

VISUALIZING AND UNDERSTANDING RECURRENT NETWORKS

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ABSTRACT

Recurrent Neural Networks (RNNs), and specifically a variant with Long Short-Term Memory (LSTM), are enjoying renewed interest as a result of successful applications in a wide range of machine learning problems that involve sequential data. However, while LSTMs provide exceptional results in practice, the source of their performance and their limitations remain rather poorly understood. Using character-level language models as an interpretable testbed, we aim to bridge this gap by providing an analysis of their representations, predictions and error types. In particular, our experiments reveal the existence of interpretable cells that keep track of long-range dependencies such as line lengths, quotes and brackets. Moreover, our comparative analysis with finite horizon n -gram models traces the source of the LSTM improvements to long-range structural dependencies. Finally, we provide analysis of the remaining errors and suggests areas for further study.

1 INTRODUCTION

Recurrent Neural Networks, and specifically a variant with Long Short-Term Memory (LSTM) Hochreiter & Schmidhuber (1997), have recently emerged as an effective model in a wide variety of applications that involve sequential data. These include language modeling Mikolov et al. (2010), handwriting recognition and generation Graves (2013), machine translation Sutskever et al. (2014); Bahdanau et al. (2014), speech recognition Graves et al. (2013), video analysis Donahue et al. (2015) and image captioning Vinyals et al. (2015); Karpathy & Fei-Fei (2015).

However, both the source of their impressive performance and their shortcomings remain poorly understood. This raises concerns of the lack of interpretability and limits our ability design better architectures. A few recent ablation studies analyzed the effects on performance as various gates and connections are removed Greff et al. (2015); Chung et al. (2014). However, while this analysis illuminates the performance-critical pieces of the architecture, it is still limited to examining the effects only on the global level of the final test set perplexity alone. Similarly, an often cited advantage of the LSTM architecture is that it can store and retrieve information over long time scales using its gating mechanisms, and this ability has been carefully studied in toy settings Hochreiter & Schmidhuber (1997). However, it is not immediately clear that similar mechanisms can be effectively discovered and utilized by these networks in real-world data, and with the common use of simple stochastic gradient descent and truncated backpropagation through time.

To our knowledge, our work provides the first empirical exploration of the predictions of LSTMs and their learned representations on real-world data. Concretely, we use character-level language models as an interpretable testbed for illuminating the long-range dependencies learned by LSTMs. Our analysis reveals the existence of cells that robustly identify interpretable, high-level patterns such as line lengths, brackets and quotes. We further quantify the LSTM predictions with comprehensive comparison to n -gram models, where we find that LSTMs perform significantly better on characters that require long-range reasoning. Finally, we conduct an error analysis in which we “peel the onion” of errors with a sequence of oracles. These results allow us to quantify the extent of remaining errors in several categories and to suggest specific areas for further study.

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2 RELATED WORK

Recurrent Networks. Recurrent Neural Networks (RNNs) have a long history of applications in various sequence learning tasks Werbos (1988); Schmidhuber (2015); Rumelhart et al. (1985). Despite their early successes, the difficulty of training simple recurrent networks Bengio et al. (1994); Pascanu et al. (2012) has encouraged various proposals for improvements to their basic architecture. Among the most successful variants are the Long Short Term Memory networks Hochreiter & Schmidhuber (1997), which can in principle store and retrieve information over long time periods with explicit gating mechanisms and a built-in constant error carousel. In the recent years there has been a renewed interest in further improving on the basic architecture by modifying the functional form as seen with Gated Recurrent Units Cho et al. (2014), incorporating content-based soft attention mechanisms Bahdanau et al. (2014); Weston et al. (2014), push-pop stacks Joulin & Mikolov (2015), or more generally external memory arrays with both content-based and relative addressing mechanisms Graves et al. (2014). In this work we focus the majority of our analysis on the LSTM due to its widespread popularity and a proven track record.

