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# OPICS to be covered

- 1 Basic Formula
- 2 Inprosper

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#### Algebra



#### Basics

### Different logics

Value putting, symmetry, degree etc.

#### **CUBE FORMULA**

$$(a + b)^3 = a^3 + b^3 + 3ab (a + b)$$

$$\Rightarrow$$
 a<sup>3</sup> + b<sup>3</sup> = (a + b)<sup>3</sup> - 3ab(a + b)

$$\Rightarrow$$
  $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ 

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$a^3 - b^3 - (a - b)^3 + 3ab(a - b)$$

$$a^3 - b^3 = (a - b) (a^2 + ab + b^2)$$

#### SPECIAL CASE

$$Arr$$
 If  $a^2 - ab + b^2 = 0$  then  $a^3 + b^3 = 0$ 

► If 
$$b = 1$$
, then  $a^2 - a + 1 = 0$ , then  $a^3 + 1 = 0$  or  $a^3 = -1$ 

$$(a+b)^2 = (a-b)^2 + 4ab$$

$$a^{2}+b^{2}=(a-b)^{2}+2ab$$
 $(a-b)^{2}=(a+b)^{2}-4ab$ 

$$a^2 - b^2 = (a+b)(a-b)$$



$$(a+b)^2 - (a-b)^2 = 4ab$$

#### SPECIAL CASE



$$Arr$$
 If  $a^2 + a + 1 = 0$  then  $a^3 - 1 = 0$   $a^3 = 1$ 

#### SPECIAL CASE

$$Arr$$
 If  $\frac{a}{b} + \frac{b}{a} = 1$  then  $a^3 + b^3 = 0$ 

#### SPECIAL CASE

$$ightharpoonup ext{If } \frac{a}{b} + \frac{b}{a} = -1 ext{ then } a^3 - b^3 = 0$$

$$ightharpoonup ext{If } rac{a}{b} + rac{b}{a} = rac{1}{a+b} ext{ then } a^3 - b^3 = 0$$

#### SPECIAL CASE

If 
$$(a + b + c)=0$$
  
Then  $a^3 + b^3 + c^3 - 3abc = 0$ 

$$a^3 + b^3 + c^3 - 3abc = 0$$

If 
$$a^3 + b^3 + c^3 - 3abc = 0$$
  
a, b and c are distinct no then,  $a + b + c = 0$ 

$$x + \frac{1}{x} = 2$$

where 
$$x=1$$
 $\Rightarrow temo+1=2$ 
 $tempo+(oto=2)$ 

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if 
$$x+1=2$$

$$x=7$$

$$m+1 = 0$$

$$m+2$$

$$(m+2)+1$$

$$(m+2)$$

$$m+2=1$$
 $m+2=x$ 
 $m=1-2$ 
 $m+2=x$ 
 $m=-1$ 
 $m+2=x$ 
 $m=-1$ 
 $m+2=x$ 
 $m=-1$ 
 $m+2=x$ 



$$(m+2)^{5}+1$$
 = 9



$$x + \frac{1}{x} = -2$$

alues: 
$$(-1)^{\text{even}} = +1$$
  
 $(-1)^{\text{odd}} = -1$ 

$$\chi^{4} + \frac{1}{\chi^{7}} = (-1)^{4} + \frac{1}{(-1)^{7}} = -1 - 1 = -2$$

$$x^{8} + \frac{1}{1} = (-1)^{8} + \frac{1}{1} = 1 + 1 = 2$$

$$x_8 + \frac{x_2}{1} = (-1)_8 + \frac{1}{1} = 1 - 1 = 0$$



$$x + \frac{1}{x} = 1$$

$$\chi^2 + | = \chi$$

$$\left(\chi_{3}^{2}\chi+1\right)=0$$

$$(x+1)(x_3-1)=0$$

$$\begin{cases} x^{17} + 1 \\ x^{17} \end{cases} \times \frac{x}{x}$$

$$\Rightarrow x^{18} + x$$

$$\frac{3}{2} \frac{x^{18}}{x^{18}} + \frac{x}{x^{18}}$$

$$= \frac{3}{2} \frac{x^{18}}{x^{18}} + \frac{x}{x^{18}}$$

$$= \frac{1}{x} (x^3)^6 = \frac{1}{x}$$

$$x^{12} + \frac{1}{x^{12}} = (x^3)^4 + \frac{1}{(x^3)^4} = (-1)^4 + \frac{1}{(-1)^4} = (-1)^4$$

