

① Design given logic function using NAND gates.

$$F(A, B, C) = A + B \cdot C$$

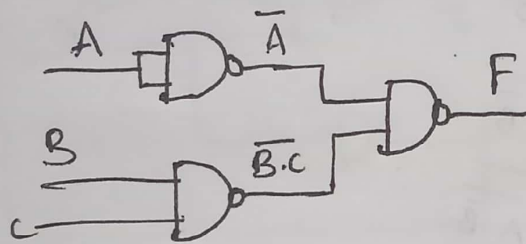
Apply double complement on both sides.

$$\overline{\overline{F}} = \overline{\overline{A + B \cdot C}} \quad \text{apply De Morgan's Theorem.}$$

$$= \overline{\overline{A} \cdot \overline{B \cdot C}} \quad \overline{X + Y} = \overline{X} \cdot \overline{Y}$$

$$F = \overline{X \cdot Y} \quad X = \overline{A}$$

$$Y = \overline{B \cdot C}$$



② Design given logic function using NOR gates

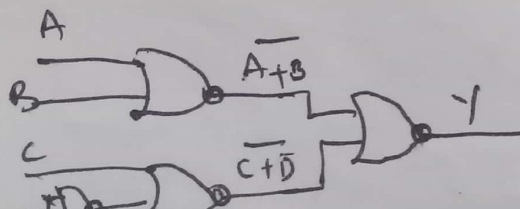
$$Y = (A + B) \cdot (C + D)'$$

$$\overline{\overline{Y}} = \overline{\overline{(A + B) \cdot (C + D)'}} \quad \text{apply De Morgan's Theorem.}$$

$$= \overline{\overline{A + B} + \overline{C + D}}$$

$$Y = \overline{X + Y}$$

$$X = \overline{A + B}, \quad Y = \overline{C + D}$$



③ Design given logic function using NAND gate.  $F = \bar{A} \cdot B + A \cdot \bar{B}$

$$F = \bar{A} \cdot B + A \cdot \bar{B}$$

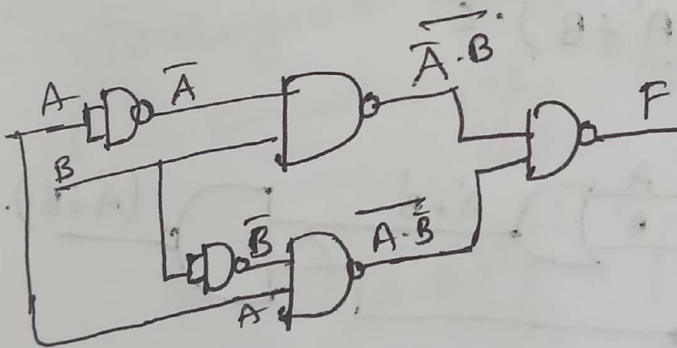
$$\bar{F} = \overline{\bar{A} \cdot B + A \cdot \bar{B}}$$

$$= \overline{\bar{A} \cdot B} \cdot \overline{A \cdot \bar{B}}$$

$$F = \overline{X \cdot Y}$$

$$X = \bar{A} \cdot B$$

$$Y = A \cdot \bar{B}$$



## Demorgan's Theorem based problems

- ① Simplify the expression using De Morgan's Theorem and draw the logic circuit.

$$Y = (A \cdot B + C)'$$

Sol:

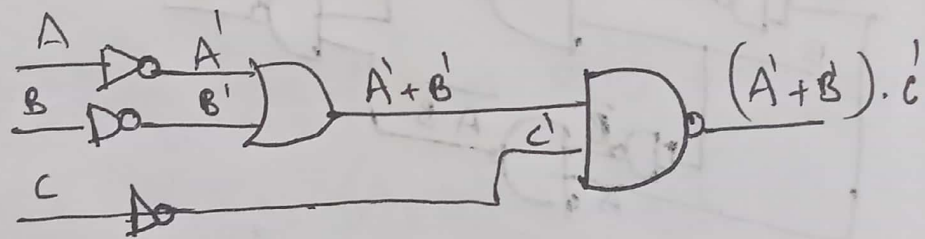
By applying Demorgan's Theorem

$$(X + Y)' = X' \cdot Y'$$

$$Y = (A \cdot B)' \cdot C'$$

$$Y = (A' + B') \cdot C'$$

$$Y = (A' + B') \cdot C'$$



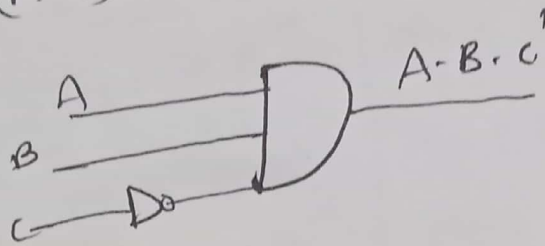
② Simplify the expression using De-Morgan's Theorem and draw the logic circuit.

