schwz

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Main Page

This is the main page for the Schwarz library pdf documentation. The repository is hosted on github. Documentation on aspects such as the build system, can be found at the # Installation Instructions page.

Modules

The structure of the Schwarz Library code is divided into different ${\tt modules}$:

- Initialization: Handles the initialization of the problem and the solver.
- Communicate: Handles the communication.
- Solve: Handles the local solution and the convergence detection.
- Schwarz Class: The Classes related to the Schwarz solvers.
- Utils: Provides some basic utilities.

2 Main Page

Installation Instructions

Building

Use the standard cmake build procedure:

```
mkdir build; cd build
cmake -G "Unix Makefiles" [OPTIONS] .. && make
```

Replace [OPTIONS] with desired cmake options for your build. The library adds the following additional switches to control what is being built:

- -DSCHWARZ_BUILD_BENCHMARKING={ON, OFF} Builds some example benchmarks. Default is ON
- -DSCHWARZ_BUILD_METIS={ON, OFF} Builds with support for the METIS partitioner. User needs to provide the path to the installation of the METIS library in METIS_DIR, preferably as an environment variable. Default is OFF
- -DSCHWARZ_BUILD_CHOLMOD={ON, OFF} Builds with support for the CHOLMOD module from the Suitesparse library. User needs to set an environment variable CHOLMOD_DIR to the path containing the CHOLMOD installation. Default is OFF
- -DSCHWARZ_BUILD_CUDA={ON, OFF} Builds with CUDA support. Though Ginkgo provides most of the required CUDA support, we do need to link to CUDA for explicit setting of GPU affinities, some custom gather and scatter operations. Default is OFF.
- -DSCHWARZ_BUILD_CLANG_TIDY={ON, OFF} Builds with support for clang-tidy Default is OFF
- -DSCHWARZ_BUILD_DEALII={ON, OFF} Builds with support for the finite element library deal.ii
 Default is OFF
- -DSCHWARZ_WITH_HWLOC={ON, OFF} Builds with support for the hardware locality library used for binding hardware. hwloc is distributed as a part of the Open-MPI project. Default is ON
- -DSCHWARZ_DEVEL_TOOLS={ON, OFF} Builds with some developer tools support. Default is ON. In particular uses git-cmake-format to automatically format the source files with clang-format.

Tips

- If you are having CUDA problems and you are not using CUDA, then feel free to switch the CUDA module off with -DSCHWARZ_BUILD_CUDA=off.
- Installing CHOLMOD can be a bit annoying. TODO add some details on fixing Suitesparse compilation.
- When doing merge commits it is possible that make format does not work. You can run cmake -DSCH ← WARZ_DEVEL_TOOLS=OFF . . to temporarily switch off the formatting. Please switch it on again when committing normally.

Testing Instructions

6 Testing Instructions

Benchmarking.

The flag -DSCHWARZ_BUILD_BENCHMARKING (default ON) enables the examples and benchmarking snippets.

If schwarz-lib has been built with deal.ii, then the deal.ii examples, ex_6 and ex_9 are also built, else only the $bench_ras$ example is built. The following command line options are available for this example. This is setup using gflags.

The executable is run in the following fashion:

```
[MPI_COMMAND] [MPI_OPTIONS] PATH_TO_EXECUTABLE [FLAGS]
```

Where FLAGS are the options below with the template flag_name [type] [default_value]. For example, to set the number of iterations of the RAS solver to 100 one would add $--num_iters=100$ to the executable command above.

Generic settings

- executor [std::string][reference]: The executor used to run the solver, one of reference, cuda or omp.
- explicit_laplacian [bool][false]: Use the explicit laplacian instead of deal.ii's matrix.
- set_1d_laplacian_size[uint32][16]: The number of grid points in one dimension for the 2D laplacian problem.
- enable_random_rhs [bool][false]: Use a random rhs instead of the default 1.0's.
- overlap [uint32][2]: Overlap between the domains.
- timings_file [std::string][null] : The filename for the timings.
- partition [std::string][regular] : The partitioner used. The choices are metis, regular or regular2d.
- metis_objtype [std::string][null]: The objective type to minimize for the metis partitioner. The choices are edgecut and totalvol.
- num_threads [uint32][1]: Number of threads to bind to a process.
- non_symmetric_matrix [bool][false] : Explicitly state that the matrix is non-symmetric so that the local GMRES solver is used.
- $\hbox{-} \verb| use_mixed_precision| [bool][false]: Use \verb| mixed| precision| in the communication.$

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Input settings

• matrix_filename [std::string][null]: The matrix file to read the global system matrix from.

Output settings

- enable_debug_write [bool][false]: Enable some debugging outputs to stdout.
- write_comm_data [bool][false]: Write the number of sends and recvs of each subdomain to files.
- write_perm_data [bool][false]: Write the permutation data from CHOLMOD to a file.
- print_config [bool][true] : Print the configuration of the run.
- print_matrices [bool][false] : Print the local system matrices to a file.
- debug [bool][false] : Enable some possible expensive debug checks.
- enable_logging [bool][false]: Enable some possible expensive logging from Ginkgo.

Solver settings

Generic settings

- num_iters [uint32][100]: The number of outer iterations for the RAS solver.
- set_tol [double][1e-6]: The Outer tolerance for the RAS solver.
- local_tol [double][1e-12]: The Inner tolerance for the local iterative solver.

Communication settings

- enable_onesided [bool][false]: Enable the onesided asynchronous communication.
- enable twosided [bool][true]: Enable the twosided asynchronous communication. A dummy flag.
- enable_one_by_one [bool][false]: Enable putting/getting of each element in onesided communication.
- enable_put_all_local_residual_norms [bool][false]: Enable putting of all local residual norms"
- enable_comm_overlap [bool][false]: Enable overlap of communication and computation.
- flush_type [std::string][flush-all]: The window flush strategy. The choices are flush-local and flush-all.
- lock_type [std::string][lock-all]: The window lock strategy. The choices are lock-local and lock-all.
- remote_comm_type [std::string][get]: The type of the remote communication. get uses MPI_Get and put uses MPI_Put.

Convergence settings

- enable_global_check [bool][false] : Use the global convergence check for twosided.
- global_convergence_type [std::string][centralized-tree] : Choose the convergence detection algorithm for onesided.
- enable_decentralized_accumulate [bool][false] : Use accumulate strategy for decentralized convergence check..
- enable_global_check_iter_offset [bool][false] : Enable global convergence check only after a certain number of iterations.

Local solver settings

- local_solver [std::string][iterative-ginkgo] : The local solver used in the local domains. The current choices are direct-cholmod, direct-ginkgo or iterative-ginkgo.
- local_factorization [std::string][cholmod] : The factorization for the local direct solver "cholmod" or "umfpack".
- local_reordering [std::string][none] : The reordering for the local direct solver "none", "metis_← reordering" or "rcm_reordering".
- factor_ordering_natural [bool][false]: If true uses natural ordering instead of the default optimized ordering. This is needed for CUDA runs as the factorization ordering needs to be given to the solver.
- enable_local_precond [bool][false]: If true uses the Block jacobi preconditioning for the local iterative solver.
- precond_max_block_size [uint32][16]: Maximum size of the blocks for the block jacobi preconditioner
- shifted_iter [uint32][1]: The number of iterations to communicate for the local subdomains.
- local_max_iters [int32][-1]: The maximum number of iterations for the local iterative solver.
- restart_iter [uint32][1]: The restart iter for the GMRES solver.
- reset_local_crit_iter [int32][-1]: The RAS iteration to reset the local iteration count.

Poisson solver using Restricted Additive Schwarz with overlap.

This example runs is written within the benchmarking/bench_ras.cpp file. This demonstrates the basic capabilities of schwarz-lib. You can use it to solve the 2D Poisson equation with a 5 point stencil or solve a generic matrix by providing it a matrix file.

Examples with deal.ii

These examples use deal.ii's capabilities to generate a matrix and solution is computed with the RAS method.

Possible settings are:

- num_refine_cycles [uint32][1][disabled]: The number of refinement cycles when used with deal.ii.
- init_refine_level [uint32][4]: The initial refinement level of the problem. This sets the initial number of dof's.
- $\bullet \ \, \text{dealii_orig} \ [\text{bool}] [\text{false}] : \textbf{Solve with the deal.ii iterative CG instead of the RAS solver}.$
- vis_sol [bool][false] : Print the solution for visualization.

Solving the n-dimensional Poisson equation with FEM.

The benchmarking/dealii_ex_6.cpp demonstrates the solution of the Poisson equation with adaptive refinement as explained on the deal.ii example documentation page

Solving the Advection equation with FEM.

The benchmarking/dealii_ex_9.cpp demonstrates the solution of the Advection equation with adaptive refinement as explained on the deal.ii example documentation page

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Module Documentation

5.1 Communicate

A module dedicated to the Communication interface in schwarz-lib.

Namespaces

• schwz::CommHelpers

The CommHelper namespace .

ProcessTopology

The ProcessTopology namespace.

Classes

class schwz::Communicate< ValueType, IndexType, MixedValueType >

The communication class that provides the methods for the communication between the subdomains.

struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

5.1.1 Detailed Description

A module dedicated to the Communication interface in schwarz-lib.

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5.2 Initialization

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

Namespaces

schwz::PartitionTools

The PartitionTools namespace.

ProcessTopology

The ProcessTopology namespace .

Classes

· class schwz::device_guard

This class defines a device guard for the cuda functions and the cuda module.

class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

struct schwz::Settings

The struct that contains the solver settings and the parameters to be set by the user.

- struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

5.2.1 Detailed Description

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

5.3 Schwarz Class

5.3 Schwarz Class

A module dedicated to the Schwarz solver classes in schwarz-lib.

Classes

- class schwz::SolverRAS< ValueType, IndexType, MixedValueType >
 An implementation of the solver interface using the RAS solver.
- $\bullet \ \, {\sf class} \ \, {\sf schwz::SchwarzBase} < \ \, {\sf ValueType}, \ \, {\sf IndexType}, \ \, {\sf MixedValueType} > \\$

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

5.3.1 Detailed Description

A module dedicated to the Schwarz solver classes in schwarz-lib.

