## schwz

Generated automatically from dealii-ex

Generated by Doxygen 1.8.13

# **Contents**

| 1 | Main  | Page                                      | 1  |
|---|-------|---|----|
| 2 | # Ins | stallation Instructions                   | 3  |
| 3 | Test  | ing Instructions                          | 5  |
| 4 | Bend  | chmarking.                                | 7  |
| 5 | Mod   | ule Documentation                         | 9  |
|   | 5.1   | Communicate                               | 9  |
|   |       | 5.1.1 Detailed Description                | 9  |
|   | 5.2   | Initialization                            | 10 |
|   |       | 5.2.1 Detailed Description                | 10 |
|   | 5.3   | Schwarz Class                             | 11 |
|   |       | 5.3.1 Detailed Description                | 11 |
|   | 5.4   | Solve                                     | 12 |
|   |       | 5.4.1 Detailed Description                | 12 |
|   | 5.5   | Utils                                     | 13 |
|   |       | 5.5.1 Detailed Description                | 13 |
| 6 | Nam   | espace Documentation                      | 15 |
|   | 6.1   | ProcessTopology Namespace Reference       | 15 |
|   |       | 6.1.1 Detailed Description                | 15 |
|   | 6.2   | schwz Namespace Reference                 | 15 |
|   |       | 6.2.1 Detailed Description                | 16 |
|   | 6.3   | schwz::CommHelpers Namespace Reference    | 16 |
|   |       | 6.3.1 Detailed Description                | 16 |
|   | 6.4   | schwz::conv_tools Namespace Reference     | 16 |
|   |       | 6.4.1 Detailed Description                | 16 |
|   | 6.5   | schwz::PartitionTools Namespace Reference | 17 |
|   |       | 6.5.1 Detailed Description                | 17 |
|   | 6.6   | schwz::SolverTools Namespace Reference    | 17 |
|   |       | 6.6.1 Detailed Description                | 17 |

ii CONTENTS

| 7 | Clas | s Docu | umentation   | 19 |
|---|------|--------|--|----|
|   | 7.1  | BadDii | mension Class Reference  | 19 |
|   |      | 7.1.1  | Detailed Description   | 19 |
|   |      | 7.1.2  | Constructor & Destructor Documentation                               | 19 |
|   |      |        | 7.1.2.1 BadDimension()   | 19 |
|   | 7.2  | schwz  | :::Settings::comm_settings Struct Reference                          | 20 |
|   |      | 7.2.1  | Detailed Description   | 21 |
|   | 7.3  | schwz  | :::Communicate< ValueType, IndexType >::comm_struct Struct Reference | 21 |
|   |      | 7.3.1  | Detailed Description   | 22 |
|   |      | 7.3.2  | Member Data Documentation  | 22 |
|   |      |        | 7.3.2.1 global_get   | 22 |
|   |      |        | 7.3.2.2 global_put   | 23 |
|   |      |        | 7.3.2.3 is_local_neighbor  | 23 |
|   |      |        | 7.3.2.4 local_get  | 23 |
|   |      |        | 7.3.2.5 local_put  | 23 |
|   |      |        | 7.3.2.6 remote_get   | 24 |
|   |      |        | 7.3.2.7 remote_put   | 24 |
|   | 7.4  | schwz  | :::Communicate < ValueType, IndexType > Class Template Reference     | 24 |
|   |      | 7.4.1  | Detailed Description   | 25 |
|   |      | 7.4.2  | Member Function Documentation  | 25 |
|   |      |        | 7.4.2.1 exchange_boundary()  | 25 |
|   |      |        | 7.4.2.2 local_to_global_vector()                                     | 26 |
|   |      |        | 7.4.2.3 setup_windows()  | 27 |
|   |      |        | 7.4.2.4 update_boundary()  | 27 |
|   | 7.5  | schwz  | :::Settings::convergence_settings Struct Reference                   | 28 |
|   |      | 7.5.1  | Detailed Description   | 28 |
|   | 7.6  | CudaE  | Error Class Reference  | 28 |
|   |      | 7.6.1  | Detailed Description   | 28 |
|   |      | 7.6.2  | Constructor & Destructor Documentation                               | 28 |
|   |      |        | 7.6.2.1 CudaError()  | 28 |

CONTENTS

| 7.7  | Cuspai | rseError Class Reference   | 29 |
|------|--------|--|----|
|      | 7.7.1  | Detailed Description   | 29 |
|      | 7.7.2  | Constructor & Destructor Documentation                                 | 29 |
|      |        | 7.7.2.1 CusparseError()  | 29 |
| 7.8  | schwz: | :device_guard Class Reference  | 30 |
|      | 7.8.1  | Detailed Description   | 30 |
| 7.9  | schwz: | :Initialize < ValueType, IndexType > Class Template Reference          | 30 |
|      | 7.9.1  | Detailed Description   | 31 |
|      | 7.9.2  | Member Function Documentation  | 31 |
|      |        | 7.9.2.1 generate_rhs()   | 32 |
|      |        | 7.9.2.2 partition()  | 32 |
|      |        | 7.9.2.3 setup_global_matrix()  | 33 |
|      |        | 7.9.2.4 setup_local_matrices()   | 34 |
|      |        | 7.9.2.5 setup_vectors()  | 35 |
| 7.10 | schwz: | :Metadata < ValueType, IndexType > Struct Template Reference           | 36 |
|      | 7.10.1 | Detailed Description   | 38 |
|      | 7.10.2 | Member Data Documentation  | 38 |
|      |        | 7.10.2.1 local_solver_tolerance  | 38 |
|      |        | 7.10.2.2 tolerance   | 38 |
| 7.11 | MetisE | rror Class Reference   | 38 |
|      | 7.11.1 | Detailed Description   | 39 |
|      | 7.11.2 | Constructor & Destructor Documentation                                 | 39 |
|      |        | 7.11.2.1 MetisError()  | 39 |
| 7.12 | schwz: | :Metadata < ValueType, IndexType >::post_process_data Struct Reference | 39 |
|      | 7.12.1 | Detailed Description   | 40 |
| 7.13 | schwz: | :SchwarzBase< ValueType, IndexType > Class Template Reference          | 40 |
|      | 7.13.1 | Detailed Description   | 41 |
|      | 7.13.2 | Constructor & Destructor Documentation                                 | 41 |
|      |        | 7.13.2.1 SchwarzBase()   | 41 |
|      | 7.13.3 | Member Function Documentation  | 42 |

iv CONTENTS

| Index |        |             |  | 61   |
|-------|--------|-------------|--|------|
|       | 7.18.1 | Detailed I  | Description  | . 58 |
| 7.18  | schwz: | :Utils< Val | lueType, IndexType > Struct Template Reference     | . 57 |
|       |        | 7.17.2.1    | UmfpackError()                                     | . 57 |
|       | 7.17.2 | Construct   | tor & Destructor Documentation                     | . 57 |
|       | 7.17.1 | Detailed I  | Description  | . 57 |
| 7.17  | Umfpa  | ckError Cla | ass Reference                                      | . 56 |
|       |        | 7.16.3.4    | update_boundary()                                  | . 55 |
|       |        | 7.16.3.3    | setup_windows()                                    | . 53 |
|       |        | 7.16.3.2    | setup_local_matrices()                             | . 50 |
|       |        | 7.16.3.1    | exchange_boundary()                                | . 49 |
|       | 7.16.3 | Member F    | Function Documentation                             | . 49 |
|       |        | 7.16.2.1    | SolverRAS()  | . 49 |
|       | 7.16.2 | Construct   | tor & Destructor Documentation                     | . 49 |
|       | 7.16.1 | Detailed I  | Description  | . 48 |
| 7.16  | schwz: | :SolverRAS  | S< ValueType, IndexType > Class Template Reference | . 48 |
|       | 7.15.1 | Detailed I  | Description  | . 47 |
| 7.15  | schwz: | :Solve< Va  | alueType, IndexType > Class Template Reference     | . 47 |
|       |        | 7.14.2.2    | naturally_ordered_factor                           | . 47 |
|       |        | 7.14.2.1    | explicit_laplacian                                 | . 47 |
|       | 7.14.2 | Member I    | Data Documentation                                 | . 47 |
|       | 7.14.1 | Detailed I  | Description  | . 46 |
| 7.14  | schwz: | :Settings S | Struct Reference                                   | . 45 |
|       |        | 7.13.3.3    | run()  | . 43 |
|       |        | 7.13.3.2    | print_vector()                                     | . 43 |
|       |        | 7.13.3.1    | print_matrix()                                     | . 42 |

# Main Page

This is the main page for the Schwarz library pdf documentation. The repository is hosted on github. Documentation on aspects such as the build system, can be found at the # Installation Instructions page.

## Modules

The structure of the Schwarz Library code is divided into different  ${\tt modules}$ :

- Initialization: Handles the initialization of the problem and the solver.
- Communicate: Handles the communication.
- Solve: Handles the local solution and the convergence detection.
- Schwarz Class: The Classes related to the Schwarz solvers.
- Utils: Provides some basic utilities.

2 Main Page

## # Installation Instructions

#### **Building**

Use the standard cmake build procedure:

```
mkdir build; cd build
cmake -G "Unix Makefiles" [OPTIONS] .. && make
```

Replace [OPTIONS] with desired cmake options for your build. The library adds the following additional switches to control what is being built:

- -DSCHWARZ\_BUILD\_BENCHMARKING={ON, OFF} Builds some example benchmarks. Default is ON
- -DSCHWARZ\_BUILD\_METIS={ON, OFF} Builds with support for the METIS partitioner. User needs to provide the path to the installation of the METIS library in METIS\_DIR, preferably as an environment variable. Default is OFF
- -DSCHWARZ\_BUILD\_CHOLMOD={ON, OFF} Builds with support for the CHOLMOD module from the Suitesparse library. User needs to set an environment variable CHOLMOD\_DIR to the path containing the CHOLMOD installation. Default is OFF
- -DSCHWARZ\_BUILD\_CUDA={ON, OFF} Builds with CUDA support. Though Ginkgo provides most of the required CUDA support, we do need to link to CUDA for explicit setting of GPU affinities, some custom gather and scatter operations. Default is OFF.
- -DSCHWARZ\_BUILD\_CLANG\_TIDY={ON, OFF} Builds with support for clang-tidy Default is OFF
- -DSCHWARZ\_BUILD\_DEALII={ON, OFF} Builds with support for the finite element library deal.ii
   Default is OFF
- -DSCHWARZ\_WITH\_HWLOC={ON, OFF} Builds with support for the hardware locality library used for binding hardware. hwloc is distributed as a part of the Open-MPI project. Default is ON
- -DSCHWARZ\_DEVEL\_TOOLS={ON, OFF} Builds with some developer tools support. Default is ON. In particular uses git-cmake-format to automatically format the source files with clang-format.

#### **Tips**

- If you are having CUDA problems and you are not using CUDA, then feel free to switch the CUDA module off with -DSCHWARZ\_BUILD\_CUDA=off.
- Installing CHOLMOD can be a bit annoying. TODO add some details on fixing Suitesparse compilation.
- When doing merge commits it is possible that make format does not work. You can run cmake -DSCH ← WARZ\_DEVEL\_TOOLS=OFF . . to temporarily switch off the formatting. Please switch it on again when committing normally.

# **Testing Instructions**

6 Testing Instructions

# Benchmarking.

# Benchmark example 1.

## Poisson solver using Restricted Additive Schwarz with overlap.

The flag  $-DSCHWARZ\_BUILD\_BENCHMARKING$  (default ON) enables the example and benchmarking snippets. The following command line options are available for this example. This is setup using gflags.

The executable is run in the following fashion:

"sh [MPI\_COMMAND] [MPI\_OPTIONS]

8 Benchmarking.

## **Module Documentation**

## 5.1 Communicate

A module dedicated to the Communication interface in schwarz-lib.

## **Namespaces**

• schwz::CommHelpers

The CommHelper namespace .

