VECTORS

$f 1 \quad 12^{th} \; { m Maths}$ - EXERCISE-10.3

1. Find $|\overrightarrow{a}|$ and $|\overrightarrow{b}|$, if $(\overrightarrow{a}+\overrightarrow{b}).(\overrightarrow{a}-\overrightarrow{b})=8$ and $\overrightarrow{a}=8|\overrightarrow{b}|$.

Solution: Given points are

$$(\overrightarrow{a} + \overrightarrow{b}).(\overrightarrow{a} - \overrightarrow{b}) = 8 \tag{1}$$

$$|\overrightarrow{a}| = 8 \left| \overrightarrow{b} \right| \tag{2}$$

$$(\overrightarrow{a} + \overrightarrow{b}).(\overrightarrow{a} - \overrightarrow{b}) = 8 \tag{3}$$

$$\overrightarrow{a}.(\overrightarrow{a}-\overrightarrow{b})+\overrightarrow{b}.(\overrightarrow{a}-\overrightarrow{b})=8 \tag{4}$$

$$\overrightarrow{a}.\overrightarrow{a} - \overrightarrow{a}.\overrightarrow{b} + \overrightarrow{b}.\overrightarrow{a} - \overrightarrow{b}.\overrightarrow{b} = 8$$
 (5)

$$\overrightarrow{a}.\overrightarrow{a} - \overrightarrow{a}.\overrightarrow{b} + \overrightarrow{a}.\overrightarrow{b} - \overrightarrow{b}.\overrightarrow{b} = 8 \tag{6}$$

$$\overrightarrow{a}.\overrightarrow{a} - \overrightarrow{b}.\overrightarrow{b} = 8 \tag{7}$$

$$(|\overrightarrow{a}|)^2 - (|\overrightarrow{b}|)^2 = 8 \tag{8}$$

$$(\left|8\overrightarrow{b}\right|)^2 - (\left|\overrightarrow{b}\right|)^2 = 8 \tag{9}$$

$$64\overrightarrow{b}^2 - \overrightarrow{b}^2 = 8 \tag{10}$$

$$63\overrightarrow{b}^2 = 8 \tag{11}$$

$$\overrightarrow{b}^2 = \frac{8}{63} \tag{12}$$

$$\overrightarrow{b} = \sqrt{\frac{8}{63}} \tag{13}$$

$$\overrightarrow{b} = \frac{2\sqrt{2}}{3\sqrt{7}} \tag{14}$$

$$|\overrightarrow{a}| = 8 \left| \overrightarrow{b} \right| \tag{15}$$

$$|\overrightarrow{a}| = 8.\frac{2\sqrt{2}}{3\sqrt{7}}\tag{16}$$

$$|\overrightarrow{a}| = \frac{16\sqrt{2}}{3\sqrt{7}}\tag{17}$$