

# Smoothing seismicity techniques applied to seismic source characterization and probabilistic seismic hazard analysis in Brazil

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Intraplate seismicity is a hard problem to solve in tectonics. Brazil, as others intraplate environments, mainly during the lack of observed seismicity the seismic hazard assessment are also difficult and the methods applied are often close correlated to the geometries defined by the experts with valuable criteria.

Three smoothed seismicity techniques are reviewed and their application on construct models of Brazilian seismicity and its applications on long-term seismic hazard assessment in Brazil are also discussed. All these smoothing methods are based on a Kernel Density Estimation (KDE). The main difference between them is the bandwidth selection process.

The method proposed by *Frankel* [1995] uses a *fixed* bandwidth in space. *Woo* [1996] suggests a bandwidth as function of the *magnitude*. *Helmstetter and Werner* [2012] propose a *locally-adaptive* kernel bandwidths in space and time, chosen for each event as background (time-independent) model on their forecast experiments.

All these methods compute the seismicity rate surface in a binned space, time and magnitude, which able us to use this occurrence rate to define a grid of seismogenic point sources as the input source model to the hazard computation.

In addition, we used the information score and the error diagrams [*Kagan, 2009*] to evaluate the models, optimize the smoothing distance on the *Frankel [1995]* method, and finally give a weighted source models logic-tree to hazard computation.

All the hazard computations was performed on Openquake (OQ) [*Pagani et al., 2014*] open source software from Global Earthquake Model (GEM) Foun-

dation. No focal mechanism information has been included or considered on these smoothed seismicity models. All hazard computations has been done using a single ground motion prediction equation (GMPE). A more detailed study on GMPEs selection should be developed further and it is beyond the scope of this work.

The results shown that all methods clearly most of the well known seismogenic regions and could be used in the Brazilian seismicity modeling. All methods improve the spatial resolution of the GSHAP hazard model, the only previously available for the region. These results should be considered on future reviews of Brazilian design building codes and procedures.

## 1. Introduction

### 1.1. Intraplate seismicity and previous studies in Brazil

Brazil occupies a large stable continental region with seismicity rate lower than Central and Eastern North America, Australia, India or Northern Europe [Giardini *et al.*, 1999; Johnston, 1996]. Spanning most of the central region of the South American plate, Brazil has earthquakes above magnitude 6 mb with a return period of 50 years or so. Historical records are very short with almost no data before the XX century. Historical evidence of magnitude a 7 has been reported in the Amazon [Berrocal *et al.*, 1984; Veloso, 2014]. However, as in other intraplate settings, seismic hazard is not negligible due to the low seismic attenuation in the cold and thick lithosphere (magnitude 5 mb can be felt up to 500 km away [Assumpção *et al.*, 2014]) and special seismic hazard studies have been required for critical facilities such as nuclear power plants [Almeida *et al.*, 2013].

Very few studies related to seismic hazard, such as Berrocal *et al.* [1996] for SE Brazil, have been carried out so far and the first Brazilian seismic building code [ABNT, 2006] was based on the GSHAP [Giardini *et al.*, 1999] results for South America [Tanner and Shepherd, 1997; Shedlock and Tanner, 1999]. Brazilian seismicity is concentrated in several seismic zones [Berrocal *et al.*, 1984; Assumpção *et al.*, 2014]. Except for a peak of activity in Northeast Brazil, both the GSHAP model and the ABNT zoning have not taken into proper account some of the other highly active seismic zones, such as the Porto dos Gaúchos, Mato Grosso state, with recurrent activity since the occurrence of the largest recorded Brazilian event with magnitude 6.2 mb in 1955 [Barros *et al.*, 2009], or the Central Amazon region where concentration of events in the last 50 years is consistent with the location of the possible historical earthquake of magnitude 7 [Veloso, 2014]. For this reason, it is important to review and update the hazard estimates for

Brazil, especially since the increase in the number of recordings of Brazilian earthquakes in the last three decades.

Despite attempts to explain the origin of some of the seismic zones, such as stress concentrations from lithospheric thinning [Assumpção *et al.*, 2004; *de Azevedo et al.*, 2015] or flexural effects [Zoback and Richardson, 1996; Assumpção and Sacek, 2013], most of them have ill-defined boundaries. Attempts to produce seismic hazard maps [Dourado, 2014] based on seismogenic zones are heavily dependent on subjective expert opinion, even more so in low seismic areas such as Brazil. As a contribution to the new seismic hazard model for Brazil, here we briefly review recent methods of smoothing seismicity rates with application to Brazilian earthquakes.

## 1.2. Smoothed seismicity models

Although the standard *Cornell* [1968]-*McGuire* [1976] methodology often used to assess seismic hazard makes use of expert opinions to pre-defined seismogenic zones, one goal of this paper is to review a few smoothed seismicity methods based on KDE which results in a grid or a smoothed seismicity surface without define any seismic zone polygon (also known as *zoneless* approaches).

The (smoothed) seismicity KDE techniques allow us to define another grid of seismic point sources. The seismicity rate (*a*-value) associated to each source is defined by the smoothed seismicity methods.

To perform the KDE, both its shape and bandwidth needs to be defined. Most kernels are Gaussian, power-laws or one of their variants like Fisher kernels. The main distinction between the methods described here is the bandwidth selection process.

*Frankel* [1995] smoothing method applies a Gaussian *Nadaraya* [1964]-*Watson* [1964] kernel smooth technique with a *fixed smoothing-distance* bandwidth to estimate the

seismicity rate by smoothing the 2D histogram from earthquakes counting. The actual version of the algorithm is already implemented on the Hazard Modeller's Toolkit (HMTK) [Weatherill *et al.*, 2012; Weatherill, 2014] with a simple variant of Frankel's method discussed by Zechar and Jordan [2010] which sum the contribution of each earthquake kernel on given cell.

Woo [1996] proposes a *magnitude-dependent* kernel bandwidth based on the nearest neighbor mean distance in magnitude bins.

Helmstetter and Werner [2012] proposes a *locally-adaptive* bandwidth on both space and time dimensions for the background (time-independent) seismicity rate on their long-term forecasts experiments.

Using the long-term background seismic rate computed for forecast and assuming its time-independence, the same Probabilistic Seismic Hazard Analysis (PSHA) assumption, it is possible, preserving their purposes differences [Marzocchi and Zechar, 2011], to use these background seismicity rate values on seismic sources characterization [Weatherill and Pagani, 2014].

### 1.3. Information scores and error diagrams (ED)

From these three smoothing methods, only Helmstetter and Werner [2012] since its formalization use optimizations to define their model parameters. All the other methods are concept to use the whole catalog and some fixed parameter (e.g. Frankel's smoothing distance).

To compare the performance of these three models, the information scores and ED [Molchan and Kagan, 1992; Kagan, 2007, 2009] where computed as alternative to the tests suggested to the Regional Earthquake Likelihood Models (RELM) forecasts experiments by Schorlemmer *et al.* [2007].

On the evaluation phase all models learned from earthquakes into 1970-2004 observation time and were tested against the target realizations occurred between 2004 and 2014-01-01.

Scores from some Frankel-based models (from different smoothing distances) was computed and the best scores should give us an reasonable choice for this parameter.

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#### **1.4. Hazard computation**

To perform the hazard computation, the Openquake (OQ) suite [*Pagani et al.*, 2014] was chosen. The modeling tool was the HMTK also open available by Global Earthquake Model (GEM) scientific board. The Frankel method was already implemented on the toolkit and the other two was implemented in the context of this paper and they are free available on a public repository.

The other parameters, like  $b$ -values, minimum and maximum magnitudes for the frequency-magnitude distributions, strike, dip and rate probabilities to the rupture plane, its top and bottom limits on the subsurface, magnitude-area scale relationships and also the depth distributions must be assigned in other ways to proceed the hazard computation and take advantages of the new developed GMPEs.

In this work, to keep our focus on seismicity models as smoothed seismic sources, we perform hazard defining a single GMPE [EXPOSE WHICH ONE] for a stable continental crust tectonic environment.

The earthquake catalog data comes from the Brazilian seismological research authorities.

#### **1.5. Specific purposes**

The specific purposes of this paper are:

(i) review three distinct smoothing (zoneless) methods to spatially model the seismic rate, (ii) update the seismic hazard studies at national scale by proposing a new simple hazard model, (iii) use the GEM-OpenQuake tools to perform hazard calculation and (iv) add and share with the community two more new smoothing methods into the HMTK.

To aim this, the Brazilian seismicity data is presented including some overview plots. Next the method's theory is presented follow by the specific decisions and optimizations performed on each method modelling. And last, the results, conclusions and further considerations are discussed.

## 2. Brazilian seismicity data

Data on intraplate seismicity in Brazil is currently the Brazilian Seismic Bulletin maintained mainly by the Seismological Center of the University of São Paulo [BSB, 2014]. This catalog is a joint compilation from different sources.

### 2.1. Hypocenters

For events up to 1981, the catalog corresponds to *Berrocal et al.* [1984] which is a comprehensive compilation of historic and instrumental data with participation of Universidade de São Paulo (USP), Universidade de Brasília (UnB), Universidade Federal do Rio Grande do Norte (UFRN), Observatório Nacional (ON) and Instituto de Pesquisas Tecnológicas do Estado de São Paulo (IPT). From 1982 to 1995 the information comes from the annual bulletins published by Revista Brasileira de Geofísica. Since 1995, the Bulletin is maintained mainly by USP under the same cooperation network in addition to Universidade Estadual Paulista (UNESP). Earlier versions of this catalog were used to compose the well-known *CERESIS* [1985, 1995] catalogs.