$$Y = ((A \cdot B)' + C)'$$

$$\boxed{(X')' = X}$$

Sol:  $Y = ((A \cdot B)')' \cdot C'$

$$= (A \cdot B) \cdot C'$$

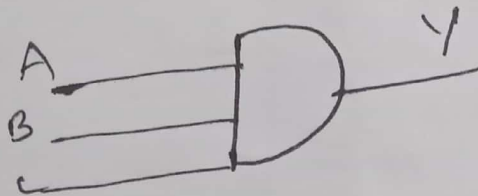


③ Simplify the expression using De-Morgan's Theorem and draw the logic circuit.  $Y = ((A \cdot B)' + C')'$

Sol:  $Y = ((A \cdot B)')' \cdot (C')'$

$$= (A \cdot B) \cdot C$$

$$\boxed{\text{Note } ((X')')' = X}$$



Long Answer Session 9 Terminal Questions

3. Create separate tables listing Min and Max terms for 2-variables (A, B) and 3-variables (A, B, C).

A	B	Minterm	Maxterm
0	0	$m_0 = \bar{A} \cdot \bar{B}$	$M_0 = A + B$
0	1	$m_1 = \bar{A} \cdot B$	$M_1 = A + \bar{B}$
1	0	$m_2 = A \cdot \bar{B}$	$M_2 = \bar{A} + B$
1	1	$m_3 = A \cdot B$	$M_3 = \bar{A} + \bar{B}$

A	B	C	Minterm	Maxterm
0	0	0	$m_0 = \bar{A} \cdot \bar{B} \cdot \bar{C}$	$M_0 = A + B + C$
0	0	1	$m_1 = \bar{A} \cdot \bar{B} \cdot C$	$M_1 = A + B + \bar{C}$
0	1	0	$m_2 = \bar{A} \cdot B \cdot \bar{C}$	$M_2 = \bar{A} + B + C$
0	1	1	$m_3 = \bar{A} \cdot B \cdot C$	$M_3 = A + \bar{B} + \bar{C}$
1	0	0	$m_4 = A \cdot \bar{B} \cdot \bar{C}$	$M_4 = \bar{A} + B + C$
1	0	1	$m_5 = A \cdot \bar{B} \cdot C$	$M_5 = \bar{A} + B + \bar{C}$
1	1	0	$m_6 = A \cdot B \cdot \bar{C}$	$M_6 = \bar{A} + \bar{B} + C$
1	1	1	$m_7 = A \cdot B \cdot C$	$M_7 = \bar{A} + \bar{B} + \bar{C}$



4. Minimize the given Product of Sum (Pos) using Boolean laws and sketch the logic circuit.

$$Y = (A+B)(A+\bar{B})(\bar{A}+B)$$

Sol:-

$$Y = (A.A + A.\bar{B} + A.B + B.\bar{B})(\bar{A}+B)$$

$$= (A + A.\bar{B} + A.B + 0)(\bar{A}+B)$$

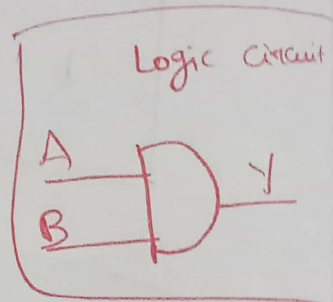
$$= (A + A[B+\bar{B}])(\bar{A}+B)$$

$$= (A + A)(\bar{A}+B)$$

$$= A(\bar{A}+B)$$

$$= A.\bar{A} + AB$$

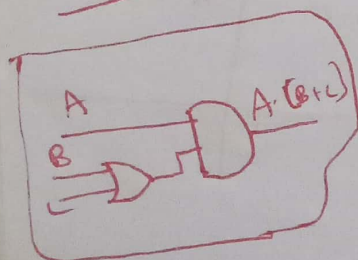
$$\boxed{Y = AB}$$



5. Minimize the given sum of products (Sop) using Boolean laws and sketch the logic circuit.

$$F(A,B,C) = A\bar{B}c + A\bar{B}\bar{c} + A\bar{B}c$$

Soln  $F = A\bar{B}c + A\bar{B}[\bar{c}+c]$



$$= A\bar{B}c + AB$$

$$= A[\bar{B}c + B]$$

$$= A[(\bar{B}+B).(c+B)]$$

$$F = A[B+c]$$

$$c+\bar{c} = 1$$

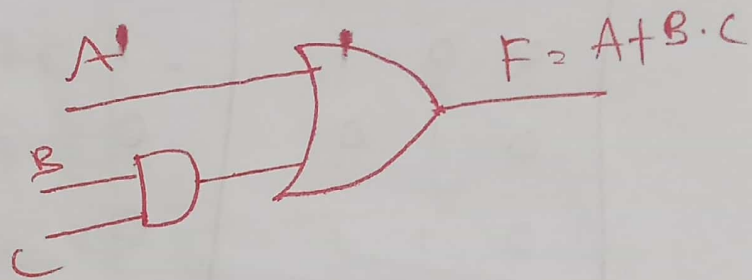
$$B+\bar{B} = 1$$

6. Minimize the given Sum of products (Sop) using Boolean laws and sketch the logic circuit.

$$F(A, B, C) = A \cdot C + A \cdot \bar{C} + B \cdot C$$

$$F = A [C + \bar{C}] + B \cdot C$$

$$F = A + B \cdot C$$



## Short Answer Questions

1. Develop a truth table that represents the Boolean equation.

$$F = \bar{A}\bar{B}C + A\bar{B}\bar{C} + AB\bar{C} + ABC$$

$$= \sum m(1, 4, 6, 7)$$

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1



2. Develop a truth table and express the Boolean function in minterm form.

$$F = \bar{A}B + A\bar{B} + ABC$$

$$F = \bar{A}B(C + \bar{C}) + A\bar{B}(C + \bar{C}) + ABC$$

$$F = \bar{A}BC + \bar{A}B\bar{C} + A\bar{B}C + A\bar{B}\bar{C} + ABC$$

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

$$F = \sum m(2, 3, 4, 5, 7)$$

Example:  $72 - 58$  (Using 1's Complement)

