

Kadane's Algorithm.

find max. sum subarray with k -concatenated array.

Δ
arr = $\{1, 2\}$, $\underline{k=3}$
k times

~~virtual~~

$B =$

$\{1, 2, 1, 2, 1, 2\}$

Max. sum subarray??

k times arr



k - concatenated - array

k - concatenated - virtual

cyclic loop

constraints

- ① A size of array = 10^5 length
- ② range of $k = 10^9$

\Rightarrow we can't make an array with concatenation.

- ③ Time limit = 1 sec.

\Rightarrow In 1 sec. we can do 10^9 operation.
 \rightarrow cyclic loop of k -concatenated array will not work.

Find Total sum of array?? Significance?

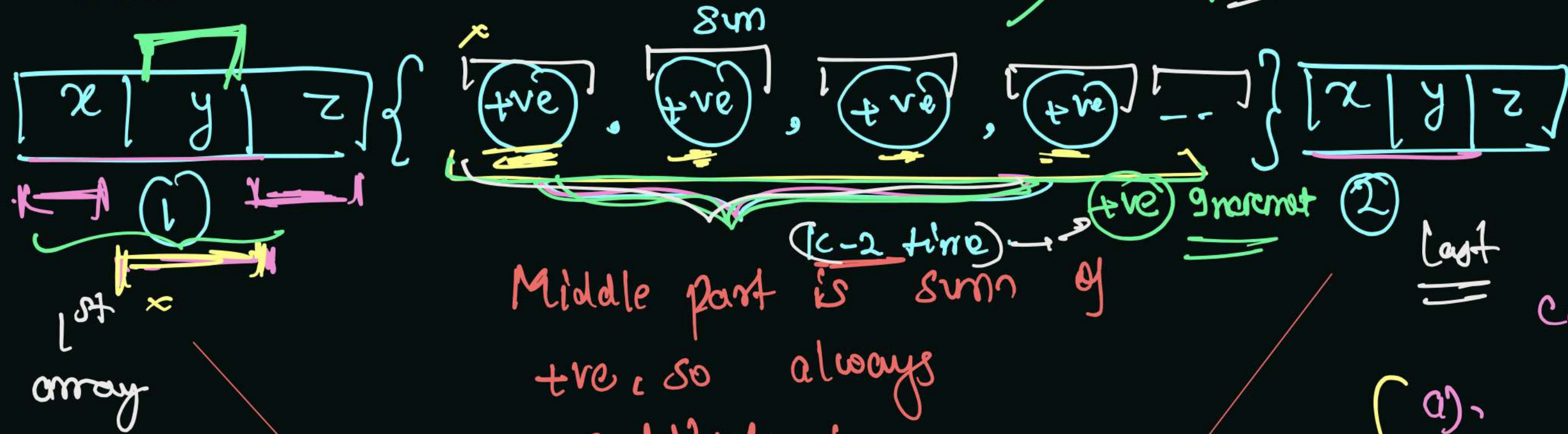
$Tsum \rightarrow \text{sum of array} \rightarrow (\text{single array}) =$ given A

Case-I

if ($Tsum \geq 0$)