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5.4 Solve

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

Namespaces

• schwz::conv_tools

The conv_tools namespace .

• schwz::SolverTools

The SolverTools namespace .

Classes

struct schwz::Metadata < ValueType, IndexType >

The solver metadata struct.

class schwz::Solve < ValueType, IndexType, MixedValueType >

The Solver class the provides the solver and the convergence checking methods.

5.4.1 Detailed Description

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

5.5 Utils 15

5.5 Utils

A module dedicated to the utilities in schwarz-lib.

Classes

 $\bullet \ \, {\sf struct\ schwz::} {\sf Utils} {< \ } {\sf ValueType,\ IndexType} >$

The utilities class which provides some checks and basic utilities.

5.5.1 Detailed Description

A module dedicated to the utilities in schwarz-lib.

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Namespace Documentation

6.1 ProcessTopology Namespace Reference

The ProcessTopology namespace.

6.1.1 Detailed Description

The ProcessTopology namespace.

proc_topo

6.2 schwz Namespace Reference

The Schwarz wrappers namespace.

Namespaces

• CommHelpers

The CommHelper namespace .

• conv_tools

The conv_tools namespace.

PartitionTools

The PartitionTools namespace.

SolverTools

The SolverTools namespace .

Classes

· class Communicate

The communication class that provides the methods for the communication between the subdomains.

· class device_guard

This class defines a device guard for the cuda functions and the cuda module.

class Initialize

The initialization class that provides methods for initialization of the solver.

struct Metadata

The solver metadata struct.

· class SchwarzBase

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

struct Settings

The struct that contains the solver settings and the parameters to be set by the user.

· class Solve

The Solver class the provides the solver and the convergence checking methods.

class SolverRAS

An implementation of the solver interface using the RAS solver.

struct Utils

The utilities class which provides some checks and basic utilities.

6.2.1 Detailed Description

The Schwarz wrappers namespace.

6.3 schwz::CommHelpers Namespace Reference

The CommHelper namespace .

6.3.1 Detailed Description

The CommHelper namespace.

comm_helpers

6.4 schwz::conv_tools Namespace Reference

The conv_tools namespace.

6.4.1 Detailed Description

The conv_tools namespace.

conv_tools

6.5 schwz::PartitionTools Namespace Reference

The PartitionTools namespace.

6.5.1 Detailed Description

The PartitionTools namespace.

part_tools

6.6 schwz::SolverTools Namespace Reference

The SolverTools namespace.

6.6.1 Detailed Description

The SolverTools namespace.

solver_tools

Class Documentation

7.1 BadDimension Class Reference

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

```
#include <exception.hpp>
```

Public Member Functions

BadDimension (const std::string &file, int line, const std::string &func, const std::string &op_name, std::size
 _t op_num_rows, std::size_t op_num_cols, const std::string &clarification)
 Initializes a bad dimension error.

7.1.1 Detailed Description

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

7.1.2 Constructor & Destructor Documentation

7.1.2.1 BadDimension()

Initializes a bad dimension error.

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Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
op_name	The name of the operator
op_num_rows	The row dimension of the operator
op_num_cols	The column dimension of the operator
clarification	An additional message further describing the error

The documentation for this class was generated from the following file:

exception.hpp (35a1195)

7.2 schwz::Settings::comm_settings Struct Reference

The settings for the various available communication paradigms.

```
#include <settings.hpp>
```

Public Attributes

• bool enable_onesided = false

Enable one-sided communication.

• bool enable_overlap = false

Enable explicit overlap between communication and computation.

• bool enable_put = false

Put the data to the window using MPI_Put rather than get.

• bool enable_get = true

Get the data to the window using MPI_Get rather than put.

bool stage_through_host = false

Stage the MPI transfers through the host.

• bool enable one by one = false

Push each element separately directly into the buffer.

bool enable_flush_local = false

Use local flush.

• bool enable_flush_all = true

Use flush all.

bool enable_lock_local = false

Use local locks.

• bool enable_lock_all = true

Use lock all.

7.2.1 Detailed Description

The settings for the various available communication paradigms.

The documentation for this struct was generated from the following file:

• settings.hpp (d458d06)

The communication struct used to store the communication data.

```
#include <communicate.hpp>
```

Public Attributes

· int num_neighbors_in

The number of neighbors this subdomain has to receive data from.

· int num_neighbors_out

The number of neighbors this subdomain has to send data to.

std::shared_ptr< gko::Array< IndexType > > neighbors_in

The neighbors this subdomain has to receive data from.

 $\bullet \quad \mathsf{std} :: \mathsf{shared_ptr} < \mathsf{gko} :: \mathsf{Array} < \mathsf{IndexType} > > \mathsf{neighbors_out}$

The neighbors this subdomain has to send data to.

std::vector< bool > is_local_neighbor

The bool vector which is true if the neighbors of a subdomain are in one node.

• int local_num_neighbors_in

The number of neighbors this subdomain has to receive data from.

· int local_num_neighbors_out

The number of neighbors this subdomain has to send data to.

std::shared_ptr< gko::Array< IndexType > > local_neighbors_in

The neighbors this subdomain has to receive data from.

std::shared_ptr< gko::Array< IndexType > > local_neighbors_out

The neighbors this subdomain has to send data to.

std::shared_ptr< gko::Array< IndexType * > > global_put

The array containing the number of elements that each subdomain sends from the other.

std::shared ptr< gko::Array< IndexType * > > local put

The array containing the number of elements that each subdomain sends from the other.

std::shared_ptr< gko::Array< IndexType * > > global_get

The array containing the number of elements that each subdomain gets from the other.

std::shared ptr< gko::Array< IndexType * > > local get

The array containing the number of elements that each subdomain gets from the other.

std::vector< IndexType > send

The number of elements being sent to each subdomain.

std::vector< IndexType > recv

The number of elements being sent to each subdomain.

 $\bullet \quad \mathsf{std} :: \mathsf{shared_ptr} < \mathsf{gko} :: \mathsf{Array} < \mathsf{IndexType} > > \mathsf{window_ids} \\$

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The RDMA window ids.

std::shared ptr< gko::Array< IndexType > > windows from

The RDMA window ids to receive data from.

std::shared_ptr< gko::Array< IndexType > > windows_to

The RDMA window ids to send data to.

std::shared ptr< gko::Array< MPI Request >> put request

The put request array.

std::shared_ptr< gko::Array< MPI_Request >> get_request

The get request array.

std::shared ptr< gko::matrix::Dense< ValueType >> send buffer

The send buffer used for the actual communication for both one-sided and two-sided (always allocated).

std::shared ptr< gko::matrix::Dense< MixedValueType > > mixedt send buffer

The mixed send buffer used for the actual communication for both one-sided and two-sided.

std::shared_ptr< gko::matrix::Dense< ValueType >> recv_buffer

The recv buffer used for the actual communication for both one-sided and two-sided (always allocated).

std::shared_ptr< gko::matrix::Dense< MixedValueType >> mixedt_recv_buffer

The mixed precision recv buffer used for the actual communication for both one-sided and two-sided.

std::shared_ptr< gko::Array< IndexType > > get_displacements

The displacements for the receiving of the buffer.

std::shared ptr< gko::Array< IndexType > > put displacements

The displacements for the sending of the buffer.

· MPI Win window recv buffer

The RDMA window for the recv buffer.

MPI_Win window_send_buffer

The RDMA window for the send buffer.

MPI_Win window_x

The RDMA window for the solution vector.

7.3.1 Detailed Description

template < typename ValueType, typename IndexType, typename MixedValueType > struct schwz::Communicate < ValueType, IndexType, MixedValueType >::comm_struct

The communication struct used to store the communication data.

7.3.2 Member Data Documentation

7.3.2.1 global_get

```
template<typename ValueType , typename IndexType , typename MixedValueType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType, Mixed↔
ValueType >::comm_struct::global_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global_get[p][0] contains the overall number of elements to be received to subdomain p and global—put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize(), schwz::SolverRAS< ValueType, IndexType, MixedValueType, S::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType, MixedValueType >::setup_windows().

7.3.2.2 global_put

```
template<typename ValueType , typename IndexType , typename MixedValueType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType, Mixed
ValueType >::comm_struct::global_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global_put[p][0] contains the overall number of elements to be sent to subdomain p and global_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize(), schwz::SolverRAS< ValueType, IndexType, MixedValueType, IndexType, IndexType, IndexType, IndexType, MixedValueType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType, MixedValueType >::setup_windows().

7.3.2.3 is local neighbor

```
template<typename ValueType , typename IndexType , typename MixedValueType >
std::vector<bool> schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct←
::is_local_neighbor
```

The bool vector which is true if the neighbors of a subdomain are in one node.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize(), schwz::SolverRAS< ValueType, IndexType, MixedValueType, S::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType, MixedValueType >::setup_windows().

7.3.2.4 local_get

```
template<typename ValueType , typename IndexType , typename MixedValueType >
std::shared_ptr<gko::Array<IndexType *> > schwz::Communicate< ValueType, IndexType, Mixed↔
ValueType >::comm_struct::local_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global_get[p][0] contains the overall number of elements to be received to subdomain p and global—_put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize(), schwz::SolverRAS< ValueType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType, MixedValueType >::setup_windows().

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7.3.2.5 | local_put

```
template<typename ValueType , typename IndexType , typename MixedValueType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType, Mixed↔
ValueType >::comm_struct::local_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global_put[p][0] contains the overall number of elements to be sent to subdomain p and global_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize(), schwz::SolverRAS< ValueType, IndexType, MixedValueType, S::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType, MixedValueType >::setup_windows().

The documentation for this struct was generated from the following file:

communicate.hpp (d458d06)

7.4 schwz::Communicate < ValueType, IndexType, MixedValueType > Class Template Reference

The communication class that provides the methods for the communication between the subdomains.

```
#include <communicate.hpp>
```

Classes

struct comm struct

The communication struct used to store the communication data.

