

## Lecture ÷ Trees

### Agenda ÷

- Introduction. ✓
- Naming conventions. ✓
- Traversals
- Assignment problems.

Class starts at 8:35 PM

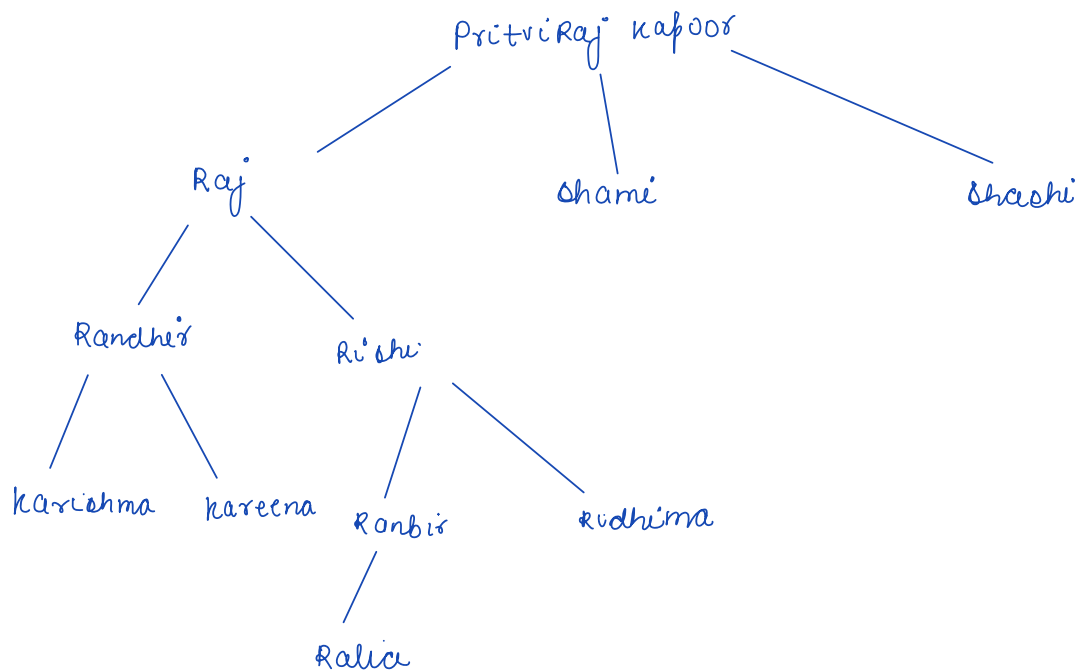
## Linear data structure

arr[] =  $\begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 3 & 4 & 5 & 6 \end{bmatrix}$   
          ↓100   ↓104   ↓108   ↓112   ↓116   ↓120

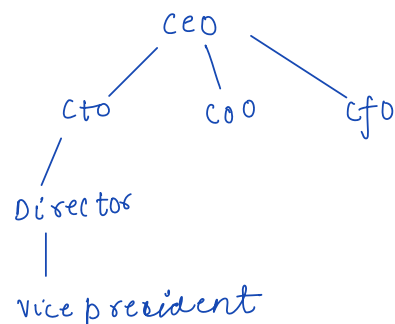
Linked list:-  
          ↓100            ↓200            ↓104            ↓219  
① → ② → ③ → ④ → null  
val=1        val=2  
next = 200   next = 104   ...

