

Solutions to DSA Questions 26-50 (Strings and Linked Lists) For 1-2 Years

Experience Roles at EPAM Compiled on September 26, 2025

Introduction

This document provides detailed solutions for 25 Data Structures and Algorithms (DSA) problems (questions 26 to 50) from the Strings and Linked Lists categories, tailored for candidates with 1-2 years of experience preparing for roles at EPAM Systems. Each problem includes a problem statement, dry run with test cases, algorithm, and a Python solution, formatted for clarity and ease of understanding. These problems cover fundamental to intermediate concepts frequently tested in technical interviews.

Contents

| | |
|---|----------|
| 1 Check if a String is a Palindrome | 4 |
| 1.1 Problem Statement | 4 |
| 1.2 Dry Run on Test Cases | 4 |
| 1.3 Algorithm | 4 |
| 1.4 Python Solution | 5 |
| 2 Reverse Words in a String | 5 |
| 2.1 Problem Statement | 5 |
| 2.2 Dry Run on Test Cases | 5 |
| 2.3 Algorithm | 5 |
| 2.4 Python Solution | 5 |
| 3 Longest Substring Without Repeating Characters | 6 |
| 3.1 Problem Statement | 6 |
| 3.2 Dry Run on Test Cases | 6 |
| 3.3 Algorithm | 6 |
| 3.4 Python Solution | 6 |
| 4 Valid Parentheses | 7 |
| 4.1 Problem Statement | 7 |
| 4.2 Dry Run on Test Cases | 7 |
| 4.3 Algorithm | 7 |
| 4.4 Python Solution | 7 |
| 5 Longest Palindromic Substring | 7 |
| 5.1 Problem Statement | 8 |
| 5.2 Dry Run on Test Cases | 8 |
| 5.3 Algorithm | 8 |
| 5.4 Python Solution | 8 |

| | |
|---|-----------|
| 6 Generate All Permutations of a String | 8 |
| 6.1 Problem Statement | 9 |
| 6.2 Dry Run on Test Cases | 9 |
| 6.3 Algorithm | 9 |
| 6.4 Python Solution | 9 |
| 7 Check if Strings are Rotations of Each Other | 9 |
| 7.1 Problem Statement | 9 |
| 7.2 Dry Run on Test Cases | 10 |
| 7.3 Algorithm | 10 |
| 7.4 Python Solution | 10 |
| 8 Find First Non-Repeating Character | 10 |
| 8.1 Problem Statement | 10 |
| 8.2 Dry Run on Test Cases | 10 |
| 8.3 Algorithm | 10 |
| 8.4 Python Solution | 11 |
| 9 String to Integer (atoi) | 11 |
| 9.1 Problem Statement | 11 |
| 9.2 Dry Run on Test Cases | 11 |
| 9.3 Algorithm | 11 |
| 9.4 Python Solution | 12 |
| 10 Longest Common Prefix | 12 |
| 10.1 Problem Statement | 12 |
| 10.2 Dry Run on Test Cases | 12 |
| 10.3 Algorithm | 12 |
| 10.4 Python Solution | 13 |
| 11 Group Anagrams | 13 |
| 11.1 Problem Statement | 13 |
| 11.2 Dry Run on Test Cases | 13 |
| 11.3 Algorithm | 13 |
| 11.4 Python Solution | 13 |
| 12 Valid IP Address | 14 |
| 12.1 Problem Statement | 14 |
| 12.2 Dry Run on Test Cases | 14 |
| 12.3 Algorithm | 14 |
| 12.4 Python Solution | 14 |
| 13 Edit Distance | 15 |
| 13.1 Problem Statement | 15 |
| 13.2 Dry Run on Test Cases | 15 |
| 13.3 Algorithm (Memoization) | 15 |
| 13.4 Python Solution (Memoization) | 15 |
| 13.5 Python Solution (Tabulation) | 16 |
| 14 Smallest Window Containing All Characters | 16 |

| | |
|--|-----------|
| 14.1 Problem Statement | 16 |
| 14.2 Dry Run on Test Cases | 16 |
| 14.3 Algorithm | 17 |
| 14.4 Python Solution | 17 |
| 15 Longest Increasing Subsequence in String | 18 |
| 15.1 Problem Statement | 18 |
| 15.2 Dry Run on Test Cases | 18 |
| 15.3 Algorithm (Memoization) | 18 |
| 15.4 Python Solution (Memoization) | 18 |
| 15.5 Python Solution (Tabulation) | 19 |
| 16 Check for Valid Shuffle of Two Strings | 19 |
| 16.1 Problem Statement | 19 |
| 16.2 Dry Run on Test Cases | 19 |
| 16.3 Algorithm | 19 |
| 16.4 Python Solution | 20 |
| 17 Remove Duplicate Letters | 20 |
| 17.1 Problem Statement | 20 |
| 17.2 Dry Run on Test Cases | 20 |
| 17.3 Algorithm | 20 |
| 17.4 Python Solution | 20 |
| 18 Find All Palindromic Substrings | 21 |
| 18.1 Problem Statement | 21 |
| 18.2 Dry Run on Test Cases | 21 |
| 18.3 Algorithm | 21 |
| 18.4 Python Solution | 21 |
| 19 Rabin-Karp String Matching | 22 |
| 19.1 Problem Statement | 22 |
| 19.2 Dry Run on Test Cases | 22 |
| 19.3 Algorithm | 22 |
| 19.4 Python Solution | 22 |
| 20 KMP Algorithm for Pattern Searching | 23 |
| 20.1 Problem Statement | 23 |
| 20.2 Dry Run on Test Cases | 23 |
| 20.3 Algorithm | 23 |
| 20.4 Python Solution | 23 |
| 21 Reverse a Linked List | 24 |
| 21.1 Problem Statement | 24 |
| 21.2 Dry Run on Test Cases | 25 |
| 21.3 Algorithm | 25 |
| 21.4 Python Solution | 25 |
| 22 Detect Cycle in a Linked List | 25 |
| 22.1 Problem Statement | 25 |