Understanding Recurrent Networks. While there is an abundance of work that modifies or extends the basic LSTM architecture, relatively little attention has been paid to understanding the properties of its representations and predictions. Greff et al. (2015) recently conducted a comprehensive study of LSTM components. Chung et al. evaluated GRU compared to LSTMs Chung et al. (2014). Jozefowicz et al. (2015) conduct an automated architecture search of thousands of RNN architectures. Pascanu et al. (2013) examined the effects of depth. **These approaches study recurrent network based only on the variations in the final test set cross entropy, while we break down the performance into interpretable categories and study individual error types.** Most related to our work is Hermans & Schrauwen (2013), who also study the long-term interactions learned by recurrent networks in the context of character-level language models, specifically in the context of parenthesis closing and time-scales analysis. Our work complements their results and provides additional types of analysis. Lastly, we are heavily influenced by work on in-depth analysis of errors in object detection Hoiem et al. (2012), where the final mean average precision is similarly broken down and studied in detail.

3 EXPERIMENTAL SETUP

We first describe three commonly used recurrent network architectures (RNN, LSTM and the GRU), then describe their used in sequence learning and finally discuss the optimization.

3.1 RECURRENT NEURAL NETWORK MODELS

The simplest instantiation of a deep recurrent network arranges hidden state vectors h_t^l in a two-dimensional grid, where $t = 1 \dots T$ is thought of as time and $l = 1 \dots L$ is the depth. The bottom row of vectors $h_t^0 = x_t$ at depth zero holds the input vectors x_t and each vector in the top row $\{h_t^L\}$ is used to predict an output vector y_t . All intermediate vectors h_t^l are computed with a recurrence formula based on h_{t-1}^l and h_t^{l-1} . Through these hidden vectors, each output y_t at time step t becomes a function of all input vectors up to t , $\{x_1, \dots, x_t\}$. The precise mathematical form of the recurrence $(h_{t-1}^l, h_t^{l-1}) \rightarrow h_t^l$ varies from model to model and we describe these details next.

Vanilla Recurrent Neural Network (RNN) has a recurrence of the form

$$h_t^l = \tanh W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix}$$

where we assume that all $h \in \mathbb{R}^n$. The parameter matrix W^l on each layer has dimensions $[n \times 2n]$ and \tanh is applied elementwise. Note that W^l varies between layers but is shared through time. We omit the bias vectors for brevity. Interpreting the equation above, the inputs from the layer below in depth (h_t^{l-1}) and before in time (h_{t-1}^l) are transformed and interact through additive interaction before being squashed by \tanh . This is known to be a weak form of coupling Sutskever et al. (2011). Both the LSTM and the GRU (discussed next) include more powerful multiplicative interactions.

Long Short-Term Memory (LSTM) Hochreiter & Schmidhuber (1997) was designed to address the difficulties of training RNNs Bengio et al. (1994). In particular, it was observed that the back-propagation dynamics caused the gradients in an RNN to either vanish or explode. It was later found that the exploding gradient concern can be alleviated with a heuristic of clipping the gradients at some maximum value Pascanu et al. (2012). On the other hand, LSTMs were designed to mitigate the vanishing gradient problem. In addition to a hidden state vector h_t^l , LSTMs also maintain a

memory vector c_t^l . At each time step the LSTM can choose to read from, write to, or reset the cell using explicit gating mechanisms. The precise form of the update is as follows:

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \text{sigm} \\ \text{sigm} \\ \text{sigm} \\ \text{tanh} \end{pmatrix} W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix} \quad \begin{aligned} c_t^l &= f \odot c_{t-1}^l + i \odot g \\ h_t^l &= o \odot \tanh(c_t^l) \end{aligned}$$

Here, the sigmoid function sigm and tanh are applied element-wise, and W^l is a $[4n \times 2n]$ matrix. The three vectors $i, f, o \in \mathbb{R}^n$ are thought of as binary gates that control whether each memory cell is updated, whether it is reset to zero, and whether its local state is revealed in the hidden vector, respectively. The activations of these gates are based on the sigmoid function and hence allowed to range smoothly between zero and one to keep the model differentiable. The vector $g \in \mathbb{R}^n$ ranges between -1 and 1 and is used to additively modify the memory contents. This additive interaction is a critical feature of the LSTM’s design, because during backpropagation a sum operation merely distributes gradients. This allows gradients on the memory cells c to flow backwards through time uninterrupted for long time periods, or at least until the flow is disrupted with the multiplicative interaction of an active forget gate. Lastly, note that an implementation of the LSTM requires one to maintain two vectors (h_t^l and c_t^l) at every point in the network.

