

Defaults

Frames offer a simple form of *default reasoning*, where a slot has a certain value by inheritance unless another one is explicitly given.

Assuming that we have $\text{Dog}(\text{fido})$ in a KB in FOL, there are only two ways to reach the conclusion $\text{Carnivore}(\text{fido})$:

1. This is explicitly mentioned in KB;
2. In KB we have the universal form $\forall x. \text{Dog}(x) \supset \text{Carnivore}(x)$.

We are interested in expressing in FOL what we know about something in general and in particular using universals.

These slides are mainly based on Ronald J. Brachman, Hector J. Levesque. Knowledge representation and reasoning, Morgan Kaufmann, 2004.

See also Ch. 12.6 – Reasoning with default information - Stuart J. Russell, Peter Norvig. Artificial Intelligence – a modern approach, 3rd edition, Pearson, 2010.

Defaults

For example, we may say that “Bikes have two wheels” but without stating that “All bikes have two wheels” because this would rule out a bike with three wheels.

A possible solution would be to say

“All bikes that are not P_1 or ...or P_n have two wheels”,

where P_i represent the exceptional cases. The challenge here is to characterize these cases.

We would like to make a distinction between universals that hold for all instances and generics that hold in general.

Much of our knowledge about the world is generic, therefore it is important to formalize it.

Defaults

Default reasoning

In general, we know that dogs are carnivores. If Fido is a dog, what are the appropriate circumstances to infer that Fido is a carnivore? We can reason as following:

Given that a P is generally a Q and knowing that $P(a)$ is true, it is reasonable to conclude that $Q(a)$ is true unless there is a good reason not to.

If all that we know about an individual is that it is an instance of P , then there is no reason not to conclude that it is an instance of Q .

For example, if we know that a polar bear has been playing in the mud, probably we do not want to conclude anything about its color. But if all we know is that it is a polar bear, then it is reasonable to conclude that it is white. The conclusion has no guarantee to be logically correct, it is only a reasonable default.

Defaults

This form of reasoning that involves general (not universal) knowledge about a particular individual, is called default reasoning.

Examples of situations when we want to conclude $Q(a)$ given $P(a)$:

- general statements: Children love playing.

 - Oranges are orange.

 - People in a long queue become impatient.

- lack of information to the contrary:

 - No country has a president taller than 2m.

 - Children learn easily foreign languages.

- conventions: The speed limit in a city.

 - The closest shop is five minute walk (by default assume that it is open).

- persistance: Marital status.

 - The size of objects.

The list of objects is not exhaustive, but it suggests the great variety of sources of default information. Our focus is to describe exactly when it is appropriate to draw a default conclusion, in the absence of universals.

Defaults

Nonmonotonicity

Ordinary deductive reasoning is monotonic, meaning that new facts produce only additional beliefs. If $KB_1 \models \alpha$ then $KB_2 \models \alpha$ for any KB_2 such that $KB_1 \subseteq KB_2$.

Default reasoning is nonmonotonic, meaning that sometimes new facts invalidate previous beliefs. For example, we believe by default that a bird flies, but if we find that the bird is an ostrich, we reconsider our belief.

Defaults

I. Closed-world reasoning

It is the simplest formalization of default reasoning. A finite vocabulary of predicate and constant symbols is used to represent facts about the world. But from all the valid atomic sentences, only a small fraction of them are expected to be true. The convention here is to explicitly represent the true atomic sentences and to assume that any unmentioned one is false.

Example:

DirectConnect(cleveland, toronto)

DirectConnect(toronto, chicago)

DirectConnect(cleveland, vancouver)

If a flight between two cities is not listed, then there is none. The closed-world assumption (CWA) is the following:

Unless an atomic sentence is known to be true, it can be assumed to be false.

Obs. A sentence assumed to be false can be later determined to be true.

Defaults

Def. $KB^+ = KB \cup \{\neg p \mid p \text{ is atomic and } KB \not\models p\}$. A new form of entailment is defined as following:

$$KB \models_c \alpha \text{ iff } KB^+ \models \alpha$$

In the previous example, KB^+ would include sentences of the form $\neg \text{DirectConnect}(c_1, c_2)$.

