

## Lecture :- Sliding window

### Agenda

- Boundary print of matrix.
- Spiral print of matrix
- Sliding window technique
  - Max subarray sum of len = k
  - Minimum swaps.

Class starts at 8:35 pm.

Ques Given mat[n][n] , print boundary (clockwise)  
 rows and cols are equal

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

print :-

op →

1	2	3	4	5
10	15	20	25	
24	23	22	21	
16	11	6		

childish approach.

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

1st row:- 1 2 3 4 5  
 last col:- 5 10 15 20 25  
 → last row:- 25 24 23 22 21  
 1st col:- 21 16 11 6 1

# Observation

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

→ Yellow : 1 2 3 4  
Red : 5 10 15 20  
Blue : 25 24 23 22  
Green : 21 16 11 6

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Yellow:  $(n-1)$  el.

$i$        $j$   
 0      0  $\rightarrow$  1  
 +1  
 0      1  $\rightarrow$  2  
 +1  
 0      2  $\rightarrow$  3  
 +1  
 0      3  $\rightarrow$  4  
 +1  
 0      4  $\rightarrow$  stop

Red:  $(n-1)$  el

$i$        $j$   
 0      4  $\rightarrow$  5  
 +1  
 1      4  $\rightarrow$  10  
 +1  
 2      4  $\rightarrow$  15  
 +1  
 3      4  $\rightarrow$  20  
 +1  
 4      4  $\rightarrow$  stop

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Blue:  $(n-1)$  el

$i$        $j$   
 4      4  $\rightarrow$  25  
 -1  
 4      3  $\rightarrow$  24  
 -1  
 4      2  $\rightarrow$  23  
 -1  
 4      1  $\rightarrow$  22  
 -1  
 4      0  $\rightarrow$  stop

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Green:

$(n-1)$  el

$i$        $j$   
 4      0  $\rightarrow$  21  
 -1  
 3      0  $\rightarrow$  16  
 -1  
 2      0  $\rightarrow$  11  
 -1  
 1      0  $\rightarrow$  6  
 -1  
 0      0  $\rightarrow$  stop

```
void printBoundary(int[][] mat) {  
    square
```

```
    int n = mat.length;
```

```
    int i = 0;
```

```
    int j = 0;
```

```
    // Print yellow.
```

```
    for (print = 1; print <= n - 1; print++) {  
        print (mat[i][j]);  
        j++;  
    }
```

```
    // Print Red
```

```
    for (print = 1; print <= n - 1; print++) {  
        print (mat[i][j]);  
        i++;  
    }
```

```
    // Print Blue
```

```
    for (print = 1; print <= n - 1; print++) {  
        print (mat[i][j]);  
        j--;
```

```
    // Print Green
```

```
    for (print = 1; print <= n - 1; print++) {  
        print (mat[i][j]);  
        i--;
```

```
}
```

TC:  $O(n)$ .

SC:  $O(1)$

Ques: Spiral print [mat[n][n]]

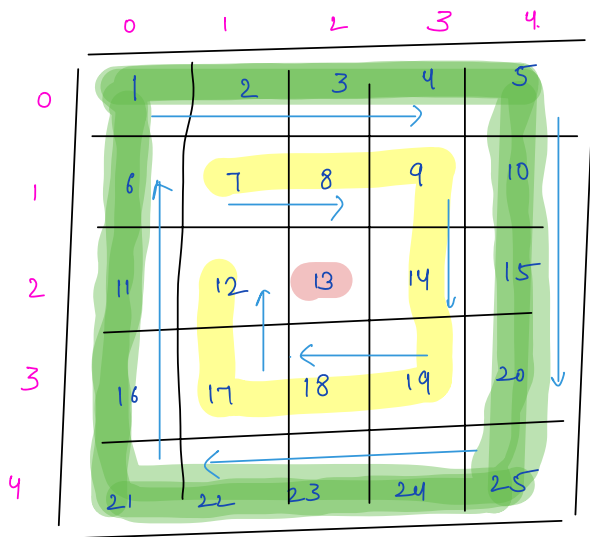
	0	1	2	3	4	5
0	1	2	3	4	5	6
1	7	8	9	10	11	12
2	13	14	15	16	17	18
3	19	20	21	22	23	24
4	25	26	27	28	29	30
5	31	32	33	34	35	36

