schwz

Generated automatically from event-based

Generated by Doxygen 1.8.13

Contents

1	Main	Page	1
2	# Ins	stallation Instructions	3
3	Test	ing Instructions	5
4	Bend	chmarking.	7
5	Mod	ule Documentation	9
	5.1	Communicate	9
		5.1.1 Detailed Description	9
	5.2	Initialization	10
		5.2.1 Detailed Description	10
	5.3	Schwarz Class	11
		5.3.1 Detailed Description	11
	5.4	Solve	12
		5.4.1 Detailed Description	12
	5.5	Utils	13
		5.5.1 Detailed Description	13
6	Nam	espace Documentation	15
	6.1	ProcessTopology Namespace Reference	15
		6.1.1 Detailed Description	15
	6.2	schwz Namespace Reference	15
		6.2.1 Detailed Description	16
	6.3	schwz::CommHelpers Namespace Reference	16
		6.3.1 Detailed Description	16
	6.4	schwz::conv_tools Namespace Reference	16
		6.4.1 Detailed Description	16
	6.5	schwz::PartitionTools Namespace Reference	17
		6.5.1 Detailed Description	17
	6.6	schwz::SolverTools Namespace Reference	17
		6.6.1 Detailed Description	17

ii CONTENTS

7	Clas	s Docu	umentation	19
	7.1	BadDii	mension Class Reference	19
		7.1.1	Detailed Description	19
		7.1.2	Constructor & Destructor Documentation	19
			7.1.2.1 BadDimension()	19
	7.2	schwz	:::Settings::comm_settings Struct Reference	20
		7.2.1	Detailed Description	21
	7.3	schwz	:::Communicate< ValueType, IndexType >::comm_struct Struct Reference	21
		7.3.1	Detailed Description	22
		7.3.2	Member Data Documentation	23
			7.3.2.1 global_get	23
			7.3.2.2 global_put	23
			7.3.2.3 is_local_neighbor	23
			7.3.2.4 local_get	24
			7.3.2.5 local_put	24
			7.3.2.6 remote_get	24
			7.3.2.7 remote_put	25
	7.4	schwz	:::Communicate < ValueType, IndexType > Class Template Reference	25
		7.4.1	Detailed Description	25
		7.4.2	Member Function Documentation	26
			7.4.2.1 exchange_boundary()	26
			7.4.2.2 local_to_global_vector()	26
			7.4.2.3 setup_windows()	27
			7.4.2.4 update_boundary()	28
	7.5	schwz	:::Settings::convergence_settings Struct Reference	28
		7.5.1	Detailed Description	28
	7.6	CudaE	Error Class Reference	29
		7.6.1	Detailed Description	29
		7.6.2	Constructor & Destructor Documentation	29
			7.6.2.1 CudaError()	29

CONTENTS

7.7	Cuspar	seError C	lass Reference	30
	7.7.1	Detailed	Description	30
	7.7.2	Construc	tor & Destructor Documentation	30
		7.7.2.1	CusparseError()	30
7.8	schwz:	:device_gı	uard Class Reference	31
	7.8.1	Detailed	Description	31
7.9	schwz:	:Initialize<	ValueType, IndexType > Class Template Reference	31
	7.9.1	Detailed	Description	32
	7.9.2	Member	Function Documentation	32
		7.9.2.1	generate_dipole_rhs()	32
		7.9.2.2	generate_random_rhs()	33
		7.9.2.3	generate_sin_rhs()	33
		7.9.2.4	partition()	34
		7.9.2.5	setup_global_matrix()	35
		7.9.2.6	setup_local_matrices()	36
		7.9.2.7	setup_vectors()	37
7.10	schwz:	:Metadata	< ValueType, IndexType > Struct Template Reference	38
	7.10.1	Detailed	Description	39
	7.10.2	Member	Data Documentation	40
		7.10.2.1	local_solver_tolerance	40
		7.10.2.2	tolerance	40
7.11	MetisE	rror Class	Reference	40
	7.11.1	Detailed	Description	40
	7.11.2	Construc	tor & Destructor Documentation	41
		7.11.2.1	MetisError()	41
7.12	schwz:	:Metadata	< ValueType, IndexType >::post_process_data Struct Reference	41
	7.12.1	Detailed	Description	41
7.13	schwz:	:SchwarzE	Base < ValueType, IndexType > Class Template Reference	42
	7.13.1	Detailed	Description	43
	7.13.2	Construc	etor & Destructor Documentation	43

iv CONTENTS

7.13.2.1 SchwarzBase()	. 43
7.13.3 Member Function Documentation	. 44
7.13.3.1 print_matrix()	. 44
7.13.3.2 print_vector()	. 44
7.13.3.3 run()	. 45
7.14 schwz::Settings Struct Reference	. 48
7.14.1 Detailed Description	. 49
7.14.2 Member Data Documentation	. 49
7.14.2.1 explicit_laplacian	. 49
7.14.2.2 naturally_ordered_factor	. 50
7.15 schwz::Solve< ValueType, IndexType > Class Template Reference	. 50
7.15.1 Detailed Description	. 50
7.16 schwz::SolverRAS< ValueType, IndexType > Class Template Reference	. 50
7.16.1 Detailed Description	. 51
7.16.2 Constructor & Destructor Documentation	. 51
7.16.2.1 SolverRAS()	. 51
7.16.3 Member Function Documentation	. 52
7.16.3.1 exchange_boundary()	. 52
7.16.3.2 setup_local_matrices()	. 53
7.16.3.3 setup_windows()	. 57
7.16.3.4 update_boundary()	. 59
7.17 UmfpackError Class Reference	. 60
7.17.1 Detailed Description	. 60
7.17.2 Constructor & Destructor Documentation	. 60
7.17.2.1 UmfpackError()	. 60
7.18 schwz::Utils< ValueType, IndexType > Struct Template Reference	
7.18.1 Detailed Description	
	-

Index

63

Main Page

This is the main page for the Schwarz library pdf documentation. The repository is hosted on github. Documentation on aspects such as the build system, can be found at the # Installation Instructions page.

Modules

The structure of the Schwarz Library code is divided into different ${\tt modules}$:

- Initialization: Handles the initialization of the problem and the solver.
- Communicate: Handles the communication.
- Solve: Handles the local solution and the convergence detection.
- Schwarz Class: The Classes related to the Schwarz solvers.
- Utils: Provides some basic utilities.

2 Main Page

Installation Instructions

Building

Use the standard cmake build procedure:

```
mkdir build; cd build
cmake -G "Unix Makefiles" [OPTIONS] .. && make
```

Replace [OPTIONS] with desired cmake options for your build. The library adds the following additional switches to control what is being built:

- -DSCHWARZ_BUILD_BENCHMARKING={ON, OFF} Builds some example benchmarks. Default is ON
- -DSCHWARZ_BUILD_METIS={ON, OFF} Builds with support for the METIS partitioner. User needs to provide the path to the installation of the METIS library in METIS_DIR, preferably as an environment variable. Default is OFF
- -DSCHWARZ_BUILD_CHOLMOD={ON, OFF} Builds with support for the CHOLMOD module from the Suitesparse library. User needs to set an environment variable CHOLMOD_DIR to the path containing the CHOLMOD installation. Default is OFF
- -DSCHWARZ_BUILD_CUDA={ON, OFF} Builds with CUDA support. Though Ginkgo provides most of the required CUDA support, we do need to link to CUDA for explicit setting of GPU affinities, some custom gather and scatter operations. Default is OFF.
- -DSCHWARZ_BUILD_CLANG_TIDY={ON, OFF} Builds with support for clang-tidy Default is OFF
- -DSCHWARZ_BUILD_DEALII={ON, OFF} Builds with support for the finite element library deal.ii
 Default is OFF
- -DSCHWARZ_WITH_HWLOC={ON, OFF} Builds with support for the hardware locality library used for binding hardware. hwloc is distributed as a part of the Open-MPI project. Default is ON
- -DSCHWARZ_DEVEL_TOOLS={ON, OFF} Builds with some developer tools support. Default is ON. In particular uses git-cmake-format to automatically format the source files with clang-format.

Tips

- If you are having CUDA problems and you are not using CUDA, then feel free to switch the CUDA module off with -DSCHWARZ_BUILD_CUDA=off.
- Installing CHOLMOD can be a bit annoying. TODO add some details on fixing Suitesparse compilation.
- When doing merge commits it is possible that make format does not work. You can run cmake -DSCH ← WARZ_DEVEL_TOOLS=OFF . . to temporarily switch off the formatting. Please switch it on again when committing normally.

Testing Instructions

6 Testing Instructions

Benchmarking.

Benchmark example 1.

Poisson solver using Restricted Additive Schwarz with overlap.

The flag $-DSCHWARZ_BUILD_BENCHMARKING$ (default ON) enables the example and benchmarking snippets. The following command line options are available for this example. This is setup using gflags.

The executable is run in the following fashion:

"sh [MPI_COMMAND] [MPI_OPTIONS]

8 Benchmarking.

Module Documentation

5.1 Communicate

A module dedicated to the Communication interface in schwarz-lib.

Namespaces

• schwz::CommHelpers

The CommHelper namespace .

ProcessTopology

The ProcessTopology namespace.

Classes

class schwz::Communicate< ValueType, IndexType >

The communication class that provides the methods for the communication between the subdomains.

struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

5.1.1 Detailed Description

A module dedicated to the Communication interface in schwarz-lib.

10 Module Documentation

5.2 Initialization

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

Namespaces

· schwz::PartitionTools

The PartitionTools namespace.

ProcessTopology

The ProcessTopology namespace .

Classes

· class schwz::device_guard

This class defines a device guard for the cuda functions and the cuda module.

class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

struct schwz::Settings

The struct that contains the solver settings and the parameters to be set by the user.

- struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

5.2.1 Detailed Description

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

5.3 Schwarz Class

5.3 Schwarz Class

A module dedicated to the Schwarz solver classes in schwarz-lib.

Classes

class schwz::SolverRAS < ValueType, IndexType >
 An implementation of the solver interface using the RAS solver.

 $\bullet \ \, {\it class schwz::} Schwarz Base < Value Type, \, Index Type >$

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

5.3.1 Detailed Description

A module dedicated to the Schwarz solver classes in schwarz-lib.

12 Module Documentation

5.4 Solve

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

Namespaces

• schwz::conv_tools

The conv_tools namespace .

• schwz::SolverTools

The SolverTools namespace.

Classes

struct schwz::Metadata < ValueType, IndexType >

The solver metadata struct.

class schwz::Solve < ValueType, IndexType >

The Solver class the provides the solver and the convergence checking methods.

5.4.1 Detailed Description

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

5.5 Utils 13

5.5 Utils

A module dedicated to the utilities in schwarz-lib.

Classes

 $\bullet \ \, {\sf struct\ schwz::} {\sf Utils} {< \ } {\sf ValueType,\ IndexType} >$

The utilities class which provides some checks and basic utilities.

5.5.1 Detailed Description

A module dedicated to the utilities in schwarz-lib.

14 Module Documentation

Namespace Documentation

6.1 ProcessTopology Namespace Reference

The ProcessTopology namespace.