$Tsum = +ve$

Include in Subarray
positive increment



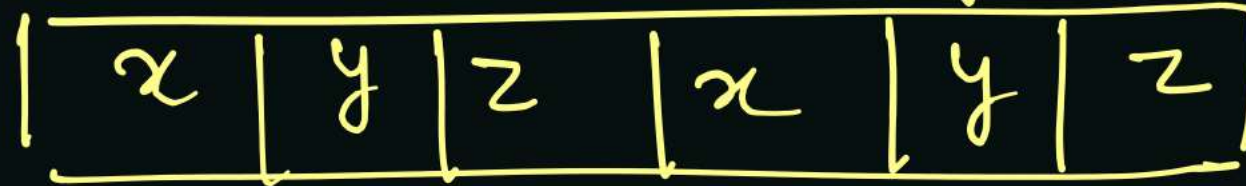
overlapping of array in finding

last sub case \rightarrow

mutual Kadane will encounter

Middle part is sum of $+ve$, so always contribute in sum of subarray

concatenate array



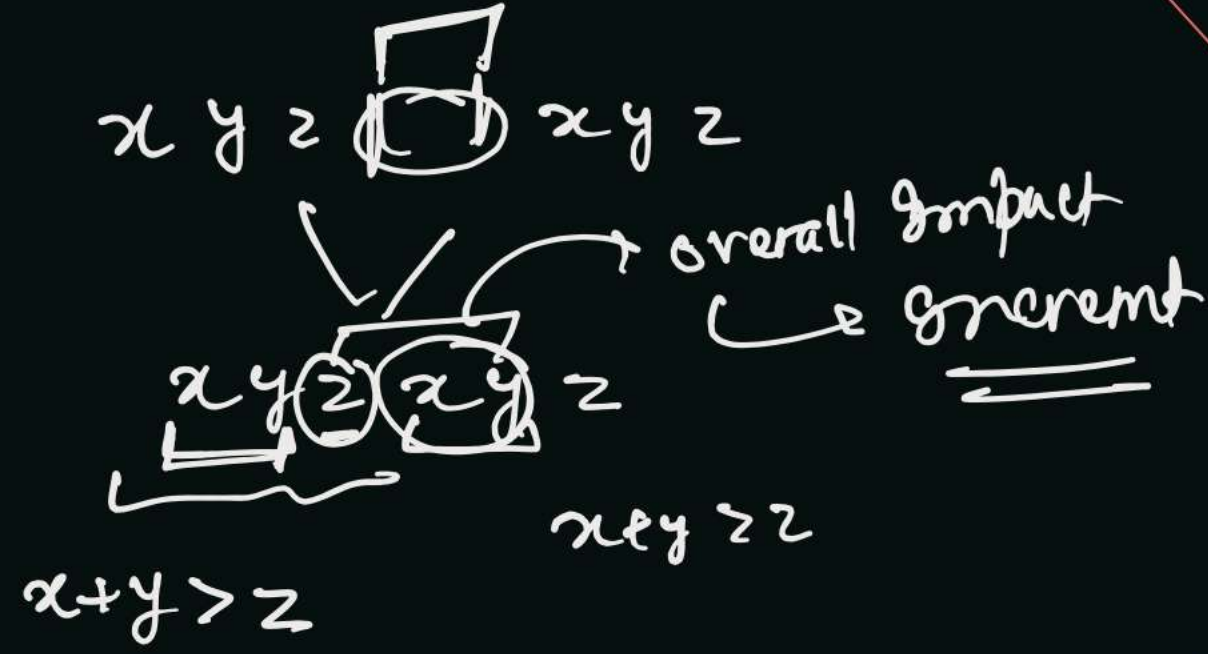
- a).
- b).
- c).
- d).



$Tsum = -ve$

Case-II, if ($Tsum < 0$)

Kadane's



overall impact \rightarrow increment

$x+y > z$

$x+y > z$

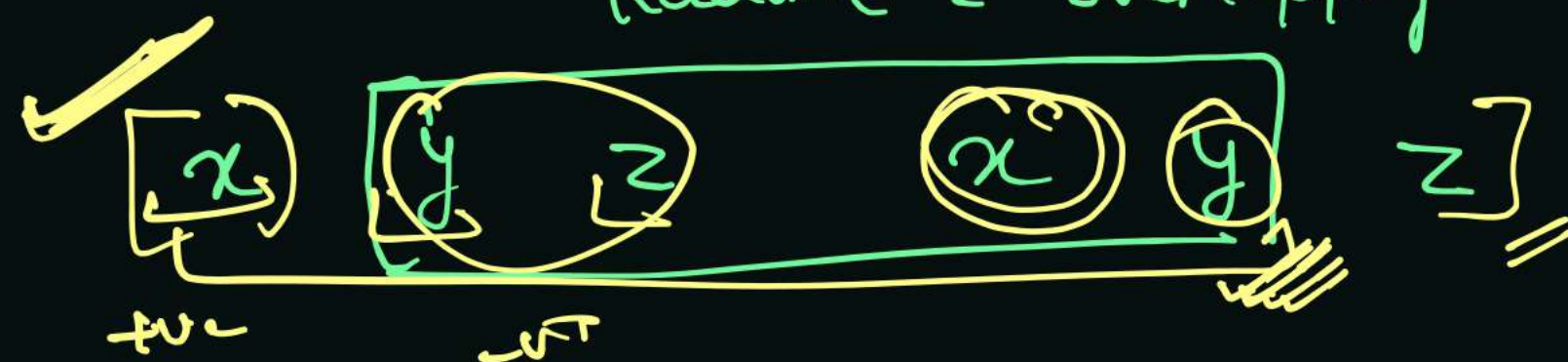
Why overlapping of array in mutual Kadane's will encounter \rightarrow