Public Member Functions

virtual void setup comm buffers ()=0

Sets up the communication buffers needed for the boundary exchange.

virtual void setup_windows (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared_ptr < gko::matrix::Dense < ValueType >> &main_buffer)=0

Sets up the windows needed for the asynchronous communication.

virtual void exchange_boundary (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense < ValueType >> &global_solution)=0

Exchanges the elements of the solution vector.

void local_to_global_vector (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, const std::shared_ptr < gko::matrix::Dense < ValueType >> &local_vector, std::shared_ptr < gko::matrix::
 Dense < ValueType >> &global_vector)

Transforms data from a local vector to a global vector.

virtual void update_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_solution, const std::shared_ptr< gko::matrix::Dense< ValueType >> &local_rhs, const std::shared_ptr< gko::matrix::Dense< ValueType >> &global_solution, const std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &interface_matrix)=0

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

void clear (Settings &settings)

Clears the data.

7.4.1 Detailed Description

 $template < typename\ ValueType,\ typename\ IndexType,\ typename\ MixedValueType > \\ class\ schwz:: Communicate < ValueType,\ IndexType,\ MixedValueType > \\$

The communication class that provides the methods for the communication between the subdomains.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Communicate

7.4.2 Member Function Documentation

7.4.2.1 exchange_boundary()

Exchanges the elements of the solution vector.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_solution	The solution vector being exchanged between the subdomains.

Implemented in schwz::SolverRAS< ValueType, IndexType, MixedValueType >.

 $Referenced \ by \ schwz:: Schwarz Base < Value Type, \ Index Type, \ Mixed Value Type > :: run().$

7.4.2.2 local_to_global_vector()

Transforms data from a local vector to a global vector.

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Parameters

settings	The settings struct.
metadata	The metadata struct.
local_vector	The local vector in question.
global_vector	The global vector in question.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::run().

```
69 {
70
       using vec = gko::matrix::Dense<ValueType>;
71
       auto alpha = gko::initialize<gko::matrix::Dense<ValueType>>(
72
            {1.0}, settings.executor);
73
       auto temp_vector = vec::create(
74
           settings.executor, gko::dim<2>(metadata.local_size, 1),
75
           gko::Array<ValueType>::view(
76
                settings.executor, metadata.local_size,
77
                &global_vector->get_values()[metadata.first_row
78
                                                    ->get_data()[metadata.my_rank]]),
79
           1);
80
       auto temp_vector2 = vec::create(
81
           settings.executor, gko::dim<2>(metadata.local_size, 1),
           gko::Array<ValueType>::view(settings.executor, metadata.local_size,
84
                                          local_vector->get_values()),
85
           1);
       if (settings.convergence_settings.convergence_crit ==
86
           Settings::convergence_settings::local_convergence_crit::
88
               residual_based) {
           local_vector->add_scaled(alpha.get(), temp_vector.get());
temp_vector->add_scaled(alpha.get(), local_vector.get());
90
91
       } else {
92
           temp_vector->copy_from(temp_vector2.get());
93
94 }
```

7.4.2.3 setup_windows()

Sets up the windows needed for the asynchronous communication.

Parameters

settings	The settings struct.
metadata	The metadata struct.
main_buffer	The main buffer being exchanged between the subdomains.

Implemented in schwz::SolverRAS< ValueType, IndexType, MixedValueType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::run().

7.4.2.4 update_boundary()

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_solution	The local solution vector in the subdomain.
local_rhs	The local right hand side vector in the subdomain.
global_solution	The workspace solution vector.
global_old_solution	The global solution vector of the previous iteration.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.

Implemented in schwz::SolverRAS< ValueType, IndexType, MixedValueType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::run().

The documentation for this class was generated from the following files:

- communicate.hpp (d458d06)
- /home/runner/work/schwarz-lib/schwarz-lib/source/communicate.cpp (d458d06)

7.5 schwz::Settings::convergence_settings Struct Reference

The various convergence settings available.

```
#include <settings.hpp>
```

7.5.1 Detailed Description

The various convergence settings available.

The documentation for this struct was generated from the following file:

• settings.hpp (d458d06)

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7.6 CudaError Class Reference

CudaError is thrown when a CUDA routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

CudaError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a CUDA error.

7.6.1 Detailed Description

CudaError is thrown when a CUDA routine throws a non-zero error code.

7.6.2 Constructor & Destructor Documentation

7.6.2.1 CudaError()

Initializes a CUDA error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the CUDA routine that failed
error_code	The resulting CUDA error code

```
137 : Error(file, line, func + ": " + get_error(error_code))
138      {}
```

The documentation for this class was generated from the following files:

- exception.hpp (35a1195)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (35a1195)

7.7 CusparseError Class Reference

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

• CusparseError (const std::string &file, int line, const std::string &func, int error_code)

Initializes a cuSPARSE error.

7.7.1 Detailed Description

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

7.7.2 Constructor & Destructor Documentation

7.7.2.1 CusparseError()

Initializes a cuSPARSE error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuSPARSE routine that failed
error_code	The resulting cuSPARSE error code

```
159 : Error(file, line, func + ": " + get_error(error_code))
160 {}
```

The documentation for this class was generated from the following files:

- exception.hpp (35a1195)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (35a1195)

7.8 schwz::device_guard Class Reference

This class defines a device guard for the cuda functions and the cuda module.

```
#include <device_guard.hpp>
```

7.8.1 Detailed Description

This class defines a device guard for the cuda functions and the cuda module.

The guard is used to make sure that the device code is run on the correct cuda device, when run with multiple devices. The class records the current device id and uses <code>cudaSetDevice</code> to set the device id to the one being passed in. After the scope has been exited, the destructor sets the device_id back to the one before entering the scope.

The documentation for this class was generated from the following file:

device_guard.hpp (5a15602)

7.9 schwz::Initialize < ValueType, IndexType > Class Template Reference

The initialization class that provides methods for initialization of the solver.

```
#include <initialization.hpp>
```

Public Member Functions

void generate_rhs (std::vector< ValueType > &rhs)

Generates the right hand side vector.

void setup_global_matrix (const std::string &filename, const gko::size_type &oned_laplacian_size, std
 ::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &global_matrix)

Generates the 2D global laplacian matrix.

The partitioning function.

void setup_vectors (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std
 ::vector< ValueType > &rhs, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_rhs, std::shared
 _ptr< gko::matrix::Dense< ValueType >> &global_rhs, std::shared_ptr< gko::matrix::Dense< ValueType
 >> &local_solution)

Setup the vectors with default values and allocate mameory if not allocated.

virtual void setup_local_matrices (Settings &settings, Metadata< ValueType, IndexType > &metadata, std
 ::vector< unsigned int > &partition_indices, std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >>
 &global_matrix, std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &local_matrix, std::shared
 _ptr< gko::matrix::Csr< ValueType, IndexType >> &interface_matrix)=0

Sets up the local and the interface matrices from the global matrix and the partition indices.

Public Attributes

- std::vector< unsigned int > partition_indices
 - The partition indices containing the subdomains to which each row(vertex) of the matrix(graph) belongs to.
- std::vector< unsigned int > cell_weights

The cell weights for the partition algorithm.

Additional Inherited Members

7.9.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Initialization

7.9.2 Member Function Documentation

7.9.2.1 generate_rhs()

Generates the right hand side vector.

Parameters

```
rhs The rhs vector.
```

References schwz::Initialize < ValueType, IndexType >::setup_global_matrix().

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

```
90 {
91     std::uniform_real_distribution<double> unif(0.0, 1.0);
92     std::default_random_engine engine;
93     for (gko::size_type i = 0; i < rhs.size(); ++i) {
94         rhs[i] = unif(engine);
95     }
96 }</pre>
```

7.9.2.2 partition()

The partitioning function.

Allows the partition of the global matrix depending with METIS and a regular 1D decomposition.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_matrix	The global matrix.
partition_indices	The partition indices [OUTPUT].

References schwz::Metadata < ValueType, IndexType >::global_size, schwz::Metadata < ValueType, IndexType >::mum_subdomains, and schwz::Settings::write_debug_ \leftarrow out.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

```
284 {
285
        partition_indices.resize(metadata.global_size);
286
        if (metadata.my_rank == 0) {
            auto partition_settings =
287
                 (Settings::partition_settings::partition_zoltan |
288
289
                  Settings::partition_settings::partition_metis |
290
                  Settings::partition_settings::partition_regular
291
                  Settings::partition_settings::partition_regular2d
292
                  Settings::partition_settings::partition_custom) &
293
                 settings.partition;
294
295
            if (partition_settings ==
296
                 Settings::partition_settings::partition_zoltan) {
297
                 SCHWARZ_NOT_IMPLEMENTED;
298
             } else if (partition_settings ==
                 Settings::partition_settings::partition_metis) {
if (metadata.my_rank == 0) {
299
300
                     std::cout << " METIS partition" << std::endl;
301
302
303
                 PartitionTools::PartitionMetis(
304
                     settings, global_matrix, this->cell_weights,
305
                     metadata.num_subdomains, partition_indices);
306
             } else if (partition_settings =
307
                        Settings::partition_settings::partition_regular) {
308
                 if (metadata.my_rank == 0)
309
                     std::cout << " Regular 1D partition" << std::endl;</pre>
310
311
                 PartitionTools::PartitionRegular(
312
                     global_matrix, metadata.num_subdomains, partition_indices);
313
             } else if (partition_settings ==
314
                        Settings::partition_settings::partition_regular2d) {
                 if (metadata.my_rank == 0) {
   std::cout << " Regular 2D partition" << std::endl;</pre>
315
316
317
318
                 PartitionTools::PartitionRegular2D(
319
                     global_matrix, settings.write_debug_out,
                     metadata.num_subdomains, partition_indices);
```

7.9.2.3 setup global matrix()

Generates the 2D global laplacian matrix.

Parameters

oned_laplacian_size	The size of the one d laplacian grid.
global_matrix	The global matrix.

