

# PROBLEM ON KMAP

Q. How many minimal expressions are represented by following Kmap

RS \ PQ	00	01	11	10
00	0	1	1	1
01	1	1	0	1
11	0	1	1	1
10	1	1	0	1

10 PI - 12 MT

	1	2	4	5	6	7	8	9	10	11	12	15
$\checkmark \bar{P}\bar{Q}$			$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$						
$\checkmark P\bar{Q}$							$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$		
$\checkmark \bar{Q}\bar{R}\bar{S}$			$\checkmark$								$\checkmark$	
$\times \bar{P}R\bar{S}$							$\checkmark$				$\checkmark$	
$\checkmark \bar{P}R\bar{S}$	$\checkmark$			$\checkmark$								
$\times \bar{Q}R\bar{S}$	$\checkmark$							$\checkmark$				
$\checkmark \bar{Q}R\bar{S}$						$\checkmark$						$\checkmark$
$\times \bar{P}R\bar{S}$										$\checkmark$		$\checkmark$
$\checkmark \bar{Q}R\bar{S}$		$\checkmark$							$\checkmark$			
$\times \bar{P}R\bar{S}$		$\checkmark$			$\checkmark$							

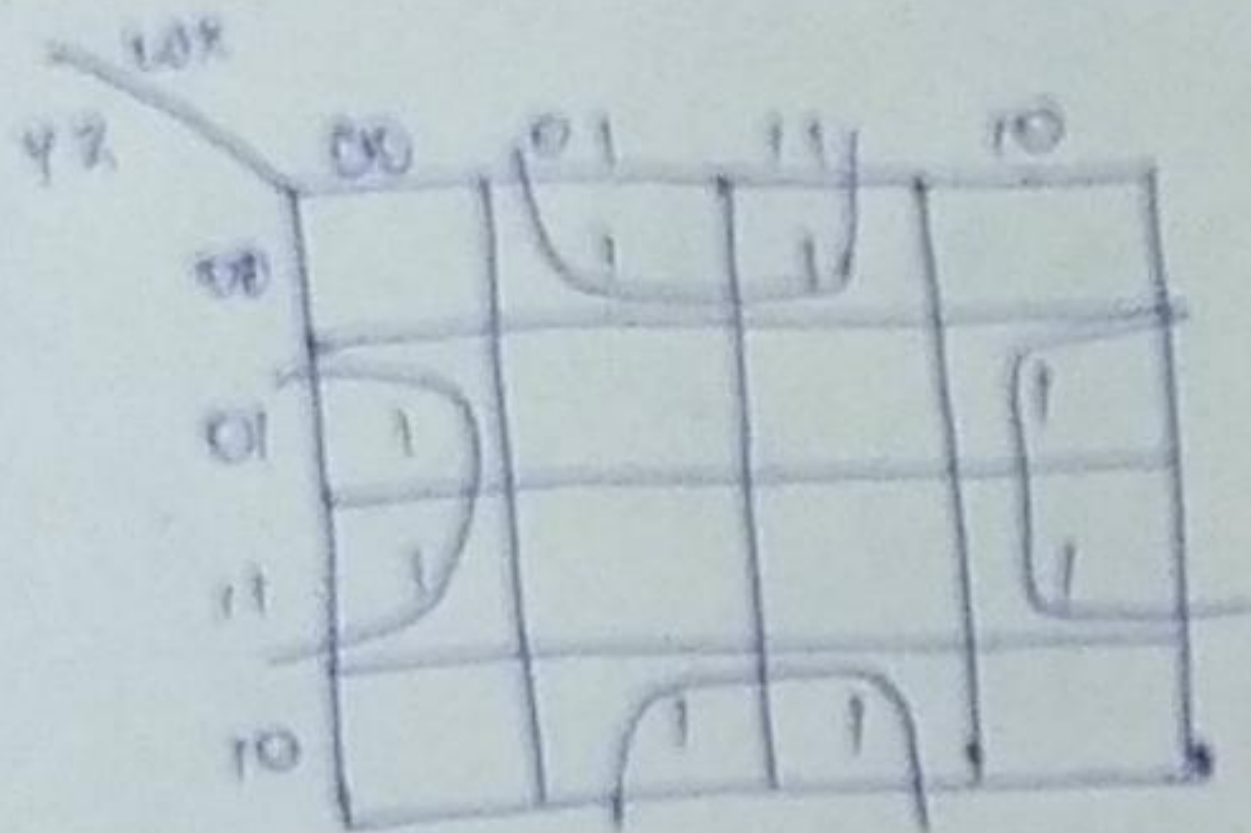
$$SOP = \bar{P}\bar{Q} + P\bar{Q} + \bar{Q}\bar{R}\bar{S} + \bar{P}R\bar{S} + \bar{Q}R\bar{S} + \bar{Q}R\bar{S}$$