Consistency and completeness of knowledge

Def. A KB exhibits consistent knowledge iff there is no sentence α such that both α and $\neg\alpha$ are known.

Def. A KB exhibits complete knowledge iff for every sentence α , either α or $\neg\alpha$ is known.

Defaults

Knowledge can be incomplete. For example, if $KB = \{(p \vee q)\}$, neither p nor $\neg p$ can be entailed from KB .

But with the CWA, the entailment relation is complete. For any sentence α , it holds that either $KB \models_c \alpha$ or $KB \models_c \neg \alpha$ (demonstration is by induction on the length of α).

Under CWA, whenever $KB \not\models p$ then either $KB \models_c \neg p$ directly or $\neg p$ is conceptually added to the KB . That means that we act as if KB represents completely knowledge.

Defaults

Query evaluation

The question $KB \models_c \alpha$ reduces to questions about the literals in α :

1. $KB \models (\alpha \wedge \beta)$ iff $KB \models \alpha$ and $KB \models \beta$
2. $KB \models \neg \neg \alpha$ iff $KB \models \alpha$
3. $KB \models \neg (\alpha \vee \beta)$ iff $KB \models \neg \alpha$ and $KB \models \neg \beta$
4. $KB \models_c (\alpha \vee \beta)$ iff $KB \models_c \alpha$ or $KB \models_c \beta$
5. $KB \models_c \neg (\alpha \wedge \beta)$ iff $KB \models_c \neg \alpha$ or $KB \models_c \neg \beta$
6. If KB^+ is consistent then $KB \models_c \neg \alpha$ iff $KB \not\models_c \alpha$

For example, $KB \models_c ((p \wedge q) \vee \neg (r \wedge \neg s))$ reduces to either both $KB \models_c p$ and $KB \models_c q$, or $KB \models_c \neg r$, or $KB \models_c s$.

Defaults

Consistency and Generalized Closed-World Assumption (GCWA)

A consistent KB does not imply that KB^+ is also consistent. For example, if $KB = \{(p \vee q)\}$ then KB^+ contains $\{(p \vee q), \neg p, \neg q\}$ because $KB \not\models p$ and $KB \not\models q$. So, KB^+ is not consistent.

Obs. If a KB consists of just atomic sentences (e.g. DirectConnect) or conjunctions of atomic sentences (e.g., $p \wedge q$) or disjunctions of negative literals (e.g., $\neg p \vee \neg q$), then KB^+ is consistent.

One way to preserve consistency is to restrict the application of CWA only to atom that are “uncontroversial” (not like p and q in the example above).

Def. The generalized closed-world assumption is

$$KB^* = KB \cup \{\neg p \mid p \text{ is atomic, } KB \not\models p \text{ and for all collections of atoms } q_1, \dots, q_n, \\ \text{if } KB \models (p \vee q_1 \vee \dots \vee q_n) \text{ then } KB \models (q_1 \vee \dots \vee q_n)\}.$$

Defaults

The entailment in GCWA is defined as following:

$$KB \models_{GC} \alpha \text{ iff } KB^* \models_c \alpha$$

Under GCWA, we will not assume that p is false if there is an entailed disjunction of atoms including p that cannot be reduced to a smaller entailed disjunction not involving p .

For example, if $KB = \{(p \vee q)\}$ then $KB \models (p \vee q)$ but $KB \not\models q$, so $\neg p \notin KB^*$ and similarly $\neg q \notin KB^*$.

Now, with the same $KB = \{(p \vee q)\}$ if we consider an atom r (meaning that $KB \not\models r$), then $\neg r \in KB^*$ because $KB \models (r \vee p \vee q)$ and $KB \models (p \vee q)$.

Defaults

An example of interpretation: we know that there is a direct flight from Cleveland to Dallas or Houston and we don't know about any flight from Cleveland to Austin. As a result, we know that there is a direct flight from Cleveland to Dallas or Houston or Austin.

