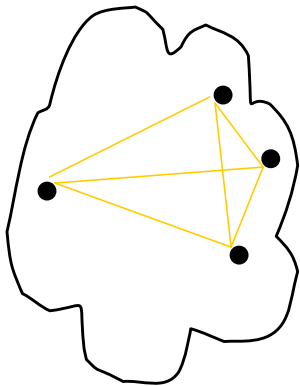


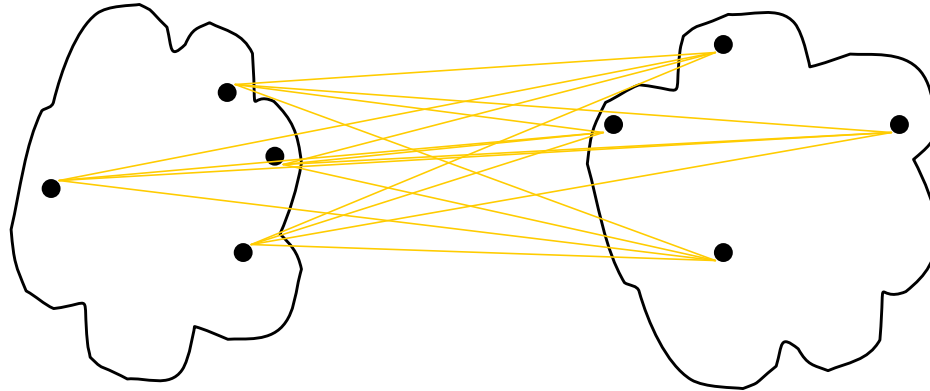
# Silhouette coefficient

[Kaufman&Rousseeuw, 1990]

- **Cohesion:** measures how close objects are in a cluster
- **Separation:** measure how separated the clusters are



cohesion



separation

# Silhouette coefficient

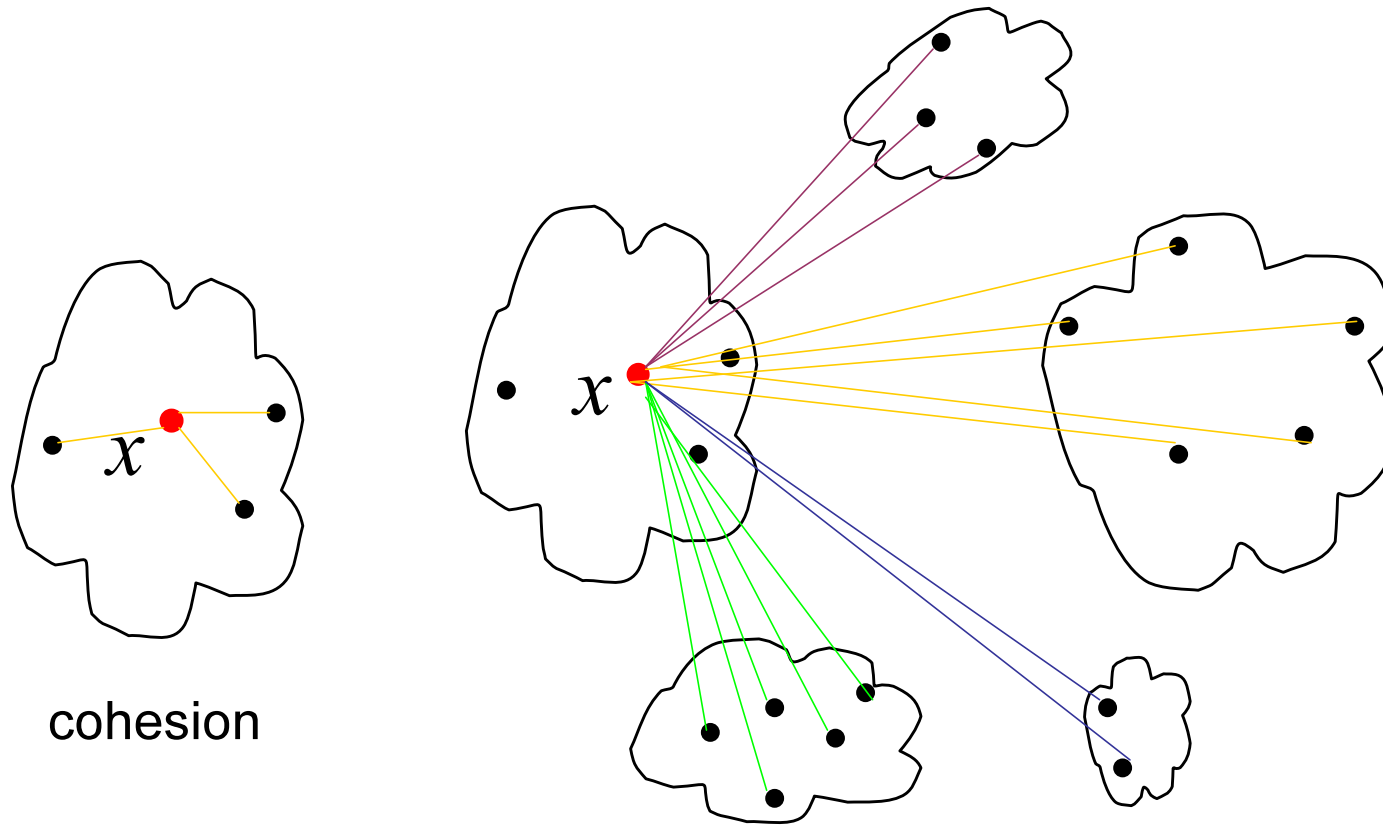
- *Cohesion*  $a(x)$ : average distance of  $x$  to all other vectors in the same cluster.
- *Separation*  $b(x)$ : average distance of  $x$  to the vectors in other clusters. Find the minimum among the clusters.
- *silhouette*  $s(x)$ :

$$s(x) = \frac{b(x) - a(x)}{\max\{a(x), b(x)\}}$$

- $s(x) = [-1, +1]$ : -1=bad, 0=indifferent, 1=good
- Silhouette coefficient (SC):

$$SC = \frac{1}{N} \sum_{i=1}^N s(x)$$

# Silhouette coefficient (SC)



cohesion

$a(x)$ : average distance  
in the cluster

separation

$b(x)$ : average distances to  
others clusters, find minimal