op →

1 2 3 4 5 6  
 12 18 24 30 36  
 35 34 33 32 31  
 25 19 13 7 8  
 9 10 11 17 23  
 29 28 27 26  
 20 14 15 16  
 22 21

colour	i	j	no of el to print in each color of boundary
Yellow. (outer bound ary).	0 ↓ +1	0 ↓ +1	5 · (n-1) ↓ -2 $\begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 6 & 12 & 18 & 24 & 30 \\ 36 & 35 & 34 & 33 & 32 \\ 31 & 25 & 19 & 13 & 7 \end{bmatrix}$
Red.	1 ↓ +1	1 ↓ +1	3 (n-3) ↓ -2 $\begin{bmatrix} 8 & 9 & 10 \\ 11 & 17 & 23 \\ 29 & 28 & 27 \\ 26 & 20 & 14 \end{bmatrix}$
Blue	2	2	1 · n-5 ↓ -2 $\begin{bmatrix} 15 & 16 \\ 21 & 22 \end{bmatrix}$ (-1) [stop].

Edge case:



$n \times n = 5 \times 5$  matrix.

colour	i	j	no of el to print in each color of boundary
Green	0 ↓ +1	0 ↓ +1	4 (n-1) ↓ -2
Yellow	1 ↓ +1 2	1 ↓ +1 2	2 (n-3) ↓ -2 0 → stopping

100% sure, only one el would  
left for print. Handle explicitly.

```

void spiralPrint (int[][] mat) {
    int n = mat.length;
    int i = 0, j = 0, steps = n-1;
    while (steps >= 0) {
        if (steps == 0) {
            print(mat[i][j]);
            break;
        }
        // first row (excluding last el)
        for (print = 1; print <= steps; print++) {
            print (mat[i][j] );
            j++;
        }

        // last col (excluding last el)
        for (print = 1; print <= steps; print++) {
            print (mat[i][j] );
            i++;
        }

        // last row (excluding last el)
        for (print = 1; print <= steps; print++) {
            print (mat[i][j] );
            j--;
        }

        // first col (excluding last el)
        for (print = 1; print <= steps; print++) {
            print (mat[i][j] );
            i--;
        }

        step = step - 2;
        i++;
        j++;
    }
}

```

TC:  $O(n^2)$

SC:  $O(1)$



Sliding window technique (fixed window length).  $\rightarrow$  carry forward 2.0

Q.3. Given  $arr[n]$ , return max subarray sum in array. of  $len=k$

Example:  $arr[9] = \begin{bmatrix} 2 & 4 & 3 & 7 & 9 & 8 & 6 & 5 & 4 \end{bmatrix}$   $ans = 24$   
 $len = 3$ .

subarray =  $arr[s, e] \rightarrow$  sum = Prefix sum.

$arr[9] = \begin{bmatrix} 2 & 4 & 3 & 7 & 9 & 8 & 6 & 5 & 4 \end{bmatrix}$   $k=3$

$pf[9] = \begin{bmatrix} 2 & 6 & 9 & 16 & 25 & 33 & 39 & 44 & 48 \end{bmatrix}$

Dry run:

$s$	$e$	$sum[s, e] = pf[e] - pf[s-1]$	max. $(-\infty)$
0	2	$pf[2] = 9$	9
1	3	$pf[3] - pf[0]$ $16 - 2 = 14$	14
2	4	$pf[4] - pf[1]$ $25 - 6 = 19$	19
3	5	$pf[5] - pf[2]$ $33 - 9 = 24$	24
4	6	$pf[6] - pf[3]$ $39 - 16 = 23$	24
$\vdots$	$\vdots$	$\vdots$	$\vdots$
6	8	$\vdots$	$\vdots$

arr[s, e]  
 (0 k-1)  
 k-1-0+1  
(k)

```
int maximum(int[] arr, int k) {
    int[] pf = prefixOptional(arr);
    int s = 0; int n = arr.length;
    int e = k-1; int max = Integer.MIN_VALUE;
    while( e < n ) {
        if( s == 0 ) {
            max = Math.max(max, pf[e]);
        } else {
            max = Math.max(max, pf[e] - pf[s-1]);
        }
        s++;
        e++;
    }
    return max;
}
```

TC:  $O(n)$

SC:  $O(n)$

Approach 2

SC:  $O(1)$ .