6.1.1 Detailed Description

The ProcessTopology namespace.

proc_topo

6.2 schwz Namespace Reference

The Schwarz wrappers namespace.

Namespaces

• CommHelpers

The CommHelper namespace .

• conv_tools

The conv_tools namespace .

PartitionTools

The PartitionTools namespace.

SolverTools

The SolverTools namespace .

Classes

· class Communicate

The communication class that provides the methods for the communication between the subdomains.

· class device_guard

This class defines a device guard for the cuda functions and the cuda module.

· class Initialize

The initialization class that provides methods for initialization of the solver.

struct Metadata

The solver metadata struct.

· class SchwarzBase

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

struct Settings

The struct that contains the solver settings and the parameters to be set by the user.

· class Solve

The Solver class the provides the solver and the convergence checking methods.

class SolverRAS

An implementation of the solver interface using the RAS solver.

struct Utils

The utilities class which provides some checks and basic utilities.

6.2.1 Detailed Description

The Schwarz wrappers namespace.

6.3 schwz::CommHelpers Namespace Reference

The CommHelper namespace.

6.3.1 Detailed Description

The CommHelper namespace.

comm_helpers

6.4 schwz::conv_tools Namespace Reference

The conv_tools namespace.

6.4.1 Detailed Description

The conv_tools namespace.

conv_tools

6.5 schwz::PartitionTools Namespace Reference

The PartitionTools namespace.

6.5.1 Detailed Description

The PartitionTools namespace.

part_tools

6.6 schwz::SolverTools Namespace Reference

The SolverTools namespace.

6.6.1 Detailed Description

The SolverTools namespace.

solver_tools

Class Documentation

7.1 BadDimension Class Reference

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

```
#include <exception.hpp>
```

Public Member Functions

BadDimension (const std::string &file, int line, const std::string &func, const std::string &op_name, std::size
 _t op_num_rows, std::size_t op_num_cols, const std::string &clarification)
 Initializes a bad dimension error.

7.1.1 Detailed Description

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

7.1.2 Constructor & Destructor Documentation

7.1.2.1 BadDimension()

Initializes a bad dimension error.

20 Class Documentation

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
op_name	The name of the operator
op_num_rows	The row dimension of the operator
op_num_cols	The column dimension of the operator
clarification	An additional message further describing the error

The documentation for this class was generated from the following file:

• exception.hpp (5af933a)

7.2 schwz::Settings::comm_settings Struct Reference

The settings for the various available communication paradigms.

```
#include <settings.hpp>
```

Public Attributes

• bool enable_onesided = false

Enable one-sided communication.

• bool enable_overlap = false

Enable explicit overlap between communication and computation.

• bool enable_put = false

Put the data to the window using MPI_Put rather than get.

• bool enable_get = true

Get the data to the window using MPI_Get rather than put.

• bool enable_one_by_one = false

Push each element separately directly into the buffer.

• bool enable_flush_local = false

Use local flush.

• bool enable flush all = true

Use flush all.

• bool enable_lock_local = false

Use local locks.

• bool enable_lock_all = true

Use lock all.

7.2.1 Detailed Description

The settings for the various available communication paradigms.

The documentation for this struct was generated from the following file:

• settings.hpp (5af933a)

7.3 schwz::Communicate < ValueType, IndexType >::comm_struct Struct Reference

The communication struct used to store the communication data.

```
#include <communicate.hpp>
```

Public Attributes

· int num neighbors in

The number of neighbors this subdomain has to receive data from.

· int num_neighbors_out

The number of neighbors this subdomain has to send data to.

std::shared_ptr< gko::Array< IndexType > > neighbors_in

The neighbors this subdomain has to receive data from.

std::shared_ptr< gko::Array< IndexType >> neighbors_out

The neighbors this subdomain has to send data to.

std::vector< bool > is_local_neighbor

The bool vector which is true if the neighbors of a subdomain are in one node.

• int local_num_neighbors_in

The number of neighbors this subdomain has to receive data from.

int local_num_neighbors_out

The number of neighbors this subdomain has to send data to.

std::shared ptr< gko::Array< IndexType > > local neighbors in

The neighbors this subdomain has to receive data from.

std::shared_ptr< gko::Array< IndexType > > local_neighbors_out

The neighbors this subdomain has to send data to.

std::shared ptr< gko::Array< IndexType * > > global put

The array containing the number of elements that each subdomain sends from the other.

std::shared_ptr< gko::Array< IndexType * > > local_put

The array containing the number of elements that each subdomain sends from the other.

std::shared ptr< gko::Array< IndexType * > remote put

The array containing the number of elements that each subdomain sends from the other.

std::shared_ptr< gko::Array< IndexType * > > global_get

The array containing the number of elements that each subdomain gets from the other.

std::shared_ptr< gko::Array< IndexType * > > local_get

The array containing the number of elements that each subdomain gets from the other.

std::shared_ptr< gko::Array< IndexType * > > remote_get

The array containing the number of elements that each subdomain gets from the other.

std::shared_ptr< gko::Array< IndexType > > window_ids

The RDMA window ids.

22 Class Documentation

std::shared_ptr< gko::Array< IndexType > > windows_from
 The RDMA window ids to receive data from.

std::shared_ptr< gko::Array< IndexType > > windows_to

The RDMA window ids to send data to.

 $\bullet \quad \mathsf{std} :: \mathsf{shared_ptr} < \mathsf{gko} :: \mathsf{Array} < \mathsf{MPI_Request} >> \mathsf{put_request} \\$

The put request array.

std::shared_ptr< gko::Array< MPI_Request >> get_request
 The get request array.

std::shared_ptr< gko::matrix::Dense< ValueType >> send_buffer

The send buffer used for the actual communication for both one-sided and two-sided.

std::shared_ptr< gko::matrix::Dense< ValueType >> recv_buffer

The recy buffer used for the actual communication for both one-sided and two-sided.

std::shared ptr< gko::matrix::Dense< ValueType >> last recv bdy

• Sid...Shared_pir< gho...matrix...Defise< value type > > last_fect_bdy

The last received boundary values for each of the in neighbors for extrapolation.

• std::shared_ptr< gko::matrix::Dense< ValueType >> sec_last_recv_bdy

The second last received boundary values for each of the in neighbors for extrapolation.

std::shared ptr< gko::matrix::Dense< ValueType >> third last recv bdy

The second last received boundary values for each of the in neighbors for extrapolation.

std::shared_ptr< gko::matrix::Dense< ValueType >> curr_send_avg

Average of values in the send buffer for each of the out neighbors.

std::shared_ptr< gko::matrix::Dense< ValueType >> last_send_avg

Average of values in the last send buffer for each of the out neighbors.

std::shared_ptr< gko::matrix::Dense< ValueType >> curr_recv_avg

Average of values in the recv buffer for each of the out neighbors.

std::shared ptr< gko::matrix::Dense< ValueType >> last recv avg

Average of values in the last recv buffer for each of the out neighbors.

std::shared_ptr< gko::Array< IndexType >> msg_count

Number of messages sent.

std::shared_ptr< gko::Array< IndexType > > last_recv_iter

Iteration stamp of last received values.

std::shared_ptr< gko::Array< IndexType > > sec_last_recv_iter

Iteration stamp of second last received values.

std::shared_ptr< gko::Array< IndexType > > third_last_recv_iter

Iteration stamp of third last received values.

std::shared_ptr< gko::Array< IndexType > > get_displacements

The displacements for the receiving of the buffer.

std::shared_ptr< gko::Array< IndexType > > put_displacements

The displacements for the sending of the buffer.

· MPI Win window recv buffer

The RDMA window for the recv buffer.

· MPI Win window send buffer

The RDMA window for the send buffer.

MPI_Win window_x

The RDMA window for the solution vector.

7.3.1 Detailed Description

template<typename ValueType, typename IndexType>
struct schwz::Communicate< ValueType, IndexType >::comm_struct

The communication struct used to store the communication data.

7.3.2 Member Data Documentation

7.3.2.1 global_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> > schwz::Communicate< ValueType, IndexType >::comm
_struct::global_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global_get[p][0] contains the overall number of elements to be received to subdomain p and global—_put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

7.3.2.2 global_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm 
_struct::global_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global_put[p][0] contains the overall number of elements to be sent to subdomain p and global_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

7.3.2.3 is_local_neighbor

```
template<typename ValueType , typename IndexType >
std::vector<bool> schwz::Communicate< ValueType, IndexType >::comm_struct::is_local_neighbor
```

The bool vector which is true if the neighbors of a subdomain are in one node.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup comm buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup windows().

24 Class Documentation

7.3.2.4 local_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm←
_struct::local_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global_get[p][0] contains the overall number of elements to be received to subdomain p and global ← put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

7.3.2.5 | local_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm
_struct::local_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global_put[p][0] contains the overall number of elements to be sent to subdomain p and global_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

7.3.2.6 remote_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm
_struct::remote_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global_get[p][0] contains the overall number of elements to be received to subdomain p and global—put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

7.3.2.7 remote_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> > schwz::Communicate< ValueType, IndexType >::comm
_struct::remote_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global_put[p][0] contains the overall number of elements to be sent to subdomain p and global_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup_comm_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup_windows().

The documentation for this struct was generated from the following file:

· communicate.hpp (5af933a)

7.4 schwz::Communicate < ValueType, IndexType > Class Template Reference

The communication class that provides the methods for the communication between the subdomains.

```
#include <communicate.hpp>
```

Classes

· struct comm struct

The communication struct used to store the communication data.

Public Member Functions

virtual void setup_comm_buffers ()=0

Sets up the communication buffers needed for the boundary exchange.

 virtual void setup_windows (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared_ptr < gko::matrix::Dense < ValueType >> &main_buffer)=0

Sets up the windows needed for the asynchronous communication.

virtual void exchange_boundary (const Settings &settings, const Metadata
 ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense
 ValueType >> &solution, std::shared_ptr< gko::matrix::Dense
 ::Dense
 ValueType >> &last_solution, std::ofstream &fpr, std::ofstream &fpr)=0

Exchanges the elements of the solution vector.

void local_to_global_vector (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, const std::shared_ptr < gko::matrix::Dense < ValueType >> &local_vector, std::shared_ptr < gko::matrix::
 Dense < ValueType >> &global_vector)

Transforms data from a local vector to a global vector.

virtual void update_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_solution, const std::shared_ptr< gko::matrix::Dense< ValueType >> &global_solution, const std::shared_ptr< gko::matrix::Dense< ValueType, IndexType >> &interface_matrix)=0

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

void clear (Settings &settings)

Clears the data.

7.4.1 Detailed Description

```
template<typename ValueType, typename IndexType> class schwz::Communicate< ValueType, IndexType>
```

The communication class that provides the methods for the communication between the subdomains.

26 Class Documentation

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Communicate

7.4.2 Member Function Documentation

7.4.2.1 exchange_boundary()

Exchanges the elements of the solution vector.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_solution	The solution vector being exchanged between the subdomains.