Referenced by schwz::Initialize< ValueType, IndexType >::generate_rhs(), and schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

```
200 {
        using index_type = IndexType;
201
202
        using value_type = ValueType;
        using mtx = gko::matrix::Csr<value_type, index_type>;
if (settings.matrix_filename != "null") {
203
204
             auto input_file = std::ifstream(filename, std::ios::in);
205
             if (!input_file) {
206
207
                 std::cerr << "Could not find the file \"" << filename
208
                            << "\", which is required for this test.\n";
209
210
             global_matrix =
211
                gko::read<mtx>(input_file, settings.executor->get_master());
212
             global_matrix->sort_by_column_index();
             std::cout << "Matrix from file " << filename << std::endl;
213
        } else if (settings.matrix_filename == "null" &&
             settings.explicit_laplacian) {
std::cout << "Laplacian 2D Matrix (generated in house) " << std::endl;</pre>
215
216
217
             gko::size_type global_size = oned_laplacian_size *
      oned_laplacian_size;
218
219
             global_matrix = mtx::create(settings.executor->get_master(),
220
                                           gko::dim<2>(global_size), 5 * global_size);
             value_type *values = global_matrix->get_values();
221
222
             index_type *row_ptrs = global_matrix->get_row_ptrs();
223
            index_type *col_idxs = global_matrix->get_col_idxs();
224
225
             std::vector<gko::size_type> exclusion_set;
226
227
             std::map<IndexType, ValueType> stencil_map = {
                 {-oned_laplacian_size, -1}, {-1, -1}, {0, 4}, {1, -1}, {oned_laplacian_size, -1},
228
229
230
             for (auto i = 2; i < global_size; ++i) {</pre>
231
232
                 gko::size_type index = (i - 1) * oned_laplacian_size;
233
                  if (index * index < global_size * global_size) {</pre>
234
                      exclusion_set.push_back(
235
                          linearize_index(index, index - 1, global_size));
236
                     exclusion_set.push_back(
                          linearize_index(index - 1, index, global_size));
```

```
238
                }
239
240
241
            std::sort(exclusion_set.begin(),
2.42
                       exclusion_set.begin() + exclusion_set.size());
243
            IndexType pos = 0;
245
            IndexType col_idx = 0;
246
            row_ptrs[0] = pos;
2.47
            gko::size_type cur_idx = 0;
            for (IndexType i = 0; i < global_size; ++i) {
    for (auto ofs : stencil_map) {</pre>
248
249
                    auto in_exclusion_flag :
250
251
                        (exclusion_set[cur_idx] ==
252
                          linearize_index(i, i + ofs.first, global_size));
253
                    if (0 <= i + ofs.first && i + ofs.first < global_size &&</pre>
254
                         !in_exclusion_flag) {
                         values[pos] = ofs.second;
col_idxs[pos] = i + ofs.first;
255
256
                         ++pos;
258
259
                     if (in_exclusion_flag) {
2.60
                         cur_idx++;
2.61
                    col_idx = row_ptrs[i + 1] - pos;
262
263
                row_ptrs[i + 1] = pos;
264
265
            }
266
        } else {
            267
268
269
                       << std::endl;
270
            std::exit(-1);
271
272 }
```

7.9.2.4 setup_local_matrices()

Sets up the local and the interface matrices from the global matrix and the partition indices.

Parameters

settings	The settings struct.
metadata	The metadata struct.
partition_indices	The array containing the partition indices.
global_matrix	The global system matrix.
local_matrix	The local system matrix.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.
local_perm	The local permutation, obtained through RCM or METIS.

Implemented in schwz::SolverRAS< ValueType, IndexType, MixedValueType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

7.9.2.5 setup_vectors()

Setup the vectors with default values and allocate mameory if not allocated.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_rhs	The local right hand side vector in the subdomain.
global_rhs	The global right hand side vector.
local_solution	The local solution vector in the subdomain.

References schwz::Settings::executor, schwz::Metadata< ValueType, IndexType >::first_row, schwz::Metadata< ValueType, IndexType >::my_rank.

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

```
339 {
340
       using vec = gko::matrix::Dense<ValueType>;
341
       auto my_rank = metadata.my_rank;
342
       auto first_row = metadata.first_row->get_data()[my_rank];
343
344
       // Copy the global rhs vector to the required executor.
345
       gko::Array<ValueType> temp_rhs{settings.executor->get_master(), rhs.begin(),
346
                                       rhs.end()};
       global_rhs = vec::create(settings.executor,
347
348
                                 gko::dim<2>{metadata.global_size, 1}, temp_rhs, 1);
349
350
       local_rhs =
351
           vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
       \ensuremath{//} Extract the local rhs from the global rhs. Also takes into account the
352
353
        // overlap.
354
       SolverTools::extract_local_vector(settings, metadata, local_rhs.get(),
                                          global_rhs.get(), first_row);
355
356
357
       local_solution =
358
            vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
359 }
```

The documentation for this class was generated from the following files:

- initialization.hpp (200bbde)
- /home/runner/work/schwarz-lib/schwarz-lib/source/initialization.cpp (92dbd95)

7.10 schwz::Metadata < ValueType, IndexType > Struct Template Reference

The solver metadata struct.

```
#include <settings.hpp>
```

Classes

· struct post_process_data

The struct used for storing data for post-processing.

Public Attributes

• MPI_Comm mpi_communicator

The MPI communicator.

• gko::size_type global_size = 0

The size of the global matrix.

• gko::size_type oned_laplacian_size = 0

The size of the 1 dimensional laplacian grid.

• gko::size_type local_size = 0

The size of the local subdomain matrix.

gko::size_type local_size_x = 0

The size of the local subdomain matrix + the overlap.

• gko::size_type local_size_o = 0

The size of the local subdomain matrix + the overlap.

• gko::size_type overlap_size = 0

The size of the overlap between the subdomains.

• gko::size_type num_subdomains = 1

The number of subdomains used within the solver.

· int my_rank

The rank of the subdomain.

int my_local_rank

The local rank of the subdomain.

int local_num_procs

The local number of procs in the subdomain.

· int comm size

The number of subdomains used within the solver, size of the communicator.

int num_threads

The number of threads used within the solver for each subdomain.

IndexType iter count

The iteration count of the solver.

ValueType tolerance

The tolerance of the complete solver.

ValueType local_solver_tolerance

The tolerance of the local solver in case of an iterative solve.

IndexType max_iters

The maximum iteration count of the Schwarz solver.

IndexType local_max_iters

The maximum iteration count of the local iterative solver.

IndexType updated_max_iters

The updated maximum iteration count of the local iterative solver.

· std::string local_precond

Local preconditioner.

unsigned int precond_max_block_size

The maximum block size for the preconditioner.

ValueType current_residual_norm = -1.0

The current residual norm of the subdomain.

ValueType min_residual_norm = -1.0

The minimum residual norm of the subdomain.

std::vector < std::tuple < int, int, std::string, std::vector < ValueType > > > time_struct

The struct used to measure the timings of each function within the solver loop.

• std::vector< std::tuple< int, std::vector< std::tuple< int, int >>, std::vector< std::tuple< int, int >>, int, int >> comm_data_struct

The struct used to measure the timings of each function within the solver loop.

std::shared_ptr< gko::Array< IndexType > > global_to_local

The mapping containing the global to local indices.

std::shared ptr< gko::Array< IndexType > > local to global

The mapping containing the local to global indices.

gko::Array< IndexType > overlap_row

The overlap row indices.

std::shared_ptr< gko::Array< IndexType > > first_row

The starting row of each subdomain in the matrix.

std::shared_ptr< gko::Array< IndexType >> permutation

The permutation used for the re-ordering.

std::shared_ptr< gko::Array< IndexType > > i_permutation

The inverse permutation used for the re-ordering.

7.10.1 Detailed Description

template<typename ValueType, typename IndexType>
struct schwz::Metadata< ValueType, IndexType>

The solver metadata struct.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.10.2 Member Data Documentation

7.10.2.1 local_solver_tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::local_solver_tolerance
```

The tolerance of the local solver in case of an iterative solve.

The residual norm reduction required.

7.10.2.2 tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::tolerance
```

The tolerance of the complete solver.

The residual norm reduction required.

The documentation for this struct was generated from the following file:

• settings.hpp (d458d06)

7.11 MetisError Class Reference

MetisError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

MetisError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a METIS error.

7.11.1 Detailed Description

MetisError is thrown when a METIS routine throws a non-zero error code.

7.11.2 Constructor & Destructor Documentation

7.11.2.1 MetisError()

Initializes a METIS error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the METIS routine that failed
error_code	The resulting METIS error code

```
182 : Error(file, line, func + ": " + get_error(error_code))
183      {}
```

The documentation for this class was generated from the following files:

- exception.hpp (35a1195)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (35a1195)

7.12 schwz::Metadata < ValueType, IndexType >::post_process_data Struct Reference

The struct used for storing data for post-processing.

```
#include <settings.hpp>
```

7.12.1 Detailed Description

```
template<typename ValueType, typename IndexType>
struct schwz::Metadata< ValueType, IndexType >::post_process_data
```

The struct used for storing data for post-processing.

The documentation for this struct was generated from the following file:

• settings.hpp (d458d06)

7.13 schwz::SchwarzBase< ValueType, IndexType, MixedValueType > Class Template Reference

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

```
#include <schwarz_base.hpp>
```

Public Member Functions

SchwarzBase (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

void initialize ()

Initialize the matrix and vectors.

void run (std::shared_ptr< gko::matrix::Dense< ValueType >> &solution)

The function that runs the actual solver and obtains the final solution.

void print_vector (const std::shared_ptr< gko::matrix::Dense< ValueType >> &vector, int subd, std::string name)

The auxiliary function that prints a passed in vector.

• void print_matrix (const std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &matrix, int rank, std::string name)

The auxiliary function that prints a passed in CSR matrix.

Public Attributes

• std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > local_matrix

std::shared_ptr< gko::matrix::Permutation< IndexType > > local_perm

The local subdomain permutation matrix/array.

std::shared_ptr< gko::matrix::Permutation< IndexType > > local_inv_perm

The local subdomain inverse permutation matrix/array.

• std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular_factor_I

The local lower triangular factor used for the triangular solves.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular_factor_u

The local upper triangular factor used for the triangular solves.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > interface_matrix

The local interface matrix.

The local subdomain matrix.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> global_matrix

The global matrix.

std::shared_ptr< gko::matrix::Dense< ValueType > > local_rhs

The local right hand side.

std::shared_ptr< gko::matrix::Dense< ValueType >> global_rhs

The global right hand side.

std::shared_ptr< gko::matrix::Dense< ValueType >> local_solution

The local solution vector.

std::shared ptr< gko::matrix::Dense< ValueType >> global solution

The global solution vector.

std::vector< ValueType > local_residual_vector_out

The global residual vector.

std::vector< std::vector< ValueType > > global_residual_vector_out

The local residual vector.

