

Lecture 4 ÷ Introduction to Arrays.

Agenda

- Arrays Revision.
- Problems on Arrays

Class starts at 7:05 AM.

You didn't come this far only to come this far

Arrays → collection of **similar data type**.
→ contiguous memory allocation.

Initialisation

`int[] arr = new int[10]` [Java]

`int arr[10];` [C++]

`int[5] arr = { 1, 2, 8, 9, 5 }` → valid.

`arr[] = { 2, 8, "Ayush", 1, 1, 5 }` — invalid.

`int[] arr = new int[5]`.

0	0	0	0	0
0	1	2	3	4

↑
idx.

[arr[n] —
idx[0, n-1]]

`arr[2] = 10.`

0	0	10	0	0
0	1	2	3	4

idx
[0 - 4]

`arr[-1]`
`arr[5]` } — out of bound exception.

Q

Print all array el.

arr[5] = { ⁰2, ¹8, ²2, ³3, ⁴5 }

```
void print(int[] arr) {
```

```
    for(i=0; i < arr.length; i++) {
```

```
        print(arr[i]);
```

```
    }
```

```
}
```

Qul Given $arr[n]$, count no. of el. having at least 1 el greater than itself.

$$arr[7] = \{ \overset{0}{-3} \overset{1}{-2} \overset{2}{6} \overset{3}{8} \overset{4}{4} \overset{5}{8} \overset{6}{5} \} \quad \text{count} = 5.$$

$-3 < 6 \quad -2 < 8$

$$arr[8] = \{ 2 \ 3 \ 10 \ 7 \ 3 \ 2 \ 10 \ 8 \} \quad \text{count} = 6$$

$$arr[5] = \{ 8 \ 8 \ 8 \ 8 \ 8 \} \quad \text{count} = 0.$$

$$arr[10] = \{ 2 \ 5 \ 1 \ 4 \ 8 \ 0 \ 8 \ 1 \ 3 \ 8 \}$$

Observation : max el of arr can never be part of my answer.

$$\text{Logic } arr[10] = \{ 2 \ 5 \ 1 \ 4 \ 8 \ 0 \ 8 \ 1 \ 3 \ 8 \}$$

$$\text{count max el} = 3.$$

$$\text{ans} = 10 - 3 = \underline{\underline{7 \text{ Ans}}}$$

- 1.) find max el.
- 2.) find occ of max el.
- 3.) $arr.length - \text{occ of max el.}$

```

int countGreaterthanItself(int[] arr) {
    int n = arr.length;
    // find max el.

```

```

    int max = arr[0];

```

```

o(n) ——— for(i=1; i < n; i++) {
    if (arr[i] > max) {
        max = arr[i];
    }
}

```

```

// occ of max el

```

```

    int count = 0;

```

```

o(n) ——— for(i=0; i < n; i++) {
    if (arr[i] == max) {
        count++;
    }
}

```

```

    return arr.length - count;
}

```

Tc :- $O(n+n) = O(2n) \simeq O(n)$.

Sc :- $O(1)$

Ques Given $arr[n]$, check if there exists a pair (i, j) such that $arr[i] + arr[j] = k$ & $i \neq j$.

Ex1. $arr[7] = \{ \overset{0}{3} \quad \overset{1}{-2} \quad \overset{2}{1} \quad \overset{3}{4} \quad \overset{4}{3} \quad \overset{5}{6} \quad \overset{6}{8} \}$
 $k = 10$. true.

Ex2. $arr[4] = \{ 2 \quad 4 \quad -3 \quad 7 \}$
 $k = 5$. false

Ex3. $arr[4] = \{ \overset{0}{2} \quad \overset{1}{4} \quad \overset{2}{-3} \quad \overset{3}{7} \}$
 $k = 8$. false

Ex4. $arr[5] = \{ \overset{0}{2}, \overset{1}{4}, \overset{2}{5}, \overset{3}{4}, \overset{4}{7} \}$
 $k = 8$. true

Approach: Go to all pairs of arr .

arr[5] = { ⁰3 ¹5 ²2 ³7 ⁴4 } k = 11.