ProcessTopology

The ProcessTopology namespace.

#### Classes

class schwz::Communicate< ValueType, IndexType >

The communication class that provides the methods for the communication between the subdomains.

struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

## 5.1.1 Detailed Description

A module dedicated to the Communication interface in schwarz-lib.

10 Module Documentation

## 5.2 Initialization

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

## **Namespaces**

· schwz::PartitionTools

The PartitionTools namespace.

ProcessTopology

The ProcessTopology namespace .

#### Classes

· class schwz::device\_guard

This class defines a device guard for the cuda functions and the cuda module.

class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

struct schwz::Settings

The struct that contains the solver settings and the parameters to be set by the user.

- struct schwz::Metadata< ValueType, IndexType >

The solver metadata struct.

## 5.2.1 Detailed Description

A module dedicated to the initialization and setup and usage of the solvers in schwarz-lib.

5.3 Schwarz Class

## 5.3 Schwarz Class

A module dedicated to the Schwarz solver classes in schwarz-lib.

## Classes

class schwz::SolverRAS < ValueType, IndexType >
 An implementation of the solver interface using the RAS solver.

 $\bullet \ \, {\it class schwz::} Schwarz Base < Value Type, \, Index Type >$ 

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

## 5.3.1 Detailed Description

A module dedicated to the Schwarz solver classes in schwarz-lib.

12 Module Documentation

## 5.4 Solve

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

## **Namespaces**

• schwz::conv\_tools

The conv\_tools namespace .

• schwz::SolverTools

The SolverTools namespace .

#### **Classes**

struct schwz::Metadata < ValueType, IndexType >

The solver metadata struct.

class schwz::Solve < ValueType, IndexType >

The Solver class the provides the solver and the convergence checking methods.

## 5.4.1 Detailed Description

A module dedicated to the solvers including local solution and convergence detection in schwarz-lib.

5.5 Utils 13

## 5.5 Utils

A module dedicated to the utilities in schwarz-lib.

## Classes

 $\bullet \ \, {\sf struct\ schwz::} {\sf Utils} {< \ } {\sf ValueType,\ IndexType} >$ 

The utilities class which provides some checks and basic utilities.

## 5.5.1 Detailed Description

A module dedicated to the utilities in schwarz-lib.

14 Module Documentation

# **Namespace Documentation**

## 6.1 ProcessTopology Namespace Reference

The ProcessTopology namespace.

## 6.1.1 Detailed Description

The ProcessTopology namespace.

proc\_topo

## 6.2 schwz Namespace Reference

The Schwarz wrappers namespace.

## **Namespaces**

• CommHelpers

The CommHelper namespace .

• conv\_tools

The conv\_tools namespace.

PartitionTools

The PartitionTools namespace.

SolverTools

The SolverTools namespace .

#### Classes

· class Communicate

The communication class that provides the methods for the communication between the subdomains.

· class device\_guard

This class defines a device guard for the cuda functions and the cuda module.

· class Initialize

The initialization class that provides methods for initialization of the solver.

struct Metadata

The solver metadata struct.

· class SchwarzBase

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

struct Settings

The struct that contains the solver settings and the parameters to be set by the user.

· class Solve

The Solver class the provides the solver and the convergence checking methods.

class SolverRAS

An implementation of the solver interface using the RAS solver.

struct Utils

The utilities class which provides some checks and basic utilities.

## 6.2.1 Detailed Description

The Schwarz wrappers namespace.

## 6.3 schwz::CommHelpers Namespace Reference

The CommHelper namespace.

#### 6.3.1 Detailed Description

The CommHelper namespace.

comm\_helpers

## 6.4 schwz::conv\_tools Namespace Reference

The conv\_tools namespace.

## 6.4.1 Detailed Description

The conv\_tools namespace.

conv\_tools

## 6.5 schwz::PartitionTools Namespace Reference

The PartitionTools namespace.

## 6.5.1 Detailed Description

The PartitionTools namespace.

part\_tools

## 6.6 schwz::SolverTools Namespace Reference

The SolverTools namespace.

## 6.6.1 Detailed Description

The SolverTools namespace.

solver\_tools

## **Class Documentation**

## 7.1 BadDimension Class Reference

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

```
#include <exception.hpp>
```

#### **Public Member Functions**

BadDimension (const std::string &file, int line, const std::string &func, const std::string &op\_name, std::size
 \_t op\_num\_rows, std::size\_t op\_num\_cols, const std::string &clarification)
 Initializes a bad dimension error.

#### 7.1.1 Detailed Description

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

#### 7.1.2 Constructor & Destructor Documentation

#### 7.1.2.1 BadDimension()

Initializes a bad dimension error.

20 Class Documentation

#### **Parameters**

| file          | The name of the offending source file                |
|---------------|--|
| line          | The source code line number where the error occurred |
| func          | The function name where the error occurred           |
| op_name       | The name of the operator                             |
| op_num_rows   | The row dimension of the operator                    |
| op_num_cols   | The column dimension of the operator                 |
| clarification | An additional message further describing the error   |

The documentation for this class was generated from the following file:

exception.hpp (68412d6)

## 7.2 schwz::Settings::comm\_settings Struct Reference

The settings for the various available communication paradigms.

```
#include <settings.hpp>
```

#### **Public Attributes**

• bool enable\_onesided = false

Enable one-sided communication.

• bool enable\_overlap = false

Enable explicit overlap between communication and computation.

• bool enable\_put = false

Put the data to the window using MPI\_Put rather than get.

• bool enable\_get = true

Get the data to the window using MPI\_Get rather than put.

• bool enable\_one\_by\_one = false

Push each element separately directly into the buffer.

• bool enable\_flush\_local = false

Use local flush.

• bool enable flush all = true

Use flush all.

• bool enable\_lock\_local = false

Use local locks.

• bool enable\_lock\_all = true

Use lock all.

#### 7.2.1 Detailed Description

The settings for the various available communication paradigms.

The documentation for this struct was generated from the following file:

settings.hpp (68412d6)

## 7.3 schwz::Communicate < ValueType, IndexType >::comm\_struct Struct Reference

The communication struct used to store the communication data.

```
#include <communicate.hpp>
```

#### **Public Attributes**

· int num neighbors in

The number of neighbors this subdomain has to receive data from.

· int num\_neighbors\_out

The number of neighbors this subdomain has to send data to.

std::shared\_ptr< gko::Array< IndexType > > neighbors\_in

The neighbors this subdomain has to receive data from.

std::shared\_ptr< gko::Array< IndexType > > neighbors\_out

The neighbors this subdomain has to send data to.

std::vector< bool > is\_local\_neighbor

The bool vector which is true if the neighbors of a subdomain are in one node.

• int local\_num\_neighbors\_in

The number of neighbors this subdomain has to receive data from.

int local\_num\_neighbors\_out

The number of neighbors this subdomain has to send data to.

 $\bullet \quad std::shared\_ptr < gko::Array < IndexType >> local\_neighbors\_in \\$ 

The neighbors this subdomain has to receive data from.

std::shared\_ptr< gko::Array< IndexType > > local\_neighbors\_out

The neighbors this subdomain has to send data to.

std::shared ptr< gko::Array< IndexType \* > > global put

The array containing the number of elements that each subdomain sends from the other.

std::shared\_ptr< gko::Array< IndexType \* > > local\_put

The array containing the number of elements that each subdomain sends from the other.

std::shared ptr< gko::Array< IndexType \* > remote put

The array containing the number of elements that each subdomain sends from the other.

std::shared\_ptr< gko::Array< IndexType \* > > global\_get

The array containing the number of elements that each subdomain gets from the other.

std::shared\_ptr< gko::Array< IndexType \* > > local\_get

The array containing the number of elements that each subdomain gets from the other.

std::shared\_ptr< gko::Array< IndexType \* > > remote\_get

The array containing the number of elements that each subdomain gets from the other.

std::shared\_ptr< gko::Array< IndexType > > window\_ids

The RDMA window ids.

22 Class Documentation

std::shared\_ptr< gko::Array< IndexType > > windows\_from

The RDMA window ids to receive data from.

std::shared\_ptr< gko::Array< IndexType > > windows\_to

The RDMA window ids to send data to.

std::shared\_ptr< gko::Array< MPI\_Request >> put\_request

The put request array.

std::shared ptr< gko::Array< MPI Request >> get request

The get request array.

std::shared ptr< gko::matrix::Dense< ValueType >> send buffer

The send buffer used for the actual communication for both one-sided and two-sided.

std::shared ptr< gko::matrix::Dense< ValueType >> recv buffer

The recv buffer used for the actual communication for both one-sided and two-sided.

std::shared\_ptr< gko::Array< IndexType > > get\_displacements

The displacements for the receiving of the buffer.

std::shared\_ptr< gko::Array< IndexType > > put\_displacements

The displacements for the sending of the buffer.

• MPI\_Win window\_recv\_buffer

The RDMA window for the recv buffer.

• MPI\_Win window\_send\_buffer

The RDMA window for the send buffer.

• MPI\_Win window\_x

The RDMA window for the solution vector.

#### 7.3.1 Detailed Description

```
template < typename ValueType, typename IndexType > struct schwz::Communicate < ValueType, IndexType >::comm_struct
```

The communication struct used to store the communication data.

## 7.3.2 Member Data Documentation

#### 7.3.2.1 global\_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm
_struct::global_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global\_get[p][0] contains the overall number of elements to be received to subdomain p and global—\_put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

#### 7.3.2.2 global\_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm←
_struct::global_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global\_put[p][0] contains the overall number of elements to be sent to subdomain p and global\_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

#### 7.3.2.3 is\_local\_neighbor

```
template<typename ValueType , typename IndexType >
std::vector<bool> schwz::Communicate< ValueType, IndexType >::comm_struct::is_local_neighbor
```

The bool vector which is true if the neighbors of a subdomain are in one node.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize(), schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

#### 7.3.2.4 local\_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm 
_struct::local_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global\_get[p][0] contains the overall number of elements to be received to subdomain p and global—\_put[p][i] contains the index of the solution vector to be received from subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

#### 7.3.2.5 local\_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> schwz::Communicate< ValueType, IndexType >::comm
_struct::local_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global\_put[p][0] contains the overall number of elements to be sent to subdomain p and global\_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

24 Class Documentation

#### 7.3.2.6 remote\_get

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> > schwz::Communicate< ValueType, IndexType >::comm
_struct::remote_get
```

The array containing the number of elements that each subdomain gets from the other.

For example. global\_get[p][0] contains the overall number of elements to be received to subdomain p and global — \_put[p][i] contains the index of the solution vector to be received from subdomain p.

 $\label{local-loc$ 

#### 7.3.2.7 remote\_put

```
template<typename ValueType , typename IndexType >
std::shared_ptr<gko::Array<IndexType *> > schwz::Communicate< ValueType, IndexType >::comm 
_struct::remote_put
```

The array containing the number of elements that each subdomain sends from the other.

For example. global\_put[p][0] contains the overall number of elements to be sent to subdomain p and global\_put[p][i] contains the index of the solution vector to be sent to subdomain p.

Referenced by schwz::SolverRAS< ValueType, IndexType >::setup\_comm\_buffers(), and schwz::SolverRAS< ValueType, IndexType >::setup\_windows().

The documentation for this struct was generated from the following file:

· communicate.hpp (68412d6)

## 7.4 schwz::Communicate < ValueType, IndexType > Class Template Reference

The communication class that provides the methods for the communication between the subdomains.

