

BT5110: Tutorial 1 — Relational Model

Pratik Karmakar

School of Computing,
National University of Singapore

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What is the relational model? (in plain words)

- Think **spreadsheets**: each **table** is a sheet, **rows** are items, **columns** are properties.
- Formally, a table is a **relation**; a row is a **tuple**; a column is an **attribute**.
- Each table has a rule for what counts as a valid row: that rulebook is the **schema**.
- Tables can be **linked**—a value in one table points to a matching value in another.
- Why it's powerful: simple structure, **strong guarantees** (constraints, transactions), and **declarative** querying (SQL).

Everyday analogy

Students table

- One row per student
- Columns: email, name, faculty, department, year
- **Primary key** (email) uniquely identifies a student

Books table

- One row per book title
- Columns: isbn13 (PK), isbn10, title, author, publisher, year

Copies & Loans

- `copy(owner, book, copy_no, ...)`
- `loan(owner, book, copy_no, borrowed, returned)`
- **Foreign keys** connect:
 - `copy.owner` → `student.email`
 - `copy.book` → `book.isbn13`
 - `loan.(owner, book, copy_no)` → `copy`

Keys, relationships, and constraints

- **Primary key (PK):** a column (or set) that uniquely identifies each row.
- **Foreign key (FK):** a column whose values must match a PK in another table.
- **Domain & CHECK constraints:** control valid values (e.g., dates, non-negative pages).
- **Entity integrity:** PK cannot be NULL.
- **Referential integrity:** FK must reference an existing PK (or be NULL if allowed).
- These rules keep data **consistent** across tables.

How we ask questions (SQL mirrors simple ops)

Core ideas

- **Filter** rows (*selection*, σ):
WHERE
- **Pick** columns (*projection*, π):
SELECT list
- **Match** tables (*join*, \bowtie): JOIN
... ON
- **Summarize** (*group/aggregate*):
GROUP BY, COUNT, SUM, ...

Example questions

- “Which copies are currently on loan?”
- “Which students own at least two books?”
- “How many Chemistry students borrowed in 2024?”

Takeaway: you describe *what* you want; the database figures out *how* to get it efficiently (query optimization).

Why Relational Algebra?

- **Foundation of SQL:** Relational algebra provides the formal, mathematical basis for relational databases.
- Defines **operations on relations** that always produce relations.
- Ensures queries are **precise**, **composable**, and **optimizable**.
- SQL = (mostly) declarative syntax built on these algebraic ideas.

Core Operators

- **Selection (σ)**: Pick rows that satisfy a condition.
 $\sigma_{\text{year}=2024}(\text{Student})$
- **Projection (π)**: Pick certain columns. $\pi_{\text{name, email}}(\text{Student})$
- **Renaming (ρ)**: Rename relation/attributes. $\rho_S(\text{Student})$
- **Union (\cup), Difference ($-$), Intersection (\cap)**: Set-like ops (schemas must match).
- **Cartesian Product (\times)**: Pair all tuples across two relations.
- **Join (\bowtie)**: Combine rows across relations on matching attributes.

Examples and SQL Mapping

Relational Algebra

- $\pi_{\text{name}}(\sigma_{\text{faculty}=\text{'SoC'}}(\text{Student}))$

```
1 SELECT name
2 FROM student
3 WHERE faculty = 'SoC';
```

- $\text{Student} \bowtie_{\text{student.email}=\text{copy.owner}} \text{Copy}$

```
1 SELECT *
2 FROM student s
3 JOIN copy c
4   ON s.email = c.owner;
```

- $\pi_{\text{isbn13}}(\text{Book}) - \pi_{\text{book}}(\text{Copy})$

```
1 SELECT isbn13
2 FROM book
3 EXCEPT
4 SELECT book
5 FROM copy;
```


Takeaway

- Relational algebra = the **mathematical core** of querying.
- SQL extends it with ordering, grouping, aggregation, etc.
- Understanding algebra clarifies how SQL queries work “under the hood.”

