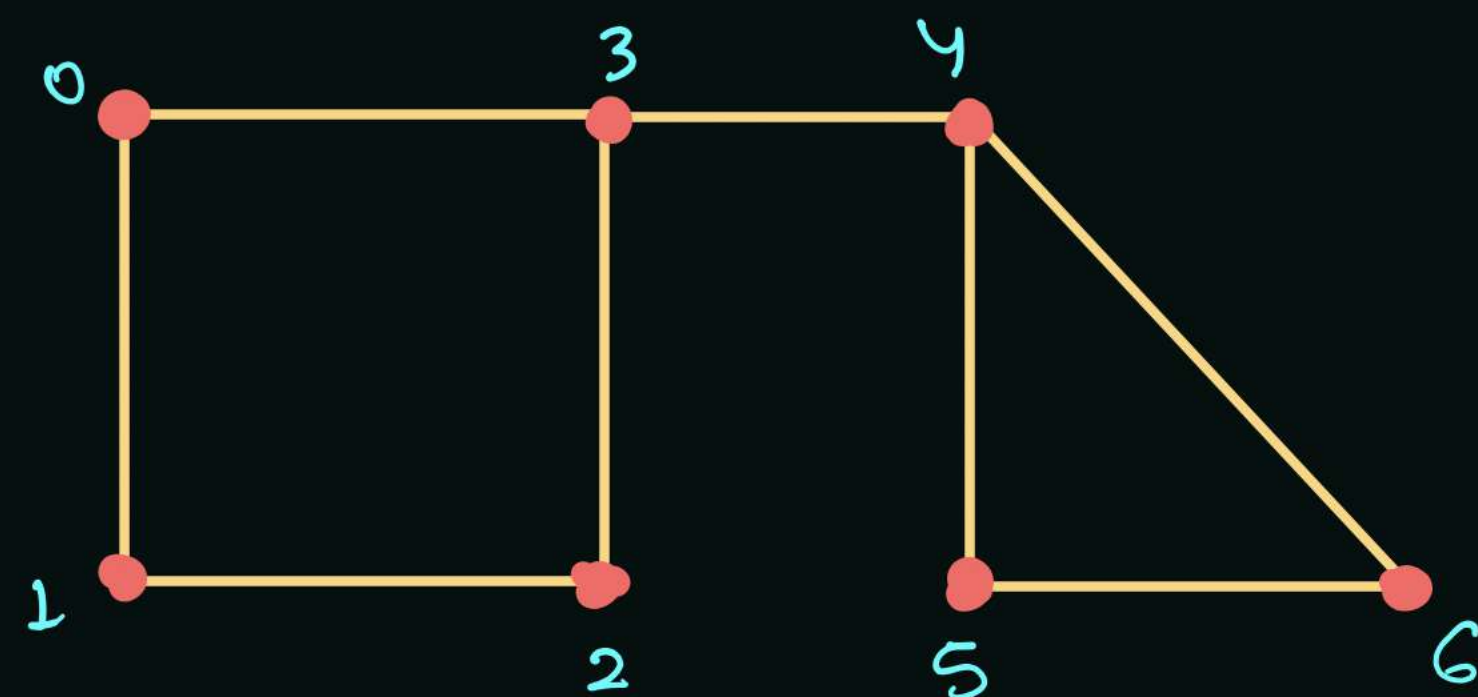


# Eulerian Path & Circuit

Sunday, 31 October 2021

9:59 AM



Travel whole graph & every edge without visit any edge twice.

