

《《《 CDS/CAPF 》》》

VIRAAAT 2.0

2024

Algebra

Mathematics

Lecture – 01

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TOPICS *to be covered*

1 - Basic Formula

2 → Improper

3

$x + \frac{1}{x}$

Algebra

Basics

$$(a+b)^2$$

Different logics



Value putting,

symmetry, degree

etc.

CUBE FORMULA

$$\checkmark (a + b)^3 = a^3 + b^3 + \underline{3ab(a + b)}$$

$$\triangleright a^3 + b^3 = (a + b)^3 - 3ab(a + b)$$

$$\triangleright a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$\triangleright (a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

$$\triangleright a^3 - b^3 - (a - b)^3 + 3ab(a - b)$$

$$\triangleright a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

SPECIAL CASE

$$\triangleright \text{If } a^2 - ab + b^2 = 0 \text{ then } a^3 + b^3 = 0$$

$$\triangleright \text{If } b = 1, \text{ then } a^2 - a + 1 = 0, \text{ then } a^3 + 1 = 0 \text{ or } a^3 = -1$$



$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$a^2 + b^2 = (a+b)^2 - 2ab$$

$$(a+b)^2 = (a-b)^2 + 4ab$$

$$(a-b)^2 = a^2 + b^2 - 2ab$$

$$a^2 + b^2 = (a-b)^2 + 2ab$$

$$(a-b)^2 = (a+b)^2 - 4ab$$

$$a^2 - b^2 = (a+b)(a-b)$$

$$(a+b)^2 - (a-b)^2 = 4ab$$

SPECIAL CASE

➤ If $a^2 + a + 1 = 0$ then $a^3 - 1 = 0$ $a^3 = 1$

SPECIAL CASE

➤ If $\frac{a}{b} + \frac{b}{a} = 1$ then $a^3 + b^3 = 0$

SPECIAL CASE

➤ If $\frac{a}{b} + \frac{b}{a} = -1$ then $a^3 - b^3 = 0$

➤ If $\frac{a}{b} + \frac{b}{a} = \frac{1}{a+b}$ then $a^3 - b^3 = 0$

SPECIAL CASE

$$\begin{aligned}
 &\triangleright a^3 + b^3 + c^3 - 3abc \\
 &= \frac{1}{2} (a + b + c) [(a - b)^2 + (b - c)^2 + (c - a)^2] \\
 &= (a + b + c) (a^2 + b^2 + c^2 - ab - bc - ca) \\
 &= (a + b + c) [(a + b + c)^2 - 3(ab + bc + ca)]
 \end{aligned}$$

$$\triangleright \text{If } (a + b + c) = 0$$

$$\text{Then } a^3 + b^3 + c^3 - 3abc = 0$$

$$a^3 + b^3 + c^3 - 3abc = 0$$

$$\triangleright \text{If } a^3 + b^3 + c^3 - 3abc = 0$$

$$a, b \text{ and } c \text{ are distinct no then, } a + b + c = 0$$

Some Important Values :

$$x + \frac{1}{x} = 2$$

where $x = 1$

$$\Rightarrow \tan \theta + \frac{1}{\tan \theta} = 2$$

$$\tan \theta + \cot \theta = 2$$

$$\tan^4 \theta + \frac{1}{\tan^4 \theta} = ?$$

$$\underline{1+1 = 2}$$

$$\text{if } x + \frac{1}{x} = 2$$

$$x = ?$$

$$\textcircled{1} x^9 + \frac{1}{x^9} = ?$$

$$x=1 = 1+1 = \underline{\underline{2}}$$

$$\tan \leftrightarrow \cot$$

$$\sin \leftrightarrow \csc$$

$$\cos \leftrightarrow \sec$$



$$m + \frac{1}{m+2} = 0$$

$$\frac{(m+2)}{(m+2)} + \frac{1}{(m+2)} = 2$$

$$\underline{m+2 = 1}$$

$$m = 1-2 \quad \underline{m+2 = x}$$

$$\underline{m = -1}$$

$$\underline{x + \frac{1}{x} = 2}$$

$$x = 1$$

$$m+2 = 1$$

$$\frac{(m+2)^5 + 1}{(m+2)^5} = ?$$

$$\frac{(1)^5 + 1}{(1)^5} = 1+1 = 2$$

Some Important Values :