But because there is a flight to one of the first two cities, under GCWA we will assume that there is no flight to Austin.

$KB \models (\text{DirectConnect}(\text{cleveland}, \text{dallas}) \vee \text{DirectConnect}(\text{cleveland}, \text{houston}))$

\Rightarrow

$KB \models (\text{DirectConnect}(\text{cleveland}, \text{dallas}) \vee \text{DirectConnect}(\text{cleveland}, \text{houston}) \vee \text{DirectConnect}(\text{cleveland}, \text{austin}))$

$\Rightarrow \neg \text{DirectConnect}(\text{cleveland}, \text{austin}) \in KB^*$.

Defaults

Entailments in GCWA are a subset of those in CWA, that is if $\neg p \in KB^*$ then $\neg p \in KB^+$.

If KB has no disjunctive knowledge, then GCWA and CWA are in complete agreement.

Prop. If KB is consistent, then KB^* is consistent.

GCWA is a weaker version of CWA that agrees with CWA in the absence of disjunctions, but remains consistent in the presence of disjunctions.

Defaults

Quantifiers and Domain Closure

Let us assume that the representation language contains the predicate `DirectConnect` and the constants c_1, \dots, c_n and another `smallTown`.

If KB contains only atomic sentences of the form `DirectConnect(c_i, c_j)`, then for any pair of constants c_i and c_j either `DirectConnect(c_i, c_j)` or $\neg \text{DirectConnect}(c_i, c_j)$ is in KB^+ .

Also, $\neg \text{DirectConnect}(c_j, \text{smallTown})$ is in KB^+ for every c_j

If we consider the query $\neg \exists x \text{DirectConnect}(x, \text{smallTown})$, under CWA neither this query nor its negation is entailed. CWA excludes any of the named cities c_1, \dots, c_n flying to `SmallTown`, but it does not exclude other unnamed city doing so.

The easiest way to overcome this problem is to assume that the named constants are the only individuals of interest.

Defaults

Def. The closed-world assumption with domain-closure is

$$KB^\diamond = KB^+ \cup \{\forall x.[x=c_1 \vee \dots \vee x=c_n]\},$$

where c_1, \dots, c_n are all the constant symbols appearing in KB. The entailment in CWA with domain-closure is defined as following:

$$KB \models_{CD} \alpha \text{ iff } KB^\diamond \models \alpha .$$

The main properties are:

$$KB \models_{CD} \forall x.\alpha \text{ iff } KB \models_{CD} \alpha_c^x \text{ for every constant } c \text{ appearing in KB.}$$

$$KB \models_{CD} \exists x.\alpha \text{ iff } KB \models_{CD} \alpha_c^x \text{ for some constant } c \text{ appearing in KB.}$$

Compared to CWA, in KB^\diamond we make the additional assumption that no other objects exist apart from the named constants.

Now, under CWA with domain-closure, our query

$$\neg \exists x \text{DirectConnect}(x, \text{smallTown})$$

is entailed.

Obs. It is the case that $KB \models_{CD} \alpha$ or $KB \models_{CD} \neg \alpha$ for any α (with or without quantifiers).

Defaults

II. Circumscription

One way to express exceptional cases where a default should not apply is by using a predicate Ab (from abnormal):

$$\forall x.[\text{Bird}(x) \wedge \neg \text{Ab}(x) \supset \text{Flies}(x)].$$

Assuming that in KB we have the additional facts:

Bird(chilly)

Bird(tweety)

(tweety ≠ chilly)

$\neg \text{Flies}(\text{chilly})$

we would like to conclude that Tweety flies, whereas Chilly does not.

But $\text{KB} \not\models \text{Flies}(\text{tweety})$ because there are interpretations that satisfy KB where $\text{Flies}(\text{tweety})$ is false. In these interpretations, the denotation of Tweety is included in the interpretation of Ab.

Defaults

The strategy for minimizing abnormality: we consider the interpretations of the KB where the interpretation of Ab is (a set) as small as possible.

