

OVERVIEW

The objective here is to test the performance of different electricity provisioning algorithms based on the demand predictions that we already have. We will be using the below objective function for performance measurement.

$$\sum_{t=1}^T p(t) * x(t) + a * \max(0, y[t] - x[t]) + b * |x[t] - x[t-1]|$$

Getting Started

Lets first import libraries and the energy usage dataset for three houses (B, C, F). We need to preprocess the data to make it usable.

```
In [1]: import pandas as pd
import numpy as np
import cvxpy as cp
import matplotlib.pyplot as plt
import warnings
import seaborn as sns
import numpy as np

warnings.filterwarnings("ignore")

# Loading the data from csv files

energyB = pd.read_csv('../Assignment 1 /data/HomeB-meter1_2014.csv')
energyC = pd.read_csv('../Assignment 1 /data/HomeC-meter1_2016.csv')
energyF = pd.read_csv('../Assignment 1 /data/HomeF-meter3_2016.csv')
```

Preprocessing Data

1. We need to convert timestamp to date time data structure
2. We need to convert the 3 datasets into bi-hourly buckets. Hence we group it into half hourly aggregates. House C & F were having minute level data.
3. As per the question we need to consider the timeline from 1st Nov to 14th Nov, hence we extract the data points for that duration.

```
In [2]: # Date column -> datetime object
energyB['Date & Time'] = pd.to_datetime(energyB['Date & Time'])
energyC['Date & Time'] = pd.to_datetime(energyC['Date & Time'])
energyF['Date & Time'] = pd.to_datetime(energyF['Date & Time'])
```

```
In [3]: start = "11-01-2014"
end = "11-15-2014"

energyB["Date & Time"] = energyB["Date & Time"].dt.floor(freq="30T")
energyB = energyB.groupby("Date & Time").sum().reset_index()

energyB = energyB.loc[energyB["Date & Time"] >= start]
energyB = energyB.loc[energyB["Date & Time"] < end]
energyB.reset_index(drop=True, inplace=True)
energyBdata = energyB['use [kW]']
energyBdata.index = np.arange(1, len(energyBdata) + 1)
```

```
In [4]: start = "11-01-2016"
end = "11-15-2016"

energyC["Date & Time"] = energyC["Date & Time"].dt.floor(freq="30T")
energyC = energyC.groupby("Date & Time").sum().reset_index()

energyC = energyC.loc[energyC["Date & Time"] >= start]
energyC = energyC.loc[energyC["Date & Time"] < end]
energyC.reset_index(drop=True, inplace=True)
energyCdata = energyC['use [kW]']
energyCdata.index = np.arange(1, len(energyCdata) + 1)
```

```
In [5]: start = "11-01-2016"
end = "11-15-2016"

energyF["Date & Time"] = energyF["Date & Time"].dt.floor(freq="30T")
energyF = energyF.groupby("Date & Time").sum().reset_index()

energyF = energyF.loc[energyF["Date & Time"] >= start]
energyF = energyF.loc[energyF["Date & Time"] < end]
energyF.reset_index(drop=True, inplace=True)
energyFdata = energyF['Usage [kW]']
energyFdata.index = np.arange(1, len(energyFdata) + 1)
```

```
In [6]: plt.rcParams["figure.figsize"] = [21, 10]
plt.rcParams['axes.labelsize'] = 10
plt.rcParams['xtick.labelsize'] = 10
plt.rcParams['ytick.labelsize'] = 10
plt.rcParams['text.color'] = 'black'

def plot_graph_offline(prov_type, x, trueValues, house):
    plt.figure(figsize=(20, 5))
    plt.title("Actual vs Optimal values for Offline " + prov_type + " provisi
    plt.plot(x, 'b', label="Optimal Values")
    plt.plot(trueValues, 'r', label="True Values")
    plt.legend()
    plt.ylabel("Electricity Units in kW")
    plt.xlabel("Time step t(1 unit = 15 minutes)")
```

```
In [7]: #Store algorithms, optimal values and decision values for objective function
opt_dict_B = {}
opt_dict_C = {}
opt_dict_F = {}
decision_dict_B = {}
decision_dict_C = {}
decision_dict_F = {}
opt_dict = [opt_dict_B, opt_dict_C, opt_dict_F]
decision_dict = [decision_dict_B, decision_dict_C, decision_dict_F]
offline_static = []
houses = ['B', 'C', 'F']
energyData = [energyBdata, energyCdata, energyFdata]
```

Offline Optimization Problem

Offline Static Optimization

In case of Static Offline optimization, we do not consider the switching cost, so our objective function reduces to below:

$$\sum_{t=1}^T p(t) * x(t) + a * \max\{(0, y[t] - x[t])\}$$

To minimize this objective function for a given x, we use the library CVXPY. For this value of x, we then find the optimal value of cost.

The const. parameters we have here are :

Price (p) = $0.4/kwH = (0.4/2) / kW \text{ 30 min} = 0.2\$ / KW \text{ 30 min} = 0.2$

$a = b = 4/kwH = 2/kw30min = 2$

```
In [8]: def calc_static_provisioning_offline(house, data):
    price = 0.4/2 #Half hourly rate
    a = 4/2
    b = 4/2
    y = data.to_list()
    x = cp.Variable(1)

    cost = price*x + a*cp.maximum(0, y - x)
    objective = cp.Minimize(cp.sum(cost) + b*x)
    constraints = [0 <= x]
    problem = cp.Problem(objective, constraints)
    result = problem.solve()
    opt = pd.Series(np.full((672), x.value), index=data.index)

    print("The optimal value for static provisioning for house ", house , " is")
    print("The optimal value of x for the same is: ", x.value)
    plot_graph_offline('static', opt, data, house)
    return result, opt
```

```
In [9]: for i in range(3):
        result, opt = calc_static_provision_offline(houses[i], energyData[i])
        opt_dict[i]['Offline Static'] = result
        decision_dict[i]['Offline Static'] = opt
        offline_static.append(result)
```

The optimal value for static provisioning for house B is 194.84252933729957

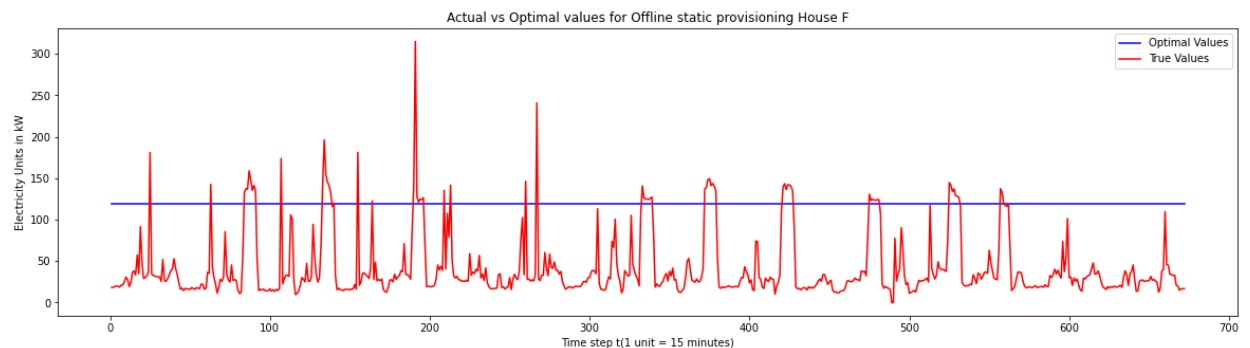
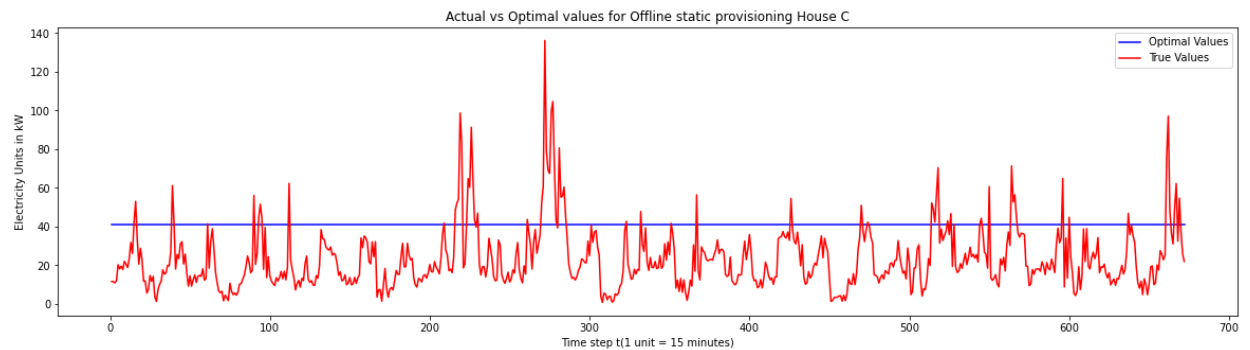
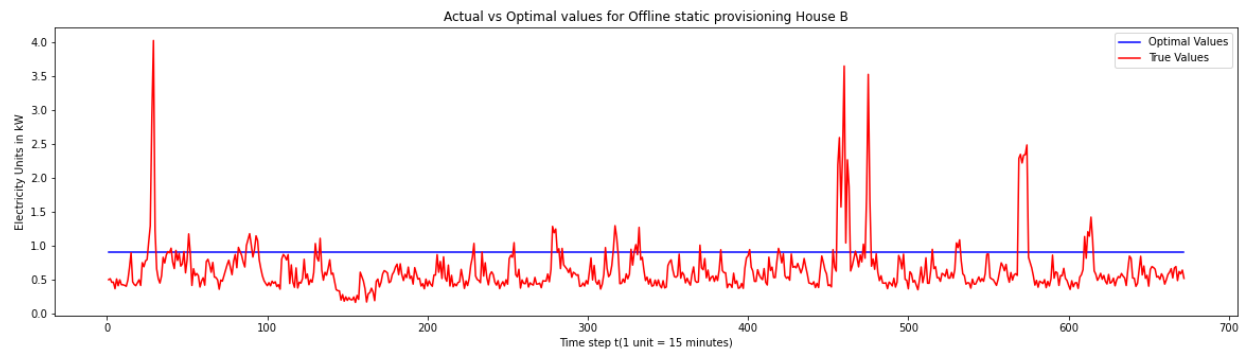
The optimal value of x for the same is: [0.907565]

The optimal value for static provisioning for house C is 7989.918093270889

The optimal value of x for the same is: [41.14206667]

The optimal value for static provisioning for house F is 19396.101745950808

The optimal value of x for the same is: [119.74353333]



As seen for the above graphs, for example: for house B, the static offline optimization gives the

value of 0.907 kW and the objective function cost as 194.84. We get a straight line as optimal plot on graph as above, since this is a static optimisation.