Gated Recurrent Unit (GRU) Cho et al. (2014) recently proposed as a simpler alternative to the LSTM that takes the form:

$$\begin{pmatrix} r \\ z \end{pmatrix} = \begin{pmatrix} \text{sigm} \\ \text{sigm} \end{pmatrix} W_r^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix} \quad \begin{aligned} \tilde{h}_t^l &= \tanh(W_x^l h_t^{l-1} + W_g^l (r \odot h_{t-1}^l)) \\ h_t^l &= (1 - z) \odot h_{t-1}^l + z \odot \tilde{h}_t^l \end{aligned}$$

Here, W_r^l are $[2n \times 2n]$ and W_g^l and W_x^l are $[n \times n]$. The GRU has the interpretation of computing a *candidate* hidden vector \tilde{h}_t^l and then smoothly interpolating towards it gated by z .

3.2 CHARACTER-LEVEL LANGUAGE MODELING

We use character-level language modeling as an interpretable testbed for sequence learning. In this setting, the input to the network is a sequence of characters and the network is trained to predict the next character in the sequence with a Softmax classifier at each time step. Concretely, assuming a fixed vocabulary of K characters we encode all characters with K -dimensional 1-of- K vectors $\{x_t\}, t = 1, \dots, T$, and feed these to the recurrent network to obtain a sequence of D -dimensional hidden vectors at the last layer of the network $\{h_t^L\}, t = 1, \dots, T$. To obtain predictions for the next character in the sequence we project this top layer of activations to a sequence of vectors $\{y_t\}$, where $y_t = W_y h_t^L$ and W_y is a $[K \times D]$ parameter matrix. These vectors are interpreted as holding the (unnormalized) log probability of the next character in the sequence and the objective is to minimize the average cross-entropy loss over all targets.

3.3 OPTIMIZATION

Following previous work Sutskever et al. (2014) we initialize all parameters uniformly in range $[-0.08, 0.08]$. We use mini-batch stochastic gradient descent with batch size 100 and RMSProp Dauphin et al. (2015) per-parameter adaptive update with base learning rate 2×10^{-3} and decay 0.95. These settings work robustly with all of our models. The network is unrolled for 100 time steps. We train each model for 50 epochs and decay the learning rate after 10 epochs by multiplying it with a factor of 0.95 after each additional epoch. We use early stopping based on validation performance and cross-validate the amount of dropout for each model individually.

4 EXPERIMENTS

Datasets. Two datasets previously used in the context of character-level language models are the Penn Treebank dataset Marcus et al. (1993) and the Hutter Prize 100MB of Wikipedia dataset Hutter (2012). However, both datasets contain a mix of common language and special markup. Our goal is not to compete with previous work but rather to study recurrent networks in a controlled setting and on both ends on the spectrum of degree of structure. Therefore, we chose to use Leo Tolstoy’s *War and Peace* (WP) novel, which consists of 3,258,246 characters of almost entirely English text with minimal markup, and at the other end of the spectrum the source code of the *Linux Kernel* (LK). We shuffled all header and source files randomly and concatenated them into a single file to form the 6,206,996 character long dataset. We split the data into train/val/test splits as 80/10/10 for WP and

