$$

$$r^2 = t \times 2R \quad \{ \text{or } t \gg R \text{ so } t \text{ is neglected.} \}$$

$$t = \frac{r^2}{2R} \quad (\text{i})$$

Eqn (i) is thickness of diameter.

$$D = 2R = \frac{r^2}{\mu}$$

Eqn (ii) is thickness of planar concave lens of Newton's Ring.

* Diameter of Bright Ring :- {constructive interference}

We know that,

$$\Delta x = \text{Even} \times \frac{\lambda}{2} \quad \rightarrow - \left\{ \begin{array}{l} \text{for} \\ \text{maxima} \end{array} \right\}$$

(For Normal incidence $\theta \ll \alpha$)

$$2ut \cos(\alpha + \theta) + \frac{\lambda}{2} = 2n \frac{\lambda}{2} \quad \dots (i)$$

$$2ut + \frac{\lambda}{2} = 2n \frac{\lambda}{2} \quad \dots (ii)$$

$$2ut = 2n \frac{\lambda}{2} - \frac{\lambda}{2}$$

$$2ut = \frac{\lambda}{2} (2n - 1) \quad \dots (iii)$$

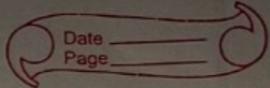
Put the value of t in Eqn (iii)

$$2u \left(\frac{r^2}{\lambda R} \right) = \frac{\lambda}{2} (2n - 1)$$

$$r^2 = \frac{(2n - 1) \lambda R}{2u}$$

$$r^2 = \frac{(2n - 1) \lambda R}{2} \quad \left\{ \begin{array}{l} \because \mu = \text{value due to} \\ \text{air arrived} \end{array} \right\}$$

D - diameter
radius (r) = $\frac{Dn^2}{2}$



$$\left(\frac{Dn}{2}\right)^2 = \frac{(2n-1)AR}{2}$$

$$(Dn)^2 = \frac{4r^2(2n-1)AR}{2}$$

$$Dn = \sqrt{2(2n-1)AR} \quad \rightarrow \text{inv}$$

$$Dn \propto (2n-1)$$

* Diameter of Newton Dark Ring :- {destructive inter.}

We know that

{Minima}

$$\Delta x = \text{odd} \times \frac{\lambda}{2}$$

$$2ut \left[\cos(r+t) \right] + \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2} \quad (1)$$

$$2ut = (2n+1) \frac{\lambda}{2} - \frac{\lambda}{2} \quad (2)$$

$$2ut = 2n \frac{\lambda}{2} + \frac{\lambda}{2} - \frac{\lambda}{2}$$

$$2ut = 2n \frac{\lambda}{2}$$

$$2ut = nd \quad \# (3)$$

Put the value of t in eqn ③

$$2u \left(\frac{r^2}{2R} \right) = nd$$

$$ur^2 = nd$$

on OnePlus



$$r^2 = \frac{nDR}{u}$$

$$\left(\frac{dn}{2}\right)^2 = \frac{nDR}{u}$$

$$\left(\frac{dn^2}{2}\right) = \frac{nDR}{u}$$

$$dn^2 = \frac{4nDR}{u}$$

$$dn^2 = 4nDR \quad \{u=2\}$$

$$dn = 2\sqrt{nDR} \quad (4)$$

$$dn = 2\sqrt{nDR}$$

Applications of Newton's Ring :-

There are many applications of Newton's Ring following are few applications of Newton's Ring

- i) Determination of wavelength of monochromatic Light.
- ii) Determination of refractive index of medium
- iii) Newton's Ring in Anti-reflective coatings.

Determination of wavelength of monochromatic light.

The diameter of Newton's dark ring is

$$D_n = \sqrt{4ndR} \quad \textcircled{I}$$

Similarly, the diameter of $(n+p)$ upcoming ring is $D_{n+p} = \sqrt{4(n+p)dR} \quad \textcircled{II}$