The default conclusions are true in models of the KB where as few of the individuals as possible are abnormal.

In the previous example, we know that Chilly is an abnormal bird, but we don't know anything about Tweety. The interpretation of Ab must include Chilly, but excludes Tweety (because nothing dictates otherwise). This technique is called circumscribing the predicate Ab.

In general, a family of predicates Ab_i is used to describe various aspects of individuals. Chilly may be in the interpretation of Ab_1 , but not in that of Ab_2 and so on.

Defaults

Minimal entailment

A new form of entailment is characterized in terms of properties of interpretations.

Let P be a fixed set of unary predicates Ab . Let $\mathcal{I}_1 = \langle D, I_1 \rangle$ and $\mathcal{I}_2 = \langle D, I_2 \rangle$ be interpretations over the same domain such that every constant and function is interpreted the same.

We define the relationship \leq as following:

$$\mathcal{I}_1 \leq \mathcal{I}_2 \text{ iff for every } Pr \in P \text{ then } I_1[Pr] \subseteq I_2[Pr].$$

We say that $\mathcal{I}_1 < \mathcal{I}_2$ iff $\mathcal{I}_1 \leq \mathcal{I}_2$ and $\mathcal{I}_2 \not\leq \mathcal{I}_1$.

\mathcal{I}_1 makes the interpretation of all Ab predicates smaller than \mathcal{I}_2 . In other words, \mathcal{I}_1 is more normal than \mathcal{I}_2 .

Defaults

Def. The minimal entailment \models_{\leq} is defined as follows:

$KB \models_{\leq} \alpha$ iff for every interpretation \mathcal{I} such that $\mathcal{I} \models KB$, either $\mathcal{I} \models \alpha$ or there is an \mathcal{I}' such that $\mathcal{I}' < \mathcal{I}$ and $\mathcal{I}' \models KB$.

In our example,

$\forall x.[\text{Bird}(x) \wedge \neg \text{Ab}(x) \supset \text{Flies}(x)]$

$\text{Bird}(\text{chilly})$

$\text{Bird}(\text{tweety})$

$(\text{tweety} \neq \text{chilly})$

$\neg \text{Flies}(\text{chilly})$

we have that $KB \not\models \text{Flies}(\text{tweety})$ but $KB \models_{\leq} \text{Flies}(\text{tweety})$.

If $\mathcal{I} \models KB$ but $\mathcal{I} \not\models \text{Flies}(\text{tweety})$ then $\mathcal{I} \models \text{Ab}(\text{tweety})$.

We take \mathcal{I}' to be exactly \mathcal{I} , except that we remove the denotation of tweety from the interpretation of Ab.

Defaults

Assuming that $P=\{Ab\}$, we have that $\mathcal{J}' < \mathcal{J}$ and $\mathcal{J}' \models KB$.

But $\mathcal{J}' \not\models Ab(tweety)$, so $\mathcal{J}' \models Flies(tweety)$.

Thus, in the minimal models of KB, Tweety is a normal bird that flies

$$KB \models_{\leq} \neg Ab(tweety)$$

$$KB \models_{\leq} Flies(tweety).$$

Instead, in all the models of KB, Chilly is an abnormal bird.

In this reasoning, the only default step was to conclude that Tweety was a normal bird; the rest was ordinary deductive reasoning.

Obs. The “most normal” models of the KB may not all satisfy exactly the same sentences.

Defaults

For example, suppose that the KB contains:

$\text{Bird}(c)$

$\text{Bird}(d)$

$\neg\text{Flies}(c) \vee \neg\text{Flies}(d)$

$\forall x. [\text{Bird}(x) \wedge \neg\text{Ab}(x) \supset \text{Flies}(x)]$.

In any model of the KB, the interpretation of Ab must contain either the denotation of c or the denotation of d. Any model containing other abnormal individuals would not be minimal (e.g., the model including both c and d).

So, in any minimal model $\mathcal{I} \models \text{KB}$, we have either $\mathcal{I} \models \text{Ab}(c)$ or $\mathcal{I} \models \text{Ab}(d)$.