$$\# \text{ minimal expression} = 2^4 = 16$$



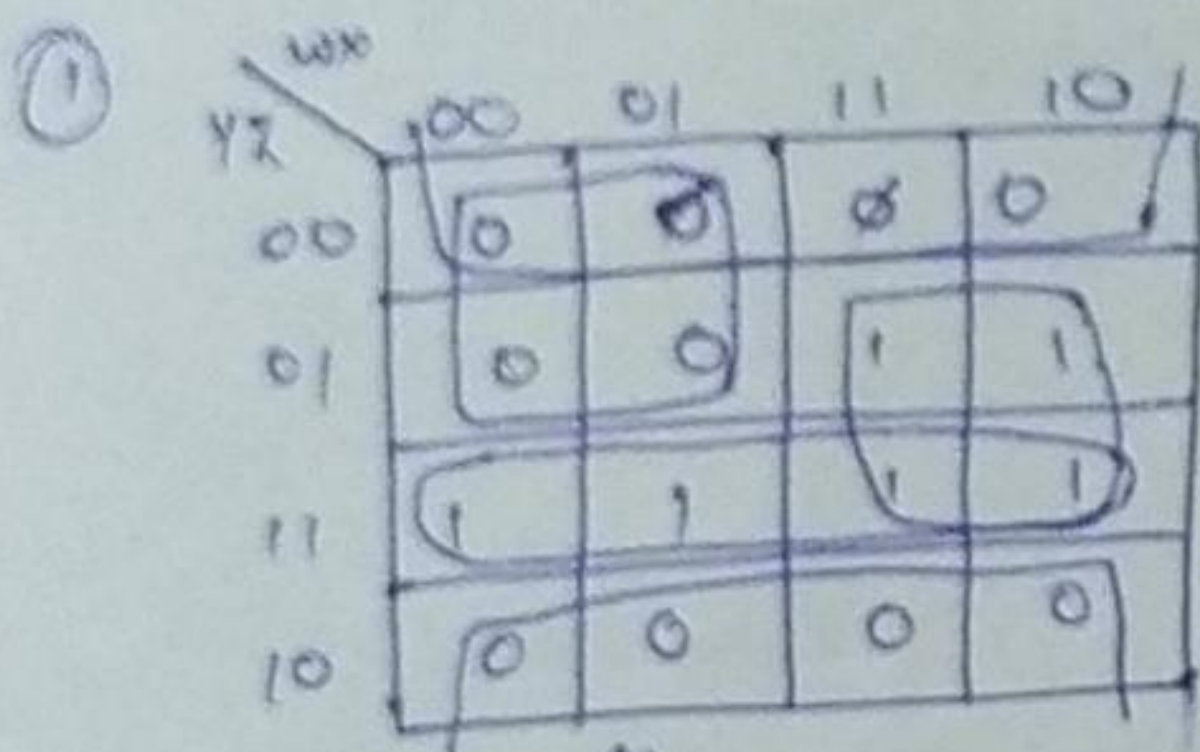
# FINDING THE FREE VARIABLES

Q. How many variables are free in the expression denoted by the following map?



$$\begin{aligned} \text{SOP} &= X\bar{Z} + \bar{X}Z \\ \text{POS} &= (X+Z)(\bar{X}+\bar{Z}) \\ \# \text{ free variable} &= 2 \quad (\text{as } 4) \end{aligned}$$