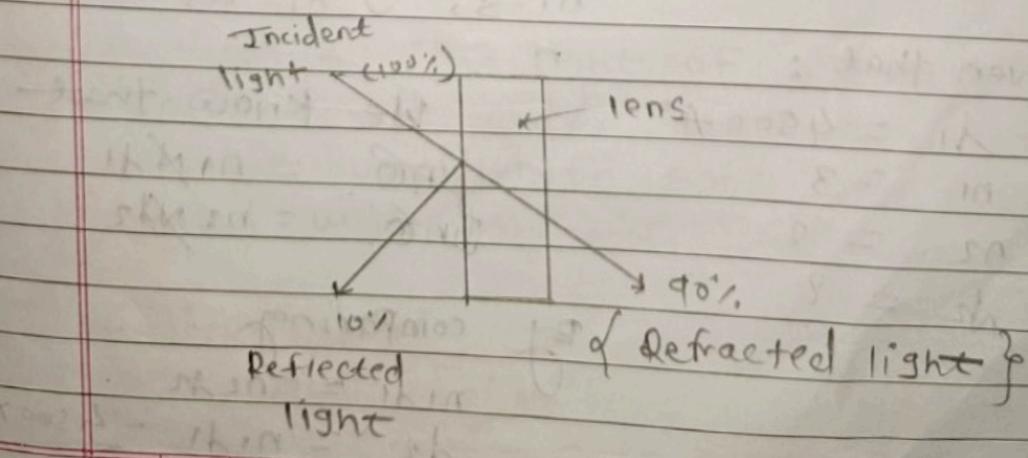
from \textcircled{I} & \textcircled{II}

$$d = D_n^2$$

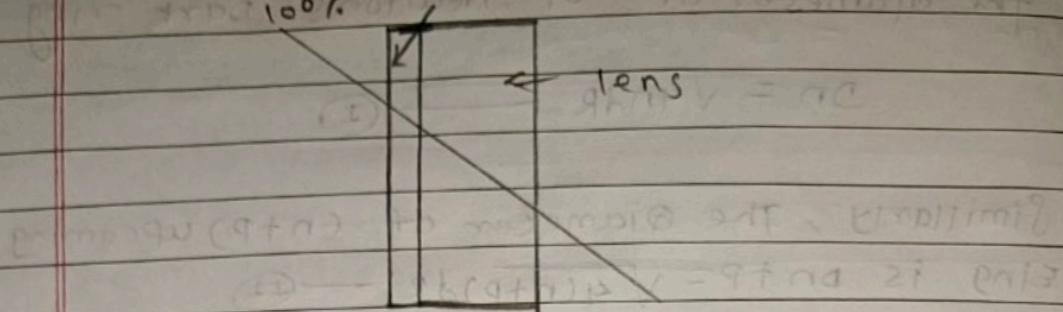
- Application of Newton's ring in Antireflective coating.

-Antireflective coating minimize the reflection of one or many wavelength and are typically used on surface lenses so that minimum light is lost.

- Lens without Anti-Reflection coating.



- Lens with Anti-reflection coating :
Incident Light.



Following are some examples where AR Coatings are done.

For Ex. : (i) Spectacles (ii) Camera lenses
(iii) Laptop screen (iv) LED & LCD Screen etc.



Numericals :

problem 10 : In case of plane diffraction

Creating in 2nd order maxima having wavelength 45000 Å coincide with 3rd order maxima of unknown wavelength. Calculate unknown wavelength.

$$n_1 = 3, \lambda_1 = 45000 \text{ Å}$$

Soln : Given that :

$$\lambda_1 = 45000 \text{ Å}$$

$$n_1 = 3$$

$$n_2 = ?$$

$$n_2 = ?$$

We know that

$$\sin \theta_1 = n_1 \times d_1$$

$$\sin \theta_2 = n_2 \times d_2$$

By comparing ...

$$n_1 d_1 = n_2 d_2$$

$$d_2 = \frac{n_1 d_1 - 45000 \times 3}{n_2} = \frac{45000 \times 3}{2}$$

$$\begin{array}{r} 6750 \\ + 3500 \\ \hline 10250 \end{array} = 6750\text{A}^\circ$$

problem 2 : If sodium light of wavelength 5893A° has doublet of 6A° , calculate total no. of lines present on Grafting to Ruone the doublet of 3^{rd} order.

Soln Given that,

$$\lambda = 5893 \text{ A}^\circ$$

$$d_1 = 6\text{A}^\circ$$

$$n/m = 3$$

$$N = ?$$

We know that....

$$\text{R.P. } \frac{1}{d_1} = m/n \cdot N$$

$$N = \frac{1}{n \times d_1} = \frac{5893}{3 \times 6}$$

$$= 327.3811$$

$$N = 327.$$

problem 3 : The light of wavelength 5890A° in the 4th order overlaps with unknown wavelength in a 5th order. Find unknown wavelength.

Given that

$$d_1 = 5890\text{A}^\circ$$

$$n_1 = 4$$

$$n_2 = 5 \quad d = ?$$

We know that

$$\sin \theta = n_1 \cancel{\propto} d_1$$

$$\sin \theta = n_2 \cancel{\propto} d_2$$

$$\therefore \frac{d_1}{n_1} = n_2 d_2$$

$$d_2 = \frac{n_1 d_1}{n_2}$$

$$= \frac{4 \times 5890}{5} = 4712 \text{ A}^\circ$$

$$\therefore d_2 = 4712 \text{ A}^\circ$$