↳ path

circuit → if starting point is same as ending point then

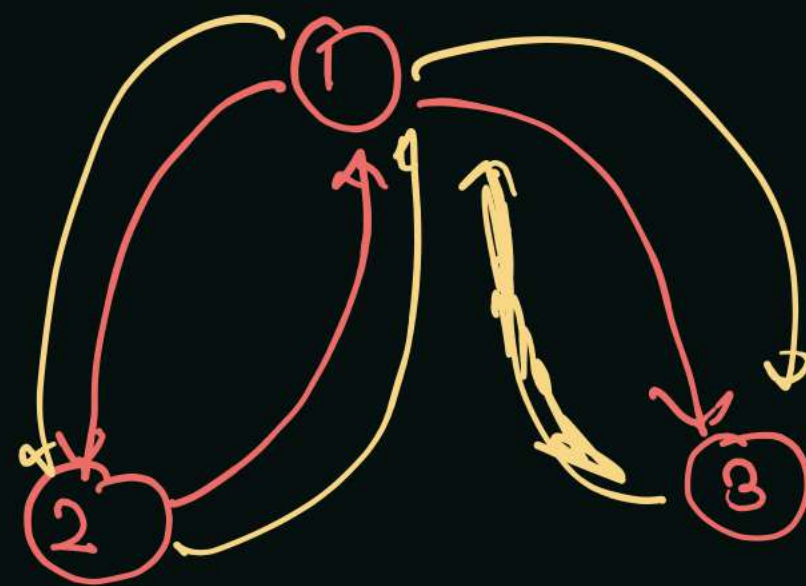
that path is known as circuit.

Eulerian path exist in undirected graph?

Eulerian circuit exist in undirected graph?

Eulerian path exist in directed graph?

Eulerian circuit exist in directed graph?



②-1-3-① → Eulerian path.  
1-2-1-3 → Eulerian path.