| | |
|---|-----------|
| 22.2 Dry Run on Test Cases | 25 |
| 22.3 Algorithm | 26 |
| 22.4 Python Solution | 26 |
| 23 Merge Two Sorted Linked Lists | 26 |
| 23.1 Problem Statement | 26 |
| 23.2 Dry Run on Test Cases | 26 |
| 23.3 Algorithm | 27 |
| 23.4 Python Solution | 27 |
| 24 Remove Nth Node from End | 27 |
| 24.1 Problem Statement | 27 |
| 24.2 Dry Run on Test Cases | 27 |
| 24.3 Algorithm | 28 |
| 24.4 Python Solution | 28 |
| 25 Find Middle of Linked List | 28 |
| 25.1 Problem Statement | 28 |
| 25.2 Dry Run on Test Cases | 28 |
| 25.3 Algorithm | 28 |
| 25.4 Python Solution | 29 |

1 Check if a String is a Palindrome

1.1 Problem Statement

Given a string, determine if it is a palindrome (reads the same forward and backward), considering only alphanumeric characters and ignoring cases.

1.2 Dry Run on Test Cases

- **Test Case 1:** Input = "A man, a plan, a canal: Panama" → Output: True
- **Test Case 2:** Input = "race a car" → Output: False
- **Test Case 3:** Input = "" → Output: True
- **Test Case 4:** Input = "0P" → Output: False

1.3 Algorithm

1. Convert string to lowercase and filter alphanumeric characters.
2. Use two pointers: left from start, right from end.
3. Compare characters; if mismatch, return False.
4. If pointers meet, return True.

Time Complexity: $O(n)$ Space Complexity: $O(1)$ or $O(n)$ if new string created

1.4 Python Solution

```
1 def is_palindrome(s):
2     # Filter alphanumeric and convert to lowercase
3     filtered = ''.join(c.lower() for c in s if c.isalnum())
4     left, right = 0, len(filtered) - 1
5
6     while left < right:
7         if filtered[left] != filtered[right]:
8             return False
9         left += 1
10        right -= 1
11    return True
12
13 # Example usage
14 print(is_palindrome("A man, a plan, a canal: Panama")) # Output:
15      True
```

2 Reverse Words in a String

2.1 Problem Statement

Given a string, reverse the order of words, removing extra spaces.

2.2 Dry Run on Test Cases

- **Test Case 1:** Input = "the sky is blue" → Output: "blue is sky the"
- **Test Case 2:** Input = " hello world " → Output: "world hello"
- **Test Case 3:** Input = "a" → Output: "a"
- **Test Case 4:** Input = "" → Output: ""

2.3 Algorithm

1. Split string into words, filter out empty strings.
2. Reverse the list of words.
3. Join words with single space.

Time Complexity: $O(n)$ Space Complexity: $O(n)$

2.4 Python Solution

```
1 def reverse_words(s):
2     words = [word for word in s.split() if word]
```

```

3     words.reverse()
4     return ' '.join(words)
5
6 # Example usage
7 print(reverse_words("the sky is blue")) # Output: "blue is sky
    the"

```

3 Longest Substring Without Repeating Characters

3.1 Problem Statement

Given a string, find the length of the longest substring without repeating characters.

3.2 Dry Run on Test Cases

- **Test Case 1:** Input = "abcabcbb" → Output: 3 ("abc")
- **Test Case 2:** Input = "bbbbbb" → Output: 1 ("b")
- **Test Case 3:** Input = "pwwkew" → Output: 3 ("wke")
- **Test Case 4:** Input = "" → Output: 0

3.3 Algorithm

1. Use sliding window with hashmap to store last seen index of characters.
2. Move right pointer, update max length.
3. If character repeats, move left pointer to last seen + 1.

Time Complexity: $O(n)$ **Space Complexity:** $O(\min(m, n))$

3.4 Python Solution

```

1 def length_of_longest_substring(s):
2     char_index = {}
3     max_length = 0
4     left = 0
5
6     for right, char in enumerate(s):
7         if char in char_index and char_index[char] >= left:
8             left = char_index[char] + 1
9         else:
10             max_length = max(max_length, right - left + 1)
11             char_index[char] = right
12     return max_length
13
14 # Example usage
15 print(length_of_longest_substring("abcabcbb")) # Output: 3

```

4 Valid Parentheses

4.1 Problem Statement

Given a string containing only '(', ')', '[', ']', determine if it is valid (matching pairs).