$$\chi^{15} + \frac{1}{\chi^{15}} = (\pi^3)^5 + \frac{1}{(\pi^3)^5} = (-1)^5 + \frac{1}{(-1)^5} = (-1)^5 = (-1)^$$

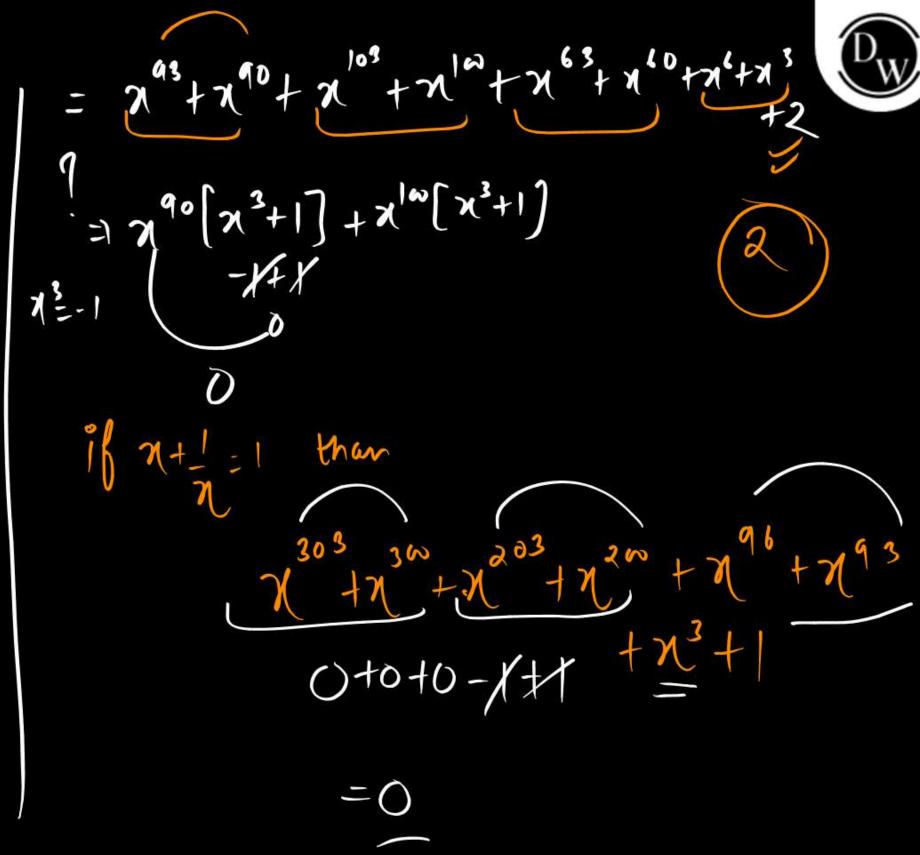
$$x^{16} + 1 = xxx^{15} + 1 = xxx^{15} + 1 = xxx^{15} + 1 = -(xx^{1})^{5}$$

$$x^{16} = -1 = xxx^{15} + 1 = -(xx^{1})^{5}$$

$$x^{17} + 1 = 1$$

$$x^{1$$

$$2xx^{2} + 1$$
 $2xx^{2} + 1$ 
 $2xx^{2} + 1$ 





$$x + \frac{1}{x} = -1$$

$$x^{3} = 1$$

### Dw

$$x + \frac{1}{x} = \sqrt{3}$$



If 
$$x + \frac{1}{x} = a$$
 then  $x - \frac{1}{x} = ?$ 

$$x^{2}+\frac{1}{x^{2}}+2=a^{2}$$

$$x^2 + 1 = \alpha^2 - 2$$

$$\left(x-\frac{1}{x}\right)^{2}=\alpha^{2}$$

$$x+\frac{1}{x}=10$$
 $x-\frac{1}{x}=\sqrt{\frac{96}{6x}}$ 
 $=\sqrt{\frac{16x}{6x}}$ 