Step 1: 72 in binary (8-bit)  $\rightarrow 01001000$   
58 in binary (8-bit)  $\rightarrow 00111010$

Step 2:- 1's complement of subtrahend (58)  
 $11000101$

Step 3: Add minuend + 1's complement of subtrahend

$$\begin{array}{r} 01001000 \\ + 11000101 \\ \hline 10000101 \end{array}$$

End around carry

$\rightarrow$  Add carry to the result.

$$\begin{array}{r} 00001101 \\ + 1 \\ \hline 00001110 \end{array}$$

Step 4: Result -  $00001110$   
Decimal Equivalent  $\rightarrow 14$

Example: Perform the 2's complement Subtraction on given decimal values.  
 $89 - 27$ .

STEP 1: 89 in binary  $\rightarrow (01011001)_2$   
26 in binary  $\rightarrow (00011010)_2$

STEP 2: Take 2's complement of subtrahend (26).

2's complement = 1's complement + 1

1's comp of 26  $\rightarrow 11100101$

Add 1

$\begin{array}{r} 11100101 \\ + 1 \\ \hline 11100110 \end{array}$

STEP 3: Add minuend with 2's complement of Subtrahend.

minuend = 89  $\rightarrow 01011001$   
2's complement of 26  $\rightarrow 11100110$   
 $\begin{array}{r} 01011001 \\ + 11100110 \\ \hline 10100001 \end{array}$   
Discard carry

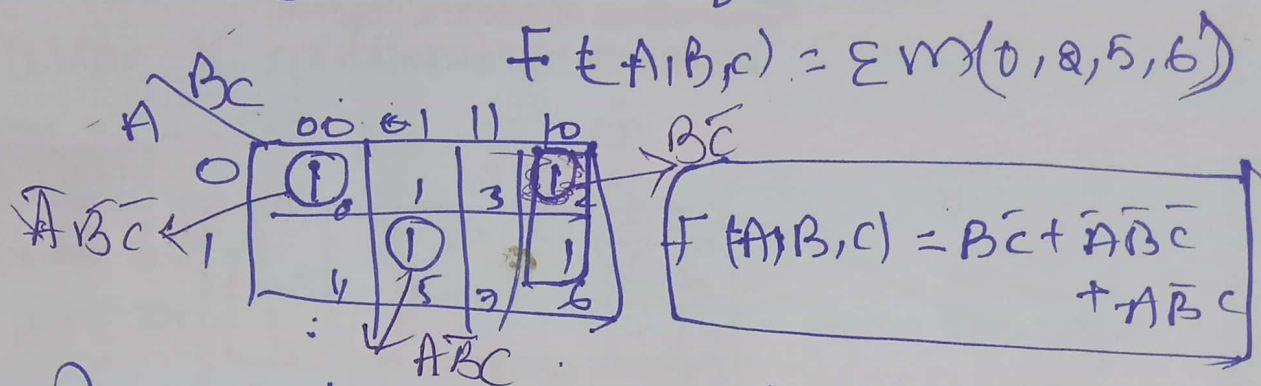
STEP 4: Interpret the result  $\rightarrow 63$