```
#include <communicate.hpp>
```

## Classes

struct comm\_struct

The communication struct used to store the communication data.

#### **Public Member Functions**

• virtual void setup\_comm\_buffers ()=0

Sets up the communication buffers needed for the boundary exchange.

virtual void setup\_windows (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared\_ptr < gko::matrix::Dense < ValueType >> &main\_buffer)=0

Sets up the windows needed for the asynchronous communication.

virtual void exchange\_boundary (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared\_ptr< gko::matrix::Dense < ValueType >> &global\_solution)=0

Exchanges the elements of the solution vector.

void local\_to\_global\_vector (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, const std::shared\_ptr < gko::matrix::Dense < ValueType >> &local\_vector, std::shared\_ptr < gko::matrix::
 Dense < ValueType >> &global\_vector)

Transforms data from a local vector to a global vector.

virtual void update\_boundary (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared\_ptr < gko::matrix::Dense < ValueType >> &local\_solution, const std::shared\_ptr < gko::matrix::Dense < ValueType >> &local\_rhs, const std::shared\_ptr < gko::matrix::Dense < ValueType >> &global\_solution, const std::shared\_ptr < gko::matrix::Csr < ValueType, IndexType >> &interface\_matrix)=0

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

void clear (Settings &settings)

Clears the data.

#### 7.4.1 Detailed Description

```
template<typename ValueType, typename IndexType> class schwz::Communicate< ValueType, IndexType>
```

The communication class that provides the methods for the communication between the subdomains.

#### **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

#### Communicate

#### 7.4.2 Member Function Documentation

#### 7.4.2.1 exchange\_boundary()

Exchanges the elements of the solution vector.

26 Class Documentation

#### **Parameters**

| setti | ings        | The settings struct.  |
|-------|-------------|---|
| meta  | adata       | The metadata struct.  |
| glob  | al_solution | The solution vector being exchanged between the subdomains. |

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

#### 7.4.2.2 local\_to\_global\_vector()

Transforms data from a local vector to a global vector.

#### **Parameters**

| settings      | The settings struct.           |
|---------------|--------------------------------|
| metadata      | The metadata struct.           |
| local_vector  | The local vector in question.  |
| global_vector | The global vector in question. |

```
69 {
       using vec = gko::matrix::Dense<ValueType>;
70
71
       auto alpha = gko::initialize<gko::matrix::Dense<ValueType>>(
72
           {1.0}, settings.executor);
       auto temp_vector = vec::create(
74
            settings.executor, gko::dim<2>(metadata.local_size, 1),
75
           gko::Array<ValueType>::view(
76
                settings.executor, metadata.local_size,
77
                &global_vector->get_values()[metadata.first_row
78
                                                     ->get_data()[metadata.my_rank]]),
79
            1);
80
       auto temp_vector2 = vec::create(
81
            settings.executor, gko::dim<2>(metadata.local_size, 1),
82
           gko::Array<ValueType>::view(settings.executor, metadata.local_size,
83
                                           local_vector->get_values()),
       if (settings.convergence_settings.convergence_crit ==
87
           {\tt Settings::} convergence\_settings::local\_convergence\_crit::
88
                residual_based) {
           local_vector->add_scaled(alpha.get(), temp_vector.get());
temp_vector->add_scaled(alpha.get(), local_vector.get());
89
90
           temp_vector->copy_from(temp_vector2.get());
93
94 }
```

#### 7.4.2.3 setup\_windows()

Sets up the windows needed for the asynchronous communication.

#### **Parameters**

| settings    | The settings struct.                                    |
|-------------|---|
| metadata    | The metadata struct.                                    |
| main_buffer | The main buffer being exchanged between the subdomains. |

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

#### 7.4.2.4 update\_boundary()

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

#### **Parameters**

| settings            | The settings struct.  |
|---------------------|---|
| metadata            | The metadata struct.  |
| local_solution      | The local solution vector in the subdomain.   |
| local_rhs           | The local right hand side vector in the subdomain.  |
| global_solution     | The workspace solution vector.  |
| global_old_solution | The global solution vector of the previous iteration.   |
| interface_matrix    | The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains. |

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::run().

The documentation for this class was generated from the following files:

28 Class Documentation

- communicate.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/communicate.cpp (68412d6)

## 7.5 schwz::Settings::convergence\_settings Struct Reference

The various convergence settings available.

```
#include <settings.hpp>
```

## 7.5.1 Detailed Description

The various convergence settings available.

The documentation for this struct was generated from the following file:

• settings.hpp (68412d6)

## 7.6 CudaError Class Reference

CudaError is thrown when a CUDA routine throws a non-zero error code.

```
#include <exception.hpp>
```

#### **Public Member Functions**

CudaError (const std::string &file, int line, const std::string &func, int error\_code)
 Initializes a CUDA error.

#### 7.6.1 Detailed Description

CudaError is thrown when a CUDA routine throws a non-zero error code.

#### 7.6.2 Constructor & Destructor Documentation

#### 7.6.2.1 CudaError()

Initializes a CUDA error.

#### **Parameters**

| file       | The name of the offending source file                |
|------------|--|
| line       | The source code line number where the error occurred |
| func       | The name of the CUDA routine that failed             |
| error_code | The resulting CUDA error code                        |

The documentation for this class was generated from the following files:

- exception.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (68412d6)

## 7.7 CusparseError Class Reference

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

```
#include <exception.hpp>
```

#### **Public Member Functions**

• CusparseError (const std::string &file, int line, const std::string &func, int error\_code)

Initializes a cuSPARSE error.

## 7.7.1 Detailed Description

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

#### 7.7.2 Constructor & Destructor Documentation

#### 7.7.2.1 CusparseError()

Initializes a cuSPARSE error.

30 Class Documentation

#### **Parameters**

| file       | The name of the offending source file                |
|------------|--|
| line       | The source code line number where the error occurred |
| func       | The name of the cuSPARSE routine that failed         |
| error_code | The resulting cuSPARSE error code                    |

```
: Error(file, line, func + ": " + get_error(error_code))
(6) {}
```

The documentation for this class was generated from the following files:

- exception.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (68412d6)

## 7.8 schwz::device\_guard Class Reference

This class defines a device guard for the cuda functions and the cuda module.

```
#include <device_guard.hpp>
```

#### 7.8.1 Detailed Description

This class defines a device guard for the cuda functions and the cuda module.

The guard is used to make sure that the device code is run on the correct cuda device, when run with multiple devices. The class records the current device id and uses <code>cudaSetDevice</code> to set the device id to the one being passed in. After the scope has been exited, the destructor sets the device\_id back to the one before entering the scope.

The documentation for this class was generated from the following file:

device\_guard.hpp (68412d6)

## 7.9 schwz::Initialize < ValueType, IndexType > Class Template Reference

The initialization class that provides methods for initialization of the solver.

```
#include <initialization.hpp>
```

## **Public Member Functions**

void generate\_rhs (std::vector< ValueType > &rhs)

Generates the right hand side vector.

void setup\_global\_matrix (const std::string &filename, const gko::size\_type &oned\_laplacian\_size, std
 ::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >> &global\_matrix)

Generates the 2D global laplacian matrix.

void partition (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, const std ←
 ::shared\_ptr < gko::matrix::Csr < ValueType, IndexType >> &global\_matrix, std::vector < unsigned int >
 &partition indices)

The partitioning function.

void setup\_vectors (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std
 ::vector< ValueType > &rhs, std::shared\_ptr< gko::matrix::Dense< ValueType >> &local\_rhs, std::shared
 \_ptr< gko::matrix::Dense< ValueType >> &global\_rhs, std::shared\_ptr< gko::matrix::Dense< ValueType
 >> &local\_solution, std::shared\_ptr< gko::matrix::Dense< ValueType >> &global\_solution)

Setup the vectors with default values and allocate mameory if not allocated.

virtual void setup\_local\_matrices (Settings &settings, Metadata< ValueType, IndexType > &metadata, std
 ::vector< unsigned int > &partition\_indices, std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >>
 &global\_matrix, std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >> &local\_matrix, std::shared
 \_ptr< gko::matrix::Csr< ValueType, IndexType >> &interface\_matrix)=0

Sets up the local and the interface matrices from the global matrix and the partition indices.

## **Public Attributes**

std::vector< unsigned int > partition indices

The partition indices containing the subdomains to which each row(vertex) of the matrix(graph) belongs to.

std::vector< unsigned int > cell\_weights

The cell weights for the partition algorithm.

## **Additional Inherited Members**

## 7.9.1 Detailed Description

template<typename ValueType = gko::default\_precision, typename IndexType = gko::int32> class schwz::Initialize< ValueType, IndexType >

The initialization class that provides methods for initialization of the solver.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

## Initialization

#### 7.9.2 Member Function Documentation

#### 7.9.2.1 generate\_rhs()

Generates the right hand side vector.

#### **Parameters**

| rhs | The rhs vector. |
|-----|-----------------|
|     |                 |

References schwz::Initialize < ValueType, IndexType >::setup\_global\_matrix().

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

```
90 {
91     std::uniform_real_distribution<double> unif(0.0, 1.0);
92     std::default_random_engine engine;
93     for (gko::size_type i = 0; i < rhs.size(); ++i) {
94         rhs[i] = unif(engine);
95     }
96 }</pre>
```

## 7.9.2.2 partition()

The partitioning function.

Allows the partition of the global matrix depending with METIS and a regular 1D decomposition.

## **Parameters**

| settings          | The settings struct.            |
|-------------------|---------------------------------|
| metadata          | The metadata struct.            |
| global_matrix     | The global matrix.              |
| partition_indices | The partition indices [OUTPUT]. |

References schwz::Metadata < ValueType, IndexType >::global\_size, schwz::Metadata < ValueType, IndexType >::my\_rank, schwz::Metadata < ValueType, IndexType >::num\_subdomains, and schwz::Settings::write\_debug\_  $\leftarrow$  out.

 $Referenced\ by\ schwz:: Schwarz Base < Value Type,\ Index Type > :: initialize ().$ 

```
284 {
        partition_indices.resize(metadata.global_size);
285
286
         if (metadata.my_rank == 0) {
287
             auto partition_settings =
288
                  (Settings::partition_settings::partition_zoltan |
                  Settings::partition_settings::partition_metis | Settings::partition_settings::partition_regular
289
290
291
                   Settings::partition_settings::partition_regular2d
292
                   Settings::partition_settings::partition_custom) &
293
                 settings.partition;
294
             if (partition_settings ==
295
296
                 Settings::partition_settings::partition_zoltan) {
297
                 SCHWARZ_NOT_IMPLEMENTED;
             } else if (partition_settings ==
298
299
                         Settings::partition_settings::partition_metis) {
                 if (metadata.my_rank == 0) {
   std::cout << " METIS partition" << std::endl;</pre>
300
301
302
303
                 PartitionTools::PartitionMetis(
304
                      settings, global_matrix, this->cell_weights,
305
                      metadata.num_subdomains, partition_indices);
306
             } else if (partition_settings ==
307
                         Settings::partition_settings::partition_regular) {
308
                 if (metadata.my_rank == 0) {
                      std::cout << " Regular 1D partition" << std::endl;
309
310
311
                 PartitionTools::PartitionRegular(
312
                      global_matrix, metadata.num_subdomains, partition_indices);
313
             } else if (partition_settings ==
314
                         Settings::partition_settings::partition_regular2d) {
                 if (metadata.my_rank == 0) {
    std::cout << " Regular 2D partition" << std::endl;</pre>
315
316
317
318
                 PartitionTools::PartitionRegular2D(
                      global_matrix, settings.write_debug_out,
319
             metadata.num_subdomains, partition_indices);
} else if (partition_settings ==
320
321
322
                         Settings::partition_settings::partition_custom) {
323
                  // User partitions mesh manually
324
                 SCHWARZ_NOT_IMPLEMENTED;
325
             } else {
326
                 SCHWARZ NOT IMPLEMENTED;
327
328
        }
329 }
```

## 7.9.2.3 setup\_global\_matrix()

Generates the 2D global laplacian matrix.

## **Parameters**

| oned_laplacian_size | The size of the one d laplacian grid. |
|---------------------|---------------------------------------|
| global_matrix       | The global matrix.                    |

 $\label{local-loc$ 