## Hierarchical data structures [Trees]

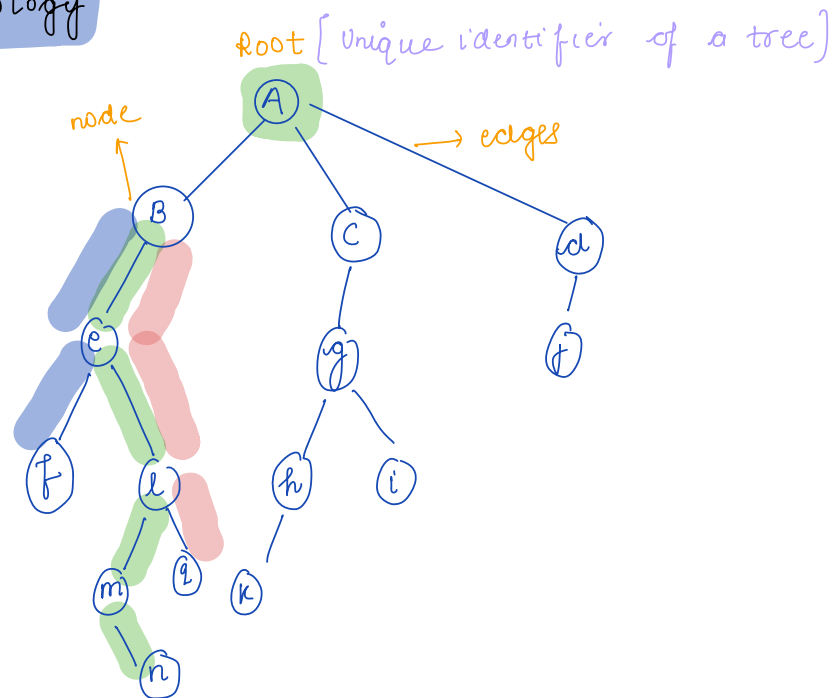
1. family tree.



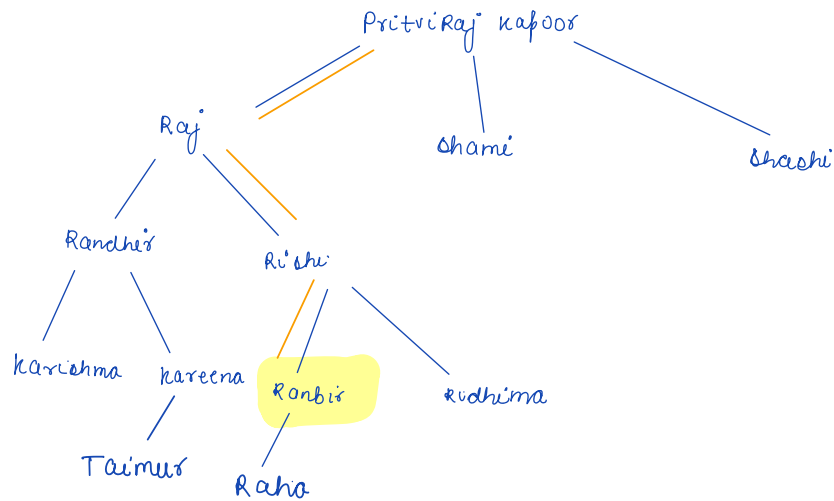
2. Corporate world



## Terminology



$$\text{height}(b) = 4$$



Parent & child: Raha is a child of Ranbir  
Ranbir is a parent of Raha.

Ancestors: ancestors[Ranbir] = Prithvi, Raj and Rishi

Descendants: descendants[Raj]: Randhir, Ranbir, Rishi, Raha,  
Karishma and Kareena  
All the nodes below given node

Siblings: Nodes with same parent  
Eg: Ranbir and Richima  
Raj, Shami and Shashi

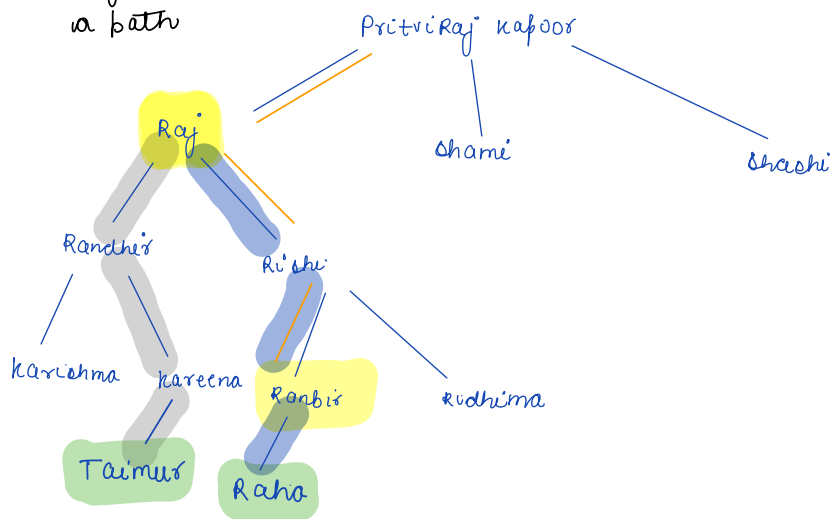
Leaf nodes: Nodes with no children.  
Karishma, Taimur, Raha and Richima, Shami, Shashi