	LSTM			RNN			GRU		
Layers	1	2	3	1	2	3	1	2	3
Size	War and Peace Dataset								
64	1.449	1.442	1.540	1.446	1.401	1.396	1.398	1.373	1.472
128	1.277	1.227	1.279	1.417	1.286	1.277	1.230	1.226	1.253
256	1.189	1.137	1.141	1.342	1.256	1.239	1.198	1.164	1.138
512	1.161	1.092	1.082	-	-	-	1.170	1.201	1.077
	Linux Kernel Dataset								
64	1.355	1.331	1.366	1.407	1.371	1.383	1.335	1.298	1.357
128	1.149	1.128	1.177	1.241	1.120	1.220	1.154	1.125	1.150
256	1.026	0.972	0.998	1.171	1.116	1.116	1.039	0.991	1.026
512	0.952	0.840	0.846	-	-	-	0.943	0.861	0.829

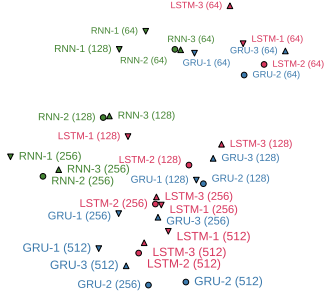


Figure 1: **Left:** The **test set cross-entropy loss** for all models and datasets (low is good). Models in each row have nearly equal number of parameters. The test set has 300,000 characters. The standard deviation, estimated with 100 bootstrap samples, is less than 4×10^{-3} in all cases. **Right:** A t-SNE embedding based on the probabilities assigned to test set characters by each model on War and Peace. The color, size, and marker correspond to model type, model size, and number of layers.

90/5/5 for LK. Therefore, there are approximately 300,000 characters in the validation/test splits in each case. The total number of characters in the vocabulary is 87 for WP and 101 for LK.

4.1 COMPARING RECURRENT NETWORKS

We first train several recurrent network models to support further analysis and to compare their performance in a controlled setting. In particular, we train models in the cross product of type (LSTM/RNN/GRU), number of layers (1/2/3), number of parameters (4 settings), and both datasets (WP/KL). For a 1-layer LSTM we used hidden size vectors of 64, 128, 256, and 512 cells, which with our character vocabulary sizes translates to approximately 50K, 130K, 400K, and 1.3M parameters respectively. The sizes of hidden layers of the other models were carefully chosen so that the total number of parameters in each case is as close as possible to these 4 settings.

The test set results are shown in Figure 1. Our consistent finding is that depth of at least two is beneficial. However, between two and three layers our results are mixed. Additionally, the results are mixed between the LSTM and the GRU, but both significantly outperform the RNN. We also computed the fraction of times that each pair of models agree on the most likely character and use it to render a t-SNE Van der Maaten & Hinton (2008) embedding (we found this more stable and robust than the KL divergence). The plot (Figure 1, right) further supports the claim that the LSTM and the GRU make similar predictions while the RNNs form their own cluster.

4.2 INTERNAL MECHANISMS OF AN LSTM

Interpretable, long-range LSTM cells. An LSTMs can in principle use its memory cells to remember long-range information and keep track of various attributes of text it is currently processing. For instance, it is a simple exercise to write down toy cell weights that would allow the cell to keep track of whether it is inside a quoted string. However, to our knowledge, the existence of such cells has never been experimentally demonstrated on real-world data. In particular, it could be argued that even if the LSTM is in principle capable of using these operations, practical optimization challenges (i.e. SGD dynamics, or approximate gradients due to truncated backpropagation through time) might prevent it from discovering these solutions. In this experiment we verify that multiple interpretable cells do in fact exist in these networks (see Figure 2). For instance, one cell is clearly acting as a line length counter, starting with a high value and then slowly decaying with each character until the next newline. Other cells turn on inside quotes, the parenthesis after if statements, inside strings or comments, or with increasing strength as the indentation of a block of code increases. In particular, note that truncated backpropagation with our hyperparameters prevents the gradient signal from directly noticing dependencies longer than 100 characters, but we still observe cells that reliably keep track of quotes or comment blocks much longer than 100 characters (e.g. ~ 230 characters in the quote detection cell example in Figure 2). We hypothesize that these cells first develop on patterns shorter than 100 characters but then also appropriately generalize to longer sequences.