# Eulerian path and circuit

graph - connected

degree  
undirected graph

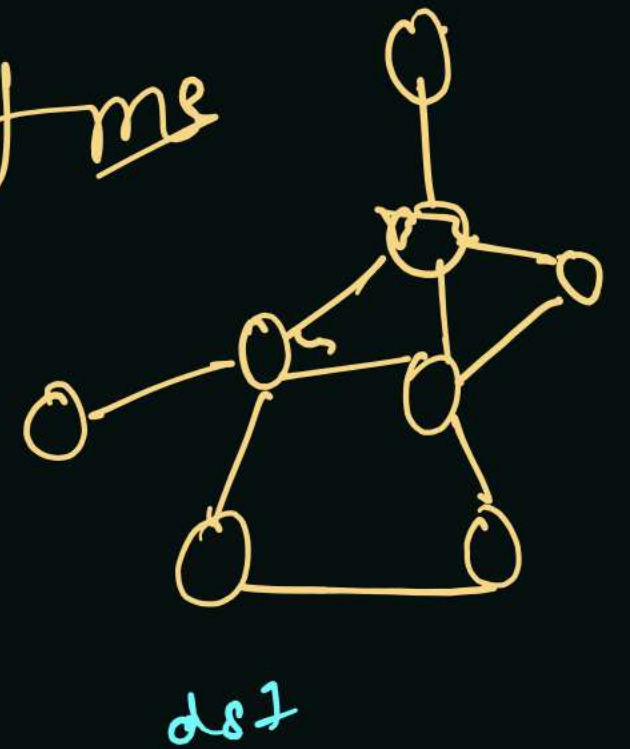
directed graph  
indegree and outdegree

undirected graph

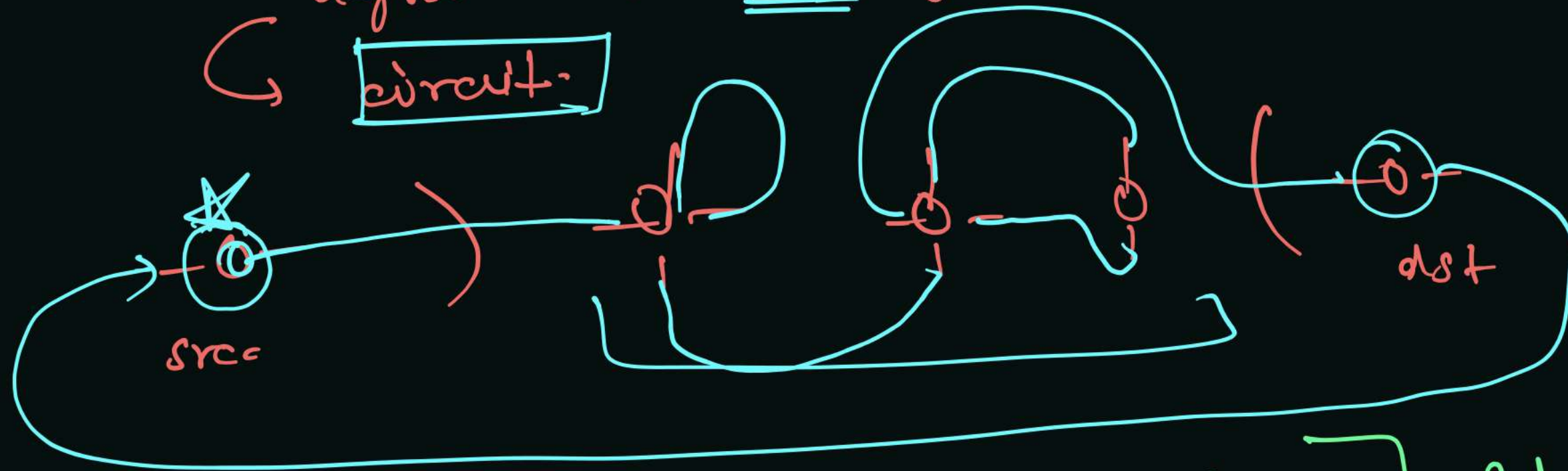
Eulerian circuit.

audio??

text ms



degree → Even for add vertex  
circuit



(n-2) vertices degree - Even  
strictly 2 nodes degree - odd  
Eulerian path

src



directed graph →

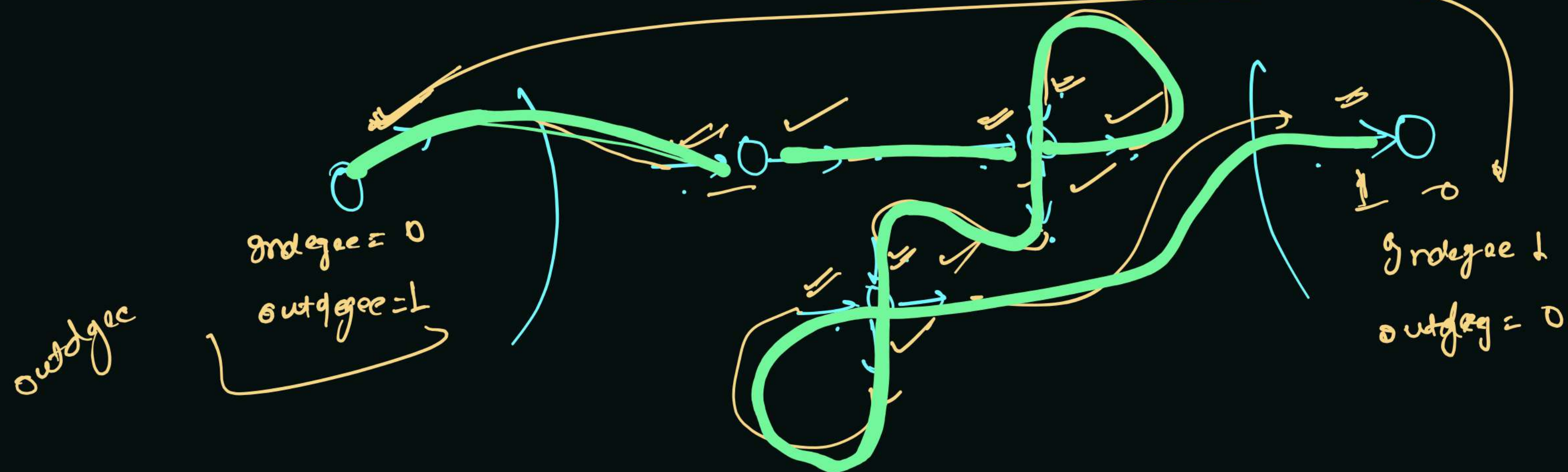
Indegree and outdegree

Eulerian circuit ↔

indegree == outdegree ] → for Every node.