RELATION B/W POS & SOP in case of don't care

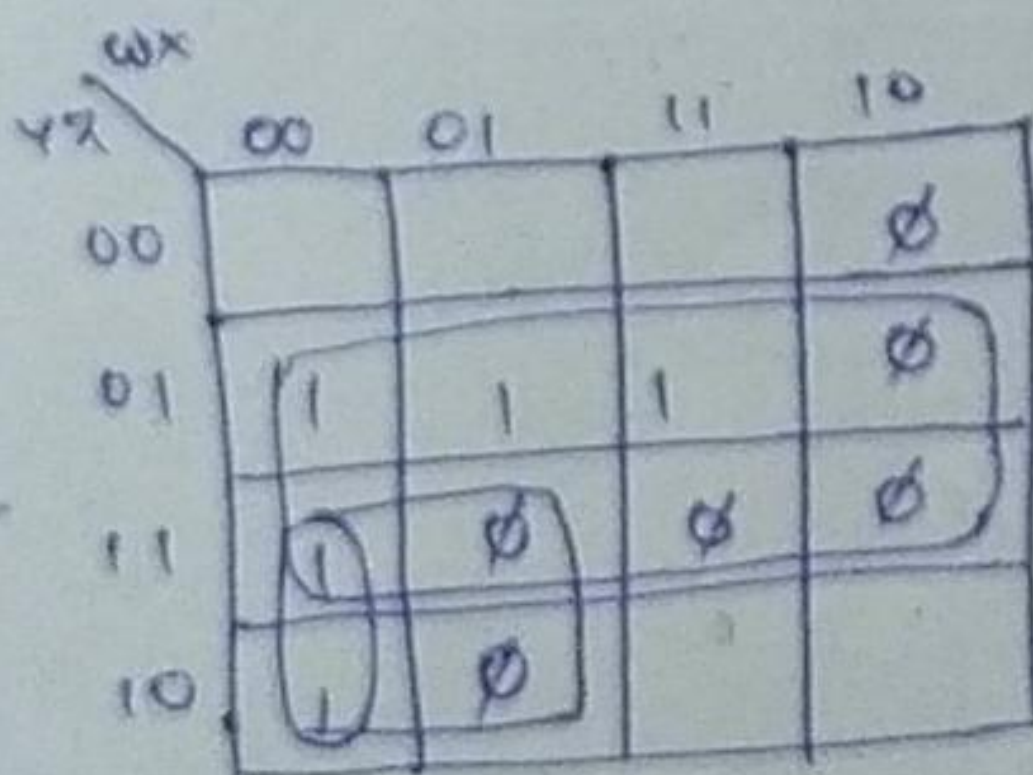


$$\begin{aligned} \Rightarrow \text{POS} &= 2(W+Y) \\ &= WZ + YZ \end{aligned}$$

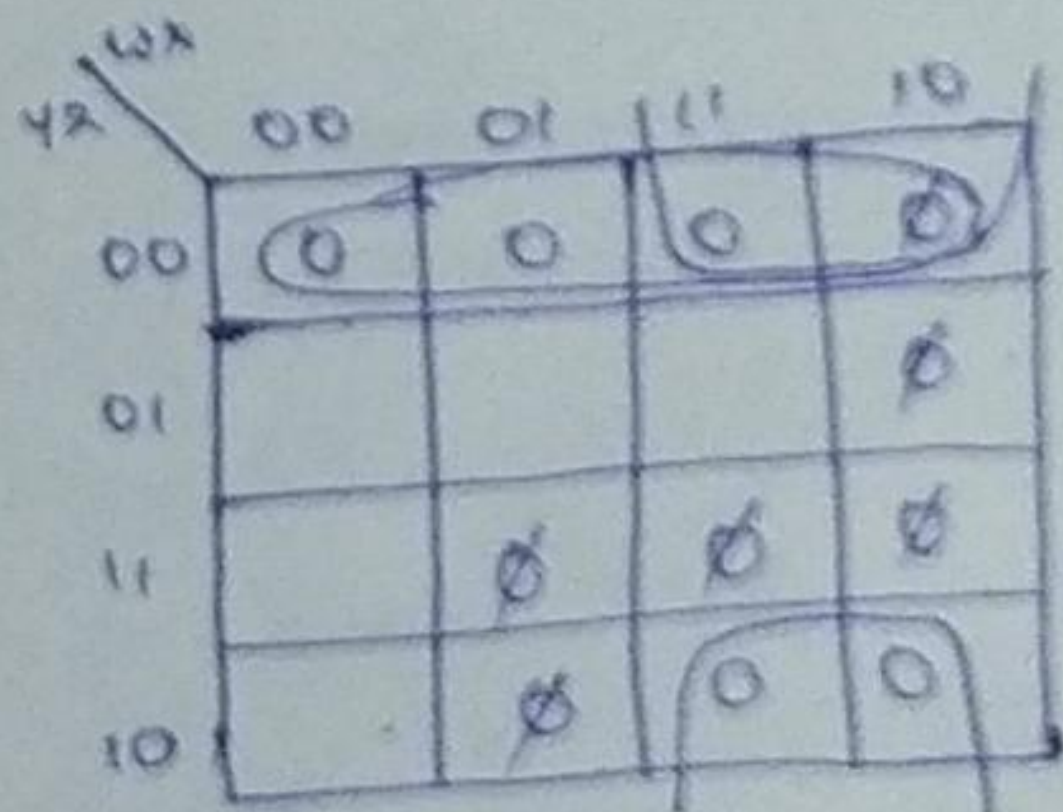
$$\text{SOP} = (WZ + YZ)$$

POS = SOP since we put 0 = 0 in both cases.

$$\textcircled{2} \quad f(W, X, Y, Z) = \sum (1, 2, 3, 5, 13) + \sum \emptyset (6, 7, 8, 9, 11, 15)$$



$$\text{SOP} = 2 + \bar{W}\bar{Y}$$



$$\begin{aligned} \text{POS} &= (Y+Z)(\bar{W}+Z) \\ &= 2 + \bar{W}Y \end{aligned}$$