# Height of a node

length of longest path from given node to a leaf node

nodes in a path

edges in a path



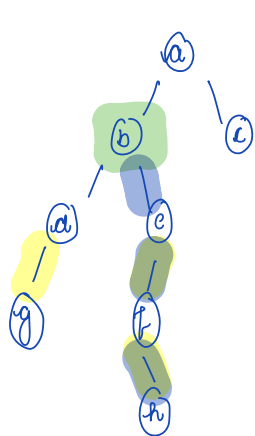
$$\text{height}(\text{Raj}) = 3$$

↑  
counting edges

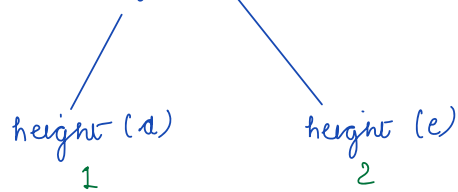
$$\text{height}(\text{Raj}) = 4$$

↓  
counting nodes

Observation: 1)  $\text{height}(\text{leaf node}) = 0$



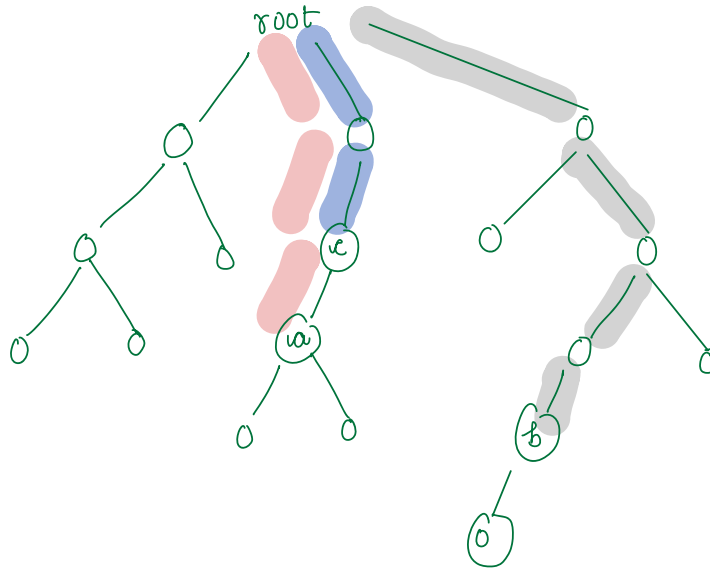
$$2) \text{height}(b) = \max(\text{height}(d), \text{height}(e)) + 1$$