$arr[9] = \left[ \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 2 & 4 & 3 & 7 & 9 & 8 & 6 & 5 & 4 \end{matrix} \right] \quad k=3$

$$S_y = 9.$$

$$S_g = S_y - 2 + 7$$

$$S_b = S_g - 4 + 9.$$

$$S_r = S_b - 3 + 8.$$

window	s	e	sum	max
1st	0	$2(k-1)$	9	9
2nd	1	$3(k)$	$9 - 2 + 7 = 14$ $\uparrow \quad \uparrow \quad \uparrow$ sum arr[s] arr[e] $sum - arr[s-1] + arr[e]$	14
3rd	2	4	$14 - 4 + 9 = 19$ $\uparrow \quad \uparrow \quad \uparrow$ sum arr[s-1] arr[e]	19.
⋮	⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮	⋮
x window	s	e	$sum - arr[s-1] + arr[e]$	$\max(\max, sum)$

↑  
edge case:-

$$s=0$$

{ handle the sum explicitly }

```

int subarrayOfSumK( int[] arr, int k) {
    int sum = 0;
    // sum of 1st window , s = 0 , e = k-1.
    for( i = 0; i < k; i++) {
        sum += arr[i];
    }
    int max = sum;
    int s = 1;
    int e = k;
    while( e < n) {
        sum = sum - arr[s-1] + arr[e];
        max = Math.max( max, sum);
        s++;
        e++;
    }
    return max;
}

```

TC:  $O(n)$

SC:  $O(1)$

Ques 4

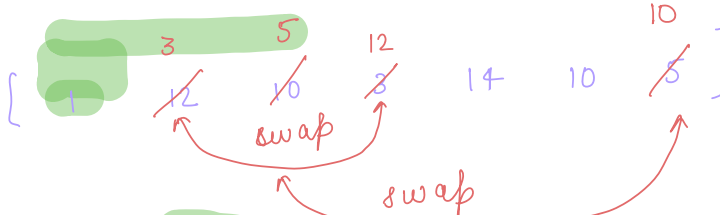
**Min swaps :-** Given  $arr[n]$  and integer  $B$ .

find and return the min no of swaps required to bring all no less than  $B$  together or equal to

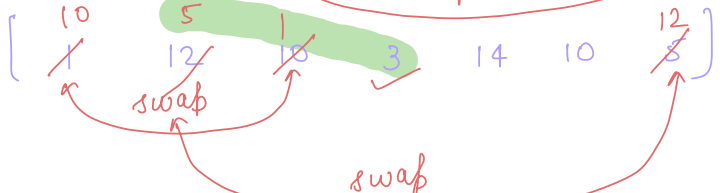
$arr[7] = [1, 12, 10, 3, 14, 10, 5]$

$B = 6$

Possibility 1:  $[1, 12, 10, 3, 14, 10, 5] \rightarrow 2 \text{ swaps.}$



Poss 2:  $[1, 12, 10, 3, 14, 10, 5] \rightarrow 2 \text{ swaps.}$



**Constraint:** SC:  $O(1)$

Idea:

$arr[10] = [1, 12, 6, 3, 8, 13, 15, 13, 4, 5]$

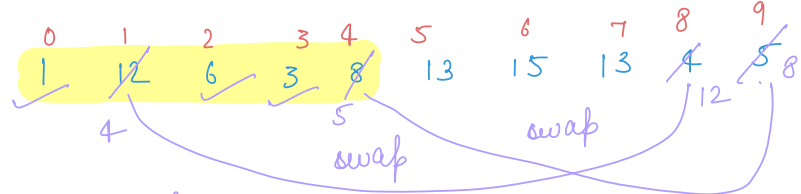
$B = 7$

window len = no of el smaller than 7. (5).

Dry run:

1:  $s = 0, e = 4$

$[1, 12, 6, 3, 8, 13, 15, 13, 4, 5]$

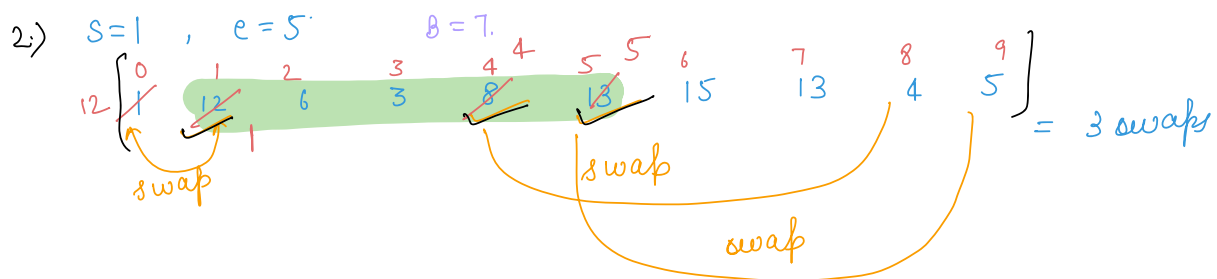


count el  $< B = 3$  el.  
(7)

swaps = len of window - count  
(or)

swaps = no of el greater than  $B$ .