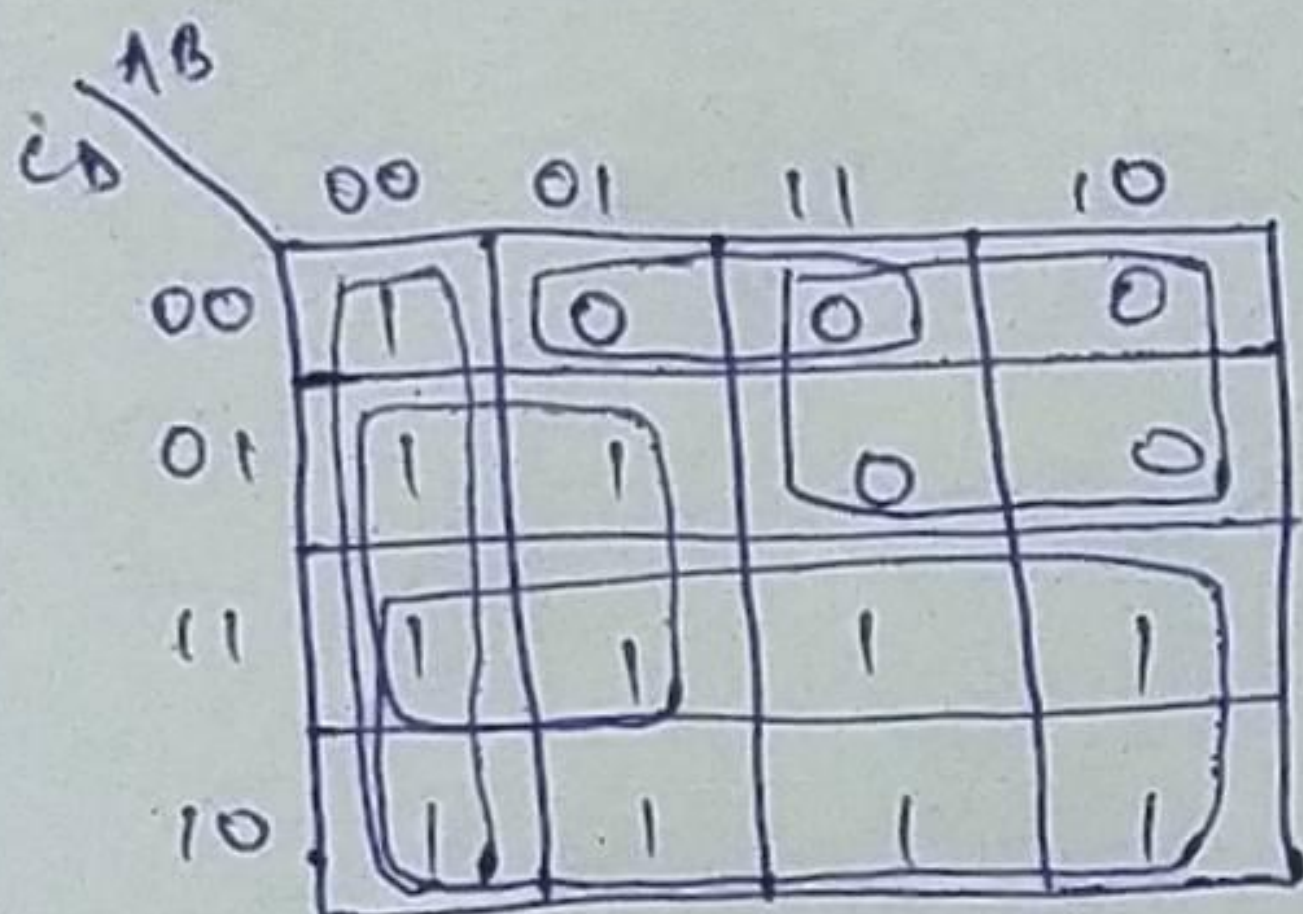
$$\boxed{\text{SOP} = \text{POS}}$$



# COMPARING INDEPENDANT VARIABLES IN MINIMAL SOP & POS :

Q) Minimal expression represented by the map is free ~~from~~ from

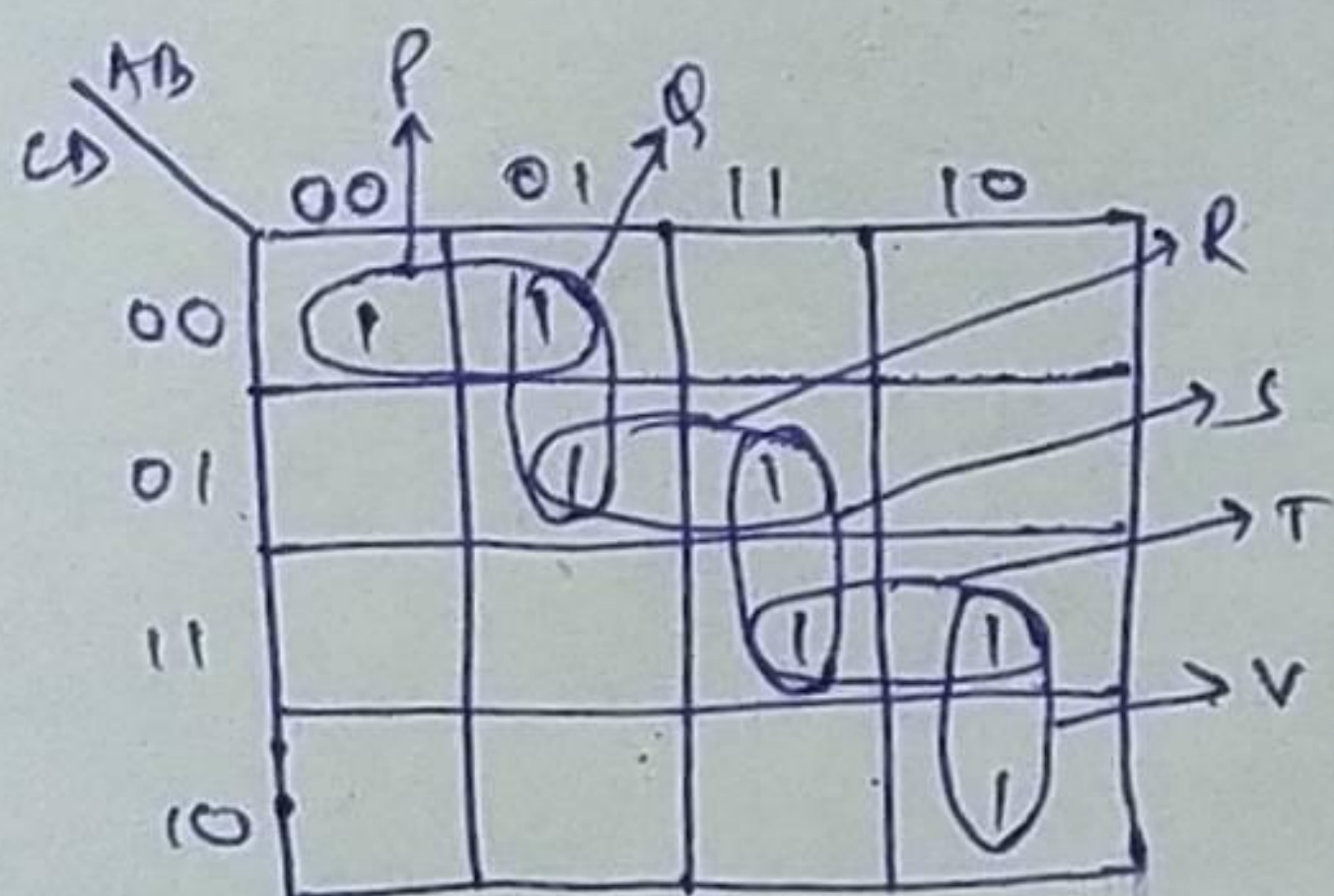
- a) 1      b) 2      c) 3      ☒ d) dependant on all.



$$SOP = C + \bar{A}\bar{B} + \bar{A}D$$

$$POS = (\bar{A} + C)(\bar{B} + C + D)$$

## NO. OF IRREDUNDANT & MINIMAL EXPRESSION



$$\# PI \rightarrow 6$$

$$\# EPI \rightarrow 2$$

$$\# RPI \rightarrow 4$$

$$\text{Minimal SOP} \rightarrow \bar{A}\bar{C}D + \bar{A}\bar{B}C + \bar{B}\bar{C}D + ACD$$

$$\# \text{ minimal exp} \rightarrow 3$$

	0	4	5	13	15	11	10
✓ P	✓	✓					
Q		✓	✓				
✓ R			✓	✓			
S				✓	✓		
✓ T					✓	✓	
✓ V						✓	✓



8)