Eulerian path → (n-2) nodes have indegree == outdegree for Every nodes

indegree == outdegree ± 1 || outdegree == indegree + 1



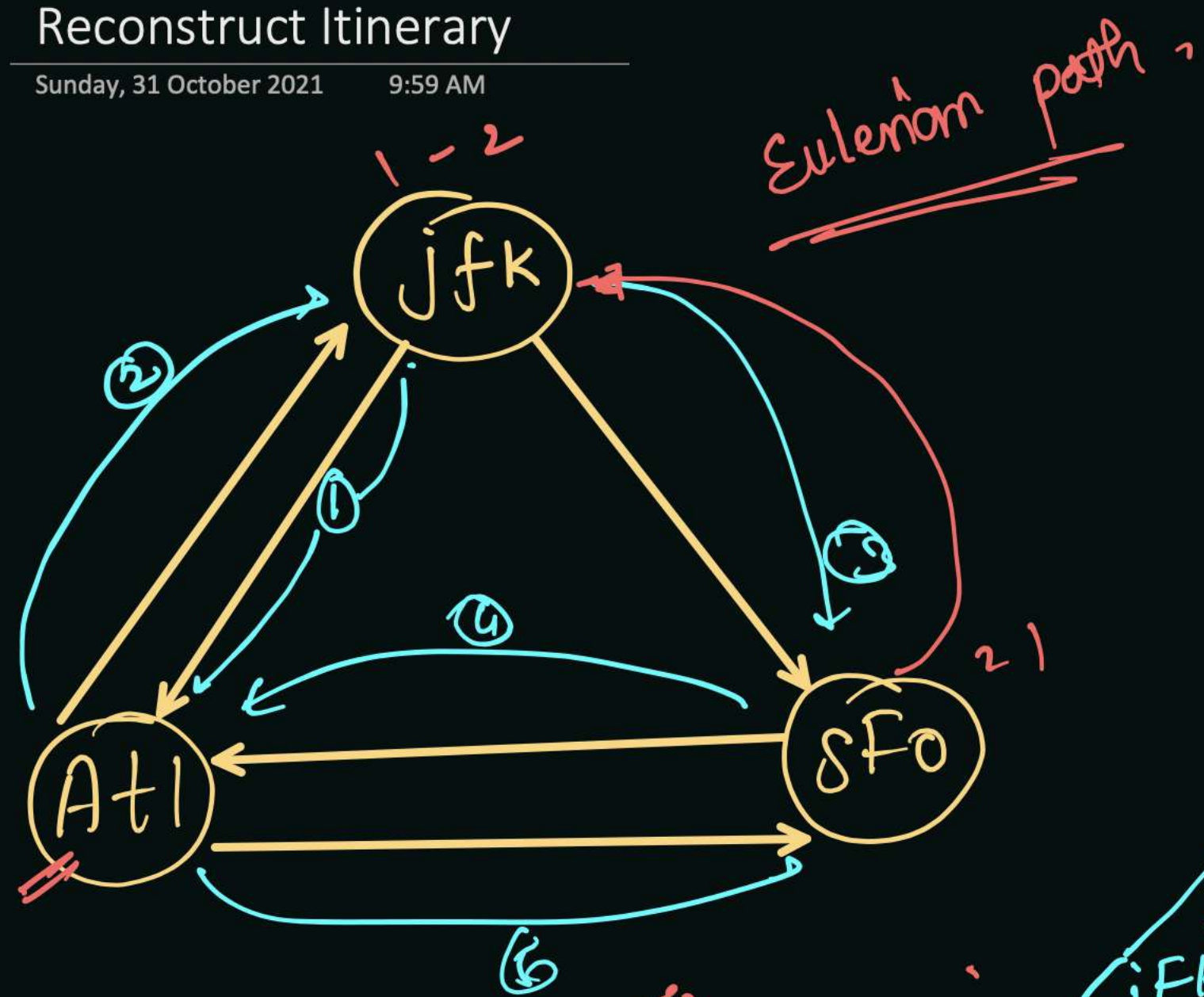
total  
indegree = 6

total  
outdegree = 7



