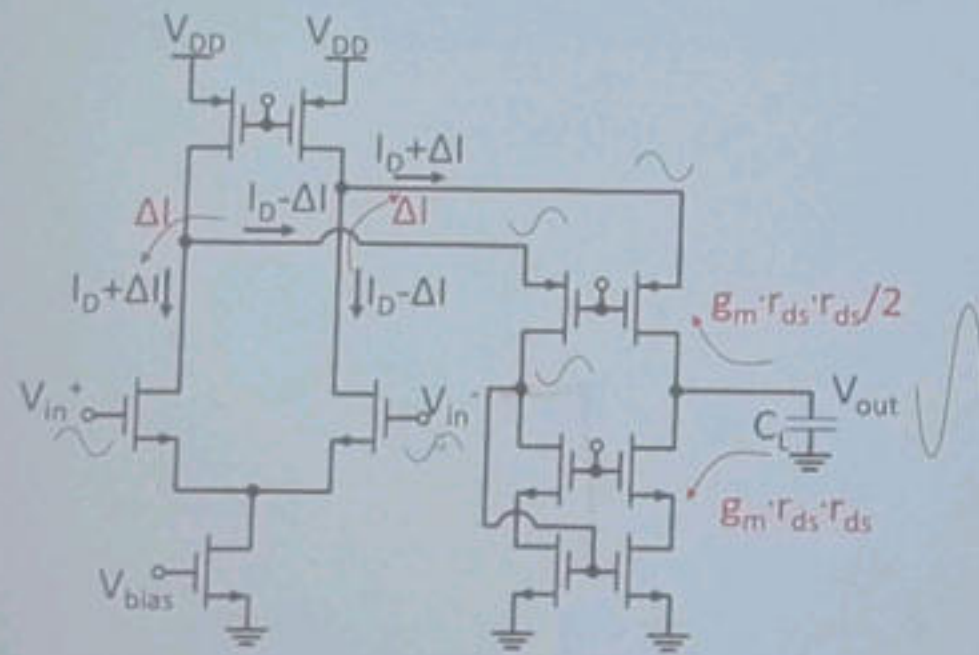


# Folded Cascode Amplifier



$$A = g_m^2 \frac{r_{ds}^2}{3} \approx 60 \text{ dB}$$

$$PM = 90^\circ$$

$$GBW = \frac{g_m}{2\pi C_L}$$

$$V_{swing} = V_{DD} - 4V_{ov}$$

Gain
PM
GBW
Swing
P

CM input range:  $V_{gs} + V_{ov} < V_{in,CM} < V_{DD} - V_{gs} + V_{th}$   
 → CM input range includes supply rail at the expense of larger supply current due to folding.

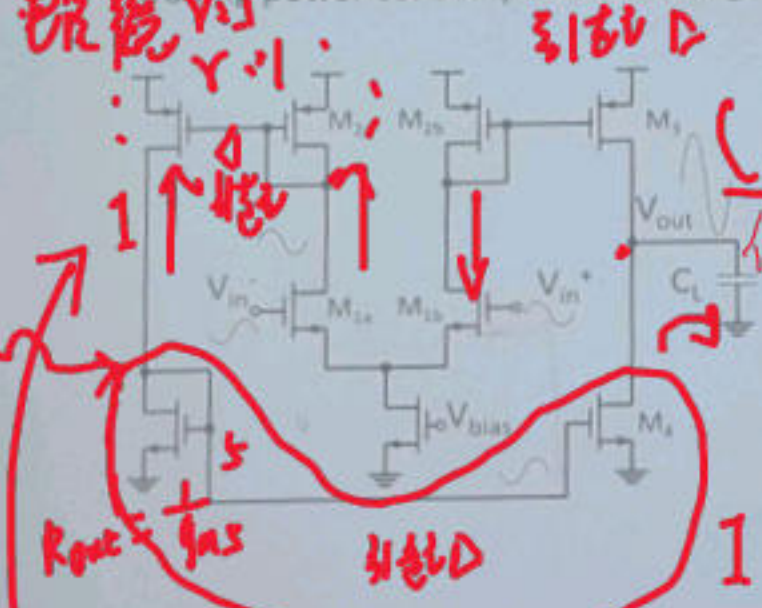
变化不大

变化一些

代价

## Single Stage OTA

minimizing power consumption for swing.



$$A = \frac{g_{m1}}{g_{m2}} \cdot \frac{g_{m3} + g_{m4}}{2} \cdot \frac{r_{ds}}{2}$$

$$PM < 90^\circ$$

$$GBW = \frac{g_{m1}}{g_{m2}} \cdot \frac{g_{m3} + g_{m4}}{2} \cdot \frac{1}{2\pi C_L}$$

$$V_{swing} = V_{DD} - 2V_{ov}$$

Gain
PM
GBW
Swing
P

电压  $V_{in}$  输入  
 电压  $V_{out}$  输出

$$\frac{V_{out}}{V_{in}} \text{ 即为 } A$$

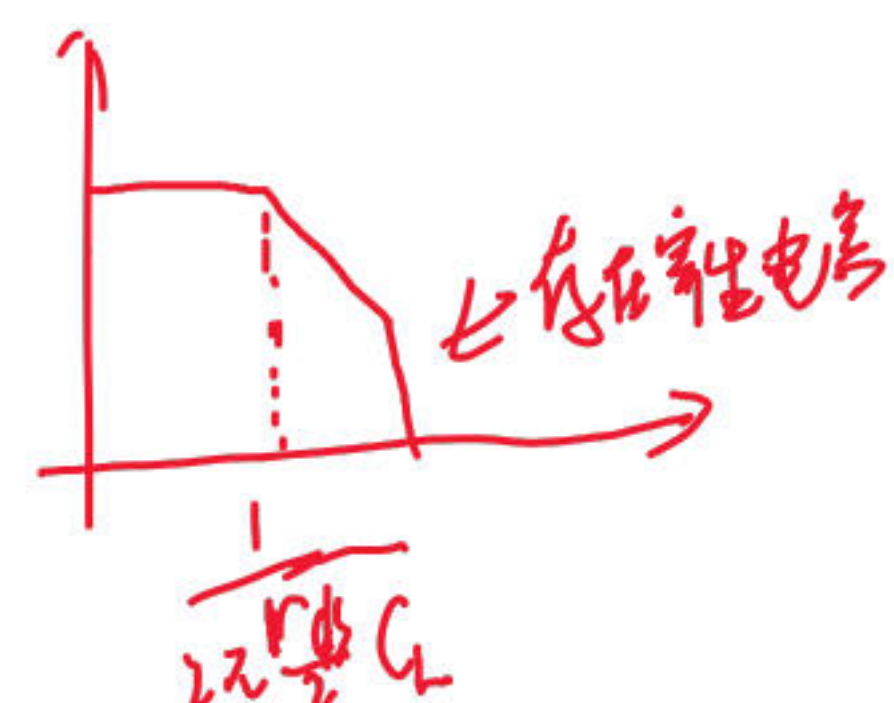
$$I \cdot r_{ds} + I \cdot r_{ds} = V_{out}$$

控制  $r$ , 增大  $A$

C 增大  
 6V 倍

2  
 +  
 2 + 2 = 6  
 增益增大

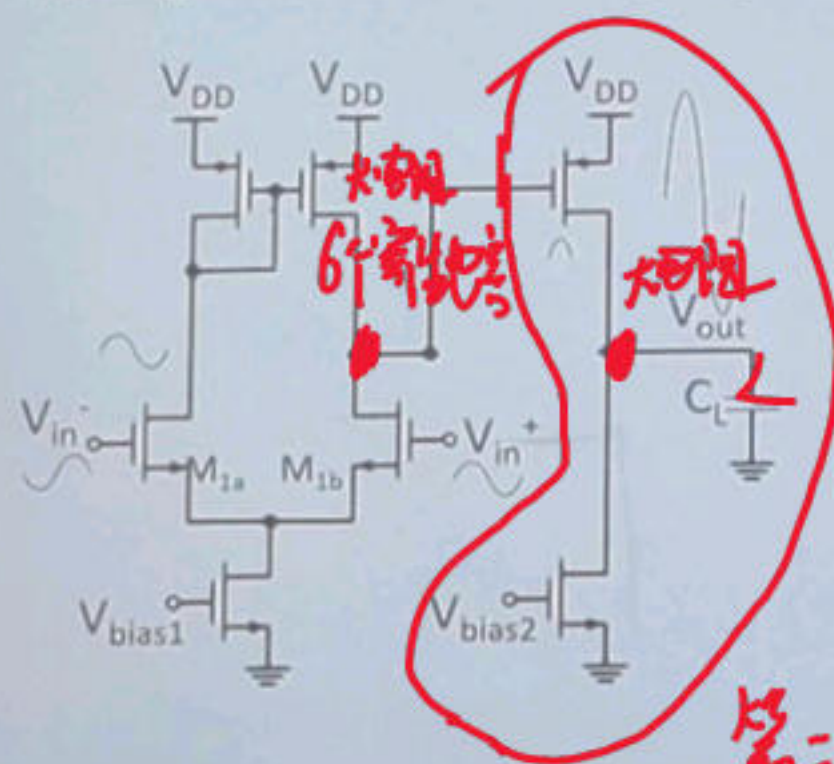
$$I = g_{m1} \frac{V_{in}}{2} \cdot \frac{1}{g_{m2}} \cdot (r g_{m2})$$