We get the below values as optimal cost using static offline optimization approach above.

```
In [10]: comparison = pd.DataFrame({
        'House': houses,
        'Cost': offline_static,
    })
    comparison
```

Out[10]:

	House	Cost
0	B	194.842529
1	C	7989.918093
2	F	19396.101746

Offline Dynamic Optimization

In case of Dynamic Offline optimization, we do consider the previous values also, hence, so our objective function reduces to below:

$$\sum_{t=1}^T p(t) \cdot x(t) + a \cdot \max(0, y[t] - x[t]) + b \cdot |x[t] - x[t-1]|$$

Similar to static offline optimizations, I am calculating the optimal cost and plotting the graph for each house.

```
In [11]: def calc_dynamic_offline_provision(house, df):
        p = 0.4/2
        a = 4/2
        b = 4/2
        y = df.to_list()
        x = cp.Variable(672)
        cost = 0

        for i in range(1,672):
            cost += p*x[i] + a*cp.maximum(0, y[i-1] - x[i]) + b*cp.abs(x[i]-x[i-1])

        objective = cp.Minimize(cost)
        constraints = [x[0] == 0, x[1:] >= 0]
        problem = cp.Problem(objective, constraints)
        result = problem.solve()
        opt = pd.Series(np.array(x.value), index=df.index)

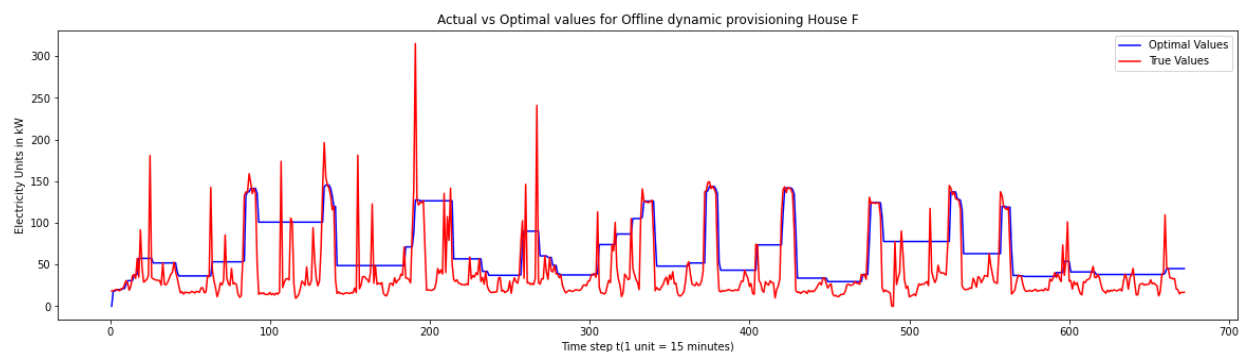
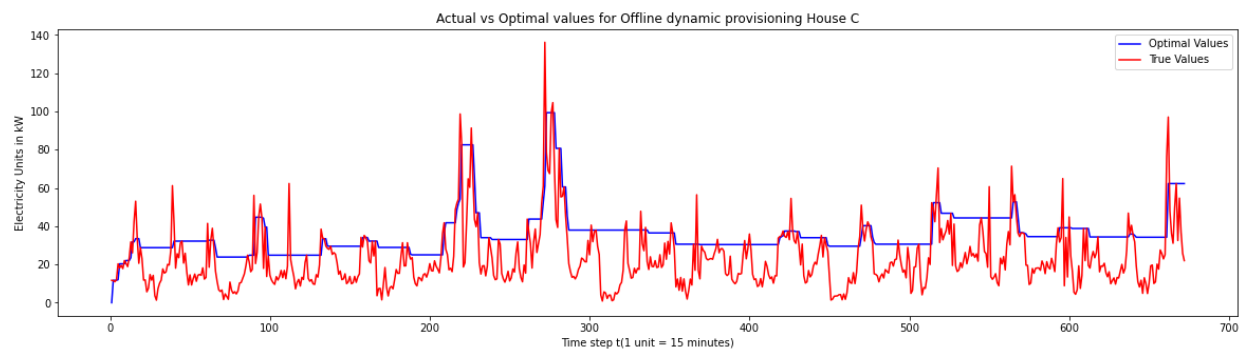
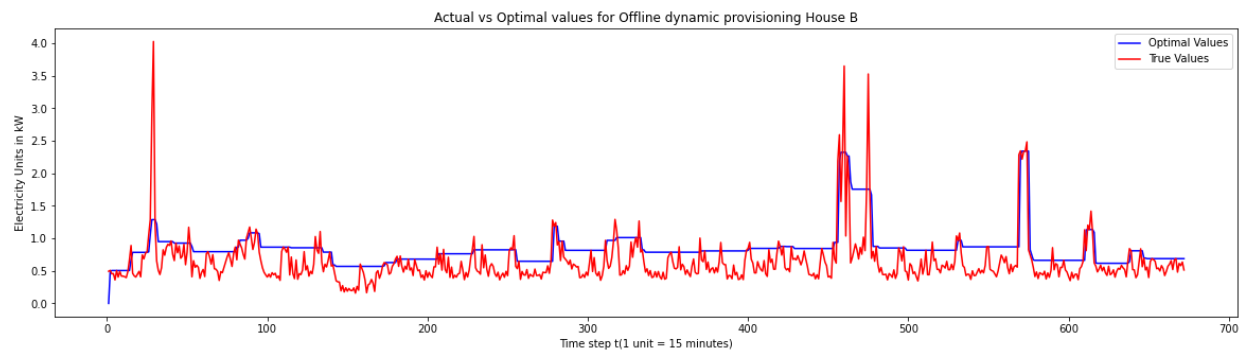
        print("\nThe optimal value of dynamic optimisation for House ", house, "
        plot_graph_offline('dynamic', opt, df, house)
        return result, opt
```

```
In [12]: offline_dynamic = []
for i in range(3):
    result, opt = calc_dynamic_offline_provision(houses[i], energyData[i])
    opt_dict[i]['Offline Dynamic'] = result
    decision_dict[i]['Offline Dynamic'] = opt
    offline_dynamic.append(result)
```

The optimal value of dynamic optimisation for House B is 161.34680706547033

The optimal value of dynamic optimisation for House C is 6696.918532777977

The optimal value of dynamic optimisation for House F is 14778.496106597464



```
In [13]: comparison = pd.DataFrame({
    'House': houses,
    'Offline Static Cost': offline_static,
    'Offline Dynamic Cost': offline_dynamic,
    })
comparison
```

Out[13]:

	House	Offline Static Cost	Offline Dynamic Cost
0	B	194.842529	161.346807
1	C	7989.918093	6696.918533
2	F	19396.101746	14778.496107

Online Algorithms

As part of online algorithms, I am exploring Online Gradient Descent (OGD), Receding Horizon Control (RHC) and Commitment Horizon Control (CHC) to find the optimal provision.

ONLINE GRADIENT DESCENT

In case of online gradient descent, we find the value of $x(t)$ iteratively using the previous values $x(t-1)$. The equation is as below:

$$x[t+1] = x[t] - \text{learning_rate} * (\text{gradient})$$

Here learning rate is the different step sizes we provide and observe how objective function value is changing for a range of learning rate.

```
In [14]: def calc_cost(method, x, y, verbose):
    cost = 0
    p = 0.4/2
    a = 4/2
    b = 4/2
    for i in range(1, len(y) + 1):
        cost += p * x[i] + a * max(0, y[i] - x[i] + b * abs(x[i] - x[i - 1])
    if (verbose == True):
        print("\nThe objective value for " + method + " is", cost)
    return cost
```

```
In [15]: def gradient(x, y, t, p, a, b):
    slope = 0

    if (y[t] > x[t]):
        if (x[t] > x[t - 1]):
            slope = p - a + b;
        else:
            slope = p - a - b;
    else:
        if (x[t] > x[t - 1]):
            slope = p + b;
        else:
            slope = p - b;
    return slope;
```

```
In [16]: def online_gradient_descent(y, steps):
    n = len(y)
    x = [0.0] * (n + 1)
    x[1] = 0
    p = 0.4/2
    a = 4/2
    b = 4/2
    for t in range(1, n):
        x[t + 1] = x[t] - steps * gradient(x, y, t, p, a, b)
    return x
```

```
In [17]: x = online_gradient_descent(energyBdata, steps = 0.1)
calc_cost('Online Gradient Descent', x, energyBdata, True)
```

The objective value for Online Gradient Descent is 371.0574300160019

```
Out[17]: 371.0574300160019
```

```
In [18]: def plot_ogd(house, steps, costs):
    plt.figure(figsize=(20, 5))
    plt.title("Online Gradient Descent Optimal Cost for House " + house)
    plt.plot(steps, costs, label = "Cost")
    plt.legend()
    plt.ylabel("Cost Value")
    plt.xlabel("Step Size")
    plt.show()
```

```
In [19]: def plot_comparison(house, optimalValues, trueValues):
    plt.figure(figsize=(20, 5))
    plt.title("Actual vs Optimal | Online Gradient Descent | House " + house)
    plt.plot(optimalValues, 'b', label="Usage Values")
    plt.plot(trueValues, 'r', label="Provision Values")
    plt.legend()
    plt.ylabel("Electricity Units in kWh")
    plt.xlabel("Time step t(1 unit = 15 minutes)")
```

```
In [20]: ogd= []
```



```

In [21]: costs = []
steps = []
step = 0
i = 0
for k in range(800):
    step += 0.0002
    x = online_gradient_descent(energyData[i], steps = step)
    steps.append(step)
    costs.append(calc_cost("Cost", x ,energyData[i], False))

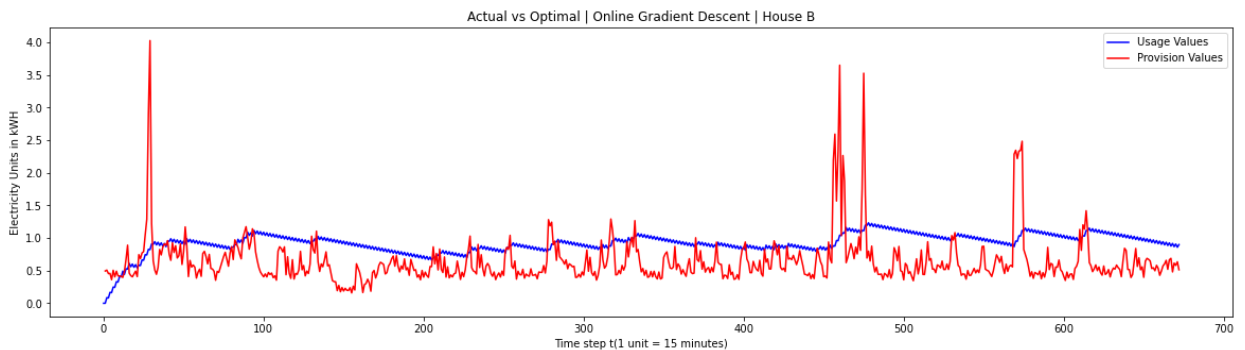
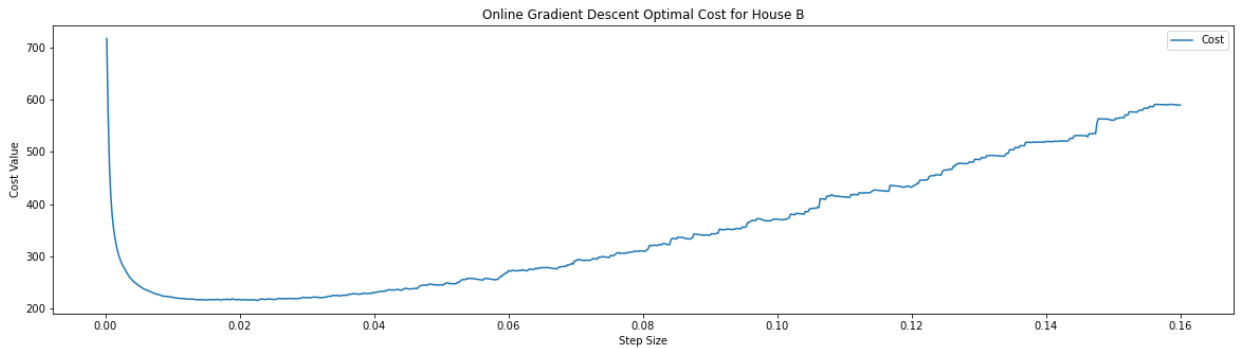
x = online_gradient_descent(energyBdata, steps = steps[steps.index(min(costs))])
print ("Results on Online Gradient Descent for House ", houses[i])
print("Optimal cost found For House B at step: ", steps[steps.index(min(costs))])
opt = calc_cost("Online Gradient Descent at Optimal cost for House B : ", x)
opt_dict[0]['OGD'] = opt
decision_dict[0]['OGD'] = x
ogd.append(opt)
plot_ogd("B", steps, costs)
plot_comparison("B", x, energyBdata)