```
200 {
201    using index_type = IndexType;
```

```
202
        using value_type = ValueType;
203
        using mtx = gko::matrix::Csr<value_type, index_type>;
204
         if (settings.matrix_filename != "null") {
             auto input_file = std::ifstream(filename, std::ios::in);
205
206
             if (!input_file) {
    std::cerr << "Could not find the file \"" << filename</pre>
207
                             << "\", which is required for this test.\n";
208
209
210
             global_matrix =
211
                 gko::read<mtx>(input_file, settings.executor->get_master());
             global_matrix->sort_by_column_index();
212
        std::cout << "Matrix from file " << filename << std::endl;
} else if (settings.matrix_filename == "null" &&
213
214
215
                     settings.explicit_laplacian) {
216
             std::cout << "Laplacian 2D Matrix (generated in house) " << std::endl;</pre>
217
             gko::size_type global_size = oned_laplacian_size *
      oned_laplacian_size;
218
219
             global_matrix = mtx::create(settings.executor->get_master(),
220
                                            gko::dim<2>(global_size), 5 * global_size);
221
             value_type *values = global_matrix->get_values();
             index_type *row_ptrs = global_matrix->get_row_ptrs();
index_type *col_idxs = global_matrix->get_col_idxs();
222
223
224
225
             std::vector<gko::size_type> exclusion_set;
226
227
             std::map<IndexType, ValueType> stencil_map = {
                  {-oned_laplacian_size, -1}, {-1, -1}, {0, 4}, {1, -1}, {oned_laplacian_size, -1},
228
229
230
             for (auto i = 2; i < global_size; ++i) {
    gko::size_type index = (i - 1) * oned_laplacian_size;
    if (index * index < global_size * global_size) {</pre>
231
232
233
234
                      exclusion_set.push_back(
235
                          linearize_index(index, index - 1, global_size));
236
                      exclusion_set.push_back(
                           linearize_index(index - 1, index, global_size));
237
238
239
240
241
             std::sort(exclusion_set.begin(),
                        exclusion_set.begin() + exclusion_set.size());
2.42
243
244
             IndexType pos = 0;
             IndexType col_idx = 0;
245
             row_ptrs[0] = pos;
246
247
             gko::size_type cur_idx = 0;
             for (IndexType i = 0; i < global_size; ++i) {</pre>
248
                  for (auto ofs : stencil_map) {
249
250
                      auto in_exclusion_flag =
251
                           (exclusion_set[cur_idx] ==
252
                            linearize_index(i, i + ofs.first, global_size));
253
                      if (0 <= i + ofs.first && i + ofs.first < global_size &&</pre>
254
                           !in_exclusion_flag) {
255
                           values[pos] = ofs.second;
                           col_idxs[pos] = i + ofs.first;
256
257
                           ++pos;
258
259
                      if (in_exclusion_flag) {
260
                           cur_idx++;
2.61
262
                      col_idx = row_ptrs[i + 1] - pos;
263
                  row_ptrs[i + 1] = pos;
265
             }
         } else {
266
             2.67
268
269
                        << std::endl;
             std::exit(-1);
270
271
272 }
```

## 7.9.2.4 setup\_local\_matrices()

```
template<typename ValueType , typename IndexType >
void schwz::Initialize< ValueType, IndexType >::setup_local_matrices (
```

```
Settings & settings,
    Metadata< ValueType, IndexType > & metadata,
    std::vector< unsigned int > & partition_indices,
    std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> & global_matrix,
    std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> & local_matrix,
    std::shared_ptr< gko::matrix::Csr< ValueType, IndexType >> & interface_matrix)
[pure virtual]
```

Sets up the local and the interface matrices from the global matrix and the partition indices.

#### **Parameters**

| settings          | The settings struct.  |
|-------------------|---|
| metadata          | The metadata struct.  |
| partition_indices | The array containing the partition indices.   |
| global_matrix     | The global system matrix.   |
| local_matrix      | The local system matrix.  |
| interface_matrix  | The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains. |
| local_perm        | The local permutation, obtained through RCM or METIS.   |

Implemented in schwz::SolverRAS< ValueType, IndexType >.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

## 7.9.2.5 setup\_vectors()

Setup the vectors with default values and allocate mameory if not allocated.

#### **Parameters**

|                 | ,  |
|-----------------|--|
| settings        | The settings struct.                               |
| metadata        | The metadata struct.                               |
| local_rhs       | The local right hand side vector in the subdomain. |
| global_rhs      | The global right hand side vector.                 |
| local_solution  | The local solution vector in the subdomain.        |
| global_solution | The global solution vector.                        |

References schwz::Settings::executor, schwz::Metadata< ValueType, IndexType >::first\_row, schwz::Metadata<

ValueType, IndexType >::global\_size, schwz::Metadata< ValueType, IndexType >::local\_size\_x, and schwz:: $\leftarrow$  Metadata< ValueType, IndexType >::my\_rank.

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

```
340 {
        using vec = gko::matrix::Dense<ValueType>;
342
        auto my_rank = metadata.my_rank;
        auto first_row = metadata.first_row->get_data()[my_rank];
343
344
345
        // Copy the global rhs vector to the required executor.
346
        gko::Array<ValueType> temp_rhs{settings.executor->get_master(), rhs.begin(),
347
                                           rhs.end()};
348
        global_rhs = vec::create(settings.executor)
349
                                    gko::dim<2>{metadata.global_size, 1}, temp_rhs, 1);
350
        global_solution = vec::create(settings.executor->get_master(),
                                         gko::dim<2>(metadata.global_size, 1));
351
352
353
        vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
// Extract the local rhs from the global rhs. Also takes into account the
354
355
356
        SolverTools::extract_local_vector(settings, metadata, local_rhs.get(),
357
358
                                              global_rhs.get(), first_row);
359
360
        local_solution =
361
             vec::create(settings.executor, gko::dim<2>(metadata.local_size_x, 1));
362 }
```

The documentation for this class was generated from the following files:

- initialization.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/initialization.cpp (68412d6)

# 7.10 schwz::Metadata < ValueType, IndexType > Struct Template Reference

The solver metadata struct.

```
#include <settings.hpp>
```

## Classes

· struct post\_process\_data

The struct used for storing data for post-processing.

## **Public Attributes**

• MPI\_Comm mpi\_communicator

The MPI communicator.

• gko::size\_type global\_size = 0

The size of the global matrix.

• gko::size\_type oned\_laplacian\_size = 0

The size of the 1 dimensional laplacian grid.

gko::size\_type local\_size = 0

The size of the local subdomain matrix.

• gko::size\_type local\_size\_x = 0

The size of the local subdomain matrix + the overlap.

gko::size\_type local\_size\_o = 0

The size of the local subdomain matrix + the overlap.

gko::size\_type overlap\_size = 0

The size of the overlap between the subdomains.

• gko::size\_type num\_subdomains = 1

The number of subdomains used within the solver.

· int my rank

The rank of the subdomain.

· int my local rank

The local rank of the subdomain.

· int local num procs

The local number of procs in the subdomain.

int comm size

The number of subdomains used within the solver, size of the communicator.

int num threads

The number of threads used within the solver for each subdomain.

IndexType iter\_count

The iteration count of the solver.

ValueType tolerance

The tolerance of the complete solver.

• ValueType local\_solver\_tolerance

The tolerance of the local solver in case of an iterative solve.

IndexType max iters

The maximum iteration count of the Schwarz solver.

• IndexType local\_max\_iters

The maximum iteration count of the local iterative solver.

std::string local\_precond

Local preconditioner.

• unsigned int precond\_max\_block\_size

The maximum block size for the preconditioner.

ValueType current\_residual\_norm = -1.0

The current residual norm of the subdomain.

• ValueType min\_residual\_norm = -1.0

The minimum residual norm of the subdomain.

std::vector< std::tuple< int, int, std::string, std::vector< ValueType >>> time\_struct

The struct used to measure the timings of each function within the solver loop.

• std::vector< std::tuple< int, std::vector< std::tuple< int, int >>, std::vector< std::tuple< int, int >>, int, int >> comm\_data\_struct

The struct used to measure the timings of each function within the solver loop.

std::shared\_ptr< gko::Array< IndexType > > global\_to\_local

The mapping containing the global to local indices.

std::shared\_ptr< gko::Array< IndexType > > local\_to\_global

The mapping containing the local to global indices.

std::shared\_ptr< gko::Array< IndexType > > overlap\_row

The overlap row indices.

std::shared\_ptr< gko::Array< IndexType > > first\_row

The starting row of each subdomain in the matrix.

std::shared\_ptr< gko::Array< IndexType >> permutation

The permutation used for the re-ordering.

std::shared\_ptr< gko::Array< IndexType > > i\_permutation

The inverse permutation used for the re-ordering.

## 7.10.1 Detailed Description

 $\label{template} \begin{tabular}{ll} template < typename \ ValueType, typename \ IndexType > \\ struct \ schwz:: Metadata < ValueType, IndexType > \\ \end{tabular}$ 

The solver metadata struct.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

## 7.10.2 Member Data Documentation

#### 7.10.2.1 local\_solver\_tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::local_solver_tolerance
```

The tolerance of the local solver in case of an iterative solve.

The residual norm reduction required.

#### 7.10.2.2 tolerance

```
template<typename ValueType, typename IndexType>
ValueType schwz::Metadata< ValueType, IndexType >::tolerance
```

The tolerance of the complete solver.

The residual norm reduction required.

The documentation for this struct was generated from the following file:

• settings.hpp (68412d6)

## 7.11 MetisError Class Reference

MetisError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

## **Public Member Functions**

MetisError (const std::string &file, int line, const std::string &func, int error\_code)
 Initializes a METIS error.

## 7.11.1 Detailed Description

MetisError is thrown when a METIS routine throws a non-zero error code.

#### 7.11.2 Constructor & Destructor Documentation

## 7.11.2.1 MetisError()

Initializes a METIS error.

## **Parameters**

| file       | The name of the offending source file                |  |
|------------|--|--|
| line       | The source code line number where the error occurred |  |
| func       | The name of the METIS routine that failed            |  |
| error_code | The resulting METIS error code                       |  |

The documentation for this class was generated from the following files:

- exception.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (68412d6)

# 7.12 schwz::Metadata < ValueType, IndexType >::post\_process\_data Struct Reference

The struct used for storing data for post-processing.

```
#include <settings.hpp>
```

## 7.12.1 Detailed Description

template<typename ValueType, typename IndexType>
struct schwz::Metadata< ValueType, IndexType >::post\_process\_data

The struct used for storing data for post-processing.

The documentation for this struct was generated from the following file:

settings.hpp (68412d6)

## 7.13 schwz::SchwarzBase < ValueType, IndexType > Class Template Reference

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

```
#include <schwarz_base.hpp>
```

#### **Public Member Functions**

SchwarzBase (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

void initialize ()

Initialize the matrix and vectors.

void run (std::shared\_ptr< gko::matrix::Dense< ValueType >> &solution)

The function that runs the actual solver and obtains the final solution.

void print\_vector (const std::shared\_ptr< gko::matrix::Dense< ValueType >> &vector, int subd, std::string name)

The auxiliary function that prints a passed in vector.

void print\_matrix (const std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >> &matrix, int rank, std::string name)

The auxiliary function that prints a passed in CSR matrix.

## **Public Attributes**

 $\bullet \quad \text{std::shared\_ptr} < \text{gko::matrix::Csr} < \text{ValueType, IndexType} >> \underline{\text{local\_matrix}}$ 

The local subdomain matrix.

std::shared\_ptr< gko::matrix::Permutation< IndexType > > local\_perm

The local subdomain permutation matrix/array.

std::shared\_ptr< gko::matrix::Permutation< IndexType > > local\_inv\_perm

The local subdomain inverse permutation matrix/array.

std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular\_factor\_l

The local lower triangular factor used for the triangular solves.

std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType > > triangular\_factor\_u

The local upper triangular factor used for the triangular solves.

std::shared ptr< gko::matrix::Csr< ValueType, IndexType > > interface matrix

The local interface matrix.

std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >> global\_matrix

The global matrix.

std::shared\_ptr< gko::matrix::Dense< ValueType >> local\_rhs

The local right hand side.

std::shared\_ptr< gko::matrix::Dense< ValueType > > global\_rhs
 The global right hand side.