## Two Stage Miller OTA

Trading PM & GBW for swing & gain.



$$A = g_{m1} \cdot \frac{r_{ds1}}{2} \cdot g_{m2} \cdot \frac{r_{ds2}}{2}$$

$$45^\circ < PM < 70^\circ$$

$$GBW = \frac{g_{m1}}{2\pi C_c}$$

$$V_{swing} = V_{DD} - 2V_{ov}$$

Gain

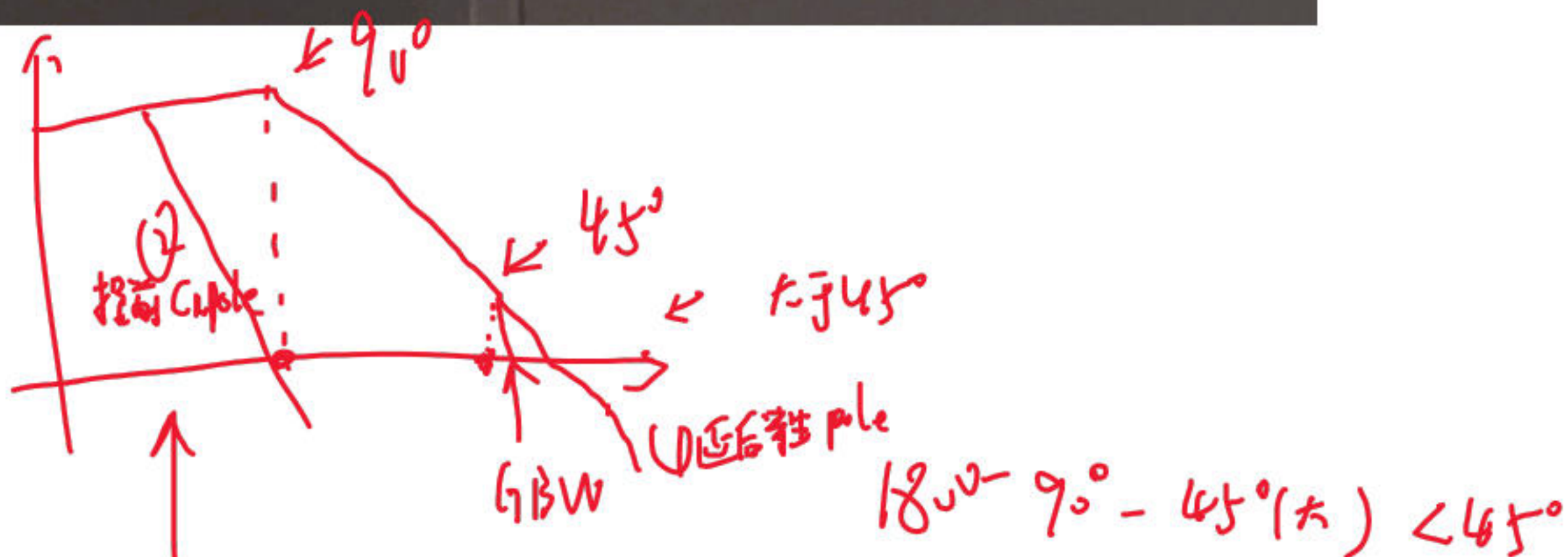
PM

GBW

Swing

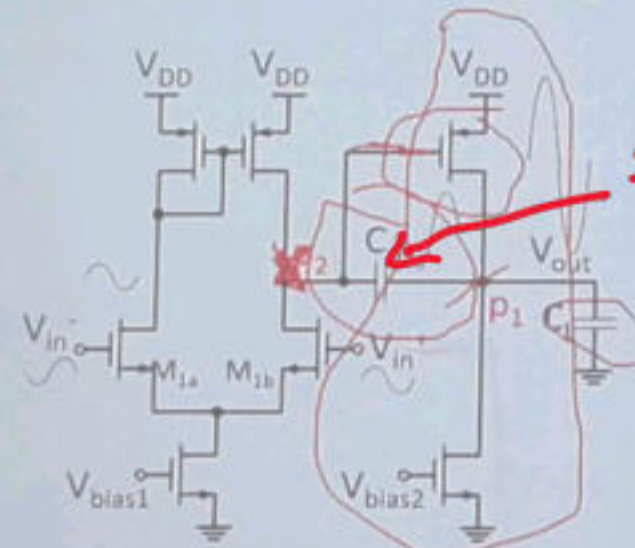
P

第二级  
Common source



## Two Stage Miller OTA

Trading PM & GBW for swing & gain.



$$A = g_{m1} \cdot \frac{r_{ds1}}{2} \cdot g_{m2} \cdot \frac{r_{ds2}}{2}$$

$$45^\circ < PM < 70^\circ$$

$$GBW = \frac{g_{m1}}{2\pi C_c}$$

$$V_{swing} = V_{DD} - 2V_{ov}$$

Gain

PM

GBW

Swing

P

two gain stages  $\Rightarrow$  two poles

$\Rightarrow$  Miller compensation required which reduces GBW.

增加  $C_L + C_C$



$$R_{in} = \frac{V_{in}}{i_{in}} = \frac{V_{in}}{\frac{V_{in} - V_{out}}{\frac{1}{sC}}} = \frac{V_{in}}{\frac{V_{in} - A V_{in}}{sC}} = \frac{1}{sC(1+A)}$$



## Recall

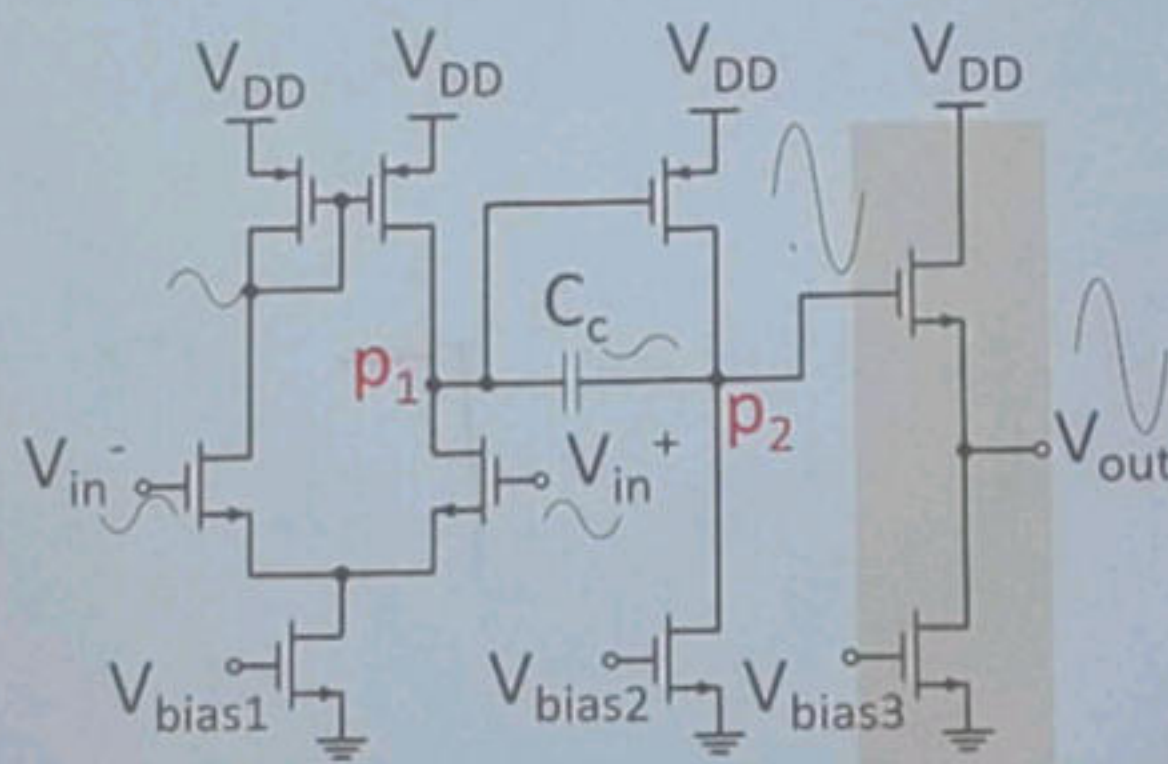
All amplifiers discussed so far are operational transconductance amplifiers (OTA).