$$\underline{\underline{x+y+z > 0}}$$

array $\rightarrow x, y, z$

Kadane - overlapping -

2x Array



Kadane's in single array

$x, [y, z]$

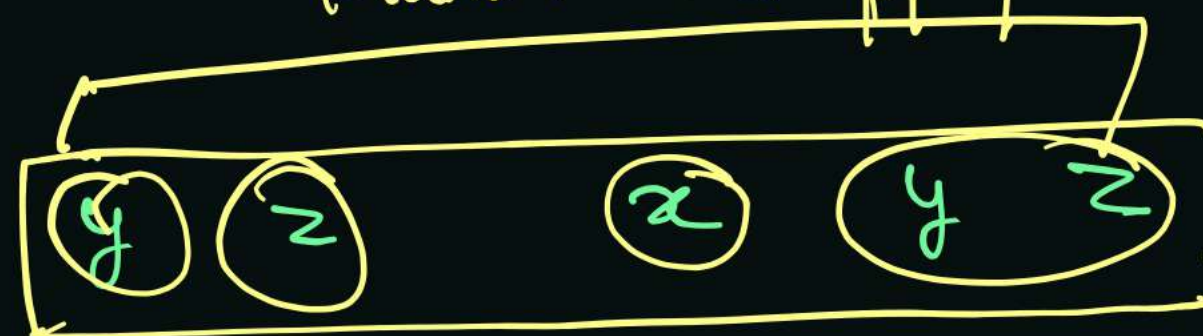
$-x$

$y, z \rightarrow +ve$

$$x > (y+z) \quad y+z > x$$

Mutual overlapping

x



$$x+y > z$$

// ✓

middle

$$x < y+z$$

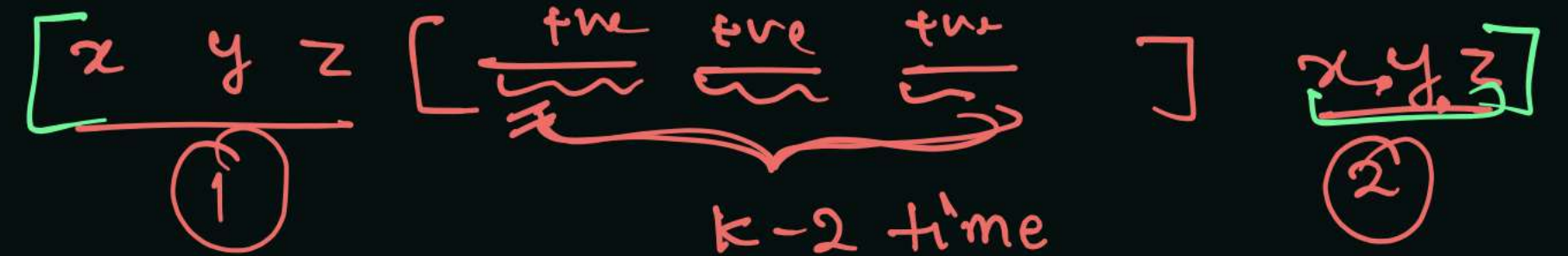