# Reconstruct Itinerary

Sunday, 31 October 2021 9:59 AM

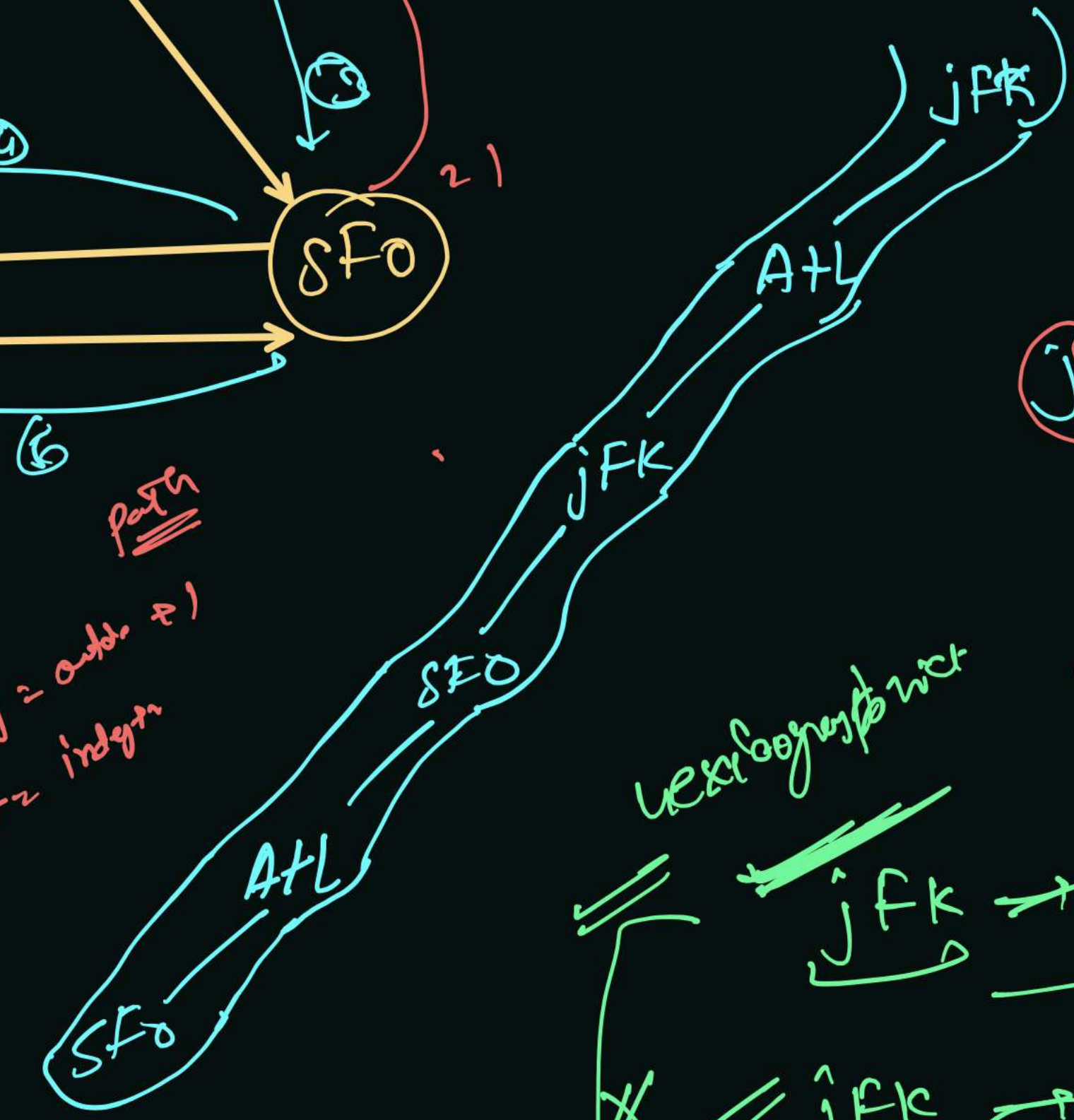


3 vertices  
 2 → int  
 2 —  
 Indeg = outdeg + 1  
 out = indeg

JFK → ~~ATL~~ ~~SFO~~  
 ATL → ~~JFK~~ ~~SFO~~  
 SFO → ~~ATL~~

source → (JFK)

