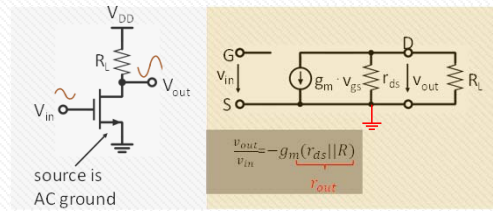


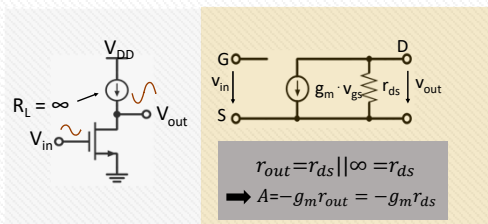
Basic Analog Blocks and Amplifiers

Common Source Amplifier



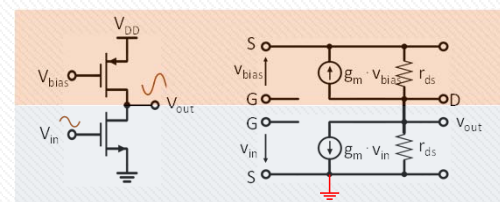
Generally we can write for an amplifier: $A = -g_m r_{out}$

Better Common Source Amplifier

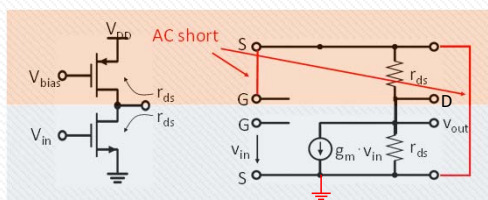


How to implement the current source load?

Better Common Source Amplifier

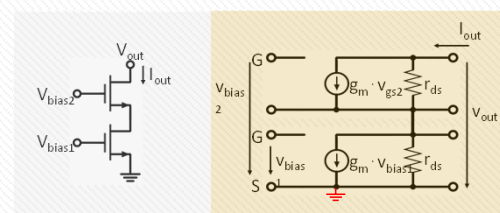


Better Common Source Amplifier

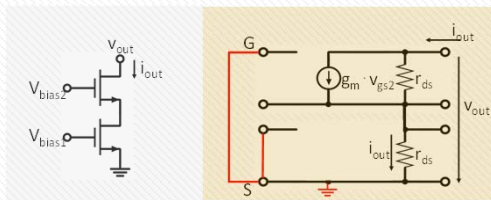


Can we still increase the gain?

Cascode Load



Cascode Load

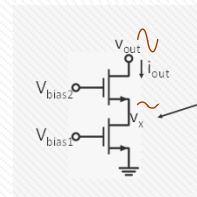


$$v_{gs2} = -i_{out} r_{ds}$$

$$\Rightarrow v_{out} = (i_{out} + g_m i_{out} r_{ds}) \cdot r_{ds} + i_{out} r_{ds}$$

$$\Rightarrow r_{out} = \frac{v_{out}}{i_{out}} = (1 + g_m r_{ds}) \cdot r_{ds} + r_{ds} \approx g_m r_{ds}^2$$

Intuition on Cascode Load



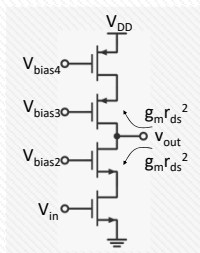
Swing is reduced by gain of upper MOS:

$$v_x = \frac{v_{out}}{g_m r_{ds2}}$$

⇒ output current reduced significantly:

$$i_{out} = \frac{v_x}{r_{ds1}} = \frac{v_{out}}{g_m r_{ds2} \cdot r_{ds1}}$$

Cascode Amplifier

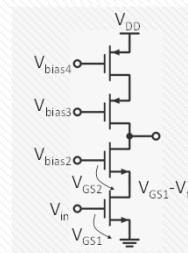


$$r_{out} = g_m \frac{r_{ds}^2}{2}$$

$$A = -g_m r_{out} = -\frac{(g_m r_{ds})^2}{2}$$

We squared the gain at the penalty of output swing.

Cascode Amplifier Output Swing

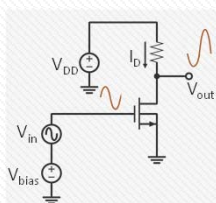


$$V_{out} < V_{DD} - V_{SG4} + V_{th} - V_{SG3} + V_{th} = V_{DD} - V_{ov4} - V_{ov3}$$

$$V_{out} > V_{GS1} - V_{th} + V_{GS2} - V_{th} = V_{ov1} + V_{ov2}$$

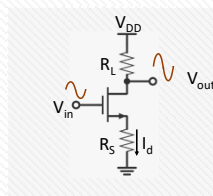
$$V_{swing} = V_{DD} - V_{ov4} - V_{ov3} - V_{ov1} - V_{ov2} = V_{DD} - 4 \cdot V_{ov}$$

Source Degeneration



Remember: CM Source amplifier is very nonlinear for large signals.