	0	1	3	4	7	12	15	19	20	22	23	29	31
$A = WXYZ$						X	X					X	X
$B = XYZ$					X		X				X		X
$C = \bar{W}YZ$			X		X			X			X		
$D =$										X	X		
$E$									X	X			
$F$				X					X				
$G$		X	X										
$H$	X			X									
$I$	X	X											

Minimal Exp =  $A + C + E + H + G$  DFGI

	0	1	4	20	22	
B					✓	<u>E H I</u>
E				✓	✓	<u><del>DEGH</del></u>
F				✓		<u>DFGH</u>
G		✓				<u><del>DEHI</del></u>
H	✓		✓			
I	✓	✓				

$(I+H) (G+I) (F+H) (E+F) (D+E)$   
 $\Rightarrow (I+GH) (F+H) (E+FD)$

$000 + 001 + 010 + 011 + 100 + 101 + 110 + 111$   
 $IIE + IIF + IIE + IIF + GHE + GHF + GHE + GHF$

$= IIE + IIF + IIE + GHF + GHE \rightarrow \text{NO. of MIN} = 4$   
 $\frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{4} \quad \frac{1}{3}$



## FUNCTIONS INVOLVING FUNCTIONS

Q) Consider 3 variable function.

$$f_1(A, B, C) = \Sigma(0, 7) + \Sigma_{\emptyset}(1, 2, 5)$$

$$f_2(A, B, C) = \Sigma(0, 1, 3) + \Sigma_{\emptyset}(4, 7)$$

find  $f_1, f_2$  &  $f_1 + f_2$  when minimized.

$$\rightarrow f_1 f_2 = \Sigma(0) + \Sigma_{\emptyset}(1, 7) \quad \begin{array}{l} 1 \cdot 1 = 1 \\ 1 \cdot \emptyset = \emptyset \end{array}$$

