

Lecture ÷ Hashing I

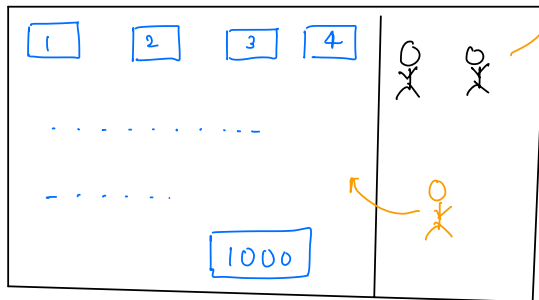
Agenda

- Introduction.
- frequency of each element
- first non-repeating element
- Hashset Introduction.
- # distinct elements.

class starts at 7:05 AM

Introduction

Priyanka



receptionist

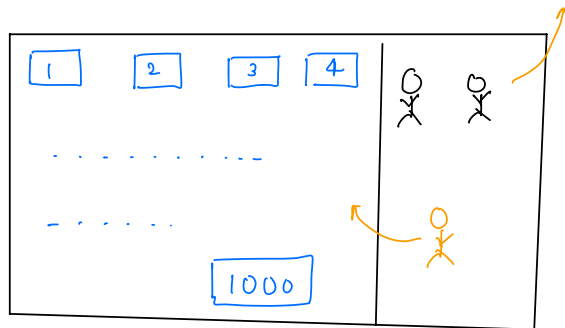
Register

Room no	Availability
1	✓
2	x
3	✓
4	✓
5	x
⋮	
1000	✓

Room ↑

searching through register

becomes tedious



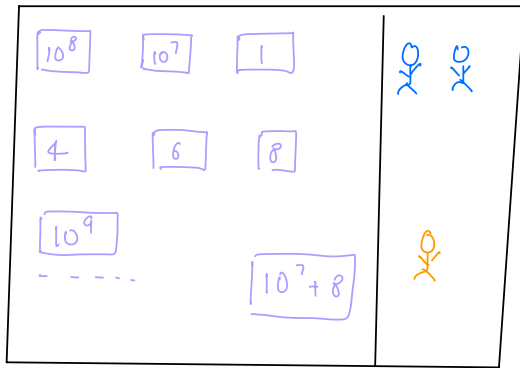
boolean[] available rooms =
new boolean[1001]

f	t	t	f		t
0	1	2	...		10000

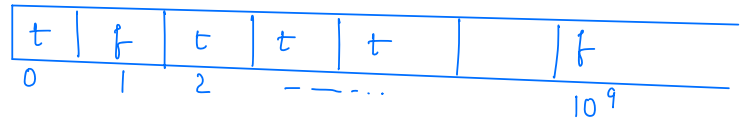
is room no 7068 empty?

availableRooms[7068] = true [empty]

= false [not empty]



boolean availableRooms[$10^9 + 1$]



Issue: for 10,000 rooms, priyanka created $10^9 + 1$ size array

[Room no] [Availability]

key	Table	value
1	—	true
2	—	false
3	—	false
4	—	true
5	—	true
⋮		⋮

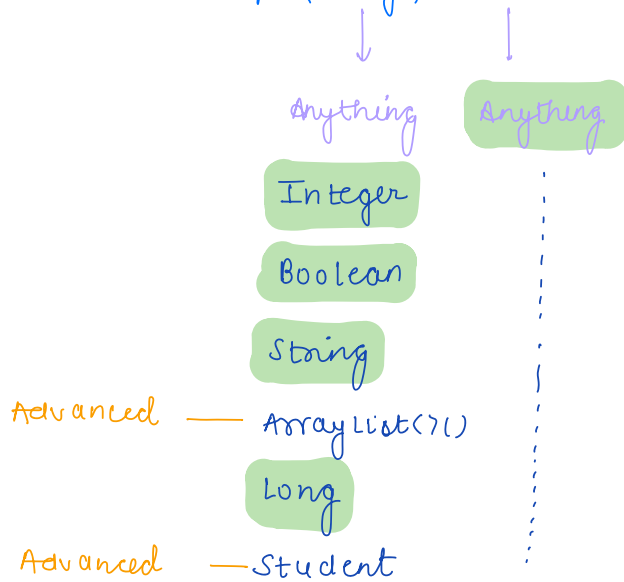
saving lot of space ←

7068 is available? $O(1)$ time complexity

HashMap table like structure [dynamic in size]
(key, value)