If $\mathcal{I} \models \text{Ab}(c)$ then $\text{KB} \not\models \text{Flies}(c)$ and thus $\text{KB} \not\models_{\leq} \text{Flies}(c)$. Similarly, if $\mathcal{I} \models \text{Ab}(d)$ then $\text{KB} \not\models_{\leq} \text{Flies}(d)$.

We cannot conclude by default that c is a normal bird, nor that d is. But we can conclude by default that one of them is:

$\text{KB} \models_{\leq} \text{Flies}(c) \vee \text{Flies}(d)$

Defaults

Obs. CWA and GCWA have a different behavior.

$$\left[\begin{array}{l} \text{KB}^+ = \text{KB} \cup \{\neg p \mid p \text{ is atomic and } \text{KB} \not\models p\} \\ \text{KB}^* = \text{KB} \cup \{\neg p \mid p \text{ is atomic, } \text{KB} \not\models p \text{ and for every collections of atoms } q_1, \dots, q_n \text{ such that} \\ \text{KB} \models (p \vee q_1 \vee \dots \vee q_n) \text{ then } \text{KB} \models (q_1 \vee \dots \vee q_n)\}. \end{array} \right.$$

Because neither $\text{KB} \models \text{Ab}(c)$ nor $\text{KB} \models \text{Ab}(d)$, it results that

$$\text{KB}^+ \supset \text{KB} \cup \{\neg \text{Ab}(c), \neg \text{Ab}(d)\}.$$

So, $\text{KB} \models_c (\text{Flies}(c) \wedge \text{Flies}(d))$, that is KB^+ is not consistent.

On the other hand, under GCWA, $\neg \text{Ab}(c) \notin \text{KB}^*$ and $\neg \text{Ab}(d) \notin \text{KB}^*$.

$$[\text{KB} \models \text{Ab}(c) \vee \text{Flies}(c) \text{ but } \text{KB} \not\models \text{Flies}(c)]$$

So, under GCWA we cannot conclude anything about $\text{Flies}(c)$ or $\text{Flies}(d)$ (or their disjunction).

Defaults

In the circumscription case, one model of the KB is preferred to another one if it has less abnormal individuals.

Assuming that we have the statements: Richard Nixon was both quaker (thus implicitly pacifist) and republican (thus implicitly not pacifist), we have the following KB:

$\text{Republican}(\text{nixon}) \wedge \text{Quaker}(\text{nixon})$

$\forall x. [\text{Republican}(x) \wedge \neg \text{Ab}_2(x) \supset \neg \text{Pacifist}(x)]$

$\forall x. [\text{Quaker}(x) \wedge \neg \text{Ab}_3(x) \supset \text{Pacifist}(x)]$

Defaults

In the circumscription case, one model of the KB is preferred to another one if it has less abnormal individuals.

Assuming that we have the statements: Richard Nixon was both quaker (thus implicitly pacifist) and republican (thus implicitly not pacifist), we have the following KB:

$$\text{Republican}(\text{nixon}) \wedge \text{Quaker}(\text{nixon})$$
$$\forall x. [\text{Republican}(x) \wedge \neg \text{Ab}_2(x) \supset \neg \text{Pacifist}(x)]$$
$$\forall x. [\text{Quaker}(x) \wedge \neg \text{Ab}_3(x) \supset \text{Pacifist}(x)]$$

If we circumscribe the predicates Ab_2 and Ab_3 , we have two minimal models:

$$\mathcal{I}_1 \models \text{Ab}_2(\text{nixon}) \text{ and } \mathcal{I}_1 \models \text{Pacifist}(\text{nixon})$$
$$\mathcal{I}_2 \models \text{Ab}_3(\text{nixon}) \text{ and } \mathcal{I}_2 \models \neg \text{Pacifist}(\text{nixon})$$

So, $\text{KB} \not\models_{\leq} \text{Pacifist}(\text{nixon})$ and $\text{KB} \not\models_{\leq} \neg \text{Pacifist}(\text{nixon})$.