4.2 Dry Run on Test Cases

- **Test Case 1:** Input = "()" → Output: True
- **Test Case 2:** Input = "()[]" → Output: True
- **Test Case 3:** Input = "()" → Output: False
- **Test Case 4:** Input = "([])" → Output: False

4.3 Algorithm

1. Use a stack to track opening brackets.
2. For each character:
 - If opening, push to stack.
 - If closing, check if matches stack top; pop if match, else return False.
3. Return True if stack empty.

Time Complexity: $O(n)$ **Space Complexity:** $O(n)$

4.4 Python Solution

```
1 def is_valid(s):
2     stack = []
3     brackets = {')': '(', '}': '{', ']': '['}
4
5     for char in s:
6         if char in brackets.values():
7             stack.append(char)
8         elif char in brackets:
9             if not stack or stack.pop() != brackets[char]:
10                 return False
11     return len(stack) == 0
12
13 # Example usage
14 print(is_valid("()[]{}")) # Output: True
```

5 Longest Palindromic Substring

5.1 Problem Statement

Given a string, find the longest substring that is a palindrome.

5.2 Dry Run on Test Cases

- **Test Case 1:** Input = "babad" → Output: "bab" or "aba"
- **Test Case 2:** Input = "cbbd" → Output: "bb"
- **Test Case 3:** Input = "a" → Output: "a"
- **Test Case 4:** Input = "" → Output: ""

5.3 Algorithm

1. For each index, expand around center for odd and even length palindromes.
2. Track max length and substring.
3. Return longest palindrome found.

Time Complexity: $O(n^2)$ **Space Complexity:** $O(1)$

5.4 Python Solution

```
1 def longest_palindrome(s):
2     def expand_around_center(left, right):
3         while left >= 0 and right < len(s) and s[left] == s[right]:
4             left -= 1
5             right += 1
6         return left + 1, right - 1
7
8     start, end = 0, 0
9     for i in range(len(s)):
10        left1, right1 = expand_around_center(i, i) # Odd length
11        left2, right2 = expand_around_center(i, i + 1) # Even
12        if right1 - left1 > end - start:
13            start, end = left1, right1
14        if right2 - left2 > end - start:
15            start, end = left2, right2
16    return s[start:end + 1]
17
18 # Example usage
19 print(longest_palindrome("babad")) # Output: "bab" or "aba"
```

6 Generate All Permutations of a String

6.1 Problem Statement

Given a string, return all possible permutations.

6.2 Dry Run on Test Cases

- **Test Case 1:** Input = "abc" → Output: ["abc", "acb", "bac", "bca", "cab", "cba"]
- **Test Case 2:** Input = "a" → Output: ["a"]
- **Test Case 3:** Input = "" → Output: []
- **Test Case 4:** Input = "aa" → Output: ["aa"]

6.3 Algorithm

1. Use backtracking: swap characters at each position.
2. Recurse to generate permutations for remaining characters.
3. Collect all permutations in result.

Time Complexity: $O(n!)$ **Space Complexity:** $O(n!)$

6.4 Python Solution

```
1 def permute(s):
2     def backtrack(arr, start, result):
3         if start == len(arr):
4             result.append(''.join(arr))
5         for i in range(start, len(arr)):
6             arr[start], arr[i] = arr[i], arr[start]
7             backtrack(arr, start + 1, result)
8             arr[start], arr[i] = arr[i], arr[start]
9
10    result = []
11    backtrack(list(s), 0, result)
12    return result
13
14 # Example usage
15 print(permute("abc")) # Output: ["abc", "acb", "bac", "bca", "cab", "cba"]
```

7 Check if Strings are Rotations of Each Other

7.1 Problem Statement

Given two strings, check if one is a rotation of the other.

7.2 Dry Run on Test Cases

- **Test Case 1:** $s1 = "abcde"$, $s2 = "cdeab"$ → Output: True
- **Test Case 2:** $s1 = "abcde"$, $s2 = "abced"$ → Output: False
- **Test Case 3:** $s1 = "", s2 = ""$ → Output: True
- **Test Case 4:** $s1 = "a"$, $s2 = "a"$ → Output: True

7.3 Algorithm

1. Check if lengths are equal; if not, return False.
2. Concatenate $s1$ with itself.
3. Check if $s2$ is a substring of $s1 + s1$.

Time Complexity: $O(n)$ Space Complexity: $O(n)$

7.4 Python Solution

```
1 def are_rotations(s1, s2):  
2     if len(s1) != len(s2):  
3         return False  
4     if not s1 and not s2:  
5         return True  
6     return s2 in (s1 + s1)  
7  
8 # Example usage  
9 print(are_rotations("abcde", "cdeab")) # Output: True
```

8 Find First Non-Repeating Character

8.1 Problem Statement

Given a string, find the index of the first non-repeating character.