Additional Inherited Members

7.13.1 Detailed Description

 $template < typename\ ValueType = gko::default_precision,\ typename\ IndexType = gko::int32,\ typename\ MixedValueType = gko :::default_precision >$

class schwz::SchwarzBase< ValueType, IndexType, MixedValueType >

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

It derives from the Initialization class, the Communication class and the Solve class all of which are templated.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.13.2 Constructor & Destructor Documentation

7.13.2.1 SchwarzBase()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

Parameters

settings	The settings struct.
metadata	The metadata struct.

References schwz::Settings::cuda_device_guard, schwz::Settings::executor, schwz::Settings::executor_string, schwz::Metadata < ValueType, IndexType >::local_num_procs, schwz::Metadata < ValueType, IndexType >::mpi \leftarrow _communicator, schwz::Metadata < ValueType, IndexType >::my_local_rank, and schwz::Metadata < ValueType, IndexType >::my rank.

```
: Initialize<ValueType, IndexType>(settings, metadata),
76
77
         settings (settings),
78
         metadata (metadata)
79 {
80
       using vec_itype = gko::Array<IndexType>;
81
       metadata.my_local_rank =
           Utils<ValueType, IndexType>::get_local_rank(metadata.mpi_communicator);
82
83
       metadata.local_num_procs = Utils<ValueType, IndexType>::get_local_num_procs(
          metadata.mpi_communicator);
       auto my_local_rank = metadata.my_local_rank;
if (settings.executor_string == "omp") {
86
87
           settings.executor = gko::OmpExecutor::create();
88
           auto exec info =
               static_cast<gko::OmpExecutor *>(settings.executor.get())
89
                    ->get_exec_info();
91
           exec_info->bind_to_core(metadata.my_local_rank);
92
93
       } else if (settings.executor_string == "cuda") {
           int num_devices = 0;
94
95 #if SCHW_HAVE_CUDA
           SCHWARZ_ASSERT_NO_CUDA_ERRORS(cudaGetDeviceCount(&num_devices));
96
97 #else
98
           SCHWARZ_NOT_IMPLEMENTED;
99 #endif
100
            Utils<ValueType, IndexType>::assert_correct_cuda_devices(
101
                num_devices, metadata.my_rank);
            settings.executor = gko::CudaExecutor::create(
102
                my_local_rank, gko::OmpExecutor::create(), false);
103
104
            auto exec_info = static_cast<gko::OmpExecutor *>(
105
                                 settings.executor->get_master().get())
106
                                  ->get_exec_info();
107
            exec_info->bind_to_core(my_local_rank);
108
            settings.cuda_device_guard =
109
                std::make_shared<schwz::device_guard>(my_local_rank);
```

```
110
              std::cout << " Rank " << metadata.my_rank << " with local rank " << my_local_rank << " has " \,
111
112
                         << (static_cast<gko::CudaExecutor *>(settings.executor.get()))
113
             ->get_device_id()
<< " id of gpu" << std::endl;
MPI_Barrier(metadata.mpi_communicator);</pre>
114
115
116
117
        } else if (settings.executor_string == "reference") {
          settings.executor = gko::ReferenceExecutor::create();
118
119
             auto exec_info =
              static_cast<gko::ReferenceExecutor *>(settings.executor.get())
120
             ->get_exec_info();
exec_info->bind_to_core(my_local_rank);
121
122
123
124 }
```

7.13.3 Member Function Documentation

7.13.3.1 print matrix()

The auxiliary function that prints a passed in CSR matrix.

Parameters

matrix	The matrix to be printed.
subd	The subdomain on which the vector exists.
name	The name of the matrix as a string.

7.13.3.2 print_vector()

The auxiliary function that prints a passed in vector.

Parameters

vector	The vector to be printed.
subd	The subdomain on which the vector exists.
name	The name of the vector as a string.

7.13.3.3 run()

The function that runs the actual solver and obtains the final solution.

Parameters

```
solution The solution vector.
```

References schwz::Communicate< ValueType, IndexType, MixedValueType >::exchange_boundary(), schwz::

Settings::executor, schwz::Settings::executor_string, schwz::SchwarzBase< ValueType, IndexType, MixedValue

Type >::global_matrix, schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::global_rhs, schwz

::SchwarzBase< ValueType, IndexType, MixedValueType >::global_solution, schwz::SchwarzBase< ValueType, IndexType, Inde

```
325 {
326
       using vec_vtype = gko::matrix::Dense<ValueType>;
327
        if (!solution.get()) {
            solution =
328
329
                vec_vtype::create(settings.executor->get_master(),
                                  gko::dim<2>(this->metadata.global_size, 1));
330
331
        MixedValueType dummy1 = 0.0;
332
333
        ValueType dummy2 = 1.0;
334
        if (metadata.my_rank == 0) {
335
            336
337
338
339
        // The main solution vector
        std::shared_ptr<vec_vtype> global_solution = vec_vtype::create(
340
341
            this->settings.executor, gko::dim<2>(this->metadata.global_size, 1));
342
        // The main solution vector on the host
        std::shared_ptr<vec_vtype> host_global_solution;
343
344
        if (settings.comm settings.stage through host) {
345
            host_global_solution =
346
                vec_vtype::create(this->settings.executor->get_master(),
347
                                  gko::dim<2>(this->metadata.global_size, 1));
348
        // A work vector.
349
350
        std::shared ptr<vec vtype> work vector = vec vtype::create(
351
            settings.executor, gko::dim<2>(2 * this->metadata.local_size_x, 1));
352
        // An initial guess.
353
        std::shared_ptr<vec_vtype> init_guess = vec_vtype::create(
354
            settings.executor, gko::dim<2>(this->metadata.local_size_x, 1));
355
        // init_guess->copy_from(local_rhs.get());
356
        if (settings.executor_string == "omp") {
357
358
            ValueType sum_rhs = std::accumulate(
359
                local_rhs->get_values(),
            local_rhs->get_values() + local_rhs->get_size()[0], 0.0);
std::cout << " Rank " << this->metadata.my_rank << " sum local rhs "</pre>
360
361
                      << sum_rhs << std::endl;
362
       }
363
364
```

```
365
            // std::vector<IndexType> local_converged_iter_count;
366
367
             // Setup the windows for the onesided communication.
368
            this->setup_windows(this->settings, this->metadata, global_solution);
369
370
            const auto solver settings =
371
                    (Settings::local_solver_settings::direct_solver_cholmod |
372
                     Settings::local_solver_settings::direct_solver_umfpack |
373
                     Settings::local_solver_settings::direct_solver_ginkgo |
374
                     Settings::local_solver_settings::iterative_solver_dealii |
375
                     Settings::local_solver_settings::iterative_solver_ginkgo) &
376
                   settings.local solver:
377
            if (settings.comm_settings.stage_through_host) {
378
                   host_global_solution->copy_from(gko::lend(global_solution));
379
380
            \label{eq:ValueType local_residual_norm = -1.0, local_residual_norm0 = -
381
                            global_residual_norm = 0.0, global_residual_norm0 = -1.0;
382
383
            metadata.iter_count = 0;
             auto start_time = std::chrono::steady_clock::now();
384
385
            int num_converged_procs = 0;
386
387
             for (; metadata.iter_count < metadata.max_iters; ++(metadata.iter_count)) {</pre>
                   \ensuremath{//} Exchange the boundary values. The communication part.
388
389
                   if (settings.comm_settings.stage_through_host) {
                         host_global_solution->copy_from(gko::lend(global_solution));
// By staging through host just transfer the host_global_solution
390
391
392
                          // instead of on device global_solution
393
                         MEASURE_ELAPSED_FUNC_TIME(
394
                                \verb|this-> exchange_boundary| (settings, metadata,
395
                                                                       host_global_solution),
396
                                0, metadata.my_rank, boundary_exchange, metadata.iter_count);
397
                         global_solution->copy_from(gko::lend(host_global_solution));
398
                   } else {
399
                         MEASURE_ELAPSED_FUNC_TIME(
                                this->exchange_boundary(settings, metadata, global_solution), 0,
400
401
                                metadata.my_rank, boundary_exchange, metadata.iter_count);
402
                   }
403
404
                   // Update the boundary and interior values after the exchanging from
405
                    // other processes
                   MEASURE_ELAPSED_FUNC_TIME(
406
                         this->update_boundary(settings, metadata, this->
407
         local_solution,
408
                                                              this->local_rhs, global_solution,
409
                                                              this->interface_matrix),
410
                         1, metadata.my_rank, boundary_update, metadata.iter_count);
411
                   // Check for the convergence of the solver.
412
413
                   // num converged procs = 0;
414
                   MEASURE_ELAPSED_FUNC_TIME(
415
                          (Solve<ValueType, IndexType, MixedValueType>::check_convergence(
416
                                settings, metadata, this->comm_struct, this->convergence_vector,
417
                                global_solution, this->local_solution, this->
         local_matrix,
418
                                work vector, local residual norm, local residual norm0,
                                global_residual_norm, global_residual_norm0,
419
420
                                num_converged_procs)),
421
                         2, metadata.my_rank, convergence_check, metadata.iter_count);
422
423
                   // break if the solution diverges.
                   424
425
426
427
                         std::exit(-1);
428
                  }
429
                   // break if all processes detect that all other processes have
430
                   // converged otherwise continue iterations.
431
432
                   if (num_converged_procs == metadata.num_subdomains) {
433
                         break;
434
                   } else {
435
                         MEASURE_ELAPSED_FUNC_TIME(
                                (Solve<ValueType, IndexType, MixedValueType>::local_solve(
    settings, metadata, this->local_matrix,
436
437
                                       this->triangular_factor_1, this->
         triangular_factor_u,
439
                                       this->local_perm, this->local_inv_perm, work_vector,
440
                                       init_guess, this->local_solution))
                                3, metadata.my_rank, local_solve, metadata.iter_count);
441
442
443
                         // Gather the local vector into the locally global vector for
                          // communication.
444
445
                         MEASURE_ELAPSED_FUNC_TIME(
446
                                (Communicate<ValueType, IndexType, MixedValueType>::
447
                                        local_to_global_vector(settings, metadata,
448
                                                                              this->local solution.
```

```
global_solution)),
450
                      4, metadata.my_rank, expand_local_vec, metadata.iter_count);
451
             }
452
453
        MPI Barrier (MPI COMM WORLD);
454
        auto elapsed time = std::chrono::duration<ValueType>(
455
             std::chrono::steady_clock::now() - start_time);
456
         // Write the residuals and iterations to files
         if (settings.write_iters_and_residuals &&
457
             solver_settings ==
458
459
                 Settings::local_solver_settings::iterative_solver_ginkgo) {
             std::string rank_string = std::to_string(metadata.my_rank);
if (metadata.my_rank < 10) {
   rank_string = "0" + std::to_string(metadata.my_rank);</pre>
460
461
462
463
464
             std::string filename = "iter_res_" + rank_string + ".csv";
465
             write iters and residuals (
                  metadata.num_subdomains, metadata.my_rank,
466
467
                  metadata.post_process_data.local_residual_vector_out.size(),
468
                  metadata.post_process_data.local_residual_vector_out,
469
                  metadata.post_process_data.local_converged_iter_count,
470
                  metadata.post_process_data.local_converged_resnorm,
471
                  metadata.post_process_data.local_timestamp, filename);
472
473
        474
475
476
            477
478
479
480
481
482
             \ensuremath{//} Compute the final residual norm. Also gathers the solution from all
483
             // subdomains.
             Solve<ValueType, IndexType, MixedValueType>::compute_residual_norm(
    settings, metadata, global_matrix, global_rhs, global_solution,
    mat_norm, rhs_norm, sol_norm, residual_norm);
484
485
486
             gather_comm_data<ValueType, IndexType, MixedValueType>(
488
                 metadata.num_subdomains, this->comm_struct,
489
                  metadata.comm_data_struct);
490
             // clang-format off
491
             if (metadata.my_rank == 0)
492
493
                  std::cout
                    << " residual norm " << residual_norm << "\n"
<< " relative residual norm of solution " << residual_norm/rhs_norm << "\n"
<< " Time taken for solve " << elapsed_time.count()</pre>
494
495
496
497
                    << std::endl:
498
             // clang-format on
499
500
501
         if (metadata.my_rank == 0) {
502
             solution->copy_from(global_solution.get());
503
504
         // Communicate<ValueType, IndexType>::clear(settings);
```