If, for example, we give priority to religious convictions rather than to political ones, we can express it by prioritized circumscription, where we prefer the (minimal) model that minimizes Ab_3 .

Defaults

III. Default Logic

It provides a mechanism that explicitly specifies which sentences should be added to the KB, maintaining consistency.

For example, if $\text{Bird}(t)$ is entailed by the KB, we might want to add the default assumption $\text{Flies}(t)$, if it is consistent to do so.

In default logic, a KB consists of two parts: a set \mathcal{F} of first-order sentences and a set \mathcal{D} of default rules, which are specifications of what assumptions can be made and when.

The role of the default logic is to specify the following:

- the appropriate set of implicit beliefs that incorporate the (explicit) facts in \mathcal{F} ;
- as many default assumptions as possible, given the default rules in \mathcal{D} ;
- the logical entailments inferred from the implicit beliefs and the default assumptions.

Defaults

Default rules

A default rule is written in the form $\langle \alpha : \beta / \delta \rangle$, where α is the prerequisite, β is the justification and δ is the conclusion. δ is considered to be true if α is true and it is consistent to believe β (that is $\neg\beta$ is not true)

$\langle \text{Bird}(\text{tweety}) : \text{Flies}(\text{tweety}) / \text{Flies}(\text{tweety}) \rangle$

A rule where the justification and conclusion are the same is called a normal default rule and it is written as $\text{Bird}(\text{tweety}) \Rightarrow \text{Flies}(\text{tweety})$.

A rule can be formulated using free variables:

$\langle \text{Bird}(x) : \text{Flies}(x) / \text{Flies}(x) \rangle$

represents the set of all its instances, formed by replacing x by a ground term.

Defaults

Default extensions

Given a default theory $KB=(\mathcal{F},\mathcal{D})$, what are the sentences that should be believed?

We define an extension of the theory as a reasonable set of beliefs given a default theory.

Def. A set of sentences ε is an extension of a default theory $(\mathcal{F},\mathcal{D})$ if for every sentence π we have:

$$\pi \in \varepsilon \text{ iff } \mathcal{F} \cup \{\delta \mid \langle \alpha:\beta/\delta \rangle \in \mathcal{D}, \alpha \in \varepsilon, \neg\beta \notin \varepsilon\} \models \pi.$$

Thus, an extension is the set of all entailments of $\mathcal{F} \cup \Delta$, where Δ is a suitable set of assumptions.

Obs. The definition of ε does not say how to find an ε , but ε is completely characterized by its set of applicable assumptions Δ .

Defaults

Example:

$$\mathcal{F} = \{\text{Bird}(\text{tweety}), \text{Bird}(\text{chilly}), \neg \text{Flies}(\text{chilly})\}$$

$$\mathcal{D} = \{\text{Bird}(x) \Rightarrow \text{Flies}(x)\}$$

Let $\varepsilon = \mathcal{F} \cup \{\text{Flies}(\text{tweety})\}$.

$\text{Flies}(\text{tweety})$ is the only assumption applicable to ε .

$$\left. \begin{array}{l} \text{Bird}(\text{tweety}) \in \varepsilon \\ \neg \text{Flies}(\text{tweety}) \notin \varepsilon \end{array} \right\} \Rightarrow \text{Flies}(\text{tweety}) \text{ is applicable.}$$

$\text{Flies}(t)$ is not applicable for any other t (in our example t could be only chilly).

Thus, $\text{Flies}(\text{tweety})$ is the only applicable assumption, so ε is an extension (it can be proven that it is the only one).

Obs. An extension ε of a default theory $(\mathcal{F}, \mathcal{D})$ is inconsistent iff \mathcal{F} is inconsistent.