Due to their high output impedance they behave like voltage controlled current sources.

## Opamp

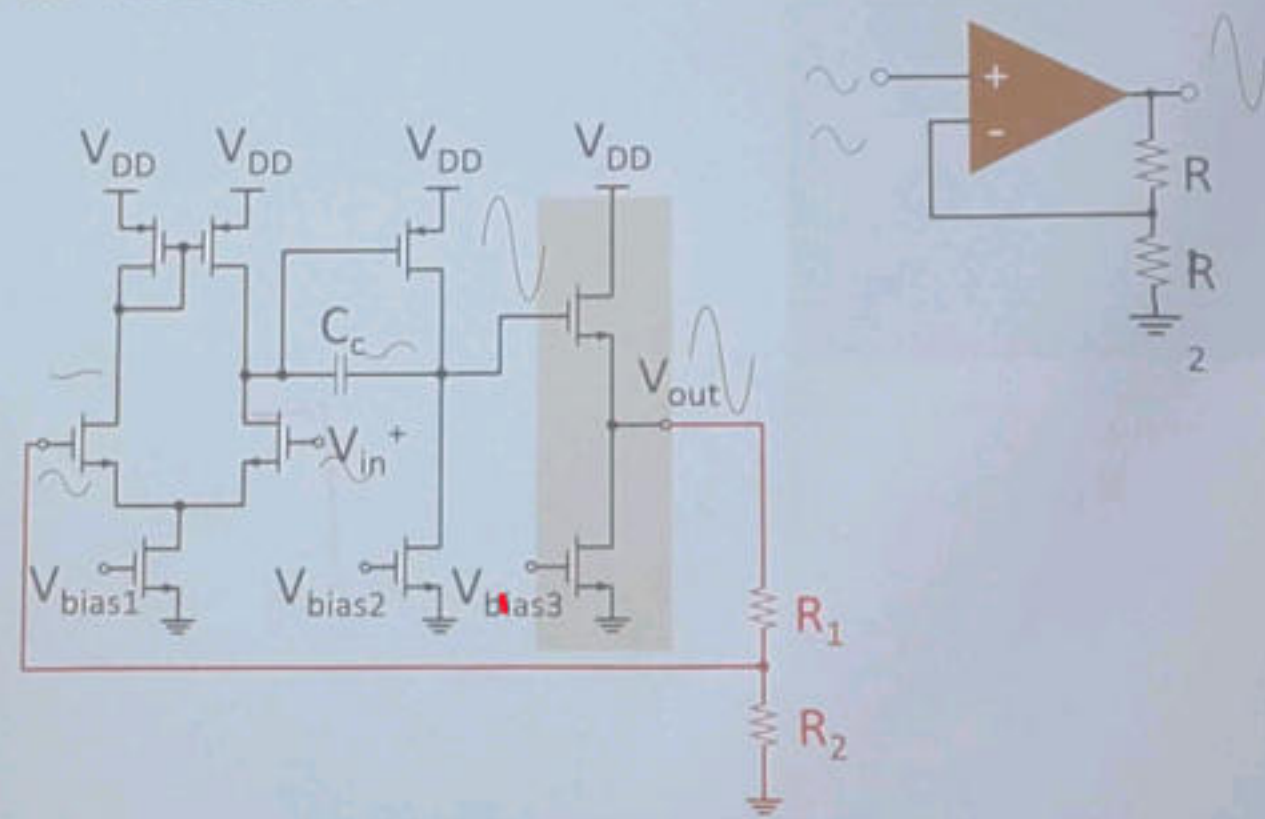
Sometimes we need to drive a resistive load.

→ Add output buffer.



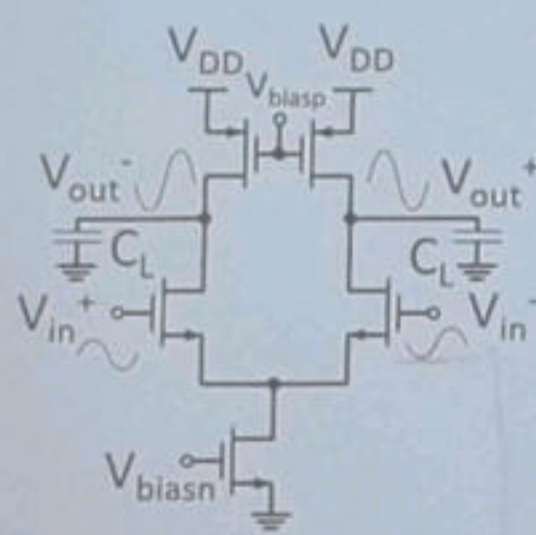


## Opamp in Feedback

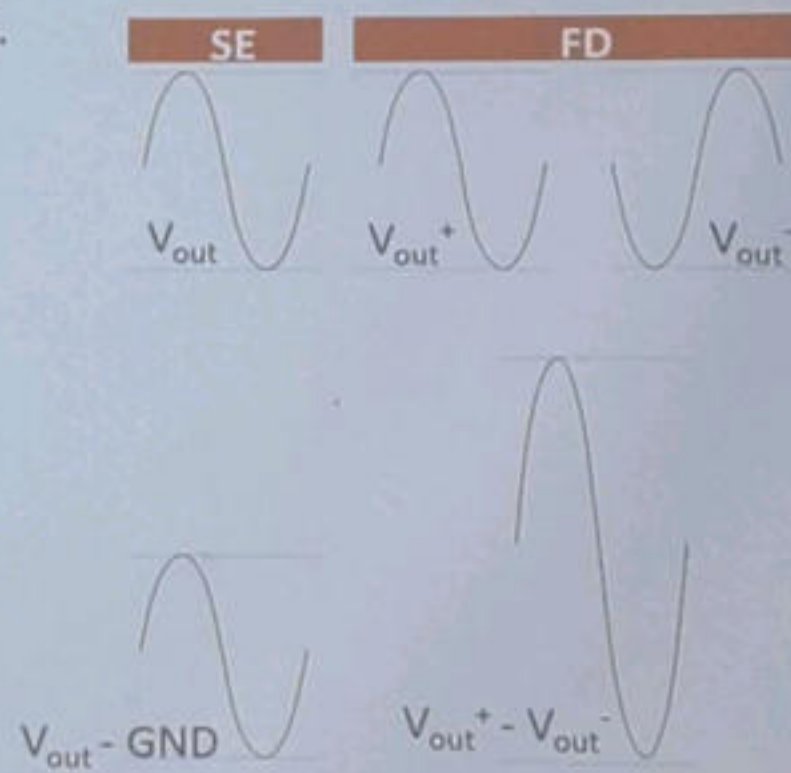


## Fully Differential

Differential in, Differential out.

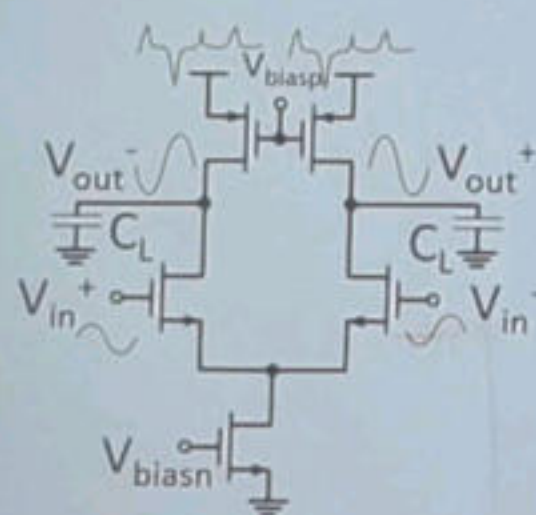


We get double the swing.



## Fully Differential 去扰动

Differential in, Differential out.