8.2 Dry Run on Test Cases

- **Test Case 1:** Input = "leetcode" → Output: 0 ('l')
- **Test Case 2:** Input = "loveleetcode" → Output: 2 ('v')
- **Test Case 3:** Input = "aabb" → Output: -1
- **Test Case 4:** Input = "" → Output: -1

8.3 Algorithm

1. Use hashmap to count character frequencies.

2. Iterate string again to find first character with count 1.

3. Return its index or -1 if none.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$ (26 chars max)

8.4 Python Solution

```
1 def first_non_repeating(s):
2     count = {}
3     for char in s:
4         count[char] = count.get(char, 0) + 1
5
6     for i, char in enumerate(s):
7         if count[char] == 1:
8             return i
9     return -1
10
11 # Example usage
12 print(first_non_repeating("leetcode")) # Output: 0
```

9 String to Integer (atoi)

9.1 Problem Statement

Convert a string to a 32-bit signed integer, handling whitespace, signs, and overflow.

9.2 Dry Run on Test Cases

- **Test Case 1:** Input = "42" → Output: 42
- **Test Case 2:** Input = " -42" → Output: -42
- **Test Case 3:** Input = "4193 with words" → Output: 4193
- **Test Case 4:** Input = "2147483648" → Output: 2147483647

9.3 Algorithm

1. Strip leading whitespace.
2. Check sign (+ or -).
3. Build number digit by digit, check for overflow.
4. Return number or clamp to 32-bit range.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$

9.4 Python Solution

```
1 def atoi(s):
2     s = s.strip()
3     if not s:
4         return 0
5
6     sign = 1
7     i = 0
8     if s[0] in ['+', '-']:
9         sign = -1 if s[0] == '-' else 1
10        i += 1
11
12    result = 0
13    while i < len(s) and s[i].isdigit():
14        result = result * 10 + int(s[i])
15        if result * sign > 2**31 - 1:
16            return 2**31 - 1
17        if result * sign < -2**31:
18            return -2**31
19        i += 1
20    return result * sign
21
22 # Example usage
23 print(atoi("-42")) # Output: -42
```

10 Longest Common Prefix

10.1 Problem Statement

Given an array of strings, find the longest common prefix among them.

10.2 Dry Run on Test Cases

- **Test Case 1:** Input = ["flower", "flow", "flight"] → Output: "fl"
- **Test Case 2:** Input = ["dog", "racecar", "car"] → Output: ""
- **Test Case 3:** Input = ["interspecies", "interstellar"] → Output: "inter"
- **Test Case 4:** Input = ["a"] → Output: "a"

10.3 Algorithm

1. If empty array, return "".
2. Take first string as prefix.
3. For each string, reduce prefix while it doesn't match.

Time Complexity: $O(S)$ (S = total characters) **Space Complexity:** $O(1)$

10.4 Python Solution

```
1 def longest_common_prefix(strs):
2     if not strs:
3         return ""
4     prefix = strs[0]
5
6     for s in strs[1:]:
7         while s[:len(prefix)] != prefix:
8             prefix = prefix[:-1]
9             if not prefix:
10                 return ""
11
12     return prefix
13
14 # Example usage
15 print(longest_common_prefix(["flower", "flow", "flight"])) # Output: "fl"
```

11 Group Anagrams

11.1 Problem Statement

Given an array of strings, group anagrams together.

11.2 Dry Run on Test Cases

- **Test Case 1:** Input = ["eat", "tea", "tan", "ate", "nat", "bat"] → Output: [["eat", "tea", "ate"], ["tan", "nat"], ["bat"]]
- **Test Case 2:** Input = [""] → Output: [[]]
- **Test Case 3:** Input = ["a"] → Output: [["a"]]
- **Test Case 4:** Input = [] → Output: []

11.3 Algorithm

1. Use hashmap with sorted string as key, list of strings as value.
2. For each string, sort and add to map.
3. Return map values.

Time Complexity: $O(n \cdot k \log k)$ ($k = \text{max string length}$) **Space Complexity:** $O(n \cdot k)$

11.4 Python Solution

```
1 def group_anagrams(strs):
2     anagrams = {}
3     for s in strs:
```

```

4     key = ''.join(sorted(s))
5     anagrams[key] = anagrams.get(key, []) + [s]
6     return list(anagrams.values())
7
8 # Example usage
9 print(group_anagrams(["eat", "tea", "tan", "ate", "nat", "bat"]))

```

12 Valid IP Address

12.1 Problem Statement

Given a string, determine if it is a valid IPv4 address.

12.2 Dry Run on Test Cases

- **Test Case 1:** Input = "192.168.1.1" → Output: True
- **Test Case 2:** Input = "192.168.01.1" → Output: False
- **Test Case 3:** Input = "256.1.2.3" → Output: False
- **Test Case 4:** Input = "1.2.3" → Output: False

12.3 Algorithm

1. Split string by '.' and check for 4 parts.
2. For each part:
 - Check length, leading zeros, and range (0-255).
 - Ensure only digits.
3. Return True if all valid.