# Terminal Questions on K-maps

1

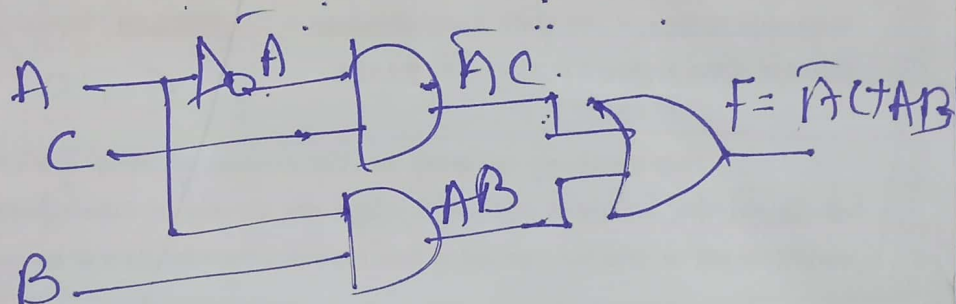
## SAD's

1) Optimize 3 variable function



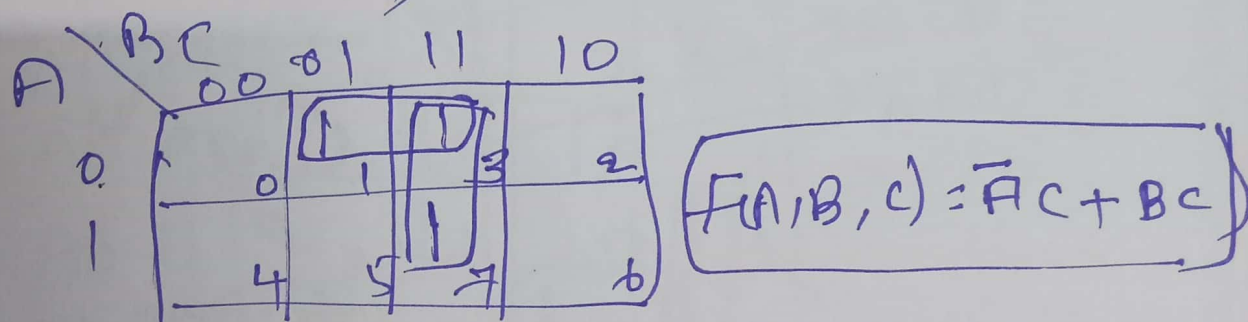
2) Realize the logic diagram for the function,