$$y+z > x$$

$$y+z + \text{true}$$

$$x+y+z \Rightarrow \underline{\underline{+ve}}$$

So, if total sum is ve or 0

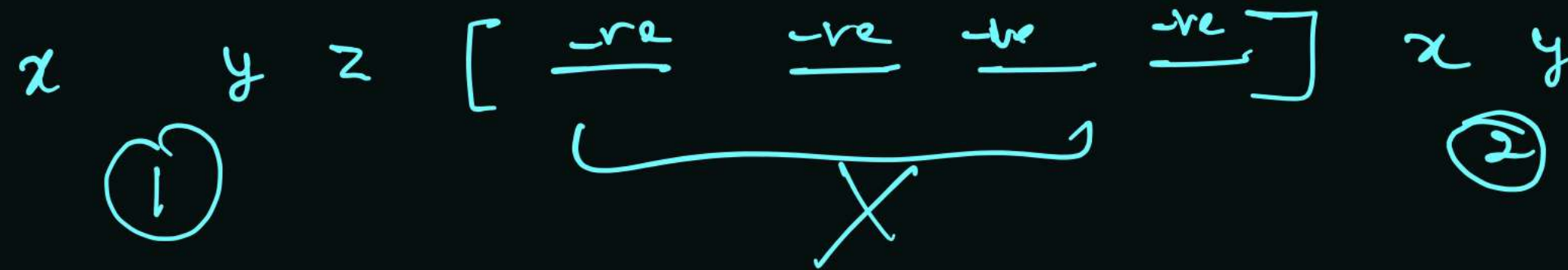
$$\text{sum} = \text{Tsum}$$



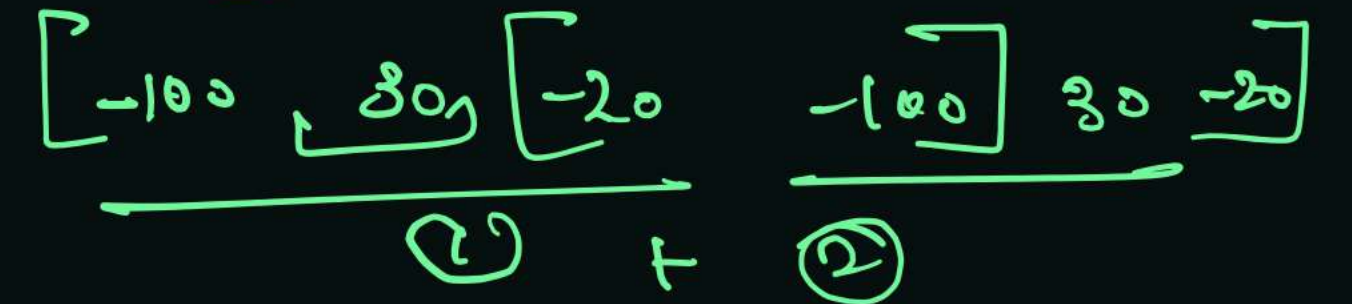
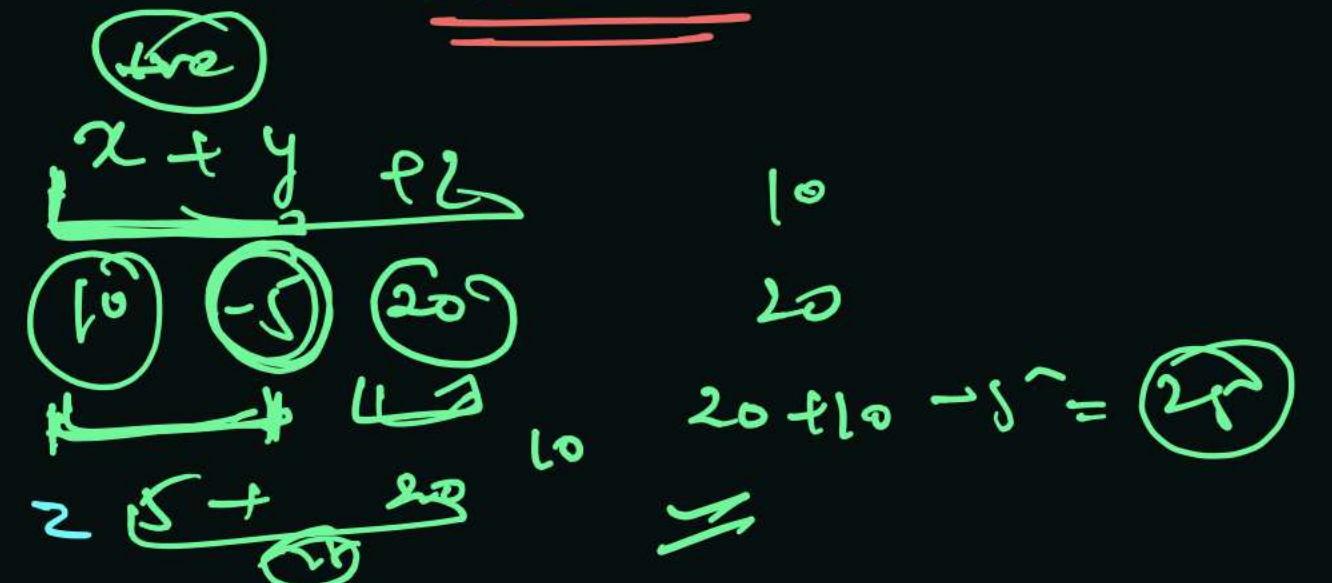
$$\text{Max Sum} = (\text{sum} * k-2) + \text{kadane's}(1+2)$$