Case Description

Students at the National University of Ngendipura (NUN) buy, lend, and borrow books. Your company, Apasaja Private Limited, is commissioned by NUN Students Association (NUNStA) to implement an online book exchange system that records information about students, books they own, and the books they lend/borrow.

The database stores:

- **Students:** name, faculty, department, join date (year). Identifier: email.
- **Books:** title, authors, publisher, year/edition, ISBN-10, ISBN-13.
- **Loans:** per-copy borrow and return dates.

Auditing policy keeps book/copy/owner info while owners are students or copies have loan records; graduated students are kept if loans exist on books they owned.

Q1. Data Definition Language (DDL)

(a) Download from Canvas ▷ Files ▷ Cases ▷ Book

Exchange:

NUNStASchema.sql, NUNStAClean.sql, NUNStAStudent.sql,
NUNStABook.sql, NUNStACopy.sql, NUNStALoan.sql.

(b) What they do:

- **Clean Up:** NUNStAClean.sql drops tables using IF EXISTS.
- **Schema:** NUNStASchema.sql creates tables with domains/constraints using IF NOT EXISTS.
- **Data:** NUNStAStudent.sql, NUNStABook.sql, NUNStACopy.sql, NUNStALoan.sql populate tables (order matters).

Q1. Create & Populate — Correct Order

(c) In **pgAdmin 4**, run:

- 1 Create: student, book
- 2 Create: copy, loan (FKs depend on 1)
- 3 Populate: student, book (any order)
- 4 Populate: copy \rightarrow loan

Cleanup is reverse: loan \rightarrow copy \rightarrow student, book.

Q2. Insert / Delete / Update — Book Inserts

(a) Insert a new book:

```
1  INSERT INTO book VALUES (  
2    'An Introduction to Database Systems',  
3    'paperback',  
4    640,  
5    'English',  
6    'C. J. Date',  
7    'Pearson',  
8    '2003-01-01',  
9    '0321197844',  
10   '978-0321197849'  
11 );  
12 -- Verify:  
13 SELECT * FROM book;
```

Q2. Book Variants & Keys

(b) Same book, different ISBN13 (unique isbn10 violated):

```
1  INSERT INTO book VALUES (  
2      'An Introduction to Database Systems',  
3      'paperback',  
4      640,  
5      'English',  
6      'C. J. Date',  
7      'Pearson',  
8      '2003-01-01',  
9      '0321197844',  
10     '978-0201385908'  
11 );
```

Q2. Book Variants & Keys

(c) Same book, different ISBN10 (PK isbn13 violated):

```
1  INSERT INTO book VALUES (  
2    'An Introduction to Database Systems',  
3    'paperback',  
4    640,  
5    'English',  
6    'C. J. Date',  
7    'Pearson',  
8    '2003-01-01',  
9    '0201385902',  
10   '978-0321197849'  
11 );
```

Q2. Insert Students

(d) Explicit values; year may be NULL:

```
1 INSERT INTO student VALUES (  
2     'TIKKI TAVI',  
3     'tikki@gmail.com',  
4     '2024-08-15',  
5     'School of Computing',  
6     'CS',  
7     NULL  
8 );
```


Q2. Insert Students

(e) Column list (omitting PK forces NULL and fails):

```
1  INSERT INTO student (email, name, year, faculty, department)
   VALUES (
2    'rikki@gmail.com',
3    'RIKKI TAVI',
4    '2024-08-15',
5    'School of Computing',
6    'CS'
7  );
8
9  -- Fails: PK email omitted -> NULL not allowed
10 INSERT INTO student (name, year, faculty, department) VALUES (
11   'RIKKI TAVI',
12   '2024-08-15',
13   'School of Computing',
14   'CS'
15 );
```

Q2. Update & Delete

(f) Normalize department spelling:

```
1 UPDATE student
2 SET department = 'Computer Science'
3 WHERE department = 'CS';
4
5 -- Checks
6 SELECT * FROM student WHERE department = 'CS';           --
   empty
7 SELECT * FROM student WHERE department = 'Computer Science'; --
   rows
```