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

7.4.2.2 local_to_global_vector()

Transforms data from a local vector to a global vector.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_vector	The local vector in question.
global_vector	The global vector in question.

```
71 {
       using vec = gko::matrix::Dense<ValueType>;
72
       auto alpha = gko::initialize<gko::matrix::Dense<ValueType>>(
           {1.0}, settings.executor);
75
       auto temp_vector = vec::create(
76
          settings.executor, gko::dim<2>(metadata.local_size, 1),
77
           gko::Array<ValueType>::view(
78
                settings.executor, metadata.local_size,
79
                &global_vector->get_values()[metadata.first_row
                                                     ->get_data()[metadata.my_rank]]),
81
           1);
82
83
       auto temp_vector2 = vec::create(
           settings.executor, gko::dim<2>(metadata.local_size, 1),
84
85
           gko::Array<ValueType>::view(settings.executor, metadata.local_size,
86
                                          local_vector->get_values()),
88
       if (settings.convergence_settings.convergence_crit ==
89
           Settings::convergence_settings::local_convergence_crit::
           residual_based) {
local_vector->add_scaled(alpha.get(), temp_vector.get());
temp_vector->add_scaled(alpha.get(), local_vector.get());
90
91
94
           temp_vector->copy_from(temp_vector2.get());
95
96 }
```

7.4.2.3 setup_windows()

Sets up the windows needed for the asynchronous communication.

Parameters

settings	The settings struct.
metadata	The metadata struct.
main buffer	The main buffer being exchanged between the subdomains.

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

28 Class Documentation

7.4.2.4 update_boundary()

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_solution	The local solution vector in the subdomain.
local_rhs	The local right hand side vector in the subdomain.
global_solution	The workspace solution vector.
global_old_solution	The global solution vector of the previous iteration.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

The documentation for this class was generated from the following files:

- · communicate.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/communicate.cpp (5af933a)

7.5 schwz::Settings::convergence_settings Struct Reference

The various convergence settings available.

```
#include <settings.hpp>
```

7.5.1 Detailed Description

The various convergence settings available.

The documentation for this struct was generated from the following file:

• settings.hpp (5af933a)

7.6 CudaError Class Reference

CudaError is thrown when a CUDA routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

CudaError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a CUDA error.

7.6.1 Detailed Description

CudaError is thrown when a CUDA routine throws a non-zero error code.

7.6.2 Constructor & Destructor Documentation

7.6.2.1 CudaError()

Initializes a CUDA error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the CUDA routine that failed
error_code	The resulting CUDA error code

The documentation for this class was generated from the following files:

- exception.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (5af933a)

30 Class Documentation

7.7 CusparseError Class Reference

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

• CusparseError (const std::string &file, int line, const std::string &func, int error_code)

Initializes a cuSPARSE error.

7.7.1 Detailed Description

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

7.7.2 Constructor & Destructor Documentation

7.7.2.1 CusparseError()

Initializes a cuSPARSE error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuSPARSE routine that failed
error_code	The resulting cuSPARSE error code

```
159 : Error(file, line, func + ": " + get_error(error_code))
160 {}
```

The documentation for this class was generated from the following files:

- exception.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (5af933a)

7.8 schwz::device_guard Class Reference

This class defines a device guard for the cuda functions and the cuda module.

```
#include <device_guard.hpp>
```

7.8.1 Detailed Description

This class defines a device guard for the cuda functions and the cuda module.

The guard is used to make sure that the device code is run on the correct cuda device, when run with multiple devices. The class records the current device id and uses <code>cudaSetDevice</code> to set the device id to the one being passed in. After the scope has been exited, the destructor sets the device_id back to the one before entering the scope.

The documentation for this class was generated from the following file:

device_guard.hpp (5af933a)

7.9 schwz::Initialize < ValueType, IndexType > Class Template Reference

The initialization class that provides methods for initialization of the solver.

```
#include <initialization.hpp>
```

Public Member Functions

void generate_random_rhs (std::vector< ValueType > &rhs)

Generates a random right hand side vector.

void generate_dipole_rhs (std::vector< ValueType > &rhs)

Generates a dipole right hand side vector.

void generate_sin_rhs (std::vector< ValueType > &rhs)

Generates a sinusoidal right hand side vector.

void setup_global_matrix (const std::string &filename, const gko::size_type &oned_laplacian_size, std
 ::shared ptr< gko::matrix::Csr< ValueType, IndexType >> &global matrix)

Generates the 2D global laplacian matrix.

The partitioning function.

void setup_vectors (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std
 ::vector< ValueType > &rhs, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_rhs, std::shared
 _ptr< gko::matrix::Dense< ValueType >> &global_rhs, std::shared_ptr< gko::matrix::Dense< ValueType
 >> &local_solution, std::shared_ptr< gko::matrix::Dense< ValueType >> &last_solution)

Setup the vectors with default values and allocate mameory if not allocated.

virtual void setup_local_matrices (Settings &settings, Metadata< ValueType, IndexType > &metadata, std
 ::vector< unsigned int > &partition_indices, std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >>
 &global_matrix, std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &local_matrix, std::shared
 _ptr< gko::matrix::Csr< ValueType, IndexType >> &interface_matrix)=0

Sets up the local and the interface matrices from the global matrix and the partition indices.

Public Attributes

std::vector< unsigned int > partition_indices

The partition indices containing the subdomains to which each row(vertex) of the matrix(graph) belongs to.

std::vector< unsigned int > cell_weights

The cell weights for the partition algorithm.

Additional Inherited Members

7.9.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Initialization

7.9.2 Member Function Documentation

7.9.2.1 generate_dipole_rhs()

Generates a dipole right hand side vector.

Parameters

```
rhs The rhs vector.
```

```
102 {
103
        auto oned_laplacian_size = metadata.oned_laplacian_size;
104
        //Placing dipole at 1/4 and 3/4 of Y-dim at the middle of X-dim
105
106
        for (int i = 0; i < oned_laplacian_size; i++)</pre>
107
            for (int j = 0; j < oned_laplacian_size; j++)</pre>
108
109
                if (i == oned_laplacian_size / 4 && j == oned_laplacian_size / 2)
110
111
                   rhs[i * oned_laplacian_size + j] = 100.0;
112
                else if (i == 3 * oned_laplacian_size / 4 && j == oned_laplacian_size / 2)
```

7.9.2.2 generate_random_rhs()

Generates a random right hand side vector.

Parameters

```
rhs The rhs vector.
```

```
91 {
92     std::uniform_real_distribution<double> unif(0.0, 1.0);
93     std::default_random_engine engine;
94     for (gko::size_type i = 0; i < rhs.size(); ++i) {
95         rhs[i] = unif(engine);
96     }
97 }</pre>
```

7.9.2.3 generate_sin_rhs()

Generates a sinusoidal right hand side vector.

Parameters

```
rhs The rhs vector.
```

References schwz::Initialize < ValueType, IndexType >::setup_global_matrix().

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

```
122 {
123     auto PI = (ValueType) (atan(1.0) * 4);
124     auto oned_laplacian_size = metadata.oned_laplacian_size;
125
126     //Source = sin(x)sin(y)
```

7.9.2.4 partition()

The partitioning function.

Allows the partition of the global matrix depending with METIS and a regular 1D decomposition.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_matrix	The global matrix.
partition_indices	The partition indices [OUTPUT].

References schwz::Metadata < ValueType, IndexType >::global_size, schwz::Metadata < ValueType, IndexType >::my_rank, schwz::Metadata < ValueType, IndexType >::num_subdomains, and schwz::Settings::write_debug_ \leftarrow out.

 $Referenced\ by\ schwz:: Schwarz Base < Value Type,\ Index Type > :: initialize ().$

```
323 {
324
        partition_indices.resize(metadata.global_size);
325
        if (metadata.my_rank == 0) {
            auto partition_settings =
326
327
                 (Settings::partition_settings::partition_zoltan |
328
                 Settings::partition_settings::partition_metis |
329
                 Settings::partition_settings::partition_regular
330
                 Settings::partition_settings::partition_regular2d |
331
                 Settings::partition_settings::partition_custom) &
332
                settings.partition;
333
334
            if (partition_settings ==
335
                 Settings::partition_settings::partition_zoltan) {
336
                SCHWARZ_NOT_IMPLEMENTED;
337
            } else if (partition_settings ==
338
                        Settings::partition_settings::partition_metis) {
                if (metadata.my_rank == 0) {
    std::cout << " METIS partition" << std::endl;</pre>
339
340
341
                PartitionTools::PartitionMetis(
342
343
                     settings, global_matrix, this->cell_weights,
344
                     metadata.num_subdomains, partition_indices);
345
            } else if (partition_settings ==
346
                        Settings::partition_settings::partition_regular) {
                 if (metadata.my_rank == 0) {
```

```
348
                    std::cout << " Regular 1D partition" << std::endl;</pre>
349
350
                PartitionTools::PartitionRegular(
351
                    global_matrix, metadata.num_subdomains, partition_indices);
352
            } else if (partition_settings ==
353
                        Settings::partition settings::partition regular2d) {
                if (metadata.my_rank == 0) {
354
355
                    std::cout << " Regular 2D partition" << std::endl;</pre>
356
357
                PartitionTools::PartitionRegular2D(
358
                    global_matrix, settings.write_debug_out,
                    metadata.num_subdomains, partition_indices);
359
            } else if (partition_settings =
360
                       Settings::partition_settings::partition_custom) {
361
362
                // User partitions mesh manually
363
                SCHWARZ_NOT_IMPLEMENTED;
364
            } else {
                SCHWARZ NOT IMPLEMENTED;
365
366
367
       }
368 }
```

7.9.2.5 setup_global_matrix()

Generates the 2D global laplacian matrix.

Parameters

oned_laplacian_size	The size of the one d laplacian grid.
global_matrix	The global matrix.

```
239 {
240
        using index_type = IndexType;
        using value_type = ValueType;
241
        using mtx = gko::matrix::Csr<value_type, index_type>;
if (settings.matrix_filename != "null") {
242
243
            auto input_file = std::ifstream(filename, std::ios::in);
244
245
            if (!input_file) {
                246
247
248
            global_matrix =
249
250
                gko::read<mtx>(input_file, settings.executor->get_master());
            global_matrix->sort_by_column_index();
251
            std::cout << "Matrix from file " << filename << std::endl;
252
253
       } else if (settings.matrix_filename == "null" &&
            settings.explicit_laplacian) {
std::cout << "Laplacian 2D Matrix (generated in house) " << std::endl;</pre>
254
255
256
            gko::size_type global_size = oned_laplacian_size *
      oned_laplacian_size;
257
258
            global_matrix = mtx::create(settings.executor->get_master(),
                                         gko::dim<2>(global_size), 5 * global_size);
259
            value_type *values = global_matrix->get_values();
260
2.61
            index_type *row_ptrs = global_matrix->get_row_ptrs();
            index_type *col_idxs = global_matrix->get_col_idxs();
262
263
264
            std::vector<gko::size_type> exclusion_set;
```

```
265
             std::map<IndexType, ValueType> stencil_map = {
                  {-oned_laplacian_size, -1}, {-1, -1}, {0, 4}, {1, -1}, {oned_laplacian_size, -1},
267
2.68
269
             for (auto i = 2; i < global_size; ++i) {
    gko::size_type index = (i - 1) * oned_laplacian_size;</pre>
270
271
272
                  if (index * index < global_size * global_size) {</pre>
273
                      exclusion_set.push_back(
274
                           linearize_index(index, index - 1, global_size));
                      {\tt exclusion\_set.push\_back} \ (
275
                          linearize_index(index - 1, index, global_size));
276
                  }
278
279
             280
281
282
283
             IndexType pos = 0;
284
             IndexType col_idx = 0;
285
             row_ptrs[0] = pos;
             for (IndexType i = 0; i < global_size; ++i) {
    for (auto ofs : stencil_map) {</pre>
286
287
288
289
                      auto in_exclusion_flag =
                          (exclusion_set[cur_idx] ==
290
291
                            linearize_index(i, i + ofs.first, global_size));
                      if (0 <= i + ofs.first && i + ofs.first < global_size &&</pre>
292
293
                           !in_exclusion_flag) {
294
                           values[pos] = ofs.second;
295
                           col_idxs[pos] = i + ofs.first;
296
                           ++pos;
297
                      if (in_exclusion_flag) {
298
299
                           cur_idx++;
300
301
                      col_idx = row_ptrs[i + 1] - pos;
302
303
                  row_ptrs[i + 1] = pos;
304
305
         } else {
             std::cerr << " Need to provide a matrix or enable the default "
"laplacian matrix."
306
307
308
                        << std::endl;
309
             std::exit(-1);
310
311 }
```

7.9.2.6 setup_local_matrices()

Sets up the local and the interface matrices from the global matrix and the partition indices.