Things to know

HashMap < key, value > map = new HashMap<>();



Example 1:

Store population of each country

key: country name \rightarrow string

value: population \rightarrow Long | Integer

```
HashMap<String, Integer> map = new HashMap<>();
```

key	value
USA	330000..
India	143000---
China	140000----

Ex 2: for every country, we want to know state names

key: country name (string)

value: All states List<string>

```
HashMap<String, ArrayList<String>> statesMap;
```

Ex 3: for every country, store population of each state

key: country name string

value: population of each state

Map<string, Integer>

```
HashMap<String, HashMap<String, Integer>> map;
```

Operations on hashmap

1. **Insert** `HashMap<Integer, Boolean> map`

```
map.put(2, true)
map.put(3, false)
map.put(4, true)
map.put(2, false)
```

(Integer) Boolean	
key	value
2	true false
3	false
4	true
2	false

All the keys of hashmap are unique

2. size of hashmap \Rightarrow `map.size()` = 3

3. **Get value of a key:**

```
map.get(4) // true
```

```
map.get(2) // false
```

```
map.get(11) // null
```

4. Check whether a key is present or not?

```
map.containsKey(4) // true
```

```
map.containsKey(11) // false
```

All these operations have $O(1)$ TC.

Advanced module

Ques Given $arr[n]$ and Q queries, for every query, find freq of each element in array.

$arr[10] = [\overset{0}{2} \overset{1}{6} \overset{2}{3} \overset{3}{8} \overset{4}{2} \overset{5}{8} \overset{6}{3} \overset{7}{8} \overset{8}{10} \overset{9}{1}]$

queries

2 — 2
8 — 3
10 — 1
49 — 0

```
void printFreq(int[] arr, int[] queries) {  
    Q — for(int i=0; i < queries.length; i++) {  
        int el = queries[i];  
        int count = 0;  
        n — for(int j : arr) {  
            if (j == el) {  
                count++;  
            }  
        }  
        print(count);  
    }  
}
```

TC: $O(Q * n)$

SC: $O(1)$

Approach 2

key: array el (Integer)

value: count of each array el (Integer)

HashMap<Integer, Integer> freqMap.

arr[10] = [⁰2 ¹6 ²3 ³8 ⁴2 ⁵8 ⁶3 ⁷8 ⁸10 ⁹1]

↑ ↑ ↑ ↑ ↑ ↑

present in map ↗ arr[i]
not present in map ↘

1. Get freq of arr[i]

2. freq = freq + 1

3. map.put(arr[i], freq)

map.put(arr[i], 1)

key	value
2	1 2
6	1
3	1 2
8	1 2
10	1
	1


```
void printfreq(int[] arr, int[] a) {
```

```
    HashMap<Integer, Integer> map =
```

```
        new HashMap<>();
```

```
    o(n) — for (int el : arr) {
```

```
        o(1) — if (map.containsKey(el)) {
```

```
            o(1) — 1. int freq = map.get(el);
```

```
                2. freq = freq + 1;
```

```
            o(1) — 3. map.put(el, freq);
```

```
        } else {
```

```
            o(1) — map.put(el, 1);
```

```
        }
```

```
    }
```

```
    o(q) — for (int currEl : a) {
```

```
        o(1) — if (map.containsKey(currEl)) {
```

```
            o(1) — print(map.get(currEl));
```

```
        } else {
```

```
            print(0);
```

```
        }
```

```
    }
```

```
}
```

TC: $O(n+q)$

SC: $O(n)$

Q42: find ^{first} non-repeating el in array.

arr[6] = [1 2 3 1 2 5] ans = 3

arr[8] = [4 3 3 2 5 6 4 5] ans = 2

map:

6	-	1
4	-	2
3	-	2
5	-	2
2	-	1

Hash map does not maintain

order of a key



Advanced Module

```

int firstNonRepeatingEl (int[] arr) {
    HashMap<Integer, Integer> map =
        new HashMap<>();

