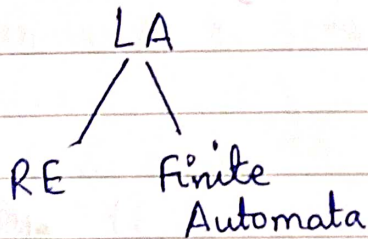


14/08/2022

## Regular Expression:

Tokens are described by regular expression.



Spaces, semicolons are delimiters.

$$\boxed{id = L(LID)^*}$$

Let  $r$  and  $s$  be two REs and language generated by those expressions are  $L(r)$  and  $L(s)$  respectively which is accepted by the finite automata  $N(r)$  &  $N(s)$  respectively.

$$r|s \rightarrow \text{regular expression} \rightarrow L(r|s) \rightarrow L(r) \cup L(s)$$

$$rs \rightarrow L(r)L(s)$$

$$r^* \rightarrow L(r)^*$$

1.  $\epsilon \longrightarrow \{\epsilon\}$
2.  $a \longrightarrow \{a\}$
3.  $a|b \longrightarrow \{a, b\}$
4.  $ab \longrightarrow \{ab\}$
5.  $a^* \longrightarrow \{\epsilon, a, aa, \dots\}$
6.  $a^+ \longrightarrow \{a, aa, \dots\}$

Date \_\_\_\_ / \_\_\_\_ / \_\_\_\_

1. The set of all strings of a's and b's of length 2.
2. The set of all strings of ~~zero or more~~ <sup>zero</sup> and more b's.
3. The set of all strings containing a and consist of zero or more a's followed by ab.
4. For exactly one a.
5. Give the RE at least 2 a.

### Answer

1. RE =

$$aa | ab | ba | bb = (a|b)(a|b)$$

2. RE =  $(a+b)^*$

3. RE =  $a|a^*b$

4. RE =  $b^*ab^*$

5. RE =

$$\rightarrow a^*b^*a^*b^*a^*b^* \times$$

$$\rightarrow (a+b)^*a(a+b)^*a(a+b)^*$$

abba

abba

### Homework

- ① Define the language i.e. it should contain at least one ~~double~~ letter.
- ② Write one regular exp over alphabet  $\{0,1\}$  for the ~~state~~ <sup>set</sup> of strings with even no of zeros followed by odd no of 1's.
- ③ Write a regular expression for the language in which word ending with either aa or single b.



4. Write the r.e. for all string with even no. of zeros followed by an odd no. of 1's.  $(00^*)^+(11^*)^1$
5. Write a regular expression for the language that the set of all string that begin or end with 00 or 11.
6. Write a regular expression for the set of all strings in which both the no. of a's and no. of b's are even.

$$x \in (V \cup T)^+ \quad x \rightarrow y$$

$$y \in (V \cup T)^*$$

### Answers

①  $(a+b)^*(aa+bb)(a+b)^*$

②  $(00)^*(11)^*1$

③  $(a+b)^*(aa+b)$

④  $(00)^*(11)^*1$

⑤  $(00+11)(0+1)^*(00+11)$

⑥  $(aa+bb)^*$

$((ab+ba)(aa+bb)^*(ab+ba) + (aa+bb)^*)^*$

$(aa + abba + bb)^*$   
 $(ab+ba)(ab+ba)$

abba

baab

baaabbbaabaabbbaa

abbabaab