Parameters

settings	The settings struct.
metadata	The metadata struct.
partition_indices	The array containing the partition indices.
global_matrix	The global system matrix.
local_matrix	The local system matrix.

Parameters

interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.
local_perm	The local permutation, obtained through RCM or METIS.

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

7.9.2.7 setup_vectors()

Setup the vectors with default values and allocate mameory if not allocated.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_rhs	The local right hand side vector in the subdomain.
global_rhs	The global right hand side vector.
local_solution	The local solution vector in the subdomain.

References schwz::Settings::executor, schwz::Metadata < ValueType, IndexType >::first_row, schwz::Metadata < ValueType, IndexType >::local_size_x, and schwz:: \leftarrow Metadata < ValueType, IndexType >::my_rank.

 $Referenced\ by\ schwz:: Schwarz Base < Value Type,\ Index Type > :: initialize ().$

```
379 {
380
       using vec = gko::matrix::Dense<ValueType>;
381
        auto my_rank = metadata.my_rank;
       auto first_row = metadata.first_row->get_data()[my_rank];
382
383
384
        // Copy the global rhs vector to the required executor.
385
       gko::Array<ValueType> temp_rhs{settings.executor->get_master(), rhs.begin(),
386
                                       rhs.end()};
       global_rhs = vec::create(settings.executor,
387
388
                                 gko::dim<2>{metadata.global_size, 1}, temp_rhs, 1);
389
390
       local_rhs =
391
           vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
392
        // Extract the local rhs from the global rhs. Also takes into account the
393
394
       SolverTools::extract_local_vector(settings, metadata, local_rhs.get(),
395
                                          global_rhs.get(), first_row);
```

```
397  local_solution =
398     vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
399
400  //contains the solution at the last event of communication
401  last_solution =
402     vec::create(settings.executor, gko::dim<2>(metadata.global_size, 1));
403 }
```

The documentation for this class was generated from the following files:

- initialization.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/initialization.cpp (5af933a)

7.10 schwz::Metadata < ValueType, IndexType > Struct Template Reference

The solver metadata struct.

```
#include <settings.hpp>
```

Classes

· struct post_process_data

The struct used for storing data for post-processing.

Public Attributes

MPI_Comm mpi_communicator

The MPI communicator.

• gko::size_type global_size = 0

The size of the global matrix.

• gko::size_type oned_laplacian_size = 0

The size of the 1 dimensional laplacian grid.

• gko::size_type local_size = 0

The size of the local subdomain matrix.

gko::size_type local_size_x = 0

The size of the local subdomain matrix + the overlap.

• gko::size type local size o = 0

The size of the local subdomain matrix + the overlap.

gko::size_type overlap_size = 0

The size of the overlap between the subdomains.

• gko::size_type num_subdomains = 1

The number of subdomains used within the solver.

int my_rank

The rank of the subdomain.

· int my_local_rank

The local rank of the subdomain.

· int local_num_procs

The local number of procs in the subdomain.

int comm_size

The number of subdomains used within the solver, size of the communicator.

· int num_threads

The number of threads used within the solver for each subdomain.

IndexType iter_count

The iteration count of the solver.

ValueType tolerance

The tolerance of the complete solver.

ValueType local_solver_tolerance

The tolerance of the local solver in case of an iterative solve.

IndexType max_iters

The maximum iteration count of the Schwarz solver.

IndexType local_max_iters

The maximum iteration count of the local iterative solver.

std::string local_precond

Local preconditioner.

unsigned int precond_max_block_size

The maximum block size for the preconditioner.

• ValueType current_residual_norm = -1.0

The current residual norm of the subdomain.

• ValueType min_residual_norm = -1.0

The minimum residual norm of the subdomain.

• ValueType constant = 0.0

Value of constant for event threshold.

• ValueType gamma = 0.0

Value of gamma for event threshold.

std::vector < std::tuple < int, int, std::string, std::vector < ValueType > > > time_struct

The struct used to measure the timings of each function within the solver loop.

std::vector< std::tuple< int, std::vector< std::tuple< int, int > >, std::vector< std::tuple< int, int > >, int, int > > comm_data_struct

The struct used to measure the timings of each function within the solver loop.

std::shared ptr< gko::Array< IndexType > > global to local

The mapping containing the global to local indices.

std::shared_ptr< gko::Array< IndexType > > local_to_global

The mapping containing the local to global indices.

std::shared_ptr< gko::Array< IndexType > > overlap_row

The overlap row indices.

std::shared ptr< gko::Array< IndexType > > first row

The starting row of each subdomain in the matrix.

std::shared_ptr< gko::Array< IndexType >> permutation

The permutation used for the re-ordering.

 $\bullet \quad std::shared_ptr < gko::Array < IndexType >> i_permutation \\$

The inverse permutation used for the re-ordering.

7.10.1 Detailed Description

template<typename ValueType, typename IndexType>
struct schwz::Metadata< ValueType, IndexType>

The solver metadata struct.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.10.2 Member Data Documentation

7.10.2.1 local_solver_tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::local_solver_tolerance
```

The tolerance of the local solver in case of an iterative solve.

The residual norm reduction required.

7.10.2.2 tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::tolerance
```

The tolerance of the complete solver.

The residual norm reduction required.

The documentation for this struct was generated from the following file:

• settings.hpp (5af933a)

7.11 MetisError Class Reference

MetisError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

MetisError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a METIS error.

7.11.1 Detailed Description

MetisError is thrown when a METIS routine throws a non-zero error code.

7.11.2 Constructor & Destructor Documentation

7.11.2.1 MetisError()

Initializes a METIS error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the METIS routine that failed
error_code	The resulting METIS error code

```
182 : Error(file, line, func + ": " + get_error(error_code))
183 {}
```

The documentation for this class was generated from the following files:

- exception.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (5af933a)

7.12 schwz::Metadata < ValueType, IndexType >::post_process_data Struct Reference

The struct used for storing data for post-processing.

```
#include <settings.hpp>
```

7.12.1 Detailed Description

```
template<typename ValueType, typename IndexType>
struct schwz::Metadata< ValueType, IndexType >::post_process_data
```

The struct used for storing data for post-processing.

The documentation for this struct was generated from the following file:

• settings.hpp (5af933a)

7.13 schwz::SchwarzBase < ValueType, IndexType > Class Template Reference

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

```
#include <schwarz_base.hpp>
```

Public Member Functions

SchwarzBase (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

void initialize ()

Initialize the matrix and vectors.

void run (std::shared_ptr< gko::matrix::Dense< ValueType >> &solution)

The function that runs the actual solver and obtains the final solution.

void print_vector (const std::shared_ptr< gko::matrix::Dense< ValueType >> &vector, int subd, std::string name)

The auxiliary function that prints a passed in vector.

void print_matrix (const std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &matrix, int rank, std::string name)

The auxiliary function that prints a passed in CSR matrix.

Public Attributes

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > local_matrix

The local subdomain matrix.

The local subdomain permutation matrix/array.

std::shared_ptr< gko::matrix::Permutation< IndexType > > local_inv_perm

The local subdomain inverse permutation matrix/array.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular_factor_I

The local lower triangular factor used for the triangular solves.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular_factor_u

The local upper triangular factor used for the triangular solves.

std::shared_ptr< gko::matrix::Csr< ValueType, IndexType > > interface_matrix

The local interface matrix.

std::shared ptr< gko::matrix::Csr< ValueType, IndexType >> global matrix

The global matrix.

std::shared_ptr< gko::matrix::Dense< ValueType >> local_rhs

The local right hand side.

std::shared_ptr< gko::matrix::Dense< ValueType >> global_rhs

The global right hand side.

std::shared_ptr< gko::matrix::Dense< ValueType >> local_solution

The local solution vector.

std::shared ptr< gko::matrix::Dense< ValueType >> last solution

The (local+overlap) solution vector at time of last event of communication The size of this vector is considered global ← _size to account for overlap.

std::shared_ptr< gko::matrix::Dense< ValueType >> global_solution

The global solution vector.

std::vector< ValueType > local_residual_vector_out

The global residual vector.

std::vector< std::vector< ValueType > > global residual vector out

The local residual vector.

Additional Inherited Members

7.13.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::SchwarzBase< ValueType, IndexType >

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

It derives from the Initialization class, the Communication class and the Solve class all of which are templated.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.13.2 Constructor & Destructor Documentation

7.13.2.1 SchwarzBase()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

Parameters

settings	The settings struct.	
metadata	The metadata struct.	

References schwz::Settings::cuda_device_guard, schwz::Settings::executor, schwz::Settings::executor_string, schwz::Metadata< ValueType, IndexType >::local_num_procs, schwz::Metadata< ValueType, IndexType >::my_local_rank, and schwz::Metadata< ValueType, IndexType >::my_rank.

```
: Initialize<ValueType, IndexType>(settings, metadata),
75
        settings(settings)
76
       metadata(metadata)
77 {
78
      using vec_itype = gko::Array<IndexType>;
79
      using vec_vecshared = gko::Array<IndexType *>;
      metadata.my_local_rank =
81
          Utils<ValueType, IndexType>::get_local_rank(metadata.mpi_communicator);
82
      metadata.local_num_procs = Utils<ValueType, IndexType>::get_local_num_procs(
83
          metadata.mpi_communicator);
      auto my_local_rank = metadata.my_local_rank;
84
      if (settings.executor_string == "omp") {
```

```
86
           settings.executor = gko::OmpExecutor::create();
           auto exec_info =
88
               static_cast<gko::OmpExecutor *>(settings.executor.get())
89
                  ->get_exec_info();
90
           exec_info->bind_to_core(metadata.my_local_rank);
91
92
       } else if (settings.executor_string == "cuda") {
           int num_devices = 0;
94 #if SCHW_HAVE_CUDA
9.5
           SCHWARZ_ASSERT_NO_CUDA_ERRORS(cudaGetDeviceCount(&num_devices));
96 #else
           SCHWARZ NOT IMPLEMENTED:
97
98 #endif
99
           Utils<ValueType, IndexType>::assert_correct_cuda_devices(
100
                num_devices, metadata.my_rank);
101
            settings.executor = gko::CudaExecutor::create(
               my_local_rank, gko::OmpExecutor::create());
102
           103
104
105
                                 ->get_exec_info();
106
           exec_info->bind_to_core(my_local_rank);
107
           settings.cuda_device_guard =
108
               std::make_shared<schwz::device_guard>(my_local_rank);
109
           std::cout << " Rank " << metadata.my_rank << " with local rank "
110
                      << my_local_rank << " has
111
112
                      << (static_cast<gko::CudaExecutor *>(settings.executor.get()))
113
                             ->get_device_id()
                      << " id of gpu" << std::endl;
114
       MPI_Barrier(metadata.mpi_communicator);
} else if (settings.executor_string == "reference") {
115
116
           settings.executor = gko::ReferenceExecutor::create();
117
118
           auto exec_info =
119
               static_cast<gko::ReferenceExecutor *>(settings.executor.get())
120
                    ->get_exec_info();
           exec_info->bind_to_core(my_local_rank);
121
       }
122
```

7.13.3 Member Function Documentation

7.13.3.1 print_matrix()

The auxiliary function that prints a passed in CSR matrix.