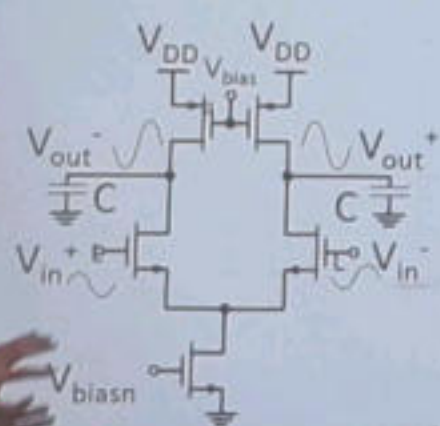
Supply Disturbances are CM.  
 ➔ Cancellation.





## Fully Differential

Differential in, Differential out.



Assume each differential branch as a nonlinear function:

$$V_{out} = \alpha_1 V_{in} + \alpha_2 V_{in}^2 + \alpha_3 V_{in}^3 + \alpha_4 V_{in}^4 + \dots$$

$$V_{out}^+ = \alpha_1 V_{in}^+ + \alpha_2 V_{in}^{+2} + \alpha_3 V_{in}^{+3} + \alpha_4 V_{in}^{+4} + \dots$$

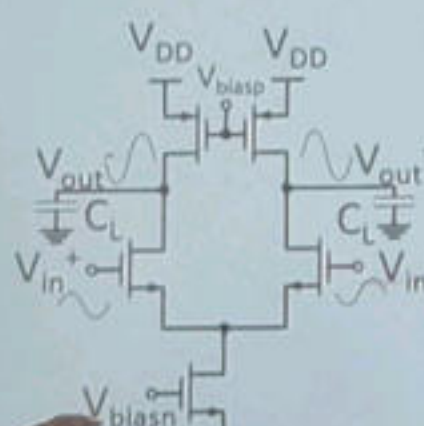
$$V_{out}^- = \alpha_1 V_{in}^- + \alpha_2 V_{in}^{-2} + \alpha_3 V_{in}^{-3} + \alpha_4 V_{in}^{-4} + \dots$$

$$\text{with } V_{in}^+ = -V_{in}^- = (V_{in}^+ - V_{in}^-)/2 :$$

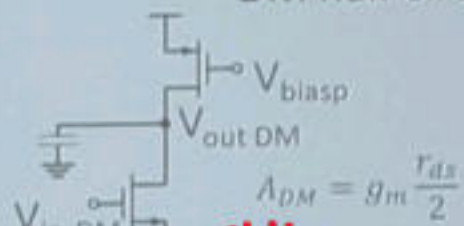
$$V_{out}^+ - V_{out}^- = \alpha_1 (V_{in}^+ - V_{in}^-) + \alpha_3 (V_{in}^+ - V_{in}^-)^3 + \dots$$

Even order harmonics are cancelled.

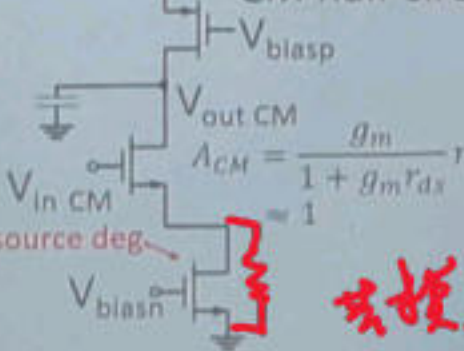
## CMFB



DM half circuit



CM half circuit



$$\frac{A_{CM}}{A_{DM}} = \frac{1}{g_m \frac{r_{ds}}{2}}$$

$$\frac{V_{in} \cdot (r_{ds} \parallel g_m r_{ds}^2)}{r_{ds}}$$

$$V_{out} = \frac{V_{in}}{r_{ds}} \cdot \left( \frac{g_m r_{ds}^2}{g_m r_{ds} + 1} \right)$$

$$A_{CM} = \frac{g_m r_{ds}}{g_m r_{ds} + 1}$$

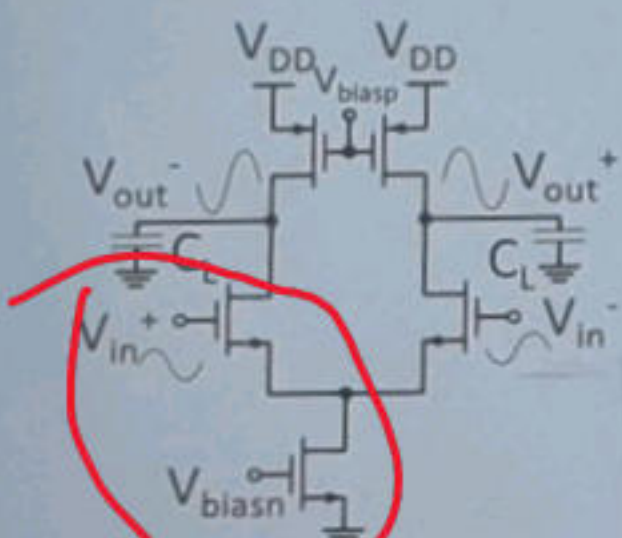
平衡点

源极退化电阻

引入负反馈

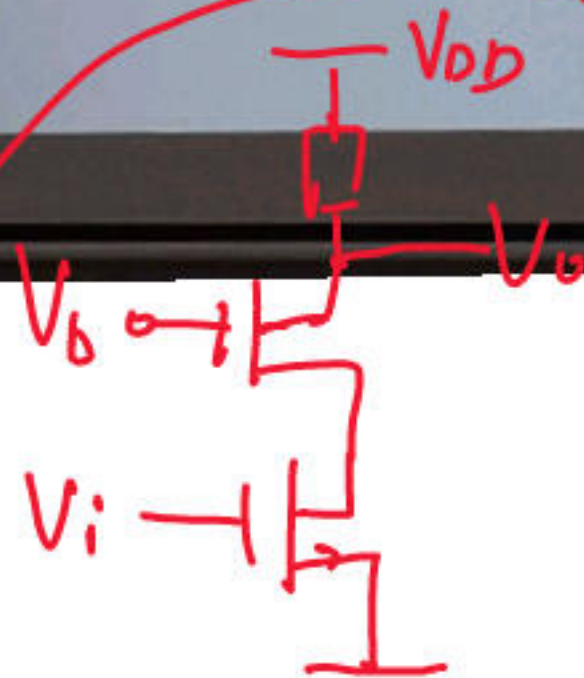
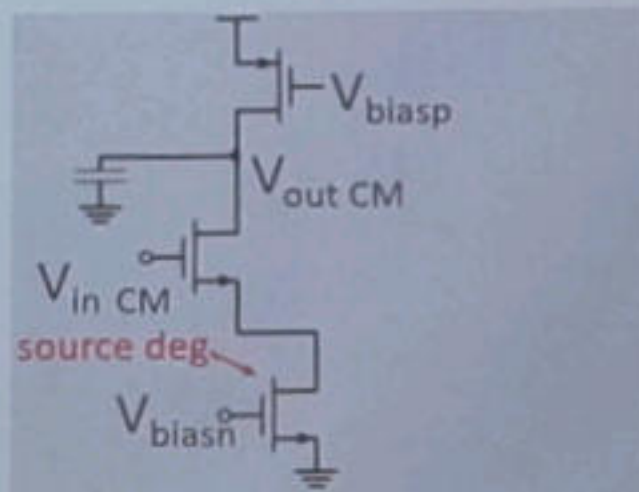
$$\text{此时, 电路电流 } I = \frac{V_{in}}{r_{ds}}$$

## CMFB



Cascode

$$\frac{V_{out CM}}{V_{biasp}} = g_{mp} (r_{ds} \parallel g_{mn} r_{ds}^2) \approx g_{mp} r_{ds}$$