$$f_1 + f_2 = \Sigma(0, 1, 3, 7) + \Sigma_{\emptyset}(2, 5, 4)$$

$$1 + 0 = 1$$

$$0 + 1 = 1$$

$$1 + 1 = 1$$

$$0 + \emptyset = \emptyset$$

$$1 + \emptyset = 1$$

Q) Consider a boolean operation '\$' defined as

$$A \$ B = \bar{A} + B \text{ then find } f_1 \$ f_2$$

C \ AB				
	00	01	11	10
0	0	1	0	1
1	0	1	1	0

C \ AB				
	00	01	11	10
0	1	0	0	1
1	0	1	1	1

C \ AB				
	00	01	11	10
0	1		1	1
1	1	1	1	1

$$= C + A + \bar{B}$$

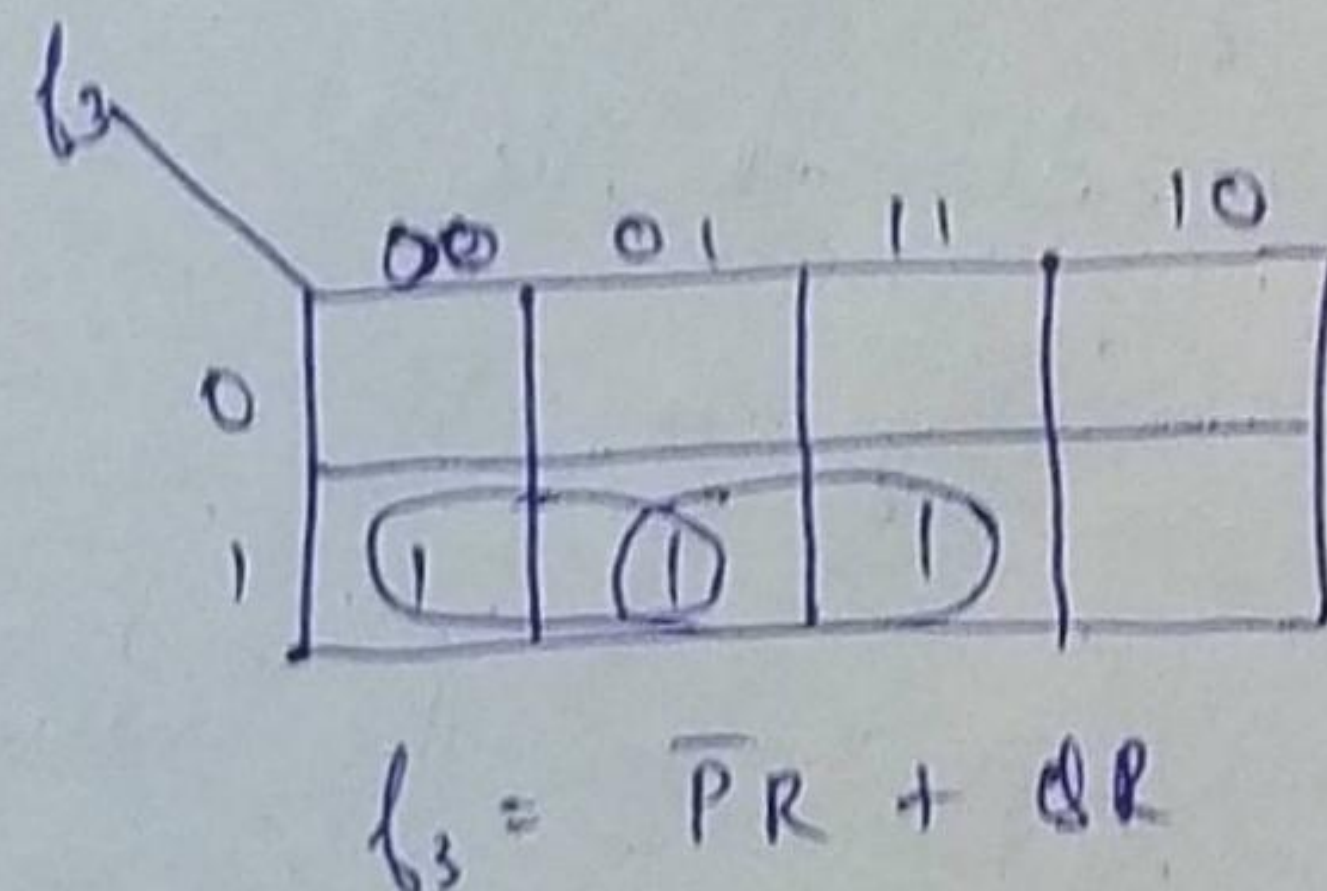
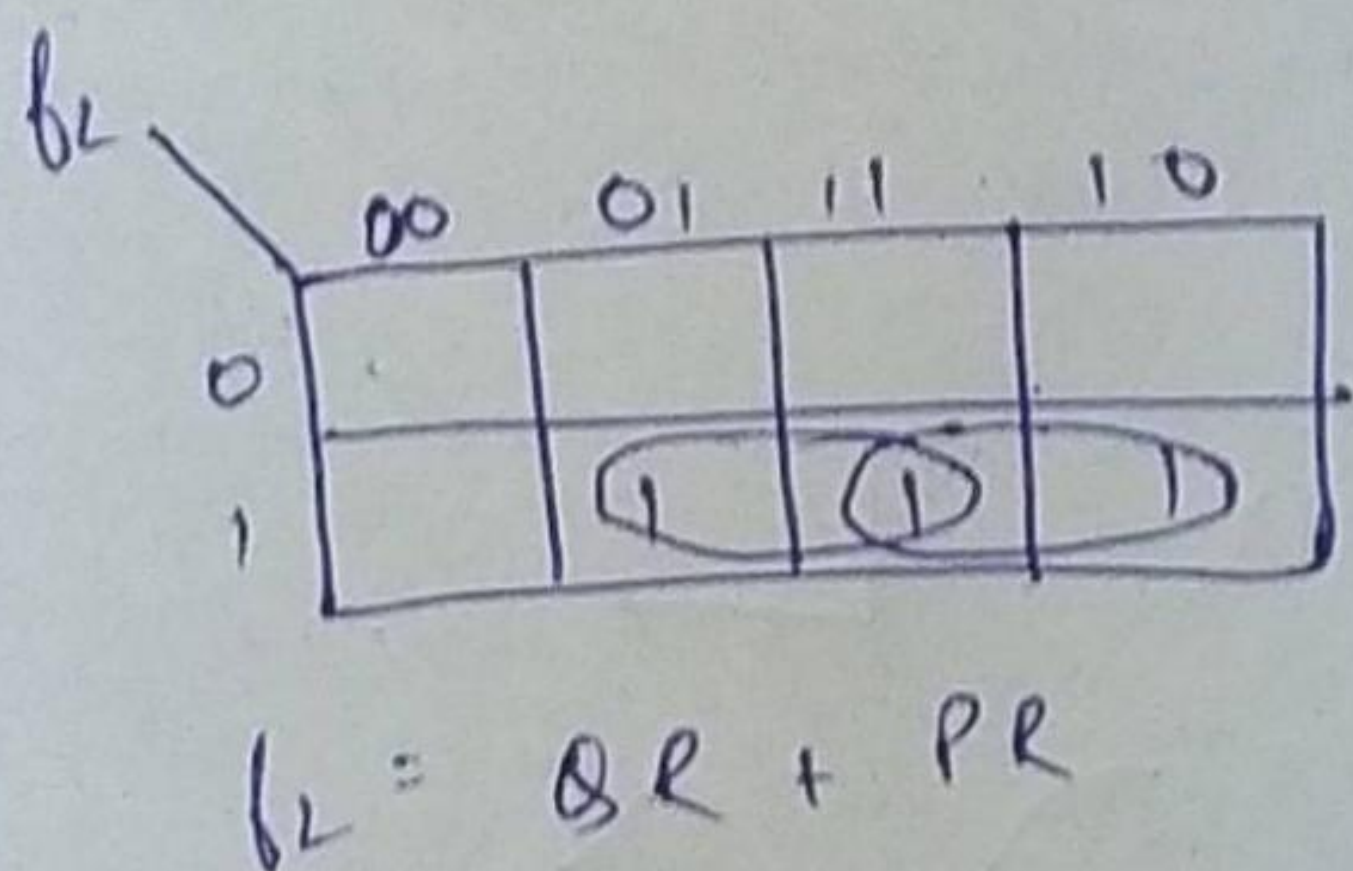
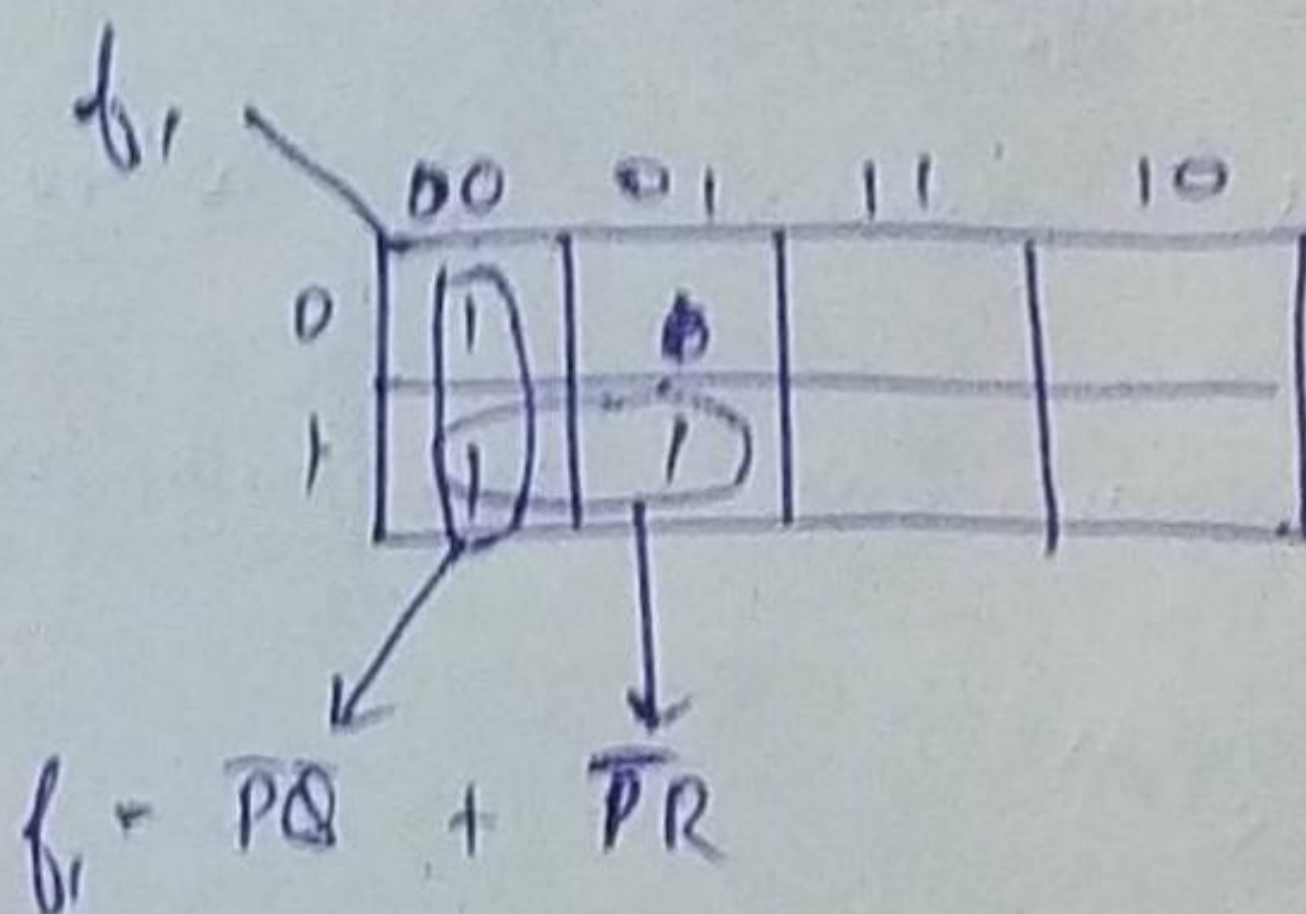
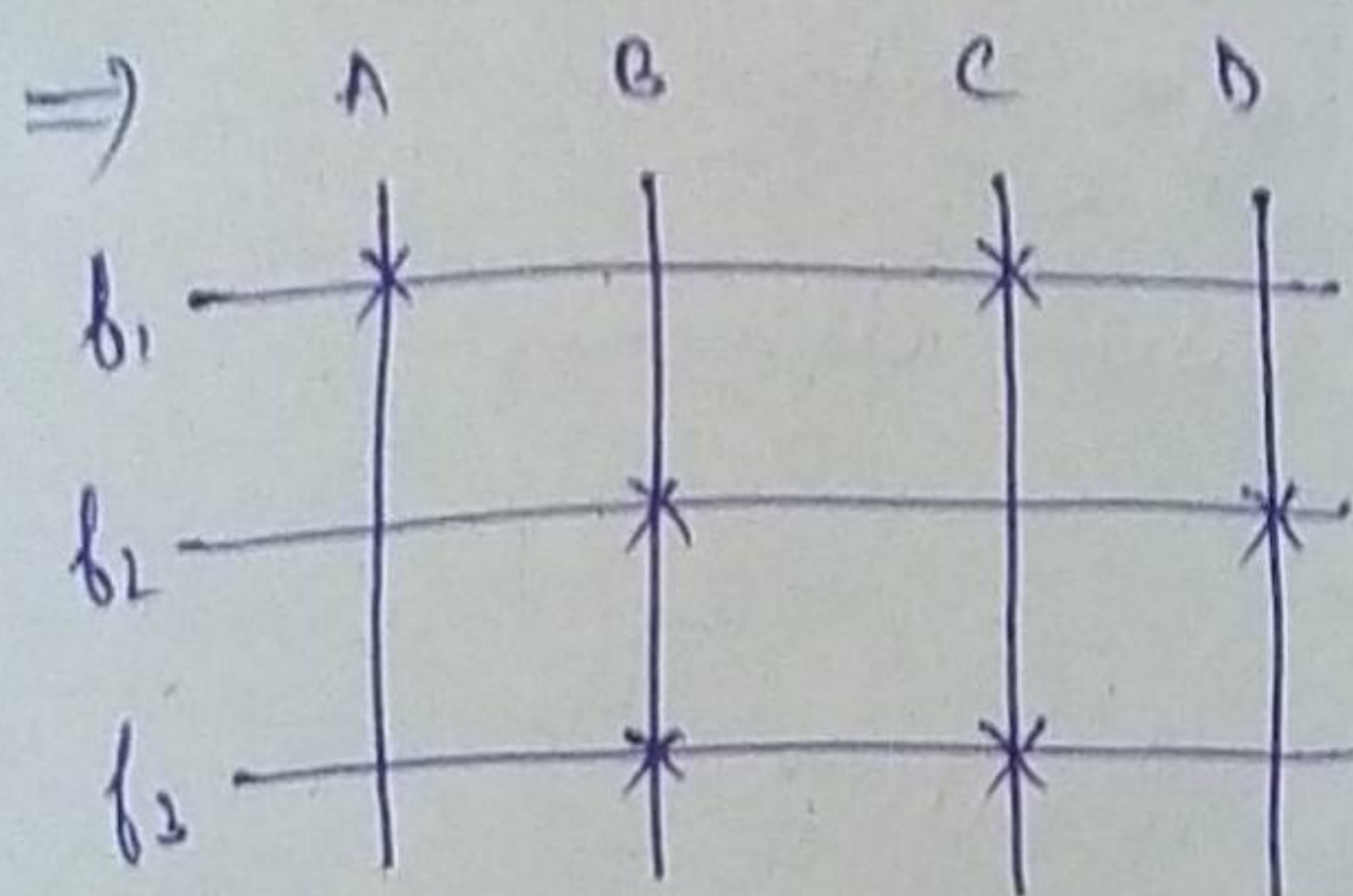