$$F = \bar{A}C + AB$$



3) Derive the simplified Boolean expressions

for  $F(A, B, C) = \sum m(1, 3, 7)$

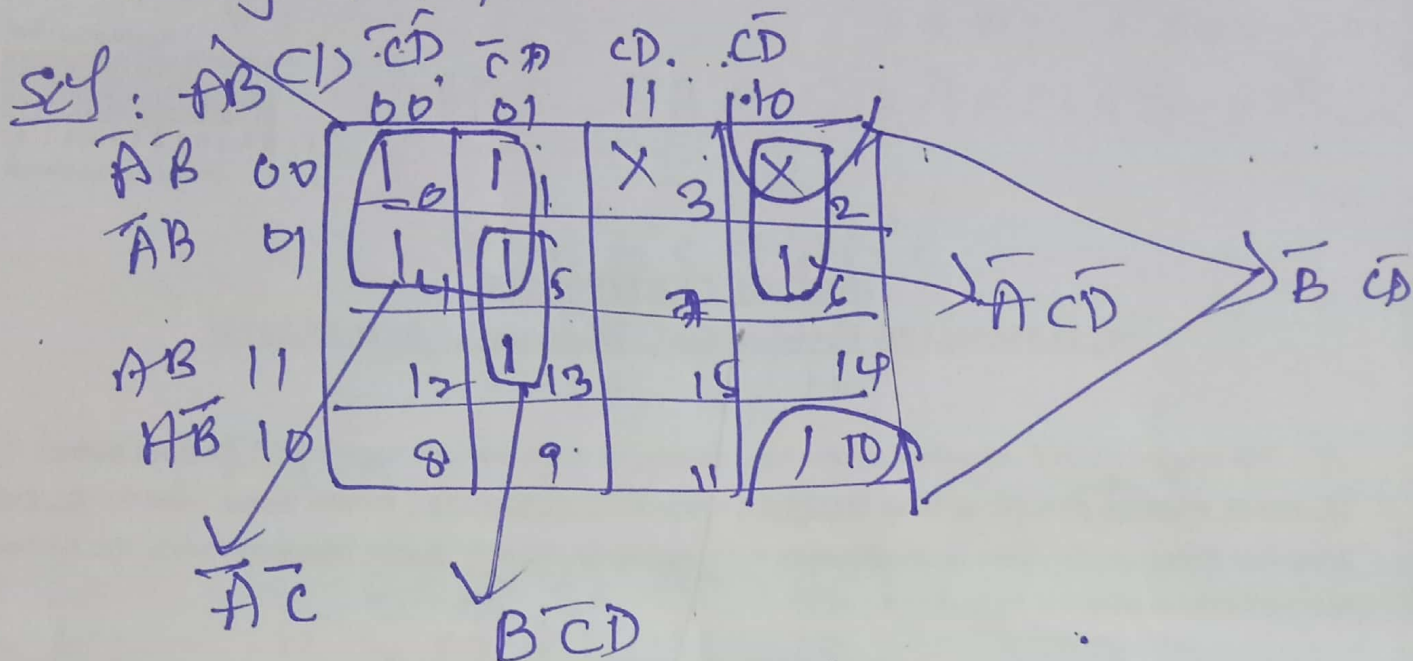




1) optimize four variable function

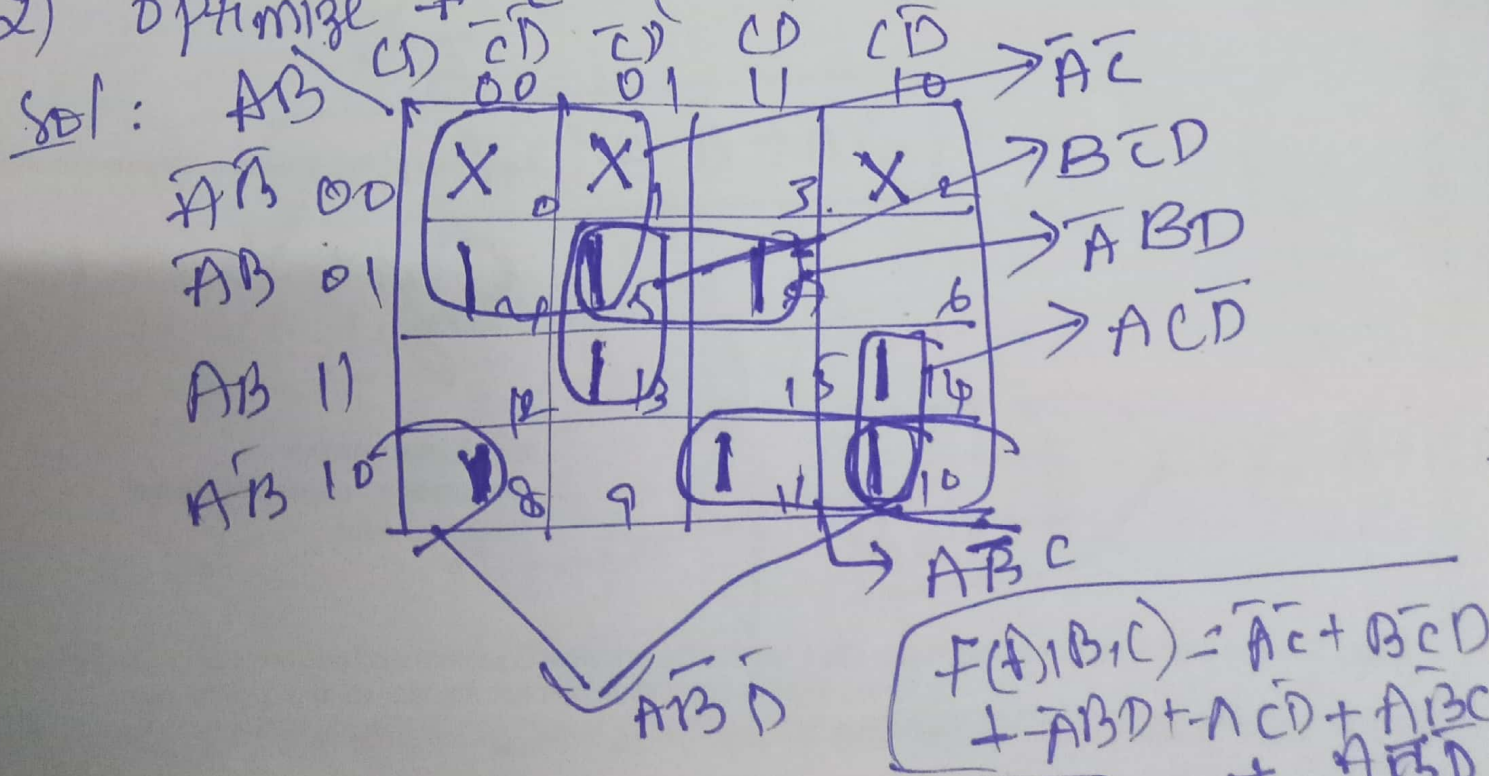
$$F(A, B, C, D) = \sum m(0, 1, 4, 5, 6, 10, 13) + d(2, 3)$$

using K-maps.



$$F(A, B, C, D) = \bar{A}\bar{C} + B\bar{C}D + \bar{A}C\bar{D} + B\bar{C}D$$

2) optimize  $F = \sum m(4, 5, 7, 8, 10, 11, 13, 14) + d(0, 12)$



$$F(A, B, C, D) = \bar{A}\bar{C} + B\bar{C}D + A B D + A C \bar{D} + A B C + A B \bar{D}$$



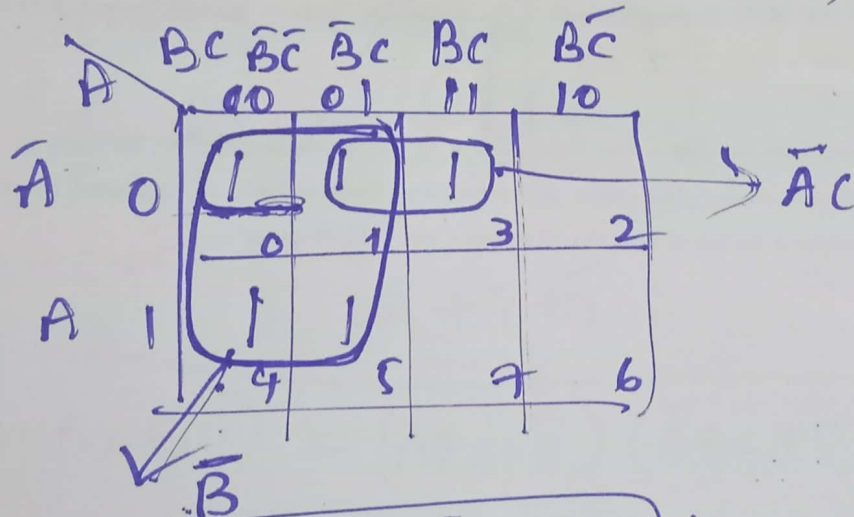
3. optimize  $F(A,B,C) = AB'C + A'B'C + A'BC + A'B'C' + AB'C'$  using K-maps and realize the resultant expression using logic gates.

