# IT5008: Tutorial 5 — Relational Algebra

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#### Scenario

Students at the National University of Ngendipura (NUN) buy, lend, and borrow books.

NUNStA commissions *Apasaja Private Limited* to implement an online book exchange system that records:

- Students: name, faculty, department, email, join year.
- Books: title, authors, publisher, edition, ISBN10, ISBN13.
- Loans: borrowed date, returned date (NULL if active).

Auditing preserves records of graduated students and copies with loans. This tutorial uses the schema/data from "SQL: Creating and Populating Tables."



# Questions

Setup

- Relational Algebra
  - (a) Find the different departments in School of Computing.
  - (b) Find emails of students who borrowed/lent a book before joining the University.
  - (c) Find emails of students who borrowed but did not lend a book *on* joining day.
- 2 Universal Quantification
  - (a) Find emails and names of students who borrowed *all* books authored by Adam Smith.

### Relational Algebra:

```
\pi_{d.department}(\sigma_{d.faculty='School\ of\ Computing'}(\rho(department,d)))
```

#### **SQL** Equivalent:

```
SELECT d.department
FROM department d
WHERE d.faculty = 'School of Computing';
```

# 1(b). Borrowed or lent before joining

### Relational Algebra:

```
\pi_{s.email}(\sigma_{(s.email=1.borrower\lor s.email=1.owner})\land (l.borrowed < s.year)(\rho(student, s) \times \rho(loan, l)))
```

# SQL Equivalent:

```
SELECT s.email
FROM student s, loan l
WHERE (s.email = l.borrower OR s.email = l.owner)
AND l.borrowed < s.year;</pre>
```

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Setup

# Using INNER JOIN:

```
SELECT s.email
FROM student s
INNER JOIN loan 1
ON (s.email = 1.borrower OR s.email = 1.owner)
AND 1.borrowed < s.year;
```

Relational Algebra

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#### Using UNION:

```
SELECT s1.email
FROM loan 11, student s1
WHERE s1.email = 11.borrower
 AND 11.borrowed < s1.year
UNTON
SELECT s2.email
FROM loan 12, student s2
WHERE s2.email = 12.owner
 AND 12.borrowed < s2.year;
```

# Relational Algebra:

```
\pi_{s1.email}(\sigma_{s1.email}=11.borrower \land 11.borrowed=s1.vear}(\rho(student, s1) \times 1)
\rho(loan, l1))) -
\pi_{s2.email}(\sigma_{s2.email}=12.owner \land 12.borrowed=s2.year(\rho(student, s2) \times 12.borrowed=s2.year(\rho(student, s2)))
\rho(loan, 12))
```

Relational Algebra

# **SQL** Equivalent:

```
SELECT sl.email
FROM loan 11, student s1
WHERE sl.email = 11.borrower
 AND 11.borrowed = s1.year
EXCEPT
SELECT s2.email
FROM loan 12, student s2
WHERE s2.email = 12.owner
 AND 12.borrowed = s2.year;
```

# 2(a). Borrowed all books by Adam Smith

# SQL Nested Query (Corrected):

```
SELECT s.email, s.name
FROM student s
WHERE NOT EXISTS (
SELECT 1
FROM book b
WHERE b.authors = 'Adam Smith'
AND NOT EXISTS (
SELECT 1
FROM loan 1
WHERE 1.book = b.ISBN13
AND 1.borrower = s.email));
```

*Idea:* For each student, check that there is no Adam Smith book that they have not borrowed.



Setup

# 2(a). Relational Algebra Strategy

Break the problem into steps (universal quantification via set difference):

Relational Algebra

Find all Adam Smith books.

$$Q1 = \pi_{\mathsf{ISBN13}}(\sigma_{\mathsf{authors}} = {}^{\mathsf{Adam}} \mathsf{Smith}^{\mathsf{Authors}})$$

2 Form all possible student-book pairs (expected borrowings).

$$Q2 = \pi_{\mathsf{email}, \mathsf{name}, \mathsf{ISBN13}}(\mathsf{student} \times Q1)$$

S Find actual borrowings of Adam Smith books.

$$Q3 = \pi_{\mathsf{email}, \; \mathsf{name}, \; \mathsf{ISBN13}}(\mathsf{student} \bowtie \mathsf{loan} \bowtie \sigma_{\mathsf{authors}='\mathsf{Adam} \; \mathsf{Smith'}}(\mathsf{book}))$$

4 Identify missing borrowings (pairs in Q2 but not in Q3).

$$Q4 = Q2 - Q3$$

Remove students in Q4 from the set of all students.

$$Q5 = \pi_{\text{email, name}}(\text{student}) - \pi_{\text{email, name}}(Q4)$$

**Answer:** Q5 = students who borrowed all Adam Smith books.

# 2(a). SQL from Relational Algebra

```
SELECT s.email, s.name
    FROM student s
    EXCEPT
    SELECT t.email, t.name
    FROM (
      SELECT s1.email, s1.name, b1.ISBN13
      FROM student s1, book b1
      WHERE bl.authors = 'Adam Smith'
      EXCEPT
      SELECT s2.email, s2.name, b2.ISBN13
      FROM student s2
           JOIN loan 12 ON s2.email = 12.borrower
13
           JOIN book by ON by TSBN13 = 12 book
14
      WHERE b2.authors = 'Adam Smith'
     AS t;
```

### Guidelines & Remarks

Setup

- Use relational algebra to reason about SQL queries.
- Remember: EXCEPT in SQL corresponds to set difference () in algebra.
- Joins in SQL correspond to natural/-joins in algebra.
- Break universal quantification into difference-based subqueries.
- Keep queries readable: aliases, indentation, uppercase SQL keywords.

Setup

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