Gate activation statistics. We can gain some insight into the internal mechanisms of the LSTM by studying the gate activations in the networks as they process test set data. We were particularly interested in looking at the distributions of saturation regimes in the networks, where we define a

Model \ n	1	2	3	4	5	6	7	8	9	20
War and Peace Dataset										
n -gram	2.399	1.928	1.521	1.314	1.232	1.203	1.194	1.194	1.194	1.195
n -NN	2.399	1.931	1.553	1.451	1.339	1.321	-	-	-	-
Linux Kernel Dataset										
n -gram	2.702	1.954	1.440	1.213	1.097	1.027	0.982	0.953	0.933	0.889
n -NN	2.707	1.974	1.505	1.395	1.256	1.376	-	-	-	-

Table 2: The **test set cross-entropy loss** on both datasets for n -gram models (low is good). The standard deviation estimate using 100 bootstrap samples is below 4×10^{-3} in all cases.

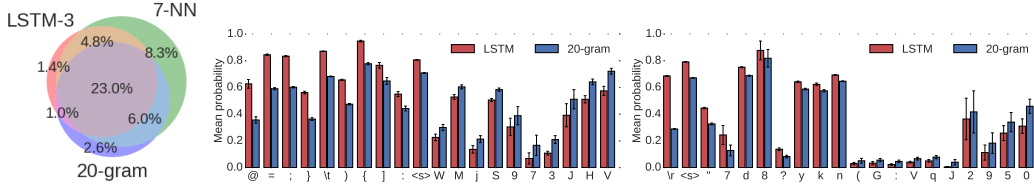


Figure 4: **Left:** Overlap between test-set errors between our best 3-layer LSTM and the n -gram models (low area is good). **Middle/Right:** Mean probabilities assigned to a correct character (higher is better), broken down by the character, and then sorted by the difference between two models. “<s>” is the space character. LSTM (red) outperforms the 20-gram model (blue) on special characters that require long-range reasoning. Middle: LK dataset, Right: WP dataset.

encodings of n consecutive characters. We optimize the model as described in Section 3.3 and cross-validate the size of the hidden layer.

2. n -gram: An unpruned $(n + 1)$ -gram language model using modified Kneser-Ney smoothing Chen & Goodman (1999). This is a standard smoothing method for language models Huang et al. (2001). All models were trained using the popular KenLM software package Heafield et al. (2013).

Performance comparisons. The performance of both n -gram models is shown in Table 2. The n -gram and n -NN models perform nearly identically for small values of n , but for larger values the n -NN models start to overfit and the n -gram model performs better. **Moreover, we see that on both datasets our best recurrent network outperforms the 20-gram model (1.077 vs. 1.195 on WP and 0.84 vs. 0.889).** It is difficult to make a direct model size comparison, but the 20-gram model file has 3GB, while our largest checkpoints are 11MB. However, the assumptions encoded in the Kneser-Ney smoothing model are intended for word-level modeling of natural language and may not be optimal for character-level data. **Despite this concern, these results already provide weak evidence that the recurrent networks are effectively utilizing information beyond 20 characters.**

Error Analysis. It is instructive to delve deeper into the errors made by both recurrent networks and n -gram models. In particular, we define a character to be an error if the probability assigned to it by a model on the previous time step is below 0.5. Figure 4 (left) shows the overlap between the test-set errors for the 3-layer LSTM, and the best n -NN and n -gram models. We see that the majority of errors are shared by all three models, but each model also has its own unique errors.