The local solution vector.

 $\bullet \quad \mathsf{std} :: \mathsf{shared\_ptr} < \mathsf{gko} :: \mathsf{matrix} :: \mathsf{Dense} < \mathsf{ValueType} > > \mathsf{global\_solution} \\$ 

The global solution vector.

std::vector< ValueType > local\_residual\_vector\_out

The global residual vector.

std::vector< std::vector< ValueType >> global\_residual\_vector\_out

The local residual vector.

#### **Additional Inherited Members**

## 7.13.1 Detailed Description

```
\label{template} $$ \ensuremath{\sf template}$$ < typename \ensuremath{\sf ValueType}$ = gko::int32 > $$ class \ensuremath{\sf schwarzBase}$ < \ensuremath{\sf ValueType}$, IndexType > $$ $$
```

The Base solver class is meant to be the class implementing the common implementations for all the schwarz methods.

It derives from the Initialization class, the Communication class and the Solve class all of which are templated.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

## 7.13.2 Constructor & Destructor Documentation

## 7.13.2.1 SchwarzBase()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

## Parameters

| settings | The settings struct. |
|----------|----------------------|
| metadata | The metadata struct. |

References schwz::Settings::cuda\_device\_guard, schwz::Settings::executor, schwz::Settings::executor\_string, schwz::Metadata < ValueType, IndexType >::local\_num\_procs, schwz::Metadata < ValueType, IndexType >::my\_local\_rank, and schwz::Metadata < ValueType, IndexType >::my\_rank.

```
: Initialize<ValueType, IndexType>(settings, metadata),
75
         settings (settings),
76
         metadata (metadata)
77 {
78
       using vec itype = gko::Array<IndexType>;
       using vec_vecshared = gko::Array<IndexType *>;
       metadata.my_local_rank =
80
81
           Utils<ValueType, IndexType>::get_local_rank(metadata.mpi_communicator);
82
       metadata.local_num_procs = Utils<ValueType, IndexType>::get_local_num_procs(
8.3
          metadata.mpi_communicator);
      auto my_local_rank = metadata.my_local_rank;
if (settings.executor_string == "omp") {
84
85
           settings.executor = gko::OmpExecutor::create();
87
           auto exec_info =
88
              static_cast<gko::OmpExecutor *>(settings.executor.get())
89
                   ->get_exec_info();
90
           exec info->bind to core(metadata.mv local rank);
       } else if (settings.executor_string == "cuda") {
93
           int num_devices = 0;
94 #if SCHW HAVE CUDA
           SCHWARZ_ASSERT_NO_CUDA_ERRORS(cudaGetDeviceCount(&num_devices));
95
96 #else
           SCHWARZ NOT IMPLEMENTED;
98 #endif
99
           Utils<ValueType, IndexType>::assert_correct_cuda_devices(
100
                num_devices, metadata.my_rank);
101
            settings.executor = gko::CudaExecutor::create(
102
               my_local_rank, gko::OmpExecutor::create());
103
           auto exec_info = static_cast<gko::OmpExecutor *>(
                                 settings.executor->get_master().get())
104
105
                                  ->get_exec_info();
106
           exec_info->bind_to_core(my_local_rank);
107
            settings.cuda_device_guard =
108
                std::make_shared<schwz::device_guard>(my_local_rank);
109
110
            \verb|std::cout| << " Rank" << metadata.my_rank << " with local rank"|
111
                       << my_local_rank << " has
112
                       << (static_cast<gko::CudaExecutor *>(settings.executor.get()))
                       ->get_device_id()
<< " id of gpu" << std::endl;
113
114
           MPI_Barrier(metadata.mpi_communicator);
115
       } else if (settings.executor_string == "reference") {
116
           settings.executor = gko::ReferenceExecutor::create();
118
            auto exec_info =
119
               static_cast<gko::ReferenceExecutor *>(settings.executor.get())
120
                     ->get_exec_info();
121
            exec_info->bind_to_core(my_local_rank);
        }
```

#### 7.13.3 Member Function Documentation

#### 7.13.3.1 print\_matrix()

The auxiliary function that prints a passed in CSR matrix.

#### **Parameters**

| matrix | The matrix to be printed.                 |
|--------|---|
| subd   | The subdomain on which the vector exists. |
| name   | The name of the matrix as a string.       |

#### 7.13.3.2 print\_vector()

The auxiliary function that prints a passed in vector.

#### **Parameters**

| vector | The vector to be printed.                 |
|--------|---|
| subd   | The subdomain on which the vector exists. |
| name   | The name of the vector as a string.       |

## 7.13.3.3 run()

The function that runs the actual solver and obtains the final solution.

#### **Parameters**

| solution | The solution vector. |
|----------|----------------------|

References schwz::Communicate< ValueType, IndexType >::exchange\_boundary(), schwz::Settings::executor, schwz::SchwarzBase< ValueType, IndexType >::global\_matrix, schwz::SchwarzBase< ValueType, IndexType >::global\_rhs, schwz::SchwarzBase< ValueType, IndexType >::global\_solution, schwz::SchwarzBase< Value Type, IndexType >::local\_inv\_perm, schwz ::SchwarzBase< ValueType, IndexType >::local\_inv\_perm, schwz ::SchwarzBase< ValueType, IndexType, IndexType >::local\_matrix, schwz::SchwarzBase< ValueType, IndexType, IndexType >::local\_rhs, schwz::SchwarzBase< ValueType, Index ::SchwarzBase< ValueType, Index ::SchwarzBase< ValueType, Index ::SchwarzBase< ValueType, Index ::SchwarzBase< ValueType, IndexType >::setup\_windows(), schwz::SchwarzBase< ValueType, IndexType >::triangular\_factor := u, schwz::SchwarzBase< ValueType, IndexType >::triangular\_factor := u, schwz::SchwarzBase< ValueType, IndexType >::triangular\_factor := u, schwz::Settings::write\_iters\_and\_ := residuals.

```
312 {
```

```
313
        using vec_vtype = gko::matrix::Dense<ValueType>;
        if (!solution.get()) {
314
315
            solution =
316
                vec_vtype::create(settings.executor->get_master(),
317
                                   gko::dim<2>(this->metadata.global_size, 1));
318
319
        // The main solution vector
        std::shared_ptr<vec_vtype> global_solution = vec_vtype::create(
320
321
            this->settings.executor, gko::dim<2>(this->metadata.global_size, 1));
        // A work vector.
322
        std::shared_ptr<vec_vtype> work_vector = vec_vtype::create(
    settings.executor, gko::dim<2>(2 * this->metadata.local_size_x, 1));
323
324
325
        // An initial guess.
326
        std::shared_ptr<vec_vtype> init_guess = vec_vtype::create(
327
            settings.executor, gko::dim<2>(this->metadata.local_size_x, 1));
328
        init_guess->copy_from(local_rhs.get());
329
330
        // std::vector<IndexType> local_converged_iter_count;
331
332
        // Setup the windows for the onesided communication.
333
        this->setup_windows(this->settings, this->metadata, global_solution);
334
335
        const auto solver_settings =
             (Settings::local_solver_settings::direct_solver_cholmod |
336
337
             Settings::local_solver_settings::direct_solver_umfpack |
Settings::local_solver_settings::direct_solver_ginkgo |
338
             Settings::local_solver_settings::iterative_solver_dealii |
339
340
             Settings::local_solver_settings::iterative_solver_ginkgo) &
341
            settings.local_solver;
342
        343
344
345
        metadata.iter_count = 0;
346
        auto start_time = std::chrono::steady_clock::now();
347
        int num_converged_procs = 0;
348
        for (; metadata.iter_count < metadata.max_iters; ++(metadata.iter_count)) {
    // Exchange the boundary values. The communication part.</pre>
349
350
351
            MEASURE_ELAPSED_FUNC_TIME(
352
                this->exchange_boundary(settings, metadata, global_solution), 0,
353
                metadata.my_rank, boundary_exchange, metadata.iter_count);
354
355
            // Update the boundary and interior values after the exchanging from
356
             // other processes.
            MEASURE_ELAPSED_FUNC_TIME(
358
                this->update_boundary(settings, metadata, this->
      local solution.
359
                                        this->local_rhs, global_solution,
                                        this->interface_matrix),
360
361
                1, metadata.my_rank, boundary_update, metadata.iter_count);
362
363
            // Check for the convergence of the solver.
364
            // num_converged_procs = 0;
365
            MEASURE_ELAPSED_FUNC_TIME(
366
                 (Solve<ValueType, IndexType>::check_convergence(
                    settings, metadata, this->comm_struct, this->convergence_vector, global_solution, this->local_solution, this->
367
368
      local matrix.
                     work_vector, local_residual_norm, local_residual_norm0,
369
370
                     global_residual_norm, global_residual_norm0,
371
                     num_converged_procs)),
372
                2, metadata.my_rank, convergence_check, metadata.iter_count);
373
374
            // break if the solution diverges.
375
            if (std::isnan(global_residual_norm) || global_residual_norm > 1e12) {
                376
377
378
                std::exit(-1);
379
380
381
            // break if all processes detect that all other processes have
382
            // converged otherwise continue iterations
383
            if (num_converged_procs == metadata.num_subdomains) {
384
                break;
385
            } else
                MEASURE_ELAPSED_FUNC_TIME(
386
                     (Solve<ValueType, IndexType>::local_solve(
387
388
                         settings, metadata, this->local_matrix,
389
                         this->triangular_factor_l, this->
      triangular factor u,
390
                         this->local_perm, this->local_inv_perm, work_vector,
                         init_guess, this->local_solution)),
391
                     3, metadata.my_rank, local_solve, metadata.iter_count);
392
393
                 // Gather the local vector into the locally global vector for
394
                 // communication.
                MEASURE ELAPSED FUNC TIME (
395
                     (Communicate<ValueType, IndexType>::local_to_global_vector
396
```

```
(
397
                          settings, metadata, this->local_solution, global_solution)),
398
                     4, metadata.my_rank, expand_local_vec, metadata.iter_count);
399
400
        MPI_Barrier(MPI_COMM_WORLD);
401
402
        auto elapsed_time = std::chrono::duration<ValueType>(
403
            std::chrono::steady_clock::now() - start_time);
        404
405
        ValueType mat_norm = -1.0, rhs_norm = -1.0, sol_norm = -1.0, residual_norm = -1.0;
406
407
408
        // Write the residuals and iterations to files
409
        if (settings.write_iters_and_residuals &&
410
            solver_settings ==
411
                 Settings::local_solver_settings::iterative_solver_ginkgo) {
412
             std::string rank_string = std::to_string(metadata.my_rank);
            if (metadata.my_rank < 10) {
    rank_string = "0" + std::to_string(metadata.my_rank);</pre>
413
414
415
            std::string filename = "iter_res_" + rank_string + ".csv";
416
417
            write_iters_and_residuals(
418
                 metadata.num_subdomains, metadata.my_rank,
419
                 {\tt metadata.post\_process\_data.local\_residual\_vector\_out.size(),}
420
                 metadata.post_process_data.local_residual_vector out,
421
                 metadata.post_process_data.local_converged_iter_count,
422
                 metadata.post_process_data.local_converged_resnorm, filename);
423
424
        \ensuremath{//} Compute the final residual norm. Also gathers the solution from all
425
426
        // subdomains.
427
        Solve<ValueType, IndexType>::compute_residual_norm(
            settings, metadata, global_matrix, global_rhs, global_solution, mat_norm, rhs_norm, sol_norm, residual_norm);
428
429
430
        gather_comm_data<ValueType, IndexType>(
431
            metadata.num_subdomains, this->comm_struct, metadata.comm_data_struct);
        // clang-format off
432
433
        if (metadata.my_rank == 0)
434
          {
435
             std::cout
                   << " residual norm " << residual_norm << "\n"
436
                   << " relative residual norm of solution " << residual_norm/rhs_norm << "\n"
<< " Time taken for solve " << elapsed_time.count()</pre>
437
438
439
                   << std::endl;
440
            if (num_converged_procs < metadata.num_subdomains)</pre>
441
                 std::cout << " Did not converge in " << metadata.iter_count << " iterations."
442
443
444
                            << std::endl;
445
              }
446
447
        // clang-format on
448
        if (metadata.my_rank == 0) {
449
             solution->copy_from(global_solution.get());
450
451
        // Communicate<ValueType, IndexType>::clear(settings);
```

The documentation for this class was generated from the following files:

- schwarz\_base.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/schwarz base.cpp (68412d6)

## 7.14 schwz::Settings Struct Reference

The struct that contains the solver settings and the parameters to be set by the user.

```
#include <settings.hpp>
```

## Classes

• struct comm\_settings

The settings for the various available communication paradigms.

