

①

a. Insertion sort

p1	p2	p3	p4	p5	p6	p6	p7
64	32	32	32	32	32	32	32
*32	64	64	64	64	64	46	46
79	*79	79	79	67	67	64	64
83	83	*83	83	79	79	67	67
67	67	67	*67	83		79	79
46	46	46	46	*46		83	83
96	96	96	96	96		*96	96
55	55	55	55	55		55	*55
68	68	68	68	68		68	68
12	12	12	12	12		12	12
p8	p9						
32	32		12				
46	46		32				
55	55		46				
64	64		55				
67	67		64				
79	68		67				
83	79		68				
96	83		79				
*68	96		83				
12	*12		96				

No. of elements = 10, passes = $n-1 = 10-1 = 9$

b. Shell sort 5, 3, 1

5 sort

64	46	46	46	46	46	46	46	46
32	32	32	32	32	32	32	32	32
79	79	79	55	55	55	55	55	55
83	83	83	83	68	68	68	68	68
67	67	67	67	67	12	12	12	12
46	46	46	46	46	46	46	46	46
96	96	96	96	96	96	96	96	96
55	55	55	79	79	79	79	79	79
68	68	68	68	83	83	83	83	83
12	12	12	12	12	67	67	67	67

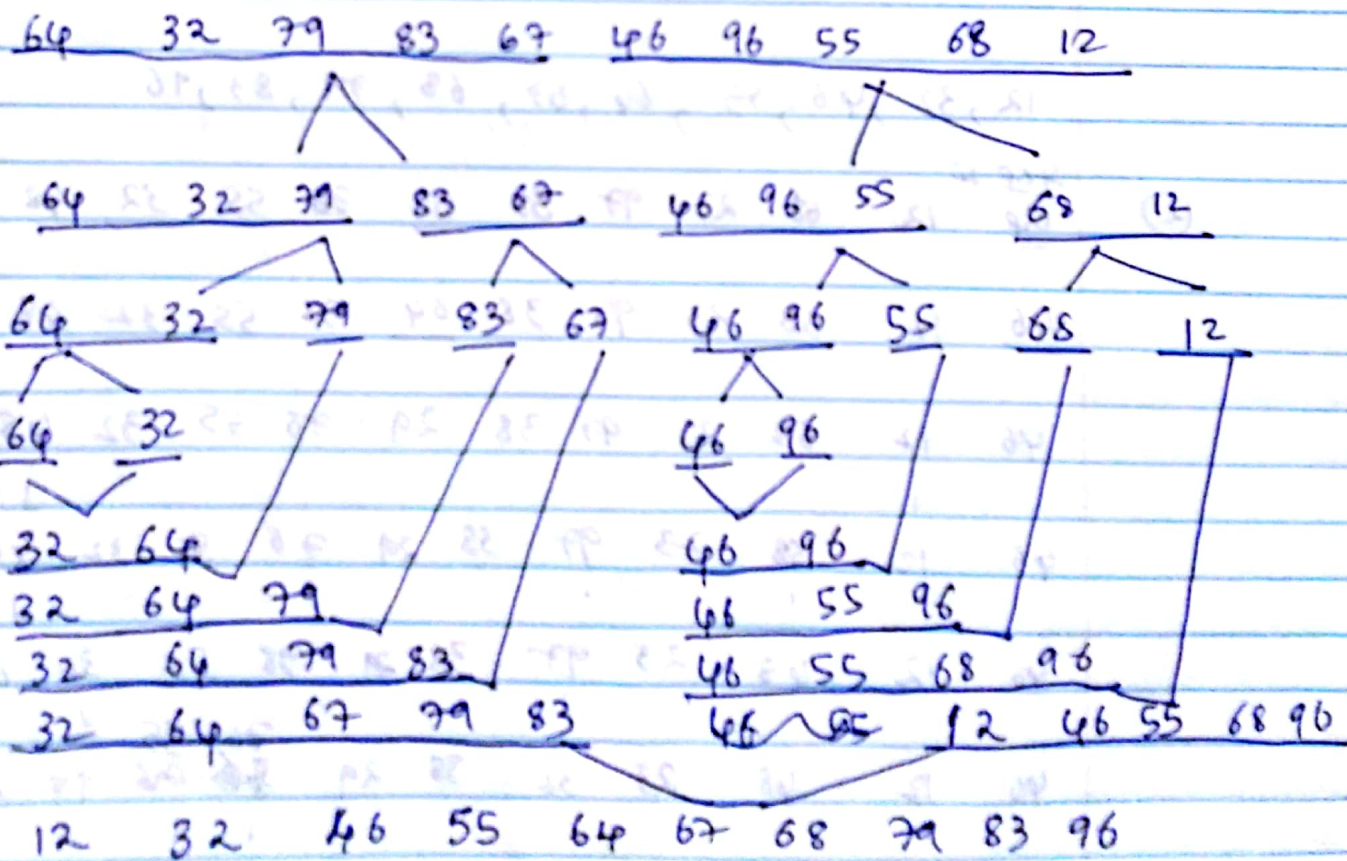
3 sort

46	46	46	46	46	46	46	46	46
32	32	12	12	12	12	12	12	12
55	55	55	55	55	55	55	55	55
68	68	68	68	68	68	68	68	68
12	12	32	32	32	32	32	32	32
64	64	64	64	64	64	64	64	64
96	96	96	96	96	96	96	96	96
79	79	79	79	79	79	79	79	79
83	83	83	83	83	83	83	83	83
67	67	67	67	67	67	67	67	67

1-sort

46	{ 12	{ 12	{ 12	{ 12	{ 12	{ 12	{ 12	12
12	{ 46	{ 46	{ 46	{ 32	{ 32	{ 32	{ 32	32