If 
$$x - \frac{1}{x} = a$$
 then  $x + \frac{1}{x} = ?$ 

$$x^2 + \frac{1}{\lambda} - 2 = \alpha^2$$

$$\left(\chi + \frac{1}{\chi}\right)^{2} = \alpha^{2} + 4$$

$$\left(\chi + \frac{1}{\chi}\right) = \sqrt{q^2 + q}$$

$$3 - \frac{1}{3} = \frac{15}{3}$$

$$X-J=3$$

$$X - 1 = 3$$
  $X + 1 = \sqrt{13}$ 

## Dw

If 
$$x + \frac{1}{x} = a$$
 then  $x^2 + \frac{1}{x^2} = ?$ 

$$\chi + \frac{1}{7} = \alpha$$



If 
$$x - \frac{1}{x} = a$$
 then  $x^2 + \frac{1}{x^2} = ?$ 

$$3 - \frac{1}{3} = 3$$
 $3^{3} + \frac{1}{3} = 1$ 

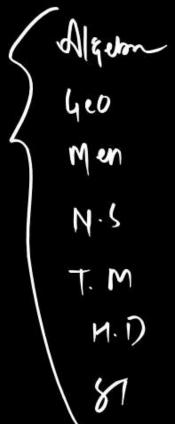
$$7 - \frac{1}{7} = 7 = 5$$

### Dw

If 
$$x + \frac{1}{x} = a$$
 then  $x^2 - \frac{1}{x^2} = ?$ 

$$\Rightarrow (x + \frac{1}{x})(x - \frac{1}{x})$$

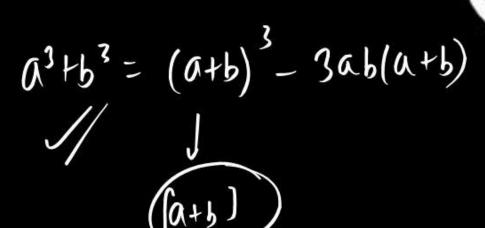
$$\Rightarrow (x - \frac{1}{x}) = \frac{1}{x^2} = ?$$