$$(-1)^{\text{even}} = +1$$

$$(-1)^{\text{odd}} = -1$$

$$x + \frac{1}{x} = -2$$

$$x = -1$$

$$x^7 + \frac{1}{x^7} = (-1)^7 + \frac{1}{(-1)^7} = -1 - 1 = -2$$

$$x^8 + \frac{1}{x^8} = (-1)^8 + \frac{1}{(-1)^8} = 1 + 1 = 2$$

$$x^8 + \frac{1}{x^7} = (-1)^8 + \frac{1}{(-1)^7} = 1 - 1 = 0$$

Some Important Values :



$$x + \frac{1}{x} = 1 \quad \checkmark \quad x^3 = -1$$

if $x + \frac{1}{x} = 1$

$$x^3 = -1$$

$$\frac{x^2 + 1}{x} = 1$$

$$x^2 + 1 = x$$

$$(x^2 - x + 1) = 0$$

$$(x+1)(x^2 - x + 1) = 0$$

$$x^3 + 1 = 0$$

$$x^3 = -1$$

$$\left[x^{17} + \frac{1}{x^{17}} \right] \times \frac{x}{x}$$

$$\Rightarrow \frac{x^{18}}{x} + \frac{x}{x^{18}}$$

$$\Rightarrow \frac{(x^3)^6}{x} + \frac{x}{(x^3)^6}$$

$$= \frac{(-1)^6}{x} + \frac{x}{(-1)^6} = \left(\frac{1}{x} + x \right) = 1$$

$$x^{12} + \frac{1}{x^{12}} = (x^3)^4 + \frac{1}{(x^3)^4} = (-1)^4 + \frac{1}{(-1)^4} = 1 + 1 = 2$$

$$x^{15} + \frac{1}{x^{15}} = (x^3)^5 + \frac{1}{(x^3)^5} = (-1)^5 + \frac{1}{(-1)^5} = -1 - 1 = -2$$

$$x^{16} + \frac{1}{x^{16}} = \frac{x \times x^{15} + 1}{x \times x^{15}} \Rightarrow \frac{x \times (x^3)^5 + 1}{x \times (x^3)^5} = \frac{x \times -1 + 1}{x \times -1} = -\left(x + \frac{1}{x}\right) = -1$$

$$\Rightarrow x^{17} + \frac{1}{x^{17}} = 1$$

$$x^{22} + \frac{1}{x^{22}} \Rightarrow x \times x^{21} + \frac{1}{x \times x^{21}}$$

$$\Rightarrow x \times (x^3)^7 + \frac{1}{x \times (x^3)^7}$$

$$x \times (-1)^7 + \frac{1}{x \times (-1)^7}$$

$$= -x - \frac{1}{x}$$

$$= -\left(x + \frac{1}{x}\right) = -1$$

if $x + \frac{1}{x} = 1$
 $x^3 = -1$

$$= x^{93} + x^{90} + x^{103} + x^{100} + x^{63} + x^{60} + x^6 + x^3 + 2$$

$$\Rightarrow x^{90} [x^3 + 1] + x^{60} [x^3 + 1]$$

$x^3 = -1$

$-x + x = 0$

0

2

if $x + \frac{1}{x} = 1$ then

$$x^{303} + x^{300} + x^{203} + x^{200} + x^{96} + x^{93} + x^3 + 1$$

$0 + 0 + 0 - x + x + x^3 + 1$

$$= 0$$

Some Important Values :

$$x + \frac{1}{x} = -1 \underline{\underline{=}}$$

$$x^3 = 1$$

Some Important Values :

$$x + \frac{1}{x} = \sqrt{3}$$

$$\chi^6 = -1$$

Some Important Values :