```

Results on Online Gradient Descent for House B

Optimal cost found For House B at step: 0.022599999999999974

The objective value for Online Gradient Descent at Optimal cost for House B : is 215.83683934600026



```

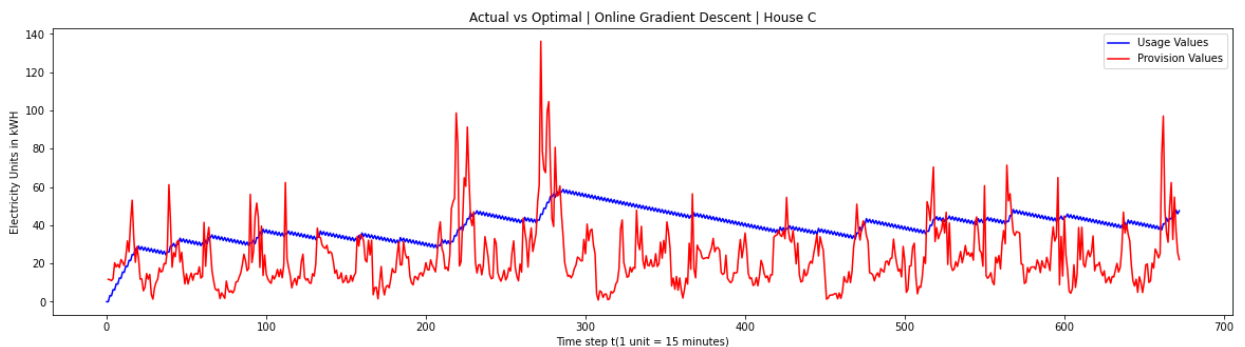
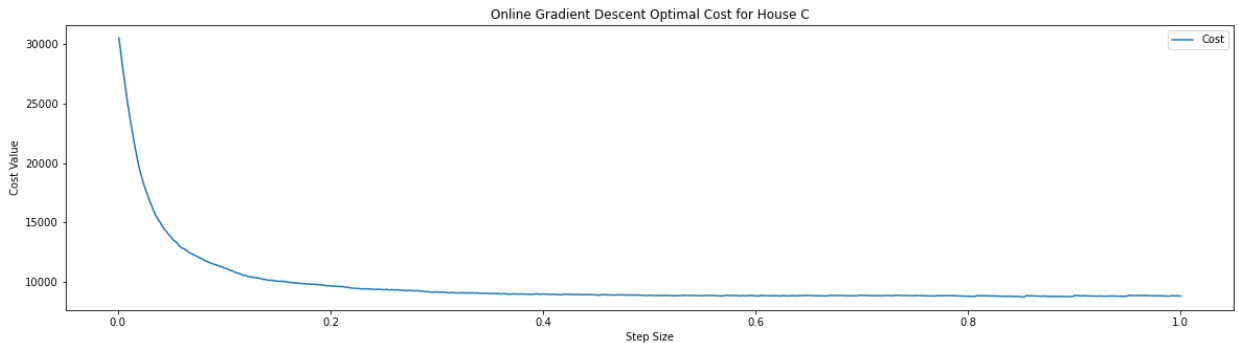
In [22]: i = 1
costs = []
steps = []
step = 0
for k in range(1000):
    step += 0.001
    x = online_gradient_descent(energyData[i], steps = step)
    steps.append(step)
    costs.append(calc_cost("Cost", x ,energyData[i], False))

x = online_gradient_descent(energyData[i], steps = steps[costs.index(min(costs))])
print ("Results on Online Gradient Descent for House ", houses[i])
print("Optimal cost found at step: ", steps[costs.index(min(costs))])
opt = calc_cost("Online Gradient Descent at Optimal cost", x, energyData[i])
opt_dict[i]['OGD'] = opt
decision_dict[i]['OGD'] = x
ogd.append(opt)
plot_ogd(houses[i], steps, costs)
plot_comparison(houses[i], x, energyData[i])

```

Results on Online Gradient Descent for House C
 Optimal cost found at step: 0.8520000000000006

The objective value for Online Gradient Descent at Optimal cost is 8717.683653388014



```

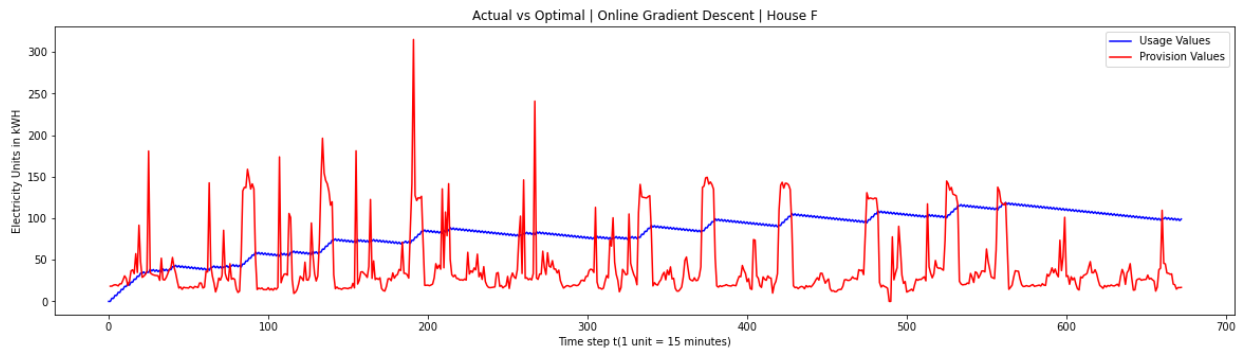
In [23]: i = 2
costs = []
steps = []
step = 0
for k in range(1000):
    step += 0.001
    x = online_gradient_descent(energyData[i], steps = step)
    steps.append(step)
    costs.append(calc_cost("Cost", x ,energyData[i], False))

x = online_gradient_descent(energyData[i], steps = steps[ costs.index(min(costs)) ])
print ("Results on Online Gradient Descent for House ", houses[i])
print("Optimal cost found at step: ", steps[ costs.index(min(costs)) ])
opt = calc_cost("Online Gradient Descent at Optimal cost", x, energyData[i])
opt_dict[i]['OGD'] = opt
decision_dict[i]['OGD'] = x
ogd.append(opt)
plot_comparison(houses[i], x, energyData[i])

```

Results on Online Gradient Descent for House F
 Optimal cost found at step: 0.9920000000000008

The objective value for Online Gradient Descent at Optimal cost is 22013.624520051995



```
In [24]: comparison = pd.DataFrame({
    'House': houses,
    'Offline Static': offline_static,
    'Offline Dynamic Cost': offline_dynamic,
    'Online Gradient Descent': ogd,
})
comparison
```

Out[24]:

	House	Offline Static	Offline Dynamic Cost	Online Gradient Descent
0	B	194.842529	161.346807	215.836839
1	C	7989.918093	6696.918533	8717.683653
2	F	19396.101746	14778.496107	22013.624520

Receding Horizon Control

RHC is a control algorithm, popularly known as Model Predictive Control. It is often used in control systems like automated cars to predict steering angle movement, acceleration and speed with time.

It is a general purpose control scheme that involves repeatedly solving a constrained optimization problem, using predictions of future costs, disturbances, and constraints over a moving time horizon to choose the control action.

In order to test the approach, We need to have prediction data. We are using the energy usage prediction data from the previous assignment for **"Linear Regression and Random Forest"**. We here load the data set and run it for the algorithms.

```
In [25]: y_b_lr = pd.read_csv("./data/b_pred_lr.csv").iloc[:, 0]
y_b_rf = pd.read_csv("./data/b_pred_rf.csv").iloc[:, 0]
```

```
In [26]: # y_extratrees = pd.read_csv("./data/prediction_B_lr.csv", usecols = ['prediction'])
# y_svr = pd.read_csv("./data/prediction_B_rf.csv", usecols = ['prediction'])

y_c_lr = pd.read_csv("./data/pred_c_lr.csv").iloc[:, 1]
y_c_rf = pd.read_csv("./data/pred_c_rf.csv").iloc[:, 1]
y_f_lr = pd.read_csv("./data/f_pred_lr.csv").iloc[:, 0]
y_f_rf = pd.read_csv("./data/f_pred_rf.csv").iloc[:, 0]

predictions = [
    # [y_extratrees['prediction'], y_svr['prediction']],
    [y_b_lr, y_b_rf],
    [y_c_lr, y_c_rf],
    [y_f_lr, y_f_rf]]
```

```
In [27]: def plot_RHC(title, windows, costs):
    fig = plt.figure(figsize=(15, 4))
    plt.title(title)
    plt.plot(windows, costs, label = "Prediction Window Value")
    plt.legend()
    plt.ylabel("Cost Value")
    plt.xlabel("Prediction Window Size")

def plot_comparisonn(house, optimalValues, trueValues, algoname):
    plt.figure(figsize=(20, 5))
    plt.title("Actual vs Provision | RHC " + algoname + " | House " + house)
    plt.plot(optimalValues, 'b', label="Usage Values")
    plt.plot(trueValues, 'r', label="Provision Values")
    plt.legend()
    plt.ylabel("Electricity Units in kWh")
    plt.xlabel("Time step t(1 unit = 15 minutes)")
```

```
In [28]: def calc_RHC(houseno, y, predictionHorizon, algo_name):
    b = 4/2
    a = 4/2
    price = 0.4/2
    T = 2*24*14
    optValues = np.zeros(T)
    for horizonStart in range(0, T):
        horizonEnd = horizonStart + predictionHorizon
        windowY = y[horizonStart: horizonEnd]

        obj = 0;
        x = cp.Variable(predictionHorizon)

        for i in range(0, predictionHorizon):
            obj += price * x[i] + a * cp.maximum(0, windowY[i] - x[i])
            if i == 0:
                obj += b * cp.abs(x[i]); #because x(0) is 0
            else:
                obj += b * cp.abs(x[i] - x[i - 1])

        objective = cp.Minimize(obj)
        problem = cp.Problem(objective)
        result = problem.solve()
        optValues[horizonStart] = x.value[0];

    obj = 0;
    for i in range(0, T):
        obj += price * optValues[i] + a * max(0, y[i] - optValues[i])
        if i == 0:
            obj += b * abs(optValues[i]); #because x(0) is 0
        else:
            obj += b * abs(optValues[i] - optValues[i - 1])

    opt_dict[houseno]['RHC' + '_' + algo_name] = obj
    decision_dict[houseno]['RHC' + '_' + algo_name] = optValues
    return obj
```