If 
$$x + \frac{1}{x} = a$$
 then  $x^3 + \frac{1}{x^3} = ?$ 

$$\chi^{3} + \frac{1}{\chi^{3}} + 3(\chi + \frac{1}{\chi}) = \alpha^{3}$$

$$\chi^3 + \frac{1}{4} = \alpha^3 = 3\alpha$$





$$\chi^{3} + \frac{1}{\sqrt{3}} = \frac{3}{3} - 3\chi^{3}$$





If 
$$x - \frac{1}{x} = a$$
 then  $x^3 - \frac{1}{x^3} = ?$ 

$$\chi^{\frac{3}{2}} = \alpha^{3} + 3\alpha$$

$$x^{3} = 4$$
 $x^{3} = 4$ 
 $x^{3} = 64$ 
 $x^{3} = 64$ 
 $x^{3} = 64$ 

If 
$$x + \frac{1}{x} = a$$
 then  $x^4 - \frac{1}{x^4} = ?$ 

1. If 
$$x + \frac{1}{x} = 4$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?  $= 4^2 \cdot 2 = 6 \cdot 2 = 4$ 

2. If 
$$x + \frac{1}{x} = 5$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?  $= 5^2 - 2 = 25 - 7 = 23$ 

3. If 
$$x + \frac{1}{x} = 3$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?

4. If 
$$x + \frac{1}{x} = 1$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?

5. If 
$$x + \frac{1}{x} = 7$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?



1. If 
$$x + \frac{1}{x} = 8$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?

2. If 
$$x + \frac{1}{x} = 9$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?

3. If 
$$x + \frac{1}{x} = 27$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?  $727$ 

4. If 
$$x + \frac{1}{x} = 25$$
, find the value of  $x^2 + \frac{1}{x^2}$ ? 63

5. If 
$$x + \frac{1}{x} = 23$$
, find the value of  $x^2 + \frac{1}{x^2}$ ?



If 
$$x + \frac{1}{x} = k$$

Hence, 
$$x^3 + \frac{1}{x^3} = k^3 - 3k$$

$$3+1=0$$
 $3+1=0^3-3a$ 



If 
$$x + \frac{1}{x} = 3$$
, find the value of  $x^3 + \frac{1}{x^3}$ ?  $= 27 - 9 = 18$ 

If  $x + \frac{1}{x} = 6$ , find the value of  $x^3 + \frac{1}{x^3}$ ?  $= 216 - 18 = 198$ 

If  $x + \frac{1}{x} = 4$ , find the value of  $x^3 + \frac{1}{x^3}$ ?  $= 69 - 12 = 52$ 

If  $x + \frac{1}{x} = 7$ , find the value of  $x^3 + \frac{1}{x^3}$ ?  $= 393 - 21 = 322$ 



$$x+\frac{1}{x}=k$$

$$\Rightarrow x^5 + \frac{1}{x^5} = (k^2 - 2)(k^3 - 3k) - k$$

$$= \left(x^2 + \frac{1}{x^2}\right) \left(x^3 + \frac{1}{x^3}\right) - \left(x + \frac{1}{x}\right)$$



$$x_3 + \frac{1}{2} = 110$$

$$7 \times 18 - 3$$

7(+) = K

= (x3+1/3) (x2+1/2) - (x+1/2)

$$x+\frac{1}{x}=k$$

$$\Rightarrow x^5 + \frac{1}{x^5} = (k^2 - 2)(k^3 - 3k) - k$$

If 
$$x + \frac{1}{x} = 5$$
, find the value of  $x^5 + \frac{1}{x^5}$ ?

If 
$$x + \frac{1}{x} = 6$$
, find the value of  $x^5 + \frac{1}{x^5}$ ?

If 
$$x + \frac{1}{x} = 10$$
, find the value of  $x^5 + \frac{1}{x^5}$ ?

If 
$$x + \frac{1}{x} = 1$$
, find the value of  $x^5 + \frac{1}{x^5}$ ?

#### **SQUARE FORMULA**



$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$(a-b)^2 = a^2 + b^2 - 2ab$$

$$(a+b)^2 = (a-b)^2 + 4ab$$

$$(a-b)^2 = (a+b)^2 - 4ab$$

$$(a^2 - ab + b^2)(a^2 + ab + b^2) = a^4 + a^2b^2 + b^2$$

$$(a+b)^2 - (a-b)^2 = 4ab$$

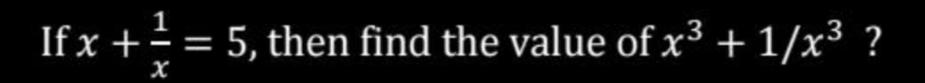
$$a^2 - b^2 = (a + b)(a - b)$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

If 
$$x + \frac{1}{x} = 3$$
, then find the value of  $x^3 + 1/x^3$ ?