Time Complexity: $O(n)$ Space Complexity: $O(1)$

12.4 Python Solution

```

1 def valid_ip_address(s):
2     parts = s.split('.')
3     if len(parts) != 4:
4         return False
5
6     for part in parts:
7         if not part or (part[0] == '0' and len(part) > 1) or not
8             part.isdigit():
9                 return False
10            num = int(part)
11            if num < 0 or num > 255:

```

```

11         return False
12     return True
13
14 # Example usage
15 print(valid_ip_address("192.168.1.1")) # Output: True

```

13 Edit Distance

13.1 Problem Statement

Given two strings, find minimum operations (insert, delete, replace) to convert one to another.

13.2 Dry Run on Test Cases

- **Test Case 1:** word1 = "horse", word2 = "ros" → Output: 3
- **Test Case 2:** word1 = "intention", word2 = "execution" → Output: 5
- **Test Case 3:** word1 = "", word2 = "abc" → Output: 3
- **Test Case 4:** word1 = "a", word2 = "a" → Output: 0

13.3 Algorithm (Memoization)

1. Use recursive function with memoization.
2. If strings empty, return length of other.
3. If characters match, recurse on rest.
4. Else, take min of insert, delete, replace.

Time Complexity: $O(m \cdot n)$ **Space Complexity:** $O(m \cdot n)$

13.4 Python Solution (Memoization)

```

1 def edit_distance(word1, word2):
2     memo = {}
3
4     def dp(i, j):
5         if i == 0:
6             return j
7         if j == 0:
8             return i
9         if (i, j) in memo:
10            return memo[(i, j)]
11
12         if word1[i-1] == word2[j-1]:
13             memo[(i, j)] = dp(i-1, j-1)

```

```

14     else:
15         memo[(i, j)] = min(
16             dp(i-1, j) + 1,    # Delete
17             dp(i, j-1) + 1,    # Insert
18             dp(i-1, j-1) + 1  # Replace
19         )
20     return memo[(i, j)]
21
22 return dp(len(word1), len(word2))
23
24 # Example usage
25 print(edit_distance("horse", "ros"))  # Output: 3

```

13.5 Python Solution (Tabulation)

```

1 def edit_distance_tab(word1, word2):
2     m, n = len(word1), len(word2)
3     dp = [[0] * (n + 1) for _ in range(m + 1)]
4
5     for i in range(m + 1):
6         dp[i][0] = i
7     for j in range(n + 1):
8         dp[0][j] = j
9
10    for i in range(1, m + 1):
11        for j in range(1, n + 1):
12            if word1[i-1] == word2[j-1]:
13                dp[i][j] = dp[i-1][j-1]
14            else:
15                dp[i][j] = min(
16                    dp[i-1][j] + 1,    # Delete
17                    dp[i][j-1] + 1,    # Insert
18                    dp[i-1][j-1] + 1  # Replace
19                )
20    return dp[m][n]
21
22 # Example usage
23 print(edit_distance_tab("horse", "ros"))  # Output: 3

```

14 Smallest Window Containing All Characters

14.1 Problem Statement

Given two strings s and t, find the smallest window in s containing all characters of t.

14.2 Dry Run on Test Cases

- **Test Case 1:** s = "ADOBECODEBANC", t = "ABC" → Output: "BANC"

- **Test Case 2:** s = "a", t = "a" → Output: "a"
- **Test Case 3:** s = "a", t = "aa" → Output: ""
- **Test Case 4:** s = "abc", t = "d" → Output: ""

14.3 Algorithm

1. Use sliding window with two hashmaps.
2. Move right pointer until window contains all t characters.
3. Shrink left pointer to minimize window.
4. Track smallest window.

Time Complexity: $O(n)$ **Space Complexity:** $O(k)$ ($k = \text{charset size}$)

14.4 Python Solution

```

1  from collections import Counter
2
3  def min_window(s, t):
4      if not s or not t:
5          return ""
6
7      t_count = Counter(t)
8      required = len(t_count)
9      formed = 0
10     window_counts = {}
11
12    left = right = 0
13    min_len = float('inf')
14    min_window_substr = ""
15
16    while right < len(s):
17        window_counts[s[right]] = window_counts.get(s[right], 0) +
18            1
19        if s[right] in t_count and window_counts[s[right]] ==
20            t_count[s[right]]:
21            formed += 1
22
23            while left <= right and formed == required:
24                if right - left + 1 < min_len:
25                    min_len = right - left + 1
26                    min_window_substr = s[left:right + 1]
27
28                window_counts[s[left]] -= 1
29                if s[left] in t_count and window_counts[s[left]] <
30                    t_count[s[left]]:
31                    formed -= 1
32                left += 1

```

```

30         right += 1
31     return min_window_substr
32
33 # Example usage
34 print(min_window("ADOBECODEBANC", "ABC")) # Output: "BANC"

```

15 Longest Increasing Subsequence in String

15.1 Problem Statement

Given a string, find the length of the longest increasing subsequence of characters.