In [29]:

```

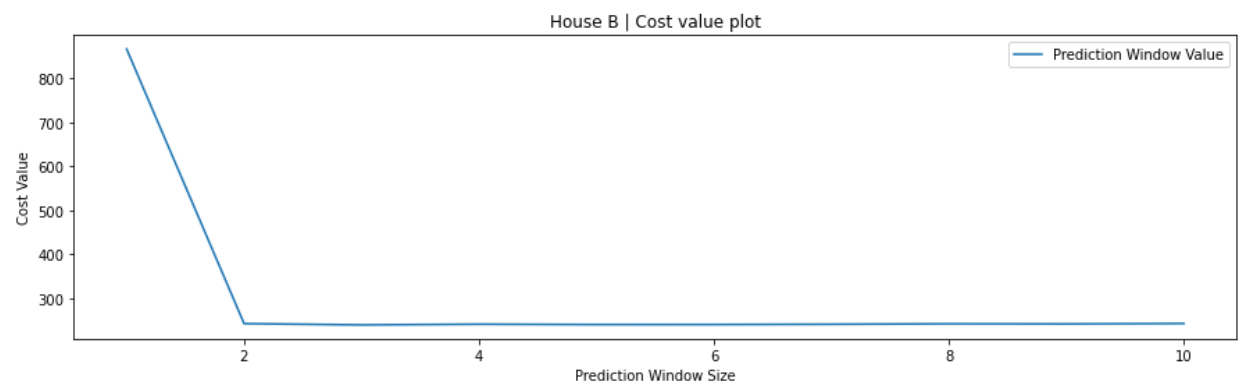
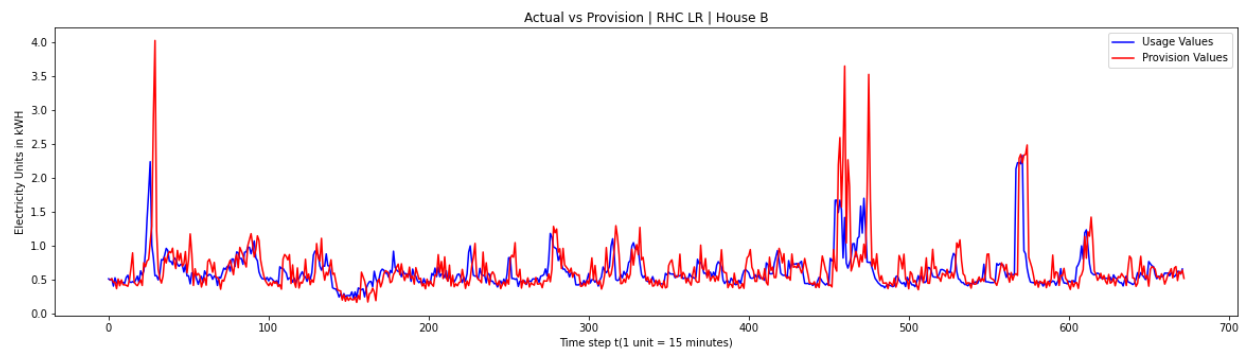
houseno = 0
predictData = predictions[houseno][0]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'LR'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[ costs.index(min(costs)) ], 'LR')
print("Optimal cost for RHC and Linear Regression found at window size: ",
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_LR'], energyD
plot_RHC("House B | Cost value plot", windows, costs)

```

Optimal cost for RHC and Linear Regression found at window size: 3

Optimal cost is: 239.20966314128637



In [30]:

```

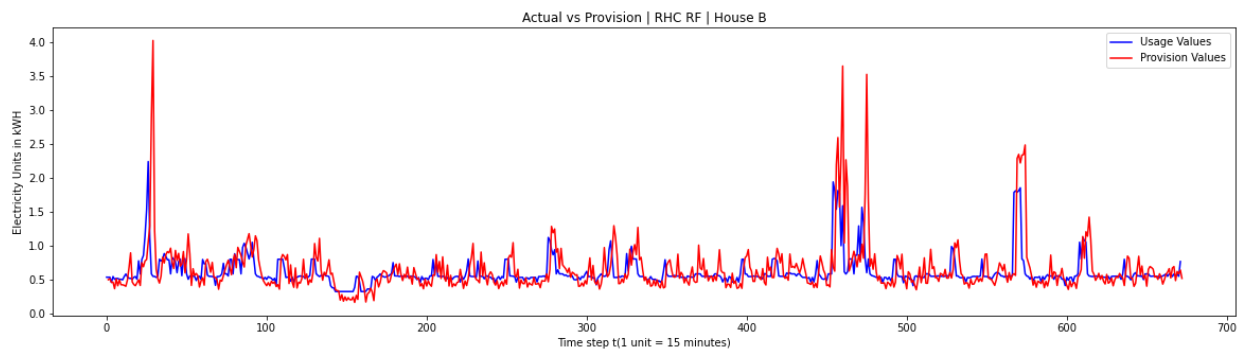
houseno = 0
predictData = predictions[houseno][1]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'RF'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[costs.index(min(costs
print("Optimal cost for RHC and Random Forest found at window size: ", wind
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_RF'], energyD
# plot_RHC("House B Cost value plot", windows, costs)

```

Optimal cost for RHC and Random Forest found at window size: 3

Optimal cost is: 224.34058586296203



In [31]:

```

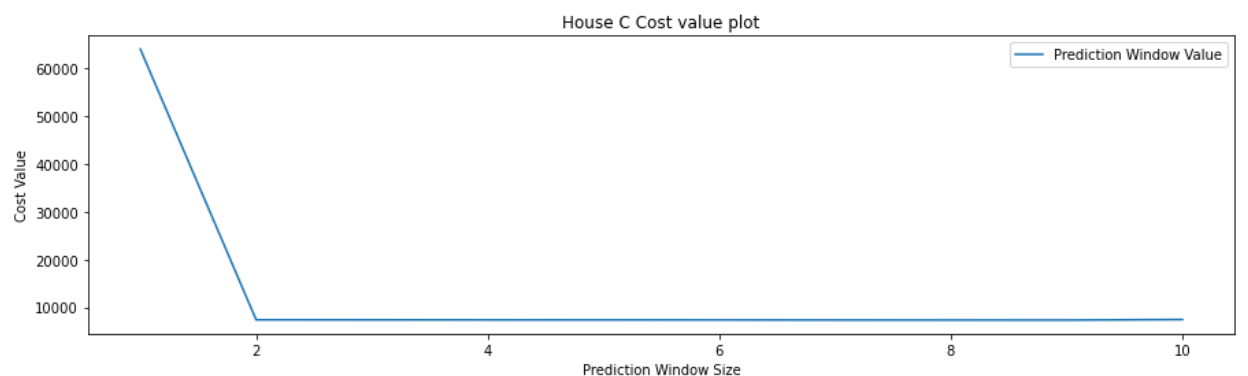
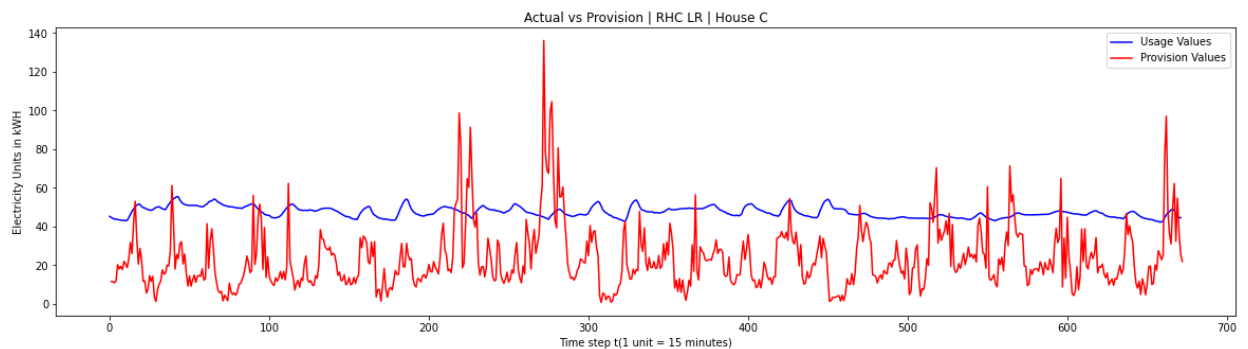
houseno = 1
predictData = predictions[houseno][0]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'LR'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[ costs.index(min(costs)) ], 'LR')
print("Optimal cost for RHC and Linear Regression found at window size: ",
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_LR'], energyD
plot_RHC("House C Cost value plot", windows, costs)

```

Optimal cost for RHC and Linear Regression found at window size: 9

Optimal cost is: 7302.797485416918



In [32]:

```

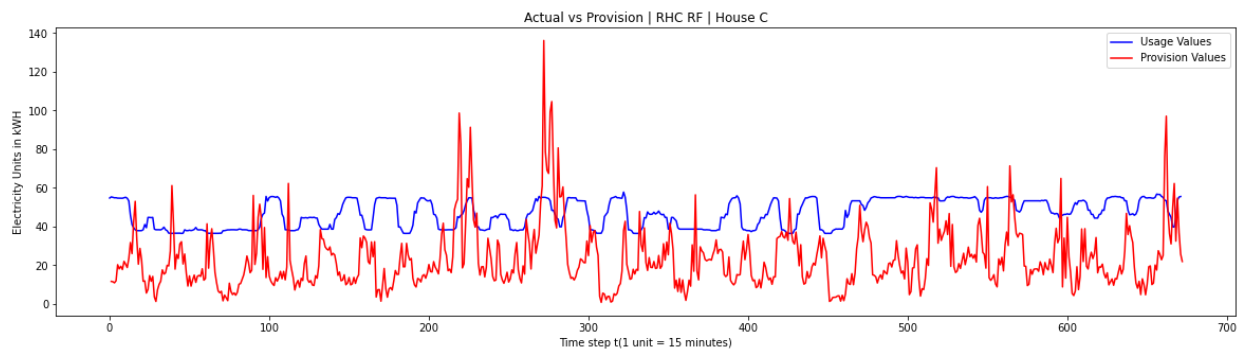
houseno = 1
predictData = predictions[houseno][1]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'RF'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[ costs.index(min(costs)) ], 'RF')
print("Optimal cost for RHC and Random Forest found at window size: ", windows[ costs.index(min(costs)) ])
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_RF'], energyD[houseno])
# plot_RHC("House C Cost value plot", windows, costs)