Sol:- Given,  $F(A,B,C) = AB'C + A'B'C + A'BC$

$$+ A'B'C' + AB'C'$$

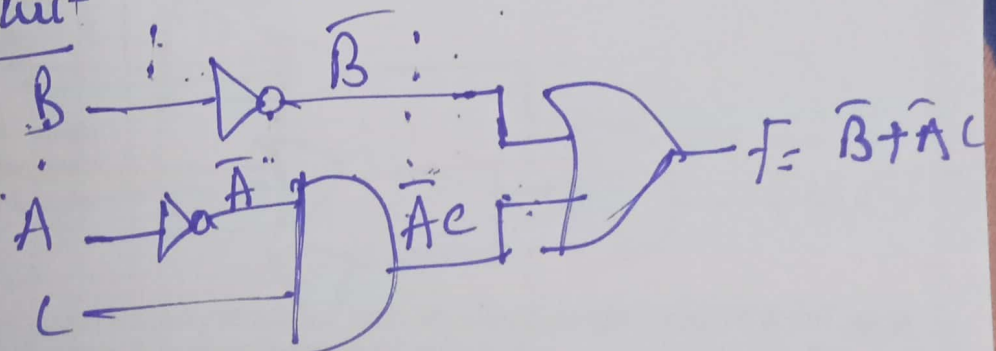
$$\begin{matrix} 000 & 100 \\ (0) & (4) \end{matrix}$$