Today the catalog is distributed in two ways. One, which could be called *raw*, contains all compiled information, such as: events outside the country which were felt in Brazil, errors in previous versions and also non-seismic events (known quarry blasts, sonic boom, etc). The other way could be called *clean*, where all non-seismic and low quality events were removed. This last one was used in this paper. There is 1941 earthquakes recorded from 1724 to the end of 2013.

This catalog only cover crustal events. Andean subduction earthquakes deeper than 50 km in the Brazil-Peru border was discarded as well earthquakes from the Mid-Atlantic ridge. The epicenters of the catalog are shown in figure 1.

## 2.2. Magnitudes

Most magnitudes were computed as  $mb$  type or the equivalent  $mR$  [Assumpção, 1983] regional magnitude. For historical events magnitudes were estimated from macroseismic data (felt area and maximum intensity) [Berrocal *et al.*, 1984]. Since most GMPE are based on  $M_W$  moment scale magnitude, in this present study, we converted all  $mb$  magnitudes to  $M_W$  values following the guidelines on table 1. REFERENCIA PARA STEPHANE/ASSUMPCAO WORK IN PROGRESS. (Johnston)

## 2.3. Catalog checking

Figure 2 shows the distribution of depths, day of the week and origin hour following *Gulia et al.* [2012]. Most events have no depth determination and the well determined depths (from  $pP$  phases or local networks) are mostly less than 10km.

Figures 2b and 2c show an almost uniform distribution of day of the week, and a slightly trend to record earthquakes during the night. This could suggest some influence of daily noise level.

The annual number of earthquakes since 1900 (figure 3) shows a steady increase since 1960 and two peaks in 1986 and 1998 derived from two large seismic sequences: João Câmara [Takeya *et al.*, 1989] and Porto dos Gaúchos [Barros *et al.*, 2009]. The increasing number of records after 1960 is due to the operation of global, regional and local stations.

## 2.4. Declustering procedures

To preserve the Poissonian assumption about the independence of the events, several declustering algorithms were tried and the results as shown in figure 4a. The window-method [Gardner and Knopoff, 1974] was tested with three different windows: Gardner and Knopoff [1974], Uhrhammer [1986] and Grüenthal [van Stiphout *et al.*, 2012]. In addition the algorithm (AFTERAN) proposed by Musson [1999] was also tested using Grüenthal distance window.

In the case of Brazilian catalog the methods did not present large differences at the final number of earthquakes (fig. 4a) and the Gardner-Knopoff/Uhrhammer combination was chosen to maximize the number of events.

The map of figure 4b locates all clusters in the catalog. It is an *a-priori* evidence of regions in Brazil where long earthquake series tend to occur more frequently.

## 2.5. Frequency-magnitude distribution

Figure 6 presents the catalog Magnitude Frequency Distribution (MFD). A general  $b = 1$  fit is also plotted, and the completeness magnitude on the incremental distribution is about 3.0.

## 2.6. Catalog completeness

The completeness of Brazilian seismicity data has evident time and space dependence. Brazil just recently was installed its permanent seismic network [Pirchiner *et al.*, 2011]. The number and quality of stations increased over time. The population density,

previously concentrated along the coast increased in other regions changing the historical detectability.

There are many methodologies to assessment of the temporal and spatial completeness [Stepp, 1972; Mignan and Wöessner, 2012; Ogata and Katsura, 1993; Wiemer and Wyss, 2000; Cao and Gao, 2002; Stucchi et al., 2004; Woessner and Wiemer, 2005; Mignan et al., 2011; Mignan, 2012; Vorobieva et al., 2013; Mignan et al., 2013; Nasir et al., 2013; Mignan and Chouliaras, 2014], or explaining how to compute the real Probability of Detecting an Earthquake (PDE) from the waveforms [Schorlemmer and Woessner, 2008], but the time and the effort to proceed this exhaustive study of the completeness magnitude, despite its relevance, was not intended to be done on the scope of this paper.

The waveforms from the earliest years was not in digital form. The histories of most regional (temporary) stations are not easy available. In addition, the low number of earthquakes in the catalog also difficults some high resolution statistical methods. All of this hinders the direct application of most that methodologies.

For this reason, the spatial completeness was not considered and the temporal completeness parameters for the whole country was defined by an easy cumulative rate criteria using historical information about the network evolution and the *Stepp* [1972] plot (fig. 5a). TALK ABOUT BRASILIA STATION???

Figure 5b shows the magnitude time distribution in a scatter plot as the cumulative number of events which is important to perform the temporal course of earthquake frequency (TCEF) [Nasir et al., 2013]. The linear behavior of cumulative rate on the recent years, gives an idea about the constant record trend. Figure 5b also show three (from many) possible completeness tables to allow quick check their distinctions. We chosen the “simplest” one.

#### IMPROVE THIS DECISION EXPLANATION

### 3. Smoothing methods

Three smoothing methods are now briefly explained.

#### 3.1. Frankel: fixed bandwidth

*Frankel* [1995] smoothing seismicity proposal consisted originally in using a “correlation distance”  $d_F$  as the *fixed* kernel bandwidth and applying the Nadaraya-Watson [*Nadaraya*, 1964; *Watson*, 1964] estimator to smooth a 2D seismicity histogram using a Gaussian kernel:

$$\tilde{n}_j = \frac{\sum_i n_i e^{-\left(\frac{d_{ij}}{d_F}\right)^2}}{\sum_i e^{-\left(\frac{d_{ij}}{d_F}\right)^2}}, \quad (1)$$

where  $\tilde{n}_j$  is the smoothed seismicity (number of earthquakes with magnitude  $m$  above the minimum magnitude  $M_d$  in the catalog) on cell  $j$ .  $n_i$  is the earthquake counting in each other cell  $i$  and  $d_{ij}$  is distance between grid cells  $i$  and  $j$ .

#### 3.2. Woo: magnitude-dependent bandwidth

*Woo* [1996] suggested to evaluate the contribution of each earthquake  $i$ , located at  $\mathbf{r}_i$ , to the seismicity rate  $R$  (number of earthquakes per year and unity area) on the cell centered in  $\mathbf{r}$ , depending on the magnitude  $m$ :

$$R(\mathbf{r}, m) = \sum_{i=1}^N \frac{K(\mathbf{r} - \mathbf{r}_i, m)}{T(\mathbf{r}_i)}, \quad (2)$$

where  $N$  is the number of earthquakes  $i$  in the magnitude bin  $m \pm dm$ , and  $T(\mathbf{r}_i)$  is the completeness time of magnitude  $m$  observed on  $\mathbf{r}_i$ .

Any kernel could be applied on that definition. I used used the *Kagan and Knopoff* [1980] kernel for infinite spatial domain as described by *Woo* [1996]:

$$K_{KK}(\mathbf{r}, m | a_W) = \frac{a_W - 1}{\pi h(m)^2} \left[ 1 + \frac{\mathbf{r}^2}{h(m)^2} \right]^{-a_W}, \quad (3)$$

where  $a_W$  is fractal dimension factor, generally about 1.5 and 2 [*Vere-Jones*, 1992].

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To compute the magnitude-dependent bandwidth function  $h(m)$ , *Woo* [1996] suggested the follow relation

$$h(m|a_0, a_1) = a_0 e^{a_1 m}, \quad (4)$$

where  $a_0$  and  $a_1$  are computed by the regression of the mean nearest distance  $h$  from each magnitude bin  $m \pm dm$ , as illustrated on figure 7.

Just to compare, in figure 7 it is shown the functions computed by *Beauval* [2003] for Norway and Spain. The angular coefficient ( $a_1$ ) is in the same range of the others but the general mean distance between events into the same magnitude bin is higher than other countries. It is in some way expected. Brazil is quite large than mentioned countries.

### 3.3. Helmstetter and Werner: locally-adaptive space and time bandwidths

Even work on a forecast perspective, the background seismicity rate for a long-term time-independent forecast could be used to characterize a diffused seismicity under the common assumption that this background seismic rate is invariant over time.

*Helmstetter and Werner* [2012] proposes a seismicity model space and time dependent using kernels for space and time independently:

$$R(\mathbf{r}, t) = \sum_{i=1}^N \frac{1}{h_i d_i^2} K_t \left( \frac{t - t_i}{h_i} \right) K_r \left( \frac{\|\mathbf{r} - \mathbf{r}_i\|}{d_i} \right), \quad (5)$$

where  $R(\mathbf{r}, t)$  is the seismic rate located  $\mathbf{r}$  distant from the earthquake occurred on the instant  $t$ ,  $K_t$  is the time domain kernel function, where  $t_i$  is the time location of earthquake  $i$  and  $h_i$  is the temporal bandwidth for earthquake  $i$ ,  $K_r$  is the space domain kernel function, where  $\mathbf{r}_i$  is the spatial location of earthquake  $i$  and  $d_i$  is the spatial bandwidth for earthquake  $i$ .

As they are interested in forecast, just past time  $t_i < t$  need to be considered. Also the observation completeness is taken in account by a set of weights  $w$  in this follow way:

$$R(\mathbf{r}, t) = R_{min} + \sum_{t_i < t} \frac{2 w(\mathbf{r}_i, t_i)}{h_i d_i^2} K_t \left( \frac{t - t_i}{h_i} \right) K_r \left( \frac{\|\mathbf{r} - \mathbf{r}_i\|}{d_i} \right), \quad (6)$$

where  $R_{min}$  is the minimum seismic rate, positive, allowing earthquakes to occur where their never occurred yet.

The weights  $w(\mathbf{r}_i, t_i)$ , computed for each earthquake  $i$ , are the Gutenberg-Richter  $a$ -value projection. This is the expression used to compute it:

$$w(\mathbf{r}, t) = 10^{b(\mathbf{r}, t)[M_c(\mathbf{r}, t) - M_d]}, \quad (7)$$

where  $w$  is the weight factor computed on location  $\mathbf{r}$  on instant  $t$ ,  $b(\mathbf{r}, t)$  is the space and time dependent b-value,  $M_c(\mathbf{r}, t)$  is the completeness magnitude on location  $\mathbf{r}$  and  $t$ ,  $M_d$  is the minimum magnitude value on the catalogue.