15.2 Dry Run on Test Cases

- **Test Case 1:** Input = "aebbcg" → Output: 3 ("abc")
- **Test Case 2:** Input = "abcde" → Output: 5
- **Test Case 3:** Input = "a" → Output: 1
- **Test Case 4:** Input = "" → Output: 0

15.3 Algorithm (Memoization)

1. Use recursive function with memoization.
2. For each index, consider including character if greater than previous.
3. Return max length.

Time Complexity: $O(n^2)$ **Space Complexity:** $O(n^2)$

15.4 Python Solution (Memoization)

```

1 def longest_increasing_subsequence(s):
2     memo = []
3
4     def lis(index, prev_char):
5         if index == len(s):
6             return 0
7         if (index, prev_char) in memo:
8             return memo[(index, prev_char)]
9
10        not_take = lis(index + 1, prev_char)
11        take = 0
12        if prev_char < s[index]:
13            take = 1 + lis(index + 1, s[index])
14
15        memo[(index, prev_char)] = max(take, not_take)
16        return memo[(index, prev_char)]

```

```

17     return lis(0, chr(0))
18
19
20 # Example usage
21 print(longest_increasing_subsequence("aebbcg")) # Output: 3

```

15.5 Python Solution (Tabulation)

```

1 def longest_increasing_subsequence_tab(s):
2     if not s:
3         return 0
4
5     n = len(s)
6     dp = [1] * n
7
8     for i in range(1, n):
9         for j in range(i):
10            if s[j] < s[i]:
11                dp[i] = max(dp[i], dp[j] + 1)
12
13
14 # Example usage
15 print(longest_increasing_subsequence_tab("aebbcg")) # Output: 3

```

16 Check for Valid Shuffle of Two Strings

16.1 Problem Statement

Given strings s_1 , s_2 , and result, check if result is a valid shuffle of s_1 and s_2 .

16.2 Dry Run on Test Cases

- **Test Case 1:** $s_1 = "abc"$, $s_2 = "def"$, result = "adbcef" → Output: True
- **Test Case 2:** $s_1 = "abc"$, $s_2 = "def"$, result = "abcdefg" → Output: False
- **Test Case 3:** $s_1 = "", s_2 = "", result = ""$ → Output: True
- **Test Case 4:** $s_1 = "a"$, $s_2 = "b"$, result = "ba" → Output: True

16.3 Algorithm

1. Check if $\text{len(result)} = \text{len}(s_1) + \text{len}(s_2)$.
2. Use two pointers for s_1 and s_2 , one for result.
3. Match characters; if no match, return False.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$

16.4 Python Solution

```
1 def is_valid_shuffle(s1, s2, result):
2     if len(result) != len(s1) + len(s2):
3         return False
4
5     i = j = k = 0
6     while k < len(result):
7         if i < len(s1) and s1[i] == result[k]:
8             i += 1
9         elif j < len(s2) and s2[j] == result[k]:
10            j += 1
11        else:
12            return False
13        k += 1
14    return i == len(s1) and j == len(s2)
15
16 # Example usage
17 print(is_valid_shuffle("abc", "def", "adbcef")) # Output: True
```

17 Remove Duplicate Letters

17.1 Problem Statement

Given a string, remove duplicate letters so each letter appears once, in smallest lexicographical order.

17.2 Dry Run on Test Cases

- **Test Case 1:** Input = "bcabc" → Output: "abc"
- **Test Case 2:** Input = "cbacdcbc" → Output: "acdb"
- **Test Case 3:** Input = "a" → Output: "a"
- **Test Case 4:** Input = "" → Output: ""

17.3 Algorithm

1. Track last occurrence of each character.
2. Use stack to build result, ensuring lexicographical order.
3. Pop from stack if current char is smaller and later occurrences exist.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$

17.4 Python Solution

```
1 def remove_duplicate_letters(s):
2     last_occurrence = {}
```

```

3     for i, char in enumerate(s):
4         last_occurrence[char] = i
5
6     stack = []
7     seen = set()
8
9     for i, char in enumerate(s):
10        if char not in seen:
11            while stack and char < stack[-1] and i <
12                last_occurrence[stack[-1]]:
13                    seen.remove(stack.pop())
14            stack.append(char)
15            seen.add(char)
16    return ''.join(stack)
17
18 # Example usage
19 print(remove_duplicate_letters("cbacdcbc")) # Output: "acdb"

```

18 Find All Palindromic Substrings

18.1 Problem Statement

Given a string, find the count of all palindromic substrings.

18.2 Dry Run on Test Cases

- **Test Case 1:** Input = "aaa" → Output: 6 ("a", "a", "a", "aa", "aa", "aaa")
- **Test Case 2:** Input = "abc" → Output: 3 ("a", "b", "c")
- **Test Case 3:** Input = "" → Output: 0
- **Test Case 4:** Input = "aba" → Output: 4 ("a", "b", "a", "aba")

18.3 Algorithm

1. For each index, expand around center for odd and even palindromes.
2. Count all valid palindromes.

Time Complexity: $O(n^2)$ **Space Complexity:** $O(1)$

18.4 Python Solution

```

1 def count_palindromic_substrings(s):
2     def expand_around_center(left, right):
3         count = 0
4         while left >= 0 and right < len(s) and s[left] == s[right]:
5             count += 1

```

```

6         left -= 1
7         right += 1
8     return count
9
10    total = 0
11    for i in range(len(s)):
12        total += expand_around_center(i, i) # Odd length
13        total += expand_around_center(i, i + 1) # Even length
14    return total
15
16 # Example usage
17 print(count_palindromic_substrings("aaa")) # Output: 6

```

19 Rabin-Karp String Matching

19.1 Problem Statement

Given a text and pattern, find all occurrences of pattern in text using Rabin-Karp.