Parameters

matrix	The matrix to be printed.
subd	The subdomain on which the vector exists.
name	The name of the matrix as a string.

7.13.3.2 print_vector()

```
template<typename ValueType = gko::default_precision, typename IndexType = gko::int32>
void schwz::SchwarzBase< ValueType, IndexType >::print_vector (
```

```
const std::shared_ptr< gko::matrix::Dense< ValueType >> & vector,
int subd,
std::string name )
```

The auxiliary function that prints a passed in vector.

Parameters

vector	The vector to be printed.
subd	The subdomain on which the vector exists.
name	The name of the vector as a string.

7.13.3.3 run()

The function that runs the actual solver and obtains the final solution.

Parameters

solution	The solution vector.
----------	----------------------

References schwz::Communicate< ValueType, IndexType >::exchange_boundary(), schwz::Settings::executor, schwz::SchwarzBase< ValueType, IndexType >::global_matrix, schwz::SchwarzBase< ValueType, IndexType >::global_rhs, schwz::SchwarzBase< ValueType, IndexType >::global_solution, schwz::SchwarzBase< Value
Type, IndexType >::interface_matrix, schwz::SchwarzBase< ValueType, IndexType >::last_solution, schwz::
SchwarzBase< ValueType, IndexType >::local_inv_perm, schwz::SchwarzBase< ValueType, IndexType >::local-perm, schwz::SchwarzBase< ValueType, Index
Type >::local_rhs, schwz::SchwarzBase< ValueType, IndexType >::local_perm, schwz::SchwarzBase< ValueType, Index
Type, IndexType >::comm_struct::msg_count, schwz::Communicate< ValueType, IndexType, IndexType >::comm_struct::num_neighbors_out, schwz::communicate< ValueType, IndexType >::comm_struct::num_neighbors_out, schwz::communicate< ValueType, IndexType >::triangular_factor_u, sch

```
326 {
327
        using vec_vtype = gko::matrix::Dense<ValueType>;
328
        if (!solution.get()) {
329
            solution =
330
                vec_vtype::create(settings.executor->get_master(),
331
                                  gko::dim<2>(this->metadata.global_size, 1));
332
333
        // The main solution vector
334
        std::shared_ptr<vec_vtype> global_solution = vec_vtype::create(
335
            this->settings.executor, gko::dim<2>(this->metadata.global_size, 1));
336
337
        //CHANGED
        auto num_neighbors_out = this->comm_struct.num_neighbors_out;
338
339
       auto neighbors_out = this->comm_struct.neighbors_out->get_data();
340
        // The last communicated solution vector
341
342
        std::shared_ptr<vec_vtype> last_solution = vec_vtype::create(
343
            settings.executor, gko::dim<2>(metadata.global_size, 1));
344
        //END CHANGED
345
        // A work vector.
```

```
347
        std::shared_ptr<vec_vtype> work_vector = vec_vtype::create(
            settings.executor, gko::dim<2>(2 * this->metadata.local_size_x, 1));
348
        // An initial guess.
349
350
        std::shared_ptr<vec_vtype> init_guess = vec_vtype::create(
        settings.executor, gko::dim<2>(this->metadata.local_size_x, 1));
init_guess->copy_from(local_rhs.get());
351
352
353
354
         // Setup the windows for the onesided communication.
355
        this->setup_windows(this->settings, this->metadata, global_solution);
356
357
        const auto solver_settings =
             (Settings::local_solver_settings::direct_solver_cholmod |
358
              Settings::local_solver_settings::direct_solver_umfpack |
359
360
              Settings::local_solver_settings::direct_solver_ginkgo
361
              Settings::local_solver_settings::iterative_solver_dealii
362
              Settings::local_solver_settings::iterative_solver_ginkgo) &
363
             settings.local_solver;
364
365
        ValueType local_residual_norm = -1.0, local_residual_norm0 = -1.0,
                   global_residual_norm = 0.0, global_residual_norm0 = -1.0;
366
367
        metadata.iter_count = 0;
368
        int num_converged_procs = 0;
369
        //CHANGED - file writing
370
        char send_name[30], recv_name[30], pe_str[3]; sprintf(pe_str, "%d", metadata.my_rank);
371
372
373
374
        strcpy(send_name, "send");
        strcat(send_name, pe_str);
strcat(send_name, ".txt");
375
376
377
378
        strcpy(recv name, "recv");
        strcat(recv_name, pe_str);
strcat(recv_name, ".txt");
379
380
381
        std::ofstream fps; //file for sending log
382
383
        fps.open(send_name);
384
385
        std::ofstream fpr; //file for receiving log
386
        fpr.open(recv_name);
387
        if (metadata.my rank == 0) std::cout << "Constant - " << metadata.constant << ", Gamma - " << metadata.</pre>
388
      gamma <<std::endl:
389
        //END CHANGED
390
        auto start_time = std::chrono::steady_clock::now();
391
392
        for (; metadata.iter_count < metadata.max_iters; ++(metadata.iter_count)) {</pre>
393
             // Exchange the boundary values. The communication part.
            MEASURE_ELAPSED_FUNC_TIME (
394
395
                this->exchange boundary (settings, metadata, global solution, last solution,
      fps, fpr), 0,
396
                metadata.my_rank, boundary_exchange, metadata.iter_count);
397
398
             // Update the boundary and interior values after the exchanging from
             // other processes.
399
            MEASURE_ELAPSED_FUNC_TIME (
400
401
                 this->update_boundary(settings, metadata, this->
      local solution.
402
                                         this->local_rhs, global_solution,
403
                                         this->interface_matrix),
404
                 1, metadata.my_rank, boundary_update, metadata.iter_count);
405
406
             // Check for the convergence of the solver.
407
             // num_converged_procs = 0;
408
            MEASURE_ELAPSED_FUNC_TIME(
409
                 (Solve<ValueType, IndexType>::check_convergence(
410
                     settings, metadata, this->comm_struct, this->convergence_vector,
                     global_solution, this->local_solution, this->
411
      local matrix.
412
                      work_vector, local_residual_norm, local_residual_norm0,
413
                     global_residual_norm, global_residual_norm0,
414
                     num_converged_procs)),
415
                 2, metadata.my_rank, convergence_check, metadata.iter_count);
416
             // break if the solution diverges.
417
             if (std::isnan(global_residual_norm) || global_residual_norm > 1e12) {
418
                 std::cout << " Rank " << metadata.my_rank << " diverged in " << metadata.iter_count << " iters " << std::endl;
419
420
421
                 std::exit(-1);
            }
422
423
424
             // break if all processes detect that all other processes have
                converged otherwise continue iterations.
425
426
                (num_converged_procs == metadata.num_subdomains) {
427
                 break;
428
             } else {
                 MEASURE_ELAPSED_FUNC_TIME(
429
```

```
430
                    (Solve<ValueType, IndexType>::local_solve(
                        settings, metadata, this->local_matrix,
431
432
                        this->triangular_factor_l, this->
      triangular_factor_u,
433
                        this->local_perm, this->local_inv_perm, work_vector,
init_quess, this->local_solution)),
434
                    3, metadata.my_rank, local_solve, metadata.iter_count);
435
436
                // Gather the local vector into the locally global vector for
437
                // communication.
438
               MEASURE ELAPSED FUNC TIME (
                    (Communicate<ValueType, IndexType>::local_to_global_vector
439
      (
440
                        settings, metadata, this->local_solution, global_solution)),
                    4, metadata.my_rank, expand_local_vec, metadata.iter_count);
441
442
            }
443
       }
444
        MPI Barrier (MPI COMM WORLD);
445
446
        auto elapsed_time = std::chrono::duration<ValueType>(
447
           std::chrono::steady_clock::now() - start_time);
448
449
        //CHANGED
450
        //Closing file
451
        fps.close():
452
        fpr.close();
453
454
        //adding 1 to include the 0-th iteration
455
        metadata.iter_count = metadata.iter_count + 1;
456
        //number of messages a PE would send without event-based
457
458
        int noevent msg count = metadata.iter count * num neighbors out:
459
460
        int total_events = 0;
461
        //Printing msg count
462
        463
464
465
466
            total_events += this->comm_struct.msg_count->get_data()[k];
467
468
        std::cout << std::endl;
469
        //Total no of messages in all PEs
470
471
        MPI_Allreduce(MPI_IN_PLACE, &total_events, 1, MPI_INT, MPI_SUM, MPI_COMM_WORLD);
472
        MPI_Allreduce(MPI_IN_PLACE, &noevent_msg_count, 1, MPI_INT, MPI_SUM, MPI_COMM_WORLD);
473
474
        if (metadata.my_rank == 0) {
         std::cout << "Total number of events - " << total_events << std::endl;
475
         std::cout << "Total number of msgs without event - " << noevent_msg_count << std::endl;
476
477
478
        //END CHANGED
479
        480
481
482
483
        // Write the residuals and iterations to files
484
485
        if (settings.write_iters_and_residuals &&
486
           solver_settings ==
487
                Settings::local_solver_settings::iterative_solver_ginkgo) {
           std::string rank_string = std::to_string(metadata.my_rank);
if (metadata.my_rank < 10) {
   rank_string = "0" + std::to_string(metadata.my_rank);</pre>
488
489
490
491
492
            std::string filename = "iter_res_" + rank_string + ".csv";
493
            write_iters_and_residuals(
494
               metadata.num_subdomains, metadata.my_rank,
495
                metadata.post_process_data.local_residual_vector_out.size(),
496
                metadata.post process data.local residual vector out,
497
                metadata.post_process_data.local_converged_iter_count,
498
                metadata.post_process_data.local_converged_resnorm, filename);
499
500
        // Compute the final residual norm. Also gathers the solution from all
501
        // subdomains.
502
503
        Solve<ValueType, IndexType>::compute_residual_norm(
            settings, metadata, global_matrix, global_rhs, global_solution,
504
505
            mat_norm, rhs_norm, sol_norm, residual_norm);
506
        gather_comm_data<ValueType, IndexType>(
           metadata.num_subdomains, this->comm_struct, metadata.comm_data_struct);
507
        // clang-format off
508
509
        if (metadata.my_rank == 0)
510
511
            std::cout
                  << " residual norm " << residual_norm << "\n"
512
                  << " relative residual norm of solution " << residual_norm/rhs_norm << "\n"
<< " Time taken for solve " << elapsed_time.count()</pre>
513
514
```

```
<< std::endl;
             if (num_converged_procs < metadata.num_subdomains)</pre>
517
                std::cout << " Did not converge in " << metadata.iter_count << " iterations."
518
519
                           << std::endl;
520
521
522
523
       // clang-format on
        if (metadata.my_rank == 0) {
524
            solution->copy_from(global_solution.get());
525
526
528
        // Communicate<ValueType, IndexType>::clear(settings);
529 }
```

The documentation for this class was generated from the following files:

- schwarz base.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/schwarz_base.cpp (5af933a)

7.14 schwz::Settings Struct Reference

The struct that contains the solver settings and the parameters to be set by the user.

```
#include <settings.hpp>
```

Classes

struct comm_settings

The settings for the various available communication paradigms.