Source Degeneration



$$i_d = g_m (v_{in} - i_d R_S)$$

$$g_{meff} = \frac{i_d}{v_{in}} = \frac{g_m}{1 + g_m R_S}$$

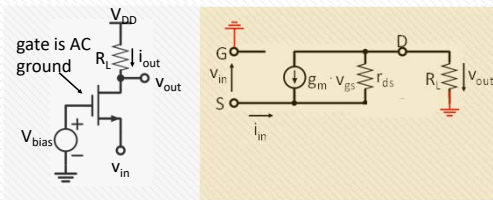
$$A = -g_{meff} R_L = -\frac{g_m R_L}{1 + g_m R_S}$$

Remember: CM Source amplifier is very nonlinear for large signals.

⇒ Use **local** feedback to improve linearity.

$$v_{in} \uparrow \Rightarrow i_d \uparrow \Rightarrow i_d R_S \uparrow \Rightarrow V_{gs} \uparrow \Rightarrow i_d \downarrow$$

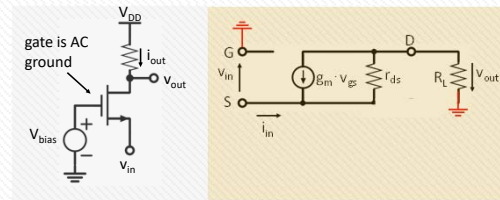
Common Gate Amplifier



Kirchhoff's current law (KCL): $\frac{v_{out}}{R_L} = g_m v_{in} - \frac{v_{out} - v_{in}}{r_{ds}}$

$\Rightarrow \frac{v_{out}}{v_{in}} = \frac{g_m r_{ds} + 1}{r_{ds} + R_L} \cdot R_L \approx g_m R_L$ ← expected from intuition

Common Gate Amplifier

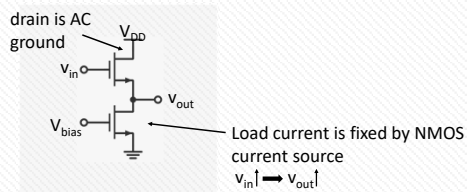


$i_{in} = \frac{v_{out}}{R_L} = v_{in} \cdot \frac{g_m r_{ds} + 1}{r_{ds} + R_L} \approx v_{in} g_m \Rightarrow r_{in} = \frac{v_{in}}{i_{in}} = \frac{1}{g_m}$

→ low input impedance (current input)

→ often used as current to voltage (transimpedance) amplifier

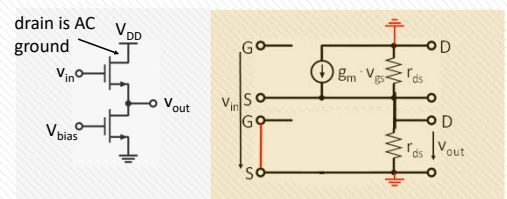
Common Drain Amplifier



The output needs to follow the source in order to keep the current constant

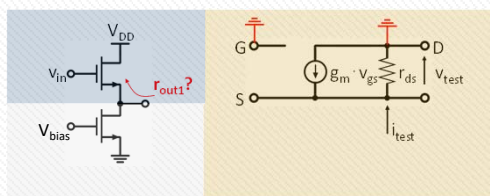
→ often referred to as **source follower**

Common Drain Amplifier



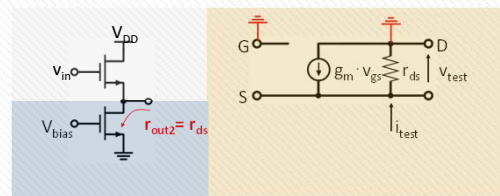
KCL: $\frac{v_{out}}{r_{ds}} = g_m(v_{in} - v_{out}) - \frac{v_{out}}{R_L} \Rightarrow \frac{v_{out}}{v_{in}} = \frac{g_m}{\frac{2}{r_{ds}} + g_m} \approx 1$

Common Drain Amplifier



KCL: $i_{test} = \frac{v_{test}}{r_{ds}} + g_m v_{test} \Rightarrow r_{out1} = \frac{v_{test}}{i_{test}} = \frac{1}{\frac{1}{r_{ds}} + g_m} \approx \frac{1}{g_m}$

Common Drain Amplifier

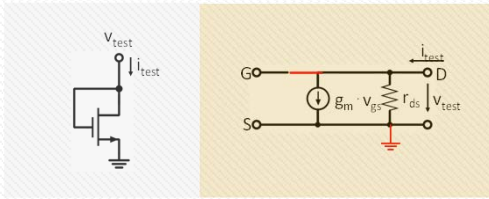


Total output resistance: $r_{out} = r_{out1} || r_{out2} \approx \frac{1}{g_m}$

→ low output impedance → high current gain

→ often used as output buffer

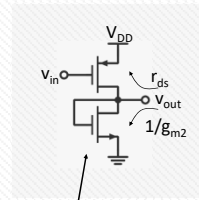
Diode Connection



$$\text{KCL: } i_{\text{test}} = \frac{v_{\text{test}}}{r_{\text{ds}}} + g_m v_{\text{test}} \Rightarrow r_{\text{out1}} = \frac{v_{\text{test}}}{i_{\text{test}}} = \frac{1}{\frac{1}{r_{\text{ds}}} + g_m} \approx \frac{1}{g_m}$$

Called diode connection, because $I(V)$ looks like a diode characteristic.