$$3) \text{height}(\text{tree}) = \text{height}(\text{root})$$

## Depth of a node

length of path from root to given node



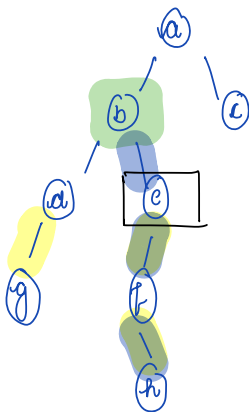
$$\text{depth}(c) = 2$$

$$\text{depth}(b) = 4$$

$$\text{depth}(a) = 3$$

$$1.) \text{depth}(\text{root node}) = 0$$

$$2.) \text{depth}(\text{node}) = \text{depth}(\text{parent}) + 1$$

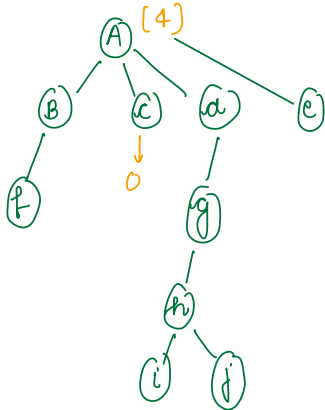


$$\text{depth}(f) = \text{depth}(c) + 1$$

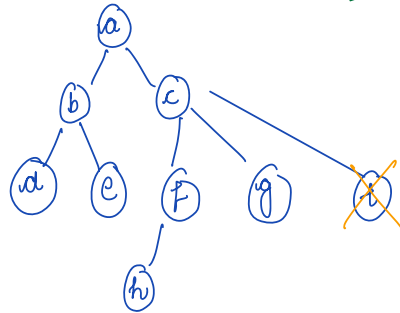
$$\text{depth}(e) = 2$$

## Type of trees

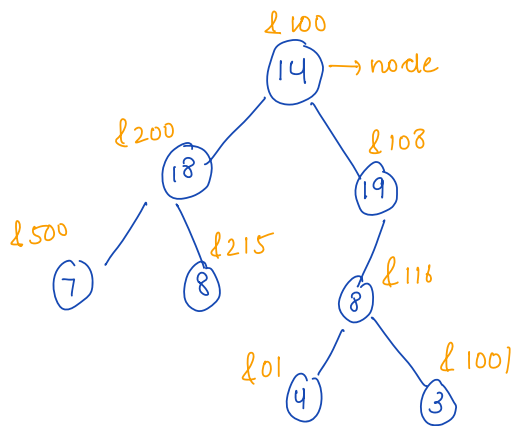
n-ary tree [Advanced]  
[Any no of children]



Binary tree [Intermediate]  
Max of only 2 children  
[0, 1, 2]



## Structure of Binary tree



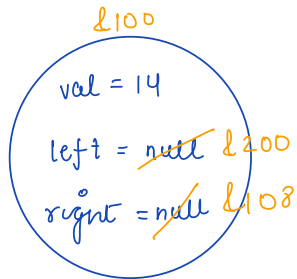
```

class Node {
    int val;
    Node left;
    Node right;

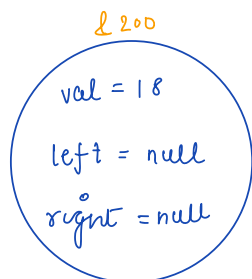
    Node(int x) {
        val = x;
    }
}
  
```

Detailed:

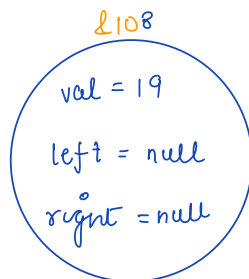
Node root = new Node(14)



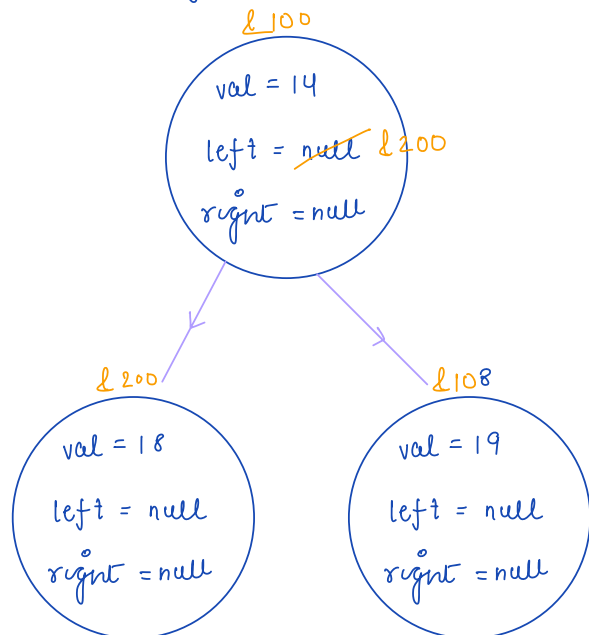
Node n1 = new Node(18);



Node n2 = new Node(19);



root.left = n1;  
root.right = n2



Break: 9:44 PM



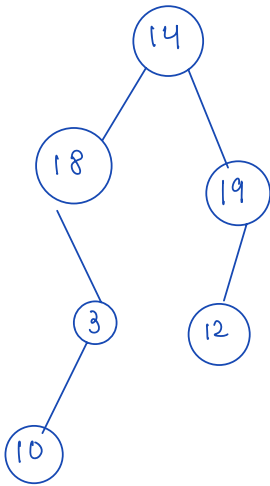
Note: if will already be given, root will be given

## Traversals

Recursive traversals.

