

Artificial Intelligence  
[week #4]  
**Local Search**

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# Finding solution with search

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- **classical search:**

- Design to explore search space sistematically
- observable, deterministic, known environments
- the solution is a sequence of actions.

- **What if:**

- $10^{10000}$  state
- state space initially unknown
- Partially observe
- cannot predict exactly what percept it will receive

# Local Search

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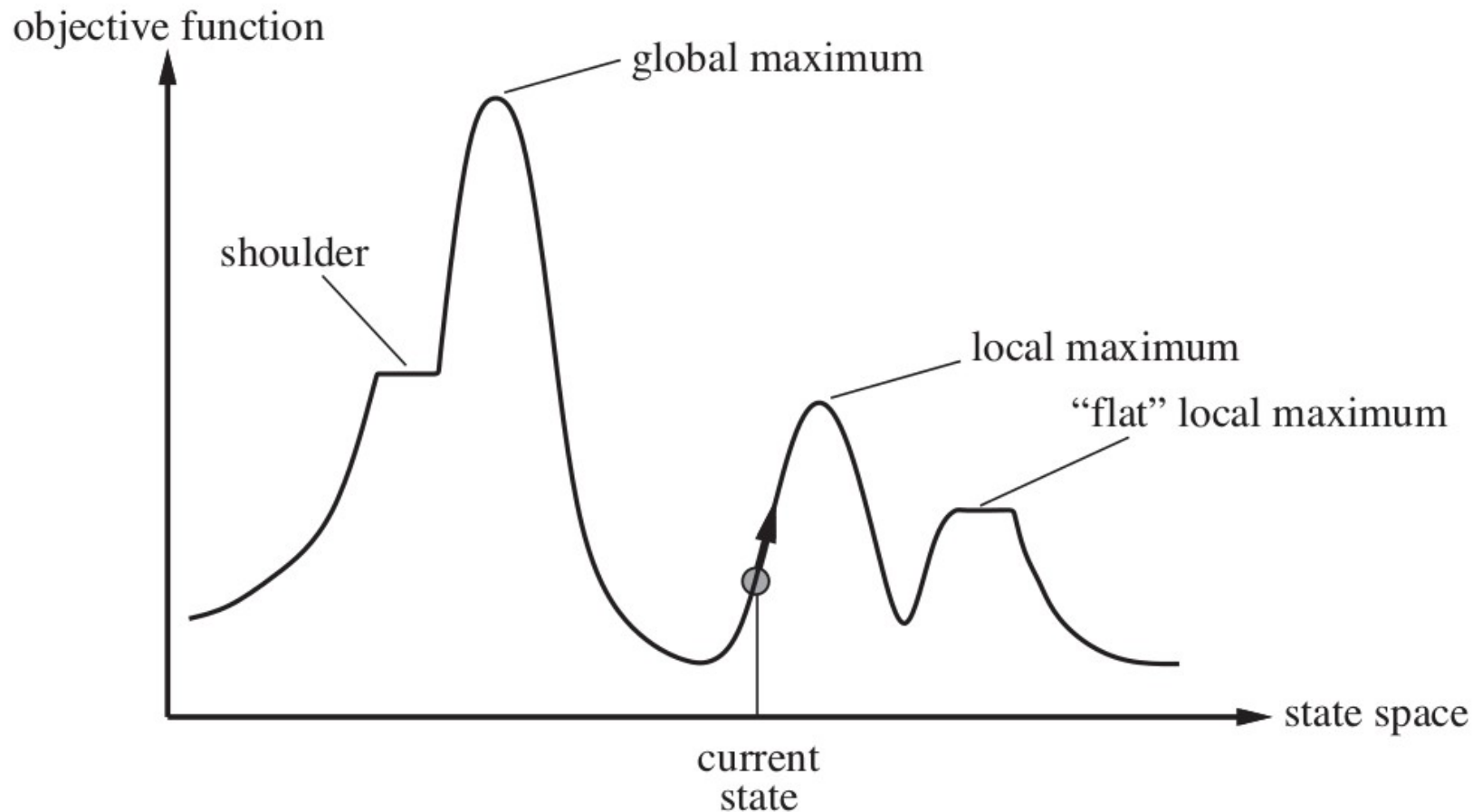
- Evaluating and **modifying** one or more **current states**
- Rather than systematically exploring paths from an initial state
- Suitable for problems in which all that matters is the **solution state**
- Not the **path cost** to reach it (remember n-queens problem?)