19.2 Dry Run on Test Cases

- **Test Case 1:** text = "AABAACAAADA", pattern = "AA" → Output: [0, 3, 6]
- **Test Case 2:** text = "abcd", pattern = "xyz" → Output: []
- **Test Case 3:** text = "", pattern = "a" → Output: []
- **Test Case 4:** text = "aaa", pattern = "aaa" → Output: [0]

19.3 Algorithm

1. Compute hash of pattern and first window of text.
2. Slide window, update hash, compare if equal.
3. Verify matches to avoid hash collisions.

Time Complexity: $O(n + m)$ average **Space Complexity:** $O(1)$

19.4 Python Solution

```

1 def rabin_karp(text, pattern):
2     if not pattern or not text:
3         return []
4
5     d = 256 # Number of characters
6     q = 101 # Prime number
7     m, n = len(pattern), len(text)
8     result = []
9

```

```

10     h = pow(d, m-1) % q
11     p = t = 0
12
13     for i in range(m):
14         p = (d * p + ord(pattern[i])) % q
15         t = (d * t + ord(text[i])) % q
16
17     for i in range(n - m + 1):
18         if p == t:
19             if text[i:i+m] == pattern:
20                 result.append(i)
21         if i < n - m:
22             t = (d * (t - ord(text[i]) * h) + ord(text[i + m])) %
23                 q
24             if t < 0:
25                 t += q
26
27     return result
28
29 # Example usage
30 print(rabin_karp("AABAACAAADA", "AA")) # Output: [0, 3, 6]

```

20 KMP Algorithm for Pattern Searching

20.1 Problem Statement

Given a text and pattern, find all occurrences of pattern in text using KMP algorithm.

20.2 Dry Run on Test Cases

- **Test Case 1:** text = "AABAACAAADA", pattern = "AA" → Output: [0, 3, 6]
- **Test Case 2:** text = "abcd", pattern = "xyz" → Output: []
- **Test Case 3:** text = "", pattern = "a" → Output: []
- **Test Case 4:** text = "aaa", pattern = "aaa" → Output: [0]

20.3 Algorithm

1. Compute LPS (longest prefix suffix) array for pattern.
2. Use LPS to skip redundant comparisons while matching.
3. Collect all match indices.

Time Complexity: $O(n + m)$ **Space Complexity:** $O(m)$

20.4 Python Solution

```

1 def kmp_search(text, pattern):
2     def compute_lps(pattern):
3         m = len(pattern)
4         lps = [0] * m
5         length = 0
6         i = 1
7         while i < m:
8             if pattern[i] == pattern[length]:
9                 length += 1
10                lps[i] = length
11                i += 1
12            else:
13                if length != 0:
14                    length = lps[length - 1]
15                else:
16                    lps[i] = 0
17                    i += 1
18        return lps
19
20    result = []
21    if not pattern or not text:
22        return result
23
24    m, n = len(pattern), len(text)
25    lps = compute_lps(pattern)
26    i = j = 0
27
28    while i < n:
29        if pattern[j] == text[i]:
30            i += 1
31            j += 1
32        if j == m:
33            result.append(i - j)
34            j = lps[j - 1]
35        elif i < n and pattern[j] != text[i]:
36            if j != 0:
37                j = lps[j - 1]
38            else:
39                i += 1
40    return result
41
42 # Example usage
43 print(kmp_search("AABAACAAADA", "AA")) # Output: [0, 3, 6]

```

21 Reverse a Linked List

21.1 Problem Statement

Given a singly linked list, reverse it and return the new head.

21.2 Dry Run on Test Cases

- **Test Case 1:** Input = 1->2->3->4->5 → Output: 5->4->3->2->1
- **Test Case 2:** Input = 1 → Output: 1
- **Test Case 3:** Input = None → Output: None
- **Test Case 4:** Input = 1->2 → Output: 2->1

21.3 Algorithm

1. Initialize prev = None, curr = head.
2. While curr, save next, set curr.next = prev, move prev and curr.
3. Return prev as new head.

Time Complexity: $O(n)$ Space Complexity: $O(1)$

21.4 Python Solution

```
1 class ListNode:
2     def __init__(self, val=0, next=None):
3         self.val = val
4         self.next = next
5
6     def reverse_list(head):
7         prev = None
8         curr = head
9
10        while curr:
11            next_node = curr.next
12            curr.next = prev
13            prev = curr
14            curr = next_node
15        return prev
16
17 # Example usage (simplified)
18 # head = ListNode(1, ListNode(2, ListNode(3)))
19 # reversed_head = reverse_list(head)
```

22 Detect Cycle in a Linked List

22.1 Problem Statement

Given a linked list, determine if it has a cycle.