→ a a g b d e  
 → a b h c d e



post order

LinkedList

JFK → ATL → JFK → SFO → ATL → SFO → JFK  
 add first  
 (0, 1)

graph

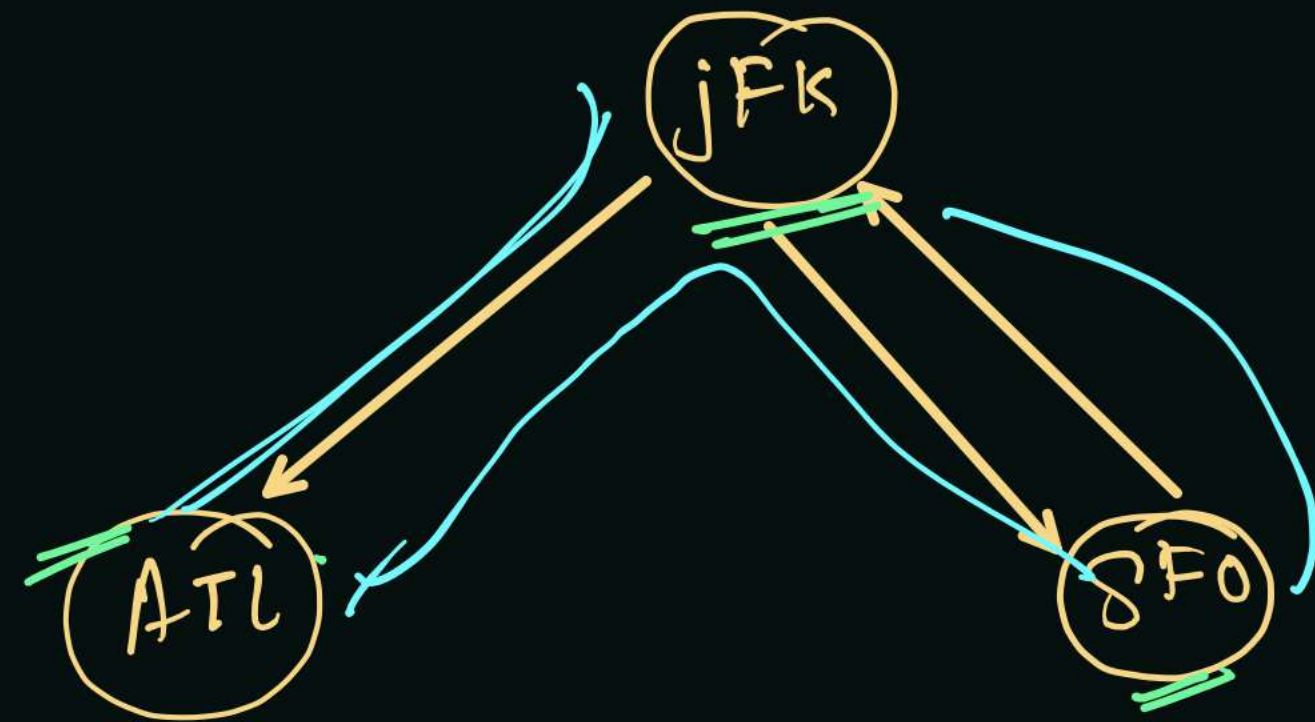
HashMap < String, PriorityQueue < String > > graph

Lexicographically

JFK → ATL → JFK → SFO → ATL → SFO  
JFK → SFO → ATL → JFK → ATL → SFO



Problem with construction of answer in Pre Order ?