To gain deeper insight into the errors that are unique to the LSTM or the 20-gram model, we compute the mean probability assigned to each character in the vocabulary across the test set. In Figure 4 (middle, right) we display the 10 characters where each model has the largest advantage over the other. On the Linux Kernel dataset, the LSTM displays a large advantage on special characters that are used to structure C programs, including whitespace and brackets. The War and Peace dataset features an interesting long-term dependency with the carriage return, which occurs approximately every 70 characters. Figure 4 (right) shows that the LSTM has a distinct advantage on this character. To accurately predict the presence of the carriage return the model likely needs to keep track of its distance since the last carriage return. The cell example we’ve highlighted in Figure 2 (top, left) seems particularly well-tuned for this specific task. Similarly, to predict a closing bracket or quotation mark, the model must be aware of the corresponding open bracket, which may have appeared many time steps ago. The fact that the LSTM performs significantly better than the 20-

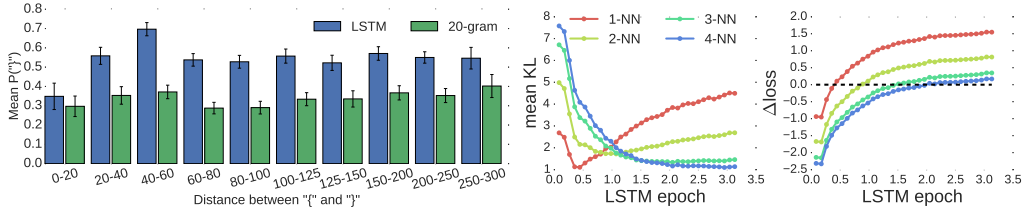


Figure 5: **Left:** Mean probabilities that the LSTM and 20-gram model assign to the “}” character, bucketed by the distance to the matching “{”. **Right:** Comparison of the similarity between 3-layer LSTM and the n -NN baselines over the first 3 epochs of training, as measured by the symmetric KL-divergence (middle) and the test set loss (right). Low KL indicates similar predictions, and positive Δ loss indicates that the LSTM outperforms the baseline.

gram model on these characters provides strong evidence that the model is capable of effectively keeping track of long-range interactions.

Case study: closing brace. Of these structural characters, the one that requires the longest-term reasoning is the closing brace (“}”) on the Linux Kernel dataset. Braces are used to denote blocks of code, and may be nested; as such, the distance between an opening brace and its corresponding closing brace can range from tens to hundreds of characters. This feature makes the closing brace an ideal test case for studying the ability of the LSTM to reason over various time scales. We group closing brace characters on the test set by the distance to their corresponding open brace and compute the mean probability assigned by the LSTM and the 20-gram model to closing braces within each group. The results are shown in Figure 5 (left). First, note that the LSTM only slightly outperforms the 20-gram model in the first bin, where the distance between braces is only up to 20 characters. After this point the performance of the 20-gram model stays relatively constant, reflecting a baseline probability of predicting the closing brace without seeing its matching opening brace. Compared to this baseline, we see that the LSTM gains significant boosts up to 60 characters, and then its performance delta slowly decays over time as it becomes difficult to keep track of the dependence.

Training dynamics. It is also instructive to examine the training dynamics of the LSTM by comparing it with trained n -NN models during training using the (symmetric) KL divergence between the predictive distributions on the test set. We plot the divergence and the difference in the mean loss in Figure 5 (right). Notably, we see that in the first few iterations the LSTM behaves like the 1-NN model but then diverges from it soon after. The LSTM then behaves most like the 2-NN, 3-NN, and 4-NN models in turn. This experiment suggests that the LSTM “grows” its competence over increasingly longer dependencies during training. This insight might be related to why Sutskever et al. (2014) observe improvements when they reverse the source sentences in their encoder-decoder architecture for machine translation. The inversion introduces short-term dependencies that the LSTM can model first, and then longer dependencies are learned over time.