If 
$$a^2 + b^2 - 5ab = 0$$
, then find the value of  $\left(\frac{a}{b}\right)^2 + \left(\frac{b}{a}\right)^2$ ?

$$a_{+b} = 5$$

$$\frac{a}{b} = x$$

$$(x-a) = \frac{1}{(x-b)}$$
  $(x-b) = \frac{1}{(x-a)}$ 

Dw

If (x-a)(x-b) = 1, and a-b+5=0 then find the value of

$$(x-a)^3 - \left(\frac{1}{x-a}\right)^3? \Rightarrow (x-a)^3 - (x-b)^3 = (+5)^3 + 3x + x + 5$$

$$(x-a)^3 - (x-b)^3$$

$$-a+b-5=0$$

$$-a+b=5$$

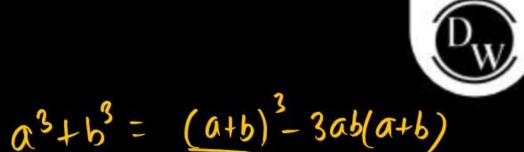
$$a^3 - b^3 = (a+b)^3 - 3ab(a+b)$$

$$a^{3}-b^{3}=(a-b)^{3}+3ab(a-b)$$

If 
$$x^2 + x = 5$$
then find the value of  $(x + 3)^3 + \left(\frac{1}{x+3}\right)^3$ ?

$$(x+3)+1=5$$

$$\frac{3}{3-x+9+6x+1} = \frac{5x+15}{5x+15} = \frac{5(x+3)}{x+3}$$



If 
$$x^2 + 4x = 4$$
then find the value of  $(x + 5)^3 + \left(\frac{1}{x+5}\right)^3$ ?

$$(x+5) + \frac{1}{(x+5)}$$

$$\Rightarrow$$

$$(6)^3 - 3 \times 6$$

$$= \frac{6x+30}{(x+5)} = \frac{6(x+8)}{(x+1)}$$

$$(a^3+b^3=(a+b)^3-3ab(a+b)$$
  
 $a^3+b^3=(a-b)^3+3ab(a-b)$ 

If 
$$x^2 + 2x = 4$$
then find the value of  $(x + 3)^3 - \left(\frac{1}{x+3}\right)^3$ ?

$$(9C+3) - \frac{1}{(7+3)} = 4$$

$$\frac{1}{3} \frac{4-2x+9+6x-1}{x+3} = \frac{4(x+3)-4}{x+3}$$

$$0^{3}-b^{3}=(a-b)^{3}+3ab(a-b)$$

If 
$$x^2 + x =$$

$$\chi^2 = ||-\chi|$$

$$\Rightarrow$$
  $(2+3) - \frac{5}{(x+3)}$ 

$$\frac{1}{2}(x+3)^{2}-\frac{5}{5}$$

$$= \chi^2 + 9 + 6\chi - 5$$

$$= \frac{31+35}{31+35} = \frac{5(31+3)}{(31+3)}$$

If 
$$x^2 + x = 11$$
then find the value of  $(x + 3)^3 - \left(\frac{5}{x+3}\right)^3$ ?



$$a^3-b^3=(a-b)^3+3ab(a-b)$$



If 
$$x^2 - 16x + 59 = 0$$
 then find the value of  $(x - 6)^2 + \left(\frac{1}{x - 6}\right)^2$ ?

$$\left(\chi-\ell\right)-\frac{1}{(\chi-\ell)}$$

$$= \frac{4x-24}{x-6}$$

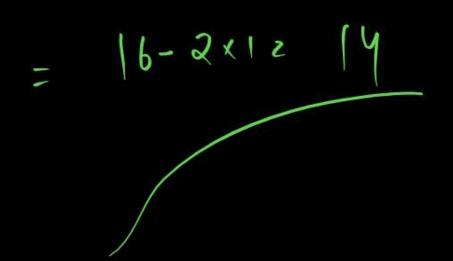
$$= \frac{4(x-6)}{(x-6)}$$

$$a^{2}+b^{2}=(a+b)^{2}-2ab$$

$$a^{2}+b^{2}=(a-b)^{2}+2ab$$

If 
$$x^2 - 12x + 33 = 0$$
 then find the value of  $(x - 4)^2 + \left(\frac{1}{x - 4}\right)^2$ ?  $(0.4\%)^2$ 