• struct convergence_settings

The various convergence settings available.

Public Types

• enum partition_settings

The partition algorithm to be used for partitioning the matrix.

• enum local_solver_settings

The local solver algorithm for the local subdomain solves.

Public Attributes

· std::string executor_string

The string that contains the ginkgo executor paradigm.

std::shared ptr< gko::Executor > executor = gko::ReferenceExecutor::create()

The ginkgo executor the code is to be executed on.

std::shared_ptr< device_guard > cuda_device_guard

The ginkgo executor the code is to be executed on.

• gko::int32 overlap = 2

The overlap between the subdomains.

• std::string matrix_filename = "null"

The string that contains the matrix file name to read from .

bool explicit_laplacian = true

Flag if the laplacian matrix should be generated within the library.

• bool enable random rhs = false

Flag to enable a random rhs.

bool print matrices = false

Flag to enable printing of matrices.

bool debug_print = false

Flag to enable some debug printing.

• bool non_symmetric_matrix = false

Is the matrix non-symmetric?, Use GMRES for local solves.

• unsigned int restart_iter = 1u

The restart iter for the GMRES solver.

bool naturally_ordered_factor = false

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

std::string metis_objtype

This setting defines the objective type for the metis partitioning.

• bool use_precond = false

Enable the block jacobi local preconditioner for the local solver.

bool write_debug_out = false

Enable the writing of debug out to file.

bool write_iters_and_residuals = false

Enable writing the iters and residuals to a file.

• bool write_perm_data = false

Enable the local permutations from CHOLMOD to a file.

• int shifted_iter = 1

Iteration shift for node local communication.

• std::string factorization = "cholmod"

The factorization for the local direct solver.

· std::string reorder

The reordering for the local solve.

7.14.1 Detailed Description

The struct that contains the solver settings and the parameters to be set by the user.

settings

7.14.2 Member Data Documentation

7.14.2.1 explicit_laplacian

```
bool schwz::Settings::explicit_laplacian = true
```

Flag if the laplacian matrix should be generated within the library.

If false, an external matrix and rhs needs to be provided

 $Referenced\ by\ schwz:: Schwarz Base < Value Type,\ Index Type > :: initialize ().$

7.14.2.2 naturally_ordered_factor

```
bool schwz::Settings::naturally_ordered_factor = false
```

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

Note

This is mainly to allow compatibility with GPU solution.

The documentation for this struct was generated from the following file:

settings.hpp (5af933a)

7.15 schwz::Solve < ValueType, IndexType > Class Template Reference

The Solver class the provides the solver and the convergence checking methods.

```
#include <solve.hpp>
```

Additional Inherited Members

7.15.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::Solve< ValueType, IndexType >

The Solver class the provides the solver and the convergence checking methods.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

Solve

The documentation for this class was generated from the following files:

- solve.hpp (5af933a)
- · /home/runner/work/schwarz-lib/schwarz-lib/source/solve.cpp (5af933a)

7.16 schwz::SolverRAS < ValueType, IndexType > Class Template Reference

An implementation of the solver interface using the RAS solver.

```
#include <restricted_schwarz.hpp>
```

Public Member Functions

SolverRAS (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

void setup_local_matrices (Settings &settings, Metadata < ValueType, IndexType > &metadata, std::vector < unsigned int > &partition_indices, std::shared_ptr < gko::matrix::Csr < ValueType, IndexType >> &global_
 matrix, std::shared_ptr < gko::matrix::Csr < ValueType, IndexType >> &local_matrix, std::shared_ptr < gko
 ::matrix::Csr < ValueType, IndexType >> &interface_matrix) override

Sets up the local and the interface matrices from the global matrix and the partition indices.

· void setup comm buffers () override

Sets up the communication buffers needed for the boundary exchange.

Sets up the windows needed for the asynchronous communication.

• void exchange_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense< ValueType >> &solution, std::shared_ptr< gko::matrix::

Dense< ValueType >> &last solution, std::ofstream &fpr, std::ofstream &fpr) override

Exchanges the elements of the solution vector.

void update_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared_ptr< gko::matrix::Dense< ValueType >> &local_solution, const std::shared_ptr< gko::matrix::Dense< ValueType >> &global = _solution, const std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> &interface_matrix) override

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Additional Inherited Members

7.16.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::SolverRAS< ValueType, IndexType >

An implementation of the solver interface using the RAS solver.

Template Parameters

ValueType	The type of the floating point values.
IndexType	The type of the index type values.

7.16.2 Constructor & Destructor Documentation

7.16.2.1 SolverRAS()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

Parameters

settings	The settings struct.
metadata	The metadata struct.
data	The additional data struct.

```
50 : SchwarzBase<ValueType, IndexType>(settings, metadata)
51 {}
```

7.16.3 Member Function Documentation

7.16.3.1 exchange_boundary()

Exchanges the elements of the solution vector.

Parameters

settings	The settings struct.
metadata	The metadata struct.
global_solution	The solution vector being exchanged between the subdomains.

Implements schwz::Communicate < ValueType, IndexType >.

References schwz::Settings::comm_settings::enable_onesided, schwz::SchwarzBase< ValueType, IndexType $> \leftarrow$::global_solution, and schwz::SchwarzBase< ValueType, IndexType > :: :last_solution.

7.16.3.2 setup_local_matrices()

Sets up the local and the interface matrices from the global matrix and the partition indices.

Parameters

settings	The settings struct.
metadata	The metadata struct.
partition_indices	The array containing the partition indices.
global_matrix	The global system matrix.
local_matrix	The local system matrix.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.
local_perm	The local permutation, obtained through RCM or METIS.

Implements schwz::Initialize < ValueType, IndexType >.