These weights increase the seismicity contribution from earthquakes occurred where and when the completeness magnitude  $M_c$  was greater than minimum catalog magnitude  $M_d$ . They also could easily take into account the space and time completeness and  $b$ -value fluctuations.

### 3.3.1. Local bandwidth computation

The method implemented to compute the space and time bandwidths for each earthquake was the Coupled-Nearest-Neighbor (CNN) [Helmstetter and Werner, 2012] expressed as:

$$h_i, d_i = \arg \min_{\substack{h_i \geq h_k \\ d_i \geq d_k}} [s(h_i, d_i | k_{cnn}, a_{cnn}) := h_i + a_{cnn}d_i], \quad (8)$$

where  $k_{cnn}$  is the  $k^{th}$  nearest neighbor,  $a_{cnn}$  is a space-time coupling factor,  $d_k$  is the  $\max \{d_j\}, j = 1, \dots, k_{cnn}$  and  $h_k$  is the  $\max \{h_j\}, j = 1, \dots, k_{cnn}$ .

The bandwidths are defined locally by this simple optimization process. It could be small on high earthquake density regions and higher where earthquakes are rarely or regions with information lack.

### 3.3.2. Stationary seismic rate

After compute the model parameters it is completely defined, and the time-independent or stationary seismic rate  $\bar{R}$  on each location  $\mathbf{r}_0$  can be computed on the way proposed by *Helmstetter and Werner* [2012] taking the median value for some location  $\mathbf{r}_0$  over all considered time window:

$$\bar{R}(\mathbf{r}_0) = \text{Median}[R(\mathbf{r}_0, t)]. \quad (9)$$

The median should avoid the seismicity rate fluctuations derived by fore and aftershocks and consequently the decluster procedures. This is one of the most important achievement of this methodology.

### 3.3.3. Maximum likelihood optimization

The model is completely defined by  $k_{cnn}$ ,  $a_{cnn}$  and  $R_{min}$ . To optimize these parameters the catalog is divided in two parts: one for *learning* about the parameters and other to test them. The *testing* catalog will able us to check the model prediction performance derived from its chosen parameters. The best model parameters will maximize the prediction model capacity likely the target catalog.

If the earthquake occurrence could be modeled by a Poisson process with rate  $N_p$ , then the probability to observe exactly  $n$  events on the considered time frame is

$$p(N_p, n) = \frac{N_p^n e^{-N_p}}{n!}. \quad (10)$$

Then, over all cells, the log-likelihood, to be maximized, between model prediction (from the learning catalog) and the observed earthquakes (on the testing catalog) is

written as

$$L = \sum_{i_x=1}^{N_x} \sum_{i_y=1}^{N_y} \log p [N_p(i_x, i_y), n(i_x, i_y)] \quad (11)$$

where  $N_p(i_x, i_y)$  is the predicted seismic rate on cell  $(i_x, i_y)$  and  $n(i_x, i_y)$  is the number of target earthquakes observed on cell  $(i_x, i_y)$ .

The model parameters  $R_{min}$ ,  $a_{cnn}$  and  $k_{cnn}$  should be optimized by the maximization of log-likelihood  $L$ .

## 4. Results

### 4.1. Simulations

#### 4.1.1. Simulation 1

## 5. Discussion

### Appendix A: Appendix Title

**Acknowledgments.** The author thanks specially to all IAG-USP seismological team. It is also grateful to Stéphane Drouet and Vincent Guigues for all helpful discussions.

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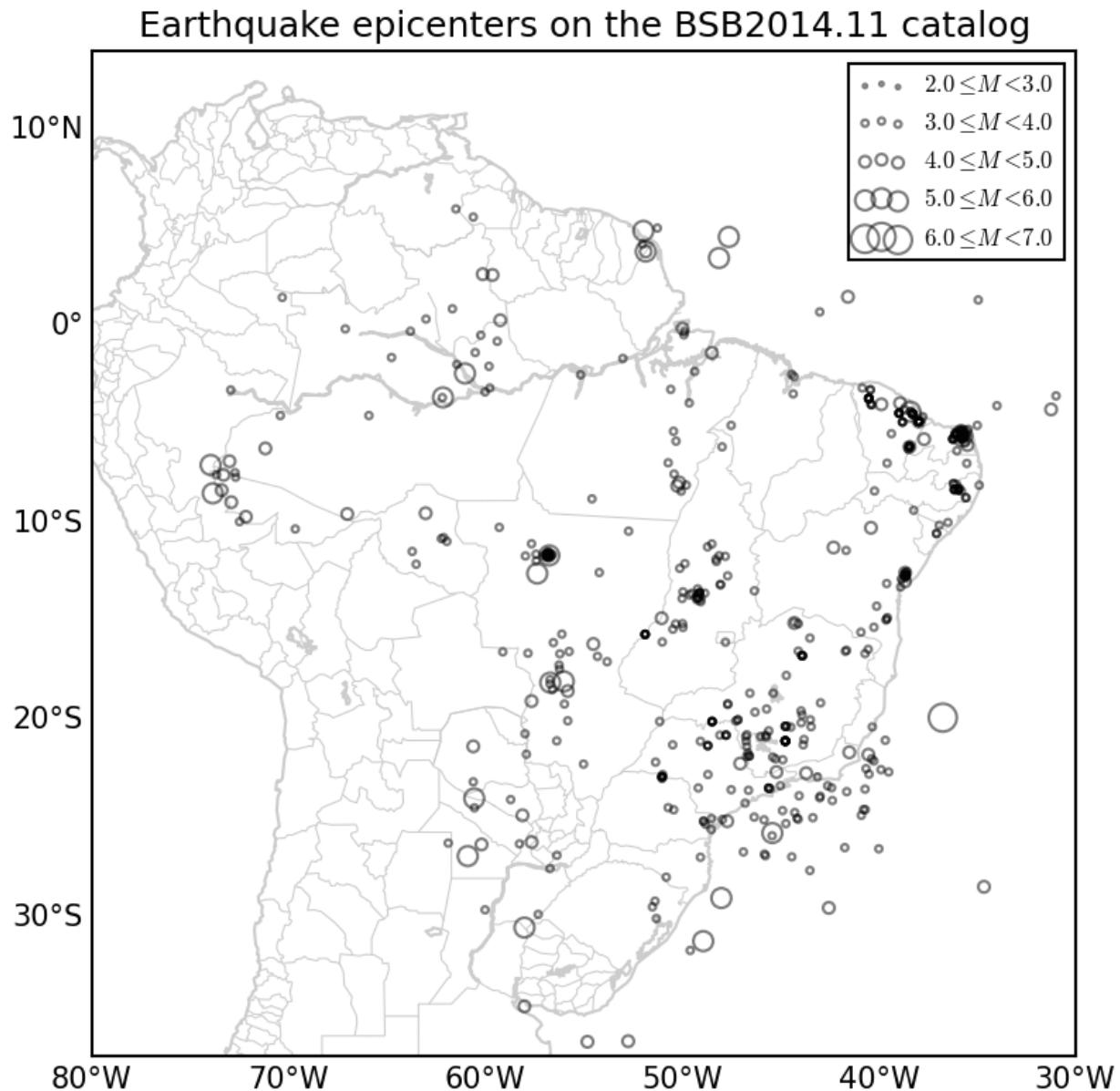
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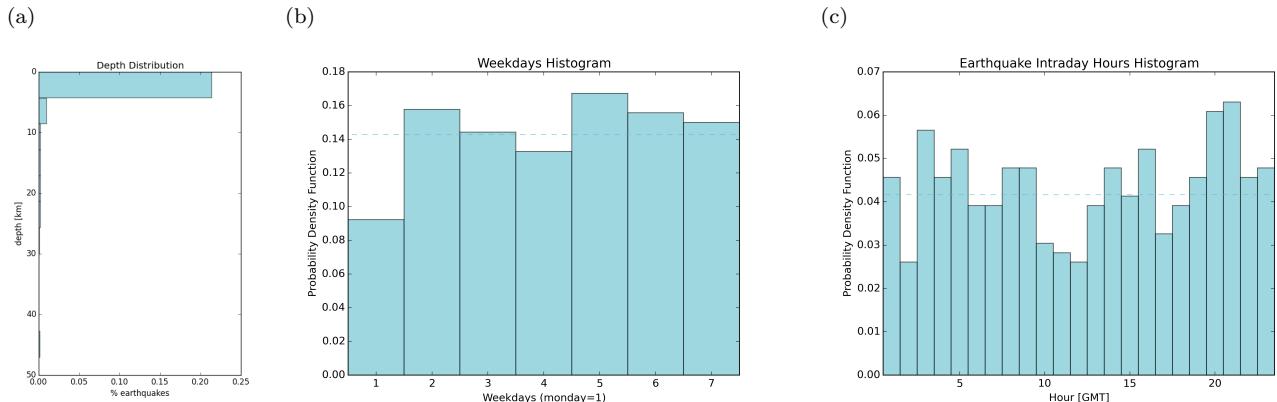
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**Figure 1.** Brazilian seismicity from 1767 to 2014. Source: [BSB, 2014].