55	{ 55	{ 55	{ 55	{ 46	{ 46	{ 46	{ 46	46
67	{ 67	{ 67	{ 67	{ 55	{ 55	{ 55	{ 55	55
32	{ 32	{ 32	{ 32	{ 67	{ 64	{ 64	{ 64	64
64	{ 64	{ 64	{ 64	{ 64	{ 67	{ 67	{ 67	67
68	{ 68	{ 68	{ 68	{ 68	{ 68	{ 68	{ 68	68
79	{ 79	{ 79	{ 79	{ 79	{ 79	{ 79	{ 79	79
83	{ 83	{ 83	{ 83	{ 83	{ 83	{ 83	{ 83	83
96	{ 96	{ 96	{ 96	{ 96	{ 96	{ 96	{ 96	96

c)



d)

Radix Sort

1st digit Sort

2nd digit Sort

64	0		0
32	1		12
79	2	12, 32	2
83	3	12, 32, 83	3
67	4	64	4
46	5	55	5
96	6	46, 96	6
55	7	67	7
68	8	68	8
12	9	79	9

12, 32, 46, 55, 64, 67, 68, 79, 83, 96

Step 1:

②

64 12 68 23 97 38 81 76 55 32 48 29 46

46 12 68 23 97 38 64 76 55 32 48 29 81

46 12 68 23 97 38 29 76 55 32 48 64 81

46 12 68 23 97 38 29 76 55 32 48 64 81

46 12 48 23 97 38 29 76 55 32 68 46 81

46 12 48 23 32 38 29 76 55 97 68 64 81

46 12 48 23 32 38 29 55 76 97 68 64 81

46 12 48 23 32 38 29 55 64 97 68 76 81

Step 2:

97 68 76 81
68 81 76 97
 68 76 81 87
 j i
 list size $= 3$

Step 3:

23 12j 32j 2a 38

23 12 29 32 38 \Rightarrow list size $c=3 \Rightarrow$ 12 23 29 32 38

12 23 29 32 38 46 64 68 76 81 97

3	8	7	4	5	6	11	9	2
	7				1			2
	4				2	11		4
	2				3	11		4
	5				4	11		5
	5				5	111		5
	2				6			5
	4				7	11		7
	5				8	11		7
	7							8
	8							8