Pre-order [ root left right ]  
Inorder [ left root right ]  
Postorder [ left right root ]

Ques: Print all the nodes of trees in any manner you want.



opt:

14	18	19	12	3	10
14	18	12	19	10	3
18	14	3	10	19	12

} valid

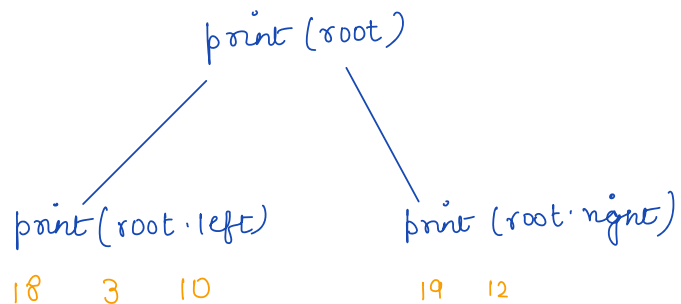
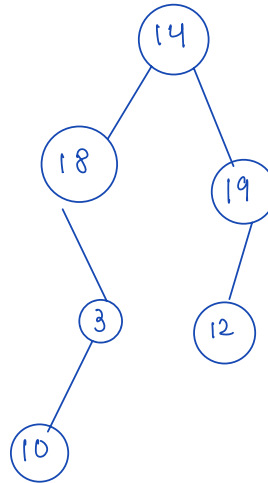
## Post order traversal

```
void traversal(Node root) {  
    if (root == null) {  
        return;  
    }  
    traversal(root.left) // 18 10 3  
    traversal(root.right) // 19 12  
    print(root.data) // 14  
}
```

## Assumption

Given a root, print whole tree  
Given a node, print all the nodes of tree starting from that node

## main logic

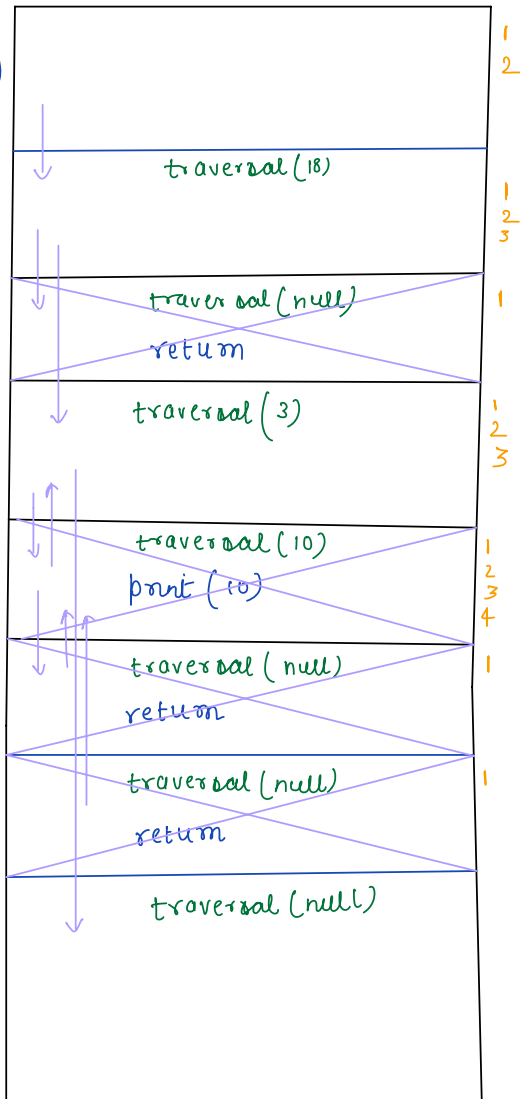


print(root.data)  
14

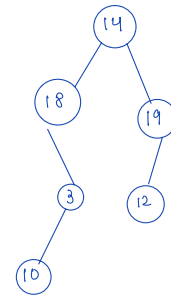
## Base condition

```
if (root == null) return;
```