If $x + \frac{1}{x} = a$ then $x - \frac{1}{x} = ?$

$$x^2 + \frac{1}{x^2} + 2 = a^2$$

$$x^2 + \frac{1}{x^2} = a^2 - 2$$

$$x^2 + \frac{1}{x^2} - 2 = a^2 - 2 - 2$$

$$\left(x - \frac{1}{x}\right)^2 = a^2 - 4$$

$$x - \frac{1}{x} = \sqrt{a^2 - 4}$$

$$x + \frac{1}{x} = 3$$

$$x - \frac{1}{x} = \sqrt{5}$$

$$x + \frac{1}{x} = 4$$

$$x - \frac{1}{x} = \sqrt{12} = 2\sqrt{3}$$

$$x + \frac{1}{x} = 10$$

$$x - \frac{1}{x} = \sqrt{96} = \sqrt{16 \times 6} = 4\sqrt{6}$$

Some Important Values :

If $x - \frac{1}{x} = a$ then $x + \frac{1}{x} = ?$

$$x^2 + \frac{1}{x^2} - 2 = a^2$$

$$x^2 + \frac{1}{x^2} + 2 = a^2 + 2 + 2$$

$$\left(x + \frac{1}{x}\right)^2 = a^2 + 4$$

$$\left(x + \frac{1}{x}\right) = \sqrt{a^2 + 4}$$

$$x - \frac{1}{x} = \sqrt{5}$$

$$x + \frac{1}{x} = 3$$

$$x - \frac{1}{x} = 4\sqrt{6}$$

$$x + \frac{1}{x} = 10$$

$$x - \frac{1}{x} = 3$$

$$x + \frac{1}{x} = \sqrt{13}$$

Some Important Values :

$$\text{If } x + \frac{1}{x} = a \text{ then } x^2 + \frac{1}{x^2} = ?$$

$$x + \frac{1}{x} = a$$

$$x^2 + \frac{1}{x^2} = a^2 - 2$$



Some Important Values :

If $x - \frac{1}{x} = a$ then $x^2 + \frac{1}{x^2} = ?$

$$x^2 + \frac{1}{x^2} = a^2 + 2$$

$$x - \frac{1}{x} = 3$$

$$x^2 + \frac{1}{x^2} = 11$$

$$x - \frac{1}{x} = 5 \quad = 27$$

$$x - \frac{1}{x} = 7 \quad = 51$$

$$x - \frac{1}{x} = 9 \quad = 81$$

Some Important Values :

(40-50) 60



$$\text{If } x + \frac{1}{x} = a \text{ then } x^2 - \frac{1}{x^2} = ?$$

$$\Rightarrow \left(x + \frac{1}{x}\right) \left(x - \frac{1}{x}\right)$$

$$x - \frac{1}{x} = \sqrt{a^2 - 4}$$

$$x - \frac{1}{x} = a \sqrt{a^2 - 4}$$

Algebra
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Men
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Some Important Values :



$$\text{If } x + \frac{1}{x} = a \text{ then } x^3 + \frac{1}{x^3} = ?$$

$$x^3 + \frac{1}{x^3} + 3\left(x + \frac{1}{x}\right) = a^3$$

$$x^3 + \frac{1}{x^3} = a^3 - 3a$$

$$a^3 + b^3 = (a+b)^3 - 3ab(a+b)$$

✓✓

$$\downarrow$$
$$(a+b)$$

$$(a \times b)$$

$$x + \frac{1}{x} = 3$$

$$x^3 + \frac{1}{x^3} = 3^3 - 3 \times 3$$
$$= 27 - 9 = \underline{18}$$

Some Important Values :

If $x - \frac{1}{x} = a$ then $x^3 - \frac{1}{x^3} = ?$

$$x^3 - \frac{1}{x^3} = a^3 + 3a$$

$$x - \frac{1}{x} = 4$$

$$x^3 - \frac{1}{x^3} = 4^3 + 3 \times 4$$

$$= 64 + 12$$

$$= 76$$

Some Important Values :