2 swaps.



Generalisation:

swaps required in a window  $[s, e]$  = no of el. greater than  $B$ .

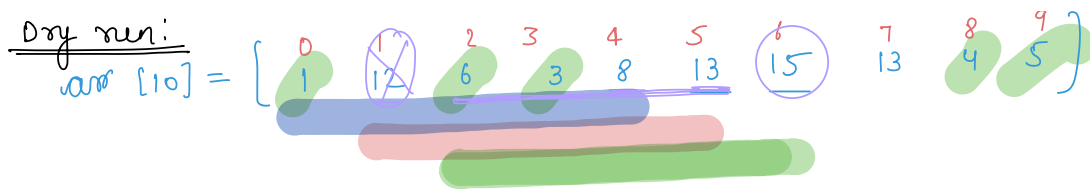
arr [10] = [1, 12, 6, 3, 8, 13, 15, 13, 4, 5]

$B=7$ .

len of window = 5 (el smaller than  $B$  or equal to)

s	e	count of el greater than $B$ (count)	swaps	ans (+2)
0	4 ( $k-1$ )	12, 8 = 2	2	2
1	5 (len)	$2 - \left[ \begin{array}{l} \text{if } \text{arr}[s-1] > 7 \rightarrow 1 \\ \text{else } \rightarrow 0 \end{array} \right]$ $+ \left[ \begin{array}{l} \text{if } \text{arr}[e] > 7 \rightarrow 1 \\ \text{else } \rightarrow 0 \end{array} \right]$ $2 - 0 + 1 = 3$	3	2
⋮	⋮	⋮	⋮	⋮
s	e	count — $\left[ \begin{array}{l} \text{if } \text{arr}[s-1] > B \rightarrow 1 \\ \text{else } \rightarrow 0 \end{array} \right]$ $+ \left[ \begin{array}{l} \text{if } \text{arr}[e] > B \rightarrow 1 \\ \text{else } \rightarrow 0 \end{array} \right]$	edge case $s=0$	

Dry run:



s = 2, e = 5

$$\text{count} = \underline{3} - \left[ \begin{array}{l} 12 > 7 \rightarrow 1 \\ \text{else} \rightarrow 0 \end{array} \right] + \left[ \begin{array}{l} 15 > 7 \rightarrow 1 \\ \text{else} \rightarrow 0 \end{array} \right]$$

$$3 - 1 + 1 = 2.$$

Implementation:

```
int minSwaps(int[] arr, int B) {
```

```
    int len = 0;    int count = 0;
```

```
    for (i = 0; i < arr.length; i++) {
```

```
        if (arr[i] <= B) {
```

```
            len++;
```

```
        }
```

```
    }
```

```
    // s = 0, first window
```

```
    for (i = 0; i < len; i++) {
```

```
        if (arr[i] > B) {
```

```
            count++;
```

```
        }
```

```
    }
```

```
    int ans = count;
```

```
    int s = 1;
```

```
    int e = len;
```

```

while ( e < arr.length ) {
    if ( arr[s-1] > B ) {
        count = count - 1;
    }
    if ( arr[e] > B ) {
        count = count + 1;
    }
    ans = Math.min( ans, count );
    s++;
    e++;
}
return ans;
}

```

TC:  $O(n)$

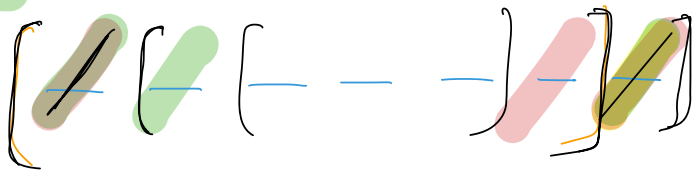
SC:  $O(1)$ .

Thankyou 😊

H/w:- Try out boundary & spiral for  $mat[n][m]$ .



Doubts



$$B - \boxed{\text{len} - B}$$

~~$\phi$~~