Case - II

Total sum < 0



$$\underline{x+z} > y$$



kadane's of 1+2 max possible sum. k time cont

Example ->

$$A = [10 \quad -100 \quad 30]$$

$$\text{max sum} = \underline{\text{kadane's}(1+2)}$$



$$\underline{\underline{(1) + (2) \text{ kadane's}}}$$

Maximum Sum of Smallest and Second Smallest in all possible subarray

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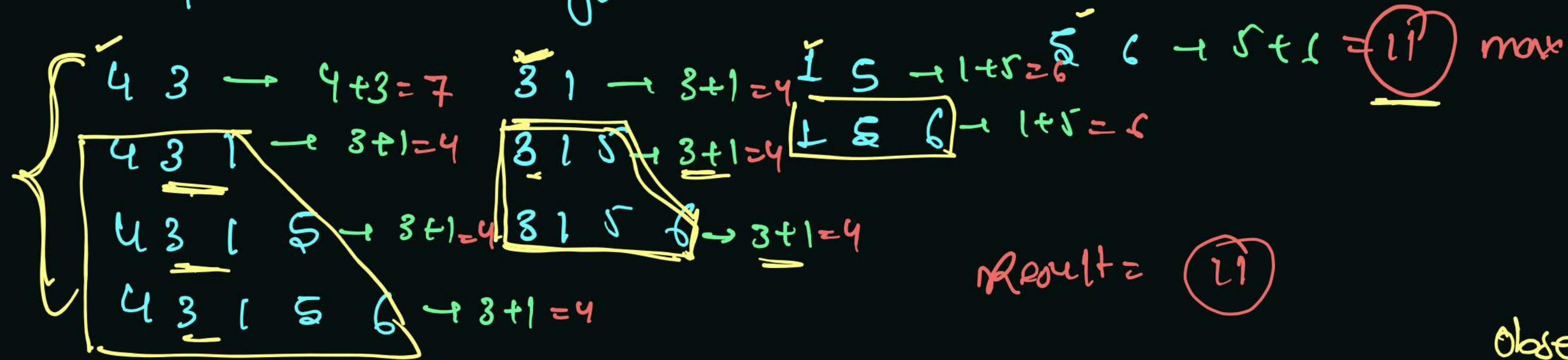
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arr \rightarrow 4 3 1 5 6

maximum of min & second min

\hookrightarrow adjacent two elements
max

all possible subarrays with atleast two values \rightarrow



use less

Subarray

logic \rightarrow find max sum of two adjacent element.

4 3 1 5 6

4 3
7

3 1
4

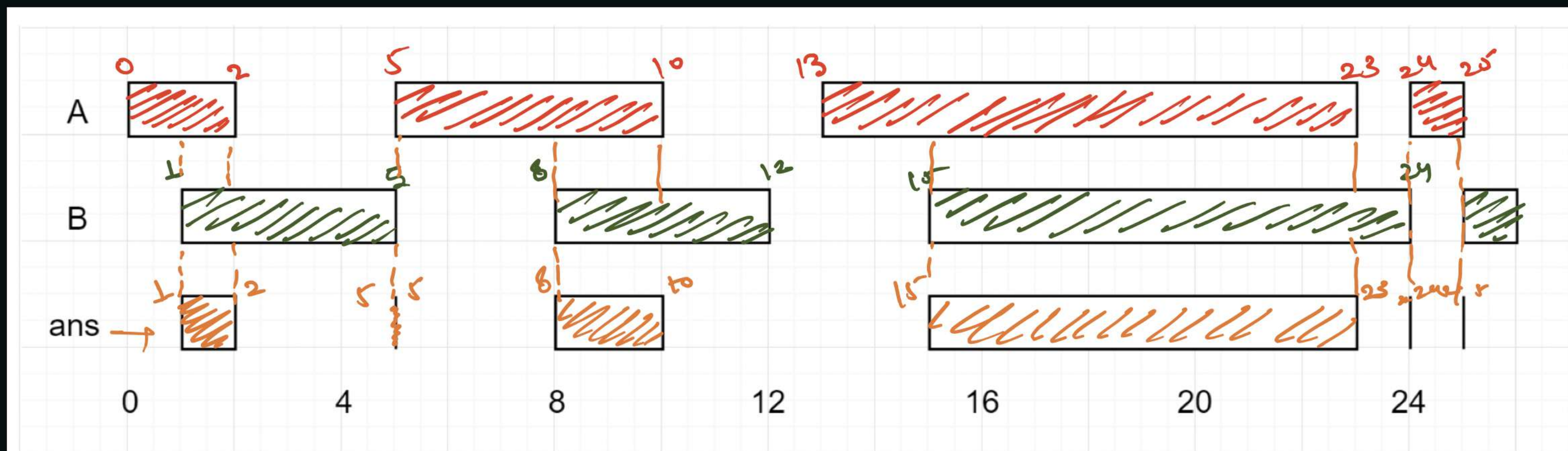
1 5
6

5 6
11

\Rightarrow 11 Result

Interval List Intersection

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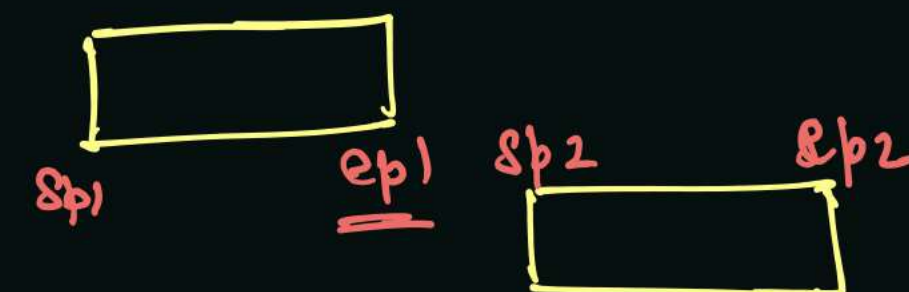
Input: firstList = $[[0,2],[5,10],[13,23],[24,25]]$, secondList = $[[1,5],[8,12],[15,24],[25,26]]$