· struct convergence\_settings

The various convergence settings available.

## **Public Types**

· enum partition\_settings

The partition algorithm to be used for partitioning the matrix.

· enum local\_solver\_settings

The local solver algorithm for the local subdomain solves.

#### **Public Attributes**

· std::string executor\_string

The string that contains the ginkgo executor paradigm.

std::shared\_ptr< gko::Executor > executor = gko::ReferenceExecutor::create()

The ginkgo executor the code is to be executed on.

• std::shared\_ptr< device\_guard > cuda\_device\_guard

The ginkgo executor the code is to be executed on.

• gko::int32 overlap = 2

The overlap between the subdomains.

std::string matrix\_filename = "null"

The string that contains the matrix file name to read from .

• bool explicit\_laplacian = true

Flag if the laplacian matrix should be generated within the library.

• bool enable\_random\_rhs = false

Flag to enable a random rhs.

• bool print\_matrices = false

Flag to enable printing of matrices.

• bool debug\_print = false

Flag to enable some debug printing.

bool naturally\_ordered\_factor = false

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

std::string metis\_objtype

This setting defines the objective type for the metis partitioning.

• bool use precond = false

Enable the block jacobi local preconditioner for the local solver.

bool write\_debug\_out = false

Enable the writing of debug out to file.

• bool write\_iters\_and\_residuals = false

Enable writing the iters and residuals to a file.

• bool write\_perm\_data = false

Enable the local permutations from CHOLMOD to a file.

• int shifted\_iter = 1

Iteration shift for node local communication.

std::string factorization = "cholmod"

The factorization for the local direct solver.

· std::string reorder

The reordering for the local solve.

## 7.14.1 Detailed Description

The struct that contains the solver settings and the parameters to be set by the user.

settings

## 7.14.2 Member Data Documentation

## 7.14.2.1 explicit\_laplacian

```
bool schwz::Settings::explicit_laplacian = true
```

Flag if the laplacian matrix should be generated within the library.

If false, an external matrix and rhs needs to be provided

Referenced by schwz::SchwarzBase< ValueType, IndexType >::initialize().

## 7.14.2.2 naturally\_ordered\_factor

```
bool schwz::Settings::naturally_ordered_factor = false
```

Disables the re-ordering of the matrix before computing the triangular factors during the CHOLMOD factorization.

Note

This is mainly to allow compatibility with GPU solution.

The documentation for this struct was generated from the following file:

• settings.hpp (68412d6)

# 7.15 schwz::Solve < ValueType, IndexType > Class Template Reference

The Solver class the provides the solver and the convergence checking methods.

```
#include <solve.hpp>
```

## **Additional Inherited Members**

## 7.15.1 Detailed Description

```
template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class schwz::Solve< ValueType, IndexType >
```

The Solver class the provides the solver and the convergence checking methods.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

#### Solve

The documentation for this class was generated from the following files:

- solve.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/solve.cpp (68412d6)

# 7.16 schwz::SolverRAS< ValueType, IndexType > Class Template Reference

An implementation of the solver interface using the RAS solver.

```
#include <restricted_schwarz.hpp>
```

#### **Public Member Functions**

SolverRAS (Settings &settings, Metadata < ValueType, IndexType > &metadata)

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

void setup\_local\_matrices (Settings &settings, Metadata < ValueType, IndexType > &metadata, std::vector < unsigned int > &partition\_indices, std::shared\_ptr < gko::matrix::Csr < ValueType, IndexType >> &global\_
 matrix, std::shared\_ptr < gko::matrix::Csr < ValueType, IndexType >> &local\_matrix, std::shared\_ptr < gko
 ::matrix::Csr < ValueType, IndexType >> &interface\_matrix) override

Sets up the local and the interface matrices from the global matrix and the partition indices.

void setup\_comm\_buffers () override

Sets up the communication buffers needed for the boundary exchange.

Sets up the windows needed for the asynchronous communication.

void exchange\_boundary (const Settings &settings, const Metadata < ValueType, IndexType > &metadata, std::shared\_ptr < gko::matrix::Dense < ValueType >> &global\_solution) override

Exchanges the elements of the solution vector.

void update\_boundary (const Settings &settings, const Metadata< ValueType, IndexType > &metadata, std::shared\_ptr< gko::matrix::Dense< ValueType >> &local\_solution, const std::shared\_ptr< gko::matrix::Dense< ValueType >> &global = \_solution, const std::shared\_ptr< gko::matrix::Dense< ValueType >> &global = \_solution, const std::shared\_ptr< gko::matrix::Csr< ValueType, IndexType >> &interface\_matrix) override

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

## **Additional Inherited Members**

## 7.16.1 Detailed Description

template<typename ValueType = gko::default\_precision, typename IndexType = gko::int32> class schwz::SolverRAS< ValueType, IndexType >

An implementation of the solver interface using the RAS solver.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

## 7.16.2 Constructor & Destructor Documentation

#### 7.16.2.1 SolverRAS()

The constructor that takes in the user settings and a metadata struct containing the solver metadata.

#### **Parameters**

| settings | The settings struct.        |
|----------|-----------------------------|
| metadata | The metadata struct.        |
| data     | The additional data struct. |

```
51 : SchwarzBase<ValueType, IndexType>(settings, metadata)
52 {}
```

## 7.16.3 Member Function Documentation

## 7.16.3.1 exchange\_boundary()

Exchanges the elements of the solution vector.

## **Parameters**

| settings The settings struct. |   |
|-------------------------------|---|
| metadata                      | The metadata struct.  |
| global_solution               | The solution vector being exchanged between the subdomains. |

Implements schwz::Communicate < ValueType, IndexType >.

References schwz::Settings::comm\_settings::enable\_onesided, and schwz::SchwarzBase< ValueType, IndexType >::global\_solution.

```
799 {
800     if (settings.comm_settings.enable_onesided) {
801         exchange_boundary_onesided<ValueType, IndexType>(
802         settings, metadata, this->comm_struct, global_solution);
803     } else {
804         exchange_boundary_twosided<ValueType, IndexType>(
805         settings, metadata, this->comm_struct, global_solution);
806     }
807 }
```

#### 7.16.3.2 setup\_local\_matrices()

Sets up the local and the interface matrices from the global matrix and the partition indices.

#### **Parameters**

| settings          | The settings struct.  |
|-------------------|---|
| metadata          | The metadata struct.  |
| partition_indices | The array containing the partition indices.   |
| global_matrix     | The global system matrix.   |
| local_matrix      | The local system matrix.  |
| interface_matrix  | The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains. |
| local_perm        | The local permutation, obtained through RCM or METIS.   |

Implements schwz::Initialize < ValueType, IndexType >.