```

Optimal cost for RHC and Random Forest found at window size: 9

Optimal cost is: 8354.494025515745



In [33]:

```

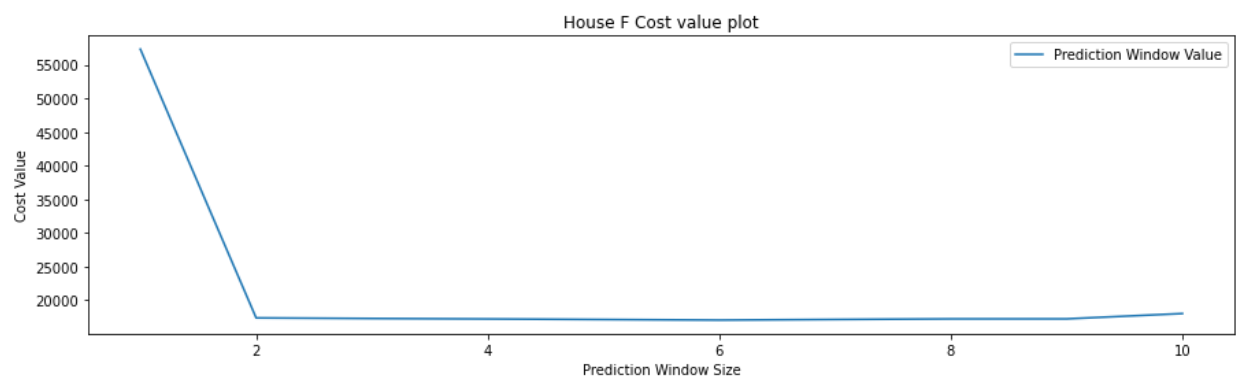
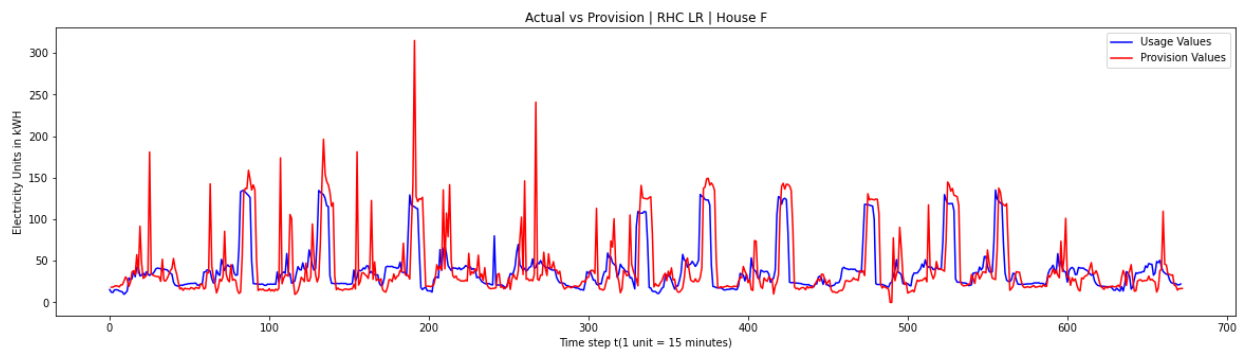
houseno = 2
predictData = predictions[houseno][0]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'LR'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[ costs.index(min(costs)) ], 'LR')
print("Optimal cost for RHC and Linear Regression found at window size: ",
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_LR'], energyD
plot_RHC("House F Cost value plot", windows, costs)

```

Optimal cost for RHC and Linear Regression found at window size: 6

Optimal cost is: 17062.672793942707



In [34]:

```

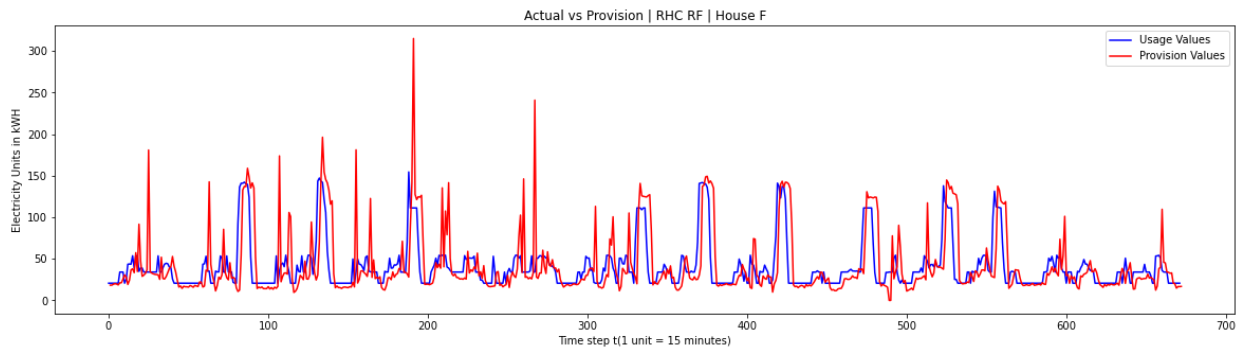
houseno = 2
predictData = predictions[houseno][1]
costs = []
windows = []
for i in range(1,11):
    windows.append(i)
    costs.append(calc_RHC(houseno, predictData.to_numpy(), i, 'RF'))

x = calc_RHC(houseno, predictData.to_numpy(), windows[ costs.index(min(costs)) ], 'RF')
print("Optimal cost for RHC and Random Forest Regression found at window size: ", x)
print("\nOptimal cost is: ", x)
plot_comparisonn(houses[houseno], decision_dict[houseno]['RHC_RF'], energyD)
# plot_RHC("House F Cost value plot", windows, costs)

```

Optimal cost for RHC and Random Forest Regression found at window size:
8

Optimal cost is: 17618.784092686874



Hence we calculated the optimal cost for 3 Houses B, C and F for Linear Regression and Random Forest. For House B, we see Random Forest Data performs quite better as compared to linear regression.

Commitment Horizon Control

Now we run the predicted data through another online algorithm called Commitment Horizon Control.

The optimal values is calculated as :

$$\sum_{i=1}^I \text{price} * x_{\text{optimal}}[i] + a * \text{maximum}(0, \text{windowY}[i] - x_{\text{optimal}}[i]) + b * \text{abs}(x_{\text{optimal}}[i] - x_{\text{optimal}}[i-1])$$

We run the algorithm for a window size of 10 and the Commitment horizon values are varied to find the optimal cost of the CHC objective function. Commitment Horizon values are varied from 2 to 11 and the different cost values are plotted against it.

```

In [35]: def calc_CHC(houseno, y, predictionHorizon, commitmentHorizon, prediction_a
    T = 2*24*14;
    p = 0.4/2;
    a = 4/2;
    b = 4/2;
    optValues = np.zeros(T + 20);
    for horizonStart in range(0, T):
        horizonEnd = horizonStart + predictionHorizon
        windowY = y[horizonStart: horizonEnd]

        obj = 0;
        x = cp.Variable(predictionHorizon)

        for i in range(0, predictionHorizon):
            obj += p * x[i] + a * cp.maximum(0, windowY[i] - x[i])
            if i == 0:
                obj += b * cp.abs(x[i]); #because x(0) is 0
            else:
                obj += b * cp.abs(x[i] - x[i - 1])

        objective = cp.Minimize(obj)
        problem = cp.Problem(objective)
        result = problem.solve()

        for i in range(0, commitmentHorizon):
            optValues[horizonStart + i] += x.value[i];

    optValues = optValues/commitmentHorizon

    obj = 0;
    for i in range(0, T):
        obj += p * optValues[i] + a * max(0, y[i] - optValues[i])
        if i == 0:
            obj += b * abs(optValues[i]); #because x(0) is 0
        else:
            obj += b * abs(optValues[i] - optValues[i - 1])

    opt_dict[houseno]['CHC' + '_' + prediction_algo] = obj
    decision_dict[houseno]['CHC' + '_' + prediction_algo] = optValues

    return obj

```

```

In [36]: def plot_CHC(title, windows, costs):
    fig = plt.figure(figsize=(15, 4))
    plt.title(title)
    plt.plot(windows, costs, label = "Commitment Horizon Value")
    plt.legend()
    plt.ylabel("Cost Value")
    plt.xlabel("Commitment Horizon Size")

```

```
In [37]: def runCHC(houseno, predData, predictionHorizon, label):
costs = []
windows = []
for i in range(2,11):
    windows.append(i)
    costs.append(calc_CHC(houseno, predData.to_numpy(), predictionHoriz
x = calc_CHC(houseno, predData.to_numpy(), predictionHorizon, windows[c
print("Optimal cost for CHC found for House ", houses[houseno], "at co
print("\nOptimal cost is: ", x)
plot_CHC("Commitment Horizon Values for CHC and "+label + "| House " +
```

House B

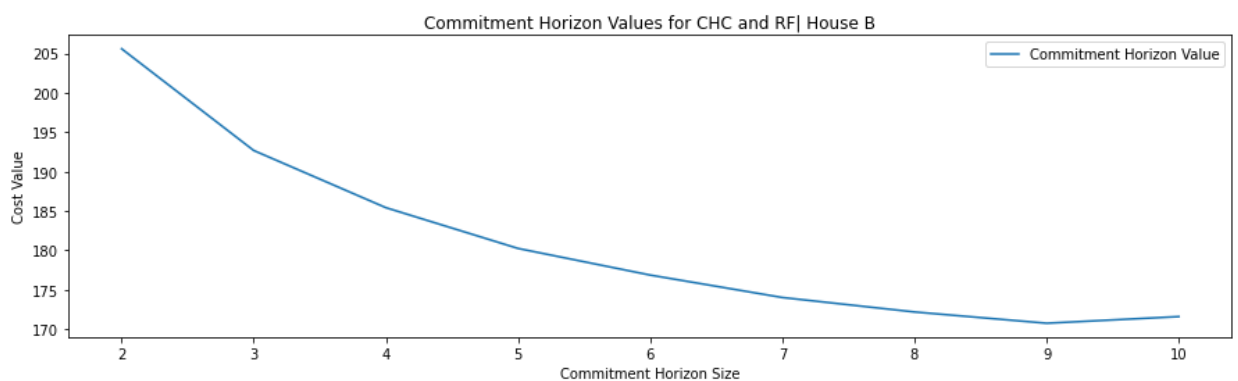
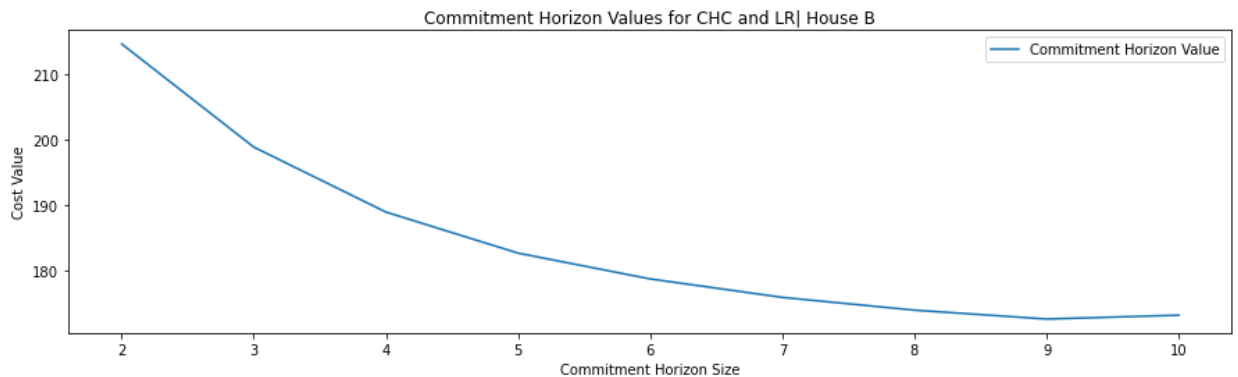
```
In [38]: runCHC(0, predictions[0][0], 10, "LR" )
runCHC(0, predictions[0][1], 10, "RF" )
```