**Table 1.** BSB 2014.11  $M_W$  proxies *ad-hoc* guidelines.

magnitude source	rule	uncertainty
$mb$ or $mR$	$M_W(m) = 1.121m - 0.76$	0.3
Felt area $A_f$	$M_W(A_f) = 0.81 + 0.639 \log(A_f) + 0.00084\sqrt{A_f}$	0.4
Maximum intensity $I_0$	$mb(I_0) = 1.21 + 0.45I_0$ then $M_W(m)$	0.6
$mb$ and $A_f$	$M_W(m, A_f) = 0.7M_W(m) + 0.3M_W(A_f)$	0.33



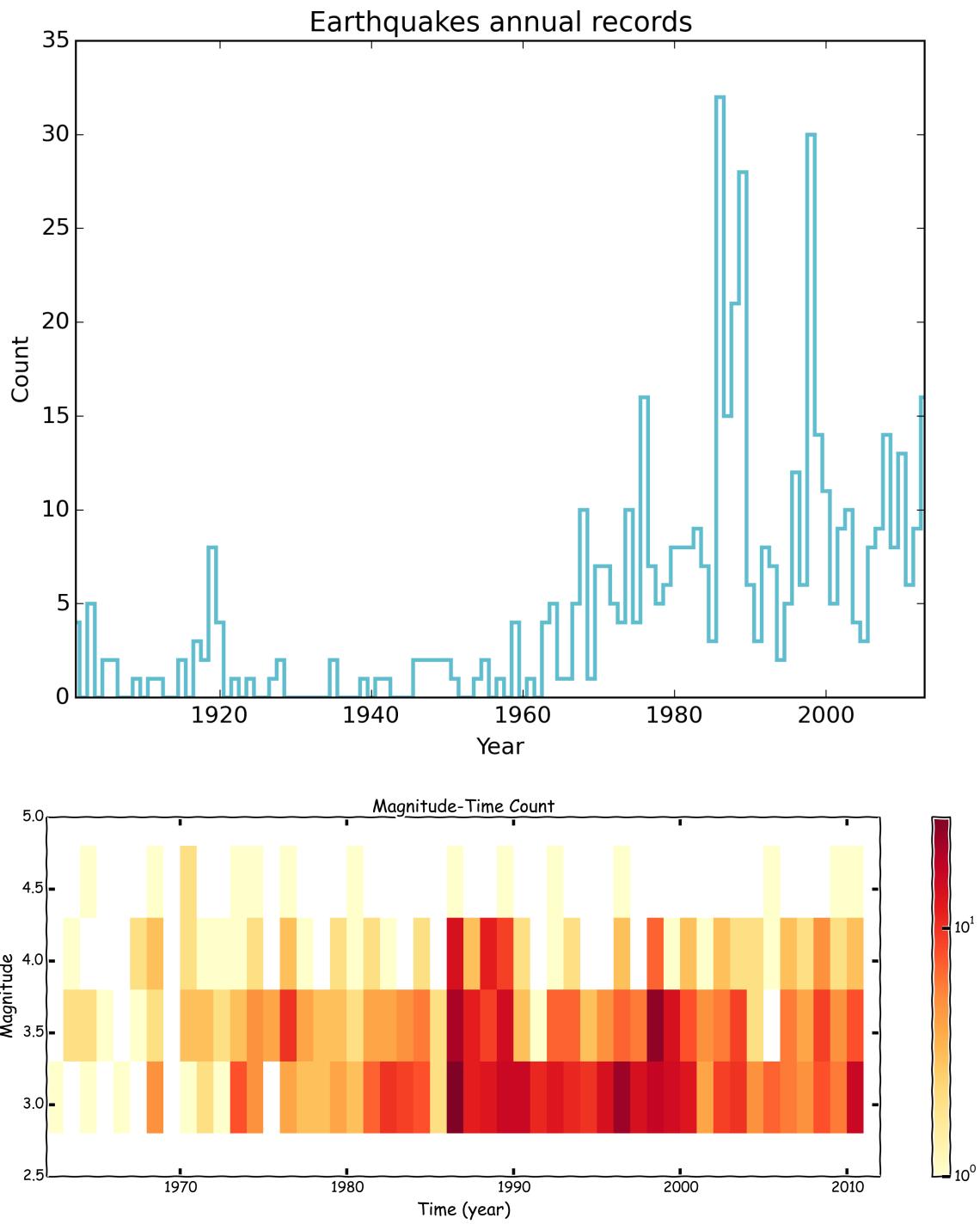
**Figure 2.** Catalogue overview. The histogram (a) shows the depth distribution. The histograms (b) and (c) represent the distributions of weekday and hour which earthquakes occur respectively. Dashed lines represent the mean value.

**Table 2.** Temporal completeness. For each magnitude interval, the completeness was computed by the *Stepp* [1972] method.

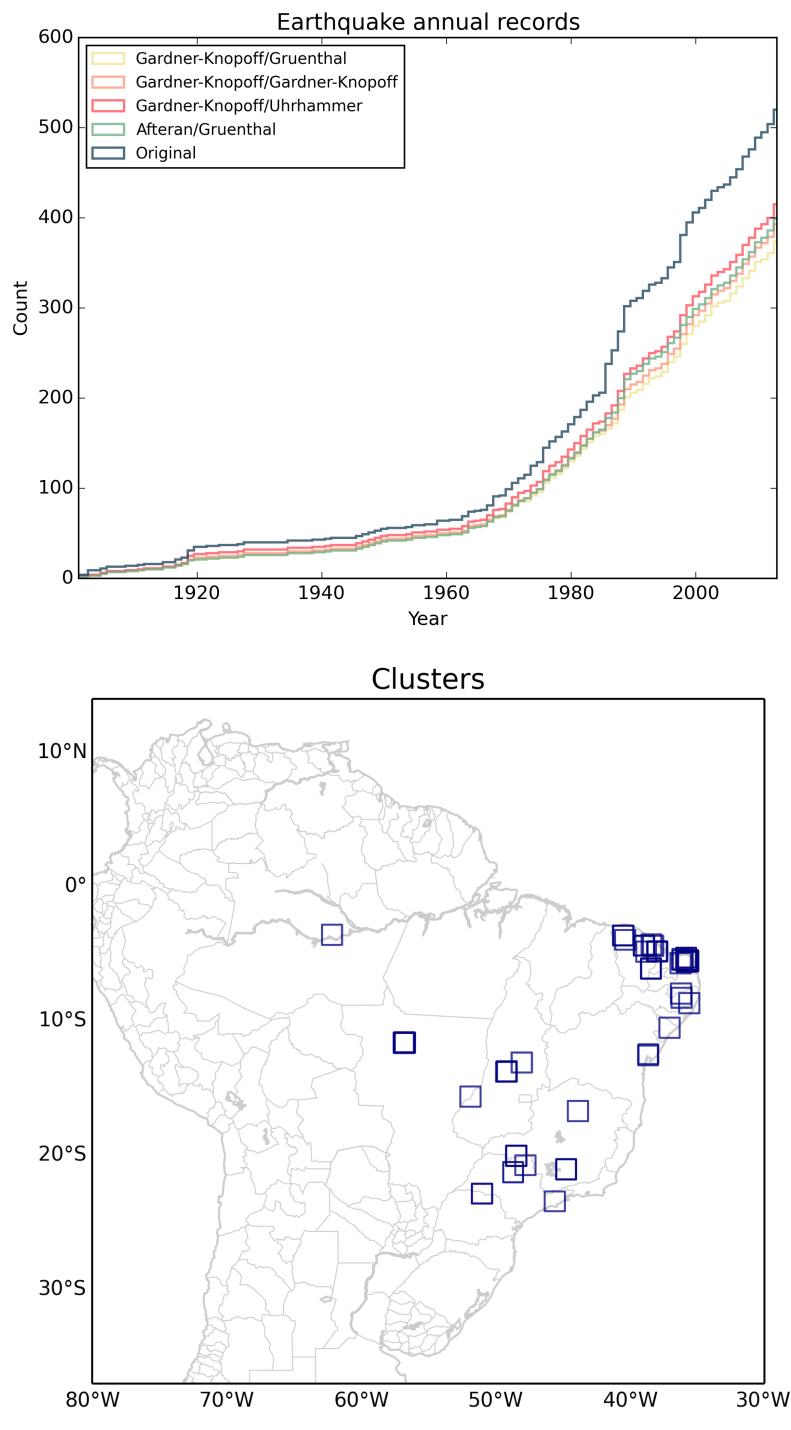
magnitude	year (Stepp)
3.0	1970
4.0	1959
4.5	1951
6.0	1933

**Table 3.** Temporal completeness. For each magnitude interval, the completeness comes from *Assumpção et al.* [2014] converted to  $M_W$  from  $m_b$  following table 1.