# Local Search

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- Operate using a **single current node** (rather than multiple paths)
- Although local search algorithms are not systematic, they have two key advantages:
  - 1) use very **little memory**
  - 2) can often find reasonable solutions in **large** or infinite (continuous) **state spaces** for which systematic algorithms are unsuitable.
- Useful for solving pure **optimization problems**
  - **find the best state according to an objective function**

# Finding Maximum



# Hill-climbing Search

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- Simply a loop that continually moves in the direction of increasing value—that is, uphill.
- Terminates when it reaches a “peak” where no neighbor has a higher value.
- Does not maintain a search tree, only record the state and the value of the objective function
- Does not look ahead beyond the immediate neighbors of the current state.
  - Trying to find the top of Mount Everest in a thick fog while suffering from amnesia.

# Hill-climbing Search

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**function** HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

*current*  $\leftarrow$  MAKE-NODE(*problem*.INITIAL-STATE)

**loop do**

*neighbor*  $\leftarrow$  a highest-valued successor of *current*

**if** *neighbor*.VALUE  $\leq$  *current*.VALUE **then return** *current*.STATE

*current*  $\leftarrow$  *neighbor*

# Hill-climbing Search

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- Sometimes called greedy local search
  - grabs a good neighbor state without thinking ahead about where to go next.
- makes rapid progress toward a solution because it is usually quite easy to improve a bad state.
- Unfortunately, hill climbing often gets stuck by:
  - Local maxima
  - Ridges
  - Plateaux



# N-queens problem

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- Starting from a randomly generated 8-queens state, steepest-ascent hill climbing **gets stuck 86%** of the time.
- Solving **only 14%** of problem instances.
- It works **quickly**, taking just **4 steps** on average when it succeeds and **3** when it gets stuck—not bad for a state space with  $8^8 \approx 17$  million states.

# Overcome problems

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- Enable sideways moves (overcome plateau)
- Allow up to, 100 consecutive sideways moves in the 8-queens problem. This raises the percentage from 14% to 94%
- Success comes at a cost: the algorithm averages roughly 21 steps for each successful instance and 64 for each failure.

# Hill-climbing variation

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- **Stochastic hill-climbing:** chooses at random from among the uphill moves
- **First-choice hill climbing:** implements stochastic hill climbing by generating successors randomly until one is generated that is better than the current state.
- **Random-restart hill-climbing:** adopts the well-known adage, “If at first you don’t succeed, try, try again.” It conducts a series of hill-climbing searches from randomly generated initial states

# Simulated annealing

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- A hill-climbing algorithm that **never makes “downhill”** moves toward states with lower value (or higher cost) **is guaranteed to be incomplete**, because it can get stuck on a local maximum.
  - In contrast, a purely random walk—that is, moving to a successor chosen uniformly at random from the set of successors—is **complete** but **extremely inefficient**.
  - Therefore, it seems reasonable to try to **combine hill climbing with a random walk** in some way that yields both efficiency and completeness.
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# Simulated Annealing

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**function** SIMULATED-ANNEALING(*problem*, *schedule*) **returns** a solution state

**inputs:** *problem*, a problem

*schedule*, a mapping from time to “temperature”

*current*  $\leftarrow$  MAKE-NODE(*problem*.INITIAL-STATE)

