

1.1

Terry & Susan have a joint bank account. Terry goes to the bank 20% of the days, Susan goes there 30% of the days. Together they are at the bank 8% of the days.

(a) Susan was at the bank last Monday. What's the probability that Terry was there too?

→ soln: Probability of Terry going to the bank when Susan is also there at the bank:-

$$P(\text{Terry} | \text{Susan}) = \frac{P(\text{Terry} \cap \text{Susan})}{P(\text{Susan})}$$

$$= \frac{8}{30} = \boxed{26.66\%} \leftarrow \text{Ans}$$

(b) last Friday, Susan wasn't at the bank. What's the probability that Terry was there?

→ soln: Probability of Terry going to the bank when ~~Susan~~ is not there

$$P(\text{Terry} | (\text{Susan})') = \frac{P(\text{Terry} \cap (\text{Susan})')}{P((\text{Susan})')}$$

$$P((\text{Susan})') = 1 - P(\text{Susan})$$

$$1 - 0.3 = 0.7 = 70\%$$

$$\therefore \frac{P(\text{T} \cap \text{S}')}{P(\text{S}')} = \frac{12}{70}$$

$$= \boxed{17.14\%} \leftarrow \text{Ans}$$

(c) last Wednesday at least one of them was at the bank. What is the probability that both of them were there?

→ Solⁿ: Probability that both Jerry & Susan either one of them was present at the bank

$$P(\text{Jerry} | \text{Susan}) = \frac{P(\text{Jerry} \cap \text{Susan})}{P(\text{Jerry} \cup \text{Susan})}$$

$$P(\text{Jerry} \cap \text{Susan}) = 8\%$$

$$\begin{aligned} P(\text{Jerry} \cup \text{Susan}) &= P(\text{Jerry}) + P(\text{Susan}) - P(\text{Jerry} \cap \text{Susan}) \\ &= 20 + 30 - 8 \\ &= 42 \end{aligned}$$

$$\therefore P(\text{Jerry} | \text{Susan}) = \frac{8}{42} = \boxed{19.04\%} \text{ Ans}$$

1.2 Homework

Harold and Sharon are studying for a test.

Harold's chances of getting a 'B' are 80%. Sharon's chances of getting a 'B' are 90%.

The probability of at least one of them getting a 'B' is 91%.

(a) What is the probability that only Harold gets a 'B'?

→ Solution: Probability that only Harold gets a 'B'

$$\begin{aligned} P(\text{Only Harold}) &= P(\text{Harold}) - P(\text{Harold} \cap \text{Sharon}) \\ &= 80 - 79 \end{aligned}$$

$$\boxed{1\%} \text{ Ans}$$

(b) what is the probability that only Sharon gets a 'B'?

→ soln: $P(\text{Sharon getting B}) = P(\text{Sharon}) - P(\text{Harold} \cap \text{Sharon})$

$$= \frac{90 - 79}{100} = \boxed{11\%} \text{ Ans}$$

(c) what is the probability that both won't get an 'B'?

→ soln: $P((\text{Harold} \cap \text{Sharon})') = \frac{100 - P(\text{Harold} \cap \text{Sharon})}{100 - 79}$

$$= \boxed{21\%} \text{ Ans.}$$

Homework

Jerry & Susan have a joint bank account. Jerry goes to the bank 20% of the days. Susan goes there 30% of the days. Together they are at the bank 8% of the days.

Are the events "Jerry is at the bank" and "Susan is at the bank" independent?

→ soln:-

Both Jerry & Susan are at the bank 8% of the days together.

If the events were going to be independent the individual parameters of going together to the bank if calculated then product would be similar. But, $20 \times 30 = 60\%$

∴ Hence the events are not independent

1.4 Homework

You roll 2 dice.

(a) Are the events "the sum is 6" and "the second die shows 5" independent?

→ Soln: If these events are independent:

$$P(\text{2nd die} = 5 \text{ and sum} = 6) = P(\text{sum} = 6) * P(\text{second die} = 5)$$

$$= \frac{5}{36} \times \frac{6}{36} = \frac{1}{36} \text{ which is not equal.}$$

Ans → ∴ The events are not independent

(b) Are the events "the sum is 7" & "the first die shows 5" independent?