ⁱ ^j 0,0 i=0 i=j	ⁱ ^j 1,0 (0,1) i=1 Already calculated	ⁱ ^j 2,0 i=2 0,2 calculated	ⁱ ^j 3,0 i=3	ⁱ ^j 4,0 i=4
0,1 3+5=8	1,1 i=j	2,1 1,2 calculated	3,1	4,1
0,2 3+2=5	1,2 5+2=7	2,2 i=j	3,2	4,2
0,3 3+7=10	1,3 5+7=12	2,3 2+7=9	3,3	4,3
0,4 3+4=7	1,4 5+4=9	2,4 2+4=6	3,4 7+4=11	4,4

Logic:

$i \in [0, n-2]$

↑
second last idx.

$j \in [i+1, n-1]$

↑
last idx.

i=0	i=1	} j → starting pt = i+1.
0 0	1 0	
0 ①	1 1	
0 2	1 ②	
0 3	1 3	
0 4	1 4	

```
boolean checkSumPair(int[] arr, int k) {
```

```
    int n = arr.length; → O(1)
```

```
    O(n). ——— for( i=0; i<=n-2; i++) {
```

```
        O(n). ——— for( j=i+1; j<=n-1; j++) {
```

```
            if ( arr[i] + arr[j] == k) {
```

```
                return true;
```

```
            }
```

```
        }
```

```
    }
```

```
    return false;
```

```
}
```

TC: $O(n^2)$

SC: $O(1)$

Optimised: HashMap

 Sorting

		for (i=0 ; i <= n-2 ; i++) arr[i]		for (i=0 ; i <= n-2 ; i++) {	
		total iter (n=5)		for (j=i+1 ; j <= n-1 ; j++) {	
i	j				
0	j=[1,4]	for (j=i+1 ; j <= n-1 ; j++) {		for (j=i+1 ; j <= n-1 ; j++) {	
1	j=[2,4]	if (arr[i] + arr[j] == k) {		if (arr[i] + arr[j] == k) {	
2	j=[3,4]	return true;		return true;	
3	j=[4,4]	}		}	

$$1 + 2 + 3 + 4 = 10$$

$$\underline{n=4}$$

$$\frac{n(n+1)}{2} \Rightarrow \frac{(n-1)(n-1+1)}{2}$$

$$= \frac{(n-1)(n)}{2}$$

$$= \frac{n^2}{2} - \frac{n}{2}$$

$$= O(n^2)$$

Ques Given $arr[n]$, reverse the entire array

$$arr[5] = \{ 2, 3, 1, 5, 8 \} \xrightarrow{\text{reverse}} \{ 8, 5, 1, 3, 2 \}$$

constraint:- $SC = O(1)$, Array should be reversed internally

$$arr[8] = \{ \overset{0}{-1}, \overset{1}{4}, \overset{2}{7}, \overset{3}{6}, \overset{4}{-2}, \overset{5}{17}, \overset{6}{8}, \overset{7}{10} \}$$

$$\text{reverse}(arr) = \{ 10, 8, 17, -2, 6, 7, 4, -1 \}$$

observation:- swapping

$$arr[8] = \{ \overset{0}{-1}, \overset{1}{4}, \overset{2}{7}, \overset{3}{6}, \overset{4}{-2}, \overset{5}{17}, \overset{6}{8}, \overset{7}{10} \}$$

$$\begin{array}{c} i \quad j \\ 0 \quad \text{swap} \quad 7 \end{array} \left[\begin{array}{cccccccc} 10 & 4 & 7 & 6 & -2 & 17 & 8 & -1 \end{array} \right]$$

$$1 \quad \text{swap} \quad 6 \left[\begin{array}{cccccccc} 10 & 8 & 7 & 6 & -2 & 17 & 4 & -1 \end{array} \right]$$