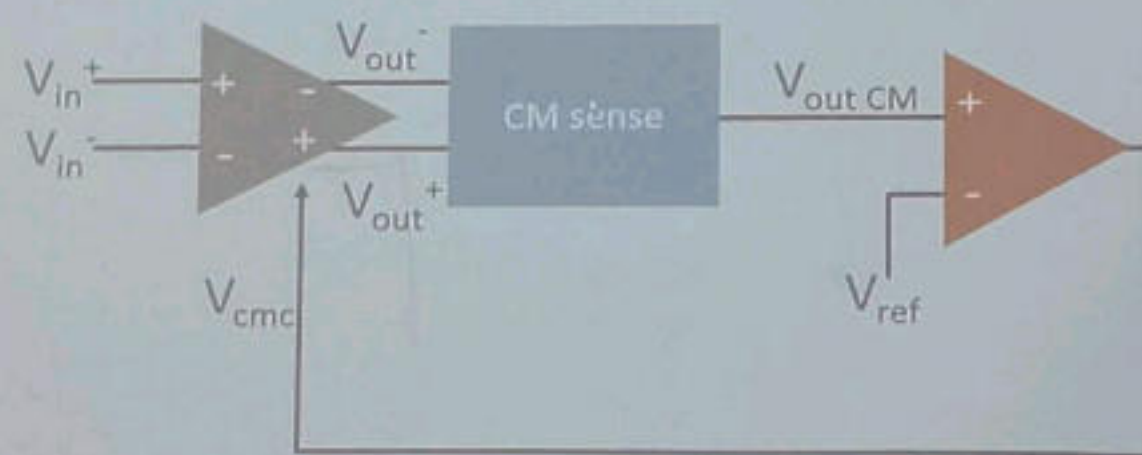


共源共栅放大器

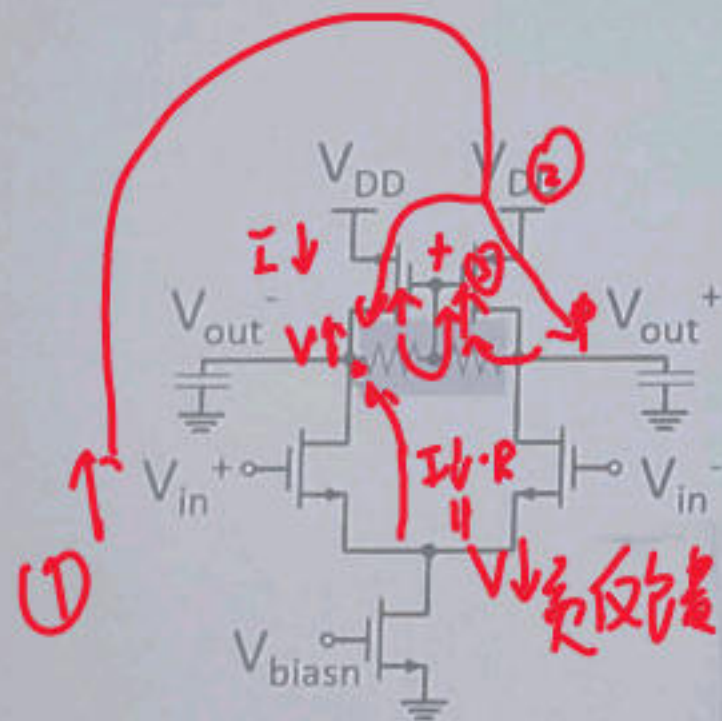


## CMFB

Use CM feedback loop to define the output CM.



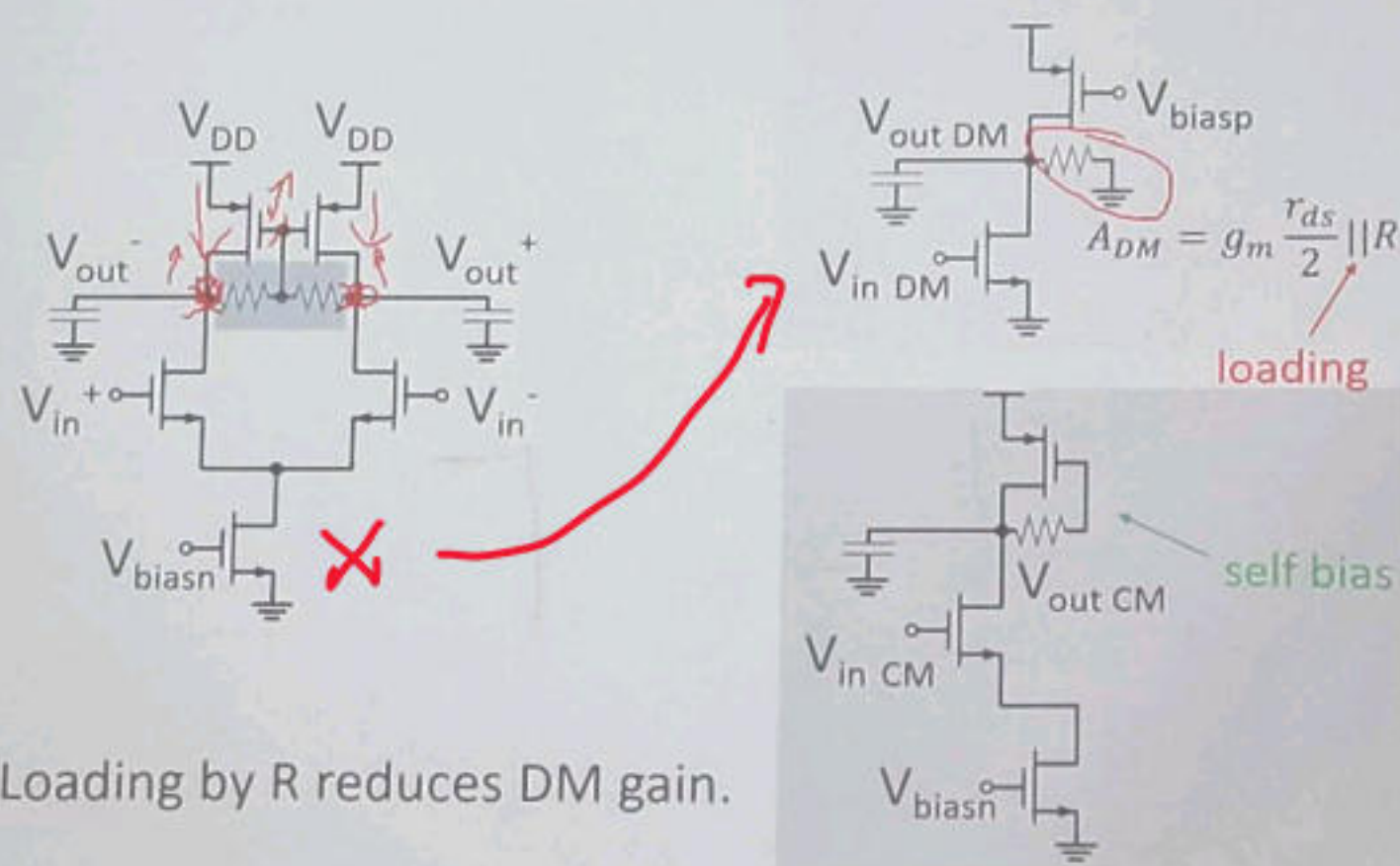
## CMFB



Loading by R reduces DM gain.