References schwz::Metadata< ValueType, IndexType >::comm\_size, schwz::Settings::executor, schwz::← Metadata< ValueType, IndexType >::first\_row, schwz::SchwarzBase< ValueType, IndexType >::global\_matrix, schwz::Metadata< ValueType, IndexType >::global\_size, schwz::Metadata< ValueType, IndexType >::global\_to← \_local, schwz::Metadata< ValueType, IndexType >::i\_permutation, schwz::SchwarzBase< ValueType, IndexType >::interface\_matrix, schwz::Metadata< ValueFype, IndexType >::local\_matrix, schwz::Metadata< Value← Type, IndexType >::local\_size\_o, schwz::Metadata< ValueFype, IndexType >::local\_size\_o, schwz::Metadata< ValueFype, IndexType >::local\_to\_global, schwz::← Metadata< ValueFype, IndexType, IndexType >::num\_subdomains, schwz::Settings::overlap, schwz::Metadata< ValueFype, IndexType >::overlap\_row, schwz::Metadata< ValueFype, IndexType >::overlap\_size, and schwz::Metadata< ValueFype, IndexType >::permutation.

```
62 {
        using mtx = gko::matrix::Csr<ValueType, IndexType>;
        using perm_type = gko::Array<IndexType>;
using perm_type = gko::matrix::Permutation<IndexType>;
64
6.5
66
        using arr = gko::Array<IndexType>;
        auto my_rank = metadata.my_rank;
67
        auto comm_size = metadata.comm_size;
68
        auto num_subdomains = metadata.num_subdomains;
69
70
        auto global_size = metadata.global_size;
71
        auto mpi_itype = boost::mpi::get_mpi_datatype(*partition_indices.data());
72
        MPI_Bcast(partition_indices.data(), global_size, mpi_itype, 0,
73
74
                   MPI_COMM_WORLD);
75
76
        std::vector<IndexType> local_p_size(num_subdomains);
        auto global_to_local = metadata.global_to_local->get_data();
auto local_to_global = metadata.local_to_global->get_data();
77
78
79
80
        auto first_row = metadata.first_row->get_data();
        auto permutation = metadata.permutation->get_data();
        auto i_permutation = metadata.i_permutation->get_data();
82
83
84
       auto nb = (global_size + num_subdomains - 1) /
       num subdomains;
85
       auto partition_settings =
            (Settings::partition_settings::partition_zoltan |
              Settings::partition_settings::partition_metis
87
88
             Settings::partition_settings::partition_regular |
89
             Settings::partition_settings::partition_regular2d |
90
             Settings::partition_settings::partition_custom) &
91
            settings.partition;
92
93
        IndexType *gmat_row_ptrs = global_matrix->get_row_ptrs();
94
        IndexType *gmat_col_idxs = global_matrix->get_col_idxs();
95
        ValueType *gmat_values = global_matrix->get_values();
96
        // default local p size set for 1 subdomain.
97
        first_row[0] = 0;
99
        for (auto p = 0; p < num_subdomains; ++p) {</pre>
100
              local_p_size[p] = std::min(global_size - first_row[p], nb);
101
              first_row[p + 1] = first_row[p] + local_p_size[p];
103
104
105
         if (partition_settings == Settings::partition_settings::partition_metis ||
106
             partition_settings ==
107
                  Settings::partition_settings::partition_regular2d) {
             if (num_subdomains > 1) {
   for (auto p = 0; p < num_subdomains; p++) {
      local_p_size[p] = 0;
}</pre>
108
109
110
111
112
                  for (auto i = 0; i < global_size; i++) {</pre>
113
                       local_p_size[partition_indices[i]]++;
114
                  first_row[0] = 0;
115
                  for (auto p = 0; p < num_subdomains; ++p) {
   first_row[p + 1] = first_row[p] + local_p_size[p];</pre>
116
117
118
119
                  // permutation
                  for (auto i = 0; i < global_size; i++) {
    permutation[first_row[partition_indices[i]]] = i;</pre>
120
121
                       first_row[partition_indices[i]]++;
122
123
124
                  for (auto p = num_subdomains; p > 0; p--) {
125
                       first_row[p] = first_row[p - 1];
126
127
                  first_row[0] = 0;
128
                  // iperm
129
                  for (auto i = 0; i < global_size; i++) {</pre>
130
131
                       i_permutation[permutation[i]] = i;
132
133
             }
134
135
             auto gmat temp = mtx::create(settings.executor->get master(),
136
                                               global_matrix->get_size(),
137
                                               global_matrix->get_num_stored_elements());
138
139
             auto nnz = 0;
              gmat_temp->get_row_ptrs()[0] = 0;
140
             for (auto row = 0; row < metadata.global_size; ++row) {
    for (auto col = gmat_row_ptrs[permutation[row]];</pre>
141
142
                        col < gmat_row_ptrs[permutation[row] + 1]; ++col) {</pre>
143
144
                       gmat_temp->get_col_idxs()[nnz] =
145
                           i_permutation[gmat_col_idxs[col]];
146
                       gmat_temp->get_values()[nnz] = gmat_values[col];
147
                       nnz++;
```

```
148
149
                   gmat_temp->get_row_ptrs()[row + 1] = nnz;
150
151
              global_matrix->copy_from(gmat_temp.get());
152
153
154
155
         for (auto i = 0; i < global_size; i++) {</pre>
156
              global_to_local[i] = 0;
157
              local_to_global[i] = 0;
158
159
         auto num = 0;
         for (auto i = first_row[my_rank]; i < first_row[</pre>
160
       my_rank + 1]; i++) {
161
             global_to_local[i] = 1 + num;
162
              local_to_global[num] = i;
163
              num++;
         }
164
165
166
         IndexType old = 0;
167
         for (auto k = 1; k < settings.overlap; k++) {</pre>
168
              auto now = num;
              for (auto i = old; i < now; i++) {</pre>
169
                   for (auto j = gmat_row_ptrs[local_to_global[i]];
    j < gmat_row_ptrs[local_to_global[i] + 1]; j++) {
    if (global_to_local[gmat_col_idxs[j]] == 0) {
        local_to_global[num] = gmat_col_idxs[j];
}</pre>
170
171
172
173
174
                            global_to_local[gmat_col_idxs[j]] = 1 + num;
175
                            num++;
176
                        }
177
                  }
178
179
180
181
         metadata.local_size = local_p_size[my_rank];
         metadata.local_size_x = num;
metadata.local_size_o = global_size;
182
183
184
         auto local_size = metadata.local_size;
185
         auto local_size_x = metadata.local_size_x;
186
187
         metadata.overlap_size = num - metadata.local_size;
         metadata.overlap_row = std::shared_ptr<vec_itype>(
188
189
             new vec_itype(gko::Array<IndexType>::view(
190
                   settings.executor, metadata.overlap_size,
                   & (metadata.local_to_global->get_data()[metadata.local_size]))),
191
192
              std::default_delete<vec_itype>());
193
         auto nnz_local = 0;
194
         auto nnz_interface = 0;
195
196
197
         for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i) {</pre>
198
              for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; j++) {</pre>
199
                   if (global_to_local[gmat_col_idxs[j]] != 0) {
200
                        nnz_local++;
                   } else {
201
                        std::cout << " debug: invalid edge?" << std::endl;</pre>
202
203
204
              }
205
206
         auto temp = 0;
         for (auto k = 0; k < metadata.overlap_size; k++) {
207
              temp = metadata.overlap_row->get_data()[k];
for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1]; j++) {
    if (global_to_local[gmat_col_idxs[j]] != 0) {</pre>
208
209
210
211
                        nnz_local++;
212
                   } else {
213
                       nnz_interface++;
214
                   }
215
              }
216
217
218
         std::shared_ptr<mtx> local_matrix_compute;
219
         local_matrix_compute = mtx::create(settings.executor->get_master(),
                                                   gko::dim<2>(local_size_x), nnz_local);
220
         IndexType *lmat_row_ptrs = local_matrix_compute->get_row_ptrs();
IndexType *lmat_col_idxs = local_matrix_compute->get_col_idxs();
221
222
223
         ValueType *lmat_values = local_matrix_compute->get_values();
224
225
         std::shared_ptr<mtx> interface_matrix_compute;
         if (nnz_interface > 0) {
226
227
              interface matrix compute =
228
                  mtx::create(settings.executor->get_master(),
229
                                 gko::dim<2>(local_size_x), nnz_interface);
230
         } else {
231
             interface_matrix_compute = mtx::create(settings.executor->get_master());
232
233
```

```
234
         IndexType *imat_row_ptrs = interface_matrix_compute->get_row_ptrs();
235
         IndexType *imat_col_idxs = interface_matrix_compute->get_col_idxs();
236
         ValueType *imat_values = interface_matrix_compute->get_values();
237
238
         num = 0:
239
         nnz local = 0:
240
         auto nnz_interface_temp = 0;
         lmat_row_ptrs[0] = nnz_local;
if (nnz_interface > 0) {
241
242
243
             imat_row_ptrs[0] = nnz_interface_temp;
244
         // Local interior matrix
245
246
         for (auto i = first_row[my_rank]; i < first_row[my_rank + 1]; ++i) {</pre>
247
             for (auto j = gmat_row_ptrs[i]; j < gmat_row_ptrs[i + 1]; ++j) {</pre>
248
                  if (global_to_local[gmat_col_idxs[j]] != 0) {
249
                       lmat_col_idxs[nnz_local] =
                           global_to_local[gmat_col_idxs[j]] - 1;
250
                       lmat_values[nnz_local] = gmat_values[j];
251
                      nnz_local++;
252
253
                  }
254
255
             if (nnz_interface > 0) {
                  imat_row_ptrs[num + 1] = nnz_interface_temp;
256
2.57
258
             lmat_row_ptrs[num + 1] = nnz_local;
259
             num++;
260
261
         // Interface matrix
2.62
         if (nnz_interface > 0) {
263
             nnz_interface = 0;
264
265
             for (auto k = 0; k < metadata.overlap_size; k++) {</pre>
266
                  temp = metadata.overlap_row->get_data()[k];
267
                  for (auto j = gmat_row_ptrs[temp]; j < gmat_row_ptrs[temp + 1];</pre>
                       j++) {
268
                       if (global_to_local[gmat_col_idxs[j]] != 0) {
269
                           lmat_col_idxs[nnz_local] =
    global_to_local[gmat_col_idxs[j]] - 1;
270
271
272
                           lmat_values[nnz_local] = gmat_values[j];
273
                           nnz_local++;
274
                       } else {
275
                           imat_col_idxs[nnz_interface] = gmat_col_idxs[j];
276
                           imat_values[nnz_interface] = gmat_values[j];
                           nnz_interface++;
278
                      }
279
                  lmat_row_ptrs[num + 1] = nnz_local;
imat_row_ptrs[num + 1] = nnz_interface;
280
281
282
                  num++;
283
             }
284
285
         auto now = num;
286
         for (auto i = old; i < now; i++) {</pre>
287
             for (auto j = gmat_row_ptrs[local_to_global[i]];
                  j < gmat_row_ptrs[local_to_global[i] + 1]; j++) {
if (global_to_local[gmat_col_idxs[j]] == 0) {
    local_to_global[num] = gmat_col_idxs[j];</pre>
288
289
290
291
                      global_to_local[gmat_col_idxs[j]] = 1 + num;
292
                      num++;
293
                  }
294
             }
295
296
297
         local_matrix = mtx::create(settings.executor);
298
         local_matrix->copy_from(gko::lend(local_matrix_compute));
299
         interface_matrix = mtx::create(settings.executor);
300
         interface_matrix->copy_from(gko::lend(interface_matrix_compute));
301
302
         local matrix->sort by column index();
303
         interface_matrix->sort_by_column_index();
304 }
```

## 7.16.3.3 setup\_windows()

```
const Metadata< ValueType, IndexType > & metadata,
    std::shared_ptr< gko::matrix::Dense< ValueType >> & main_buffer ) [override],
[virtual]
```

Sets up the windows needed for the asynchronous communication.

#### **Parameters**

| settings    | The settings struct.                                    |
|-------------|---|
| metadata    | The metadata struct.                                    |
| main_buffer | The main buffer being exchanged between the subdomains. |

Implements schwz::Communicate < ValueType, IndexType >.

schwz::Settings::comm\_settings::enable\_get, schwz::Settings::comm\_settings::enable\_lock\_ all, schwz::Settings::comm\_settings::enable\_one\_by\_one, schwz::Settings::comm\_settings::enable\_onesided, schwz::Settings::comm settings::enable overlap, schwz::Settings::comm settings::enable put, schwz::Settings⇔ ::executor, schwz::Communicate< ValueType, IndexType >::comm\_struct::get\_displacements, schwz::← Communicate < ValueType, IndexType >::comm struct::get request, schwz::Communicate < ValueType, Index← Type >::comm\_struct::global\_get, schwz::Communicate< ValueType, IndexType >::comm\_struct::global\_put, schwz::SchwarzBase< ValueType, IndexType >::global solution, schwz::Communicate< ValueType, Index← Type >::comm\_struct::is\_local\_neighbor, schwz::Metadata< ValueType, IndexType >::iter\_count, schwz::← Communicate < ValueType, IndexType >::comm\_struct::local\_get, schwz::Communicate < ValueType, Index ← Type >::comm\_struct::local\_neighbors\_in, schwz::Communicate< ValueType, IndexType >::comm\_struct← ::local neighbors out, schwz::Communicate < ValueType, IndexType >::comm struct::local num neighbors in, schwz::Communicate < ValueType, IndexType >::comm\_struct::local\_num\_neighbors\_out, schwz::Communicate < ValueType, IndexType >::comm\_struct::local\_put, schwz::Metadata< ValueType, IndexType >::local\_size\_← o, schwz::SchwarzBase< ValueType, IndexType >::local\_solution, schwz::Communicate< ValueType, IndexType >::comm\_struct::neighbors\_in, schwz::Communicate< ValueType, IndexType >::comm\_struct::neighbors\_← out, schwz::Communicate < ValueType, IndexType >::comm struct::num neighbors in, schwz::Communicate < ValueType, IndexType >::comm struct::num neighbors out, schwz::Metadata < ValueType, IndexType >::num ← subdomains, schwz::Communicate< ValueType, IndexType >::comm struct::put displacements, schwz::← Communicate < ValueType, IndexType >::comm struct::put request, schwz::Communicate < ValueType, Index← Type >::comm\_struct::recv\_buffer, schwz::Communicate< ValueType, IndexType >::comm\_struct::remote\_get, schwz::Communicate < ValueType, IndexType >::comm\_struct::remote\_put, schwz::Communicate < ValueType, IndexType >::comm struct::send buffer, schwz::Communicate < ValueType, IndexType >::comm struct::window ← recv buffer, schwz::Communicate < ValueType, IndexType >::comm struct::window send buffer, and schwz:: ← Communicate < ValueType, IndexType >::comm\_struct::window\_x.

```
508 {
509
        using vec_itype = gko::Array<IndexType>;
510
        using vec_vtype = gko::matrix::Dense<ValueType>;
511
        auto num_subdomains = metadata.num_subdomains;
512
        auto local size o = metadata.local size o:
513
        auto neighbors_in = this->comm_struct.neighbors_in->get_data();
514
        auto global_get = this->comm_struct.global_get->get_data();
515
        auto neighbors_out = this->comm_struct.neighbors_out->get_data();
516
        auto global_put = this->comm_struct.global_put->get_data();
517
        // set displacement for the MPI buffer
518
        auto get_displacements = this->comm_struct.get_displacements->get_data();
519
       auto put_displacements = this->comm_struct.put_displacements->get_data();
520
521
522
            std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
523
            tmp_num_comm_elems[0] = 0;
524
            for (auto j = 0; j < this->comm_struct.num_neighbors_in; j++) {
                if ((global_get[j])[0] > 0) {
525
                    int p = neighbors_in[j];
527
                    tmp_num_comm_elems[p + 1] = (global_get[j])[0];
528
529
            for (auto j = 0; j < num_subdomains; j++) {</pre>
530
531
                tmp_num_comm_elems[j + 1] += tmp_num_comm_elems[j];
532
```

```
534
            auto mpi_itype = boost::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
535
            MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, put_displacements,
536
                         1, mpi_itype, MPI_COMM_WORLD);
537
538
539
540
           std::vector<IndexType> tmp_num_comm_elems(num_subdomains + 1, 0);
541
            tmp_num_comm_elems[0] = 0;
542
            for (auto j = 0; j < this->comm_struct.num_neighbors_out; j++) {
543
                if ((global_put[j])[0] > 0)
544
                    int p = neighbors_out[j];
545
                    tmp_num_comm_elems[p + 1] = (global_put[j])[0];
546
                }
547
548
           for (auto j = 0; j < num_subdomains; j++) {</pre>
549
                tmp_num_comm_elems[j + 1] += tmp_num_comm_elems[j];
550
551
552
           auto mpi_itype = boost::mpi::get_mpi_datatype(tmp_num_comm_elems[0]);
553
           MPI_Alltoall(tmp_num_comm_elems.data(), 1, mpi_itype, get_displacements,
                         1, mpi_itype, MPI_COMM_WORLD);
554
555
556
557
       // setup windows
558
       if (settings.comm_settings.enable_onesided) {
559
            // Onesided
560
           MPI_Win_create(main_buffer->get_values(),
561
                           main_buffer->get_size()[0] * sizeof(ValueType)
562
                           sizeof(ValueType), MPI_INFO_NULL, MPI_COMM_WORLD,
563
                           &(this->comm_struct.window_x));
564
565
566
567
        if (settings.comm_settings.enable_onesided) {
568
            // MPI_Alloc_mem ? Custom allocator ? TODO
           569
570
571
                           MPI_INFO_NULL, MPI_COMM_WORLD,
572
                           &(this->window_residual_vector));
573
            std::vector<IndexType> zero_vec(num_subdomains, 0);
574
           gko::Array<IndexType> temp_array{settings.executor->get_master(),
575
                                             zero_vec.begin(), zero_vec.end()};
           this->convergence_vector = std::shared_ptr<vec_itype>(
576
577
                new vec_itype(settings.executor->get_master(), temp_array),
578
                std::default_delete<vec_itype>());
579
           this->convergence_sent = std::shared_ptr<vec_itype>(
580
                new vec_itype(settings.executor->get_master(), num_subdomains),
581
                std::default_delete<vec_itype>());
582
           this->convergence_local = std::shared_ptr<vec_itype>(
583
               new vec itype(settings.executor->get master(), num subdomains),
584
                std::default_delete<vec_itype>());
585
           MPI_Win_create(this->convergence_vector->get_data(),
586
                           (num_subdomains) * sizeof(IndexType), sizeof(IndexType),
587
                           MPI_INFO_NULL, MPI_COMM_WORLD,
588
                           &(this->window_convergence));
589
       }
590
591
        if (settings.comm_settings.enable_onesided && num_subdomains > 1) {
592
           // Lock all windows.
593
           if (settings.comm_settings.enable_get &&
594
                settings.comm_settings.enable_lock_all) {
595
                MPI_Win_lock_all(0, this->comm_struct.window_send_buffer);
596
597
           if (settings.comm_settings.enable_put &&
598
                settings.comm_settings.enable_lock_all) {
599
                MPI_Win_lock_all(0, this->comm_struct.window_recv_buffer);
600
            if (settings.comm_settings.enable_one_by_one &&
    settings.comm_settings.enable_lock_all) {
601
602
603
                MPI_Win_lock_all(0, this->comm_struct.window_x);
604
605
            MPI_Win_lock_all(0, this->window_residual_vector);
606
           MPI_Win_lock_all(0, this->window_convergence);
607
608 }
```

