

① All Repeating three time except one: →

Date: 27th January 2022

4 3 2 1 0 ← bit index
 19 → 1 0 0 1 1

12 → 0 1 1 0 0

14 → 0 1 1 1 0

19 → 1 0 0 1 1

19 → 1 0 0 1 1

12 → 0 1 1 0 0

15 → 0 1 1 1 1

21 → 1 0 1 0 1

15 → 0 1 1 1 1

14 → 0 1 1 1 0

12 → 0 1 1 0 0

15 → 0 1 1 1 1

14 → 0 1 1 1 0

res = 1 0 1 0 1

Complexity ! → $O(2n)$

NOTE:

if all numbers are

present three time in an array →

↳ then no. of ON bits must
be multiple of 3

if one number is extra present

then possibility of no. of 1's in i^{th} bit

→ $\text{Result's } i^{th} \text{ bit is } 0 = \text{Result's } i^{th} \text{ bit is } 1$

1. All Repeating three time except one

2. Triplet - 1

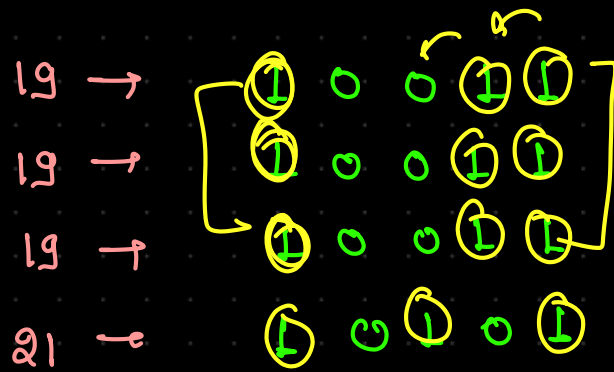
3. Reduce N to 1

4. Decoder and Bits

5. XOR of sum of all pairs

[Not possible]
what if $3n+2$??
is it possible

eg.



19 is thrice time present
& 21 is one time.

res = 1 0 1 0 1

[22 times]



1 1 1 0

max no.
le 100

bit similarity → ON

weight

3n+1

↑

total element
in array

✓ 56 → 0 1 1 1 0 0 0

✓ 71 → 1 0 0 0 1 1 1

✓ 63 → 0 1 1 1 1 1 1

✓ 49 → 0 1 1 0 0 0 1

✓ 63 → 0 1 1 1 1 1 1

✓ 71 → 1 0 0 0 1 1 1

✓ 71 → 1 0 0 0 1 1 1 $3n$

63 → 0 1 1 1 1 1 1 num

56 → 0 1 1 1 0 0 0 $3np1c =$

56 → 0 1 1 1 0 0 0

$3n \neq 1$ count

$$3np1c = 3n \& \text{num}$$

$$3np2c = 3np1 \& \text{num}$$

$$3np2c = 3np2 \& \text{num}$$

$3n$

1 1 1 1 1 1 1

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

$3n+1$

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

$3n+2$

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

0 0 0 0 0 0 0

$3np1$

0 1 1 0 1 1 0

num 1 0 0 0 1 1 1

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

0 0 0 0 1 1 0

$3np2$

1 0 0 0 0 0 1

num 1 0 0 0 1 1 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

1 0 0 0 0 0 1

$$3np2c = 11111001$$

off in $3np1$

$$3np1 = [3np1 \& (\sim 3np2c)]$$

ON in $3np2$

$$3np2 = (3np2 \mid 3np2c)$$

$$10110101 \rightarrow \begin{array}{cccccccc} & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ \hline 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \end{array}$$

$$10110101 \rightarrow 01001010$$

$$10110101 \rightarrow \begin{array}{cccccccc} \cancel{1} & \cancel{1} & \cancel{1} & \cancel{1} & \cancel{1} & \cancel{1} & \cancel{1} & \cancel{1} \\ 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 \end{array}$$

$$11001100 \rightarrow \begin{array}{cccccccc} & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 3n+1 & & & & & & & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \end{array}$$

$$00000000$$

$$\begin{array}{cccccccc} \cancel{0} & \cancel{0} & \cancel{0} & \cancel{0} & \cancel{0} & \cancel{0} & \cancel{0} & \cancel{0} \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 3n+2 & & & & & & & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

$$10110101$$

$$\begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

$$\begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array}$$

$$\underline{\underline{11001100}}$$

Triplet-1 →

$$0 \leq i < j < k < \text{arr.length},$$

i, j and k → index

$$X = \text{arr}[i] \wedge \text{arr}[i+1] \wedge \text{arr}[i+2] \wedge \dots \wedge \text{arr}[j-1]$$

$$Y = \text{arr}[j] \wedge \text{arr}[j+1] \wedge \text{arr}[j+2] \wedge \dots \wedge \text{arr}[k]$$

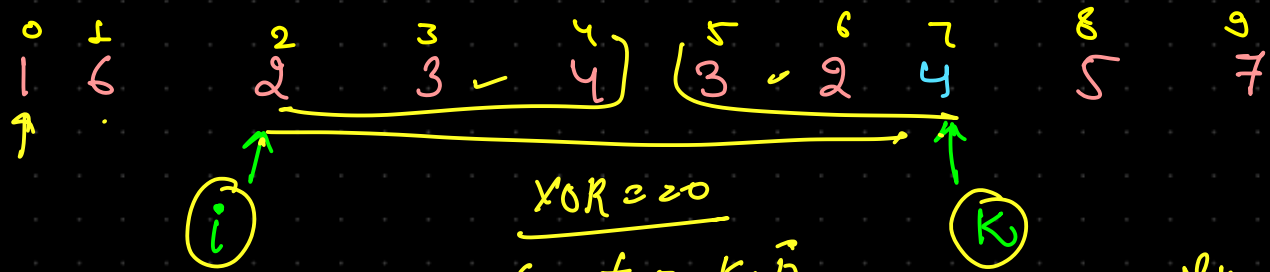
no. of triplet of i, j and k where $X = Y$

$i=4$
 $k=4$

a b c d e f g h
0 1 2 3 4 5 6 7 8
↑
i
↑
k

$j=2$ $b) = c \wedge d \wedge e$
 $j=3$ $b \wedge c = d \wedge e$
 $j=4$ $b \wedge c \wedge d = e$

bruteforce → triplet for, i, j, k
 $O(n^3)$



$i=2, k=7$

j	x	y
3	2	3 4 3 2 4
4	2 \wedge 3	4 \wedge 3 \wedge 2 \wedge 4
5	2 \wedge 3 \wedge 4	3 \wedge 2 \wedge 4
6	2 3 4 3	2 \wedge 4
7	2 3 4 3 2	4

$7-2$ triplets

all possibilities $i \wedge k$
 $\hookrightarrow O(n^2)$
 $x == y ??$

all are
 Equal ??

- 2, 3, 7
- 2, 4, 7
- 2, 5, 7
- !

$O(n^2)$

XOR between two num

between i to k
 \hookrightarrow XOR of all elmt
 including i & k

is 0, then we
 can say that
 there are ' $k-i$ '
 triplet available