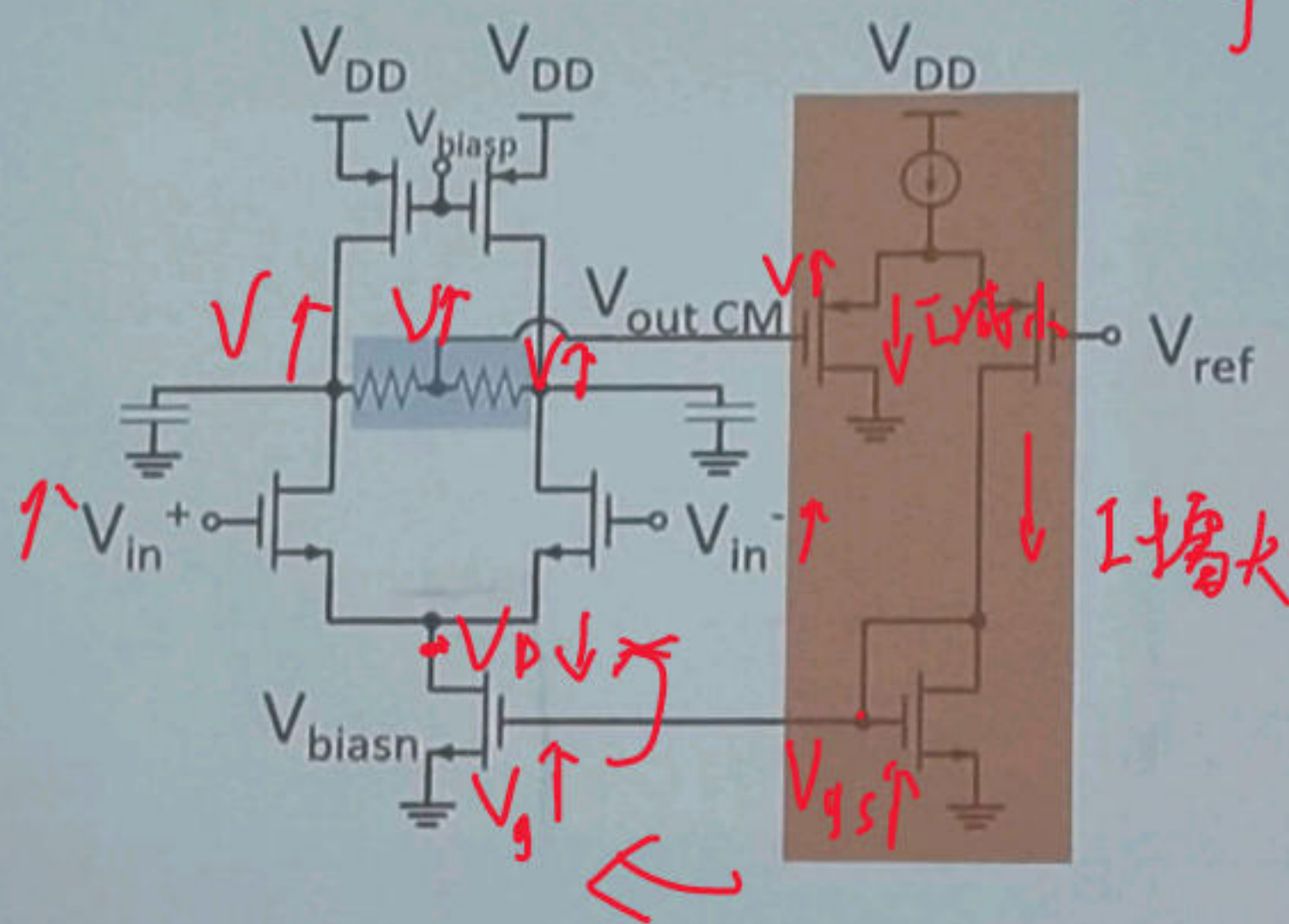


## CMFB



Loading by R reduces DM gain.

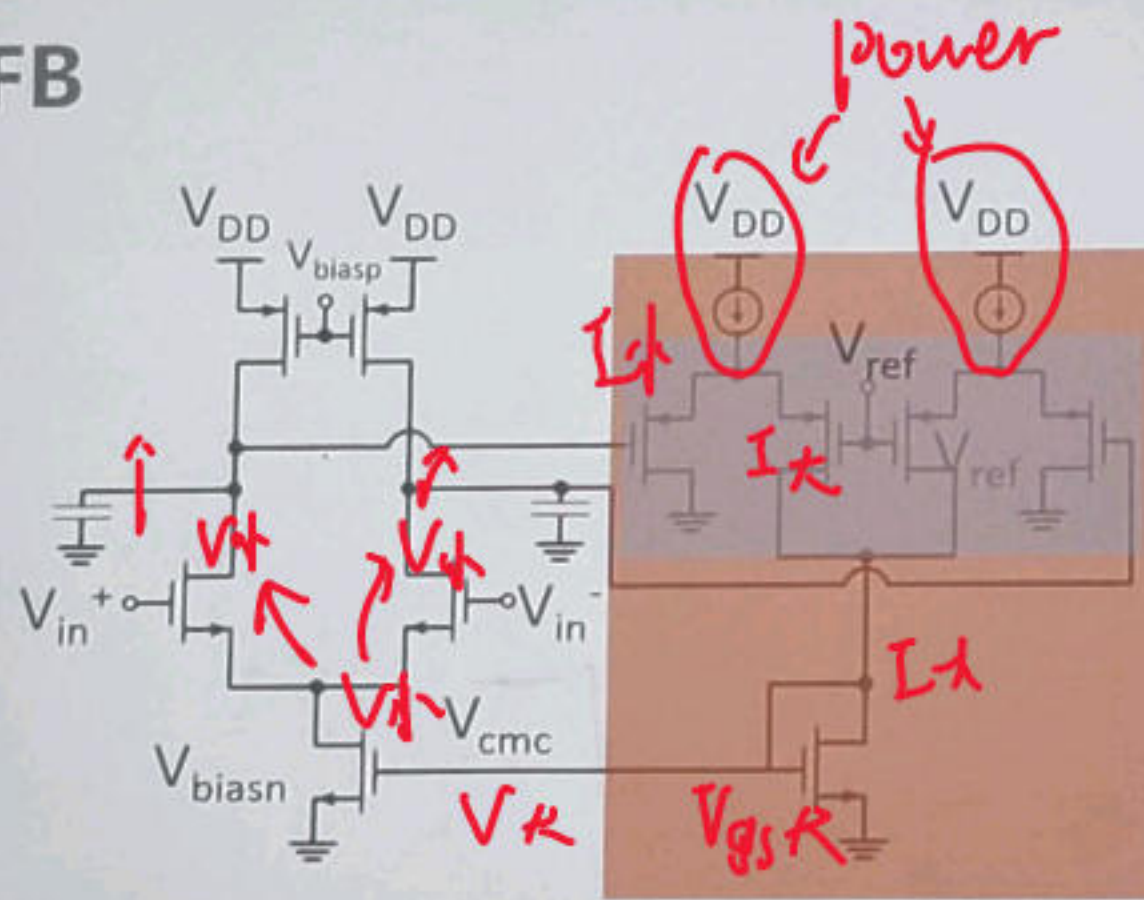
## CMFB



Output CM can be set to an arbitraral level  $V_{ref}$ .



## CMFB



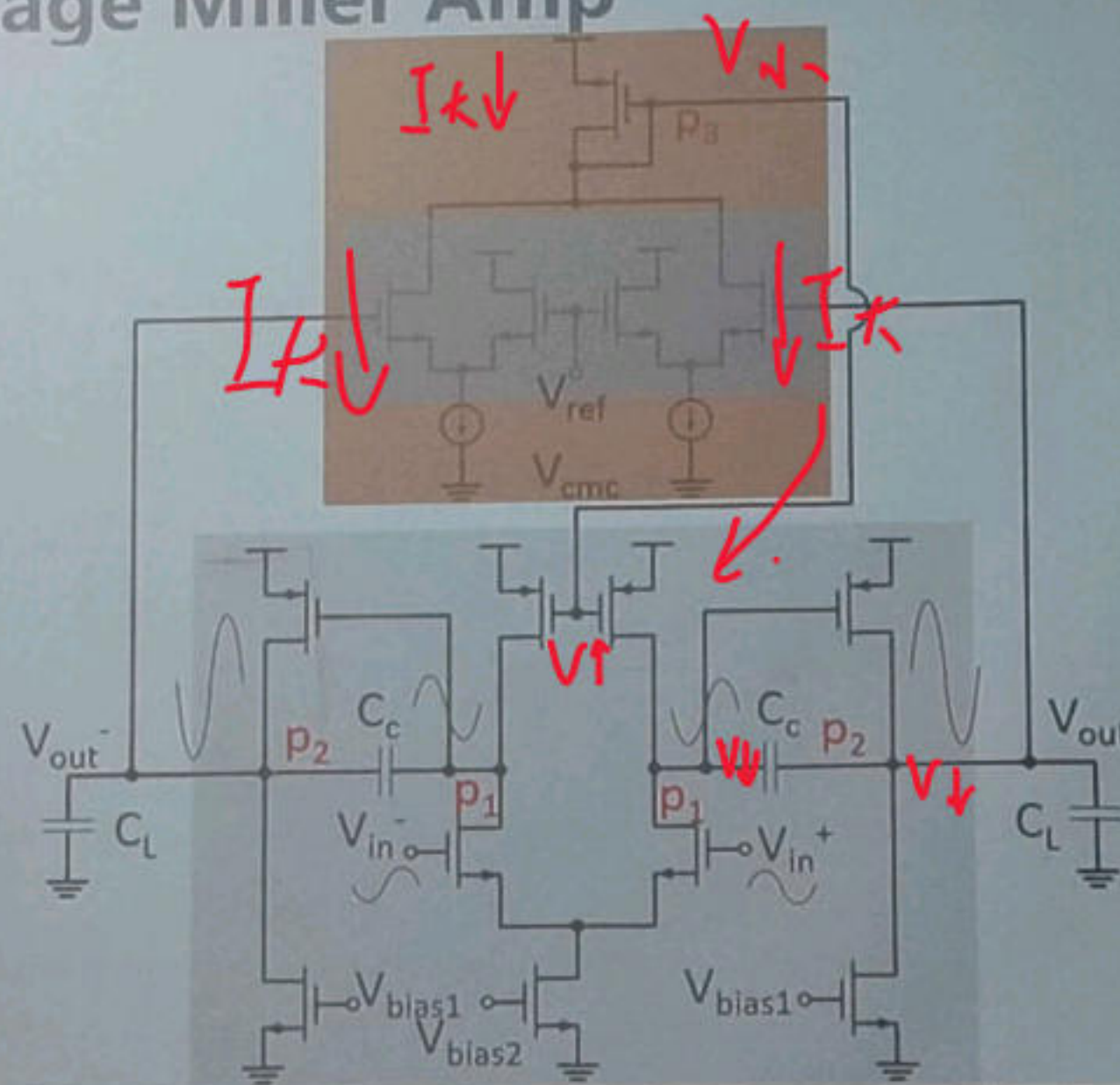
实际是一个  
1个极点

No loading of differential amplifier output.