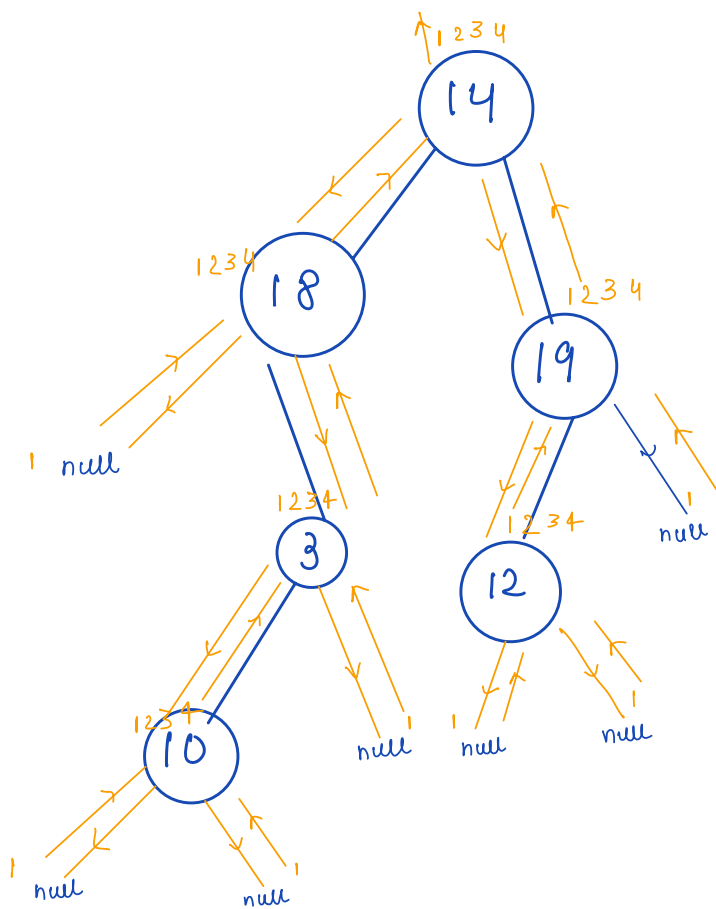
traversal(14)



```
void traversal(Node root) {
    1 if (root == null) {
        return;
    }
    2 traversal(root.left)
    3 traversal(root.right)
    4 print(root.data)
}
```



op: 10



```

void traversal(Node root) {
    1 if (root == null) {
        return;
    }
    2 traversal(root.left)

    3 traversal(root.right)

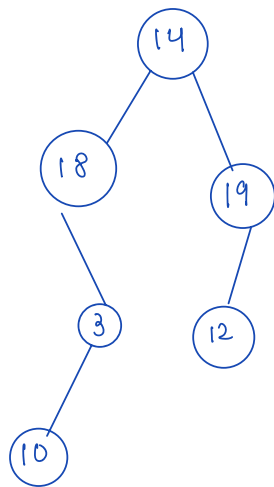
    4 print(root.data)
}