4.4 ERROR ANALYSIS: BREAKING DOWN THE FAILURE CASES

In this section we break down LSTM’s errors into categories to study the remaining limitations, the relative severity of each error type, and to suggest areas for further study. We focus on the War and Peace dataset where it is easier to categorize the errors. Our approach is to “peel the onion” by iteratively removing the errors with a series of constructed oracles. As in the last section, we consider a character to be an error if the probability it was assigned by the model in the previous time step is below 0.5. Note that the order in which the oracles are applied influences the results. We tried to apply the oracles in order of increasing difficulty of removing each error category and believe that the final results are instructive despite this downside. The oracles we use are, in order:

n -gram oracle. First, we construct optimistic n -gram oracles that eliminate errors that might be fixed with better modeling of short dependencies. In particular, we evaluate the n -gram model ($n = 1, \dots, 9$) and remove a character error if it is correctly classified (probability assigned to that character greater than 0.5) by any of these models. This gives us an approximate idea of the amount of signal present only in the last 9 characters, and how many errors we could optimistically hope to eliminate without needing to reason over long time horizons.

Dynamic n -long memory oracle. To motivate the next oracle, consider the string “Jon yelled at Mary but Mary couldn’t hear him.” One interesting and consistent failure mode that we noticed in

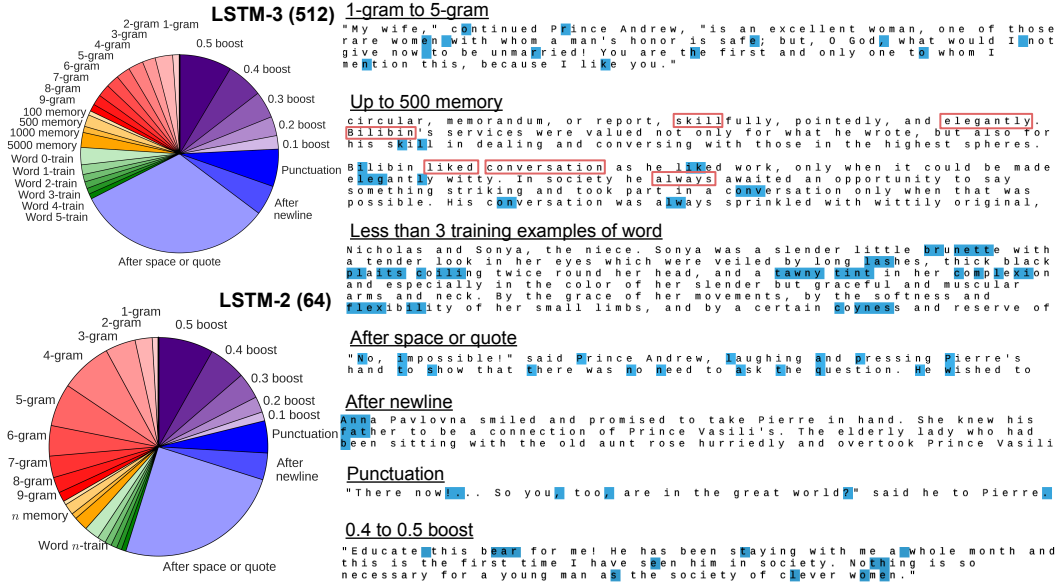


Figure 6: **Left:** LSTM errors removed one by one with oracles, starting from top of the pie chart and going counter-clockwise. The area of each slice corresponds to fraction of errors contributed. “ n -memory” refers to dynamic memory oracle with context of n previous characters. “Word t -train” refers to the rare words oracle with word count threshold of t . **Right:** Concrete examples of text from the test set for each error type. Blue color highlights the relevant characters with the associated error. For the memory category we also highlight the repeated substrings with red bounding rectangles.

the predictions is that if the LSTM fails to predict the characters of the first occurrence of “Mary” then it will almost always also fail to predict the same characters of the second occurrence, with a nearly identical pattern of errors. However, in principle the presence of the first mention should make the second much more likely. The LSTM could conceivably store a summary of previously seen characters in the data and fall back on this memory when it is uncertain. However, this does not appear to take place in practice. This limitation is related to the improvements seen in “dynamic evaluation” Mikolov (2012); Jelinek et al. (1991) of recurrent language models, where an RNN is allowed to train on the test set characters during evaluation as long as it sees them only once. In this mode of operation when the RNN trains on the first occurrence of “Mary”, the log probabilities on the second occurrence are significantly better. We hypothesize that this *dynamic* aspect is a common feature of sequence data, where certain subsequences that might not frequently occur in the training data should still be more likely if they were present in the immediate history. However, this general algorithm does not seem to be learned by the LSTM. Our dynamic memory oracle quantifies the severity of this limitation by removing errors in all words (starting with the second character) that can be found as a substring in the last n characters (we use $n \in \{100, 500, 1000, 5000\}$).