$$\text{If } x + \frac{1}{x} = a \text{ then } x^4 - \frac{1}{x^4} = ?$$

$$x + \frac{1}{x} = a \quad x^2 + \frac{1}{x^2} = a^2 - 2$$



1. If $x + \frac{1}{x} = 4$, find the value of $x^2 + \frac{1}{x^2}$? $= 4^2 - 2 = 16 - 2 = 14$

2. If $x + \frac{1}{x} = 5$, find the value of $x^2 + \frac{1}{x^2}$? $= 5^2 - 2 = 25 - 2 = 23$

3. If $x + \frac{1}{x} = 3$, find the value of $x^2 + \frac{1}{x^2}$? $= 7$

4. If $x + \frac{1}{x} = 1$, find the value of $x^2 + \frac{1}{x^2}$? $= -1$

5. If $x + \frac{1}{x} = 7$, find the value of $x^2 + \frac{1}{x^2}$? 47

1. If $x + \frac{1}{x} = 8$, find the value of $x^2 + \frac{1}{x^2}$? 62

2. If $x + \frac{1}{x} = 9$, find the value of $x^2 + \frac{1}{x^2}$? 79

3. If $x + \frac{1}{x} = 27$, find the value of $x^2 + \frac{1}{x^2}$? 727

4. If $x + \frac{1}{x} = 25$, find the value of $x^2 + \frac{1}{x^2}$? 623

5. If $x + \frac{1}{x} = 23$, find the value of $x^2 + \frac{1}{x^2}$? 527



$$\text{If } x + \frac{1}{x} = k$$

$$\text{Hence, } x^3 + \frac{1}{x^3} = k^3 - 3k$$

$$x + \frac{1}{x} = a \quad x^3 + \frac{1}{x^3} = a^3 - 3a$$



- ✓ If $x + \frac{1}{x} = 3$, find the value of $x^3 + \frac{1}{x^3}$? $= 27 - 9 = 18$
- ✓ If $x + \frac{1}{x} = 6$, find the value of $x^3 + \frac{1}{x^3}$? $= 216 - 18 = 198$
- ✓ If $x + \frac{1}{x} = 4$, find the value of $x^3 + \frac{1}{x^3}$? $= 64 - 12 = 52$
- ✓ If $x + \frac{1}{x} = 7$, find the value of $x^3 + \frac{1}{x^3}$? $= 343 - 21 = \underline{322}$

$$x + \frac{1}{x} = k$$

$$\Rightarrow x^5 + \frac{1}{x^5} = (k^2 - 2)(k^3 - 3k) - k$$

$$= \underbrace{\left(x^2 + \frac{1}{x^2}\right)}_{\text{}} \underbrace{\left(x^3 + \frac{1}{x^3}\right)}_{\text{}} - \left(x + \frac{1}{x}\right)$$



$$x + \frac{1}{x} = 5$$

$$x^5 + \frac{1}{x^5} =$$

$$x^2 + \frac{1}{x^2} = 23$$

$$= 23 \times 110 - 5$$

$$x^3 + \frac{1}{x^3} = 110$$

$$= 2530 - 5$$

$$= 2525$$

$$x + \frac{1}{x} = 3$$

$$x^5 + \frac{1}{x^5} =$$

$$7 \times 18 - 3$$

$$= 126 - 3$$

$$= 123$$

$$x + \frac{1}{x} = k$$

$$= \left(x^3 + \frac{1}{x^3}\right) \left(x^2 + \frac{1}{x^2}\right) - \left(x + \frac{1}{x}\right)$$

$$x + \frac{1}{x} = k \quad \text{(H/W)}$$

$$\Rightarrow x^5 + \frac{1}{x^5} = (k^2 - 2)(k^3 - 3k) - k$$

✓ 1. If $x + \frac{1}{x} = 5$, find the value of $x^5 + \frac{1}{x^5}$?

2. If $x + \frac{1}{x} = 6$, find the value of $x^5 + \frac{1}{x^5}$?

3. If $x + \frac{1}{x} = 10$, find the value of $x^5 + \frac{1}{x^5}$?

✓ If $x + \frac{1}{x} = 1$, find the value of $x^5 + \frac{1}{x^5}$?