dst

Pre Order





## Hint

- add Reverse Edge with cost 1
- find shortest path from 1 to N using Dijkstra's <sup>interns of weights</sup>

Algor

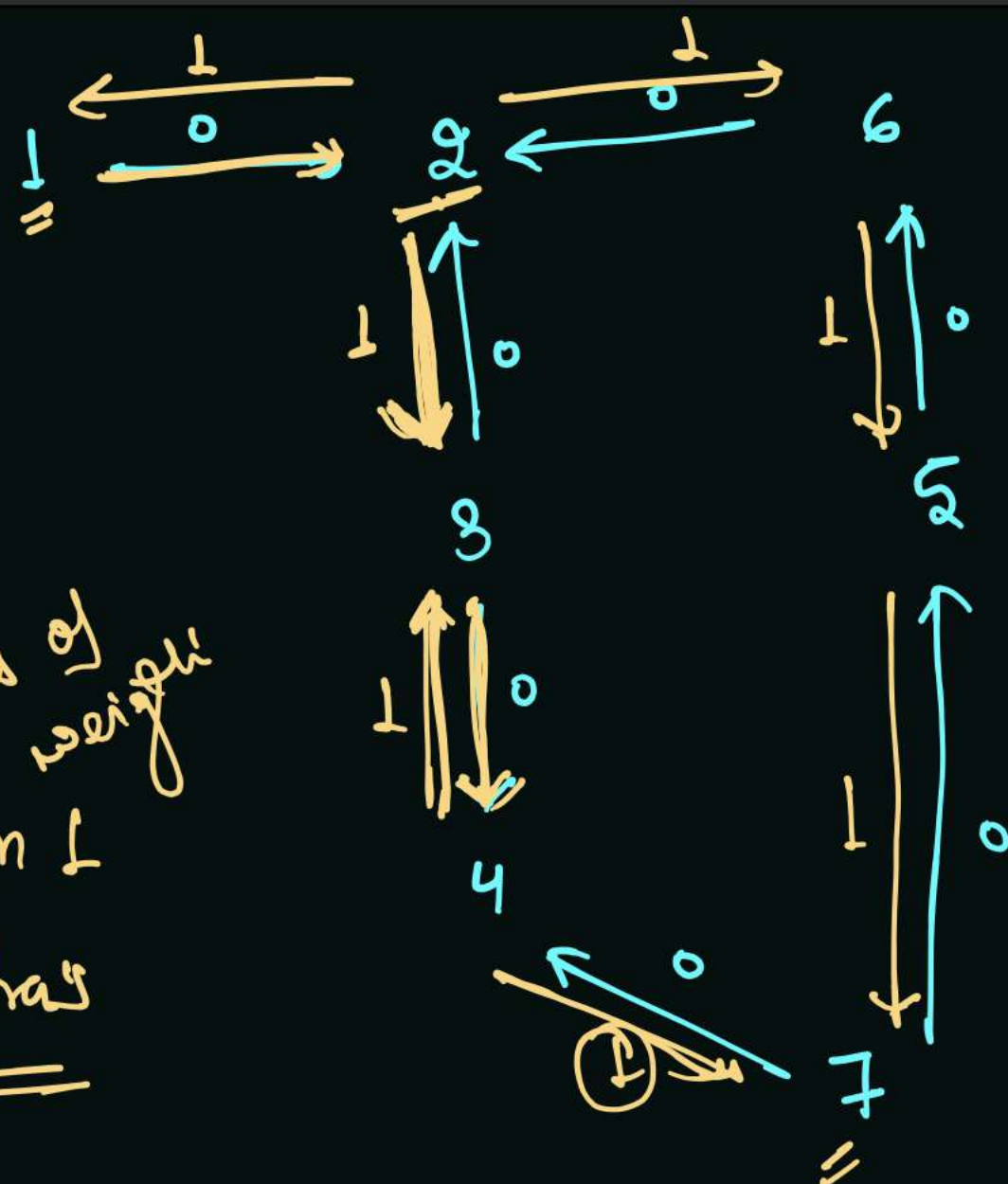
cost == Result

1 to N

$(E \log V)$

Result == 2

2 == Revs



Min Number of Edge required to reverse, such that we can visit from 1 to N, i.e

1 to 7-

vtx, pxf, cst

1, 1, 0

2, 12, 0