**but:** CM sense is nonlinear

→ Restriction on DM output swing to prevent DM to CM conversion.

## FD Two Stage Miller Amp



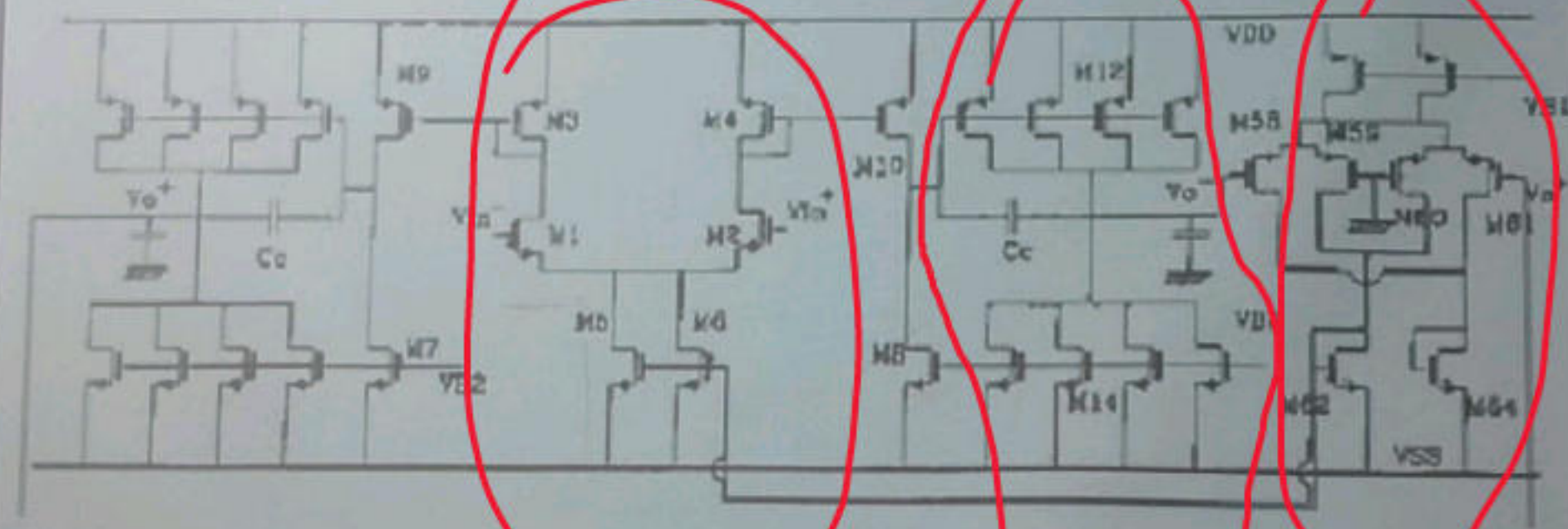
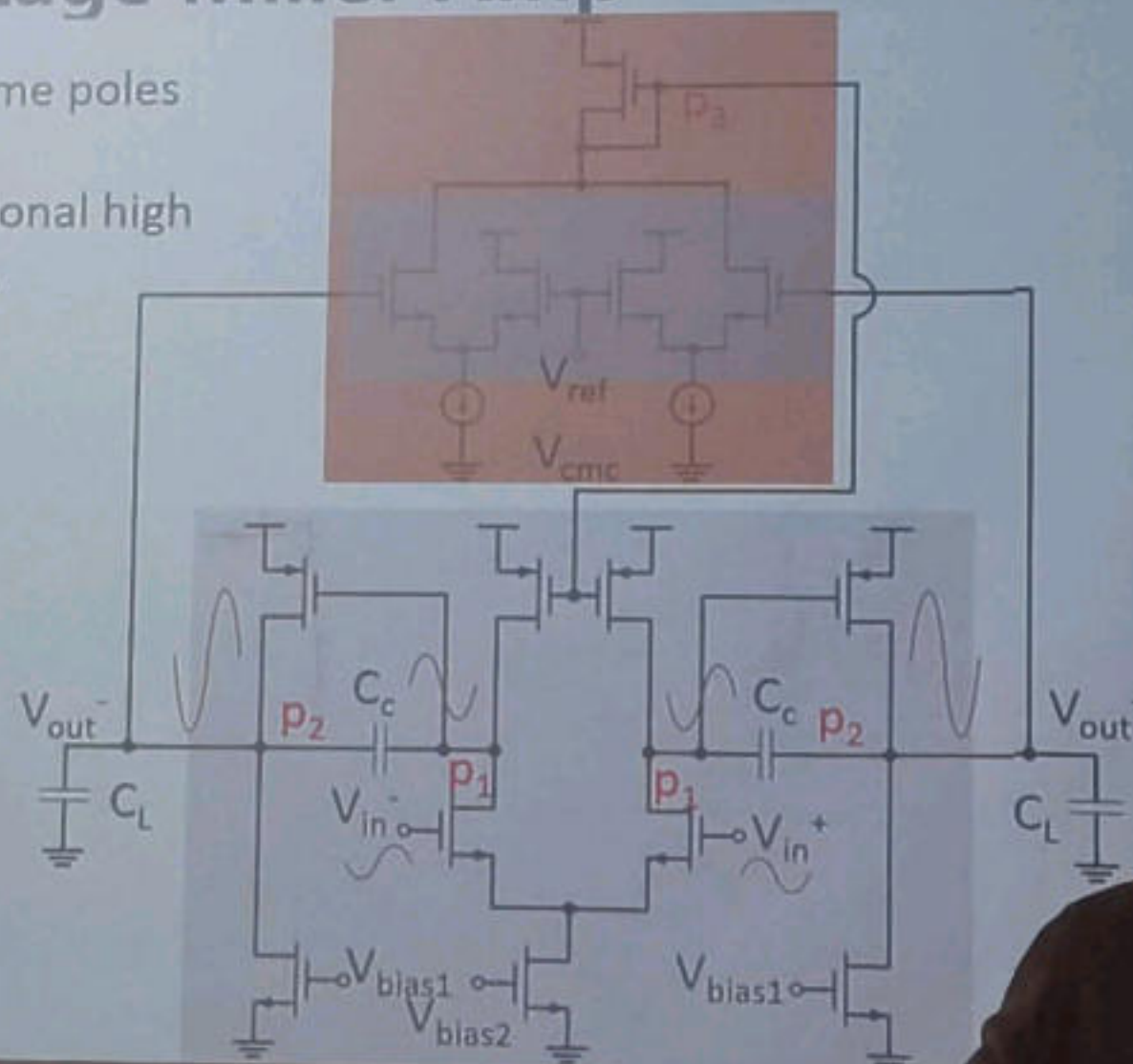
控制 - 级即可

3个 Pole -



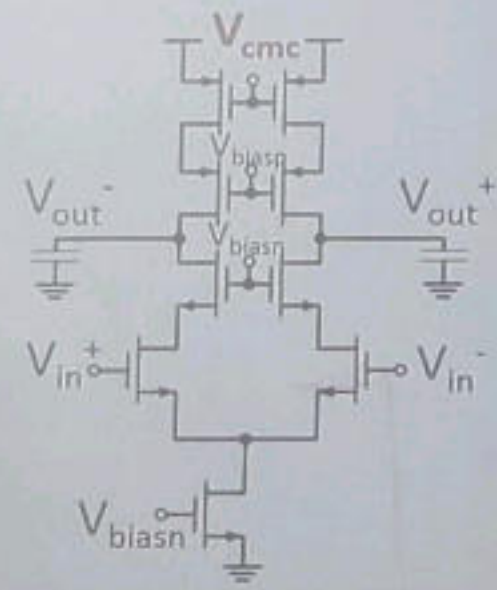
## FD Two Stage Miller Amp

CMFB sees the same poles as main amplifier but has one additional high frequency pole  $p_3$ .