SQUARE FORMULA

➤ $(a + b)^2 = a^2 + b^2 + 2ab$

➤ $(a - b)^2 = a^2 + b^2 - 2ab$

➤ $(a + b)^2 = (a - b)^2 + 4ab$

➤ $(a - b)^2 = (a + b)^2 - 4ab$

➤ $(a^2 - ab + b^2)(a^2 + ab + b^2) = a^4 + a^2b^2 + b^4$

➤ $(a + b)^2 - (a - b)^2 = 4ab$

➤ $a^2 - b^2 = (a + b)(a - b)$

➤ $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$



If $x + \frac{1}{x} = 3$, then find the value of $x^3 + 1/x^3$?

H/W



If $x + \frac{1}{x} = 5$, then find the value of $x^3 + 1/x^3$?

H/W

If $a^2 + b^2 - 5ab = 0$, then find the value of $\left(\frac{a}{b}\right)^2 + \left(\frac{b}{a}\right)^2$?

↓

$$\frac{a^2}{ab} + \frac{b^2}{ab} = \frac{5ab}{ab}$$

$$\frac{a}{b} + \frac{b}{a} = 5$$

$$x + \frac{1}{x} = 5$$

$$x^2 + \frac{1}{x^2} = 23 \quad \left(\frac{a}{b}\right)^2 + \left(\frac{b}{a}\right)^2 = 23$$

$$\left(\frac{a}{b}\right)^2 + \left(\frac{b}{a}\right)^2$$

$$\frac{a}{b} = x$$



$$(x-a) = \frac{1}{(x-b)} \quad (x-b) = \frac{1}{(x-a)}$$

If $(x-a)(x-b) = 1$, and $a-b+5=0$ then find the value of

$$(x-a)^3 - \left(\frac{1}{x-a}\right)^3? \Rightarrow (x-a)^3 - (x-b)^3 = (+5)^3 + 3 \times 1 \times 5$$

$$(x-a)^3 - (x-b)^3$$

$$\Rightarrow 5^3 + 3 \times 1 \times 5$$

$$= 125 + 15$$

$$= 140$$

$$-a+b-5=0$$

$$-a+b=5$$

)

$$a-b+5=0$$

$$\boxed{-a+b=5}$$

$$x-a - x+b$$

$$-a+b=5$$

$$a-b=-5$$

$$-a+b=5$$

$$a^3 - b^3 = (a+b)^3 - 3ab(a+b)$$

$$a^3 - b^3 = (a-b)^3 + 3ab(a-b)$$



If $x^2 + x = 5$ then find the value of $(x+3)^3 + \left(\frac{1}{x+3}\right)^3$?

$$\underline{\underline{x^2 = (5-x)}}$$

$$a^3 + b^3 = \underline{(a+b)^3} - 3ab(a+b)$$

$$\underbrace{(x+3)}_{\wedge (x+3)} + \underbrace{1}_{(x+3)} = 5$$

$$\Rightarrow \frac{(x+3)^2 + 1}{(x+3)}$$

$$\Rightarrow \frac{x^2 + 9 + 6x + 1}{x+3}$$

$$\Rightarrow \frac{5-x+9+6x+1}{x+3}$$

$$\Rightarrow \frac{5x+15}{x+3}$$

$$\frac{5(x+3)}{(x+3)} = 5$$

$$= 5^3 - 3 \times 1 \times 5$$

$$= 125 - 15$$

$$= \underline{\underline{110}}$$



If $x^2 + 4x = 4$ then find the value of $(x+5)^3 + \left(\frac{1}{x+5}\right)^3$?

$$x^2 = 4 - 4x$$

$$(x+5) + \frac{1}{(x+5)}$$

\Rightarrow

$$(6)^3 - 3 \times 6$$

$$\Rightarrow 216 - 18$$

$$\Rightarrow 198$$

$$\frac{x^2 + 25 + 10x + 1}{(x+5)}$$

$$\frac{4 - 4x + 25 + 10x + 1}{(x+5)}$$

$$\Rightarrow \frac{6x + 30}{(x+5)} \Rightarrow \frac{6(x+5)}{\cancel{(x+5)}}$$

$$\Rightarrow \underline{6}$$

<

$$a^3 + b^3 = (a+b)^3 - 3ab(a+b)$$

$$a^3 + b^3 = (a-b)^3 + 3ab(a-b)$$

$$x^2 = 4 - 2x$$

If $\underbrace{x^2 + 2x = 4}$ then find the value of $(x+3)^3 - \left(\frac{1}{x+3}\right)^3$?

