

Assignment - 11

18K41A0551

Let us consider a sample dataset have one input (x_i) and one output (y_i) and number of samples. Develop a SLR model using normal accelerated gradient (NAG) optimiser.

Sample (i)	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

* Do manual calculations for 2 iterations with 1st 2 samples.

Step 1: $[X, Y], m=1, c=-1, \eta=0.1, \text{epochs}=2,$
 $\gamma=0.9, \downarrow m = \downarrow c = 0, n_s = 2$

Step 2: $\text{itr} = 1$

Step 3: Sample = 1

$$\begin{aligned}\text{Step 4: } g_m &= \frac{dE}{dm} = - (y_i - (m + \downarrow m) x_i - (c + \gamma \downarrow c)) x_i \\ &= - (3.4 - (1 + (0.9) 0) 0.2 - (-1 + (0.9) 0) 0.2) \\ &= -0.84.\end{aligned}$$

$$g_c = -\frac{dE}{dc} = -(y_i - (m + \eta V_m) x_i - (c + \eta c))$$

$$= -(3.4 - (1 + 0.9) \times 0) 0.2$$

$$= -(-1 + (0.9) \times 0)$$

$$g_c = -4.2$$

Step 5 : $V_m = \eta V_m - \eta g_m$

$$= (0.9) 0 - (-0.1) (-0.84)$$

$$= -0.084$$

$$V_c = \eta V_c - \eta g_c$$

$$= (0.9) 0 - (-0.1) (-4.2)$$

$$= -0.42$$

Step 6 : $m = m + V_m = 1 - 0.084 = 0.916$

$$c = c + V_c = -1 - 0.42 = -1.42$$

Step 7 : sample + 1 = 2

Step 8 : if (sample > n_s)

do step 9.

else

step 4

Step 4 : $g_m = \frac{dE}{dm} = -\left(3.8 - (0.916 + (0.9 \times -0.084))\right)$

$$(0.4 - (-1.42 + (0.98 - 0.084) \times 0.4))$$

$$= -1.983$$

$$g_c = \frac{dE}{dc} = -4.939$$

Step 5 : $V_m = fV_m - \eta g_m$

$$= (0.9 \times (-0.054)) - (-0.1 \times -1.933)$$

$$= -0.2739$$

$$V_c = (0.9 \times -0.42) - (-0.1 \times -4.939)$$

$$= 0.8729$$

Step 6 : $m+ = V_m$

$$= 0.916 - 0.2739$$

$$= 0.6421$$

$$c+ = V_c$$

$$= -1.42 - 0.8739$$

$$= -2.2939$$

Step 7 : Sample + = 1

$$i+1 = 3$$

Step 8 : if (Sample $\geq n_s$)

goto step 11

else goto step 3 ✓

Step 3 : Sample = 1

Step 4 : $g_m = \frac{dE}{dm} = - (2.8 - (2.2939 + (0.9 \times -1.32)))$

$$= 2.04 - (-2.6646 + (0.9))$$

$$= -2.985$$

$$g_c = \frac{dE}{dc} = -2.4645$$

$$\text{step 5 : } v_m = [0.1 * -0.3627] - [-0.1 * -2.985] \\ = -0.6249$$

$$v_c = [0.9 * -1.3707] - [0.1 * 2.6845] \\ = -1.9800$$

$$\text{step 6 : } m + = v_m \\ = 0.2974 + (-0.6249) \\ = -0.3275$$

$$c + = v_c \\ = -3.6646 + 1.9800 \\ = -4.6446$$

step 7 : Sample $t+1$ \Rightarrow
 $2+1=3$

step 8 : if (sample $> n_s$)
 goto step 9. ✓
 else goto step 4 :

step 9 : its $+= 1$
 $2+1=3$

step 10 : if (its $> \text{epochs}$)
 goto step 4
 else goto step -3

Step 11 : print m, c
 $m = 0.3275, c = -4.6446$