$$2 \quad \text{swap} \quad 5 \left[\begin{array}{cccccccc} 10 & 8 & 17 & 6 & -2 & 7 & 4 & -1 \end{array} \right]$$

$$3 \quad \text{swap} \quad 4 \left[\begin{array}{cccccccc} 10 & 8 & 17 & -2 & 6 & 7 & 4 & -1 \end{array} \right]$$

$$i < j$$

$$4 \quad 3 \quad [\text{stop}]$$

arr[7] = { ⁰1, ¹2, ²8, ³3, ⁴4, ⁵6, ⁶7 }

i	j	
0	6	[1 2 8 3 4 6 1]
1	5	[1 6 8 3 4 2 1]
2	4	[1 6 4 3 8 2 1]
3	3	<u>stop</u>

Conclusion: $i < j$

```
void reverse(int[] arr) {
```

```
    int i=0; — 4B
```

SC:- 4B+4B=8B

```
    int j = arr.length-1; — 4B
```

$O(8B) = O(1)$

```
    while( i < j ) {
```

```
        swap(arr, i, j); → h/w
```

```
        i++;
```

```
        j--;
```

```
    }
```

```
}
```

TC:- $O(n)$.

SC: $O(1)$.

Break:- 8:45 AM

Ques Given arr[n], si & ei, reverse arr from si to ei.

arr[] = { ⁰-3 ¹4 ²2 ³8 ⁴7 ⁵9 ⁶6 ⁷2 ⁸10 }

si=2, ei=6 [-3 4 6 9 7 8 2 2 10]

```
void reverse(int[] arr, int si, int ei)
```

```
    int i = si;
```

```
    int j = ei;
```

```
    while(i < j) {
```

```
        swap(arr, i, j); → h/w
```

```
        i++;
```

```
        j--;
```

```
    }
```

```
}
```

TC: O(n)

SC: O(1)

Reverse of entire arr: reverse(arr, 0, arr.length-1);

Amazon, Meta, Google ---

Q Given $arr[n]$, rotate array from last to first by k times.

Examples $arr[7] = \{ \overset{0}{3} \overset{1}{-2} \overset{2}{1} \overset{3}{4} \overset{4}{6} \overset{5}{9} \overset{6}{8} \}$
 $k=3.$

rotate 1.
↓
{ 8 3 -2 1 4 6 9 }
↓ rotate 2.
{ 9 8 3 -2 1 4 6 }
↓ rotate 3

{ 6 9 8 3 -2 1 4 } Ans

$arr[9] = [\overset{0}{4} \overset{1}{1} \overset{2}{6} \overset{3}{9} \overset{4}{2} \overset{5}{14} \overset{6}{7} \overset{7}{8} \overset{8}{3}]$

$k=4$

rotate 1.
↓
[3 4 1 6 9 2 14 7 8]
↓ rotate 2
[8 3 4 1 6 9 2 14 7]
↓ rotate 3
[7 8 3 4 1 6 9 2 14]
↓ rotate 4
[14 7 8 3 4 1 6 9 2]

case 1: $k < \text{arr.length}$

$\text{arr}[9] = [\overset{0}{4} \ \overset{1}{1} \ \overset{2}{6} \ \overset{3}{9} \ \overset{4}{2} \ \overset{5}{14} \ \overset{6}{7} \ \overset{7}{8} \ \overset{8}{3}]$ initial

$k=4$

$\downarrow \text{reverse}(0, 8)$
 $[\text{3} \ \text{8} \ \text{7} \ \text{14} \ \text{2} \ \text{9} \ \text{6} \ \text{1} \ \text{4}]$

$\downarrow \text{reverse}(0, 3)$
 $\text{0} \ \text{k}-1$

$\downarrow \text{reverse}(4, 8)$
 $\text{k}, \text{n}-1$

$[\text{14} \ \text{7} \ \text{8} \ \text{3} \ \text{4} \ \text{1} \ \text{6} \ \text{9} \ \text{2}]$