8) Consider three three variable functions  $f_1(P, Q, R) = \Sigma(0, 1, 3)$

$f_2(P, Q, R) = \Sigma(3, 5, 7)$ ,  $f_3(P, Q, R) = \Sigma(1, 3, 7)$  these

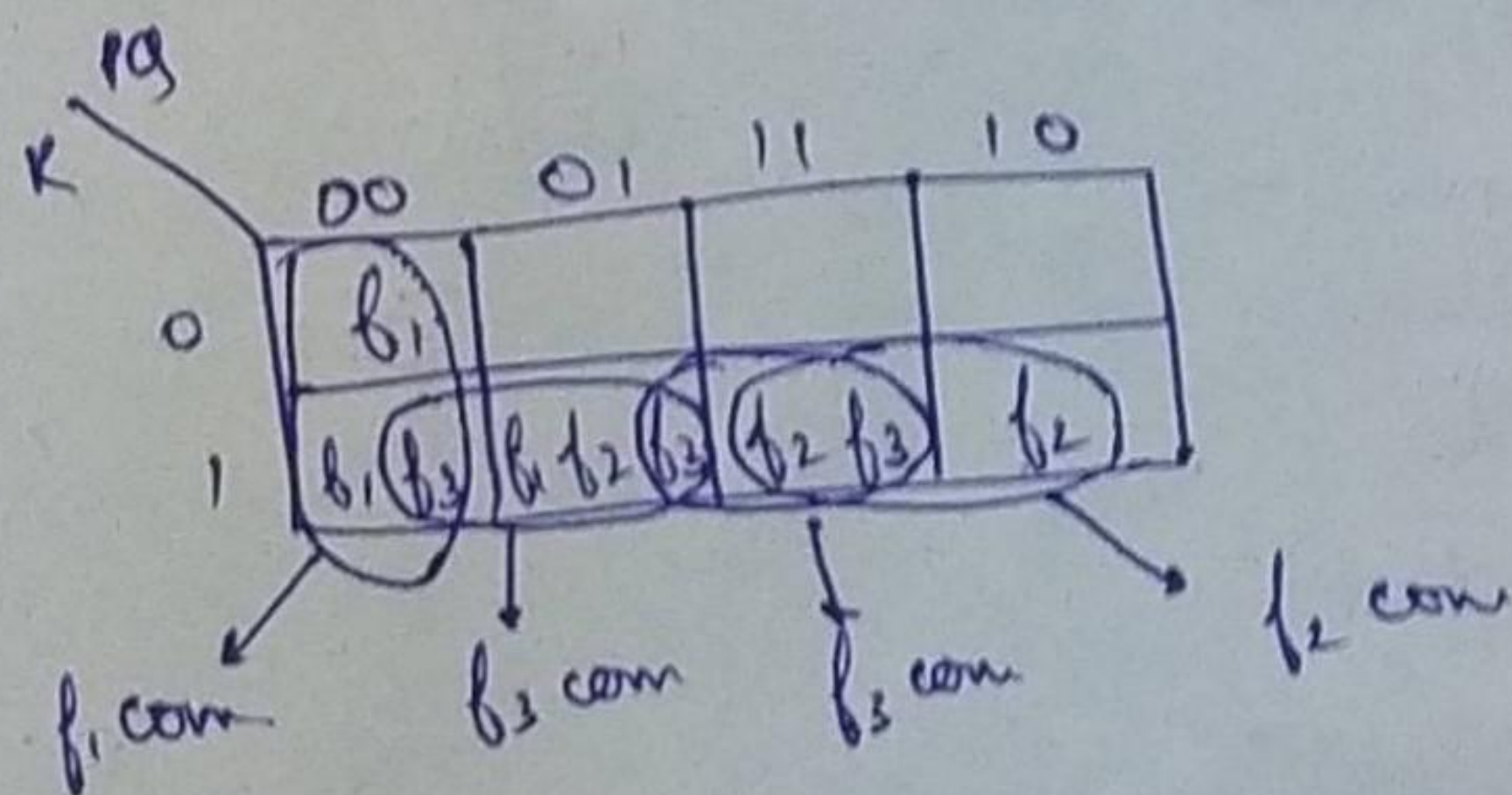
functions are sharing 4 prime & implicants A, B, C, D

(all of them are false) as shown.



$A = \overline{P}Q$ ,  $B = QR$ ,  $C = \overline{P}R$ ;  $D = \overline{Q}R$

$\Rightarrow$



$f_1 - f_3 \rightarrow C = \overline{P}R$