3, 123, 0

3, 123, 1

4, 1234, 1

7, 12347, 2

6, 126, 1

5, 1265, 2

7, 12657, 3

\* BFS == Dijkstra

queue == priority

\* weight = 0, 1

priority

Queue

1, 2  
2, 2  
2, 3

1, 2  
2, 2  
2, 3

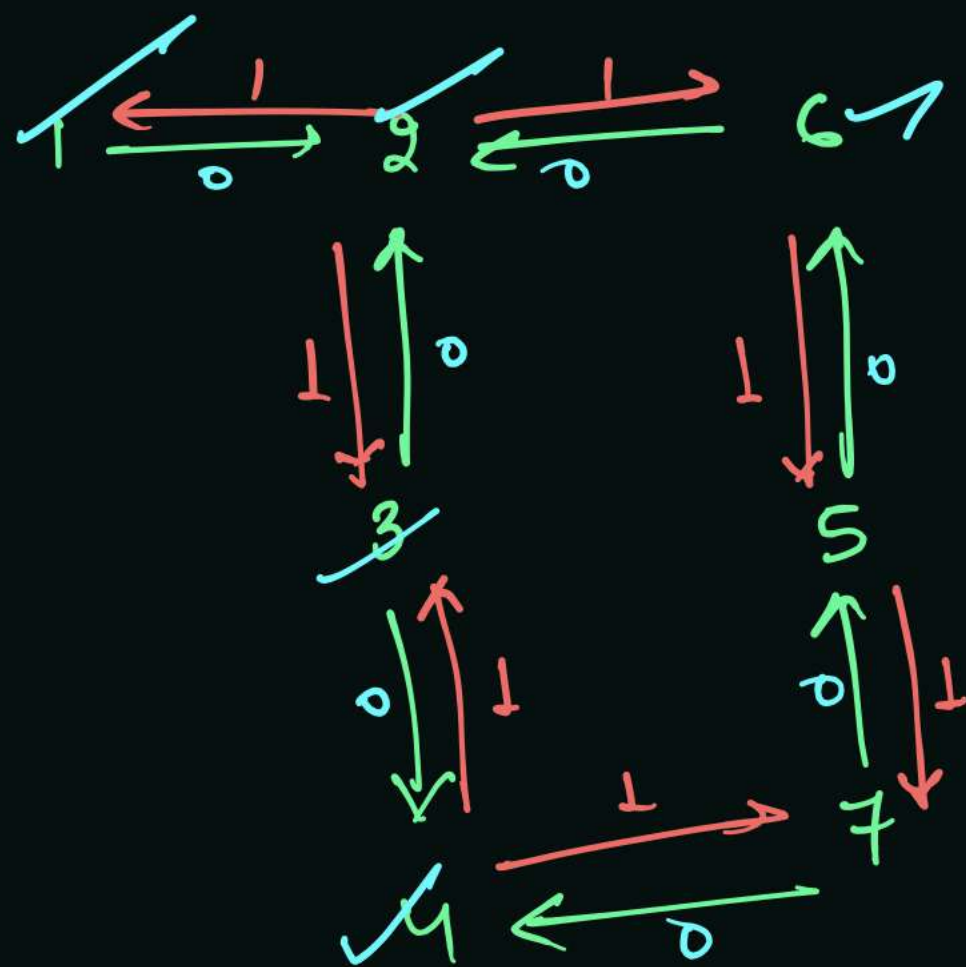
BFS

$E+V$

$y+n$

$y+2$





0-1 BFS.

(0, 1)

Linked list  
ptr, pos, cost so far

y type - addFirst → Remove  
y+1 type - addLast