```

```

    o(n) — for (int el : arr) {
        o(1) — if (map.containsKey(el)) {
            o(1) — 1. int freq = map.get(el);
                2. freq = freq + 1;
            o(1) — 3. map.put (el, freq);
        } else {
            o(1) — map.put (el, 1);
        }
    }

```

```

    for (int el : arr) {
        if (map.get(el) == 1) {
            return el;
        }
    }

```

```

    return -1;
}

```

Break: 8:44 AM

HashSet

- hashmap but only key part
- when you don't need values

Things to know

```
HashSet<key> set = new HashSet<>();
```

↑
anything

Operations

1. add — set.add(el).
2. size: set.size()
3. get: Get the value of a key { invalid }
4. contains: set.contains(key)

Ques Given arr[n], find no of distinct elements

arr[5] = [3 5 6 5 4] ans = 4

arr[3] = [3 3 3] ans = 1.

hashset
arr[] = [3 5 6 5 4]

set = { 3 5 6 4 }

set.size() = ans

hashmap

key	value
3	1
5	2
6	1
4	1

map.size() = ans

```
int countDistinctIntegers(int[] arr)
```

```
HashSet<Integer> set = new HashSet<>();
```

```
o(n) — for (int el : arr) {
```

```
    o(1) — set.add(el);  
}
```

```
o(1) — return set.size();  
}
```

TC: $O(n)$

SC: $O(n)$

Google.

Ques Given $arr[n]$, check if there exists a subarray with sum = 0

$arr[10] = [2, 2, 1, -3, 4, 3, 1, -2, -3, 2]$

Brute-force: Go to every subarray -
check if sum is 0 or not?

TC: $O(n^2)$

SC: $O(1)$.

Expected TC: $O(n)$.

Approach: $sum(l, r) \div$ prefix sum.

$arr[] = [\overset{0}{2}, \overset{1}{2}, \overset{2}{1}, \overset{3}{-3}, \overset{4}{4}, \overset{5}{3}, \overset{6}{1}, \overset{7}{-2}, \overset{8}{-3}, \overset{9}{2}]$

$pf[] = [2, 4, 5, 2, 6, 9, 10, 8, 5, 7] - O(n)$

observation

1. $pf[i] = 0$ [true]

└ There is a subarray from 0th idx to i th idx with sum = 0

$$\text{arr}[] = \left[\overset{0}{2} \quad \overset{1}{2} \quad \overset{2}{1} \quad \overset{3}{-3} \quad \overset{4}{4} \quad \overset{5}{3} \quad \overset{6}{1} \quad \overset{7}{-2} \quad \overset{8}{-3} \quad \overset{9}{2} \right]$$

$$\text{pf}[] = [2 \quad 4 \quad 5 \quad 2 \quad 6 \quad 9 \quad 10 \quad 8 \quad 5 \quad 7] \rightarrow O(n)$$

Obs 2:

$$\left. \begin{array}{l} \text{pf}[2] = 5 \\ \text{pf}[8] = 5 \end{array} \right\} \rightarrow \text{true} \{ \text{subarray with sum} = 0 \}$$

$$\cancel{\text{arr}[0]} + \cancel{\text{arr}[1]} + \cancel{\text{arr}[2]} = \cancel{5} \quad \text{--- ①}$$

$$\cancel{\text{arr}[0]} + \cancel{\text{arr}[1]} + \cancel{\text{arr}[2]} + \quad = \cancel{5} \quad \text{--- ①}$$

$$\text{arr}[3] + \text{arr}[4] + \text{arr}[5] +$$

$$\text{arr}[6] + \text{arr}[7] + \text{arr}[8]$$

$$\left\{ \overset{\text{①}}{\cancel{\text{arr}[0]} + \cancel{\text{arr}[1]} + \cancel{\text{arr}[2]}} \right\} - \overset{\text{①}}{\left\{ \cancel{\text{arr}[0]} + \cancel{\text{arr}[1]} + \cancel{\text{arr}[2]} \right\}} = 5 - 5$$

$$\text{arr}[3] + \dots + \text{arr}[8]$$

$$\text{arr}[3] + \dots + \text{arr}[8] = 0$$

$$\text{arr}[3] + \text{arr}[4] + \text{arr}[5] + \dots + \text{arr}[8] = 0$$

$$\text{sumArray}[3, 8] = 0$$

challenge: Does pf[] contains repeating el or not?

```
boolean subArraySumWithZeroValue(int[] arr) {
```

```
    int[] pf = prefixOptimal(arr);
```

