

## Experiment no - 8

**Aim:** Beginning with an empty binary search tree, construct binary search tree by inserting the values in the order given. After constructing a binary tree -

- Insert new node
- Find no. of nodes in longest path
- Minimum data value found in the tree
- Change a tree so that the roles of the left & right pointers are swapped at every node
- Search a value

### Theory:

Binary Search Tree is node-based binary tree data structure which has the following properties:

- The left subtree of a node contains only nodes with keys lesser than the node's key.
- The right subtree of a node contains only nodes with keys greater than the node's key.
- The left and right subtree each must also be a binary search tree

### Algorithms:

#### Create and Insert:

- ① Accept a random order of numbers from the user. The first no. would be inserted at the root node.
- ② Thereafter, every no. is compared with the root node. If less than or equal to the data in the root node, proceed left of the BST, else proceed right.
- ③ Perform this till you reach a null pointer, the place where the present data is to be inserted
- ④ Allocate a new node and assign the data in this node and allocate pointers appropriately.



### Height of BST:

- ① This algorithm is based on the idea of storing the nodes of every level of the BST in a dynamic queue (link list). It is also simultaneously useful to print the tree level wise. The total no. of levels accessed would be the height of the tree.
- ② Initialize the contents of the list with the root of the BST. The counter no.-of-nodes-in-current-level = 1 and the level-accessed = 1.
- ③ Access no.-of-nodes-in-current-level from the link list and add all their children to the list at the end and simultaneously keep track of the no. of nodes accessed in the next level in a variable which at the end is assigned back to no.-of-nodes-in-current-level. Also increment level-accessed, indicating one more level accessed in the BST.
- ④ Continue step 3 repeatedly till no.-of-nodes-in-current-level is 0, which means no more nodes in the next level. The value stored in the variable level-accessed is the height of the BST.

### Leaf Nodes of BST:

- ① There are many algorithms to find the leaf nodes of an BST. The one considered here is based on the idea that one could do a simple inorder traversal of the BST & just before printing the data as one normally does in an inorder traversal, check if both the left and right nodes are NULL. If so, it means the node under consideration is a leaf node and must be printed.
- ② Inorder: The recursive function will receive the root of the tree (or subtree) from where inorder traversal is to be initiated. Algorithm is to process left, which in this case is to call the same function with the left child of the node, print the data if both left & right pointers are NULL & then process right, which in this case is to call the same function with the right child of the root node.
- ③ Thus all the leaf nodes of the BST are printed



## Mirror of Tree:

1. Following is a algorithm of a recursive function to find mirror of the tree. The function `mirror-tree` accepts a pointer to a tree as the parameter. Initially the root node is passed later the roots of the subsequent subtrees are passed as the parameters.
2. The function begins by checking if the pointer passed is not NULL. If not, allocated a new node. Assigns the data of the original node to the copied node. Assigns the left child of the new node by calling the function `mirror-Tree` with the right child of the original node & assigns the right child of the new node by calling the function `mirror-Tree` with the left child of the original node. If the pointer passed is NULL, NULL is returned by the function else the new node created is returned.

## Level wise printing:

1. This algorithm is based on the idea of storing the nodes of every level of the BST in a dynamic queue (link list).
2. Initialize the contents of the list with the root of the BST. The counter `no-of-nodes-in-current-level = 1` and the `level-accessed = 1`
3. Access `no-of-nodes-in-current-level` from the link list. Print the level Number and all the data of all the nodes of the current level. Simultaneously add all their children to the list at the end and keep track of the no. of nodes accessed in the next level in a variable which at the end is assigned back to `no-of-nodes-in-current-level`. Also increment `level-accessed`, indicating one more level accessed in the BST
4. Continue step 3 repeatedly till `no-of-nodes-in-current-level` is 0, which means no more nodes in the next level.

## Test conditions:

Simple input of random no. Display the height of the tree & the leaf nodes. The BST entered could be drawn on the rough page and one could check if the height calculated and the leaf nodes printed are correct.



For eg. Enter : 34, 12, 56, 6, 14, 40, 70.

The height of the BST is 3

The leaf nodes are 6, 14, 40 & 70.

For Mirror Image:

Enter : 34, 12, 56, 6, 14, 40, 70

Level wise printed of original tree.

Level 1 : 34

Level 2 : 12, 56

Level 3 : 6, 14, 40, 70

Level wise printed of the mirror tree

level 1 : 34

level 2 : 56, 12

level 3 : 70, 40, 14, 6

Input :

Enter data (no.) to be stored in the binary search tree. Every node in the BST would contain 3 fields:

data, left child pointer and right child pointer.

Output:

The height of the tree and the list of its leaf nodes.

The original & mirror image printed levelwise