$$a^3 - b^3 = (a-b)^3 + 3ab(a-b)$$

$$(x+3) - \frac{1}{(x+3)} = 4$$

$$= 4^3 + 3 \times 4$$

$$= 64 + 12$$

$$= \underline{76}$$

$$\Rightarrow \frac{(x+3)^2 - 1}{x+3}$$

$$\Rightarrow \frac{x^2 + 9 + 6x - 1}{x+3}$$

$$\Rightarrow \frac{4 - 2x + 9 + 6x - 1}{x+3}$$

$$\Rightarrow \frac{4x + 12}{x+3} \Rightarrow \frac{4(x+3)}{(x+3)} = 4$$



If $x^2 + x = 11$ then find the value of $(x+3)^3 - \left(\frac{5}{x+3}\right)^3$?

$$x^2 = 11 - x$$

$$\Rightarrow (x+3) - \frac{5}{(x+3)}$$

$$\Rightarrow \frac{(x+3)^2 - 5}{(x+3)}$$

$$= \frac{x^2 + 9 + 6x - 5}{x+3}$$

$$= \frac{11 - x + 9 + 6x - 5}{x+3}$$

$$= \frac{5x + 15}{x+3} = \frac{5(x+3)}{(x+3)} = 5$$

$$= 5^3 + 3 \times 5 \times 5$$

$$= 125 + 75$$

$$= 125 + 75$$

$$= \underline{200}$$

$$a^3 - b^3 = (a-b)^3 + 3ab(a-b)$$

$$\cancel{(x+3)} \times \frac{5}{\cancel{(x+3)}}$$



If $x^2 - 16x + 59 = 0$ then find the value of $(x - 6)^2 + \left(\frac{1}{x-6}\right)^2$?

$$(x-6) - \frac{1}{(x-6)}$$

$$= \frac{x^2 + 36 - 12x + 1}{x-6}$$

$$= \frac{16x - 59 + 36 - 12x + 1}{x-6}$$

$$= \frac{4x - 24}{x-6}$$

$$= \frac{4(x-6)}{(x-6)} = 4$$

$$\begin{array}{r} 59 \\ 35 \\ \hline 24 \end{array}$$

$$= (4)^2 + 2 \times 1$$

$$= 16 + 2 = 18$$

$$a^2 + b^2 = (a+b)^2 - 2ab$$

$$a^2 + b^2 = (a-b)^2 + 2ab$$

If $x^2 - 12x + 33 = 0$ then find the value of $(x - 4)^2 + \left(\frac{1}{x-4}\right)^2$? (a+b)²

$$x-4 + \frac{1}{x-4}$$

$$\Rightarrow \frac{x^2 + 16 - 8x + 1}{x-4}$$

$$\frac{12x - 33 + 16 - 8x + 1}{x-4}$$

$$\Rightarrow \frac{4x - 16}{x-4} \quad \frac{4(x-4)}{(x-4)} = 4$$

$$= 16 - 2 \times 12 + 14$$

Basic Formula:

$$\square (a + b)^3 = a^3 + b^3 + 3ab(a + b)$$

$$\square (a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

If $P = \frac{X+Y}{X-Y}$ and $Q = \frac{X-Y}{X+Y}$ than what is the value of $P+Q$

$$P+Q = \frac{x+y}{x-y} + \frac{x-y}{x+y}$$

$$= \frac{(x+y)^2 + (x-y)^2}{x^2 - y^2}$$

$$= \frac{2(x^2 + y^2)}{(x^2 - y^2)}$$

$$P = \frac{\sqrt{2}+1}{\sqrt{2}-1}$$

$$Q = \frac{\sqrt{2}-1}{\sqrt{2}+1}$$

$$P+Q = \frac{2(2+1)}{2-1} = \frac{2 \times 3}{1} = 6$$

Find $\frac{\sqrt{3}+1}{\sqrt{3}-1} + \frac{\sqrt{3}-1}{\sqrt{3}+1}$?