Defaults

Multiple extensions

Consider the following default theory:

$$\mathcal{F} = \{\text{Republican}(\text{nixon}), \text{Quaker}(\text{nixon})\}$$

$$\mathcal{D} = \{\text{Republican}(x) \Rightarrow \neg \text{Pacifist}(x), \text{Quaker}(x) \Rightarrow \text{Pacifist}(x)\}$$

Let ε_1 be the extension characterized by the assumption $\text{Pacifist}(\text{nixon})$ and ε_2 be the extension characterized by the assumption $\neg \text{Pacifist}(\text{nixon})$.

ε_1 and ε_2 are extensions because their assumptions are applicable and there are no other applicable ones (for $t \neq \text{nixon}$).

For any other extensions, assumptions would be of the form $\text{Pacifist}(t)$ or $\neg \text{Pacifist}(t)$, but none are applicable for $t \neq \text{nixon}$.

Thus, ε_1 and ε_2 are the only extensions possible.

Defaults

On the basis of what we know, either Nixon is a pacifist or he is not a pacifist are reasonable beliefs. There are two options:

1. A skeptical reasoner will only believe those sentences that are common to all extensions of the default theory;
2. A credulous reasoner will simply choose an extension as a set of sentences to believe.

In some cases, the existence of multiple extensions is an indication that more knowledge is necessary to make a reasonable decision.

Defaults

In the previous example, we may want to say that the default about Quakers should apply only to individuals that are not politically active.

If we add in \mathcal{F} the fact

$$\forall x. [\text{Republican}(x) \supset \text{Political}(x)],$$

we can replace the rule $\text{Quaker}(x) \Rightarrow \text{Pacifist}(x)$ by a non-normal one:

$$\frac{\text{Quaker}(x): [\text{Pacifist}(x) \wedge \neg \text{Political}(x)]}{\text{Pacifist}(x)}$$

$$\mathcal{F} = \{\text{Republican}(\text{nixon}), \text{Quaker}(\text{nixon}), \forall x. [\text{Republican}(x) \supset \text{Political}(x)]\}$$

$$\mathcal{D} = \{\text{Republican}(x) \Rightarrow \neg \text{Pacifist}(x), \frac{\text{Quaker}(x): [\text{Pacifist}(x) \wedge \neg \text{Political}(x)]}{\text{Pacifist}(x)}\}$$

For ordinary Quakers, the assumption is that they are pacifists. But for Quaker Republicans like Nixon, we assume that they are not pacifists.

Defaults

If we replace $\forall x.[\text{Republican}(x) \supset \text{Political}(x)]$ by the default rule

$$\text{Republican}(x) \Rightarrow \text{Political}(x),$$

$$\mathcal{F} = \{\text{Republican}(\text{nixon}), \text{Quaker}(\text{nixon})\}$$

$$\mathcal{D} = \{\text{Republican}(x) \Rightarrow \neg \text{Pacifist}(x), \text{Republican}(x) \Rightarrow \text{Political}(x), \\ \frac{\text{Quaker}(x):[\text{Pacifist}(x) \wedge \neg \text{Political}(x)]}{\text{Pacifist}(x)}\}$$

then we have two extensions:

- one characterized by the assumptions $\{\neg \text{Pacifist}(\text{nixon}), \text{Political}(\text{nixon})\}$
- one characterized by the assumptions $\{\text{Pacifist}(\text{nixon})\}$

Defaults

Resolving conflicts among default rules is crucial when we deal with concept hierarchies.

For example, for the following KB

$$\mathcal{F} = \{\forall x. [\text{Penguin}(x) \supset \text{Bird}(x)], \text{Penguin}(\text{chilly})\}$$

$$\mathcal{D} = \{\text{Bird}(x) \Rightarrow \text{Flies}(x), \text{Penguin}(x) \Rightarrow \neg \text{Flies}(x)\}$$

we have two extensions: one where Chilly is assumed to fly and one where Chilly is assumed not to fly.

The default that penguins do not fly should preempt the more general default that birds fly.

$$\frac{\text{Bird}(x): [\text{Flies}(x) \wedge \neg \text{Penguin}(x)]}{\text{Flies}(x)}$$

Unlike defaults in an inheritance mechanism, the default logic do not automatically prefer the most specific defaults.