Output: $[[1,2],[5,5],[8,10],[15,23],[24,24],[25,25]]$

Possible cases with two list

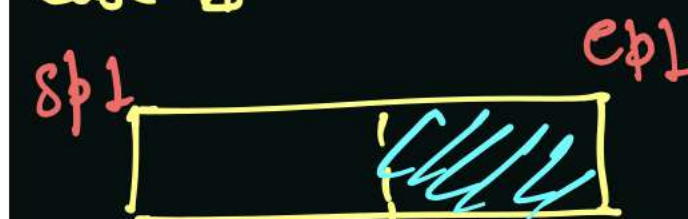
Case-I

$ep1 < sp2 \rightarrow \text{No Int}$



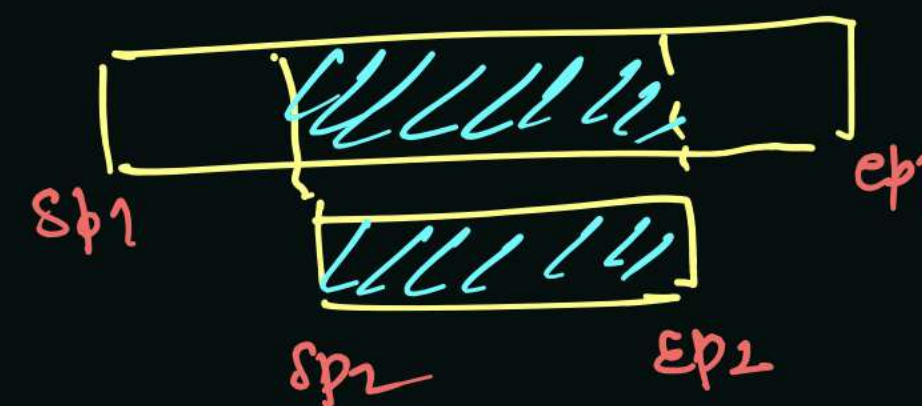
No Intersection.

Case-II

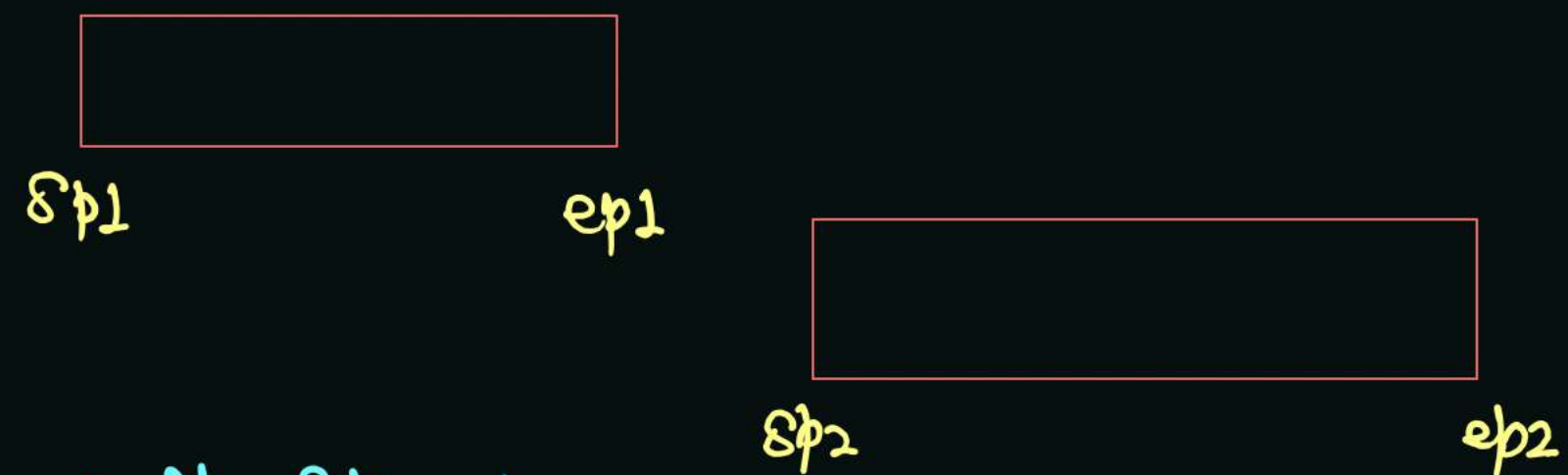


Intersection $st \rightarrow \max(sp1, sp2)$
End $\rightarrow \min(ep1, ep2)$

Case-III



Case-I



→ No Intersection

$$\text{Starting} = \max(sp1, sp2) = sp2$$
$$\text{Ending} = \min(ep1, ep2) = ep1$$