References schwz::Metadata< ValueType, IndexType >::comm_size, schwz::Settings::executor, schwz::← Metadata< ValueType, IndexType >::first_row, schwz::SchwarzBase< ValueType, IndexType >::global_matrix, schwz::Metadata< ValueType, IndexType >::global_size, schwz::Metadata< ValueType, IndexType >::global_to← _local, schwz::Metadata< ValueType, IndexType >::i_permutation, schwz::SchwarzBase< ValueType, IndexType >::interface_matrix, schwz::Metadata< Value← Type, IndexType >::local_size, schwz::Metadata< ValueType, IndexType >::local_size_o, schwz::Metadata< ValueType, IndexType >::local_size_o, schwz::Metadata< ValueType, IndexType >::local_to_global, schwz::← Metadata< ValueType, IndexType >::num_subdomains, schwz::Settings::overlap, schwz::Metadata< ValueType, IndexType >::overlap_row, schwz::Metadata< ValueType, IndexType >::overlap_size, and schwz::Metadata< ValueType, IndexType >::permutation.

```
62
       using mtx = gko::matrix::Csr<ValueType, IndexType>;
       using vec_itype = gko::Array<IndexType>;
using perm_type = gko::matrix::Permutation<IndexType>;
using arr = gko::Array<IndexType>;
63
64
65
       auto my_rank = metadata.my_rank;
       auto comm_size = metadata.comm_size;
68
       auto num_subdomains = metadata.num_subdomains;
69
       auto global_size = metadata.global_size;
70
       auto mpi_itype = boost::mpi::get_mpi_datatype(*partition_indices.data());
71
72
       MPI_Bcast(partition_indices.data(), global_size, mpi_itype, 0,
                  MPI_COMM_WORLD);
75
       std::vector<IndexType> local_p_size(num_subdomains);
76
       auto global_to_local = metadata.global_to_local->get_data();
       auto local_to_global = metadata.local_to_global->get_data();
77
79
       auto first_row = metadata.first_row->get_data();
       auto permutation = metadata.permutation->get_data();
80
81
       auto i_permutation = metadata.i_permutation->get_data();
82
83
       auto nb = (global_size + num_subdomains - 1) /
      num_subdomains;
       auto partition_settings =
```

```
85
            (Settings::partition_settings::partition_zoltan |
             Settings::partition_settings::partition_metis
86
87
             Settings::partition_settings::partition_regular
88
             Settings::partition_settings::partition_regular2d |
89
            Settings::partition_settings::partition_custom) &
90
            settings.partition:
91
92
       IndexType *gmat_row_ptrs = global_matrix->get_row_ptrs();
93
       IndexType *gmat_col_idxs = global_matrix->get_col_idxs();
94
       ValueType *gmat_values = global_matrix->get_values();
95
96
        // default local p size set for 1 subdomain.
       first_row[0] = 0;
       for (auto p = 0; p < num_subdomains; ++p)</pre>
98
99
       {
             local_p_size[p] = std::min(global_size - first_row[p], nb);
first_row[p + 1] = first_row[p] + local_p_size[p];
100
101
        }
102
103
104
        if (partition_settings == Settings::partition_settings::partition_metis ||
105
            partition_settings == Settings::partition_settings::partition_regular2d)
106
107
             if (num_subdomains > 1)
108
109
                 for (auto p = 0; p < num_subdomains; p++)</pre>
110
111
                      local_p_size[p] = 0;
112
                 for (auto i = 0; i < global_size; i++)</pre>
113
114
115
                     local_p_size[partition_indices[i]]++;
116
117
                 first_row[0] = 0;
                 for (auto p = 0; p < num_subdomains; ++p)</pre>
118
119
                      first_row[p + 1] = first_row[p] + local_p_size[p];
120
121
122
                 // permutation
123
                 for (auto i = 0; i < global_size; i++)</pre>
124
125
                      permutation[first_row[partition_indices[i]]] = i;
126
                      first_row[partition_indices[i]]++;
127
128
                 for (auto p = num_subdomains; p > 0; p--)
129
130
                      first_row[p] = first_row[p - 1];
131
132
                 first_row[0] = 0;
133
134
                 // iperm
135
                 for (auto i = 0; i < global_size; i++)</pre>
136
137
                      i_permutation[permutation[i]] = i;
138
139
140
141
            auto gmat_temp = mtx::create(settings.executor->get_master(),
142
                                            global_matrix->get_size(),
143
                                            global_matrix->get_num_stored_elements());
144
145
            auto nnz = 0:
146
             gmat_temp->get_row_ptrs()[0] = 0;
147
             for (auto row = 0; row < metadata.global_size; ++row)</pre>
148
149
                 for (auto col = gmat_row_ptrs[permutation[row]];
150
                      col < gmat_row_ptrs[permutation[row] + 1]; ++col)</pre>
151
                     gmat_temp->get_col_idxs()[nnz] =
152
153
                         i_permutation[gmat_col_idxs[col]];
154
                     gmat_temp->get_values()[nnz] = gmat_values[col];
155
156
157
                 gmat_temp->get_row_ptrs()[row + 1] = nnz;
158
159
             global matrix->copy from(gmat temp.get());
160
161
        for (auto i = 0; i < global_size; i++)</pre>
162
163
             global_to_local[i] = 0;
             local_to_global[i] = 0;
164
165
        for (auto i = first_row[my_rank]; i < first_row[</pre>
166
167
      my_rank + 1]; i++)
168
             global_to_local[i] = 1 + num;
169
             local_to_global[num] = i;
170
```

```
171
            num++;
172
        }
173
174
        IndexType old = 0;
175
        for (auto k = 1; k < settings.overlap; k++)
176
177
             auto now = num;
178
             for (auto i = old; i < now; i++)</pre>
179
180
                 for (auto j = gmat_row_ptrs[local_to_global[i]];
181
                      j < gmat_row_ptrs[local_to_global[i] + 1]; j++)</pre>
182
183
                      if (global to local[gmat col idxs[j]] == 0)
184
185
                          local_to_global[num] = gmat_col_idxs[j];
186
                          global_to_local[gmat_col_idxs[j]] = 1 + num;
187
                          n11m++:
188
                     }
189
                 }
190
191
             old = now;
192
193
        metadata.local_size = local_p_size[my_rank];
194
        metadata.local_size_x = num;
195
        metadata.local_size_o = global_size;
        auto local_size = metadata.local_size;
196
197
        auto local_size_x = metadata.local_size_x;
198
199
        metadata.overlap_size = num - metadata.local_size;
200
        metadata.overlap_row = std::shared_ptr<vec_itype>(
201
            new vec_itype(gko::Array<IndexType>::view(
202
                 settings.executor, metadata.overlap_size,
203
                 & (metadata.local_to_global->get_data()[metadata.local_size]))),
204
            std::default_delete<vec_itype>());
205
        auto nnz_local = 0;
206
207
        auto nnz_interface = 0;
208
209
        for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i)</pre>
210
211
             for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; j++)</pre>
212
213
                 if (global_to_local[gmat_col_idxs[j]] != 0)
214
                 {
215
                     nnz_local++;
216
                 }
217
                 else
218
                     std::cout << " debug: invalid edge?" << std::endl;
219
220
221
            }
222
223
        auto temp = 0;
224
        for (auto k = 0; k < metadata.overlap_size; k++)</pre>
225
226
             temp = metadata.overlap row->get data()[k];
             for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1]; j++)</pre>
228
229
                 if (global_to_local[gmat_col_idxs[j]] != 0)
230
2.31
                     nnz local++;
232
233
                 else
234
                 {
235
                     nnz_interface++;
236
237
238
        }
239
240
        std::shared_ptr<mtx> local_matrix_compute;
241
        local_matrix_compute = mtx::create(settings.executor->get_master(),
242
                                              gko::dim<2>(local_size_x), nnz_local);
        IndexType *lmat_row_ptrs = local_matrix_compute->get_row_ptrs();
IndexType *lmat_col_idxs = local_matrix_compute->get_col_idxs();
243
244
245
        ValueType *lmat_values = local_matrix_compute->get_values();
246
247
        std::shared_ptr<mtx> interface_matrix_compute;
248
        if (nnz_interface > 0)
249
250
             interface matrix compute =
251
                mtx::create(settings.executor->get master(),
252
                              gko::dim<2>(local_size_x), nnz_interface);
253
254
        else
255
256
             interface_matrix_compute = mtx::create(settings.executor->get_master());
257
```

```
258
         IndexType *imat_row_ptrs = interface_matrix_compute->get_row_ptrs();
IndexType *imat_col_idxs = interface_matrix_compute->get_col_idxs();
259
260
2.61
        ValueType *imat_values = interface_matrix_compute->get_values();
2.62
263
        num = 0;
264
        nnz_local = 0;
265
         auto nnz_interface_temp = 0;
266
         lmat_row_ptrs[0] = nnz_local;
2.67
         if (nnz_interface > 0)
268
269
              imat_row_ptrs[0] = nnz_interface_temp;
270
        }
271
272
         // Local interior matrix
273
         for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i)</pre>
274
275
             for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; ++j)</pre>
276
277
                  if (global_to_local[gmat_col_idxs[j]] != 0)
278
279
                      lmat_col_idxs[nnz_local] =
280
                          global_to_local[gmat_col_idxs[j]] - 1;
                      lmat_values[nnz_local] = gmat_values[j];
281
282
                      nnz_local++;
283
284
285
             if (nnz_interface > 0)
286
287
                  imat_row_ptrs[num + 1] = nnz_interface_temp;
288
289
             lmat_row_ptrs[num + 1] = nnz_local;
290
291
292
        // Interface matrix
293
294
         if (nnz_interface > 0)
295
296
             nnz_interface = 0;
297
             for (auto k = 0; k < metadata.overlap_size; k++)</pre>
298
299
                  temp = metadata.overlap_row->get_data()[k];
300
                  for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1];</pre>
301
                       j++)
302
303
                      if (global_to_local[gmat_col_idxs[j]] != 0)
304
305
                           lmat_col_idxs[nnz_local] =
                           global_to_local[gmat_col_idxs[j]] - 1;
lmat_values[nnz_local] = gmat_values[j];
306
307
308
                           nnz_local++;
309
310
                      else
311
                           imat_col_idxs[nnz_interface] = gmat_col_idxs[j];
312
                           imat_values[nnz_interface] = gmat_values[j];
313
314
                           nnz_interface++;
315
316
317
                  lmat_row_ptrs[num + 1] = nnz_local;
                  imat_row_ptrs[num + 1] = nnz_interface;
318
319
                  num++;
320
             }
321
322
         auto now = num;
323
         for (auto i = old; i < now; i++)
324
             for (auto j = gmat_row_ptrs[local_to_global[i]];
325
                   j < gmat_row_ptrs[local_to_global[i] + 1]; j++)</pre>
326
327
328
                  if (global_to_local[gmat_col_idxs[j]] == 0)
329
330
                      local_to_global[num] = gmat_col_idxs[j];
331
                      global_to_local[gmat_col_idxs[j]] = 1 + num;
332
                      num++;
333
                  }
334
335
336
337
         local matrix = mtx::create(settings.executor);
        local_matrix = mtx::create(settings.caceta);
local_matrix = mtx::create(settings.executor);
338
339
340
         interface_matrix->copy_from(gko::lend(interface_matrix_compute));
341
342
         local_matrix->sort_by_column_index();
343
         interface_matrix->sort_by_column_index();
344 }
```

7.16.3.3 setup windows()

Sets up the windows needed for the asynchronous communication.

Parameters

settings	The settings struct.
metadata	The metadata struct.
main_buffer	The main buffer being exchanged between the subdomains.

Implements schwz::Communicate < ValueType, IndexType >.