(g) Case-sensitive delete (no-op):

```
1 DELETE FROM student WHERE department = 'chemistry';
```

(h) Delete protected by FKs (likely fails unless schema permits):

```
1 DELETE FROM student WHERE department = 'Chemistry';
```

Q3. DEFERRABLE Constraints (Semantics)

(a) In PostgreSQL, UNIQUE/PRIMARY KEY/FOREIGN KEY may be:

- NOT DEFERRABLE (always *IMMEDIATE*),
- DEFERRABLE INITIALLY IMMEDIATE,
- DEFERRABLE INITIALLY DEFERRED.

Q3. Delete Book + Copy (Immediate vs Deferred)

Insert a copy owned by tikki:

```
1 INSERT INTO copy VALUES (  
2     'tikki@gmail.com',  
3     '978-0321197849',  
4     1,  
5     'TRUE'  
6 );
```

Transaction #1 (IMMEDIATE) — violates FK on first delete:

```
1 BEGIN TRANSACTION;  
2  
3 SET CONSTRAINTS ALL IMMEDIATE;  
4 DELETE FROM book WHERE ISBN13 = '978-0321197849';  
5 DELETE FROM copy WHERE book = '978-0321197849';  
6  
7 END TRANSACTION;
```

Q3. Deferred Transaction (Succeeds)

Transaction #2 (DEFERRED) — combined effect OK at commit:

```
1 BEGIN TRANSACTION;  
2  
3 SET CONSTRAINTS ALL DEFERRED;  
4 DELETE FROM book WHERE ISBN13 = '978-0321197849';  
5 DELETE FROM copy WHERE book = '978-0321197849';  
6  
7 END TRANSACTION;
```

Check intermediate state after deleting the book (line 3):

```
1 -- Book is gone  
2 SELECT * FROM book b WHERE b.ISBN13 = '978-0321197849';  
3  
4 -- Copy still present -> intermediate state inconsistent  
5 SELECT * FROM copy c WHERE c.book = '978-0321197849';
```

Q4. Modifying the Schema — Drop Redundant Availability

(a) Availability is derivable: a copy is unavailable iff it has an open loan.

```
1  -- Unreturned loans
2  SELECT owner, book, copy, returned
3  FROM loan
4  WHERE returned ISNULL;
5
6  -- Remove redundant column
7  ALTER TABLE copy
8  DROP COLUMN available;
```

Q4. Modifying the Schema — Drop Redundant Availability

```
1  -- View that recomputes availability
2  CREATE OR REPLACE VIEW copy_view (owner, book, copy, available)
   AS (
3    SELECT DISTINCT c.owner, c.book, c.copy,
4    CASE
5      WHEN EXISTS (
6        SELECT * FROM loan l
7        WHERE l.owner = c.owner
8              AND l.book = c.book
9              AND l.copy = c.copy
10             AND l.returned ISNULL
11      ) THEN 'FALSE'
12      ELSE 'TRUE'
13    END
14    FROM copy c
15 );
```

Q4. Modifying the Schema — Drop Redundant Availability

```
1  -- Example update attempt (requires INSTEAD OF trigger/rule in
   practice)
2  UPDATE copy_view
3  SET owner = 'tikki@google.com'
4  WHERE owner = 'tikki@gmail.com';
5
6  -- Drop when done
7  DROP VIEW copy_view;
```


Q4. Normalize Department \rightarrow Faculty Mapping

(b) department \rightarrow faculty (FD) — store mapping once.

```
1 CREATE TABLE department (  
2     department VARCHAR(32) PRIMARY KEY,  
3     faculty     VARCHAR(62) NOT NULL  
4 );  
5  
6 INSERT INTO department  
7 SELECT DISTINCT department, faculty  
8 FROM student;  
9  
10 ALTER TABLE student  
11 DROP COLUMN faculty;  
12  
13 ALTER TABLE student  
14 ADD FOREIGN KEY (department) REFERENCES department(department);
```

Questions?

Drop a mail at: pratik.karmakar@u.nus.edu