```

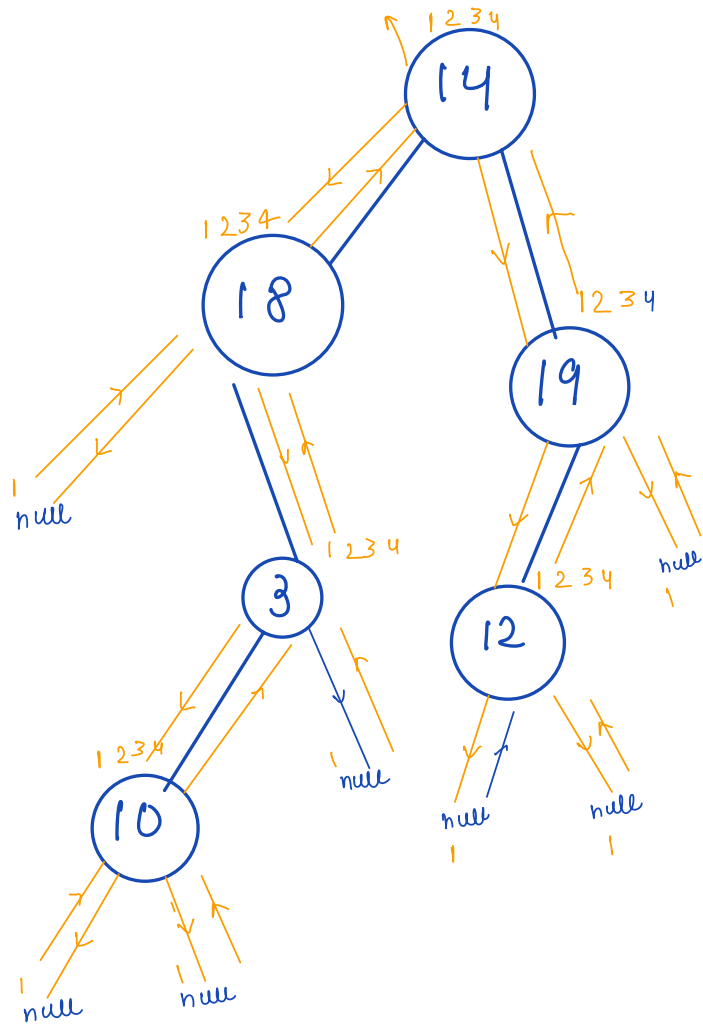
op: 10 3 18 12  
19 14

## Pre-order traversal

[ root   left   right ]  
                    subproblem   subproblem



```
void preorderTraversal(Node root) {  
    if (root == null) {  
        return;  
    }  
    print(root.data);  
    preorderTraversal(root.left);  
    preorderTraversal(root.right);  
}
```



```

void preorderTraversal(Node root) {
    1 if (root == null) {
        return;
    }
    2 print (root.data);
    3 preorderTraversal (root.left);
    4 preorderTraversal (root.right);
}

```

op: 14 18 3 10 19 12

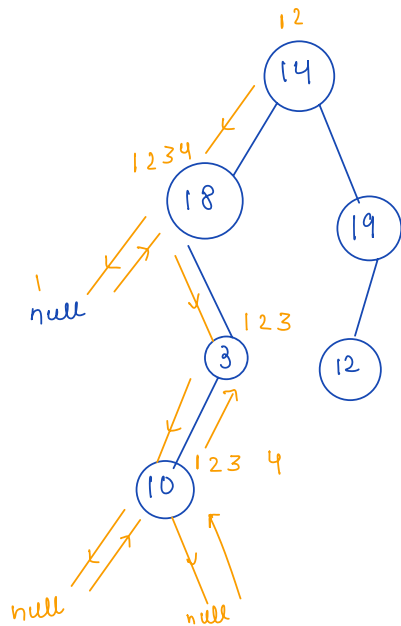
## Inorder traversal

Left  
subproblem

Root

Right  
subproblem

```
void inorder(Node root) {
    if (root == null) {
        return;
    }
    inorder(root.left);
    print(root.data);
    inorder(root.right);
}
```

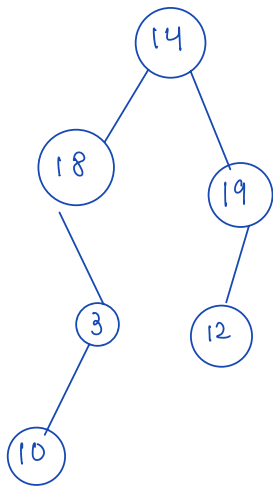


```
void inorder(Node root) {
    1 if (root == null) {
        return;
    }
    2 inorder(root.left);
    3 print(root.data);
    4 inorder(root.right);
}
```

op: 18 10 3 \_\_\_\_\_

Assignment: complete dry run

Q. Count no. of nodes in a tree



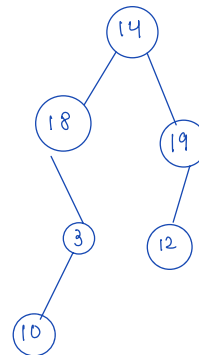
op: 6

```
int count(Node root) {  
    if (root == null) {  
        return 0;  
    }  
    int la = count(root.left);  
    int ra = count(root.right);  
    return la + ra + 1;  
}
```