Here $ep1 < sp2$
So it is not possible
to end before interval
start.

i.e. \Rightarrow No Intersection

Case-II

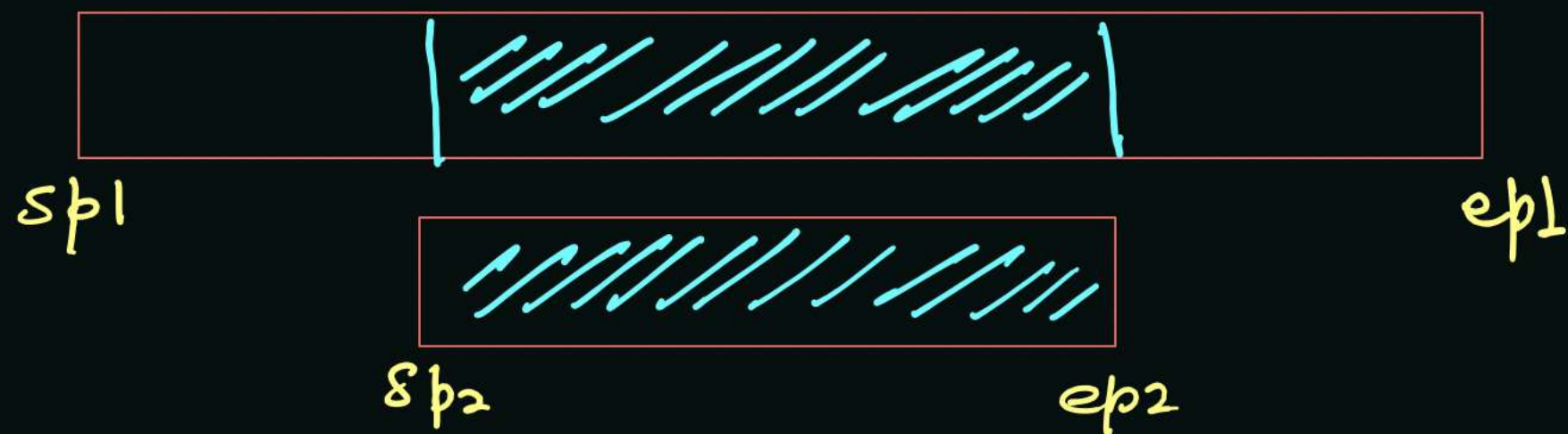


$$\text{Starting} = \max(sp1, sp2) = sp2$$

$$\text{Ending} = \min(ep1, ep2) = ep1$$

$(sp2 - ep1)$

Case-III



$$\text{Starting} = \max(sp1, sp2) = sp2$$

$$\text{Ending} = \min(ep1, ep2) = ep2$$

$$\text{Interval} = \underline{(sp2, ep2)}$$

First List = $[[0,2],[5,10],[13,23],[24,25]]$,
 second List = $[[1,5],[8,12],[15,24],[25,26]]$

i →

0	2
5	10
13	23
24	25

j →

1	5
8	12
15	24
25	26

$[i \rightarrow]$

How to increase pointer -

→ on the basis of ending point.