References schwz::Metadata < ValueType, IndexType >::constant, schwz::Communicate < ValueType, Index ← Type >::comm struct::curr recv avg, schwz::Communicate< ValueType, IndexType >::comm struct::curr ← send_avg, schwz::Settings::comm_settings::enable_flush_all, schwz::Settings::comm_settings::enable_flush_← local, schwz::Settings::comm_settings::enable_get, schwz::Settings::comm_settings::enable_lock_all, schwz⇔ ::Settings::comm_settings::enable_one_by_one, schwz::Settings::comm_settings::enable_onesided, schwz::⇔ Settings::comm_settings::enable_overlap, schwz::Settings::comm_settings::enable_put, schwz::Settings::executor, schwz::Metadata< ValueType, IndexType >::gamma, schwz::Communicate< ValueType, IndexType >::comm_← struct::get_displacements, schwz::Communicate< ValueType, IndexType >::comm_struct::get_request, schwz← ::Communicate< ValueType, IndexType >::comm struct::global get, schwz::Communicate< ValueType, Index↔ Type >::comm struct::global put, schwz::SchwarzBase< ValueType, IndexType >::global solution, schwz::← Communicate < ValueType, IndexType >::comm_struct::is_local_neighbor, schwz::Metadata < ValueType, Index ← Type >::iter_count, schwz::Communicate< ValueType, IndexType >::comm_struct::last_recv_avg, schwz::← Communicate < ValueType, IndexType >::comm struct::last recv bdy, schwz::Communicate < ValueType, Index← Type >::comm_struct::last_recv_iter, schwz::Communicate < ValueType, IndexType >::comm_struct::last_send_ ← avg, schwz::SchwarzBase< ValueType, IndexType >::last_solution, schwz::Communicate< ValueType, IndexType >::comm_struct::local_get, schwz::Communicate< ValueType, IndexType >::comm_struct::local_neighbors_ in, schwz::Communicate < ValueType, IndexType >::comm struct::local neighbors out, schwz::Communicate < ValueType, IndexType >::comm struct::local num neighbors in, schwz::Communicate< ValueType, Index← Type >::comm struct::local num neighbors out, schwz::Communicate< ValueType, IndexType >::comm ← struct::local put, schwz::Metadata< ValueType, IndexType >::local size o, schwz::SchwarzBase< Value↔ Type, IndexType >::local_solution, schwz::Communicate < ValueType, IndexType >::comm_struct::msg_count, schwz::Communicate< ValueType, IndexType >::comm_struct::neighbors_in, schwz::Communicate< Value -Type, IndexType >::comm_struct::neighbors_out, schwz::Communicate< ValueType, IndexType >::comm_← struct::num_neighbors_in, schwz::Communicate< ValueType, IndexType >::comm_struct::num_neighbors_out, schwz::Metadata< ValueType, IndexType >::num_subdomains, schwz::Communicate< ValueType, IndexType >::comm_struct::put_displacements, schwz::Communicate< ValueType, IndexType >::comm_struct::put_c request, schwz::Communicate< ValueType, IndexType >::comm_struct::recv_buffer, schwz::Communicate< ValueType, IndexType >::comm struct::remote get, schwz::Communicate< ValueType, IndexType >::comm ← struct::remote put, schwz::Communicate< ValueType, IndexType >::comm struct::sec last recv bdy, schwz ::Communicate< ValueType, IndexType >::comm_struct::sec_last_recv_iter, schwz::Communicate< ValueType, IndexType >::comm struct::send buffer, schwz::Communicate< ValueType, IndexType >::comm struct::third ← last recv bdy, schwz::Communicate< ValueType, IndexType >::comm struct::third last recv iter, schwz::← Communicate < ValueType, IndexType >::comm struct::window recv buffer, schwz::Communicate < ValueType, IndexType >::comm_struct::window_send_buffer, and schwz::Communicate< ValueType, IndexType >::comm_← struct::window x.

```
651 {
652
        using vec_itype = gko::Array<IndexType>;
653
        using vec_vtype = gko::matrix::Dense<ValueType>;
654
        auto num_subdomains = metadata.num_subdomains;
655
        auto local_size_o = metadata.local_size_o;
        auto neighbors_in = this->comm_struct.neighbors_in->qet_data();
656
657
        auto global_get = this->comm_struct.global_get->get_data();
658
        auto neighbors_out = this->comm_struct.neighbors_out->get_data();
659
        auto global_put = this->comm_struct.global_put->get_data();
660
661
        // set displacement for the MPI buffer
662
        auto get_displacements = this->comm_struct.get_displacements->get_data();
        auto put_displacements = this->comm_struct.put_displacements->get_data();
663
664
            std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
665
666
            tmp_num_comm_elems[0] = 0;
            for (auto j = 0; j < this->comm_struct.num_neighbors_in; j++) {
667
                if ((global_get[j])[0] > 0) {
   int p = neighbors_in[j];
668
669
670
                     tmp_num_comm_elems[p + 1] = (global_get[j])[0];
671
672
            for (auto j = 0; j < num_subdomains; j++) {
   tmp_num_comm_elems[j] + 1] += tmp_num_comm_elems[j];</pre>
673
674
675
676
677
            auto mpi_itype = boost::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
678
            MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, put_displacements,
679
                          1, mpi_itype, MPI_COMM_WORLD);
680
        }
681
682
683
            std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
684
            tmp_num_comm_elems[0] = 0;
685
            for (auto j = 0; j < this->comm_struct.num_neighbors_out; j++) {
                 if ((global_put[j])[0] > 0) {
686
687
                     int p = neighbors_out[j];
688
                     tmp_num_comm_elems[p + 1] = (global_put[j])[0];
689
690
691
            for (auto j = 0; j < num_subdomains; j++) {</pre>
692
                tmp_num_comm_elems[j + 1] += tmp_num_comm_elems[j];
693
694
695
            auto mpi_itype = boost::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
696
            MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, get_displacements,
697
                          1, mpi_itype, MPI_COMM_WORLD);
698
699
700
        // setup windows
701
        if (settings.comm_settings.enable_onesided)
702
703
             // Onesided
            704
705
                            sizeof(ValueType), MPI_INFO_NULL, MPI_COMM_WORLD,
706
                            &(this->comm_struct.window_x));
707
708
709
710
        if (settings.comm_settings.enable_onesided)
711
712
             // MPI Alloc mem ? Custom allocator ? TODO
713
            MPI_Win_create(this->local_residual_vector->get_values(),
                             (num_subdomains) * sizeof(ValueType), sizeof(ValueType),
714
715
                            MPI_INFO_NULL, MPI_COMM_WORLD,
716
                            &(this->window_residual_vector));
            std::vector<IndexType> zero_vec(num_subdomains, 0);
717
718
            \verb|gko::Array<IndexType>| temp\_array(settings.executor->get\_master()|,
719
                                               zero vec.begin(), zero vec.end() };
720
            this->convergence_vector = std::shared_ptr<vec_itype>(
721
                new vec_itype(settings.executor->get_master(), temp_array),
722
                 std::default_delete<vec_itype>());
723
            this->convergence_sent = std::shared_ptr<vec_itype>(
724
                new vec_itype(settings.executor->get_master(), num_subdomains),
725
                std::default delete<vec itvpe>());
726
            this->convergence_local = std::shared_ptr<vec_itype>(
727
                new vec_itype(settings.executor->get_master(), num_subdomains),
728
                 std::default_delete<vec_itype>());
729
            \label{lem:mpi_win_create} \texttt{MPI\_Win\_create(this-} \\ \texttt{convergence\_vector-} \\ \texttt{get\_data(),}
                             (num_subdomains) * sizeof(IndexType), sizeof(IndexType),
730
                            MPI_INFO_NULL, MPI_COMM_WORLD,
731
732
                            &(this->window_convergence));
733
734
735
         \  \  \, \text{if (settings.comm\_settings.enable\_onesided \&\& num\_subdomains} \, > \, 1) \\
736
737
            // Lock all windows.
```

```
if (settings.comm_settings.enable_get &&
                settings.comm_settings.enable_lock_all) {
740
                //MPI_Win_lock_all(0, this->comm_struct.window_send_buffer);
741
742
            if (settings.comm_settings.enable_put &&
743
                settings.comm_settings.enable_lock_all) {
                //MPI_Win_lock_all(0, this->comm_struct.window_recv_buffer);
745
            if (settings.comm_settings.enable_one_by_one &&
746
747
                settings.comm_settings.enable_lock_all)
748
                //MPI_Win_lock_all(0, this->comm_struct.window_x);
749
750
            MPI_Win_lock_all(0, this->window_residual_vector);
751
           MPI_Win_lock_all(0, this->window_convergence);
752
753 }
```

7.16.3.4 update_boundary()

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

Parameters

settings	The settings struct.
metadata	The metadata struct.
local_solution	The local solution vector in the subdomain.
local_rhs	The local right hand side vector in the subdomain.
global_solution	The workspace solution vector.
global_old_solution	The global solution vector of the previous iteration.
interface_matrix	The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains.

 $Implements\ schwz:: Communicate < Value Type,\ Index Type >.$

References schwz::Settings::executor, schwz::SchwarzBase< ValueType, IndexType >::global_solution, schwz::SchwarzBase< ValueType, IndexType >::interface_matrix, schwz::SchwarzBase< ValueType, IndexType >::local_rhs, schwz::Metadata< ValueType, IndexType >::local_size_x, schwz::SchwarzBase< ValueType, Indextype >::local_solution, schwz::Metadata< ValueType, IndexType >::num_subdomains, and schwz::Settings::overlap.

```
if (metadata.num_subdomains > 1 && settings.overlap > 0) {
             auto temp_solution = vec_vtype::create()
settings.executor, local_solution->get_size(),
1173
1174
                  gko::Array<ValueType>::view(settings.executor,
                                                  local_solution->get_size()[0],
1175
1176
                                                  global_solution->get_values()),
1177
1178
              interface_matrix->apply(neg_one.get(), temp_solution.get(), one.get(),
1179
                                        local_solution.get());
1180
1181 }
```

The documentation for this class was generated from the following files:

- restricted_schwarz.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/restricted schwarz.cpp (5af933a)

7.17 UmfpackError Class Reference

UmfpackError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

Public Member Functions

UmfpackError (const std::string &file, int line, const std::string &func, int error_code)
 Initializes a METIS error.

7.17.1 Detailed Description

UmfpackError is thrown when a METIS routine throws a non-zero error code.

7.17.2 Constructor & Destructor Documentation

7.17.2.1 UmfpackError()

Initializes a METIS error.

Parameters

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the METIS routine that failed
error_code	The resulting METIS error code

```
205 : Error(file, line, func + ": " + get_error(error_code))
206      {}
```

The documentation for this class was generated from the following files:

- exception.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (5af933a)

7.18 schwz::Utils < ValueType, IndexType > Struct Template Reference

The utilities class which provides some checks and basic utilities.

```
#include <utils.hpp>
```

7.18.1 Detailed Description

template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> struct schwz::Utils< ValueType, IndexType >

The utilities class which provides some checks and basic utilities.

Template Parameters

_	ValueType	The type of the floating point values.
	IndexType	The type of the index type values.

Utils

The documentation for this struct was generated from the following files:

- utils.hpp (5af933a)
- /home/runner/work/schwarz-lib/schwarz-lib/source/utils.cpp (5af933a)

Index

BadDimension, 19 BadDimension, 19	ProcessTopology, 15
BadBimonolon, 10	remote get
Communicate, 9	schwz::Communicate::comm_struct, 24
CudaError, 29	remote_put
CudaError, 29	schwz::Communicate::comm_struct, 24
CusparseError, 30	run
CusparseError, 30	schwz::SchwarzBase, 45
exchange_boundary	Schwarz Class, 11
schwz::Communicate, 26	SchwarzBase
schwz::SolverRAS, 52	schwz::SchwarzBase, 43
explicit_laplacian	schwz, 15
schwz::Settings, 49	schwz::CommHelpers, 16
	schwz::Communicate
generate_dipole_rhs	exchange_boundary, 26
schwz::Initialize, 32	local_to_global_vector, 26
generate_random_rhs	setup_windows, 27
schwz::Initialize, 33	update_boundary, 27
generate_sin_rhs	schwz::Communicate < ValueType, IndexType >, 25
schwz::Initialize, 33	schwz::Communicate< ValueType, IndexType >-
global_get	::comm_struct, 21
schwz::Communicate::comm_struct, 23	schwz::Communicate::comm_struct
global_put	global_get, 23
schwz::Communicate::comm_struct, 23	global_put, 23
	is_local_neighbor, 23
Initialization, 10	local_get, 23
is_local_neighbor	local_put, 24
schwz::Communicate::comm_struct, 23	remote_get, 24
land not	remote_put, 24
local_get	schwz::Initialize
schwz::Communicate::comm_struct, 23	generate_dipole_rhs, 32
local_put	generate_random_rhs, 33
schwz::Communicate::comm_struct, 24	generate_sin_rhs, 33
local_solver_tolerance	partition, 34
schwz::Metadata, 40	setup_global_matrix, 35
local_to_global_vector	setup_local_matrices, 36
schwz::Communicate, 26	setup_vectors, 37
MetisError, 40	schwz::Initialize < ValueType, IndexType >, 31
MetisError, 41	schwz::Metadata
Metischor, 41	local_solver_tolerance, 40
naturally_ordered_factor	tolerance, 40
schwz::Settings, 49	schwz::Metadata < ValueType, IndexType >, 38
·	schwz::Metadata< ValueType, IndexType >::post_←
partition	process_data, 41
schwz::Initialize, 34	schwz::PartitionTools, 17
print_matrix	schwz::SchwarzBase
schwz::SchwarzBase, 44	print_matrix, 44
print_vector	print_vector, 44
schwz::SchwarzBase, 44	run. 45

64 INDEX

```
SchwarzBase, 43
schwz::SchwarzBase< ValueType, IndexType >, 42
schwz::Settings, 48
    explicit_laplacian, 49
    naturally_ordered_factor, 49
schwz::Settings::comm settings, 20
schwz::Settings::convergence_settings, 28
schwz::Solve < ValueType, IndexType >, 50
schwz::SolverRAS< ValueType, IndexType >, 50
schwz::SolverRAS
    exchange_boundary, 52
    setup_local_matrices, 52
    setup_windows, 57
    SolverRAS, 51
    update_boundary, 59
schwz::SolverTools, 17
schwz::Utils< ValueType, IndexType >, 61
schwz::conv_tools, 16
schwz::device_guard, 31
setup_global_matrix
    schwz::Initialize, 35
setup_local_matrices
    schwz::Initialize, 36
    schwz::SolverRAS, 52
setup_vectors
    schwz::Initialize, 37
setup_windows
    schwz::Communicate, 27
    schwz::SolverRAS, 57
Solve, 12
SolverRAS
    schwz::SolverRAS, 51
tolerance
    schwz::Metadata, 40
UmfpackError, 60
    UmfpackError, 60
update_boundary
    schwz::Communicate, 27
    schwz::SolverRAS, 59
Utils, 13
```