Low Gain Amplifier



self biased load

$$r_{\text{out}} = r_{\text{out1}} \parallel r_{\text{out2}} \approx \frac{1}{g_{m2}}$$

$$A = g_{m1} r_{\text{out}} \approx \frac{g_{m1}}{g_{m2}}$$

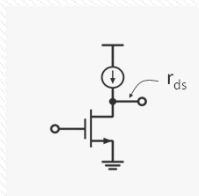
Recall

$$A = g_m \cdot r_{\text{out}}$$

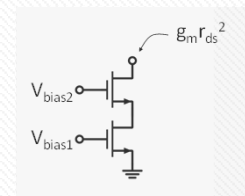
Recall

| Topology | Gain | Rout | Rin |
|-----------|------|------|------|
| CM source | high | high | high |
| CM gate | high | high | low |
| CM drain | low | low | high |

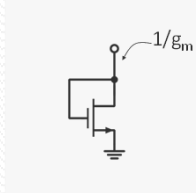
Recall



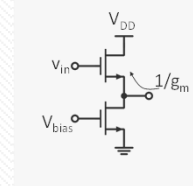
Recall



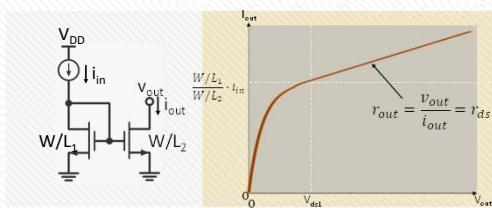
Recall



Recall

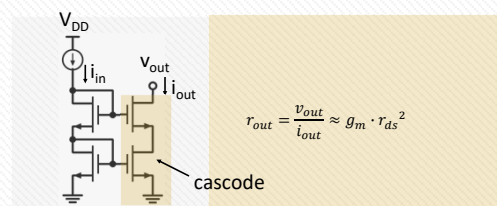


Basic Current Mirror



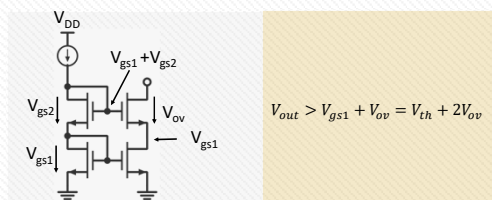
For an ideal current mirror the output current is independent of V_{out} .
 ➔ large r_{out} desired

Cascode Current Mirror



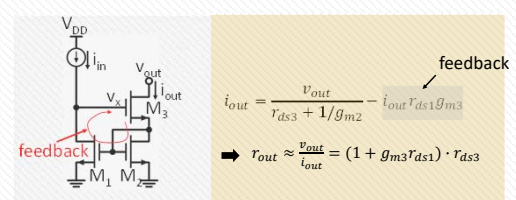
Increased output resistance due to cascoding.

Cascode Current Mirror



Reduced swing compared to basic current mirror.

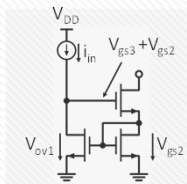
Wilson Current Mirror



Output resistance increased via feedback loop:

$$V_{out} \uparrow \rightarrow I_{out} \uparrow \rightarrow v_x \downarrow \rightarrow I_{out} \uparrow$$

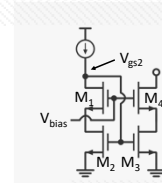
Wilson Current Mirror



$$V_{out} > V_{gs2} + V_{ov3} = V_{th} + 2V_{ov}$$

How to increase the output swing?

High Swing Cascode Current Mirror



$$V_{out} > V_{bias} - V_{gs4} + V_{ov4} = V_{bias} - V_{th}$$

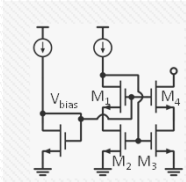
$$V_{bias} > V_{gs1} + V_{ov2}$$

$$\Rightarrow V_{out} > V_{ov1} + V_{ov2} = 2V_{ov}$$

Output swing increased by V_{th} .

How to generate V_{bias} ?

High Swing Cascode Current Mirror



$$V_{bias} > V_{ov2} + V_{gs1}$$

Use long ($L > W$) diode connected transistor to generate V_{bias} .

Recall

| Current Mirror | Rout | Swing |
|----------------|------|-------|
| Basic | - | ++ |
| Cascode | + | - |
| Wilson | + | - |
| High Swing | + | + |