The documentation for this class was generated from the following files:

- schwarz base.hpp (ca00a18)
- /home/runner/work/schwarz-lib/schwarz-lib/source/schwarz base.cpp (d458d06)

7.14 schwz::Settings Struct Reference

The struct that contains the solver settings and the parameters to be set by the user.

```
#include <settings.hpp>
```

Classes

• struct comm_settings

The settings for the various available communication paradigms.

· struct convergence_settings

The various convergence settings available.

Public Types

· enum partition_settings

The partition algorithm to be used for partitioning the matrix.

enum local_solver_settings

The local solver algorithm for the local subdomain solves.

Public Attributes

· std::string executor_string

The string that contains the ginkgo executor paradigm.

std::shared_ptr< gko::Executor > executor = gko::ReferenceExecutor::create()

The ginkgo executor the code is to be executed on.

std::shared_ptr< device_guard > cuda_device_guard

The ginkgo executor the code is to be executed on.

gko::int32 overlap = 2

The overlap between the subdomains.

• std::string matrix_filename = "null"

The string that contains the matrix file name to read from .

bool explicit laplacian = true

Flag if the laplacian matrix should be generated within the library.

• bool use mixed precision = false

Flag if mixed precision should be used.

bool enable_random_rhs = false

Flag to enable a random rhs.

• bool print_matrices = false

Flag to enable printing of matrices.

• bool debug_print = false

Flag to enable some debug printing.

• bool non_symmetric_matrix = false

Is the matrix non-symmetric?, Use GMRES for local solves.

• unsigned int restart_iter = 1u

The restart iter for the GMRES solver.

• int reset_local_crit_iter = -1

The global iter at which to reset the local solver criterion.

• bool naturally_ordered_factor = false

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

std::string metis_objtype

This setting defines the objective type for the metis partitioning.

• bool use_precond = false

Enable the block jacobi local preconditioner for the local solver.

• bool write_debug_out = false

Enable the writing of debug out to file.

· bool write iters and residuals = false

Enable writing the iters and residuals to a file.

bool enable_logging = false

Flag to enable logging for local iterative solvers.

• bool write perm data = false

Enable the local permutations from CHOLMOD to a file.

int shifted_iter = 1

Iteration shift for node local communication.

std::string factorization = "cholmod"

The factorization for the local direct solver.

· std::string reorder

The reordering for the local solve.

7.14.1 Detailed Description

The struct that contains the solver settings and the parameters to be set by the user.

settings

7.14.2 Member Data Documentation

7.14.2.1 enable_logging

```
bool schwz::Settings::enable_logging = false
```

Flag to enable logging for local iterative solvers.

Note: Probably will have a significant performance hit.

7.14.2.2 explicit_laplacian

```
bool schwz::Settings::explicit_laplacian = true
```

Flag if the laplacian matrix should be generated within the library.

If false, an external matrix and rhs needs to be provided

Referenced by schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::initialize().

7.14.2.3 naturally_ordered_factor

```
bool schwz::Settings::naturally_ordered_factor = false
```

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

Note

This is mainly to allow compatibility with GPU solution.

The documentation for this struct was generated from the following file:

• settings.hpp (d458d06)

7.15 schwz::Solve ValueType, IndexType, MixedValueType > Class Template Reference

The Solver class the provides the solver and the convergence checking methods.

```
#include <solve.hpp>
```

Additional Inherited Members

7.15.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32, typename MixedValueType = gko::default_precision>
class schwz::Solve< ValueType, IndexType, MixedValueType>

The Solver class the provides the solver and the convergence checking methods.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Solve

The documentation for this class was generated from the following files:

- solve.hpp (228ce7a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/solve.cpp (92dbd95)

7.16 schwz::SolverRAS< ValueType, IndexType, MixedValueType > Class Template Reference

An implementation of the solver interface using the RAS solver.

```
#include <restricted_schwarz.hpp>
```

Public Member Functions

SolverRAS (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

Sets up the local and the interface matrices from the global matrix and the partition indices.

void setup_comm_buffers () override

Sets up the communication buffers needed for the boundary exchange.

void setup_windows (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std
 ::shared_ptr < gko::matrix::Dense < ValueType >> &main_buffer) override

Sets up the windows needed for the asynchronous communication.

void exchange_boundary (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared_ptr < gko::matrix::Dense < ValueType >> &global_solution) override

Exchanges the elements of the solution vector.

void update_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_solution, const std::shared_ptr< gko::matrix::Dense< ValueType >> &global = solution, const std::shared_ptr< gko::matrix::Dense
 valueType >> &global = solution, const std::shared_ptr< gko::matrix::Csr
 valueType, IndexType >> &interface_matrix) override

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Additional Inherited Members

7.16.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32, typename MixedValueType = gko ::default_precision>

class schwz::SolverRAS< ValueType, IndexType, MixedValueType >

An implementation of the solver interface using the RAS solver.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.16.2 Constructor & Destructor Documentation

7.16.2.1 SolverRAS()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

Parameters

settings	The settings struct.
metadata	The metadata struct.
data	The additional data struct.

```
51 : SchwarzBase<ValueType, IndexType, MixedValueType>(settings, metadata)
52 {}
```

7.16.3 Member Function Documentation

7.16.3.1 exchange_boundary()

Exchanges the elements of the solution vector.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_solution	The solution vector being exchanged between the subdomains.

Implements schwz::Communicate < ValueType, IndexType, MixedValueType >.

References schwz::Settings::comm_settings::enable_onesided, and schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::global_solution.

7.16.3.2 setup_local_matrices()

Sets up the local and the interface matrices from the global matrix and the partition indices.

Parameters

settings	The settings struct.
metadata	The metadata struct.
partition_indices	The array containing the partition indices.
global_matrix	The global system matrix.
local_matrix	The local system matrix.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.
local_perm	The local permutation, obtained through RCM or METIS.

Implements schwz::Initialize < ValueType, IndexType >.