$$F(A,B,C) = \sum m(0,1,3,4,5)$$



$$F(A,B,C) = \bar{B} + \bar{A}C$$

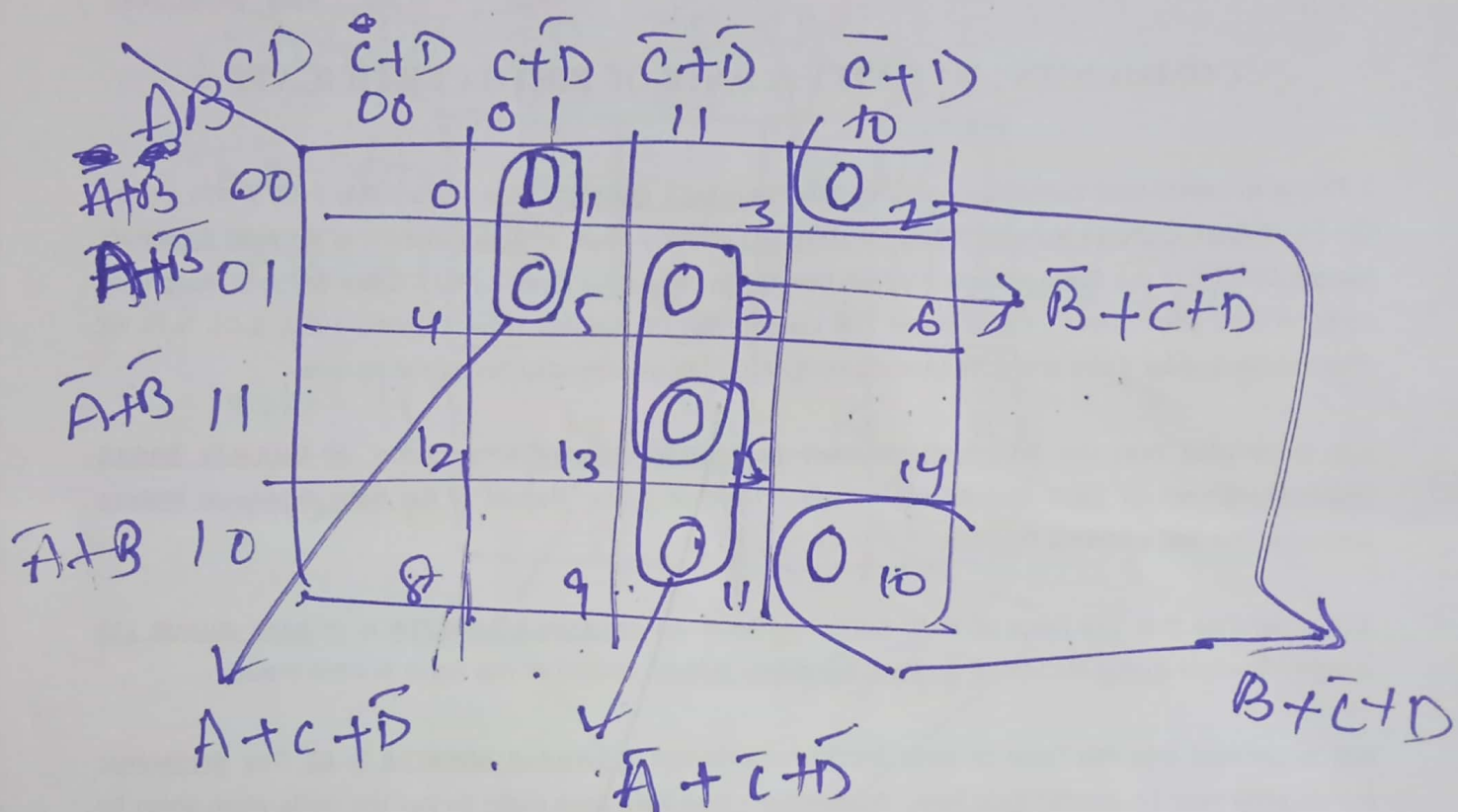
Logic circuit



4. Minimize the given pos using K-map and construct the optimized circuit.

$$F(A, B, C) = \text{TIM}(1, 2, 5, 7, 10, 11, 15)$$

Sol: Given,  $F(A, B, C) = \text{TIM}(1, 2, 5, 7, 10, 11, 15)$



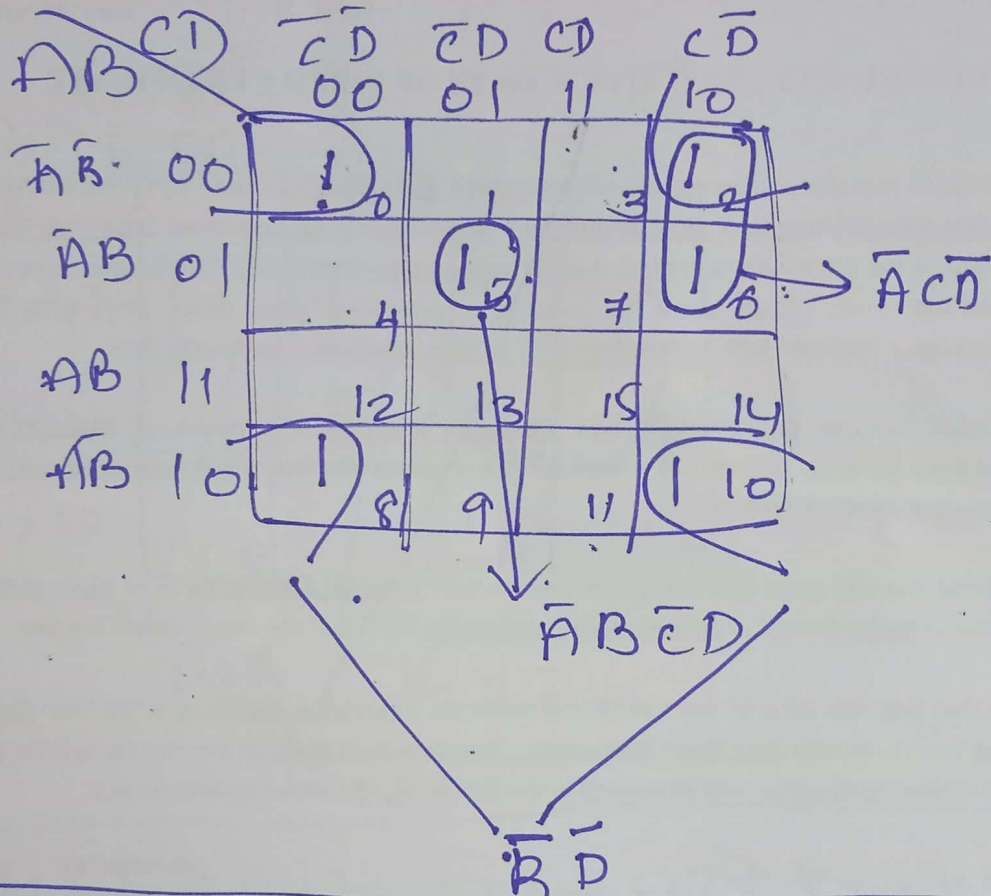
$$f(A, B, C, D) = (A + C + \bar{D})(\bar{A} + C + \bar{D})(B + C + \bar{D}) + B + C + D$$



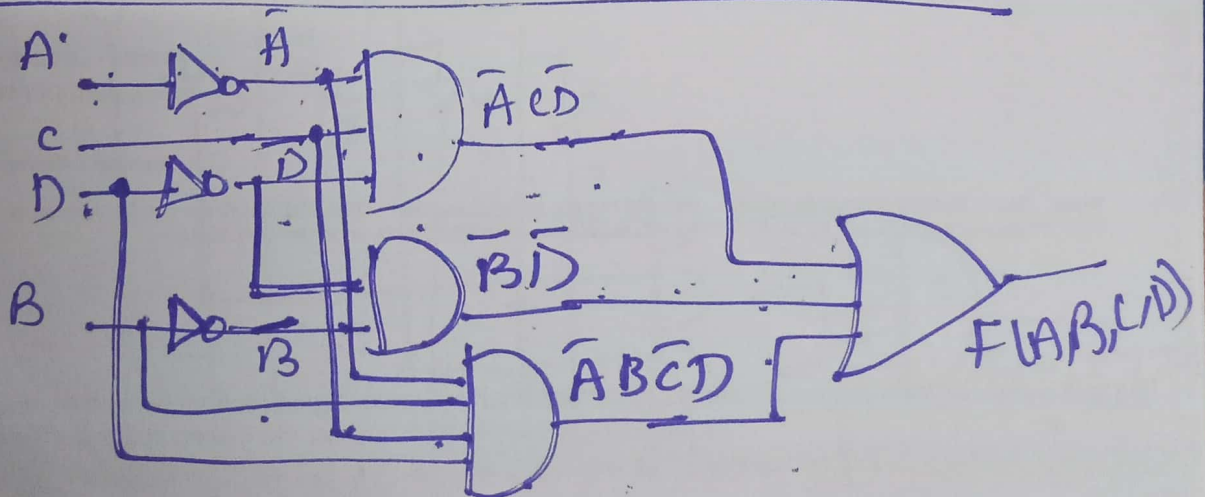
5

5) Minimize the given SOP using K-Map and construct the optimized logic circuit.  $F(A, B, C, D) = \sum m(0, 2, 5, 6, 8, 10)$