Optimal cost for CHC found for House B at commitment horizon size 9

Optimal cost is: 172.49815019540276

Optimal cost for CHC found for House B at commitment horizon size 9

Optimal cost is: 170.7424917838389



House C

In [39]:

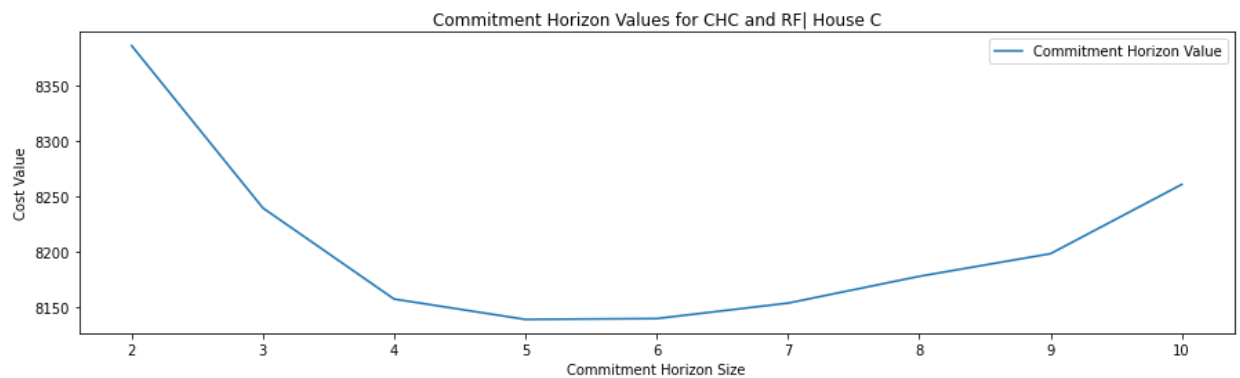
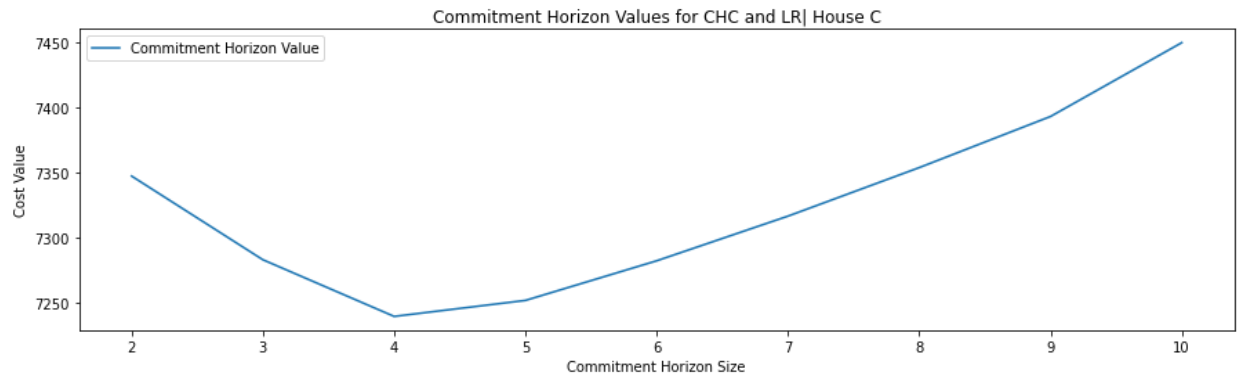
```
runCHC(1, predictions[1][0], 10, "LR" )  
  
runCHC(1, predictions[1][1], 10, "RF" )
```

Optimal cost for CHC found for House C at commitment horizon size 4

Optimal cost is: 7239.712430338386

Optimal cost for CHC found for House C at commitment horizon size 5

Optimal cost is: 8138.516449446927



House F

In [46]:

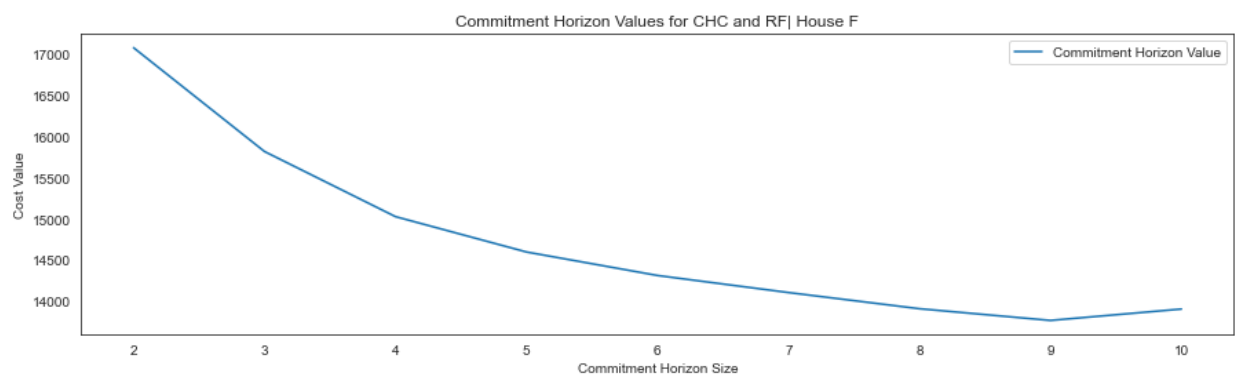
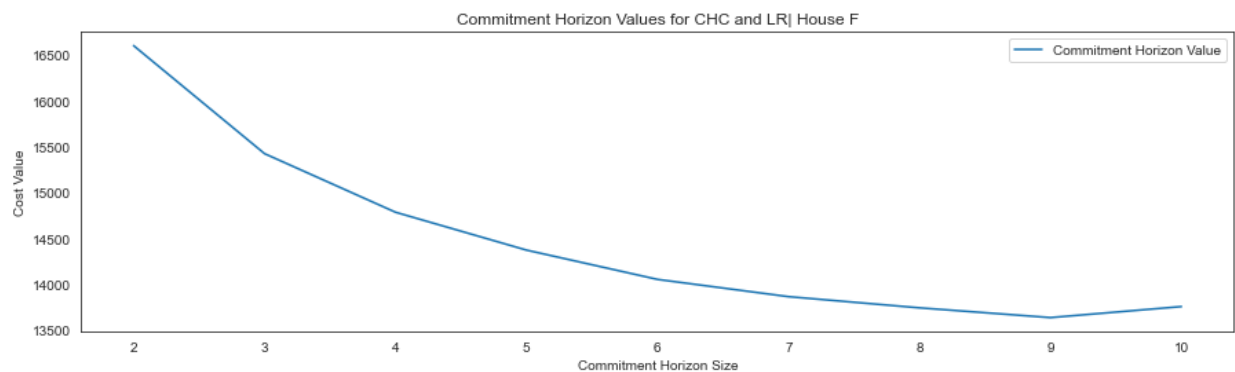
```
runCHC(2, predictions[2][0], 10, "LR" )  
runCHC(2, predictions[2][1], 10, "RF" )
```

Optimal cost for CHC found for House F at commitment horizon size 9

Optimal cost is: 13633.879284797671

Optimal cost for CHC found for House F at commitment horizon size 9

Optimal cost is: 13766.367281932491



Comparisons with Static Offline and Dynamic Offline Algorithms

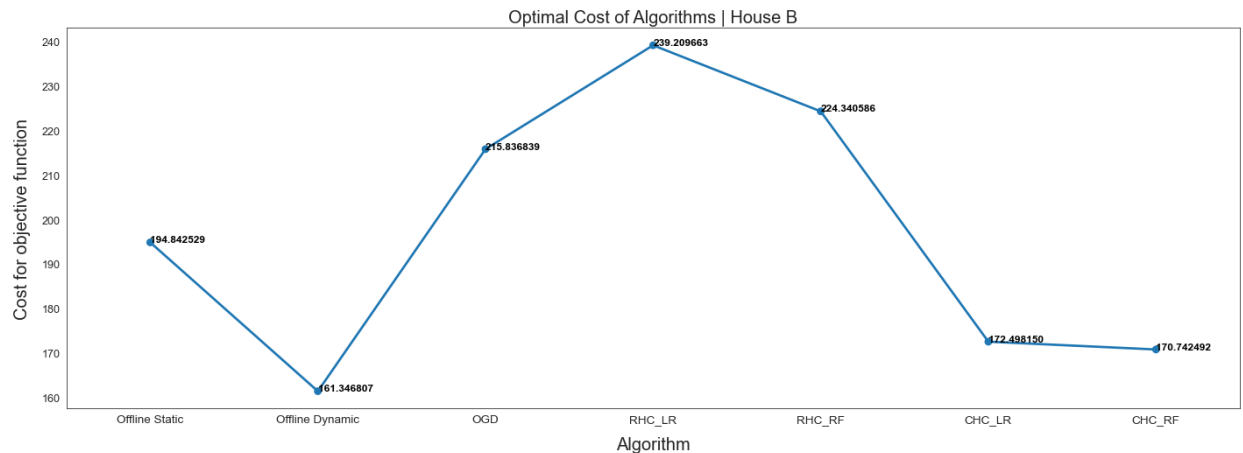
We now compare different algorithms by plotting the cost for objective function for different houses.

```
In [47]: houseno = 0
sns.set_style("white")
fig = plt.figure(figsize=(24, 8))
opts = opt_dict[houseno]
x=list(opts.keys())
ax = sns.pointplot(x=list(opts.keys()), y=[score for score in opts.values()
for i, score in enumerate(opts.values())]:
    ax.text(i, score + 0.002, '{:.6f}'.format(score), horizontalalignment='

plt.ylabel('Cost for objective function', size=20, labelpad=12.5)
plt.xlabel('Algorithm', size=20, labelpad=12.5)
plt.tick_params(axis='x', labelsize=13.5)
plt.tick_params(axis='y', labelsize=12.5)

plt.title('Optimal Cost of Algorithms | House B', size=20)

plt.show()
```




```

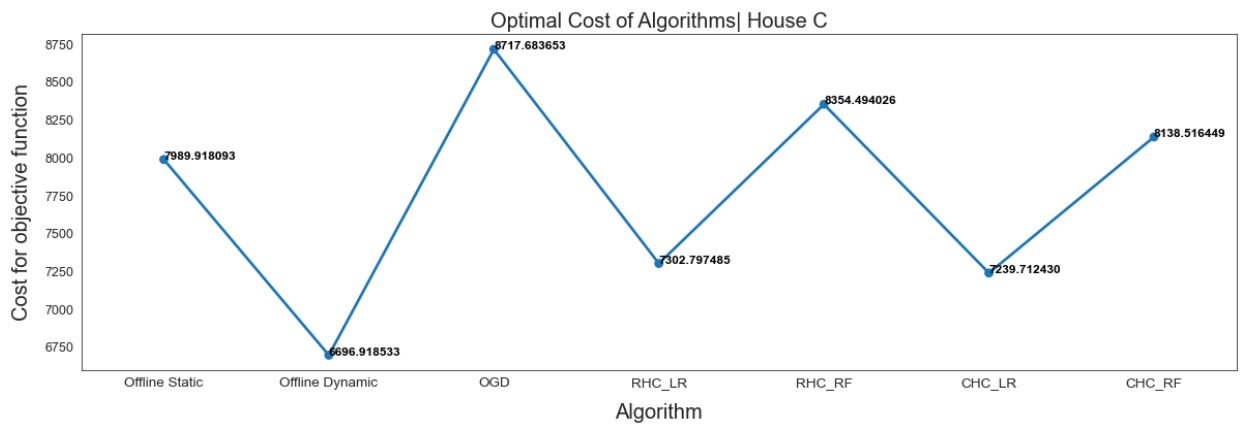
In [48]: seno = 1
         .set_style("white")
         = plt.figure(figsize=(20, 6))
         s = opt_dict[houseno]
         list(opts.keys())
         = sns.pointplot(x=list(opts.keys()), y=[score for score in opts.values()], m
         i, score in enumerate(opts.values()):
         ax.text(i, score + 0.002, '{:.6f}'.format(score), horizontalalignment='left

         .ylabel('Cost for objective function', size=20, labelpad=12.5)
         .xlabel('Algorithm', size=20, labelpad=12.5)
         .tick_params(axis='x', labelsize=13.5)
         .tick_params(axis='y', labelsize=12.5)

         .title('Optimal Cost of Algorithms| House C', size=20)

         .show()

