

Optimal Binary Search Tree

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#include <iostream>
#include <algorithm>
#include <vector>
#define LL long long int
using namespace std;
typedef vector<long long> vi;
typedef vector< vector<long long> > vii;
const LL inf = 1LL << 60;

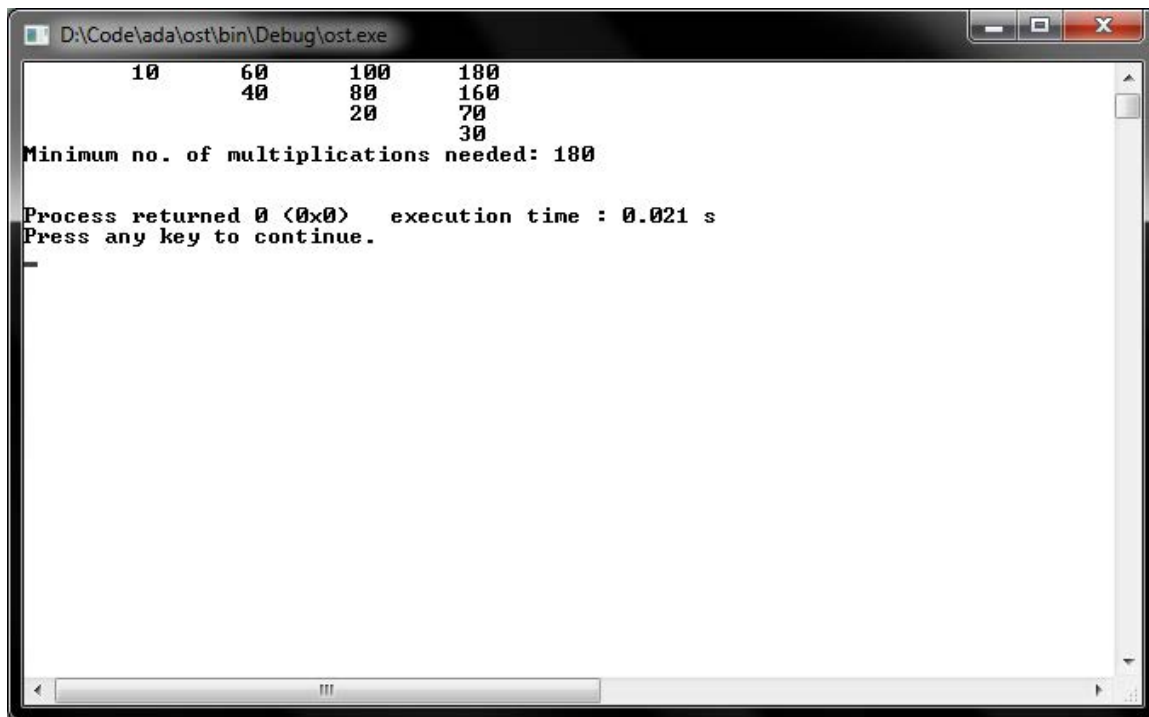
void print(vii M) {...}

LL OST(vi& V) {
    vii M(V.size()+1,vi(V.size()+1,inf)), S(V.size()+1,vi(V.size()+1,0));
    LL n = V.size()+1;
    for(LL i=1; i<n; i++) {
        M[i][i] = V[i-1];
        S[i][i] = V[i-1];
    }
    for(LL i=1; i<n; i++) {
        for(LL j=i+1; j<n; j++) {
            S[i][j] = S[i][j-1] + V[j-1];
        }
    }

    for(LL l=1; l<=n; l++) { //No of matrices to be multiplied, i.e range of j
        LL depth = n-l; //Range till which i will go
        for(LL i=1; i<depth; i++) {
            LL j=i+l;
            for(LL k=i; k<=j; k++) {
                M[i][j] = min(M[i][j], (k<=i ? 0:M[i][k-1]) + (k>=j ? 0:M[k+1][j]) + S[i][j]);
            }
        }
    }
    print(M);
    return M[1][n-1];
}

int main() {
    vi V = {10,40,20,30};
    cout<<"Minimum no. of multiplications needed: "<<OST(V)<<"\n\n";
    return 0;
}
```

Output:



```
D:\Code\ada\ost\bin\Debug\ost.exe

  10    60   100   180
    40    80   160
      20    70
        30
Minimum no. of multiplications needed: 180
Process returned 0 (0x0) execution time : 0.021 s
Press any key to continue.
```