\updownarrow same

$[\text{14} \ \text{7} \ \text{8} \ \text{3} \ \text{4} \ \text{1} \ \text{6} \ \text{9} \ \text{2}]$ final

Steps involved

1. $\text{reverse}(0, n-1)$ = reverse the entire array
2. reverse first k el $\Rightarrow \text{reverse}(0, k-1)$
3. reverse remaining el $\Rightarrow \text{reverse}(k, n-1)$

```
void rotate(int[] arr, int k) {
```

```
    reverse(arr, 0, arr.length-1); //  $O(n)$ 
```

```
    reverse(arr, 0, k-1); //  $O(n)$ 
```

```
    reverse(arr, k, arr.length-1); //  $O(n)$ 
```

```
}
```

TC: $O(3n) \simeq O(n)$

SC: $O(1)$

case2: $k > \text{arr.length}$

$\text{arr}[7] = \{ 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \quad 8 \} \Rightarrow k=0$

rotate 1.
 $= \{ 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \} \Rightarrow k=1$

rotate 2.
 $\{ 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \} \Rightarrow k=2$

rotate 3.
 $\{ 6 \quad 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \} \Rightarrow k=3$

rotate 4.
 $\{ 4 \quad 6 \quad 9 \quad 8 \quad 3 \quad -2 \quad 1 \} \Rightarrow k=4$

rotate 5.
 $\{ 1 \quad 4 \quad 6 \quad 9 \quad 8 \quad 3 \quad -2 \} \Rightarrow k=5$

rotate 6.
 $\{ -2 \quad 1 \quad 4 \quad 6 \quad 9 \quad 8 \quad 3 \} \Rightarrow k=6$

rotate 7.
 $\{ 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \quad 8 \} \Rightarrow k=7$

$\left[\begin{array}{l} k = \text{arr.length} \\ \text{arr will not change} \end{array} \right]$

rotate 8.
 $\{ 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \}$

rotate 9.
 $\{ 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \}$

rotate 10.
 $\{ 6 \quad 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \}$

Observation

arr[] =

k=0

k = n. (7) (Arrays same)

k=1.

k = n+1. (8) (Arrays same)

k=2

k = 9

(" ")

k=3

k=10

(" ")

$k = k \% \text{arr.length}$

```
void rotate (int[] arr, int k) {
```

```
    k = k % arr.length;
```

```
    reverse(arr, 0, arr.length-1); —  $O(n)$ 
```

```
    reverse(arr, 0, k-1); —  $O(n)$ 
```

```
    reverse(arr, k, arr.length-1); —  $O(n)$ 
```

```
}
```

Thankyou 😊

Doubt

$k=1$ (00) 8 { Array is same }
 $k=8$ [$k=1$]
 arr length = 7

$k =$
 $k \% 7$
 $8 \% 7 = 1$ Any

$k=0$ (array)
 \vdots
 $k=7$ (array)
 \vdots

$k=14$ (array)
 \vdots
 $k=21$ (array)

10 11
 | |
 5 5
 | |
 2 2
 | |
 ① ①
 | |
 0 0

$a=0$
 $i=n$
 while ($i > 0$) {
 $a += i$;
 $i = i / 2$;
 }

$i = n$
 \downarrow 1. $= \frac{n}{2^1}$
 \downarrow 2. $= \frac{n}{2^2}$
 \downarrow 3. $= \frac{n}{2^3}$
 \downarrow 4. $= \frac{n}{2^4}$
 \vdots k.

$$\frac{n}{2^k} = 1.$$

$$n = 2^k$$

$$2^k = n. \text{ { Applying } } \log_2 \text{ both sides}$$

$$\log_2 2^k = \log_2 n$$

```

for (i=0; i<=n; i++)
    for (j=i-1; j>=0; j++)
        1

```

1

1

↙ check

int fun(int() ans)

6(n2) → int() temp = new int(n);

temp = ans

}

i	-i-1, 0
0	0
1	j = 0, 1, 2, 3, ... — <u>in</u>
2	
3	
⋮	
n	