Assumption

Given a node, count all nodes starting from the given node

Main logic



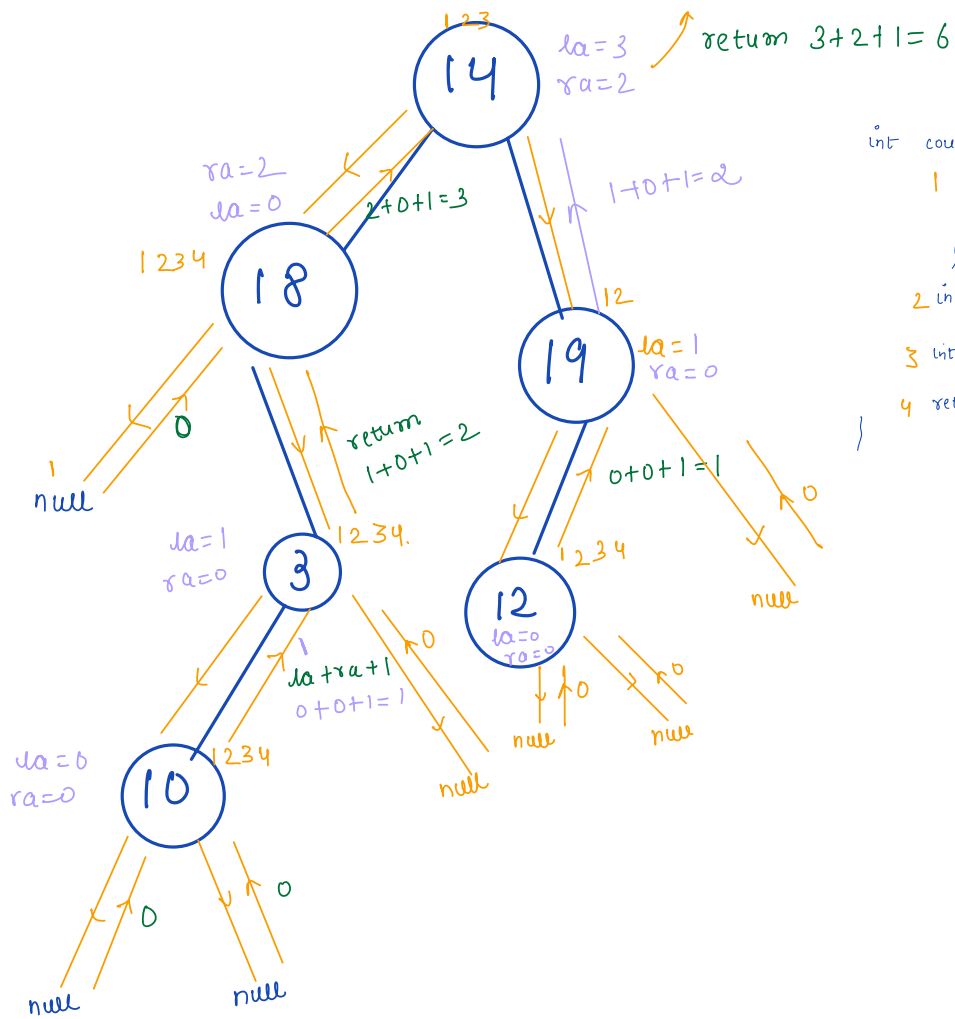
count(14)

18, 3, 10  
count(18)  
la = 3

19, 12  
count(19)  
ra = 2

ans = la + ra + 1 → root data





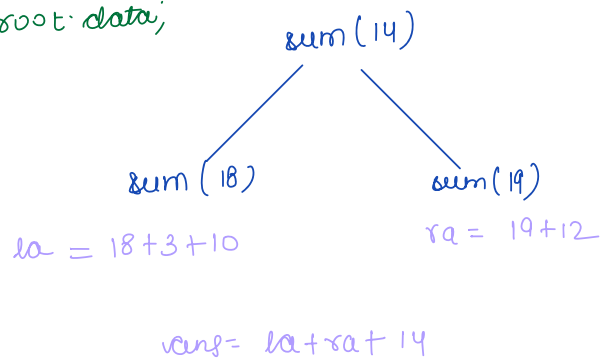
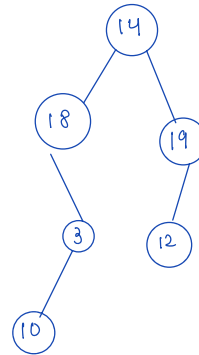
```

int count(Node root) {
    1 if (root == null) {
        return 0;
    }
    2 int la = count(root->left);
    3 int ra = count(root->right);
    4 return la + ra + 1;
}

```

Ques find sum of all the nodes in a tree

```
int sum(Node root) {  
    if (root == null) {  
        return 0;  
    }  
    int la = sum(root.left);  
    int ra = sum(root.right);  
    return la + ra + root.data;  
}
```



Thankyou 😊

Practice Viva