## Basic Formula:



$$\Box (a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$\Box (a - b)^3 = a^3 - b^3 - 3ab(a - b)$$



## If $P = \frac{X+Y}{X-Y}$ and $Q = \frac{X-Y}{X+Y}$ than what is the value of P+Q

$$= (x+y)^{2} + (x-y)^{2}$$

$$= Q[x^{2}+y^{2}]$$

$$= (x^{2}-y^{2})$$

Find 
$$\frac{\sqrt{3}+1}{\sqrt{3}-1} + \frac{\sqrt{3}-1}{\sqrt{3}+1}$$
?

$$-2 \left( ([3)^{2} + (1)^{2} \right)$$

$$- \left( ([3)^{2} - (1)^{2} \right)$$

$$=2\left[\frac{3+1}{3+1}\right]=\cancel{X}\cancel{X}\cancel{Y}$$

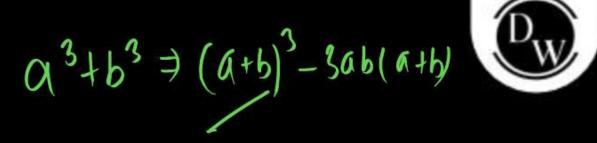
$$=\cancel{Y}$$



Find 
$$\left(\frac{\sqrt{3}+1}{\sqrt{3}-1}\right)^3 + \left(\frac{\sqrt{3}-1}{\sqrt{3}+1}\right)^3$$
?

$$=2[([3)^{2}+(1)^{2}]$$

$$=([3)^{2}-(1)^{2}$$







If 
$$x = \frac{2+\sqrt{3}}{2-\sqrt{3}}$$
 and  $y = \frac{2-\sqrt{3}}{2+\sqrt{3}}$  then find the value of  $\frac{x}{y} + \frac{y}{x}$ ?

$$y = \frac{2-13}{2+13}$$

alue of 
$$\frac{1}{y} + \frac{1}{x}$$
?
$$= 194$$

$$= 194$$

$$2+y=2[4+3]$$
[4-3]



If 
$$x = \frac{\sqrt{13} + \sqrt{11}}{\sqrt{13} - \sqrt{11}}$$
 and  $y = \frac{\sqrt{13} - \sqrt{11}}{\sqrt{13} + \sqrt{11}}$  then find the value of  $4x^2 - 2xy + 4y^2$ ?

$$2(+y) = 2[13+11]$$

$$-2[24]$$

$$7+4y=24$$
 $(24)^{2}-2x1$ 
 $=576-2$ 
 $=574$ 

= 
$$U(x^{2}+y^{2})-2xy$$
  
=  $4x574-2x1$ 

If 
$$x = \frac{\sqrt{5} + \sqrt{1}}{\sqrt{5} - \sqrt{1}}$$
 and  $y = \frac{\sqrt{5} - \sqrt{1}}{\sqrt{5} + \sqrt{1}}$  then find the value of  $\frac{x^2 - xy + y^2}{x^2 + xy + y^2}$ ?







If 
$$a = \frac{\sqrt{3} + \sqrt{1}}{\sqrt{3} - \sqrt{1}}$$
 and  $b = \frac{\sqrt{3} - \sqrt{1}}{\sqrt{3} + \sqrt{1}}$  then find the value of  $\frac{a}{b} + \frac{b}{a}$ ?





If 
$$a = \frac{\sqrt{3} + \sqrt{1}}{\sqrt{3} - \sqrt{1}}$$
 and  $b = \frac{\sqrt{3} - \sqrt{1}}{\sqrt{3} + \sqrt{1}}$  then find the value of  $\frac{a^2}{b} + \frac{b^2}{a}$ ?





If 
$$a = \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} - \sqrt{2}}$$
 and  $b = \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}}$  then find the value of  $a^2 + b^2 - 3ab$ ?