$$\underline{24 - 25}$$

$$15 - 24$$

$$\underline{\underline{25 - 24}}$$

$$\underline{24 - 25}$$

$$\underline{25 - 24}$$

$$(25 - 25)$$

Result

$[1-2] [5-5] [8-10] [15-23]$

$[24-24] [25-25]$

Insert Intervals

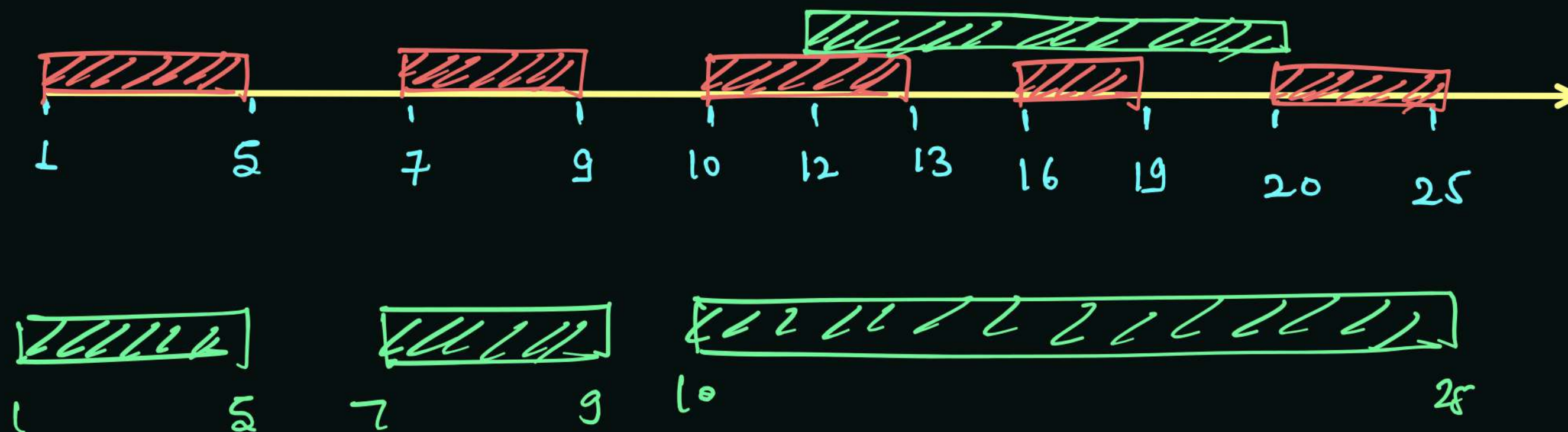
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Intervals → 5 → no. of intervals

Merge Intervals → time interval
 $O(n \log n)$

n intervals {
1 5 ✓
7 9 ✓
10 13 ✓
16 19 ✓
20 25 ✓
12 20 ✓
new interval

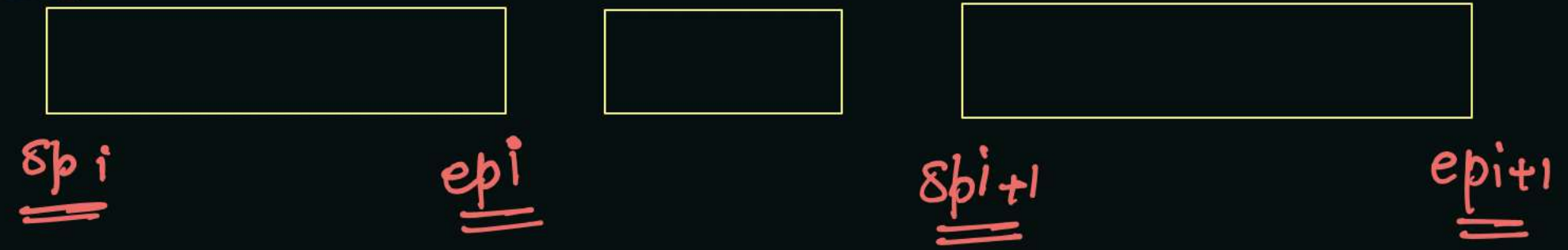


After
insertion

1-5 7-9 10-25] 1-

Allowed → $O(n)$

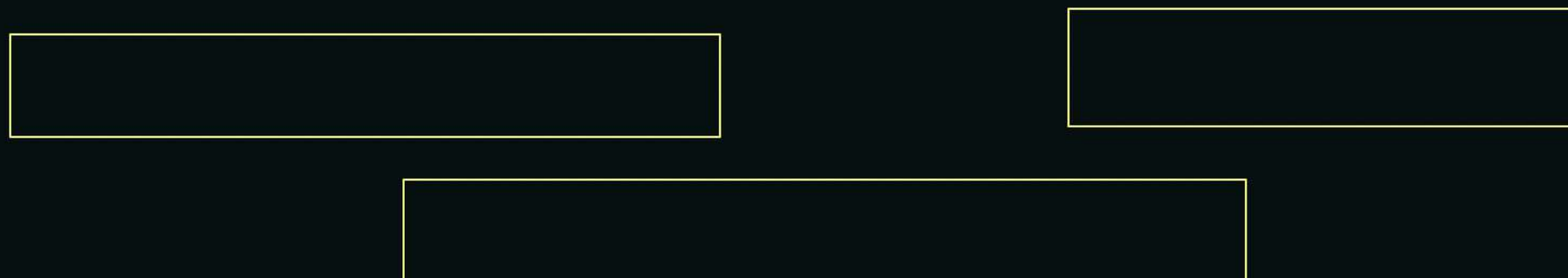
Case-I



Case-II



Case-III



Merge Sort

1-3

4-6
↑
i

7-10
↑

11-16
↑

13-21
↑

20-25
↑

13-21
↑

16p = 1 4 7 11

16p = 2 6 10 16 21 25

[1-3] [4-6] [7-10] [11-25]