**for**  $t = 1$  **to**  $\infty$  **do**

$T \leftarrow \text{schedule}(t)$

**if**  $T = 0$  **then return** *current*

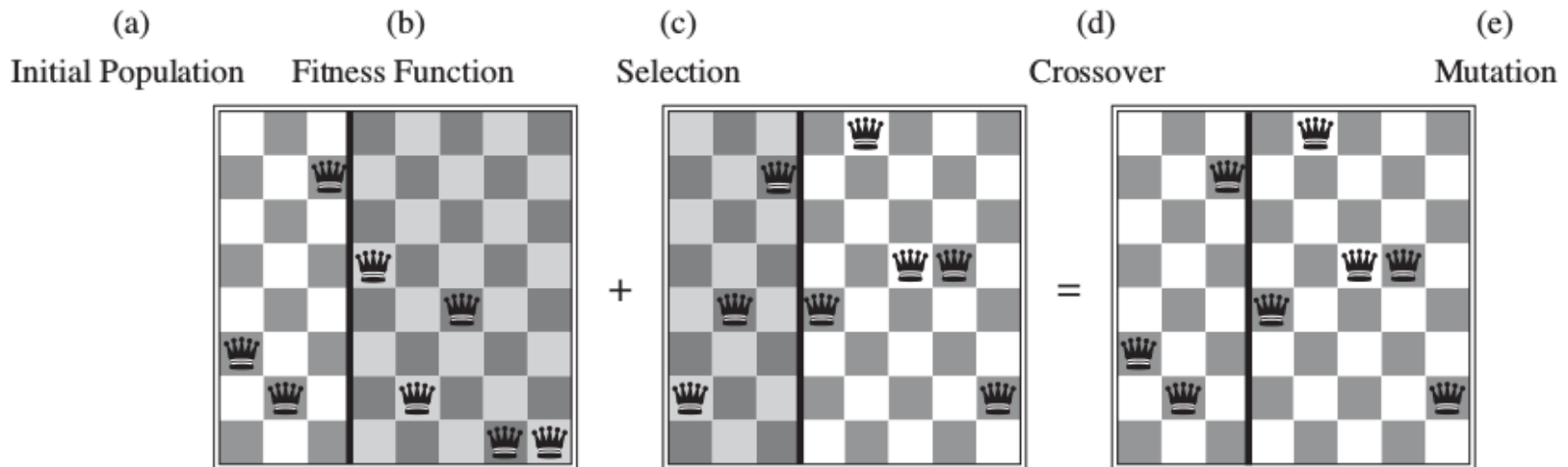
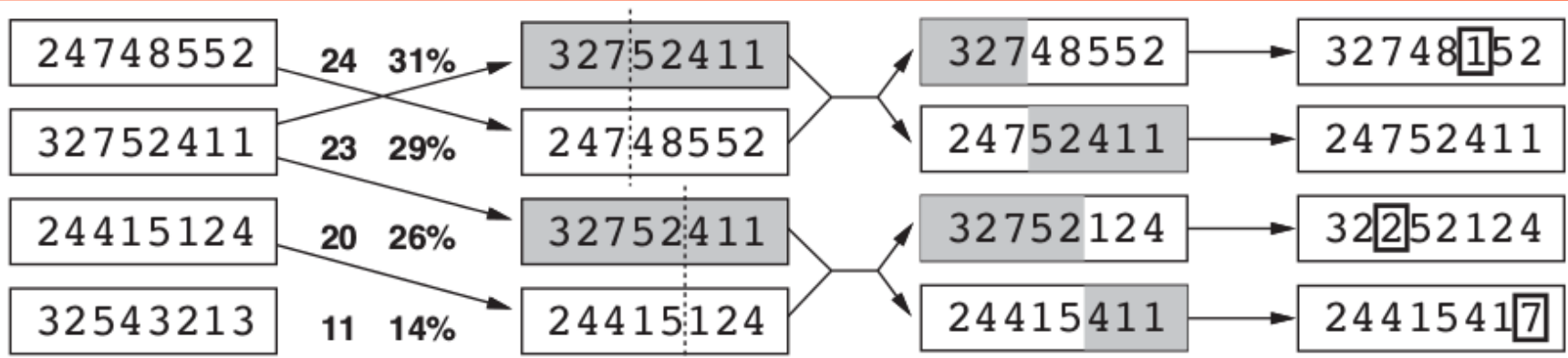
*next*  $\leftarrow$  a randomly selected successor of *current*

$\Delta E \leftarrow \text{next.VALUE} - \text{current.VALUE}$

**if**  $\Delta E > 0$  **then** *current*  $\leftarrow$  *next*

**else** *current*  $\leftarrow$  *next* only with probability  $e^{\Delta E/T}$

# Genetic algorithms



# Genetic algorithms

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**function** GENETIC-ALGORITHM(*population*, FITNESS-FN) **returns** an individual

**inputs:** *population*, a set of individuals

FITNESS-FN, a function that measures the fitness of an individual

**repeat**

*new\_population*  $\leftarrow$  empty set

**for**  $i = 1$  **to** SIZE(*population*) **do**

$x \leftarrow$  RANDOM-SELECTION(*population*, FITNESS-FN)

$y \leftarrow$  RANDOM-SELECTION(*population*, FITNESS-FN)

*child*  $\leftarrow$  REPRODUCE( $x, y$ )

**if** (small random probability) **then** *child*  $\leftarrow$  MUTATE(*child*)

add *child* to *new\_population*

*population*  $\leftarrow$  *new\_population*

**until** some individual is fit enough, or enough time has elapsed

**return** the best individual in *population*, according to FITNESS-FN

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**function** REPRODUCE( $x, y$ ) **returns** an individual

**inputs:**  $x, y$ , parent individuals

$n \leftarrow$  LENGTH( $x$ );  $c \leftarrow$  random number from 1 to  $n$

**return** APPEND(SUBSTRING( $x, 1, c$ ), SUBSTRING( $y, c + 1, n$ ))

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