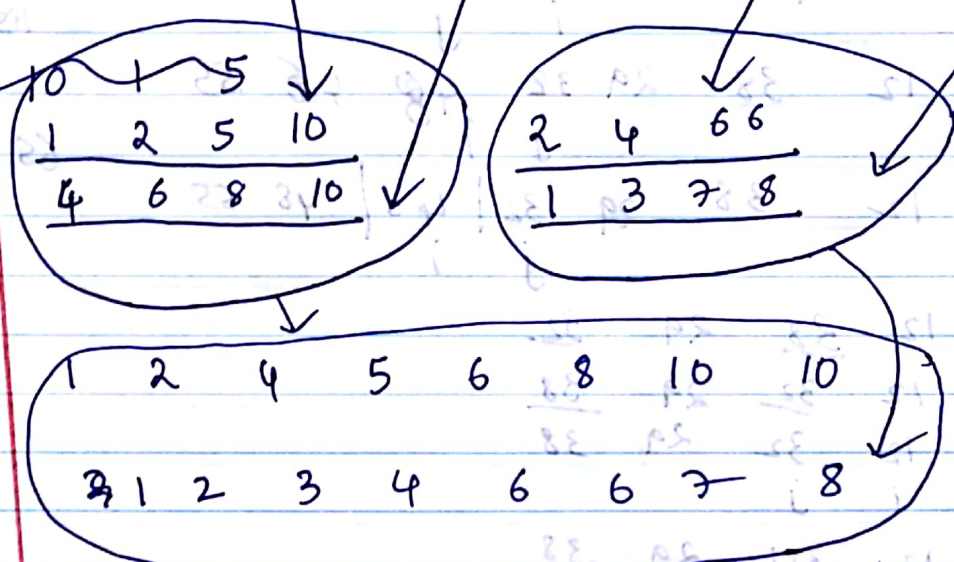
④ T1: 10 1 5 2 6 8 4 10 6 6 2 4 1 8 7 3

T2

T3

T3

T4



T1

T2

T3

1 1 2 2 3 4 4 5 6 6 7 8 8 10 10

⑤

M=3

10 1 5 2 6 8 4 10 6 6 2 4 1 8 7

10

1

5

2

6

8

4

10

6

6

10

10

10

10

10

10

10

10

6*

6*

1

1 5

2 5

6 5

6 8

4*

4*

6*

4*

5

5

8

8

10

10

10

6*

Run 1

1

2

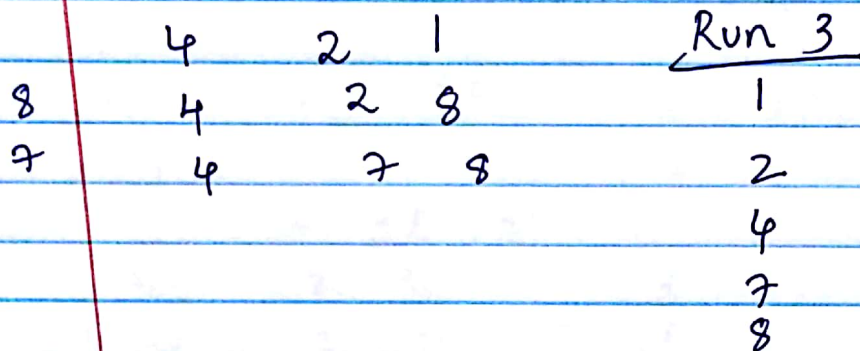
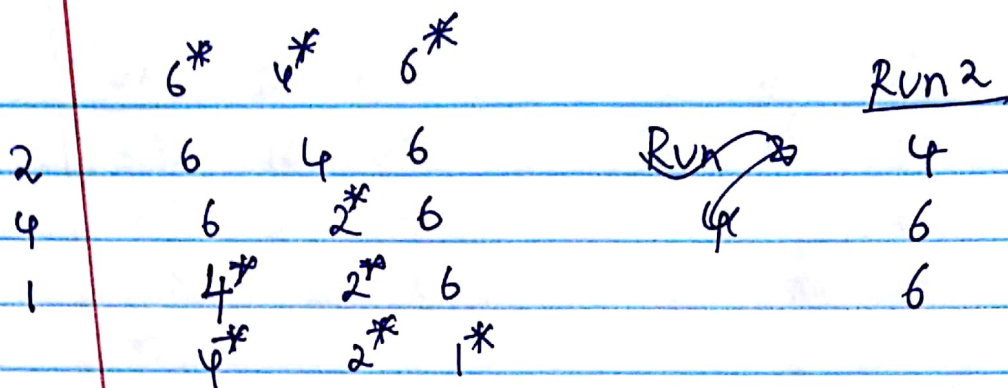
5

6

8

10

10



⑥ ~~4 items can be compared in 4! ways~~
~~in 24 ways~~

⑥ 4 items have $4!$ possible arrangements.

This would lead to a tree with $4! = 24$ leaves & $\log(4!)$ depth \Rightarrow hence $\log(4!)$ comparisons.

$$\log(4!) = 4 \cdot 584 \approx 5$$

It would take 5 comparisons at worst to sort them.