22.2 Dry Run on Test Cases

- **Test Case 1:** 1->2->3->4->2(cycle) → Output: True

- **Test Case 2:** $1 \rightarrow 2 \rightarrow 3 \rightarrow$ Output: False
- **Test Case 3:** None \rightarrow Output: False
- **Test Case 4:** $1 \rightarrow$ Output: False

22.3 Algorithm

1. Use two pointers: slow (1 step), fast (2 steps).
2. If they meet, cycle exists.
3. If fast reaches end, no cycle.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$

22.4 Python Solution

```

1 def has_cycle(head):
2     slow = fast = head
3     while fast and fast.next:
4         slow = slow.next
5         fast = fast.next.next
6         if slow == fast:
7             return True
8     return False
9
10 # Example usage
11 # head = ListNode(1, ListNode(2, ListNode(3)))
12 # head.next.next.next = head.next # Creates cycle
13 # print(has_cycle(head)) # Output: True

```

23 Merge Two Sorted Linked Lists

23.1 Problem Statement

Given two sorted linked lists, merge them into one sorted list.

23.2 Dry Run on Test Cases

- **Test Case 1:** $l1 = 1 \rightarrow 2 \rightarrow 4$, $l2 = 1 \rightarrow 3 \rightarrow 4 \rightarrow$ Output: $1 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 4 \rightarrow$
- **Test Case 2:** $l1 = \text{None}$, $l2 = \text{None} \rightarrow$ Output: None
- **Test Case 3:** $l1 = 1$, $l2 = \text{None} \rightarrow$ Output: 1
- **Test Case 4:** $l1 = 2$, $l2 = 1 \rightarrow$ Output: 1 \rightarrow 2

23.3 Algorithm

1. Use dummy node to simplify merging.
2. Compare heads of l1 and l2, append smaller to result.
3. Move to next node of chosen list.
4. Append remaining nodes.

Time Complexity: $O(n + m)$ **Space Complexity:** $O(1)$

23.4 Python Solution

```
1 def merge_two_lists(l1, l2):
2     dummy = ListNode(0)
3     curr = dummy
4
5     while l1 and l2:
6         if l1.val <= l2.val:
7             curr.next = l1
8             l1 = l1.next
9         else:
10            curr.next = l2
11            l2 = l2.next
12        curr = curr.next
13
14    curr.next = l1 if l1 else l2
15    return dummy.next
16
17 # Example usage
18 # l1 = ListNode(1, ListNode(2, ListNode(4)))
19 # l2 = ListNode(1, ListNode(3, ListNode(4)))
20 # merged = merge_two_lists(l1, l2)
```

24 Remove Nth Node from End

24.1 Problem Statement

Given a linked list and integer n, remove the nth node from the end.

24.2 Dry Run on Test Cases

- **Test Case 1:** head = 1->2->3->4->5, n = 2 → Output: 1->2->3->5
- **Test Case 2:** head = 1, n = 1 → Output: None
- **Test Case 3:** head = 1->2, n = 2 → Output: 2
- **Test Case 4:** head = None, n = 1 → Output: None

24.3 Algorithm

1. Use two pointers: fast moves n steps ahead.
2. Move slow and fast until fast reaches end.
3. Slow points to node before nth from end; remove it.

Time Complexity: $O(n)$ Space Complexity: $O(1)$

24.4 Python Solution

```
1 def remove_nth_from_end(head, n):
2     dummy = ListNode(0, head)
3     slow = fast = dummy
4
5     for _ in range(n):
6         fast = fast.next
7
8     while fast.next:
9         slow = slow.next
10        fast = fast.next
11
12    slow.next = slow.next.next
13    return dummy.next
14
15 # Example usage
16 # head = ListNode(1, ListNode(2, ListNode(3, ListNode(4, ListNode(5)))))
17 # new_head = remove_nth_from_end(head, 2)
```

25 Find Middle of Linked List

25.1 Problem Statement

Given a linked list, return the middle node (if even, second middle node).

25.2 Dry Run on Test Cases

- **Test Case 1:** head = 1->2->3->4->5 → Output: 3
- **Test Case 2:** head = 1->2->3->4 → Output: 3
- **Test Case 3:** head = 1 → Output: 1
- **Test Case 4:** head = None → Output: None

25.3 Algorithm

1. Use two pointers: slow (1 step), fast (2 steps).

2. When fast reaches end, slow is at middle.

3. Return slow.

Time Complexity: $O(n)$ **Space Complexity:** $O(1)$

25.4 Python Solution

```
1 def middle_node(head):
2     slow = fast = head
3     while fast and fast.next:
4         slow = slow.next
5         fast = fast.next.next
6     return slow
7
8 # Example usage
9 # head = ListNode(1, ListNode(2, ListNode(3, ListNode(4, ListNode
10 # (5)))))  
# middle = middle_node(head)
```