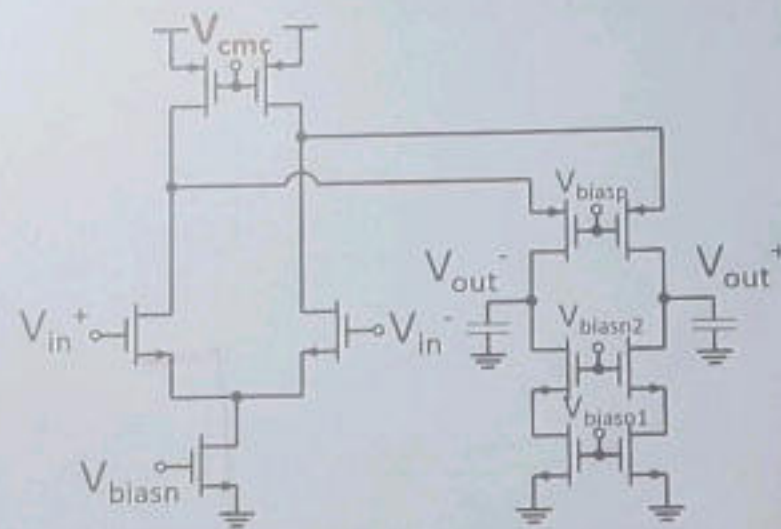


## Single Stage FD Amplifiers



Telescopic Cascode

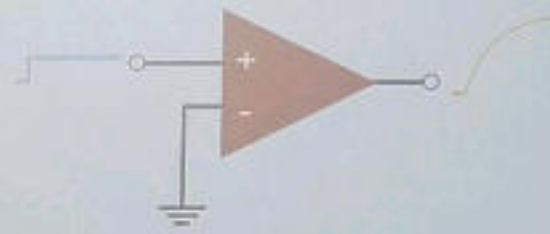
## Single Stage FD Amplifiers



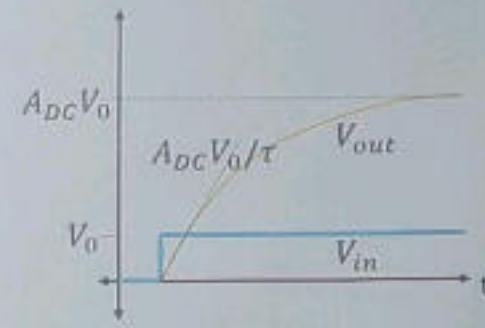
Folded Cascode



## Slew Rate



$$A(s) = \frac{A_{DC}}{1 + s/p}$$

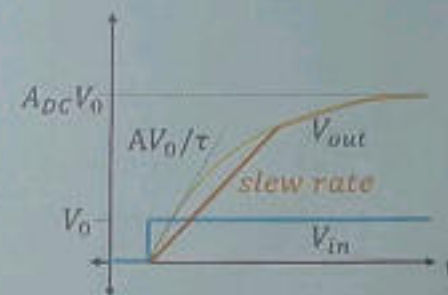
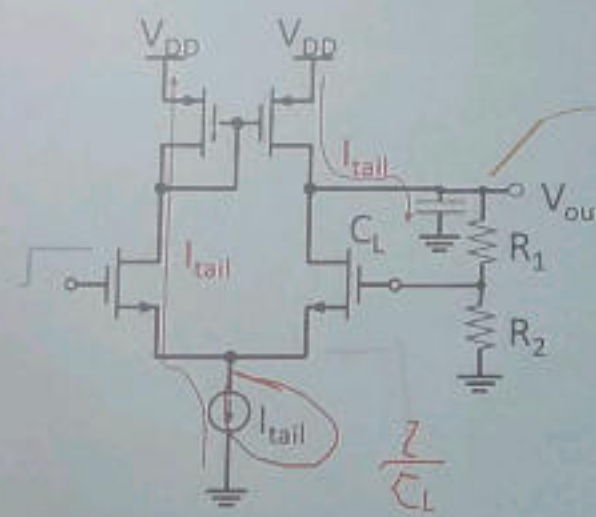


$$V_{out} = A_{DC} V_0 \cdot (1 - e^{-t/\tau}) \text{ with } \tau = \frac{1}{p}$$

$$\frac{dV_{out}}{dt} = \frac{A_{DC} V_0}{\tau} \cdot e^{-t/\tau}$$

max. slope  $A_{DC} V_0 / \tau$  at  $t = 0$ .

## Slew Rate

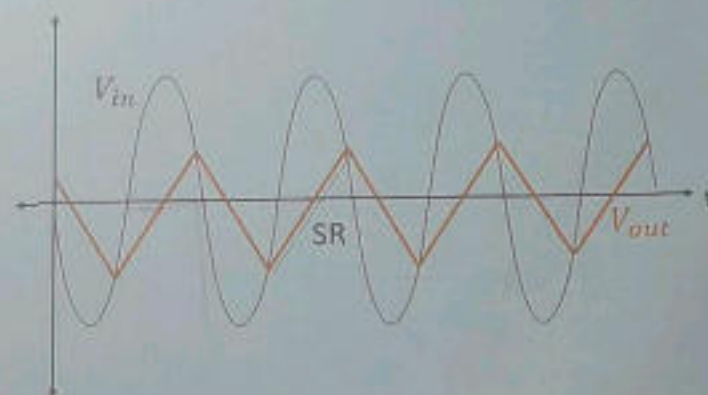


$$I_{tail} = 1\text{mA}, C_L = 1\text{ }\mu\text{F} \Rightarrow \text{SR} = 1000\text{ V/s}$$

If  $V_0/\tau > \text{slew rate}$  then settling is slew rate limited.  $\Rightarrow$  nonlinear

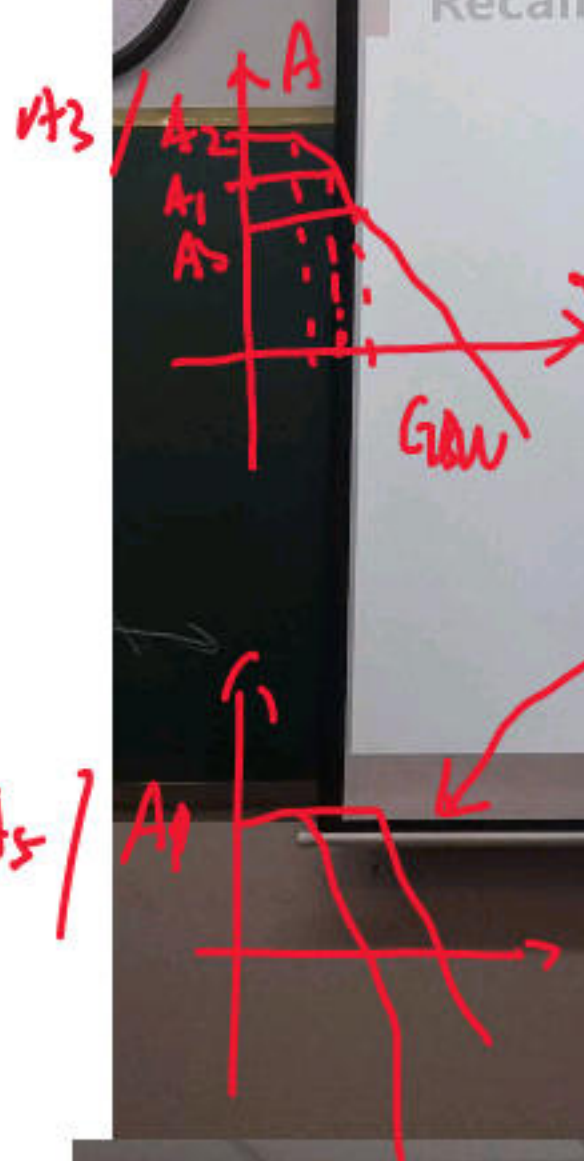
## Slew Rate

An extreme example of slewing:





Recall



Topology	Gain	PM	GBW	Swing	P
Basic Diff Pair	- $A_0$	+	+	0	+
Telescopic Cascode	0 $A_1$	+	+	-	+
Gain Boosted Tel. Cascode	+ $A_2$	+	+	-	-
Folded Cascode	0 $A_3$	+	+	0	-
Single Stage OTA	- $A_4$	+	+	+	-
2 stage Miller	0 $A_5$	0	-	+	-

low power

low output

GBW

$A_5 / A_1$

Recall

Fully differential benefits from

- twice the output swing
- supply noise suppression
- even order nonlinearity cancellation

Fully differential requires CM feedback to stabilize the output CM.

Bias current and  $C_L$  define the slew rate ( $dV_{out}/dt$ ).