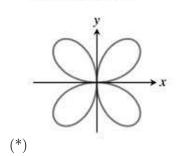
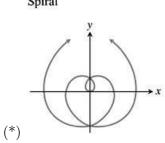
MAS115 Calculus I 2006-2007

Problem sheet for exercise class 9

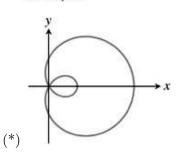
Four-leaved rose



Spiral



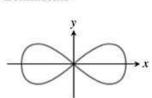
Limaçon

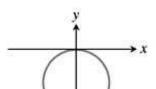


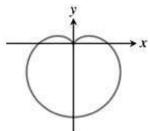
Circle

Cardioid

Lemniscate

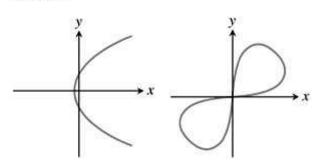






Parabola

Lemniscate



Problem 1: Match each of the eight graphs with one of the following equations.

a.
$$r = \cos 2\theta$$
,

b.
$$r\cos\theta = 1$$
.

b.
$$r \cos \theta = 1$$
, **c.** $r = \frac{6}{1 - 2 \cos \theta}$,

$$\mathbf{d.} \quad r = \sin 2\theta \ .$$

e.
$$r = \theta$$
,

$$\mathbf{f.} \quad r^2 = \cos 2\theta \; ,$$

g.
$$r = 1 + \cos \theta$$

$$h. \quad r = 1 - \sin \theta$$

d.
$$r = \sin 2\theta$$
, e. $r = \theta$, f. $r^2 = \cos 2\theta$, g. $r = 1 + \cos \theta$, h. $r = 1 - \sin \theta$, i. $r = \frac{2}{1 - \cos \theta}$, j. $r^2 = \sin 2\theta$, k. $r = -\sin \theta$, l. $r = 2\cos \theta + 1$.

$$j. r^2 = \sin 2\theta$$

$$\mathbf{k.} \quad r = -\sin\theta$$

$$1. \quad r = 2\cos\theta + 1$$

Problem 2: Show that the equations $x = r \cos \theta$, $y = r \sin \theta$ transform the polar equation

$$r = \frac{k}{1 + e\cos\theta}$$

into the Cartesian equation

$$(1 - e^2)x^2 + y^2 + 2kex - k^2 = 0.$$

Problem 3: Find polar equations for the following four circles. Sketch each circle in the coordinate plane and label it with both its Cartesian and polar equations.

- **a.** $x^2 + y^2 + 5y = 0$, **b.** $x^2 + y^2 2y = 0$, **c.** $x^2 + y^2 3x = 0$, **d.** $x^2 + y^2 + 4x = 0$.

Extra: Show that if you roll a circle of radius a about another circle of radius a in the polar coordinate plane, the original point of contact P will trace a cardioid. (Hint: start by showing that $\angle OBC$ and $\angle PAD$ are equal to each other.)