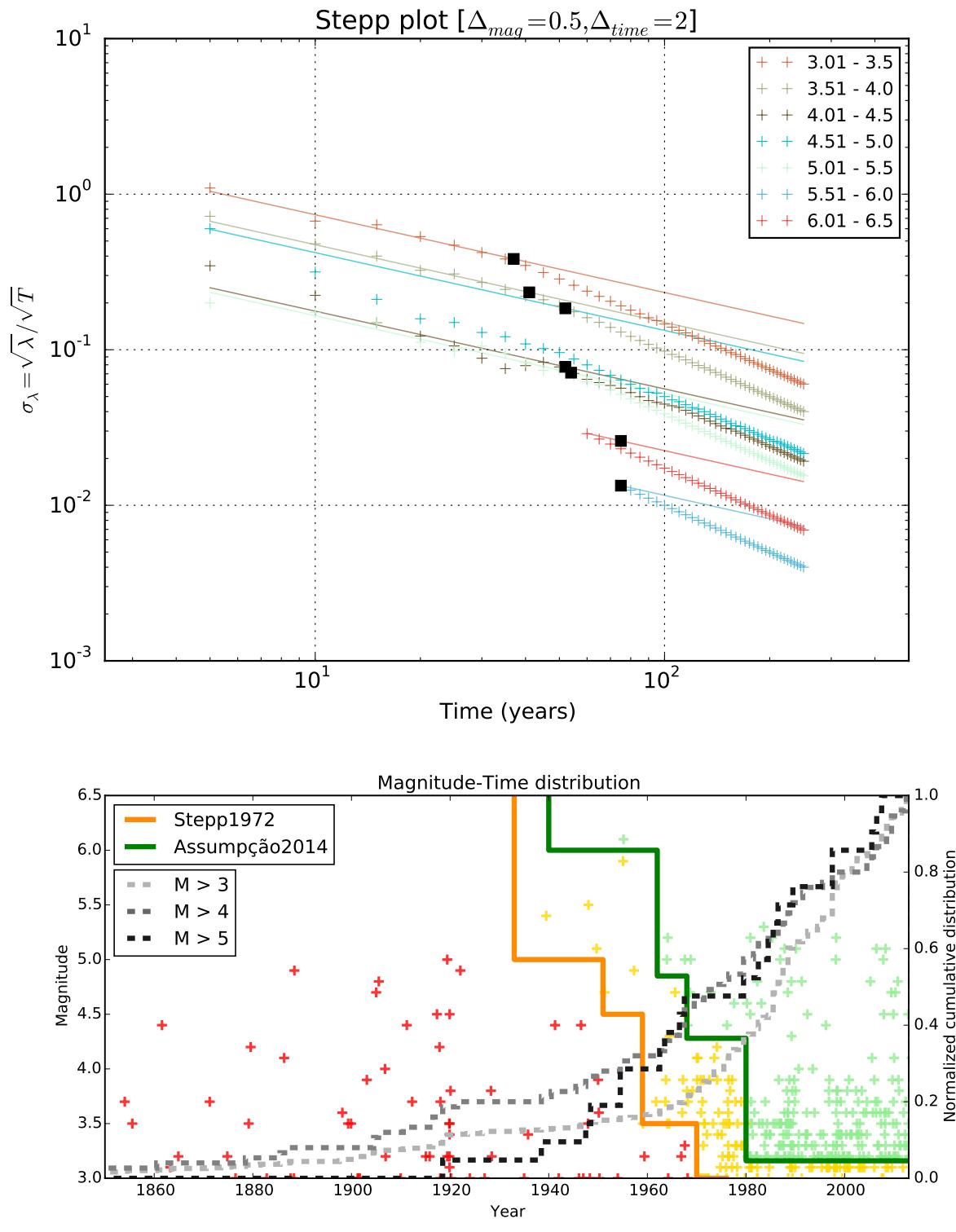
magnitude	year (Assumpção)
3.1	1980
4.3	1968
4.8	1962
6.0	1940



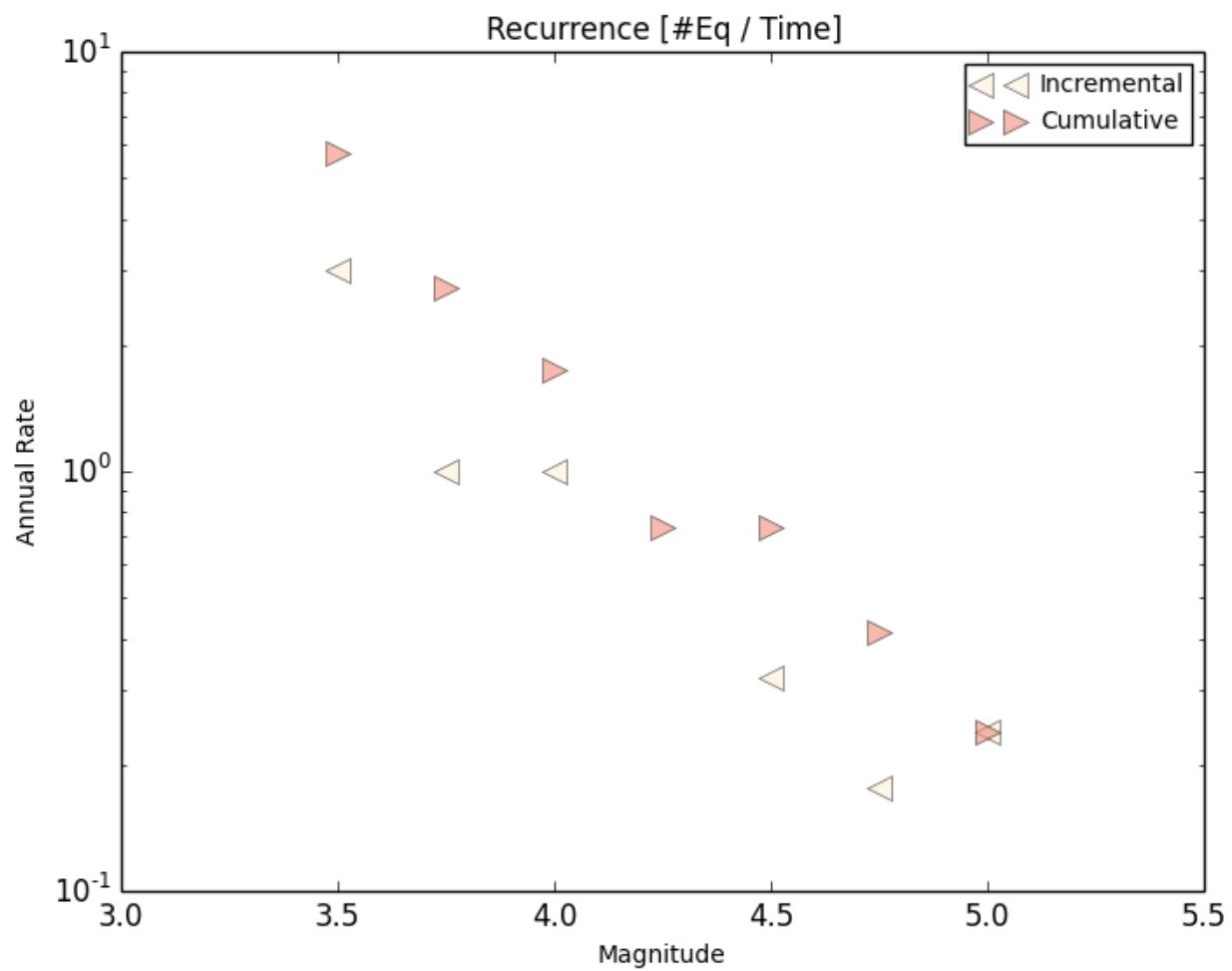
**Figure 3.** Earthquakes by year (a) and discriminated by magnitude (b).



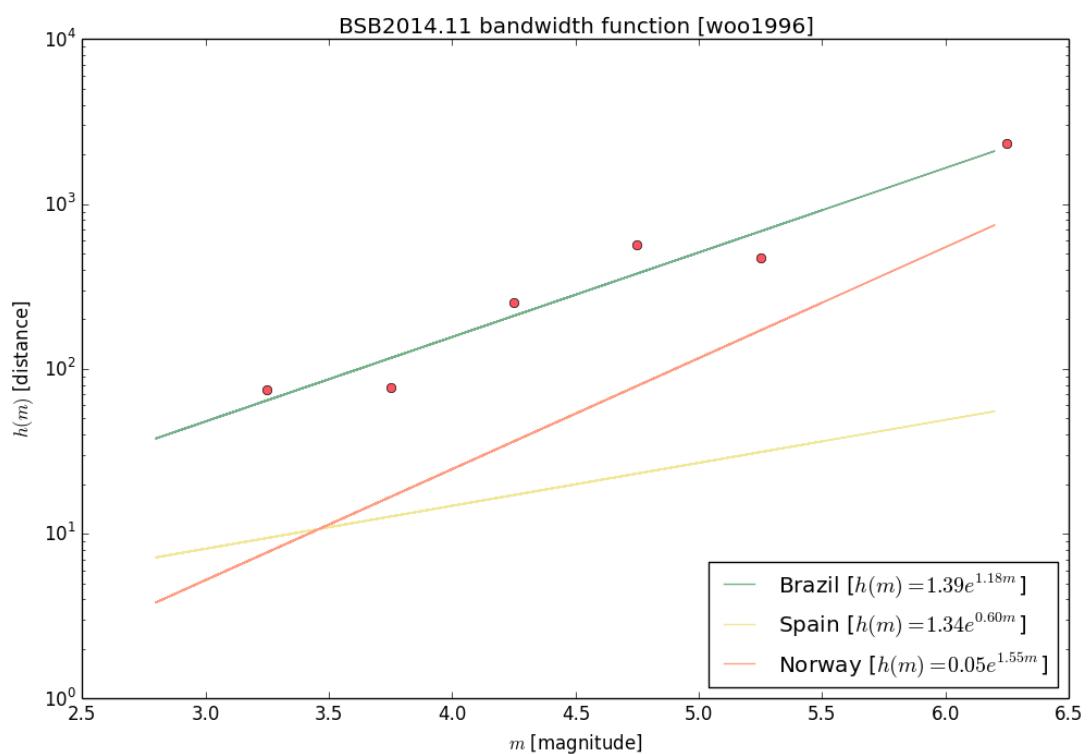
**Figure 4.** Decluster evaluation (a) using distinct algorithms and windows. There is no significant differences between final results. The map (b) of clusters from selected method shows places where earthquake sequences tends to occur more frequently.