```



```

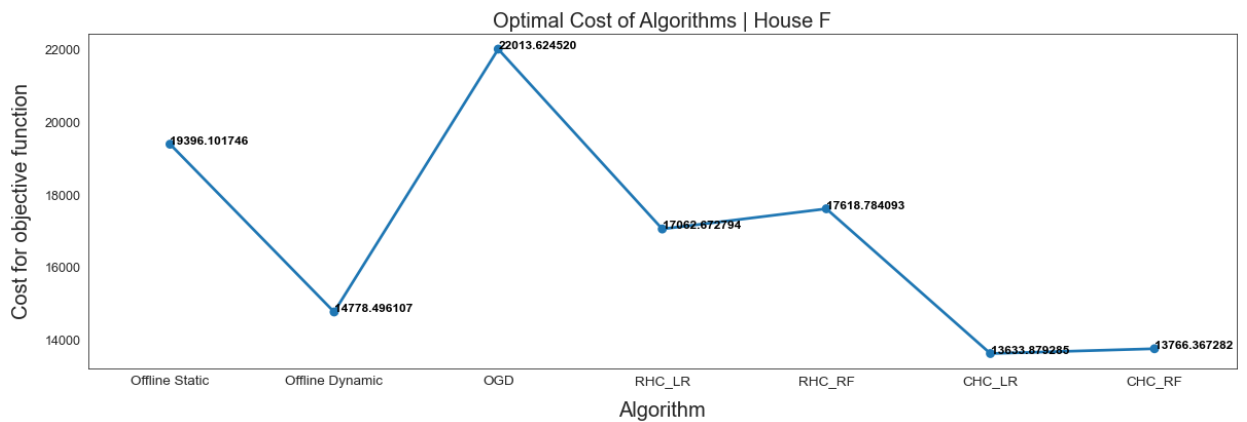
In [49]: o = 2
         t_style("white")
         plt.figure(figsize=(20, 6))
         opt_dict[houseno]
         (opts.keys())
         ns.pointplot(x=list(opts.keys()), y=[score for score in opts.values()], mark
         score in enumerate(opts.values()):
         .text(i, score + 0.002, '{:.6f}'.format(score), horizontalalignment='left',

         abel('Cost for objective function', size=20, labelpad=12.5)
         abel('Algorithm', size=20, labelpad=12.5)
         ck_params(axis='x', labelsz=13.5)
         ck_params(axis='y', labelsz=12.5)

         tle('Optimal Cost of Algorithms | House F', size=20)

         ow()

```



We observe that CHC performed better than RHC and OGD in most of the cases. Specifically for House B

Varying a and b for the best combination of control algorithm and prediction algorithm

Since we find for House B, the best performance is observed by CHC on Random Forest with commitment horizon size 9 with $a=4$, $b=4$. We now keep commitment horizon constant and vary first a keeping b as constant and then b , keeping a as constant. the values of penalty(a) and switching costs(b) in our objective function to see how our algorithms perform. We did this analysis and plotted graphs for each of the combination as shown below.

```

In [50]: def chc_vary_and_b(y, predictionHorizon, commitmentHorizon, prediction_algo):
    T = 2*24*14;
    p = 0.4/2;
    a = a/2;
    b = b/2;
    optValues = np.zeros(T + 20);
    for horizonStart in range(0, T):
        horizonEnd = horizonStart + predictionHorizon
        windowY = y[horizonStart: horizonEnd]

        obj = 0;
        x = cp.Variable(predictionHorizon)

        for i in range(0, predictionHorizon):
            obj += p * x[i] + a * cp.maximum(0, windowY[i] - x[i])
            if i == 0:
                obj += b * cp.abs(x[i]); #because x(0) is 0
            else:
                obj += b * cp.abs(x[i] - x[i - 1])

        objective = cp.Minimize(obj)
        problem = cp.Problem(objective)
        result = problem.solve()

        for i in range(0, commitmentHorizon):
            optValues[horizonStart + i] += x.value[i];

    optValues = optValues/commitmentHorizon

    obj = 0;
    for i in range(0, T):
        obj += p * optValues[i] + a * max(0, y[i] - optValues[i])
        if i == 0:
            obj += b * abs(optValues[i]); #because x(0) is 0
        else:
            obj += b * abs(optValues[i] - optValues[i - 1])

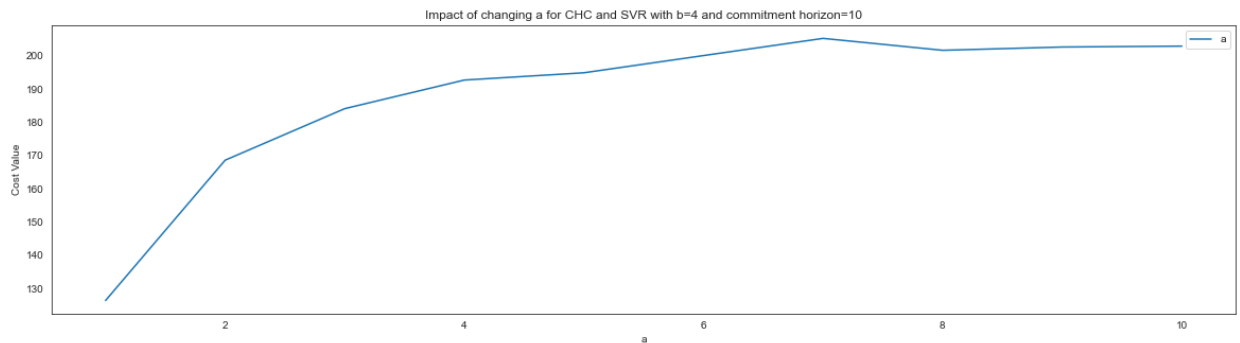
    return obj

```

```
In [51]: costs = []
windows = []
b = 4
for i in range(1,11):
    windows.append(i)
    costs.append(chc_vary_and_b(predictions[0][1].to_numpy(), 10, 3, 'RF',

fig = plt.figure(figsize=(20, 5))
plt.title("Impact of changing a for CHC and SVR with b=4 and commitment hor
plt.plot(windows, costs, label = "a")
plt.legend()
plt.ylabel("Cost Value")
plt.xlabel("a")
```

Out[51]: Text(0.5, 0, 'a')



The above graph shows the change in cost values for increasing the value of a, with commitment horizon size 10. The cost goes on increasing with increase in value of a.

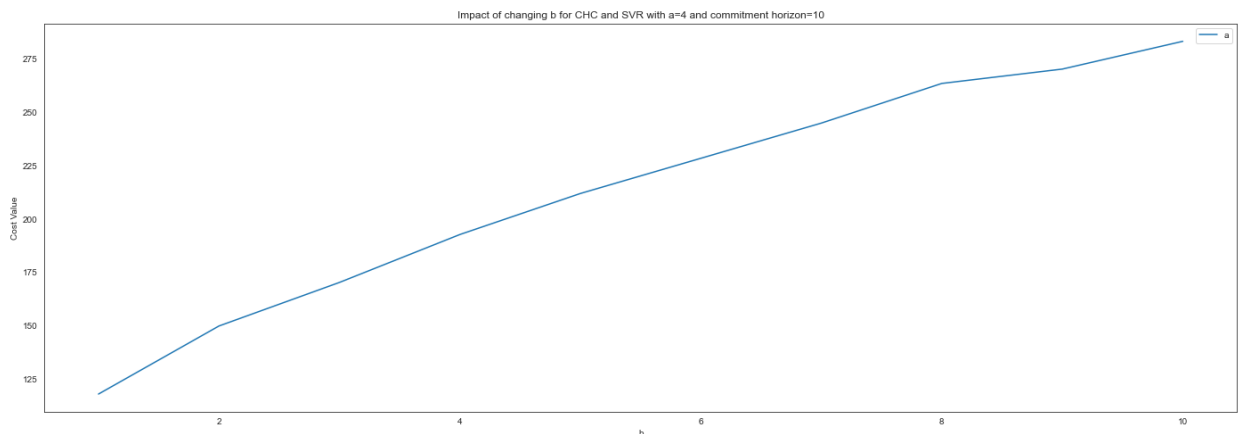
```

In [52]: costs = []
         windows = []
         a = 4
         for i in range(1,11):
             windows.append(i)
             costs.append(chc_vary_and_b(predictions[0][1].to_numpy(), 10, 3, 'RF',

fig = plt.figure(figsize=(24, 8))
plt.title("Impact of changing b for CHC and SVR with a=4 and commitment horizon=10")
plt.plot(windows, costs, label = "a")
plt.legend()
plt.ylabel("Cost Value")
plt.xlabel("b")

```

Out[52]: Text(0.5, 0, 'b')



The above graph shows the change in cost values for increasing the value of b , with commitment horizon size 10. The cost goes on increasing with increase in value of b , thus showing positive correlation with each other.