References schwz::Metadata< ValueType, IndexType >::comm_size, schwz::Settings::executor, schwz::← Metadata< ValueType, IndexType >::first_row, schwz::SchwarzBase< ValueType, IndexType, MixedValueType, IndexType >::global_matrix, schwz::Metadata< ValueType, IndexType >::global_size, schwz::Metadata< ValueType, IndexType >::ipermutation, schwz::SchwarzBase< ValueType, IndexType, IndexType, MixedValueType, IndexType, IndexType >::local_matrix, schwz::Metadata< ValueType, IndexType >::local_size, schwz::Metadata< ValueType, IndexType >::local_size_x, schwz::Metadata< ValueType, IndexType >::local_size_x, schwz::Metadata< ValueType, IndexType >::local_to_global, schwz::Metadata< ValueType, IndexType >::my_rank, schwz::Metadata< ValueType, IndexType, IndexType >::num_subdomains, schwz::Settings::overlap, schwz::Metadata< ValueType, IndexType, IndexType >::overlap, schwz::Metadata< ValueType, IndexType >::overlap

```
62 {
       using mtx = gko::matrix::Csr<ValueType, IndexType>;
       using perm_type = gko::Array<IndexType>;
using perm_type = gko::matrix::Permutation<IndexType>;
64
6.5
       using arr = gko::Array<IndexType>;
66
       auto my_rank = metadata.my_rank;
67
68
       auto comm_size = metadata.comm_size;
       auto num_subdomains = metadata.num_subdomains;
70
       auto global_size = metadata.global_size;
71
       auto mpi_itype = schwz::mpi::get_mpi_datatype(*partition_indices.data());
72
      MPI_Bcast(partition_indices.data(), global_size, mpi_itype, 0,
73
74
                 MPI_COMM_WORLD);
75
76
       std::vector<IndexType> local_p_size(num_subdomains);
       auto global_to_local = metadata.global_to_local->get_data();
77
78
       auto local_to_global = metadata.local_to_global->get_data();
79
80
       auto first_row = metadata.first_row->get_data();
       auto permutation = metadata.permutation->get_data();
       auto i_permutation = metadata.i_permutation->get_data();
83
84
      auto nb = (global_size + num_subdomains - 1) /
      num subdomains:
85
      auto partition_settings =
86
           (Settings::partition_settings::partition_zoltan |
            Settings::partition_settings::partition_metis |
88
            Settings::partition_settings::partition_regular
89
            Settings::partition_settings::partition_regular2d |
90
            Settings::partition_settings::partition_custom) &
91
           settings.partition;
92
       IndexType *gmat_row_ptrs = global_matrix->get_row_ptrs();
       IndexType *gmat_col_idxs = global_matrix->get_col_idxs();
95
       ValueType *gmat_values = global_matrix->get_values();
96
       // default local p size set for 1 subdomain.
97
98
       first_row[0] = 0;
       for (auto p = 0; p < num_subdomains; ++p) {</pre>
99
100
            local_p_size[p] = std::min(global_size - first_row[p], nb);
101
            first_row[p + 1] = first_row[p] + local_p_size[p];
103
104
        if (partition_settings == Settings::partition_settings::partition_metis ||
```

```
106
              partition_settings ==
                   Settings::partition_settings::partition_regular2d) {
107
              if (num_subdomains > 1) {
   for (auto p = 0; p < num_subdomains; p++) {
      local_p_size[p] = 0;
}</pre>
108
109
110
111
112
                   for (auto i = 0; i < global_size; i++) {</pre>
113
                        local_p_size[partition_indices[i]]++;
114
115
                   first_row[0] = 0;
                   for (auto p = 0; p < num_subdomains; ++p) {
   first_row[p + 1] = first_row[p] + local_p_size[p];</pre>
116
117
118
119
                   // permutation
120
                   for (auto i = 0; i < global_size; i++) {</pre>
                        permutation[first_row[partition_indices[i]]] = i;
121
122
                        first_row[partition_indices[i]]++;
123
124
                   for (auto p = num_subdomains; p > 0; p--) {
125
                        first_row[p] = first_row[p - 1];
126
127
                   first_row[0] = 0;
128
                   // iperm
129
                   for (auto i = 0; i < global_size; i++) {</pre>
130
                        i_permutation[permutation[i]] = i;
131
132
133
              }
134
135
              auto gmat_temp = mtx::create(settings.executor->get_master(),
136
                                                  global matrix->get size().
137
                                                  global_matrix->get_num_stored_elements());
138
139
              auto nnz = 0;
140
              gmat_temp->get_row_ptrs()[0] = 0;
              for (auto row = 0; row < metadata.global_size; ++row) {
   for (auto col = gmat_row_ptrs[permutation[row]];
      col < gmat_row_ptrs[permutation[row] + 1]; ++col) {</pre>
141
142
143
144
                        gmat_temp->get_col_idxs()[nnz] =
145
                             i_permutation[gmat_col_idxs[col]];
146
                        gmat_temp->get_values()[nnz] = gmat_values[col];
147
                        nnz++;
148
149
                   gmat_temp->get_row_ptrs()[row + 1] = nnz;
150
151
              global_matrix->copy_from(gmat_temp.get());
152
153
154
         for (auto i = 0; i < global_size; i++) {</pre>
155
              global_to_local[i] = 0;
156
157
              local_to_global[i] = 0;
158
159
         auto num = 0;
         for (auto i = first_row[my_rank]; i < first_row[
160
       my_rank + 1]; i++) {
161
             global_to_local[i] = 1 + num;
              local_to_global[num] = i;
162
163
164
         }
165
166
         IndexType old = 0;
167
         for (auto k = 1; k < settings.overlap; k++) {</pre>
              auto now = num;
168
169
              for (auto i = old; i < now; i++) {</pre>
170
                   for (auto j = gmat_row_ptrs[local_to_global[i]];
                        j < gmat_row_ptrs[local_to_global[i] + 1]; j++) {
if (global_to_local[gmat_col_idxs[j]] == 0) {
    local_to_global[num] = gmat_col_idxs[j];</pre>
171
172
173
                             global_to_local[gmat_col_idxs[j]] = 1 + num;
175
176
                        }
177
                   }
178
179
              old = now;
180
181
         metadata.local_size = local_p_size[my_rank];
         metadata.local_size_x = num;
metadata.local_size_o = global_size;
182
183
         auto local_size = metadata.local_size;
auto local_size_x = metadata.local_size_x;
184
185
186
187
         metadata.overlap_size = num - metadata.local_size;
188
         auto host_ov_row = gko::Array<IndexType>::view(
189
              settings.executor->get_master(), metadata.overlap_size,
190
              &(metadata.local_to_global->get_data()[metadata.local_size]));
191
         metadata.overlap_row = vec_itype(settings.executor, metadata.overlap_size);
```

```
192
        metadata.overlap_row = host_ov_row;
193
194
        auto nnz_local = 0;
195
        auto nnz_interface = 0;
196
        for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i) {</pre>
197
             for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; j++) {</pre>
198
199
                 if (global_to_local[gmat_col_idxs[j]] != 0) {
200
                     nnz_local++;
201
                 } else {
                     std::cout << " debug: invalid edge?" << std::endl;
202
203
204
             }
205
206
         auto temp = 0;
207
        for (auto k = 0; k < metadata.overlap_size; k++) {</pre>
208
             temp = host_ov_row.get_data()[k];
             for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1]; j++) {
    if (global_to_local[gmat_col_idxs[j]] != 0) {</pre>
209
210
211
                     nnz_local++;
212
                 } else {
213
                     nnz_interface++;
214
                 }
215
             }
216
217
         std::shared_ptr<mtx> local_matrix_compute;
218
219
        local_matrix_compute = mtx::create(settings.executor->get_master(),
220
                                              gko::dim<2>(local_size_x), nnz_local);
221
         IndexType *lmat_row_ptrs = local_matrix_compute->get_row_ptrs();
         IndexType *lmat_col_idxs = local_matrix_compute->get_col_idxs();
222
223
        ValueType *lmat_values = local_matrix_compute->get_values();
224
        std::shared_ptr<mtx> interface_matrix_compute;
225
226
        if (nnz_interface > 0) {
             interface_matrix_compute =
227
228
                mtx::create(settings.executor->get master(),
                              gko::dim<2>(local_size_x), nnz_interface);
229
230
231
            interface_matrix_compute = mtx::create(settings.executor->get_master());
232
233
        IndexType *imat_row_ptrs = interface_matrix_compute->get_row_ptrs();
234
         IndexType *imat_col_idxs = interface_matrix_compute->get_col_idxs();
235
        ValueType *imat_values = interface_matrix_compute->get_values();
236
237
238
        num = 0:
        nnz_local = 0;
239
        auto nnz_interface_temp = 0;
240
        lmat_row_ptrs[0] = nnz_local;
241
        if (nnz_interface > 0) {
242
243
             imat_row_ptrs[0] = nnz_interface_temp;
244
245
         // Local interior matrix
         for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i) {
246
             for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; ++j) {
    if (global_to_local[gmat_col_idxs[j]]! = 0) {
247
248
249
                      lmat_col_idxs[nnz_local] =
250
                          global_to_local[gmat_col_idxs[j]] - 1;
251
                     lmat_values[nnz_local] = gmat_values[j];
252
                     nnz_local++;
253
                 }
254
255
             if (nnz_interface > 0) {
                 imat_row_ptrs[num + 1] = nnz_interface_temp;
256
257
258
             lmat_row_ptrs[num + 1] = nnz_local;
259
             num++;
260
261
262
         // Interface matrix
263
         if (nnz_interface > 0) {
             nnz_interface = 0;
2.64
             for (auto k = 0; k < metadata.overlap_size; k++) {</pre>
265
                 temp = host_ov_row.get_data()[k];
266
                 for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1];</pre>
267
268
                       j++) {
269
                        (global_to_local[gmat_col_idxs[j]] != 0) {
270
                          lmat_col_idxs[nnz_local] =
271
                          global_to_local[gmat_col_idxs[j]] - 1;
lmat_values[nnz_local] = gmat_values[j];
272
273
                          nnz_local++;
274
275
                          imat_col_idxs[nnz_interface] = gmat_col_idxs[j];
276
                          imat_values[nnz_interface] = gmat_values[j];
2.77
                          nnz_interface++;
278
                      }
```

```
279
                 lmat_row_ptrs[num + 1] = nnz_local;
imat_row_ptrs[num + 1] = nnz_interface;
280
281
282
283
284
285
        auto now = num;
        for (auto i = old; i < now; i++) {</pre>
286
287
             for (auto j = gmat_row_ptrs[local_to_global[i]];
288
                   j < gmat_row_ptrs[local_to_global[i] + 1]; j++) {</pre>
                 if (global_to_local[gmat_col_idxs[j]] == 0) {
289
290
                      local_to_global[num] = gmat_col_idxs[j];
291
                      global_to_local[gmat_col_idxs[j]] = 1 + num;
292
293
294
             }
295
296
297
        local_matrix_compute->sort_by_column_index();
298
        interface_matrix_compute->sort_by_column_index();
299
300
        local_matrix = mtx::create(settings.executor);
301
        local_matrix->copy_from(gko::lend(local_matrix_compute));
302
        interface matrix = mtx::create(settings.executor);
303
        interface_matrix->copy_from(gko::lend(interface_matrix_compute));
304 }
```

7.16.3.3 setup_windows()

Sets up the windows needed for the asynchronous communication.

Parameters

settings	The settings struct.
metadata	The metadata struct.
main_buffer	The main buffer being exchanged between the subdomains.

Implements schwz::Communicate < ValueType, IndexType, MixedValueType >.