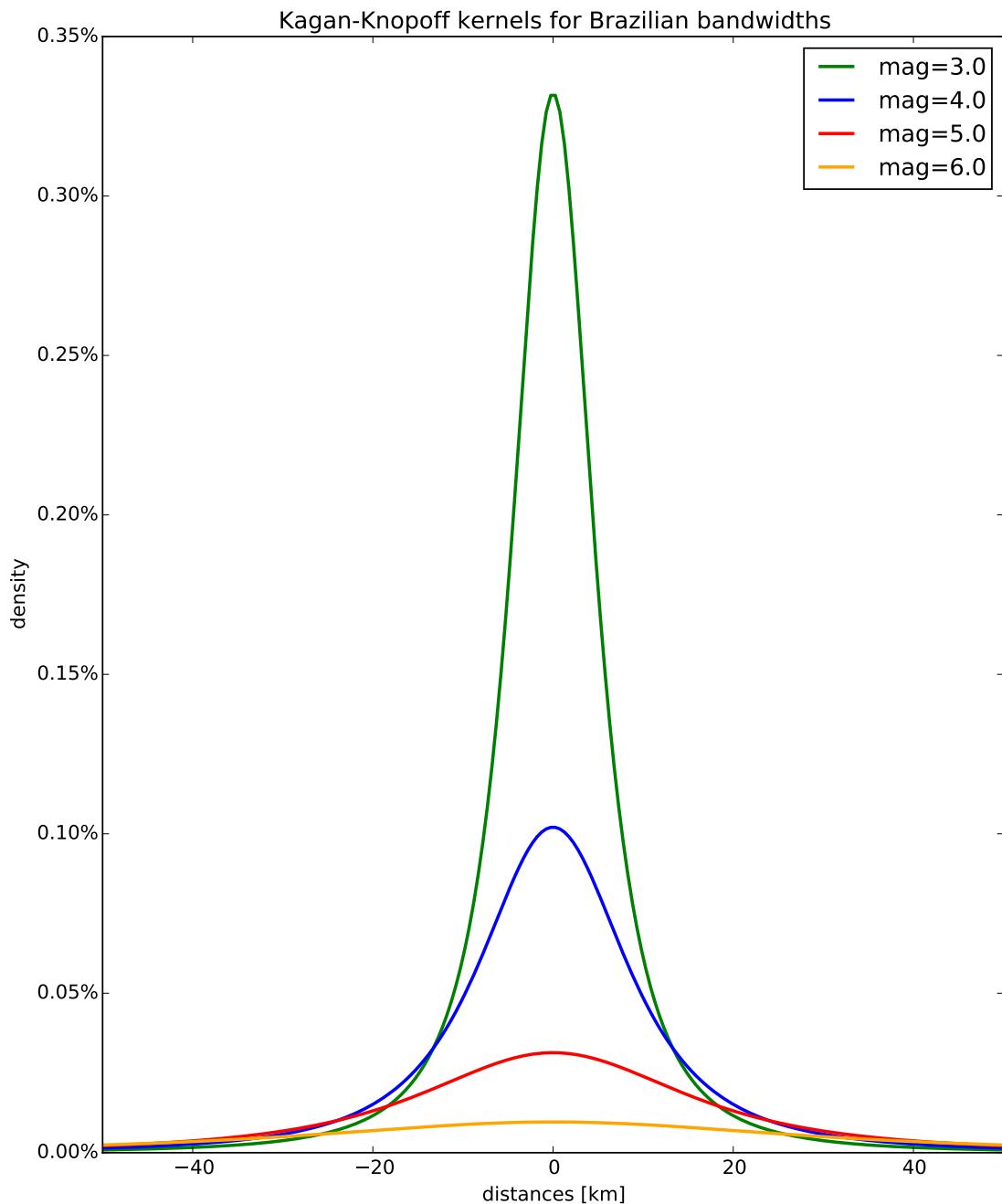
**Figure 5.** Completeness evaluation. The Stepp plot (a) was made using  $\Delta_{mag} = 0.5$  and  $\Delta_{time} = 2$  as magnitude and time bins. The magnitude-time scatter plot (b) shows in addition, three different temporal completeness models and some cumulative rates to better perform a visual analysis.



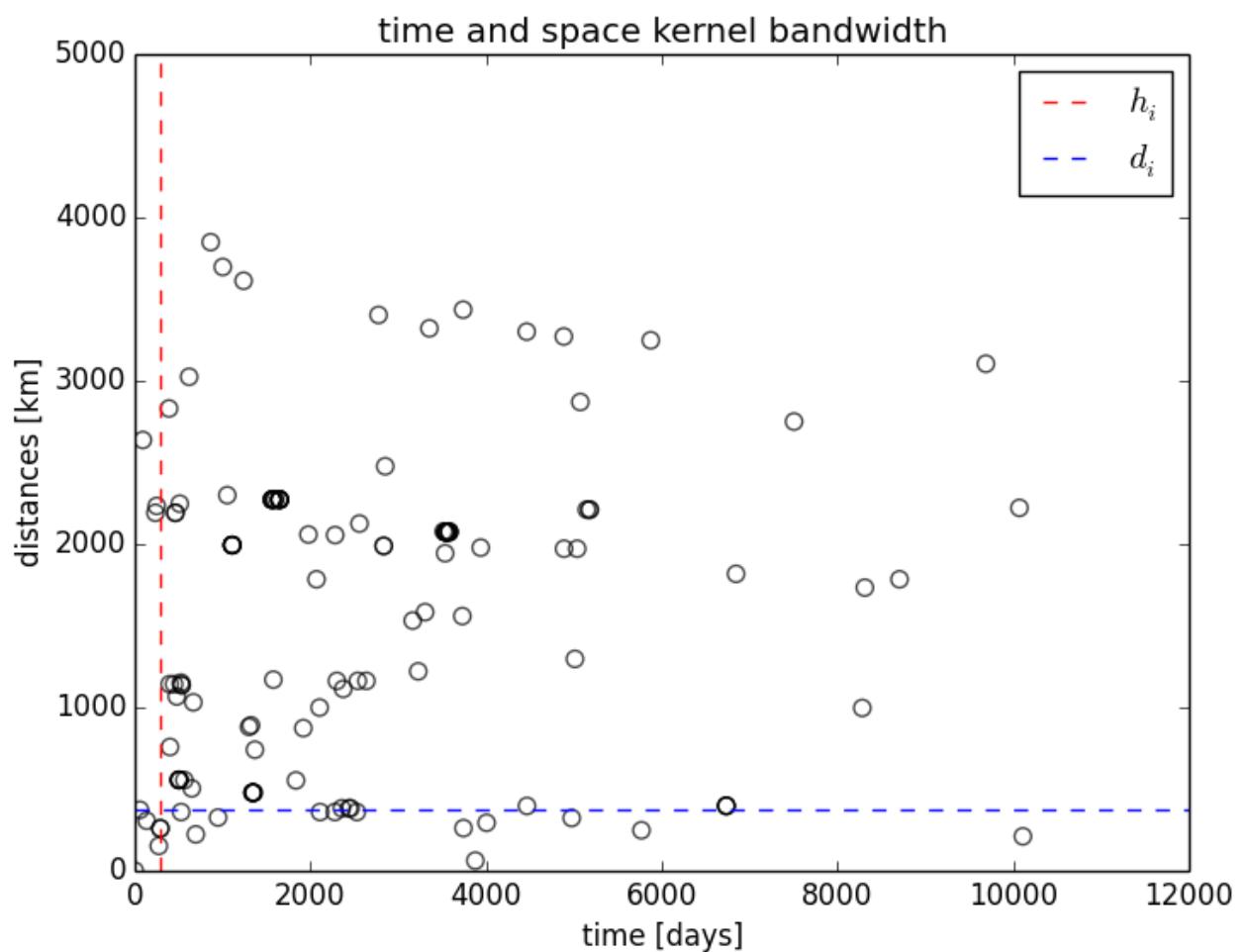
**Figure 6.** Annual earthquake recurrence.



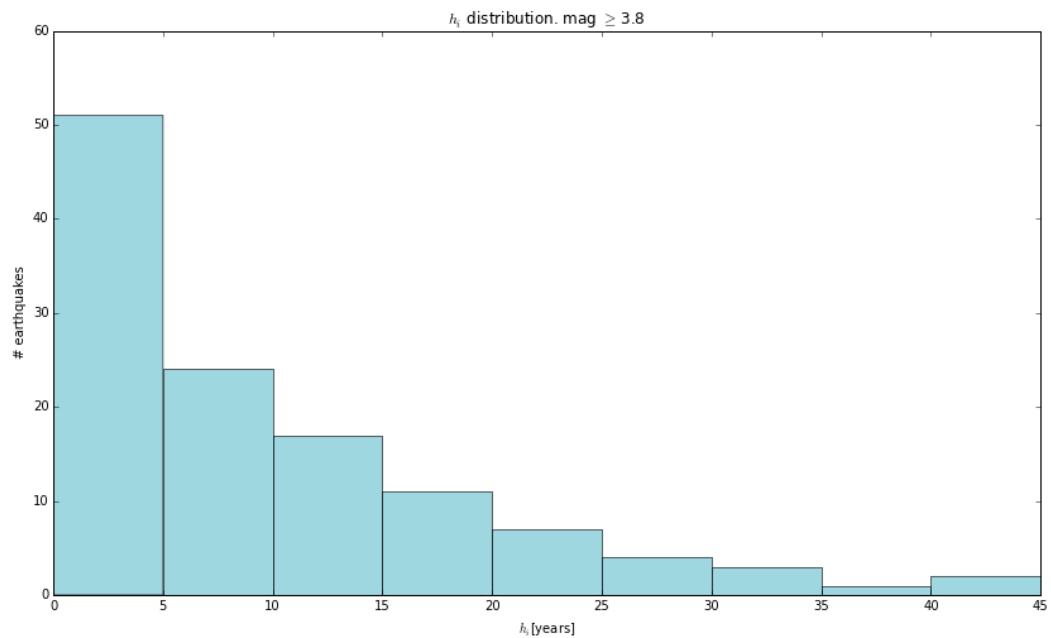
**Figure 7.** Magnitude dependence bandwidth.