$$= \frac{2 \left[(\sqrt{3})^2 + (1)^2 \right]}{(\sqrt{3})^2 - (1)^2}$$

$$= \frac{2 \left[3+1 \right]}{3-1} = \frac{\cancel{2} \times 4}{\cancel{2}}$$

$$= 4$$



Find $\left(\frac{\sqrt{3}+1}{\sqrt{3}-1}\right)^3 + \left(\frac{\sqrt{3}-1}{\sqrt{3}+1}\right)^3$?

$$= \frac{2[(\sqrt{3})^2 + (1)^2]}{(\sqrt{3})^2 - (1)^2} = \textcircled{1}$$

$$= \frac{2[4]}{2}$$
$$= 4$$

$$\left(\frac{\sqrt{3}+1}{\sqrt{3}-1}\right) \times \left(\frac{\sqrt{3}-1}{\sqrt{3}+1}\right)$$

$$a^3 + b^3 \Rightarrow (a+b)^3 - 3ab(a+b)$$

$$\Rightarrow 4^3 - 3 \times 1 \times 4$$

$$= 64 - 12$$

$$= \underline{52}$$



If $x = \frac{2+\sqrt{3}}{2-\sqrt{3}}$ and $y = \frac{2-\sqrt{3}}{2+\sqrt{3}}$ then find the value of $\frac{x}{y} + \frac{y}{x}$ $= \frac{x^2 + y^2}{xy}$

$$x = \frac{2+\sqrt{3}}{2-\sqrt{3}}$$

$$y = \frac{2-\sqrt{3}}{2+\sqrt{3}}$$

$$x \times y = 1$$

$$= \frac{194}{1}$$

$$= 194$$

$$x^2 + y^2 = (x+y)^2 - 2xy$$

$$x+y = 2 \frac{[4+3]}{[4-3]}$$

$$x+y = 14$$

$$x^2 + y^2 = 196 - 2$$
$$= \underline{194}$$

If $x = \frac{\sqrt{13}+\sqrt{11}}{\sqrt{13}-\sqrt{11}}$ and $y = \frac{\sqrt{13}-\sqrt{11}}{\sqrt{13}+\sqrt{11}}$ then find the value of $4x^2 - 2xy + 4y^2$?

$$x+y = \frac{2(13+11)}{13-11}$$

$$= \frac{2(24)}{2}$$

$$x+y = 24$$

$$\begin{aligned} \underline{\underline{(x^2+y^2)}} &= (24)^2 - 2 \times 1 \\ &= 576 - 2 \\ &= \underline{\underline{574}} \end{aligned}$$

$$= 4(x^2+y^2) - 2xy$$

$$= 4 \times 574 - 2 \times 1$$

$$= 2296 - 2$$

$$= \underline{\underline{2294}}$$

$$x^2+y^2 = (x+y)^2 - 2xy$$



If $x = \frac{\sqrt{5}+\sqrt{1}}{\sqrt{5}-\sqrt{1}}$ and $y = \frac{\sqrt{5}-\sqrt{1}}{\sqrt{5}+\sqrt{1}}$ then find the value of $\frac{x^2-xy+y^2}{x^2+xy+y^2}$?

H/W

If $a = \frac{\sqrt{3}+\sqrt{1}}{\sqrt{3}-\sqrt{1}}$ and $b = \frac{\sqrt{3}-\sqrt{1}}{\sqrt{3}+\sqrt{1}}$ then find the value of $\frac{a}{b} + \frac{b}{a}$?

4/5



If $a = \frac{\sqrt{3}+\sqrt{1}}{\sqrt{3}-\sqrt{1}}$ and $b = \frac{\sqrt{3}-\sqrt{1}}{\sqrt{3}+\sqrt{1}}$ then find the value of $\frac{a^2}{b} + \frac{b^2}{a}$?

H/W



If $a = \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}$ and $b = \frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$ then find the value of $a^2 + b^2 - 3ab$?

H/w



**JAI
HIND**