# Kericho

## greyhypotheses

## Problem 4

Considering the time series model

$$Y(t) = \beta_0 + \beta_1 t + \beta_2 I(pmax(t - 50, 0)) + \beta_3 I(t > 225)$$

$$+ \beta_4 minT(t - k) + \beta_5 maxT(t - k) + \beta_6 Rain(t - k)$$

$$+ \mathcal{W}(t) + Z(t)$$
(1)

for the Kericho malaria cases data, wherein

variable	description
$\overline{t}$	time (months)
minT	mininum temperature
maxT	maximum temperature
Rain	rainfall (millimetres)
k	lag; $k = 2$ months
$\mathcal{W}(t)$	A Matern process whereby $\kappa=2.5$
Z(t)	Gaussian noise

### Data Set-up

The original data set, with appended time dependent variables, is

```
'data.frame': 310 obs. of 11 variables:
        $ Month : Ord.factor w/ 12 levels "Jan"<"Feb"<"Mar"<..: 1 2 3 4 5 6 7 8 9 10 ...</pre>
$ Cases : int 25 25 20 30 18 18 15 15 10 20 ...
$ Rain
        : num 3.7 3.2 5.6 8.3 8.1 5.4 5.5 6.1 5.7 5.6 ...
$ minT
        : num 11.8 11.3 10.9 12 10.9 11.4 10.2 10.1 10.2 11.1 ...
$ maxT
        : num 24 23.5 25.1 23.6 22.9 22.1 22.1 23 23.9 25.2 ...
$ VCAP
       : num 78.5 56.6 131.9 467.6 277 ...
$ CasesLN: num 3.22 3.22 3 3.4 2.89 ...
$ datestr: chr "1979-01" "1979-02" "1979-03" "1979-04" ...
       : Date, format: "1979-01-01" "1979-02-01" ...
$ time
        : num 0 1 2 3 4 5 6 7 8 9 ...
```

The function TimeDependentLag() creates lagged fields. Hence, the lagged minimum temperature, maximum temperature, and rain fields:

### Exercise 1: Model Fitting

Prior to fitting Eq. 1, records that have NaN values ...

```
condition <- !is.na(instances$rain_lag_2) | !is.na(instances$mint_lag_2) |
  !is.na(instances$maxt_lag_2)
excerpt <- instances[condition, ]</pre>
```

Hence, via the fit.matern() function

The summary of the model fitted for Eq. 1 is ...

```
Geostatistical linear model
linear.model.MLE(formula = log(Cases) ~ time + I(pmax(time -
    50, 0)) + I(time > 225) + mint_lag_2 + maxt_lag_2 + rain_lag_2,
    coords = as.formula(paste("~", time, "+ t_aux")), data = data,
    kappa = 2.5, start.cov.pars = ..1, method = "nlminb")
                                    StdErr z.value p.value
                       Estimate
(Intercept)
                      1.5546882 0.5374136 2.8929 0.0038169 **
time
                      0.0266066 0.0053688 4.9558 7.205e-07 ***
I(pmax(time - 50, 0)) -0.0258646 0.0059857 -4.3211 1.553e-05 ***
                      0.6931965 0.1792059 3.8682 0.0001097 ***
I(time > 225)TRUE
                     0.1449852 0.0418763 3.4622 0.0005357 ***
mint_lag_2
                     -0.0140655 0.0078728 -1.7866 0.0740030 .
maxt_lag_2
                     0.0185512 0.0101402 1.8295 0.0673303 .
rain_lag_2
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
Log-likelihood: 98.64848
Covariance parameters Matern function (kappa=2.5)
            Estimate StdErr
log(sigma^2) -1.61326 0.1580
log(phi)
            -0.49494 0.1617
log(tau^2)
           -2.72287 0.5096
Legend:
```

```
sigma^2 = variance of the Gaussian process
phi = scale of the spatial correlation
tau^2 = variance of the nugget effect
```

The natural logarithm scale values of  $\sigma^2$ ,  $\phi^2$ , and  $\tau^2$ , and their confidence intervals:

```
parameters <- data.frame(estimates$cov.pars)
parameters$interval <- qnorm(p = 0.975, lower.tail = TRUE) * parameters$StdErr
parameters[, c('ln_lower_ci', 'ln_upper_ci')] <- parameters$Estimate +
   matrix(data = parameters$interval) %*% matrix(data = c(-1, 1), nrow = 1, ncol = 2)</pre>
```

Consequently, their normal scale values are

```
parameters[, c('lower_ci', 'upper_ci')] <- as.matrix(exp(parameters[, c('ln_lower_ci', 'ln_upper_ci')]))</pre>
```

Hence

```
Estimate StdErr ln_lower_ci ln_upper_ci lower_ci upper_ci log(sigma^2) -1.6132574 0.1580131 -1.9229573 -1.3035574 0.14617404 0.2715640 log(phi) -0.4949422 0.1616900 -0.8118489 -0.1780356 0.44403635 0.8369126 log(tau^2) -2.7228684 0.5095813 -3.7216294 -1.7241074 0.02419451 0.1783322
```

#### Exercise 2: Predictions

The foci herein are the ln(cases) point predictions, and their 95% prediction intervals, w.r.t. the months of the Kericho data set. Using the time.predict() function of  $auxiliary\_function.R$ :

```
predictor <- time.predict(
   fitted.model = fit2.5,
   predictors = excerpt[, c('time', 'mint_lag_2', 'maxt_lag_2', 'rain_lag_2')],
   time.pred = excerpt$time,
   scale.pred = 'exponential')</pre>
```

```
log(Cases) ~ time + I(pmax(time - 50, 0)) + I(time > 225) + mint_lag_2 +
    maxt_lag_2 + rain_lag_2
```

creates the time.predict() object of predictions, including the confidence intervals. The resulting graph . . .

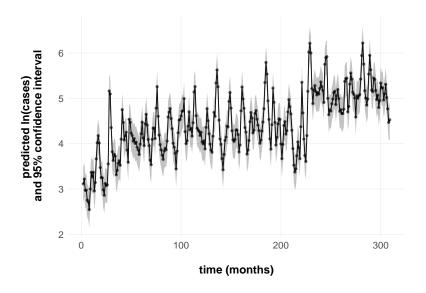


Figure 1: Predictions: ln(cases) and confidence interval