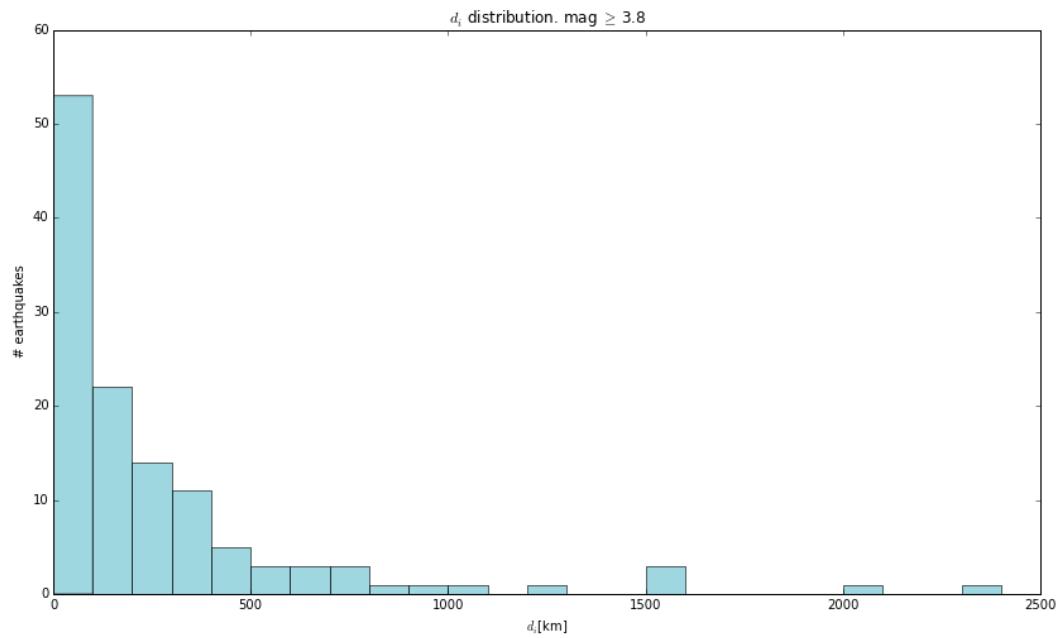
**Figure 8.** *Kagan and Knopoff* [1980] kernel shapes for some magnitude values.



**Figure 9.** Local bandwidth example.

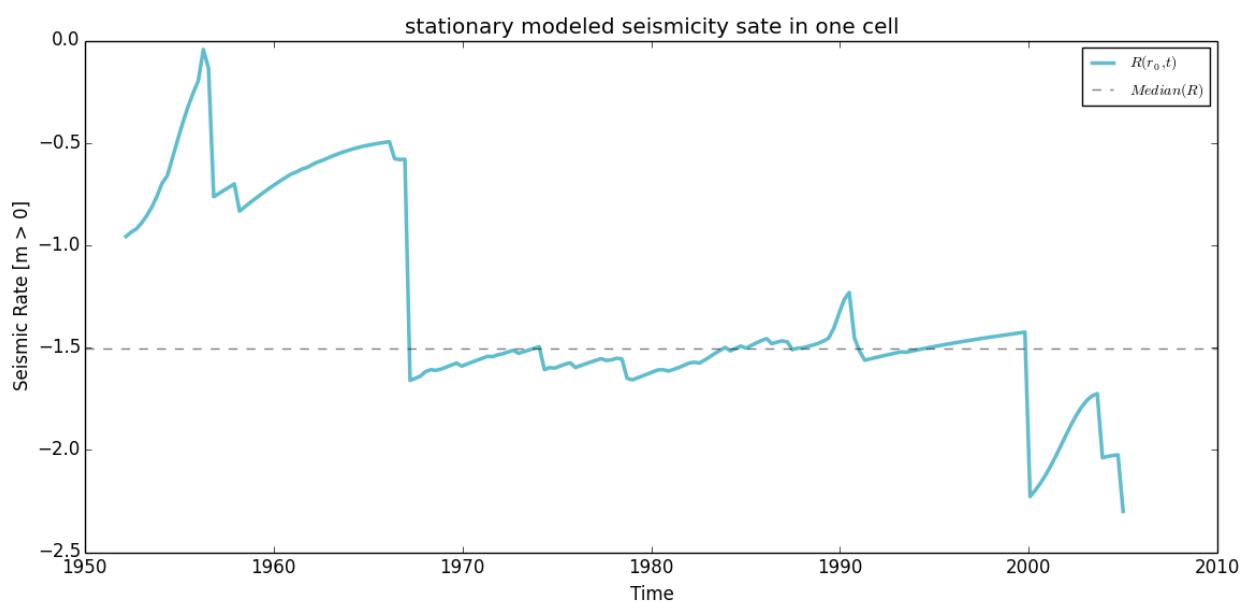


(a)



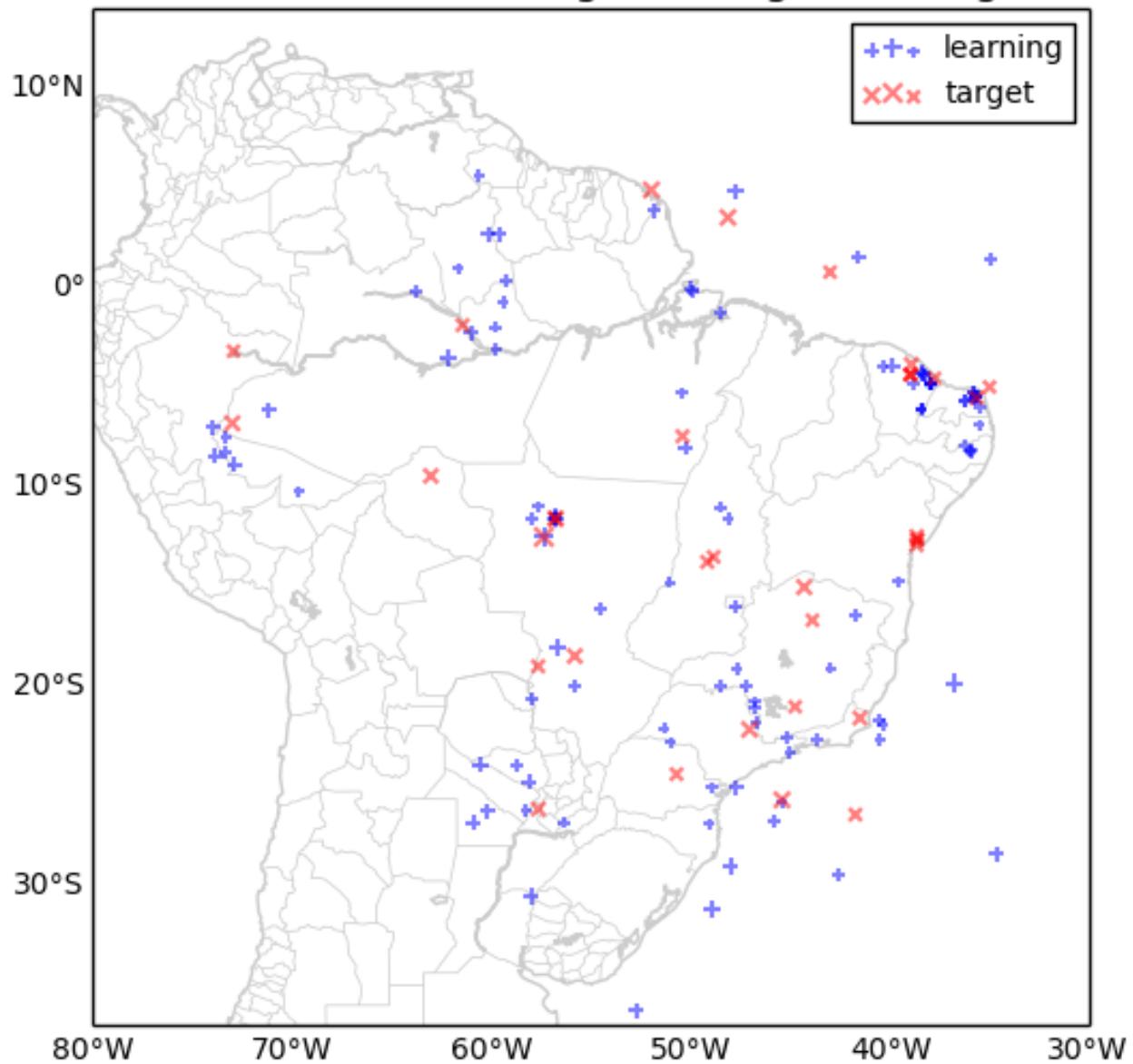
(b)