References schwz::Settings::comm_settings::enable_get, schwz::Settings::comm_settings::enable_lock_ <schwz::Settings::comm_settings::enable_one_by_one, schwz::Settings::comm_settings::enable_onesided, schwz::Settings::comm_settings::enable_overlap, schwz::Settings::comm_settings::enable_put, schwz::Settings⇔ ::executor, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::get_displacements, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::get_request, schwz::← Communicate < ValueType, IndexType, MixedValueType >::comm_struct::global_get, schwz::Communicate < ValueType, IndexType, MixedValueType >::comm struct::global put, schwz::SchwarzBase < ValueType, Index← Type, MixedValueType >::global solution, schwz::Communicate < ValueType, IndexType, MixedValueType >← ::comm_struct::is_local_neighbor, schwz::Metadata < ValueType, IndexType >::iter_count, schwz::Communicate < ValueType, IndexType, MixedValueType >::comm struct::local get, schwz::Communicate < ValueType, IndexType, MixedValueType >::comm struct::local neighbors in, schwz::Communicate< ValueType, IndexType, Mixed← ValueType >::comm struct::local neighbors out, schwz::Communicate< ValueType, IndexType, MixedValue← Type >::comm_struct::local_num_neighbors_in, schwz::Communicate< ValueType, IndexType, MixedValue← Type >::comm_struct::local_num_neighbors_out, schwz::Communicate < ValueType, IndexType, MixedValueType

>::comm_struct::local_put, schwz::Metadata< ValueType, IndexType >::local_size_o, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::mixedt_recv_buffer, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::mixedt_send_buffer, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::neighbors_in, schwz::Communicate< ValueType, IndexType, IndexType, MixedValueType >::comm_etruct::neighbors_out, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::num_neighbors_out, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::put_displacements, schwz::Communicate< ValueFype, IndexType, MixedValueType >::comm_struct::put_request, schwz::Communicate< ValueType, IndexType, MixedValueType >::comm_struct::put_request, schwz::Communicate< ValueType, IndexType, MixedValueType, IndexType, IndexType, IndexType, MixedValueType, IndexType, IndexType, IndexType, MixedValueType, IndexType, MixedValueType, IndexType, MixedValueType, IndexType, MixedValueType, IndexType, MixedValueType >::comm_struct::send_buffer, schwz::Settings::comm_settings::stage_through_host, schwz::Settings::use_mixed communicate

precision, schwz::Communicate

ValueType, IndexType, MixedValueType >::comm_struct::window_send_buffer, and schwz::Communicate

ValueType, IndexType, MixedValueType >::comm_struct::window_send_buffer, and schwz::Communicate

```
611 {
        using vec_itype = gko::Array<IndexType>;
        using vec_vtype = gko::matrix::Dense<ValueType>;
613
614
        auto num_subdomains = metadata.num_subdomains;
615
        auto local_size_o = metadata.local_size_o;
        auto neighbors_in = this->comm_struct.neighbors_in->get_data();
616
617
        auto global_get = this->comm_struct.global_get->get_data();
618
        auto neighbors_out = this->comm_struct.neighbors_out->get_data();
        auto global_put = this->comm_struct.global_put->get_data();
619
620
        // set displacement for the MPI buffer
621
        auto get_displacements = this->comm_struct.get_displacements->get_data();
auto put_displacements = this->comm_struct.put_displacements->get_data();
622
623
624
625
            std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
626
            tmp_num_comm_elems[0] = 0;
627
            for (auto j = 0; j < this->comm_struct.num_neighbors_in; <math>j++) {
                 if ((global_get[j])[0] > 0) {
62.8
629
                     int p = neighbors_in[j];
630
                     tmp_num_comm_elems[p + 1] = (global_get[j])[0];
632
633
            for (auto j = 0; j < num_subdomains; j++) {</pre>
634
                tmp_num_comm_elems[j + 1] += tmp_num_comm_elems[j];
635
636
637
            auto mpi_itype = schwz::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
638
            MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, put_displacements,
639
                          1, mpi_itype, MPI_COMM_WORLD);
640
641
642
643
            std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
644
            tmp_num_comm_elems[0] = 0;
645
                (auto j = 0; j < this->comm_struct.num_neighbors_out; j++) {
646
                if ((global_put[j])[0] > 0) {
647
                     int p = neighbors_out[j];
648
                     tmp_num_comm_elems[p + 1] = (global_put[j])[0];
649
650
651
            for (auto j = 0; j < num_subdomains; j++) {</pre>
652
                 tmp_num_comm_elems[j + 1] += tmp_num_comm_elems[j];
653
654
            auto mpi_itype = schwz::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
656
            MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, get_displacements,
657
                          1, mpi_itype, MPI_COMM_WORLD);
658
659
660
        // setup windows
        if (settings.comm_settings.enable_onesided) {
661
663
            MPI_Win_create(main_buffer->get_values(),
                            main_buffer->get_size()[0] * sizeof(ValueType),
664
665
                             sizeof(ValueType), MPI_INFO_NULL, MPI_COMM_WORLD,
666
                            &(this->comm_struct.window_x));
667
        }
668
669
670
        if (settings.comm_settings.enable_onesided) {
671
             // MPI_Alloc_mem ? Custom allocator ? TODO
            MPI_Win_create(this->local_residual_vector->get_values(),
672
673
                             (num_subdomains) * sizeof(ValueType), sizeof(ValueType),
                            MPI_INFO_NULL, MPI_COMM_WORLD,
```

```
&(this->window_residual_vector));
676
            std::vector<IndexType> zero_vec(num_subdomains, 0);
677
            gko::Array<IndexType> temp_array{settings.executor->get_master(),
678
                                               zero_vec.begin(), zero_vec.end());
            this->convergence_vector = std::shared_ptr<vec_itype>(
679
680
                new vec_itype(settings.executor->get_master(), temp_array),
681
                std::default_delete<vec_itype>());
682
            this->convergence_sent = std::shared_ptr<vec_itype>(
683
               new vec_itype(settings.executor->get_master(), num_subdomains),
684
                std::default_delete<vec_itype>());
           this->convergence_local = std::shared_ptr<vec_itype>(
685
               new vec_itype(settings.executor->get_master(), num_subdomains),
686
687
                std::default delete<vec itvpe>());
688
            MPI_Win_create(this->convergence_vector->get_data(),
689
                            (num_subdomains) * sizeof(IndexType), sizeof(IndexType),
690
                            MPI_INFO_NULL, MPI_COMM_WORLD,
691
                            &(this->window_convergence));
692
       }
693
694
        if (settings.comm_settings.enable_onesided && num_subdomains > 1) {
695
            // Lock all windows.
696
            if (settings.comm_settings.enable_get &&
697
                settings.comm_settings.enable_lock_all) {
698
                MPI_Win_lock_all(0, this->comm_struct.window_send_buffer);
699
700
            if (settings.comm_settings.enable_put &&
701
                settings.comm_settings.enable_lock_all) {
702
                MPI_Win_lock_all(0, this->comm_struct.window_recv_buffer);
703
            if (settings.comm_settings.enable_one_by_one &&
    settings.comm_settings.enable_lock_all) {
704
705
706
                MPI_Win_lock_all(0, this->comm_struct.window_x);
707
708
            MPI_Win_lock_all(0, this->window_residual_vector);
709
            MPI_Win_lock_all(0, this->window_convergence);
710
711 }
```

7.16.3.4 update_boundary()

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_solution	The local solution vector in the subdomain.
local_rhs	The local right hand side vector in the subdomain.
global_solution	The workspace solution vector.
global_old_solution	The global solution vector of the previous iteration.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.

Implements schwz::Communicate < ValueType, IndexType, MixedValueType >.

References schwz::Settings::executor, schwz::SchwarzBase< ValueType, IndexType, IndexType, MixedValueType >::global --_solution, schwz::SchwarzBase< ValueType, IndexType, MixedValueType >::interface_matrix, schwz::Schwarz --Base< ValueType, IndexType, MixedValueType >::local_rhs, schwz::Metadata< ValueType, IndexType, IndexType, IndexType, MixedValueType, MixedValueType >::local_solution, schwz::Metadata
ValueType, IndexType, IndexType, IndexType, SchwarzBase

```
999 {
1000
         using vec_vtype = gko::matrix::Dense<ValueType>;
         auto one = gko::initialize<gko::matrix::Dense<ValueType>>(
             {1.0}, settings.executor);
1002
1003
         auto neg_one = gko::initialize<gko::matrix::Dense<ValueType>>(
1004
             {-1.0}, settings.executor);
1005
         auto local_size_x = metadata.local_size_x;
         local_solution->copy_from(local_rhs.get());
if (metadata.num_subdomains > 1 && settings.overlap > 0) {
1006
1007
              auto temp_solution = vec_vtype::create(
1008
                  settings.executor, local_solution->get_size(),
1009
1010
                  gko::Array<ValueType>::view(settings.executor,
1011
                                                local_solution->get_size()[0],
1012
                                                global_solution->get_values()),
1013
                 1);
1014
              interface_matrix->apply(neg_one.get(), temp_solution.get(), one.get(),
1015
                                        local_solution.get());
         }
1017 }
```

The documentation for this class was generated from the following files:

- restricted_schwarz.hpp (d458d06)
- /home/runner/work/schwarz-lib/schwarz-lib/source/restricted_schwarz.cpp (d458d06)

7.17 UmfpackError Class Reference

UmfpackError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

UmfpackError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a METIS error.

7.17.1 Detailed Description

UmfpackError is thrown when a METIS routine throws a non-zero error code.

7.17.2 Constructor & Destructor Documentation

7.17.2.1 UmfpackError()

Initializes a METIS error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the METIS routine that failed
error_code	The resulting METIS error code

```
205 : Error(file, line, func + ": " + get_error(error_code))
206 {}
```

The documentation for this class was generated from the following files:

- exception.hpp (35a1195)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (35a1195)

7.18 schwz::Utils < ValueType, IndexType > Struct Template Reference

The utilities class which provides some checks and basic utilities.

```
#include <utils.hpp>
```

7.18.1 Detailed Description

 $template < typename\ ValueType = gko::default_precision,\ typename\ IndexType = gko::int32 > struct\ schwz::Utils < ValueType,\ IndexType >$

The utilities class which provides some checks and basic utilities.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Utils

The documentation for this struct was generated from the following files:

- utils.hpp (1cd0e3b)
- /home/runner/work/schwarz-lib/schwarz-lib/source/utils.cpp (f366659)

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