## 7.16.3.4 update\_boundary()

```
template<typename ValueType , typename IndexType >
void schwz::SolverRAS< ValueType, IndexType >::update_boundary (
```

Update the values into local vector from obtained from the neighboring sub-domains using the interface matrix.

#### **Parameters**

| settings   | The settings struct.  |
|--|---|
| metadata   | The metadata struct.  |
| local_solution   | The local solution vector in the subdomain.   |
| local_rhs  | The local right hand side vector in the subdomain.  |
| global_solution  | The workspace solution vector.  |
| global_old_solution  The global solution vector of the previous iteration. |   |
| interface_matrix   | The interface matrix containing the interface and the overlap data mainly used for exchanging values between different sub-domains. |

Implements schwz::Communicate < ValueType, IndexType >.

References schwz::Settings::executor, schwz::SchwarzBase< ValueType, IndexType >::global\_solution, schwz::SchwarzBase< ValueType, IndexType >::interface\_matrix, schwz::SchwarzBase< ValueType, IndexType >::local\_rhs, schwz::Metadata< ValueType, IndexType >::local\_size\_x, schwz::SchwarzBase< ValueType, IndexType >::local\_solution, schwz::Metadata< ValueType, IndexType >::num\_subdomains, and schwz::Settings::overlap.

```
818 {
819
        using vec_vtype = gko::matrix::Dense<ValueType>;
820
        auto one = gko::initialize<gko::matrix::Dense<ValueType>>(
            {1.0}, settings.executor);
821
        auto neg_one = gko::initialize<gko::matrix::Dense<ValueType>>(
            {-1.0}, settings.executor);
824
        auto local_size_x = metadata.local_size_x;
825
        local_solution->copy_from(local_rhs.get());
826
        if (metadata.num_subdomains > 1 && settings.overlap > 0) {
827
            auto temp_solution = vec_vtype::create(
    settings.executor, local_solution->get_size(),
828
829
                 gko::Array<ValueType>::view(settings.executor,
830
                                               local_solution->get_size()[0],
831
                                               global_solution->get_values()),
832
833
            interface_matrix->apply(neg_one.get(), temp_solution.get(), one.get(),
834
                                      local solution.get());
        }
```

The documentation for this class was generated from the following files:

- restricted\_schwarz.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/restricted\_schwarz.cpp (68412d6)

# 7.17 UmfpackError Class Reference

UmfpackError is thrown when a METIS routine throws a non-zero error code.

```
#include <exception.hpp>
```

## **Public Member Functions**

UmfpackError (const std::string &file, int line, const std::string &func, int error\_code)
 Initializes a METIS error.

## 7.17.1 Detailed Description

UmfpackError is thrown when a METIS routine throws a non-zero error code.

#### 7.17.2 Constructor & Destructor Documentation

## 7.17.2.1 UmfpackError()

Initializes a METIS error.

## **Parameters**

| file  | The name of the offending source file     |
|---|---|
| line The source code line number where the error of |   |
| func  | The name of the METIS routine that failed |
| error_code  | The resulting METIS error code            |

```
205 : Error(file, line, func + ": " + get_error(error_code))
206      {}
```

The documentation for this class was generated from the following files:

- exception.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/exception.cpp (68412d6)

# 7.18 schwz::Utils < ValueType, IndexType > Struct Template Reference

The utilities class which provides some checks and basic utilities.

```
#include <utils.hpp>
```

# 7.18.1 Detailed Description

 $template < typename\ ValueType = gko::default\_precision,\ typename\ IndexType = gko::int32 > struct\ schwz::Utils < ValueType,\ IndexType >$ 

The utilities class which provides some checks and basic utilities.

## **Template Parameters**

| ValueType | The type of the floating point values. |
|-----------|--|
| IndexType | The type of the index type values.     |

## Utils

The documentation for this struct was generated from the following files:

- utils.hpp (68412d6)
- /home/runner/work/schwarz-lib/schwarz-lib/source/utils.cpp (68412d6)

# Index

| BadDimension, 19                    | remote_put   |
|-------------------------------------|--|
| BadDimension, 19                    | schwz::Communicate::comm_struct, 24                        |
|                                     | run  |
| Communicate, 9                      | schwz::SchwarzBase, 43                                     |
| CudaError, 28                       |  |
| CudaError, 28                       | Schwarz Class, 11  |
| CusparseError, 29                   | SchwarzBase  |
| CusparseError, 29                   | schwz::SchwarzBase, 41                                     |
|                                     | schwz, 15  |
| exchange_boundary                   | schwz::CommHelpers, 16                                     |
| schwz::Communicate, 25              | schwz::Communicate   |
| schwz::SolverRAS, 49                | exchange_boundary, 25                                      |
| explicit_laplacian                  | local_to_global_vector, 26                                 |
| schwz::Settings, 47                 | setup_windows, 26  |
|                                     | update_boundary, 27  |
| generate_rhs                        | schwz::Communicate < ValueType, IndexType >, 24            |
| schwz::Initialize, 31               | schwz::Communicate< ValueType, IndexType > -               |
| global_get                          | ::comm_struct, 21  |
| schwz::Communicate::comm_struct, 22 | schwz::Communicate::comm_struct                            |
| global_put                          | global_get, 22   |
| schwz::Communicate::comm_struct, 22 | global_put, 22   |
|                                     | is_local_neighbor, 23                                      |
| Initialization, 10                  | local get, 23  |
| is_local_neighbor                   | local_put, 23  |
| schwz::Communicate::comm_struct, 23 | remote_get, 23   |
|                                     | remote_put, 24   |
| local_get                           | schwz::Initialize  |
| schwz::Communicate::comm_struct, 23 | generate_rhs, 31   |
| local_put                           | partition, 32  |
| schwz::Communicate::comm_struct, 23 | setup_global_matrix, 33                                    |
| local_solver_tolerance              | setup_local_matrices, 34                                   |
| schwz::Metadata, 38                 | setup_vectors, 35  |
| local_to_global_vector              | schwz::Initialize < ValueType, IndexType >, 30             |
| schwz::Communicate, 26              | schwz::Metadata  |
|                                     | local_solver_tolerance, 38                                 |
| MetisError, 38                      | tolerance, 38  |
| MetisError, 39                      | schwz::Metadata< ValueType, IndexType >, 36                |
|                                     | schwz::Metadata < ValueType, IndexType >::post_ \leftarrow |
| naturally_ordered_factor            | process data, 39   |
| schwz::Settings, 47                 | schwz::PartitionTools, 17                                  |
| on audition                         | schwz::SchwarzBase   |
| partition                           | print_matrix, 42   |
| schwz::Initialize, 32               | print_vector, 43   |
| print_matrix                        | • –  |
| schwz::SchwarzBase, 42              | run, 43  |
| print_vector                        | SchwarzBase, 41  |
| schwz::SchwarzBase, 43              | schwa::SchwarzBase< ValueType, IndexType >, 40             |
| ProcessTopology, 15                 | schwz::Settings, 45  |
|                                     | explicit_laplacian, 47                                     |
| remote_get                          | naturally_ordered_factor, 47                               |
| schwz::Communicate::comm_struct, 23 | schwz::Settings::comm_settings, 20                         |

62 INDEX

```
schwz::Settings::convergence_settings, 28
schwz::Solve < ValueType, IndexType >, 47
schwz::SolverRAS< ValueType, IndexType >, 48
schwz::SolverRAS
    exchange_boundary, 49
    setup local matrices, 50
    setup_windows, 53
    SolverRAS, 49
    update boundary, 55
schwz::SolverTools, 17
schwz::Utils < ValueType, IndexType >, 57
schwz::conv_tools, 16
schwz::device_guard, 30
setup_global_matrix
    schwz::Initialize, 33
setup_local_matrices
    schwz::Initialize, 34
    schwz::SolverRAS, 50
setup_vectors
    schwz::Initialize, 35
setup windows
    schwz::Communicate, 26
    schwz::SolverRAS, 53
Solve, 12
SolverRAS
    schwz::SolverRAS, 49
tolerance
    schwz::Metadata, 38
UmfpackError, 56
    UmfpackError, 57
update_boundary
    schwz::Communicate, 27
    schwz::SolverRAS, 55
Utils, 13
```