Sol: Given,  $F(A, B, C, D) = \sum m(0, 2, 5, 6, 8, 10)$



$$F(A, B, C, D) = \bar{A}C\bar{D} + \bar{A}B\bar{C}D + AB\bar{C}D$$

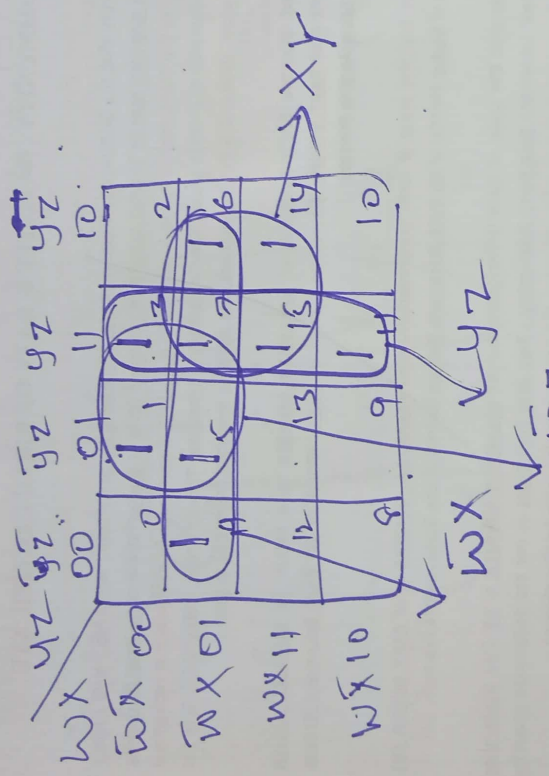


6. Optimize given function using K-map

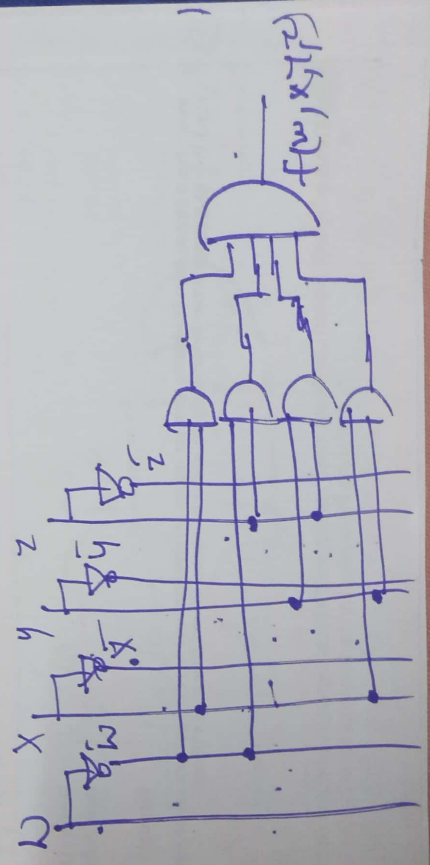
$$F(W, X, Y, Z) = \sum m(1, 3, 4, 5, 6, 7, 11, 14, 15)$$

and implement using logic gates.

Sol: Given,  $F(W, X, Y, Z) = \sum m(1, 3, 4, 5, 6, 7, 11, 14, 15)$



$$F(W, X, Y, Z) = WY + WZ + XZ$$



7

7. Optimize 4-variable function

$$F(w, x, y, z) = \sum m(1, 3, 7, 11, 15) + \sum d(0, 2, 5)$$

using K-maps and realize minimized expression using K-maps.

Sol: Given,  $F(w, x, y, z) = \sum m(1, 3, 7, 11, 15) + \sum d(0, 2, 5)$

$w \backslash yz$	$yz = 00$	$yz = 01$	$yz = 11$	$yz = 10$
$w = 0$	$\bar{w} \bar{x} \bar{y} \bar{z} = 0$	$\bar{w} \bar{x} \bar{y} z = 1$	$\bar{w} \bar{x} y z = 3$	$\bar{w} \bar{x} y \bar{z} = 2$
$w = 1$	$w \bar{x} \bar{y} \bar{z} = 4$	$w \bar{x} \bar{y} z = 5$	$w \bar{x} y z = 7$	$w \bar{x} y \bar{z} = 6$
$w = 1$	$w x \bar{y} \bar{z} = 12$	$w x \bar{y} z = 13$	$w x y z = 15$	$w x y \bar{z} = 14$
$w = 0$	$\bar{w} x \bar{y} \bar{z} = 8$	$\bar{w} x \bar{y} z = 9$	$\bar{w} x y z = 11$	$\bar{w} x y \bar{z} = 10$

$$F(w, x, y, z) = \bar{w} \bar{x} + yz$$