Algorithm Selection

If we wish to capture the best algorithm out of multiple algorithms for online convex optimization, we need to have constant performance criteria amongst all of them. Dynamic regret is taken factor is taken as the evaluation criteria, and the objective function is minimized for algorithms.

```

In [53]: def online_gradient_descent_fixed_window(y, steps):
    n = 4
    x = [0.0] * (n + 1)
    x[1] = 0
    p = 0.4/2
    a = 4/2
    b = 4/2
    for t in range(1, n):
        if (y[t] > x[t]):
            if (x[t] > x[t - 1]):
                slope = p - a + b;
            else:
                slope = p - a - b;
        else:
            if (x[t] > x[t - 1]):
                slope = p + b;
            else:
                slope = p - b;
        x[t + 1] = x[t] - steps * slope
    return x

def rhc_fixed_window(y, predictionHorizon, prediction_algo):
    T = 4;
    p = 0.4/2;
    a = 4/2;
    b = 4/2;
    optValues = np.zeros(T);
    for horizonStart in range(0, T):
        horizonEnd = horizonStart + predictionHorizon
        windowY = y[horizonStart: horizonEnd]

        obj = 0;
        x = cp.Variable(predictionHorizon)

        for i in range(0, predictionHorizon):
            obj += p * x[i] + a * cp.maximum(0, windowY[i] - x[i])
            if i == 0:
                obj += b * cp.abs(x[i]); #because x(0) is 0
            else:
                obj += b * cp.abs(x[i] - x[i - 1])

        objective = cp.Minimize(obj)
        problem = cp.Problem(objective)
        result = problem.solve()

        optValues[horizonStart] = x.value[0];

    obj = 0;
    for i in range(0, T):
        obj += p * optValues[i] + a * max(0, y[i] - optValues[i])
        if i == 0:
            obj += b * abs(optValues[i]); #because x(0) is 0
        else:
            obj += b * abs(optValues[i] - optValues[i - 1])

    return obj

```

```

def chc_fixed_window(y, predictionHorizon, commitmentHorizon, prediction_al
    T = 4;
    p = 0.4/2;
    a = 4/2;
    b = 4/2;
    optValues = np.zeros(T + 20);
    for horizonStart in range(0, T):
        horizonEnd = horizonStart + predictionHorizon
        windowY = y[horizonStart: horizonEnd]

        obj = 0;
        x = cp.Variable(predictionHorizon)

        for i in range(0, predictionHorizon):
            obj += p * x[i] + a * cp.maximum(0, windowY[i] - x[i])
            if i == 0:
                obj += b * cp.abs(x[i]); #because x(0) is 0
            else:
                obj += b * cp.abs(x[i] - x[i - 1])

        objective = cp.Minimize(obj)
        problem = cp.Problem(objective)
        result = problem.solve()

        for i in range(0, commitmentHorizon):
            optValues[horizonStart + i] += x.value[i];

    optValues = optValues/commitmentHorizon

    obj = 0;
    for i in range(0, T):
        obj += p * optValues[i] + a * max(0, y[i] - optValues[i])
        if i == 0:
            obj += b * abs(optValues[i]); #because x(0) is 0
        else:
            obj += b * abs(optValues[i] - optValues[i - 1])

    return obj

def cost_fixed_window(x, y):
    cost = 0
    p = 0.4/2
    a = 4/2
    b = 4/2
    for i in range(1, 5):
        cost += p * x[i] + a * max(0, y[i] - x[i] + b * abs(x[i] - x[i - 1])

    return cost

def offline_dynamic_provision_fixed_window(y):
    p = 0.4/2
    a = 4/2
    b = 4/2
    x = cp.Variable(4)
    cost = 0

```

```
for i in range(1,4):
    cost += p*x[i] + a*cp.maximum(0, y[i-1] - x[i]) + b*cp.abs(x[i]-x[i-1])

objective = cp.Minimize(cost)
constraints = [x[0] == 0, x[1:] >= 0]
problem = cp.Problem(objective, constraints)
result = problem.solve()
opt = np.array(x.value)
opt = np.insert(opt, 0, 0., axis=0)

return opt
```

Deterministic Approach

The algorithm followed in the Deterministic approach is as follows:

1. Choose a fixed window size. Ex. $w = 4$ and different time slots t_1 & t_2 at step size 4
2. Now, we need to iterate over the time horizon ($T=672$) with step size = window size
3. In each window, evaluate the objective function value for each algorithm
4. The algorithm which gives the value closest as compared to the offline algorithm wins that round or window size
5. We then measured the number of times OGD, RHC and CHC won respectively
6. In the end, The algorithm which won the maximum number of times is the winner


```
In [54]: import operator

def deterministicApproach(y):
    win_ogd = 0;
    win_rhc = 0;
    win_chc = 0;
    obj_diff_dict = {}
    y = y.to_numpy()
    for i in range(1, 673):
        obj_ogd = cost_fixed_window(online_gradient_descent_fixed_window(y, 0.0
        obj_rhc = rhc_fixed_window(y[i:], 3, 'LR')
        obj_chc = chc_fixed_window(y[i:], 10, 9, 'LR')
        obj_offline_dynamic = cost_fixed_window(offline_dynamic_provision_fixed
        obj_diff_dict['OGD'] = abs(obj_offline_dynamic - obj_ogd)
        obj_diff_dict['RHC'] = abs(obj_offline_dynamic - obj_rhc)
        obj_diff_dict['CHC'] = abs(obj_offline_dynamic - obj_chc)
        optimal_algo = min(obj_diff_dict.items(), key=operator.itemgetter(1))[0]

        if optimal_algo == 'OGD':
            win_ogd += 1
        elif optimal_algo == 'RHC':
            win_rhc += 1
        else:
            win_chc += 1

    obj_win_dict = {}
    obj_win_dict['OGD'] = win_ogd
    obj_win_dict['RHC'] = win_rhc
    obj_win_dict['CHC'] = win_chc
    print(obj_win_dict)
    return max(obj_win_dict.items(), key=operator.itemgetter(1))[0]
```

```
In [55]: print('The winner for deterministic approach for HOUSE B is: ',deterministi
{'OGD': 89, 'RHC': 5, 'CHC': 578}
The winner for deterministic approach for HOUSE B is:  CHC
```

```
In [56]: print('The winner for deterministic approach for HOUSE C is: ',deterministi
{'OGD': 0, 'RHC': 0, 'CHC': 672}
The winner for deterministic approach for HOUSE C is:  CHC
```

```
In [57]: print('The winner for deterministic approach for HOUSE F is: ',deterministi
{'OGD': 183, 'RHC': 28, 'CHC': 461}
The winner for deterministic approach for HOUSE F is:  CHC
```

We observed that CHC won most of the times, providing the optimal value as compared to the offline algorithm. Our observed order was CHC > OGD > RHC

Randomized Algorithm

Randomized Algorithm

The randomized algorithm is as follows.

1. We assign random weights to each algorithm. Ex. w_1 , w_2 , w_3
2. Pick a window size. Say 4
3. Run all 3 algorithms on each window
4. After each iteration,
 - a. Rank the algorithms on the basis of performance
 - b. Update the weights using any heuristic. We incremented the weight of winner by 0.1 and decreased the weight of loser by 0.1.
5. After all iterations, the final values of weights gives optimal value

```

In [58]: import math

obj_wt_dict = [{}, {}, {}]

def randomizeAlgo(y, houseno):
    wt_ogd = 1/3;
    wt_rhc = 1/3;
    wt_chc = 1/3;
    obj_diff_dict = {}
    y = y.to_numpy()

    for i in range(1, 673):
        obj_ogd = cost_fixed_window(online_gradient_descent_fixed_window(y, 0.0
        obj_rhc = rhc_fixed_window(y[i:], 3, 'LR')
        obj_chc = chc_fixed_window(y[i:], 10, 9, 'LR')
        obj_offline_dynamic = cost_fixed_window(offline_dynamic_provision_fixed
        obj_diff_dict['OGD'] = abs(obj_offline_dynamic - obj_ogd)
        obj_diff_dict['RHC'] = abs(obj_offline_dynamic - obj_rhc)
        obj_diff_dict['CHC'] = abs(obj_offline_dynamic - obj_chc)
        most_optimal_algo = min(obj_diff_dict.items(), key=operator.itemgetter(
        least_optimal_algo = max(obj_diff_dict.items(), key=operator.itemgetter

    if i > 1:
        if most_optimal_algo == 'OGD':
            wt_ogd += 0.0005
        elif most_optimal_algo == 'RHC':
            wt_rhc += 0.0005
        else:
            wt_chc += 0.0005

        if least_optimal_algo == 'OGD':
            wt_ogd -= 0.0005
        elif least_optimal_algo == 'RHC':
            wt_rhc -= 0.0005
        else:
            wt_chc -= 0.0005

    last_winner = most_optimal_algo
    last_loser = least_optimal_algo

    obj_wt_dict[houseno] = {}
    obj_wt_dict[houseno]['OGD'] = wt_ogd
    obj_wt_dict[houseno]['RHC'] = wt_rhc
    obj_wt_dict[houseno]['CHC'] = wt_chc
    return obj_wt_dict

```

```

In [59]: randomizeAlgo(predictions[0][1], 0)
print('The final weights for randomized approach for House B is: ', obj_wt

```

```

The final weights for randomized approach for House B is: {'OGD': 0.3758
333333333335, 'RHC': 0.005333333333333330235, 'CHC': 0.61883333333333204}

```

```
In [60]: randomizeAlgo(predictions[1][1], 1)
print('The final weights for randomized approach for House C is: ', obj_wt)
```

The final weights for randomized approach for House C is: {'OGD': 0.3333333333333333, 'RHC': -0.00216666666666669775, 'CHC': 0.66883333333333149}

```
In [61]: randomizeAlgo(predictions[2][1], 2)
print('The final weights for randomized approach for House F is: ', obj_wt)
```

The final weights for randomized approach for House F is: {'OGD': 0.4088333333333334, 'RHC': 0.036833333333333305, 'CHC': 0.55433333333333275}

For e.g. : For House B, Our final weights are $0.405 * \text{OGD} + 0.056 * \text{RHC} + 0.537 * \text{CHC}$. We can see that the Sum of weights is equal to 1.

```
In [62]: gorithmsCompare(y, houseno):
y.to_numpy()
deterministic = 0
offline_dynamic = 0
randomized = 0

i in range(1, 673):
j_deterministic += chc_fixed_window(y[i:], 10, 9, 'LR')
j_offline_dynamic += cost_fixed_window(offline_dynamic_provision_fixed_window(y[i:], 10, 9, 'LR'))
j_randomized += obj_wt_dict[houseno]['CHC']*chc_fixed_window(y[i:], 10, 9, 'LR')

dict = {}
dict['Deterministic'] = obj_deterministic
dict['Offline Dynamic'] = obj_offline_dynamic
dict['Randomized'] = obj_randomized
t("House "+houses[houseno]+" : Randomized Algorithm Selection")
t(obj_dict)

rn max(obj_dict.items(), key=operator.itemgetter(1))[0]
```

```
In [63]: algorithmsCompare(predictions[0][1], 0)
```

House B : Randomized Algorithm Selection
{'Deterministic': 2978.3389955386256, 'Offline Dynamic': 3032.72725030731, 'Randomized': 3168.148907959773}

Out[63]: 'Randomized'

```
In [64]: algorithmsCompare(predictions[1][1], 1)
```

House C : Randomized Algorithm Selection
{'Deterministic': 218889.10749781667, 'Offline Dynamic': 213351.45390163022, 'Randomized': 230866.34005066013}

Out[64]: 'Randomized'

```
In [65]: algorithmsCompare(predictions[2][1], 2)
```

```
House F : Randomized Algorithm Selection  
{'Deterministic': 200140.99417846955, 'Offline Dynamic': 211817.496378074  
9, 'Randomized': 209840.15772000447}
```

```
Out[65]: 'Offline Dynamic'
```

In the above section we capture the objective function value for Offline Dynamic, Deterministic and Randomized approaches. The Randomized algorithm is the closest to Offline Dynamic (which is taken as a baseline here) and thus it performs better.