

Optimizing Matrix chain multiplication

2019101098

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Optimizing the code for Matrix chain multiplication

Matrix chain multiplication

For 4 matrices with result size 1000 1000

Time taken without optimization:

34.32 seconds

Optimizations made in Assignment 1:

1. Changing the loop order to improve the chances of getting cache hit. Previous order was i,j,k. I changed it to i,k,j.
2. Pre increment over post increment Pre-increment is faster than post-increment because post increment keeps a copy of previous (existing) value and adds 1 in the existing value while pre-increment is simply adds 1 without keeping the existing value.
3. Storing in 1D array The best optimisation in terms of time, as now only 1D arrays are used instead of 2D referencing which is most time consuming.

Time taken with the optimizations made in Assignment 1:

9.20 seconds

Optimizations made in this Assignment :

4. Compiler Optimization.

Running the code with -O2 , decreases the time taken for running code.

Time taken: 2.79 seconds.

5. Parallelizing the ith loop.

Parallelizing the loop allows all iterations of the loop to execute in parallel.

Time taken: 1.72 seconds.

6. Tiled Matrix Multiplication.

We Restructure the computation to reuse data in the cache as much as possible.

In tiled matrix multiplication, cache hits are more and cache misses are low. We divide the matrix into blocks of size 32 and reuse the data.

Time taken: 1.22 seconds

Results of perf, cachegrind and gprof for the final optimized code.

perf

```
pravalika@pravalika: ~/Desktop/2019101098/Q1 x pravalika@pravalika: ~/Desktop/sem4/spp/as2 x
pravalika@pravalika:~/Desktop/sem4/spp/as2$ sudo perf stat ./a.out < ../Q1/90.txt > q1.txt

Performance counter stats for './a.out':

      4,694.85 msec task-clock                #    4.626 CPUs utilized
         648      context-switches           #    0.138 K/sec
          23      cpu-migrations             #    0.005 K/sec
        9,912      page-faults               #    0.002 M/sec
  15,89,33,58,589 cycles                     #    3.385 GHz
  22,45,29,73,066 instructions               #    1.41 insn per cycle
   3,95,94,17,541 branches                   # 843.354 M/sec
    88,75,546    branch-misses               #    0.22% of all branches

1.014835218 seconds time elapsed

4.656047000 seconds user
0.040000000 seconds sys
```

Cachegrind

```
pravalika@pravalika: ~/Desktop/sem4/spp/as2
pravalika@pravalika: ~/Desktop/2019101098/Q1 x pravalika@pravalika: ~/Desktop/sem4/spp/as2 x
pravalika@pravalika:~/Desktop/sem4/spp/as2$ valgrind --tool=cachegrind ./a.out < ../Q1/20.txt > 20.txt
==21718== Cachegrind, a cache and branch-prediction profiler
==21718== Copyright (C) 2002-2017, and GNU GPL'd, by Nicholas Nethercote et al.
==21718== Using Valgrind-3.14.0 and LibVEX; rerun with -h for copyright info
==21718== Command: ./a.out
==21718==
--21718-- warning: L3 cache found, using its data for the LL simulation.
==21718==
==21718== Process terminating with default action of signal 27 (SIGPROF)
==21718==   at 0x49935BF: __open_nocancel (open64_nocancel.c:45)
==21718==   by 0x49A0B2F: write_gmon (gmon.c:370)
==21718==   by 0x49A13EA: _mcleanup (gmon.c:444)
==21718==   by 0x48C8956: __cxa_finalize (cxa_finalize.c:83)
==21718==   by 0x1094E2: ??? (in /home/pravalika/Desktop/sem4/spp/as2/a.out)
==21718==   by 0x4010CE5: _dl_fini (dl-fini.c:138)
==21718==   by 0x48C82AB: __run_exit_handlers (exit.c:108)
==21718==   by 0x48C83D9: exit (exit.c:139)
==21718==   by 0x48A7B71: (below main) (libc-start.c:342)
==21718==
==21718== I   refs:      1,053,852,303
==21718== I1 misses:      1,676
==21718== LLi misses:      1,571
==21718== I1 miss rate:      0.00%
==21718== LLi miss rate:      0.00%
==21718==
==21718== D   refs:      480,138,392 (420,569,005 rd + 59,569,387 wr)
==21718== D1 misses:      1,671,500 ( 1,554,680 rd + 116,820 wr)
==21718== LLD misses:      72,883 ( 48,711 rd + 24,172 wr)
==21718== D1 miss rate:      0.3% ( 0.4% + 0.2% )
==21718== LLD miss rate:      0.0% ( 0.0% + 0.0% )
==21718==
==21718== LL refs:      1,673,176 ( 1,556,356 rd + 116,820 wr)
==21718== LL misses:      74,454 ( 50,282 rd + 24,172 wr)
==21718== LL miss rate:      0.0% ( 0.0% + 0.0% )
Profiling timer expired
pravalika@pravalika:~/Desktop/sem4/spp/as2$
```

gprof:

```
pravalika@pravalika: ~/Desktop/sem4/spp/as2
pravalika@pravalika: ~/Desktop/2019101098/Q1 x pravalika@pravalika: ~/Desktop/sem4/spp/as2 x
pravalika@pravalika:~/Desktop/sem4/spp/as2$ gprof ./a.out gmon.out >anal.txt
pravalika@pravalika:~/Desktop/sem4/spp/as2$ cat anal.txt
Flat profile:

Each sample counts as 0.01 seconds.
%   cumulative   self           self       total
time  seconds    seconds   calls   Ts/call   Ts/call   name
100.17      1.22      1.22                1.22      1.22      frame_dummy

%
time      the percentage of the total running time of the
          program used by this function.

cumulative a running sum of the number of seconds accounted
seconds    for by this function and those listed above it.

self       the number of seconds accounted for by this
seconds    function alone. This is the major sort for this
           listing.

calls      the number of times this function was invoked, if
           this function is profiled, else blank.

self       the average number of milliseconds spent in this
ms/call    function per call, if this function is profiled,
           else blank.

total      the average number of milliseconds spent in this
ms/call    function and its descendents per call, if this
           function is profiled, else blank.

name       the name of the function. This is the minor sort
           for this listing. The index shows the location of
           the function in the gprof listing. If the index is
           in parenthesis it shows where it would appear in
           the gprof listing if it were to be printed.

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pravalika@pravalika:~/Desktop/sem4/spp/as2$
```