Rare words oracle. Next, we construct an oracle that eliminates errors for rare words that occur only up to n times in the training data ($n = 0, \dots, 5$). This estimates the severity of errors that could optimistically be eliminated by increasing the size of the training data, or with pretraining.

Word model oracle. We noticed that a large portion of the errors occur on the first character of each word. Intuitively, the task of selecting the next word in the sequence is harder than completing the last few characters of a known word. Motivated by this observation we constructed an oracle that eliminated all errors after a space, quote or a newline. Interestingly, a high portion of errors can be found after a newline, since the models have to learn that newline has semantics similar to a space.

Punctuation oracle. The remaining errors become difficult to blame on one particular, interpretable aspect of the modeling. At this point we construct an oracle that removes errors on all punctuation.

Boost oracles. The remaining errors that do not show salient structures or patterns are removed by an oracle that boosts the probability of the correct letter by a fixed amount. These oracles allow us to understand the distribution of the difficulty of the remaining errors.

We now subject two LSTM models to the error analysis: First, our best LSTM model and second, the best LSTM model in the smallest model category (50K parameters). The small and large models

allow us to understand how the error break down changes as we scale up the model. The error breakdown after applying each oracle for both models can be found in Figure 6.

The error breakdown. In total, our best LSTM model made a total of 140K errors out of 330K test set characters (42%). Of these, the n -gram oracle eliminates 18%, suggesting that the model is not taking full advantage of the last 9 characters. The dynamic memory oracle eliminates 6% of the errors. In principle, a dynamic evaluation scheme could be used to mitigate this error, but we believe that a more principled approach could involve an approach similar to Memory Networks Weston et al. (2014), where the model is allowed to attend to a recent history of the sequence while making its next prediction. Finally, the rare words oracle accounts for 9% of the errors. This error type might be mitigated with unsupervised pretraining Dai & Le (2015), or by increasing the size of the training set. The majority of the remaining errors (37%) follow a space, a quote, or a newline, indicating the model’s difficulty with word-level predictions. This suggests that longer time horizons in backpropagation through time, or possibly hierarchical context models, could provide improvements. See Figure 6 (right) for examples of each error type. We believe that this type of error breakdown is a valuable tool for isolating and understanding the source of improvements provided by new proposed models.

Errors eliminated by scaling up. In contrast, the smaller LSTM model makes a total of 184K errors (or 56% of the test set), or approximately 44K more than the large model. Surprisingly, 36K of these errors (81%) are n -gram errors, 5K come from the boost category, and the remaining 3K are distributed across the other categories relatively evenly. That is, scaling the model up by a factor 26 in the number of parameters has almost entirely provided gains in the local, n -gram error rate and has left the other error categories untouched in comparison. This analysis provides some evidence that it might be necessary to develop new architectural improvements instead of simply scaling up the basic model.

5 CONCLUSION

We have used character-level language models as an interpretable test bed for analyzing the predictions, representations training dynamics, and error types present in Recurrent Neural Networks. In particular, our qualitative visualization experiments, cell activation statistics and comparisons to finite horizon n -gram models demonstrate that these networks learn powerful, and often interpretable long-range interactions on real-world data. Our error analysis broke down cross entropy loss into several interpretable categories, and allowed us to illuminate the sources of remaining limitations and to suggest further areas for study. In particular, we found that scaling up the model almost entirely eliminates errors in the n -gram category, which provides some evidence that further architectural innovations may be needed to address the remaining errors.

ACKNOWLEDGMENTS

We gratefully acknowledge the support of NVIDIA Corporation with the donation of the GPUs used for this research.

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