

Question 1: A die is rolled. What is the probability of getting:

(a) An even number

(b) A number greater than 4

Answer: (a) Even numbers on a die = {2, 4, 6}

Total outcomes = 6

$$P(\text{Even}) = 3/6 = \frac{1}{2}$$

(b) A number greater than 4 = {5, 6}

$$P(\text{no. greater than 4}) = 2/6 = 1/3$$

Question 2: In a class of 50 students:

- 20 like Mathematics (M)
- 15 like Science (S)
- 5 like both subjects.

What is the probability that a student chosen at random likes Mathematics or Science?

Answer: Total students = 50

$$|M| = 20, |S| = 15, |M \cap S| = 5$$

Students who like M or S:

$$|M \cup S| = |M| + |S| - |M \cap S| = 20 + 15 - 5 = 30$$

$$P(M \text{ or } S) = 30/50 = 3/5$$

Question 3: A bag has 3 red and 2 blue balls. If one ball is drawn randomly and is red, what is the probability that the next ball is also red (without replacement)?

Answer: The bag has 3 red and 2 blue balls.

One red is already drawn (without replacement).

Remaining balls = 2 red, 2 blue (Total = 4)

$$P(\text{Next is Red}) = 2/4 = \frac{1}{2}$$

Question 4: The population of a school is divided into 60% boys and 40% girls. If you want equal representation of both genders in the sample, which method should you use: Simple Random Sampling or Stratified Sampling? Why?

Answer: We use stratified Sampling because the population has unequal groups (60% boys,40% girls), and stratified sampling ensures equal representation of both genders in the sample by selecting proportionally from each group.

Question 5: The average height of 1000 students = 160 cm. A sample of 100 students shows an average height = 158 cm. Find the sampling error.

Answer: Sampling Error = Population Mean- Sample Mean = 160-158 = 2cm

Question 6: The population mean salary is ₹50,000 with $\sigma = ₹5,000$. If we take a sample of 100 employees, what is the standard error of the mean (SEM)?

Answer: Population SD (σ) = ₹5,000

Sample size (n) = 100

$$SEM = SD / \sqrt{n} = 5000 / 10 = 500.$$

Question 7: In a group of 100 students:

- 40 like Cricket (C)
- 30 like Football (F)
- 10 like both Cricket and Football.

Find the probability that a student likes at least one sport.

Answer: Total students = 100

$$|C| = 40, |F| = 30, |C \cap F| = 10$$

$$|C \cup F| = 40 + 30 - 10 = 60$$

$$P(\text{at least one sport}) = 60/100 = 0.6$$

Question 8: From a deck of 52 cards, two cards are drawn without replacement. What is the probability that both are Aces?

Answer: Total cards = 52

Number of Aces = 4

$$P(\text{First Ace}) = 4/52$$

$$P(\text{Second Ace}) = 3/51$$

$$P(\text{Both Ace}) = 4/52 * 3/51 = 1/221$$

Question 9: A factory produces bulbs with 2% defective rate. If 5 bulbs are chosen at random, what is the probability that all are non-defective?

Answer : Defective rate = 2%

So, non-defective rate = 98% = 0.98

$P(\text{all 5 non-defective}) = (0.98)^5 \text{ power} = 0.9039 \text{ (approx.)}$

Question 10: Differentiate between discrete and continuous random variables with examples.

Answer: Discrete Random Variable:

A random variable that takes **countable values**.

Example: Number of heads when tossing 3 coins (0, 1, 2, 3)

Continuous Random Variable:

A random variable that takes **any value in a given range**.

Example: Height of students, time taken to complete a task