└ refer prefix sum class.

```
    HashSet<Integer> set = new HashSet<>();
```

```
    for (int el: pf) {
```

```
        if (el == 0) {
```

```
            return true;
```

```
        }
```

```
        set.add(el);
```

```
    }
```

// Repeating el in array

```
    if (set.size() != arr.length) {
```

```
        return true;
```

```
    }
```

```
    return false;
```

```
}
```

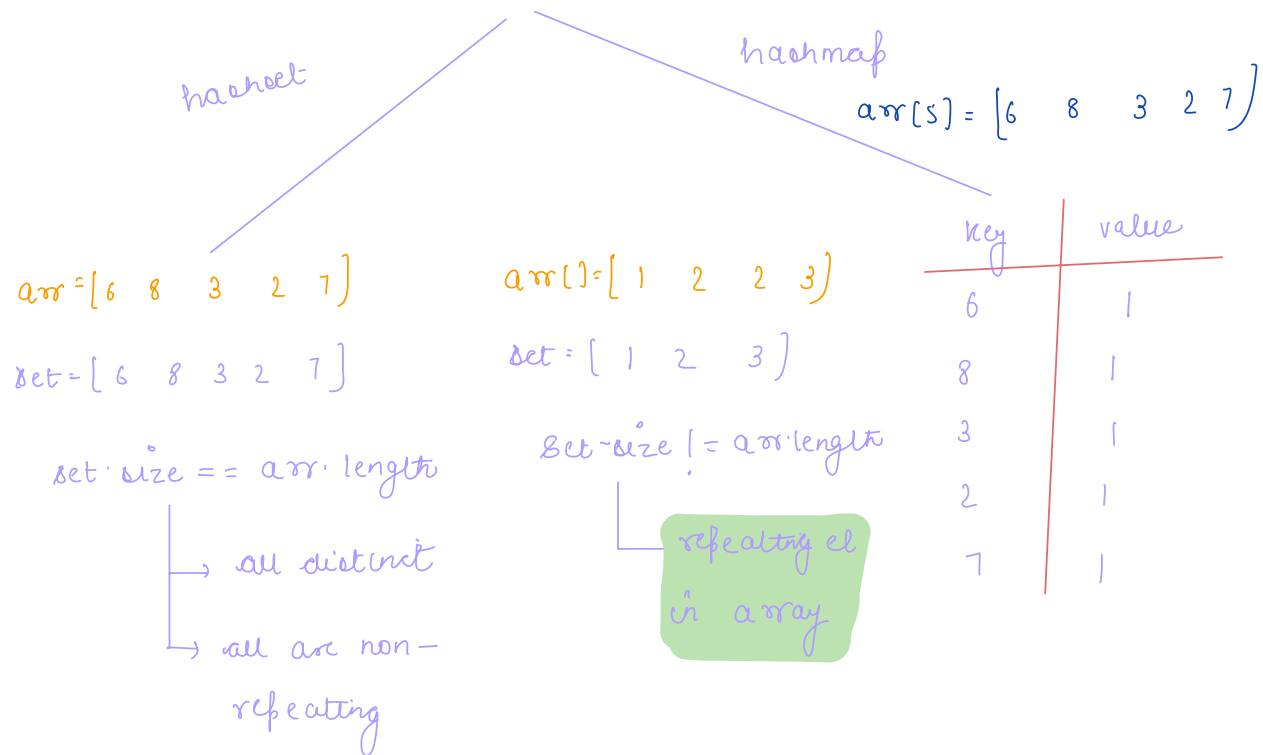
TC: $O(n)$

SC: $O(n)$

Q: Given $arr[n]$, check if all el are distinct or not?

$arr[5] = [6 \ 8 \ 3 \ 2 \ 7] \rightarrow \text{true}$

$arr[7] = [3 \ 1 \ 6 \ 1 \ 4 \ 2 \ 9] \rightarrow \text{false}$



Thankyou 😊