→ Soln: If these events are independent

$$P(\text{first die} = 5 \text{ \& sum} = 7) = P(\text{sum} = 7) \times P(\text{first die} = 5)$$
$$\frac{1}{36} = \frac{6}{36} \times \frac{6}{36}$$

Ans As both events are equal, the events are independent

1.5 Homework

An oil company is considering drilling in either TX, AK and NJ. The company may operate in only one state. There is 60% chance the company will choose TX & 10% chance - NJ. There is 30% chance of finding oil in TX, 20% - in AK & 10% in NJ.

Q1. What is the probability of finding oil?

→ Solⁿ :-

Find the probability of finding oil in a state & probability of choosing that state.

For TX

$$P(\text{oil} | \text{TX}) * P(\text{TX}) = 30\% * 60\% = 18\%$$

For AK

$$P(\text{oil} | \text{AK}) * P(\text{AK}) = 20\% * 30\% = \cancel{60\%} 6\%$$

For NJ

$$P(\text{oil} | \text{NJ}) * P(\text{NJ}) = 10\% * 10\% = 1\%$$

$$\therefore \text{Probability of finding oil} = 18\% + 6\% + 1\% = 25\%$$

$$\text{Ans} \rightarrow \boxed{\text{Probability of finding oil} = 25\%}$$

Q2. The company decided to drill & found oil. What is the probability that they drilled in TX?

→ Solⁿ : Probability of drilling in TX & finding oil

$$P(\text{TX} | \text{oil}) = \frac{P(\text{TX} \cap \text{oil})}{P(\text{oil})} = \frac{18}{25} \rightarrow \text{found in TX solⁿ}$$
$$= \boxed{72\%} \text{ Ans}$$

1.6 Homework

Answering Questions based on Titanic survivors provided data

Q1. What is the probability that a passenger did not survive?

$$\rightarrow \text{soln: } P(\text{Not survived}) = \frac{1490 - 673}{2201 - 885} = 62.08\% \quad \text{Ans.}$$

$$\frac{\text{Not survived} - \text{Crew}}{\text{(Total) Not survived}}$$

$$\text{Total} - \text{Total (Crew)}$$

Q2. What is the probability that the passenger was staying in the first class?

$$\begin{aligned} \rightarrow \text{soln: } P(\text{First class}) &= \frac{P(\text{Total 1st})}{P(\text{Total}) - P(\text{Crew})} \\ &= \frac{325}{2201 - 885} = \frac{325}{1316} \\ &= 24.69\% \quad \text{Ans} \end{aligned}$$

Q3. Given that the passenger survived, what is the probability that the passenger was staying in the 1st class?

\rightarrow soln:

$$\begin{aligned} P(\text{passenger survived staying in First class}) \\ = P(S \cap F) &= \frac{203}{499} = 40.68\% \quad \text{Ans} \end{aligned}$$

Q4 Are survival & staying in the First class independent?

→ solⁿ: If probability of staying in First class and surviving are equally by being mutually exclusive ^{then} they are independent

$$\begin{aligned} P(\text{Surviving}) &= 100 - P(\text{Not surviving}) \\ &= 100 - 62.08 \\ &= \boxed{37.92\%} \end{aligned}$$

$$\therefore 24.69 * 37.92 = 9.36\%$$

Ans → survival and staying in First class are not independent

Q5 Given that a passenger survived, what is the probability that the passenger was staying in the First class & the passenger was a child?

$$\begin{aligned} \Rightarrow \text{sol}^n &:- P(\text{survived, staying in first class and is a child}) \\ &= \frac{6}{499} = \boxed{1.2\%} \end{aligned}$$

Q6 Given that the passenger survived, what is the probability that the passenger was an adult?

$$\begin{aligned} P(\text{Passenger ~~adult~~ and Adult}) &= \frac{442}{499} = \boxed{88.57\%} \\ &\quad (654 - 212) \end{aligned}$$

Q7 Given that a passenger survived, are age & staying in First class independent?

$$\begin{aligned} P(\text{age passenger survived}) &= P(A|S) * P(C|S) \\ &= \frac{442}{499} + \frac{57}{499} = 1 \end{aligned}$$

$$P(\text{Passenger survived \& staying in 1st class}) \\ = 40 \cdot 68\%$$

$$\therefore P(\text{Age \& staying in 1st class}) = 40 \cdot 68\%$$

→ since probability of age & first class are equal
ANS then events are independent