**Figure 10.** (a)  $h_i$  and (b)  $d_i$  distributions from BSB.

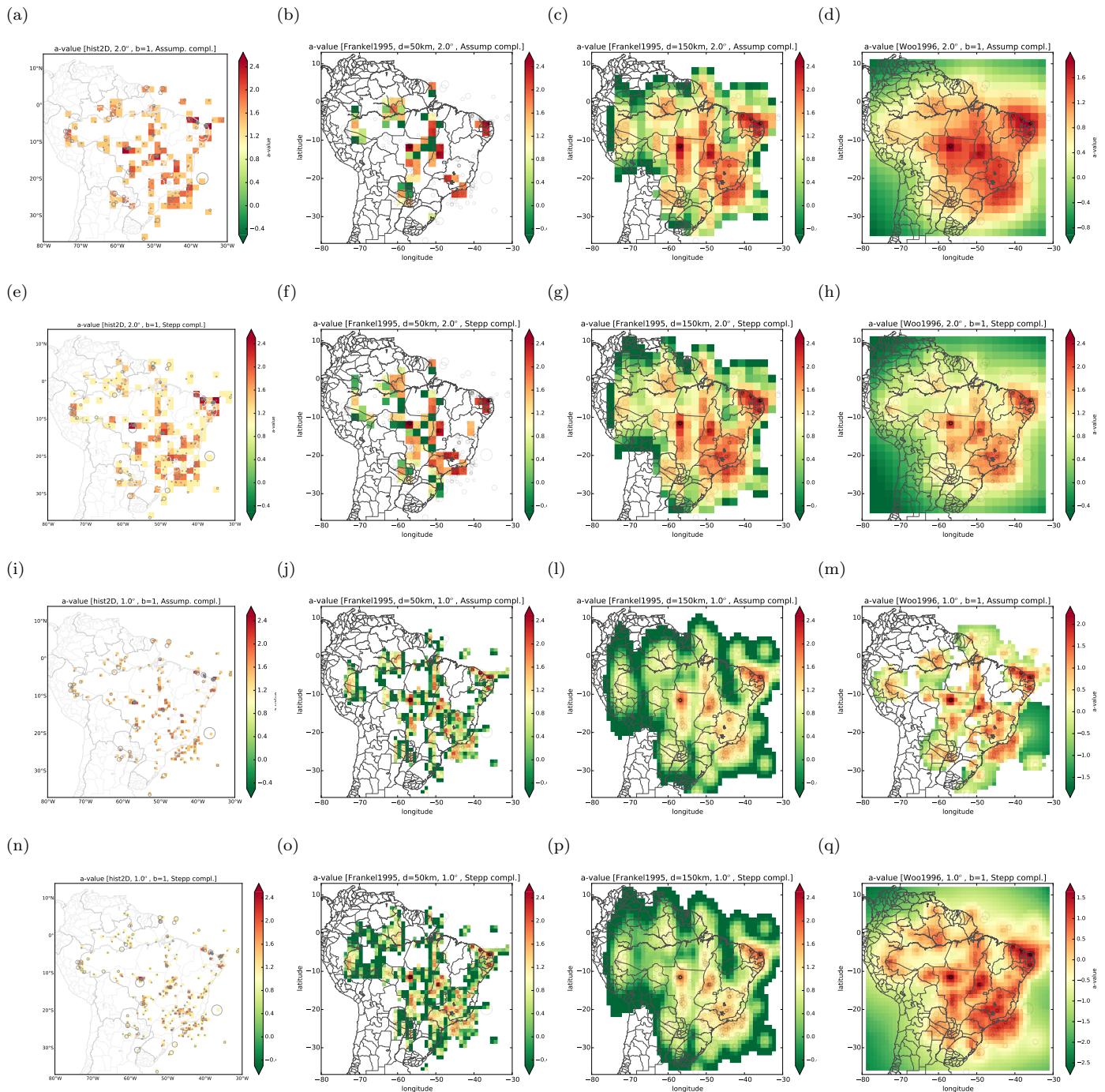


**Figure 11.** Stationary seismic rate

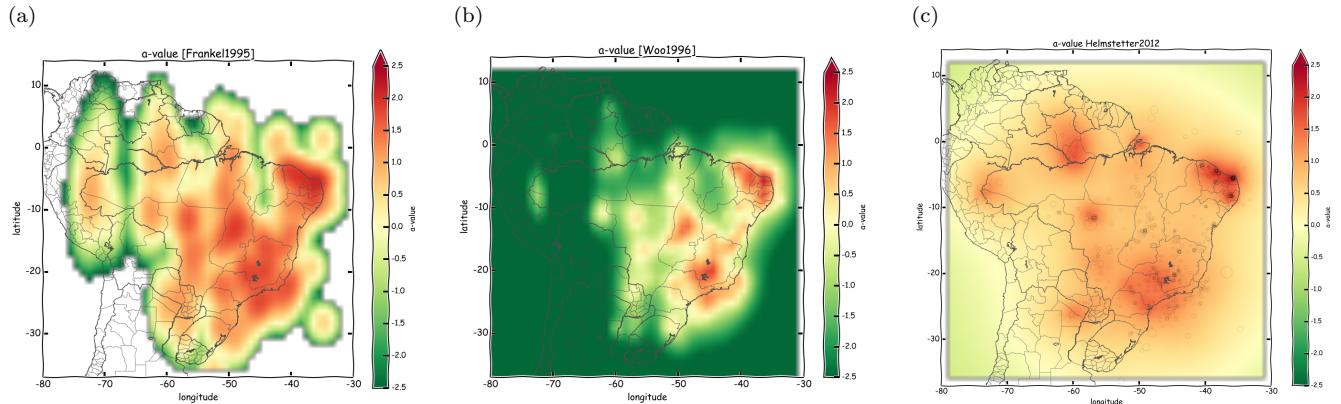
### BSB2014.11 learning and target catalogs



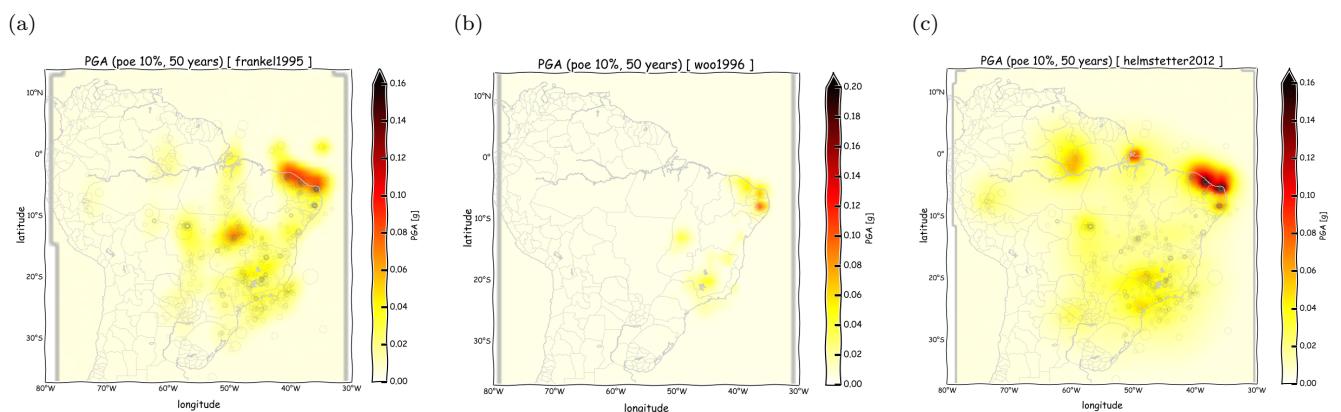
**Figure 12.** Learning and testing catalogs.



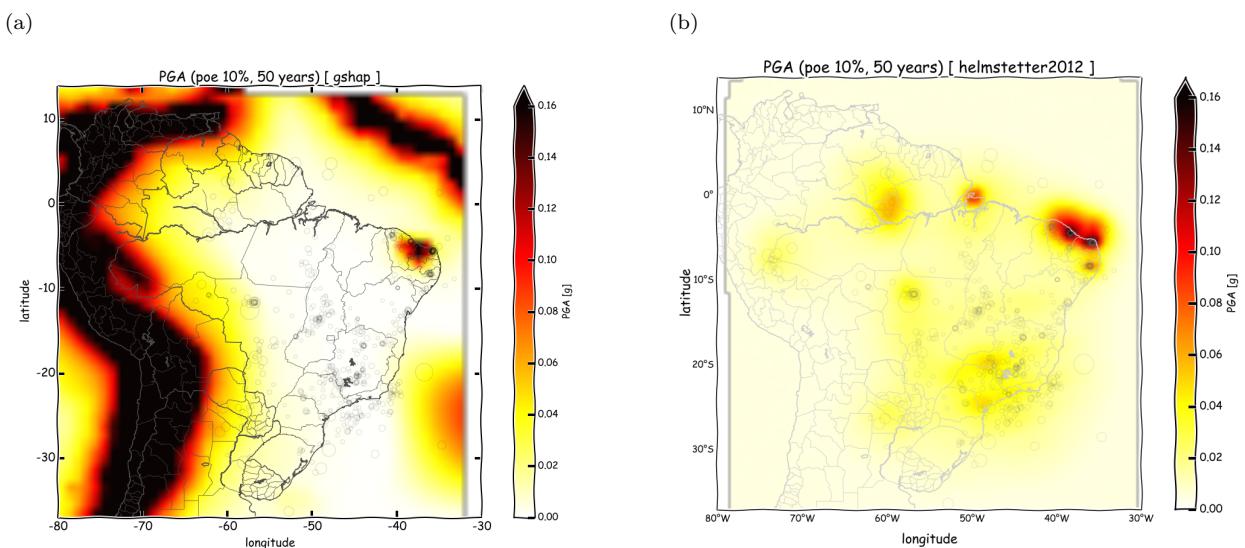
**Figure 13.** Smoothed rates comparission: (a) shows *Frankel* [1995] method smoothed rate results, (b) and (c) represent rates smoothed by *Woo* [1996] and *Helmstetter and Werner* [2012] methods respectively.



**Figure 14.** Smoothed rates comparission: (a) shows *Frankel* [1995] method smoothed rate results, (b) and (c) represent rates smoothed by *Woo* [1996] and *Helmstetter and Werner* [2012] methods respectively.



**Figure 15.** PGA (poe 10%/50y) comparission for (a) *Frankel* [1995], (b) *Woo* [1996] and (c) *Helmstetter and Werner* [2012] methods.



**Figure 16.** Previous available Brazilian PSHA from (a) GSHAP project and the PSHA proposed by this work (b).